

$\nu_\tau/\bar{\nu}_\tau - N(A)$ deep inelastic scattering in the multi-GeV energy region

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Tau Neutrinos from GeV to EeV 2021

Outline

- 1 *Introduction*
- 2 *Charged current $\nu_l/\bar{\nu}_l$ – nucleon scattering*
- 3 *Charged current $\nu_l/\bar{\nu}_l$ – nucleus scattering*
- 4 *Conclusion*

Introduction

- ✦ Among the three generations of the standard model leptons, we know least about the neutral partner (ν_τ) of the third generation weak isospin doublet.
- ✦ DONuT, OPERA, SuperK and IceCube have observed tau (anti)neutrino events but with very limited statistics.
- ✦ SHiP, DUNE, HyperK, FASER ν and DsTau are among the experiments which plan to observe $\nu_\tau/\bar{\nu}_\tau$ interactions on the different nuclear targets.
- ✦ Various groups have theoretically studied the $\nu_\tau/\bar{\nu}_\tau$ –nucleon induced DIS interactions, but there is a large model dependence.
- ✦ We have performed calculations to theoretically study the $\nu_\tau/\bar{\nu}_\tau$ –N induced DIS cross sections by taking into account, various perturbative (PDF evolution at NLO) and nonperturbative (kinematical and dynamical HT) effects.
- ✦ This is the first calculation, where ν_τ -A interaction cross section in the DIS region has been studied by taking into account, the nuclear medium effects like the Fermi motion, binding energy, nucleon correlation effects, mesonic contributions and the (anti)shadowing effects.

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Formalism: $\nu_l/\bar{\nu}_l - N$ scattering

The basic reaction for the (anti)neutrino induced charged current deep inelastic scattering process on a free nucleon target is given by

$$\nu_l(k)/\bar{\nu}_l(k) + N(p) \rightarrow l^-(k')/l^+(k') + X(p'), \quad (l = e, \nu, \tau)$$

The general expression for the double differential scattering cross section (DCX):

$$\frac{d^2\sigma}{dx dy} = \frac{y M_N}{\pi} \frac{E}{E'} \frac{|\mathbf{k}'|}{|\mathbf{k}|} \frac{G_F^2}{2} \left(\frac{M_W^2}{Q^2 + M_W^2} \right)^2 L_{\mu\nu} W_N^{\mu\nu},$$

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Leptonic tensor:

$$L_{\mu\nu} = 8(k_\mu k'_\nu + k_\nu k'_\mu - k \cdot k' g_{\mu\nu} \pm i \epsilon_{\mu\nu\rho\sigma} k^\rho k'^\sigma)$$

Hadronic tensor:

$$\begin{aligned} W_N^{\mu\nu} = & -g^{\mu\nu} W_{1N}(v, Q^2) + W_{2N}(v, Q^2) \frac{p^\mu p^\nu}{M_N^2} - \frac{i}{M_N^2} \epsilon^{\mu\nu\rho\sigma} p_\rho q_\sigma W_{3N}(v, Q^2) + \frac{W_{4N}(v, Q^2)}{M_N^2} q^\mu q^\nu \\ & + \frac{W_{5N}(v, Q^2)}{M_N^2} (p^\mu q^\nu + q^\mu p^\nu) + \frac{i}{M_N^2} (p^\mu q^\nu - q^\mu p^\nu) W_{6N}(v, Q^2). \end{aligned}$$

$W_{iN}(v, Q^2)$ ($i = 1 - 6$) are the weak nucleon structure functions

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$$\begin{aligned} F_{1N}(x) &= W_{1N}(v, Q^2) & F_{2N}(x) &= \frac{Q^2}{2xM_N^2} W_{2N}(v, Q^2) & F_{3N}(x) &= \frac{Q^2}{xM_N^2} W_{3N}(v, Q^2) \\ F_{4N}(x) &= \frac{Q^2}{2M_N^2} W_{4N}(v, Q^2) & F_{5N}(x) &= \frac{Q^2}{2xM_N^2} W_{5N}(v, Q^2) \end{aligned}$$

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The differential scattering cross section is given by

$$\frac{d^2\sigma}{dxdy} = \frac{G_F^2 M_N E_\nu}{\pi(1 + \frac{Q^2}{M_W^2})^2} \left\{ \left[y^2 x + \frac{m_l^2 y}{2E_\nu M_N} \right] F_{1N}(x, Q^2) + \left[\left(1 - \frac{m_l^2}{4E_\nu^2}\right) - \left(1 + \frac{M_N x}{2E_\nu}\right) y \right] F_{2N}(x, Q^2) \right. \\ \left. \pm \left[xy \left(1 - \frac{y}{2}\right) - \frac{m_l^2 y}{4E_\nu M_N} \right] F_{3N}(x, Q^2) + \frac{m_l^2 (m_l^2 + Q^2)}{4E_\nu^2 M_N^2 x} F_{4N}(x, Q^2) - \frac{m_l^2}{E_\nu M_N} F_{5N}(x, Q^2) \right\}.$$

