

g-2 Revisited  
*The Dark Z Strikes Back*

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BNL Lunch Discussion  
May 21, 2021

Based on H. Davoudiasl, H.-S. Lee, and W. J. Marciano. 2012-2015

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HEP-PH April 21, 2021

**Recent Fits  $g-2$ ,  $Q_W(Cs)$ ,  $Q_W(P)$  for  $Z_d$  Model**

*Magnet Leaves BNL (Summer 2013)*



*Fermilab + Storage Ring at Night*



## Status of Muon & Electron SM $g-2$ Values

$a^{\text{exp}}(\mu) = 116\,592\,061(41) \times 10^{-11}$  Recent BNL + Fermilab

$\Delta a(\mu) = a^{\text{exp}}(\mu) - a^{\text{SM}}(\mu) = 251(59) \times 10^{-11}$  4.2 sigma deviation

$\Delta a(e) = a^{\text{exp}}(e) - a^{\text{SM}}(e) = 48(30) \times 10^{-14}$  1.6 sigma deviation using  $\alpha(Rb)$

Expect for heavy “new physics”  $\Delta a(\mu)/\Delta a(e) = m_\mu^2/m_e^2 \approx 4 \times 10^4$   
off by a factor of 8

New Physics Scale  $M$ :  $m_e < M < m_\mu$   $\Delta a(\mu) \ \& \ \Delta a(e) = \frac{\alpha}{2\pi} \varepsilon^2 F\left(\frac{m_l^2}{m_d^2}\right)$

*new physics mass & coupling*

Dark Photon mass  $\sim$  30-100 MeV

Kinetic Mixing  $\varepsilon \approx$   $2 \times 10^{-3}$

## Dark Symmetry & Our World

**\*1. Kinetic  $U(1)_Y \times U(1)_d$  Mixing (B. Holdom):  $B_{\mu\nu} D^{\mu\nu}$**

**\*2.  $Z$ - $\gamma_d$  mass mixing (DLM)**

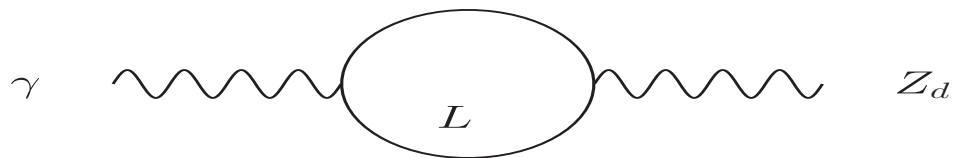
**3.  $U(1)_d = B-L, L_\mu-L_\nu, L_e-L_\mu, L_e-L_\tau \dots$  Dark Symmetry  
(some particles have dark charge & ordinRT)  
(P. Fayet) Very Small Couplings  $U(1)_d$**

Example

One Loop gamma- $\gamma_d$  Kinetic Mixing  
(Through Heavy Charged Leptons)

That also carry  $U(1)_d$  charge

Expect  $\epsilon \sim eg_d Q Q_d / 8\pi^2 \leq O(10^{-3})$

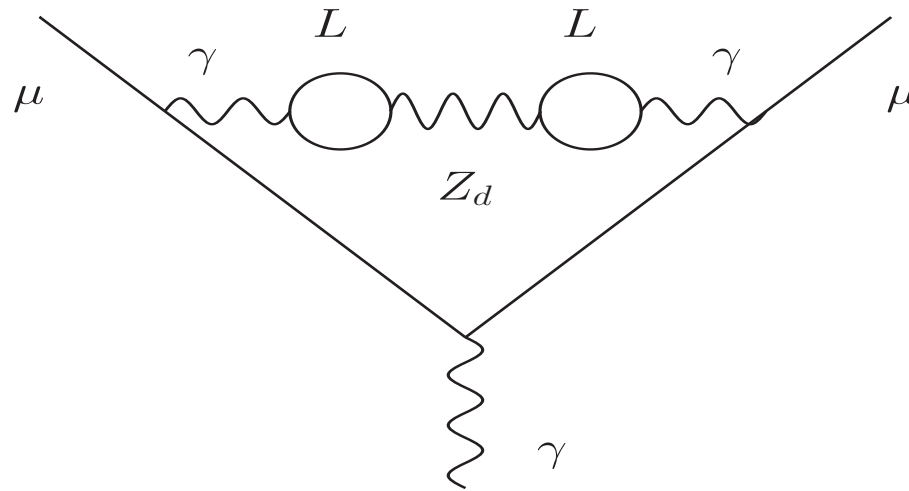


## Muon Anomalous Magnetic Moment

$$a_{\mu}^{Z_d} = \alpha / 2\pi \epsilon^2 F(m_{Z_d}/m_{\mu}), F(0) = 1$$

solves  $(g_{\mu} - 2)/2$  discrepancy  $\approx 288(80) \times 10^{-11}$

for  $\epsilon^2 \approx 10^{-6} - 10^{-4}$  &  $m_{Z_d} \approx 10 - 300 \text{ MeV}$  (see figure)

