



Probing the Standard Model with $B \rightarrow K^{(*)} l^+ l^-$ decays at LHCb

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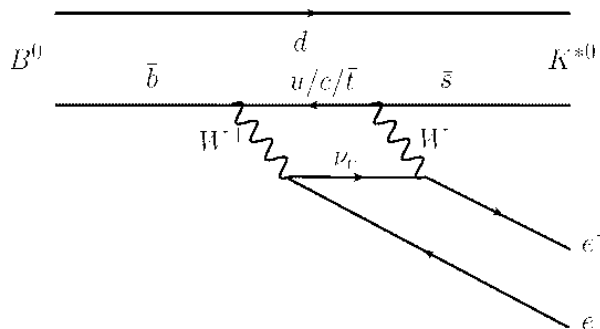
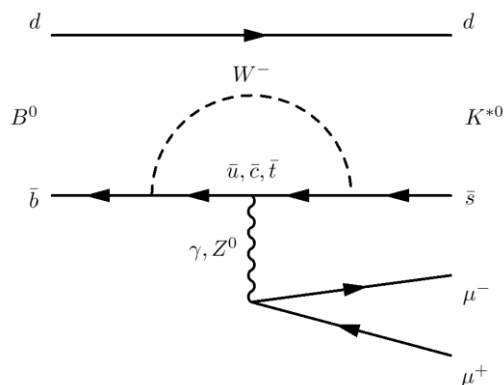
Rutherford Appleton Laboratory

On behalf of the LHCb collaboration

Brookhaven Forum 2015, 7th-9th Oct.



$B \rightarrow K^* l^+ l^-$ and rare decays of heavy mesons



Effective Hamiltonian can be expressed via Operator Product Expansion (OPE) in terms of operators O and calculable Wilson coefficients C .

$$H_{eff} = -\frac{4G_F}{\sqrt{2}} V_{tq}^* V_{tb} \sum_{i=1} C_i^{(l)}(\mu) O_i^{(l)}(\mu) + \sum_i \frac{C_i^{NP}}{\Lambda^2} O_i^{NP}$$

$i = 1, 2$	Tree
$i = 3 - 6, 8$	Gluon Penguin
$i = 7$	Photon Penguin
$i = 9$	EW Penguin (axial)
$i = 10$	EW Penguin (vector)
$i = S$	Scalar Penguin
$i = P$	Pseudoscalar Penguin

New Physics (NP) can enter via new particles in loops

Potentially modifies magnitude and phase of SM C_i

Potentially introduces new couplings C^{NP} .

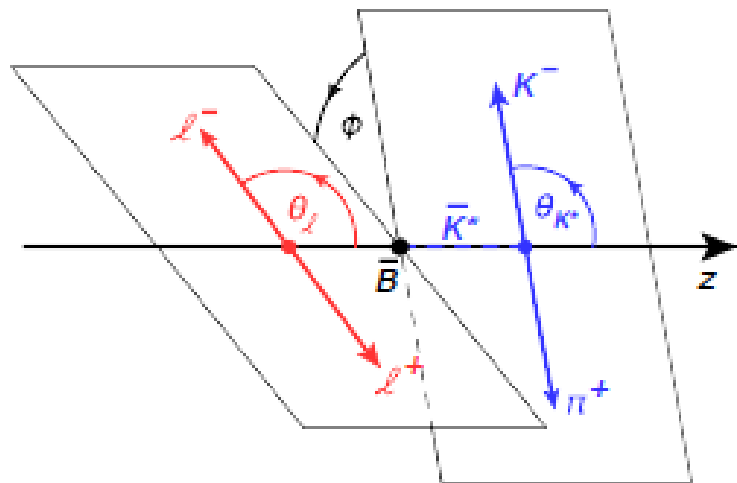
Potentially different couplings to the leptons.

Look for changes in branching fractions, angular distributions, and lepton universality.

Results are based on 3 fb^{-1} ($\sim 1 \text{ fb}^{-1}$ @ 7 GeV and $\sim 2 \text{ fb}^{-1}$ @ 8 GeV)

Full Angular Analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} \bigg|_P = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ \left. + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_l + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + S_5 \sin 2\theta_K \sin \theta_l \cos \phi \right. \\ \left. + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_l + S_7 \sin 2\theta_K \sin \theta_l \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right].$$



θ_K between K^+ & B^0 in K^* rest frame.

θ_l between $l^+(l^-)$ & $B(\bar{B})$ in l^+l^- rest frame.

ϕ between the di-lepton and $K\pi$ plane in B rest frame.

F_L , Longitudinal Polarization.