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For $\nu(\bar{\nu})$ -proton scattering

$$F_{2p}^{\nu} (x) = 2x[d(x) + s(x) + \bar{u}(x) + \bar{c}(x)] \\ F_{2p}^{\bar{\nu}} (x) = 2x[u(x) + c(x) + \bar{d}(x) + \bar{s}(x)] \\ xF_{3p}^{\nu} (x) = 2x[d(x) + s(x) - \bar{u}(x) - \bar{c}(x)] \\ xF_{3p}^{\bar{\nu}} (x) = 2x[u(x) + c(x) - \bar{d}(x) - \bar{s}(x)]$$

For $\nu(\bar{\nu})$ -neutron scattering

$$F_{2n}^{\nu} (x) = 2x[u(x) + s(x) + \bar{d}(x) + \bar{c}(x)] \\ F_{2n}^{\bar{\nu}} (x) = 2x[d(x) + c(x) + \bar{u}(x) + \bar{s}(x)] \\ xF_{3n}^{\nu} (x) = 2x[u(x) + s(x) - \bar{d}(x) - \bar{c}(x)] \\ xF_{3n}^{\bar{\nu}} (x) = 2x[d(x) + c(x) - \bar{u}(x) - \bar{s}(x)].$$

At the leading order

Callan-Gross relation:

$$F_2(x) = 2xF_1(x)$$

Albright-Jarlskog relations:

$$F_4(x) = 0 \quad F_2(x) = 2xF_5(x)$$

In this work MMHT PDFs parameterization (Harland-Lang *et al.*, Eur. Phys. J. C **75**, no. 5, 204 (2015)) has been used.

Charm quark is considered to be a massive object and in four flavor scheme we consider:

$$F_{iN}(x, Q^2) = F_{iN}^{n_f=4}(x, Q^2) = \underbrace{F_{iN}^{n_f=3}(x, Q^2)}_{\text{for massless}(u, d, s) \text{ quarks}} + \underbrace{F_{iN}^{n_f=1}(x, Q^2)}_{\text{for massive charm quark}}$$

Details in ref. Ansari *et al.*, Phys. Rev. D **102**, 113007 (2020)

Perturbation and nonperturbative effects at nucleon level

In the kinematic region of low and moderate Q^2 , both the higher order perturbative and the nonperturbative ($\propto \frac{1}{Q^2}$) QCD effects come into play.

- Perturbative effects like the QCD corrections at the next-to-next-to-leading order (NNLO) in the strong coupling constant α_s .
- In the present work we have evaluated the structure functions at NLO, following the works of Kretzer and Reno (Phys. Rev. D **66**, 113007 (2002); *ibid* **69**, 034002 (2004)) and Jeong and Reno (Phys. Rev. D **82**, 033010 (2010).)
- The nonperturbative effect like:
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 - HT originates due to the interactions of struck quarks with the other quarks via gluon exchange and is incorporated following the works of Dasgupta *et al.*, Phys. Lett. B **382**, 273 (1996).
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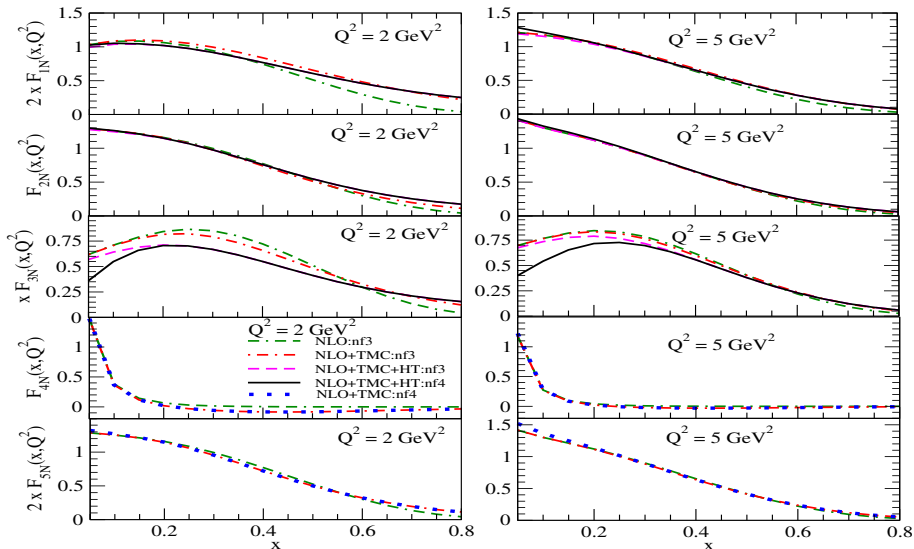
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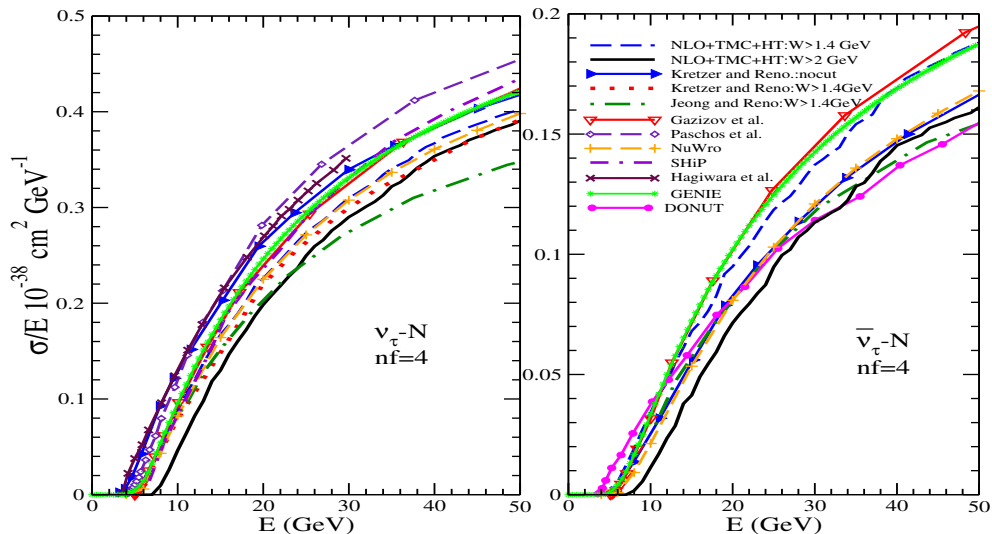
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Free nucleon structure functions: $F_{iN}^{WI}(x, Q^2)$ vs x ($i = 1 - 5$)