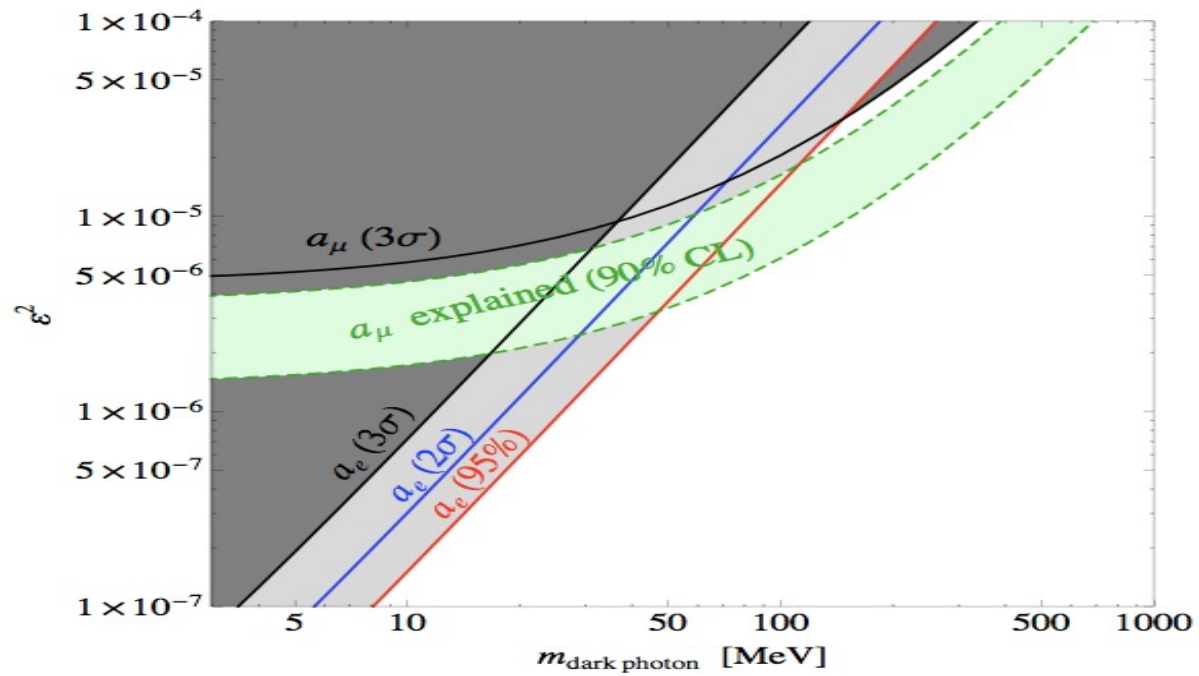


## Lepton Magnetic Moment Constraints on the Dark Photon

Green Band Corresponds to  $a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 288(63)(49) \times 10^{-11}$  90% CL