A_{FB} , Forward-Backward di-lepton asymmetry.

$$P'_{4,5,6,8} = S_{4,5,7,8} / \sqrt{F_L(1 - F_L)} \quad [\text{JHEP 01 (2013) 048}]$$

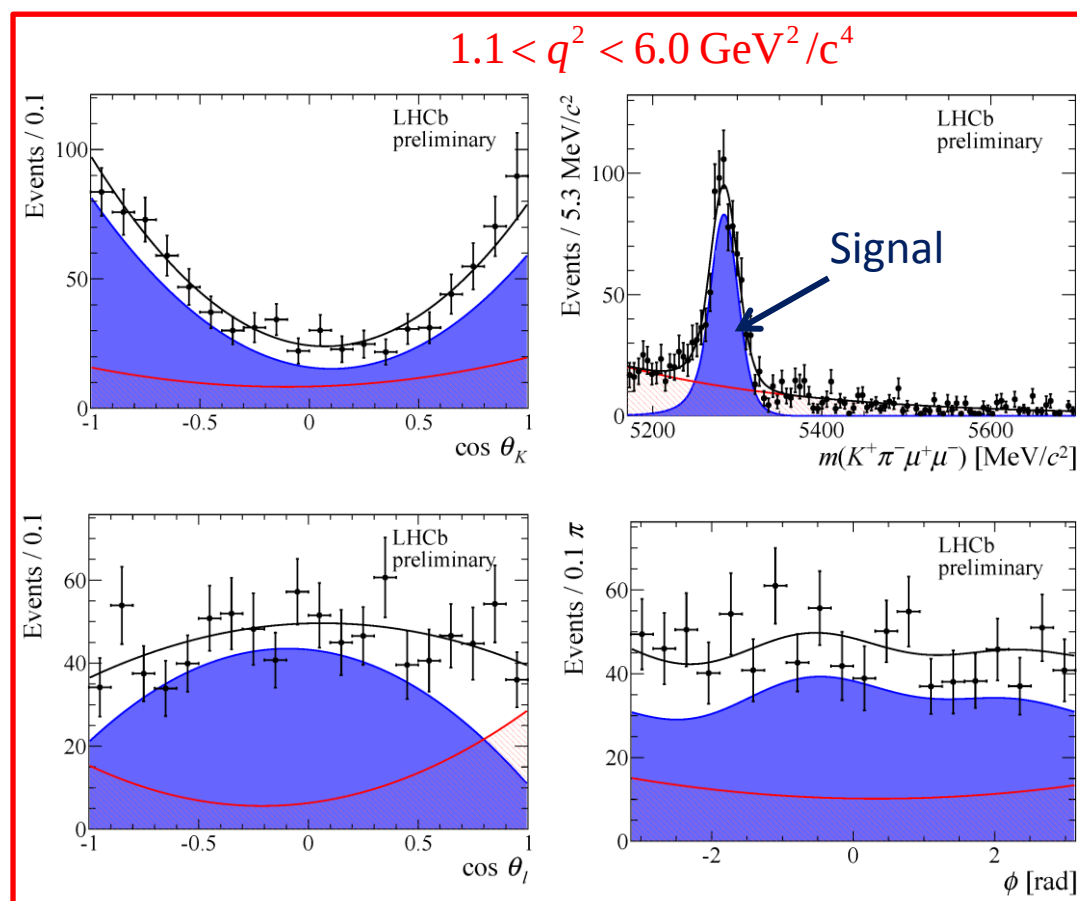
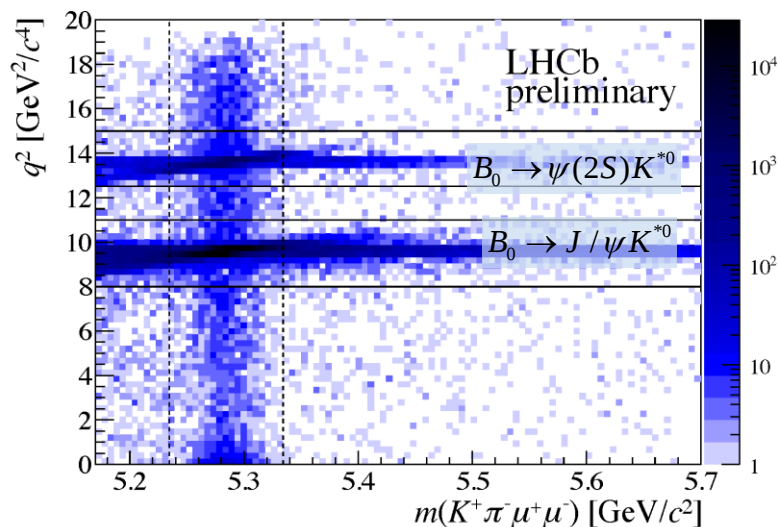
SM theoretical predictions exist for F_L , A_{FB} , P' , $S_{3,4,5}$ as a function of q^2 . Other S_i are expected to be $\sim$ zero in the SM.