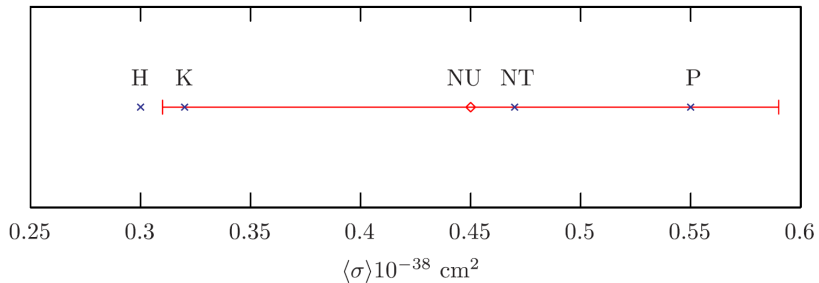


$\nu_\tau(\bar{\nu}_\tau) - N$ CC DIS cross section



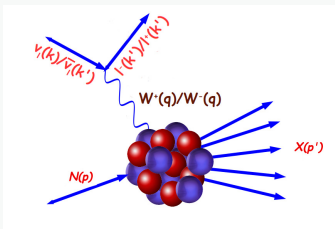
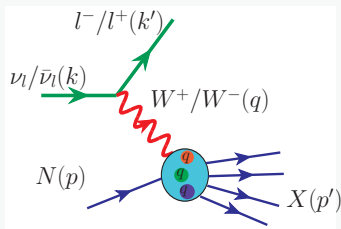
Ansari *et al.*, Phys. Rev. D **102**, 113007 (2020)

Flux-averaged total CC $\nu_\tau + \bar{\nu}_\tau$ cross section ($6 < E_{\text{vis}} < 20 \text{ GeV}$)



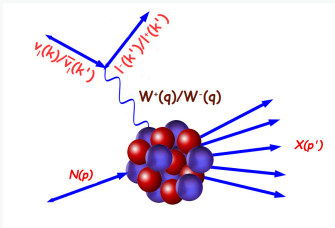
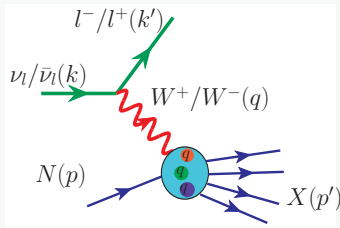
Conrad *et al.*, Phys. Rev D **82**, 093012 (2010)

$\nu_l/\bar{\nu}_l - A$ scattering



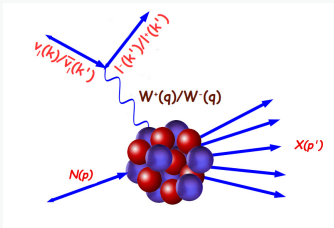
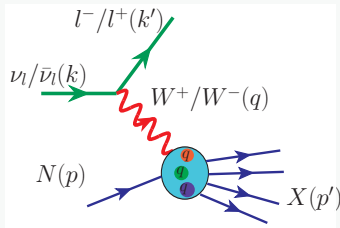
- Fermi motion, binding energy and nucleon correlations through spectral function and is calculated using Lehmann's representation for the relativistic nucleon propagator.
- Nuclear many body theory is used to calculate it for an interacting Fermi sea in nuclear matter. A local density approximation is then applied to translate these results to finite nuclei.
- There are virtual mesons associated with the nucleon bound inside the nucleus. These meson clouds get strengthened by the strong attractive nature of nucleon-nucleon interactions.
- This leads to an increase in the interaction probability of virtual mediating quanta with the meson cloud. The effect of meson cloud is more pronounced in heavier nuclear targets and dominate in the intermediate region of x ($0.2 < x < 0.6$).
- The shadowing suppression at small x occurs due to coherent multiple scattering of quark-anti quark pair coming from the virtual boson with destructive interference of the amplitudes and is incorporated following the works of Kulagin and Petti. Phys. Rev. D **76**, 094033(2007).