$g_e - 2$  Constraint DAVOUDI, LEE, MARCIANO

$a_e(\text{exp}) - a_e(\text{theory}) = 0.48 (0.30) \times 10^{-12}$

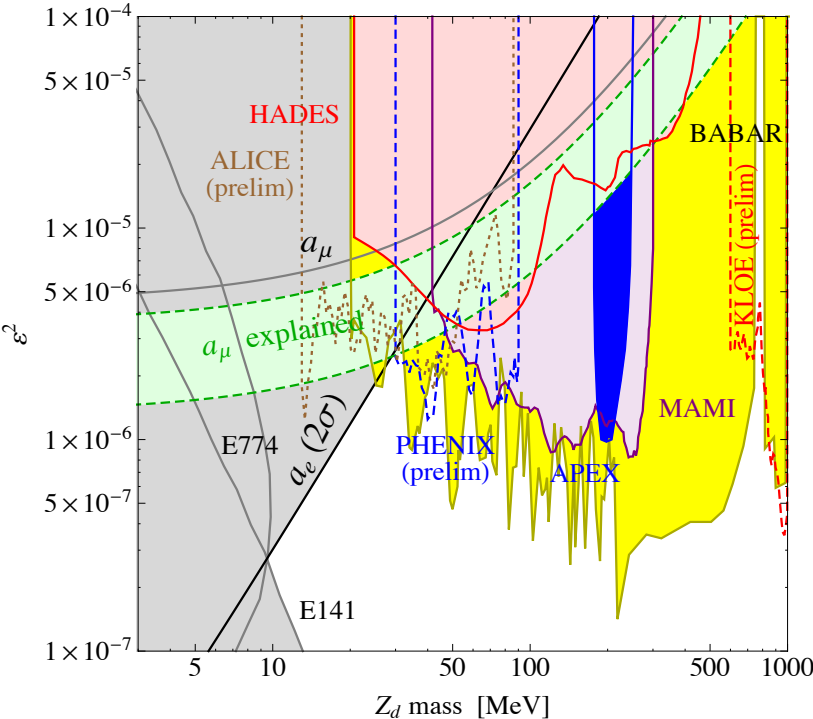


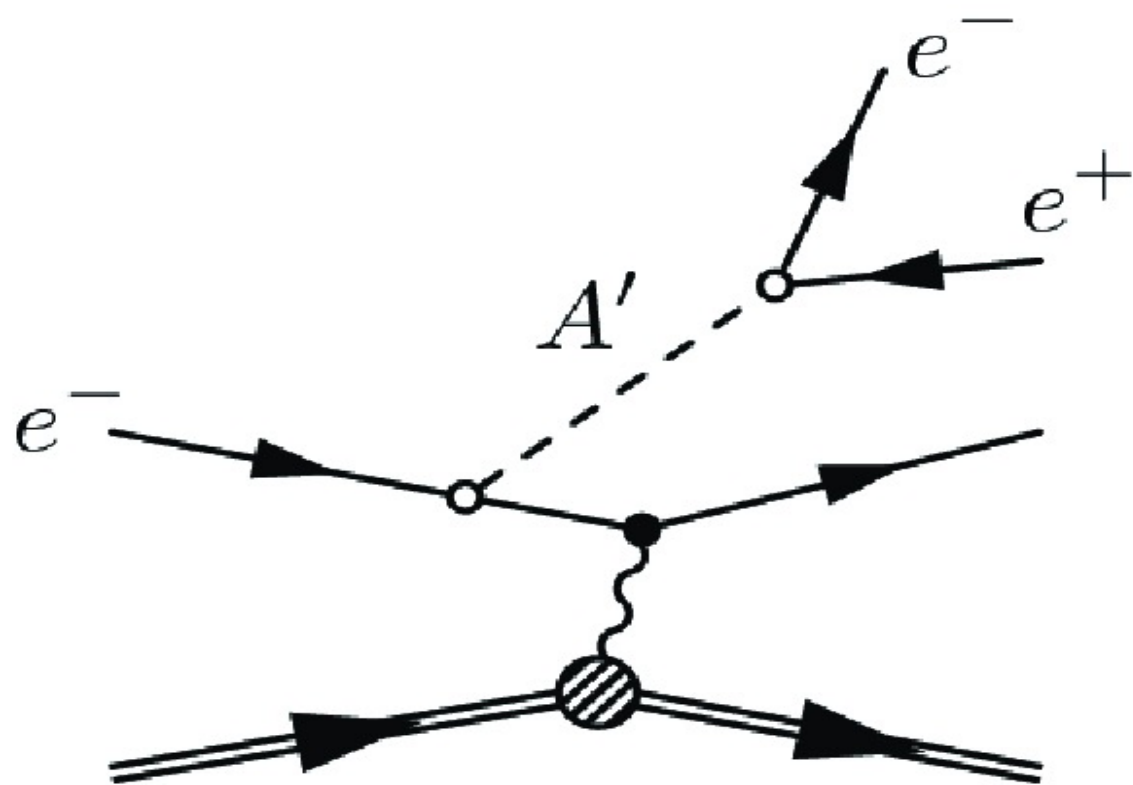


Current Dark Photon Constraints

Assuming  $BR(Z_d \rightarrow e+e-) \sim 1$ . (ruled out)