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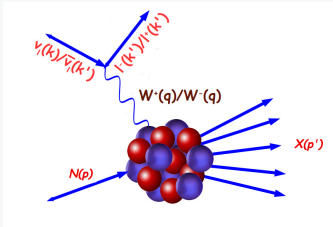
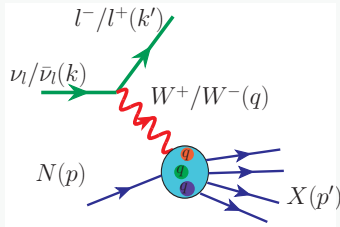
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In the limit of $Q^2 \rightarrow \infty$, $v \rightarrow \infty$, $x \rightarrow$ finite and $W_{iN}(v, Q^2)$ ($i = 1 - 6$) are written in terms of the dimensionless nuclear structure functions as:

$$\begin{aligned} F_{1A}(x) &= W_{1A}(v, Q^2) & F_{2A}(x) &= \frac{Q^2}{2xM_A^2} W_{2A}(v, Q^2) & F_{3A}(x) &= \frac{Q^2}{xM_A^2} W_{3A}(v, Q^2) \\ F_{4A}(x) &= \frac{Q^2}{2M_A^2} W_{4A}(v, Q^2) & F_{5A}(x) &= \frac{Q^2}{2xM_A^2} W_{5A}(v, Q^2) \end{aligned}$$

Formalism: $\nu_l/\bar{\nu}_l - A$ scattering

- To calculate the scattering cross section for a neutrino interacting with a target nucleon in the nuclear medium, we write

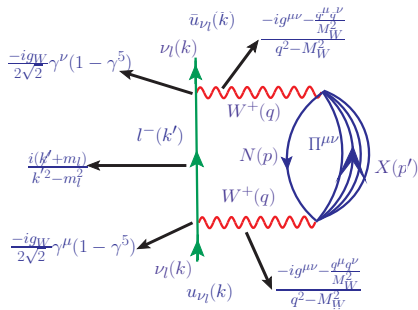
$$d\sigma_A = -2 \frac{m_\nu}{|\mathbf{k}|} \text{Im}\Sigma(k) d^3r.$$

- The neutrino self energy $\Sigma(k)$:

$$\Sigma(k) = \frac{iG_F}{\sqrt{2}} \int \frac{d^4q}{(2\pi)^4} \frac{4L_{\mu\nu}^{Wl}}{m_l} \frac{1}{(k'^2 - m_l^2 + i\epsilon)} \left(\frac{M_W}{q^2 - M_W^2} \right)^2 \Pi^{\mu\nu}(q),$$

- $\Pi^{\mu\nu}(q)$ written in terms of the nucleon propagator (G_l) and meson propagator (D_j):

$$\begin{aligned} \Pi^{\mu\nu}(q) &= \left(\frac{G_F M_W^2}{\sqrt{2}} \right) \times \int \frac{d^4p}{(2\pi)^4} G(p) \sum_X \sum_{s_p, s_l} \prod_{i=1}^N \int \frac{d^4p'_i}{(2\pi)^4} \prod_i G_l(p'_i) \prod_j D_j(p'_j) \\ &\quad \langle X | J^\mu | N \rangle \langle X | J^\nu | N \rangle^* (2\pi)^4 \delta^4 \left(k + p - k' - \sum_{i=1}^N p'_i \right), \end{aligned}$$



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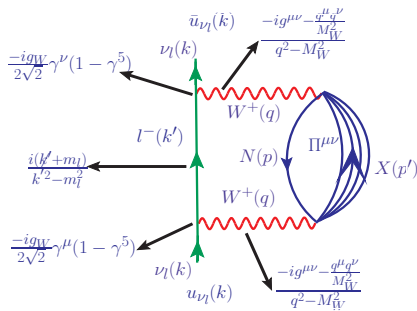
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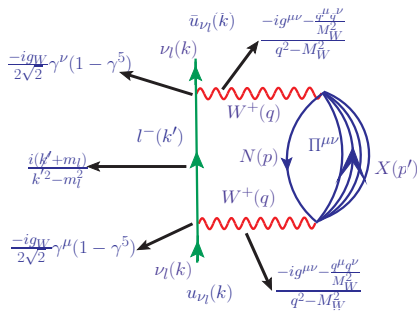
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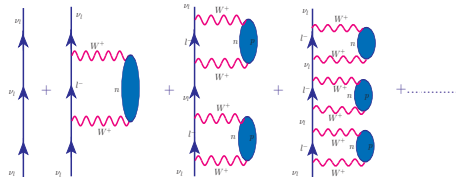
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In the nuclear matter the dressed nucleon propagator is written as:

$$G(p) = \frac{M_N}{E(\mathbf{p})} \sum_r u_r(\mathbf{p}) \bar{u}_r(\mathbf{p}) \left[\int_{-\infty}^{\mu} d\omega \frac{S_h(\omega, \mathbf{p})}{p^0 - \omega - i\eta} + \int_{\mu}^{\infty} d\omega \frac{S_p(\omega, \mathbf{p})}{p^0 - \omega + i\eta} \right],$$



The spectral function $F_{iA,N}(x_A, Q^2)$ ($i = 1 - 5$) are obtained as:

$$F_{iA,N}(x_A, Q^2) = 4 \int d^3r \int \frac{d^3p}{(2\pi)^3} \frac{M_N}{E_N(\mathbf{p})} \int_{-\infty}^{\mu} dp^0 S_h(p^0, \mathbf{p}, \rho(r)) \times f_{iN}(x, Q^2),$$

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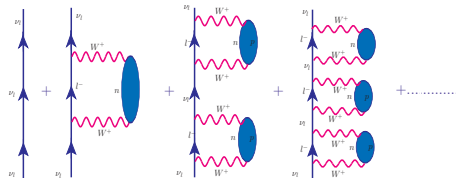
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Zaidi *et al.* Phys. Rev. D **101** (2020), 033001, Phys. Rev. D **99** (2019), 093011

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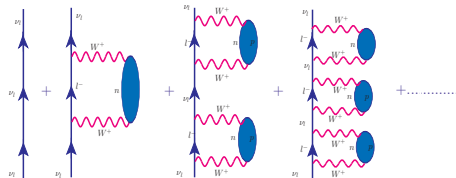
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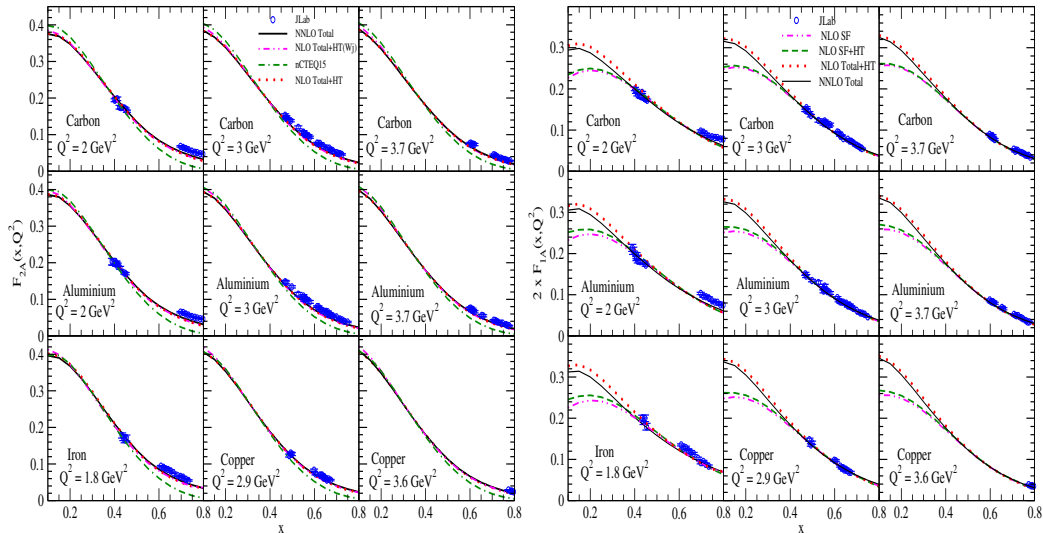
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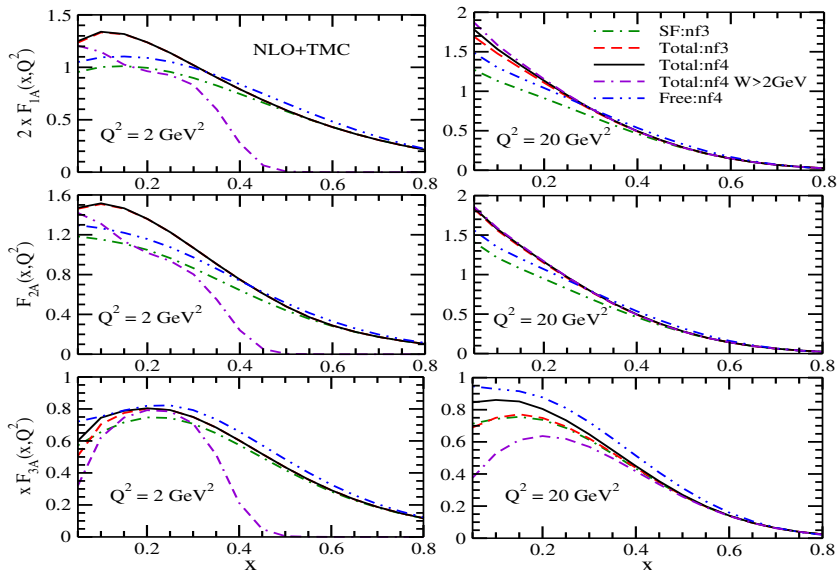
Zaidi *et al.* Phys. Rev. D **101** (2020), 033001, Phys. Rev. D **99** (2019), 093011

EM Nuclear Structure Functions

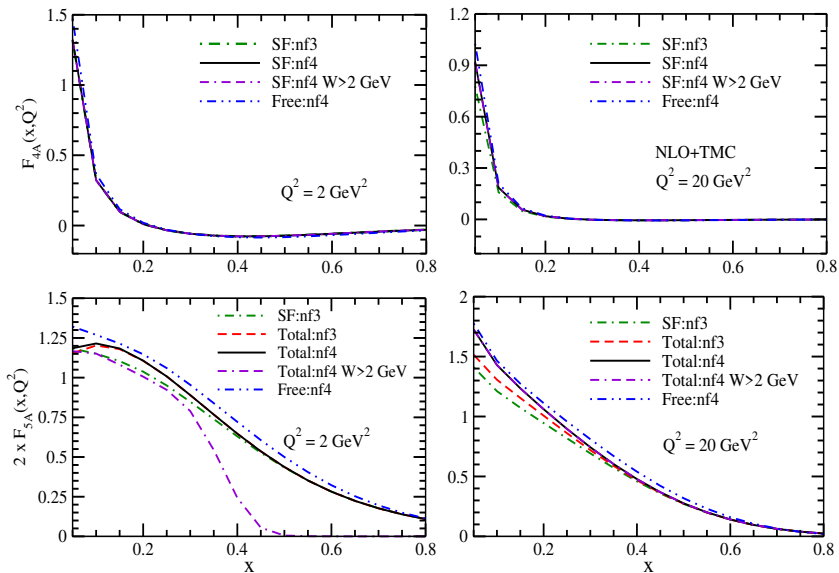


Zaidi *et al.*, Phys. Rev. D **99**, 093011 (2019).