Require  $Z_d$  decays to light dark matter Most bounds go away





## Near Term Sensitivity Improvements

MAMI 2013  $\epsilon^2 \geq 10^{-6}$  for  $m_{Z_d} > 40\text{MeV}$  explored

**NA48 DATA  $\epsilon^2 \geq 10^{-6}$  for  $m_{Z_d} > 10\text{-}20\text{MeV}$  explored**

Using  $\pi^0 \rightarrow \gamma Z_d$   $Z_d \rightarrow e^+e^-$

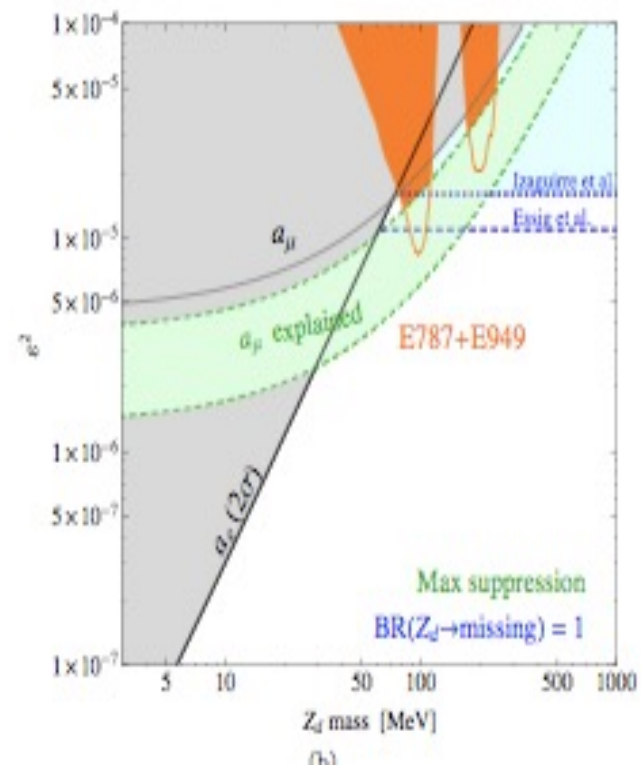
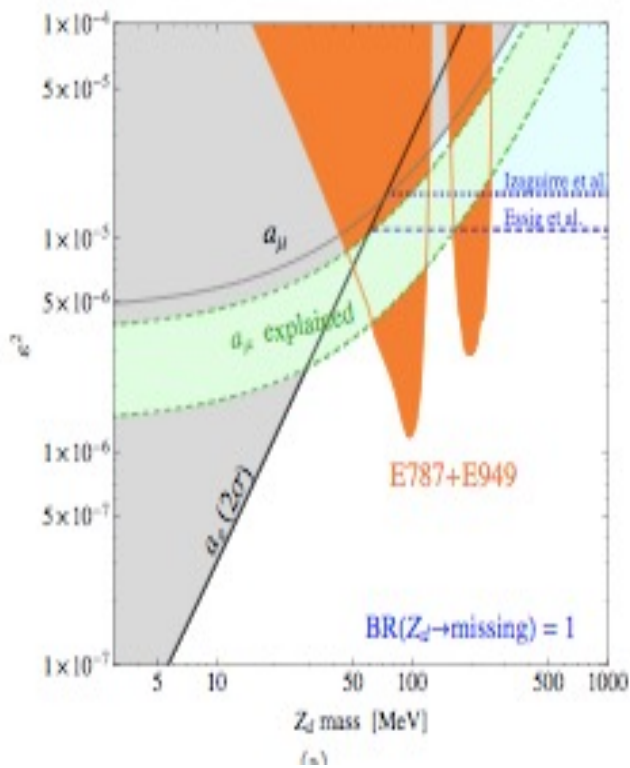
The  $g_\mu-2$  scenario may soon be ruled out for  $Z_d \rightarrow e^+e^-$

Very light dark matter allows  $Z_d \rightarrow$  dark matter (invisible)

New scenario eliminates many constraints but allows

**$K \rightarrow \pi Z_d$   $Z_d \rightarrow K$  + “missing energy” constraints**

$K \rightarrow \pi^+ Z_d$  Constraints for  $BR(\gamma_d(\text{dark matter}) \sim 1$   
 $m_{Z_d} = 100, 200 \text{ MeV}$  ruled out?