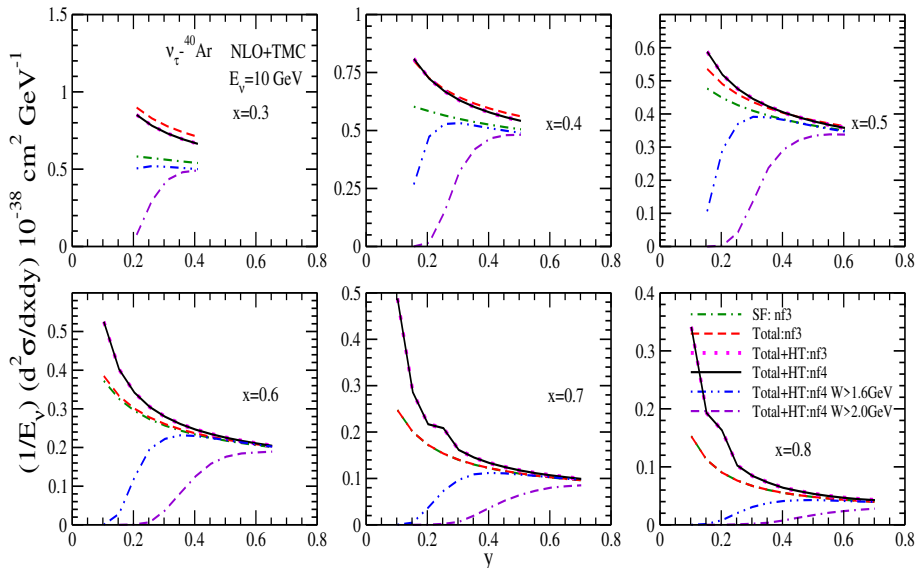
Nuclear structure functions: $2xF_{1A}(x, Q^2)$, $F_{2A}(x, Q^2)$ and $xF_{3A}(x, Q^2)$ for ^{40}Ar



Nuclear structure functions: $F_{4A}(x, Q^2)$ and $2xF_{5A}(x, Q^2)$ for ^{40}Ar



$\frac{1}{E_\nu} \frac{d^2\sigma}{dx dy}$ vs y at $E_\nu = 10\text{GeV}$



Conclusion

- Perturbative and nonperturbative effects are quite important in the evaluation of nucleon structure functions as well as the differential cross section. These effects are important in the different regions of x and Q^2 .

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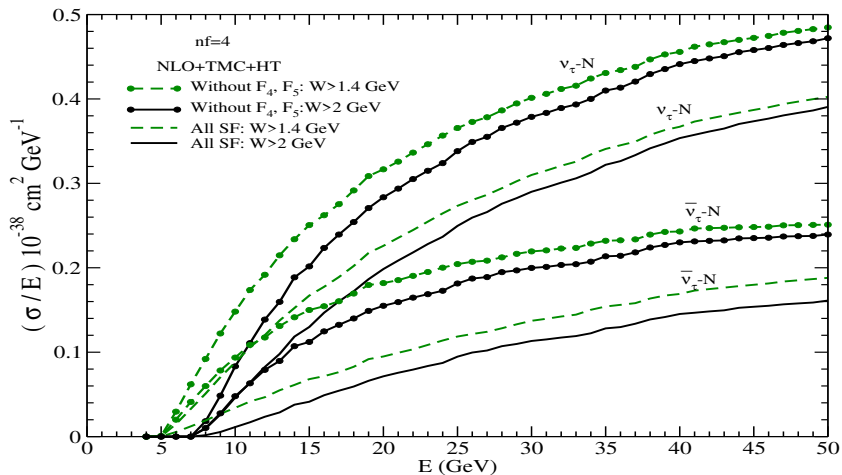
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Thank You!

Backup

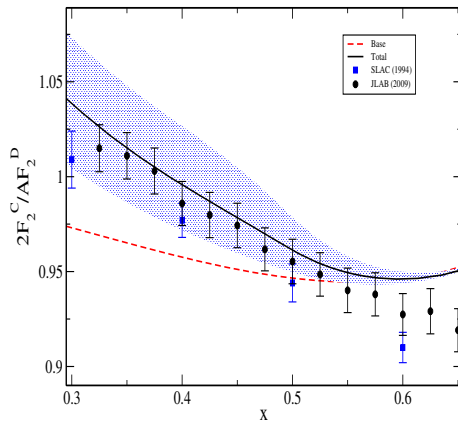
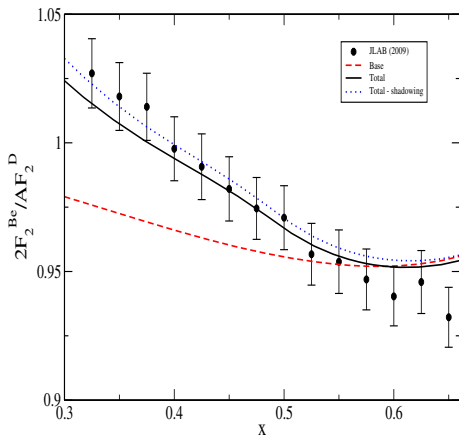
$\frac{\sigma}{E}$ vs E for $\nu_\tau/\bar{\nu}_\tau - N$ DIS



Total scattering cross section with center of mass energy cut of 1.4 GeV and 2 GeV for $\nu_\tau - N$ and $\bar{\nu}_\tau - N$ DIS.

Ansari *et al.*, Phys. Rev. D **102**, 113007 (2020)

EM nuclear structure function $\frac{2F_2^A}{AF_2^D}$ ($A = Be, C$) vs x



M. Sajjad Athar *et al.*, Nucl. Phys A **857**, 29(2011)

Nuclear structure functions

The spectral function $F_{iA,N}(x_A, Q^2)$ are obtained as:

$$F_{iA,N}(x_A, Q^2) = 4 \int d^3r \int \frac{d^3p}{(2\pi)^3} \frac{M_N}{E_N(\mathbf{p})} \int_{-\infty}^{\mu} dp^0 S_h(p^0, \mathbf{p}, \rho(r)) \times f_{iN}(x, Q^2),$$

where $i = 1 - 5$ and

$$f_{1N}(x, Q^2) = AM_N \left[\frac{F_{1N}(x_N, Q^2)}{M_N} + \left(\frac{p^x}{M_N} \right)^2 \frac{F_{2N}(x_N, Q^2)}{v_N} \right],$$

$$f_{2N}(x, Q^2) = \left[\frac{Q^2}{(q^z)^2} \left(\frac{|\mathbf{p}|^2 - (p^z)^2}{2M_N^2} \right) + \frac{(p^0 - p^z \gamma)^2}{M_N^2} \left(\frac{p^z Q^2}{(p^0 - p^z \gamma) q^0 q^z} + 1 \right)^2 \right] \times \left(\frac{M_N}{p^0 - p^z \gamma} \right) \times F_{2N}(x_N, Q^2),$$

$$f_{3N}(x, Q^2) = A \frac{q^0}{q^z} \times \left(\frac{p^0 q^z - p^z q^0}{p \cdot q} \right) F_{3N}(x_N, Q^2), \quad f_{4N}(x, Q^2) = A F_{4N}(x_N, Q^2),$$

$$f_{5N}(x, Q^2) = A F_{5N}(x_N, Q^2) \times \frac{2x_N}{M_N v_N} \times (a_1 + a_2 + a_3),$$

$$a_1 = \frac{|\mathbf{q}|q_0}{q^2} \left(\frac{|\mathbf{q}| + q_0}{|\mathbf{q}| + 2q^0} \right) \times \left\{ -p_x^2 + \frac{|\mathbf{q}|^2}{Q^2} \frac{M_N v_N}{q_0(p_N^0 - \gamma p_N^z)} \left(\frac{Q^2}{|\mathbf{q}|^2} \left[\frac{|\bar{p}_N|^2 - p_N^z{}^2}{2} \right] + (p_N^0 - \gamma p_N^z)^2 \left[1 + \frac{p_N^z Q^2}{q^0 |\mathbf{q}| (p_N^0 - \gamma p_N^z)} \right]^2 \right) \right\},$$

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Nuclear structure functions

The mesonic structure functions $F_{iA,a}(x_a, Q^2)$, ($i = 1, 2, 5; a = \pi, \rho$) are obtained as:

$$F_{iA,a}(x_a, Q^2) = -6\kappa \int d^3r \int \frac{d^4p}{(2\pi)^4} \theta(p^0) \delta \text{Im} D_a(p) 2m_a f_{ia}(x_a),$$

where

$$f_{2a}(x_a) = \left(\frac{m_a}{p^0 - p^z \gamma} \right) \left[\frac{Q^2}{(q^z)^2} \left(\frac{|\mathbf{p}|^2 - (p^z)^2}{2m_a^2} \right) + \frac{(p^0 - p^z \gamma)^2}{m_a^2} \times \left(\frac{p^z Q^2}{(p^0 - p^z \gamma) q^0 q^z} + 1 \right)^2 \right] F_{2a}(x_a)$$

$$f_{1a}(x_a) = AM_N \left[\frac{F_{1a}(x_a)}{m_a} + \frac{|\mathbf{p}|^2 - (p^z)^2}{2(p^0 q^0 - p^z q^z)} \frac{F_{2a}(x_a)}{m_a} \right], \quad f_{5a}(x_a) = \frac{2x_a}{m_a v} (a_1 + a_2 + a_3) F_{5a}(x_a),$$

$$a_1 = \frac{|\mathbf{q}|q_0}{q^2} \left(\frac{|\mathbf{q}| + q_0}{|\mathbf{q}| + 2q^0} \right) \times \left\{ -p_x^2 + \frac{|\mathbf{q}|^2}{Q^2} \frac{m_a v}{q_0 (\gamma p_N^z - p_N^0)} \left(\frac{Q^2}{|\mathbf{q}|^2} \left[\frac{|\bar{p}_N|^2 - p_N^2}{2} \right] + (\gamma p_N^z - p_N^0)^2 \left[1 + \frac{p_N^z Q^2}{q^0 |\mathbf{q}| (\gamma p_N^z - p_N^0)} \right]^2 \right) \right\}$$