## Dark Parity Violation (needs study of $O(\epsilon^2)$ )

H. DAVOUDIASL, H-S LEE, W. MARCIANO

Effect of  $\epsilon$  &  $\epsilon_z$  together: (at low  $Q^2 \ll m_z^2$ )

$$\Delta \sin^2 \theta_W(Q^2) = -0.42 \epsilon \delta m_z m_{z_d} / (Q^2 + m_{z_d}^2)$$

For  $\delta \approx m_{z_d} / m_z$ ,  $\Delta \sin^2 \theta_W(Q^2) = \pm 0.42 \epsilon m_{z_d}^2 / (Q^2 + m_{z_d}^2)$

Shift largest at small  $Q^2 \ll m_{z_d}^2$  ( $\approx O(1\%)$ )! Eg APV

(1.5 sigma APV deviation) fit ( $\epsilon \delta = 4 \times 10^{-6}$ )

or  $\epsilon \approx \delta \approx 2 \times 10^{-3}$  for  $(g_\mu - 2)$  & APV ( $m_{z_d} \approx 50 \text{ MeV}$  region)

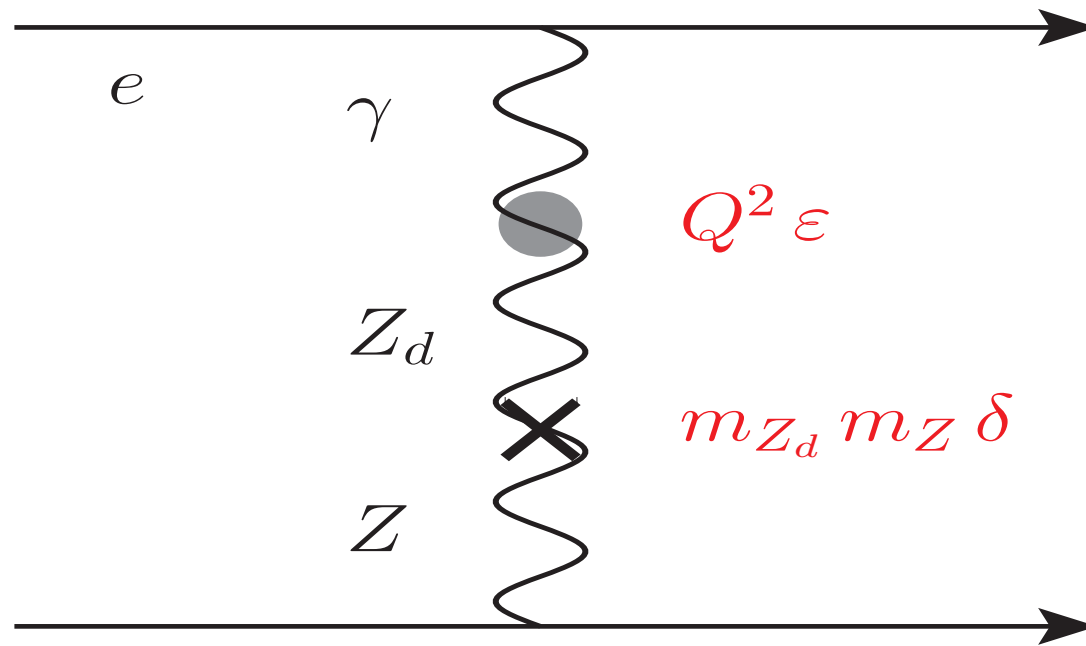
$\sin^2 \theta_W(Q \approx 75 \text{ MeV})$  shift by  $\pm O(0.5-1\%)$ !!