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$D_a(p)$ is the meson(π or ρ) propagator in the nuclear medium and is written as

$$D_a(p) = [p_0^2 - \mathbf{p}^2 - m_a^2 - \Pi_a(p_0, \mathbf{p})]^{-1}, \quad \text{with} \quad \Pi_a(p_0, \mathbf{p}) = \frac{f^2}{m_\pi^2} \frac{C_\rho F_a^2(p) \mathbf{p}^2 \Pi^*}{1 - \frac{f^2}{m_\pi^2} V'_J \Pi^*},$$

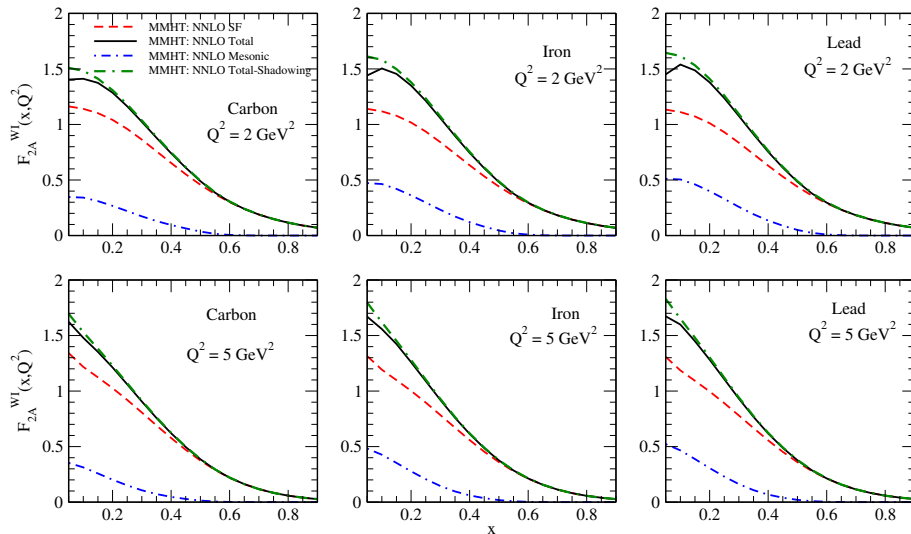
Zaidi *et al.* Phys.Rev. D**101** (2020) no.3, 033001, Phys.Rev. D**99** (2019) no.9, 093011

Nuclear structure functions

$\kappa = 1(2)$ for pion(rho meson), $\mathbf{v} = \frac{q_0(\gamma p_N^z - p_N^0)}{m_a}$, $x_a = -\frac{Q^2}{2p \cdot q}$, m_a is the mass of the meson(π or ρ).

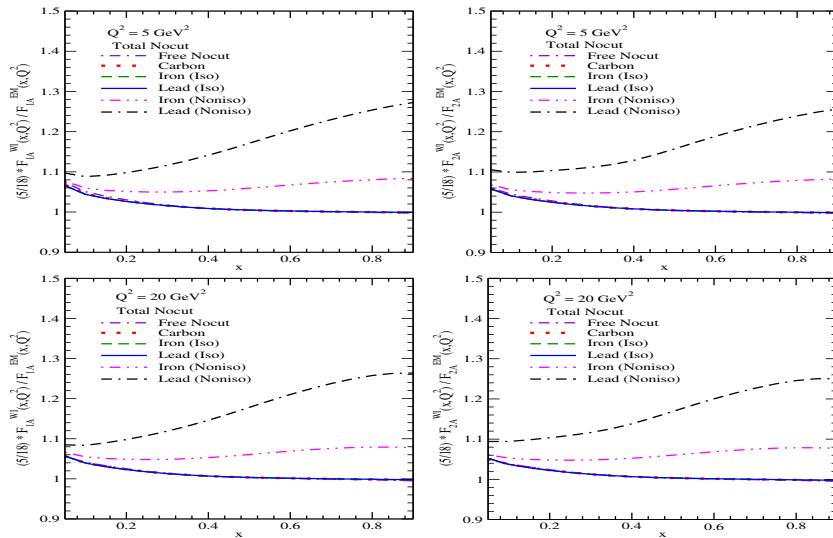
where, $C_\rho = 1(3.94)$ for pion(rho meson). $F_a(p) = \frac{(\Lambda_a^2 - m_a^2)}{(\Lambda_a^2 - p^2)}$ is the πNN or ρNN form factor, $\Lambda_a = 1 \text{ GeV}$ (fixed by Aligarh-Valencia group) and $f = 1.01$. V_j' is the longitudinal(transverse) part of the spin-isospin interaction for pion(rho meson), and Π^* is the irreducible meson self energy that contains the contribution of particle-hole and delta-hole excitations.

Weak Nuclear Structure Functions



Athar and Morfin, Jour. Phys. G 48, 034001 (2021).

NME in Weak & EM interactions



Zaidi *et al.* Phys Rev. D **101**, 033001 (2020)