$\delta$  down to  $\approx 10^{-3}$  Potentially Observable

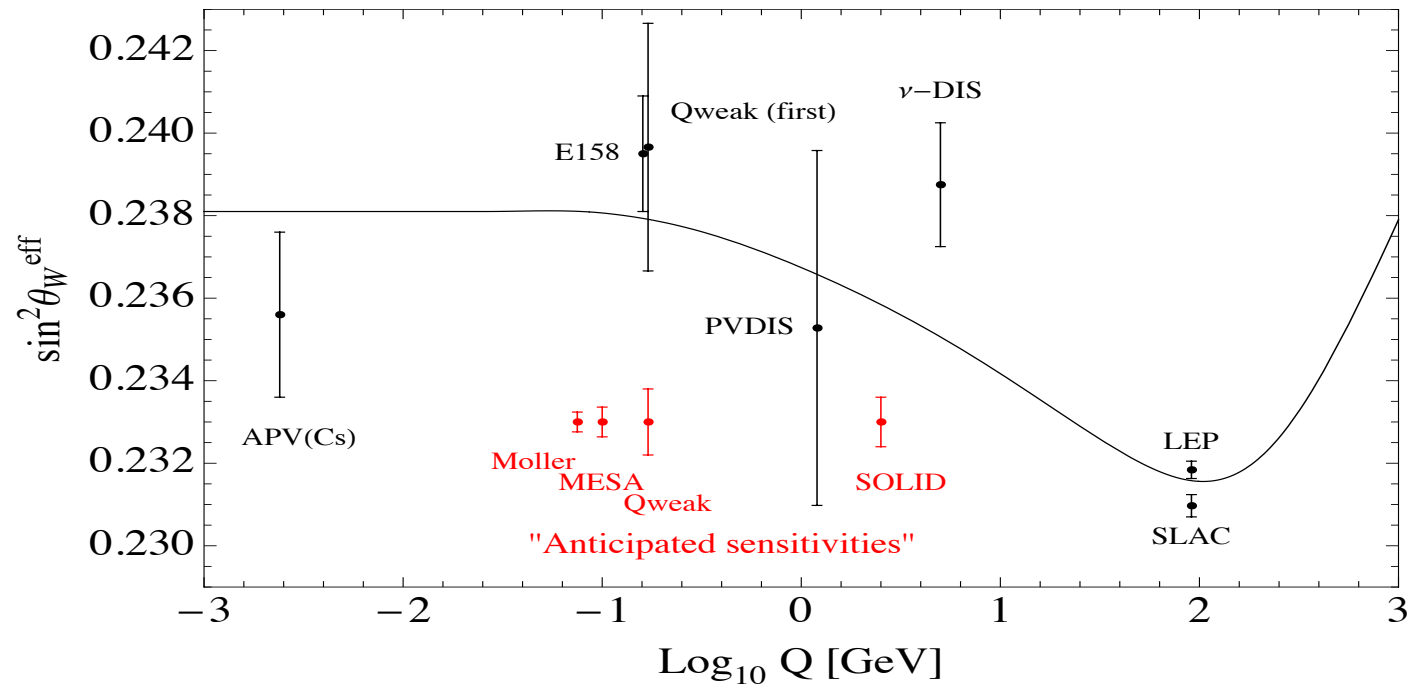
$A_{RL}(ee)$  &  $A_{RL}(eC)$  at low  $Q^2$  Potentially Important

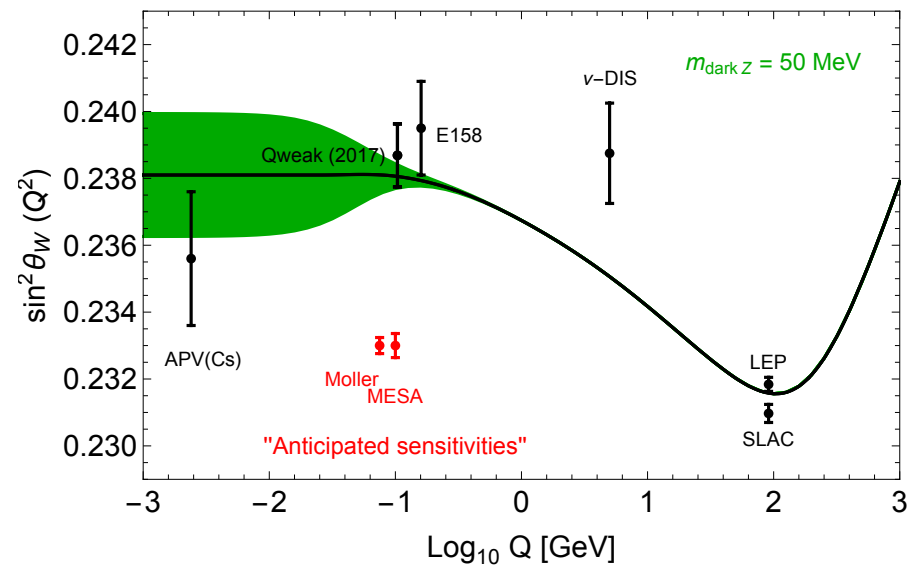
Negligible effect at the Z Pole!

Dark Z Effect on electron scattering  
Photon-Z Mixing through  $Z_d$   
from H-S Lee



## $\sin^2\theta_W(Q^2)$ Measurements & expected Future Sensitivities







Light dark Z solution to  $g-2$  is Viable with mass apprx 50MeV  
Decays to light dark matter

- Possible Exp. Consequences: mixing ( $10^{-3}$ )
- Electron  $g-2$  Exp. Improve muon  $g-2$  theory & exp.
- Parity Violation at Jlab (under investigation)
- K decay to pi + missing energy