Full Angular Analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

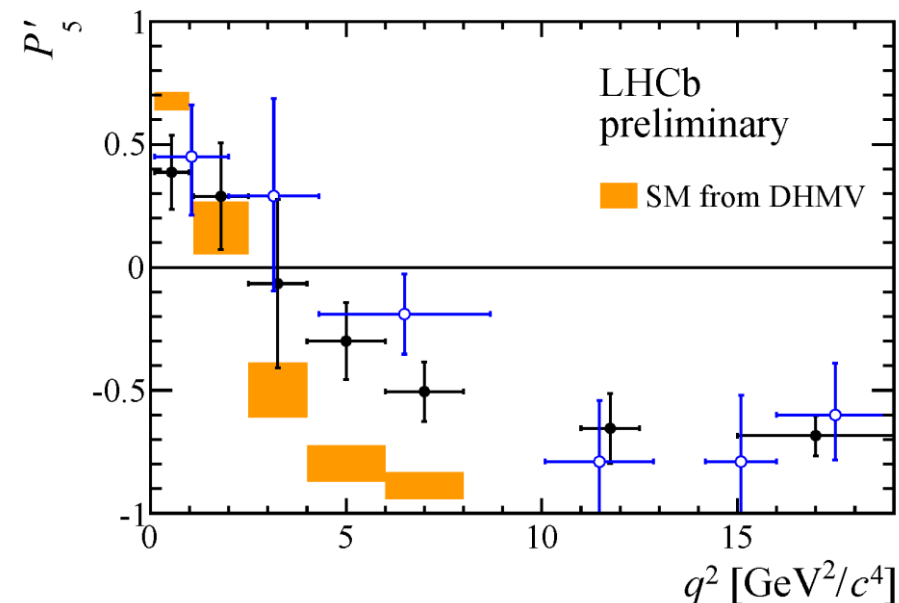
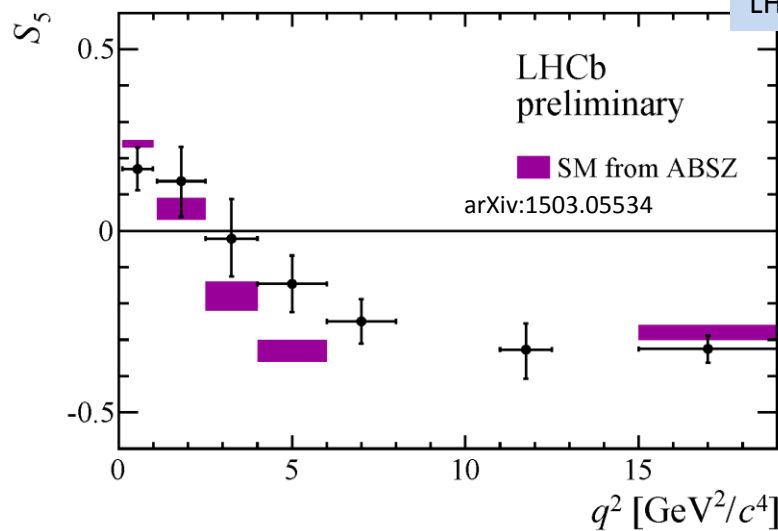
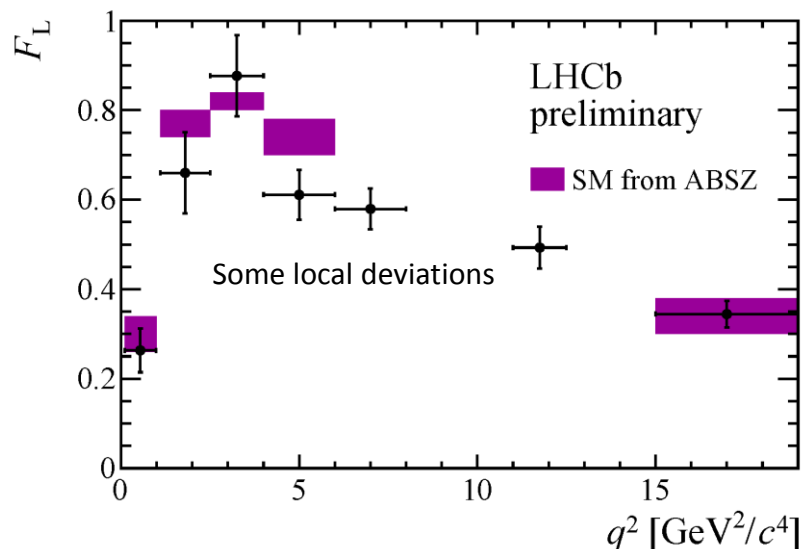
Require $795.9 < m(K^+ \pi^-) < 995.9 \text{ MeV}/c^2$ and $0.1 < q^2 < 19 \text{ GeV}^2/c^4$.

But need to account for S-wave from $K^+ \pi^-$ final state via fits to $m(K^+ \pi^-)$.

Maximum likelihood (ML) fit in q^2 bins to $\cos \theta_K$, $\cos \theta_l$, ϕ , $m(K^+ \pi^- \mu^+ \mu^-)$, $m(K^+ \pi^-)$.



Full Angular Analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$



Black – this result with SM prediction

Orange - SM prediction JHEP 1412 (2014) 129)

Blue - earlier LHCb 1fb⁻¹ PRL 111 (2013) 191801).

New data agrees with 2013 result.

Tension in P'_5 confirmed.

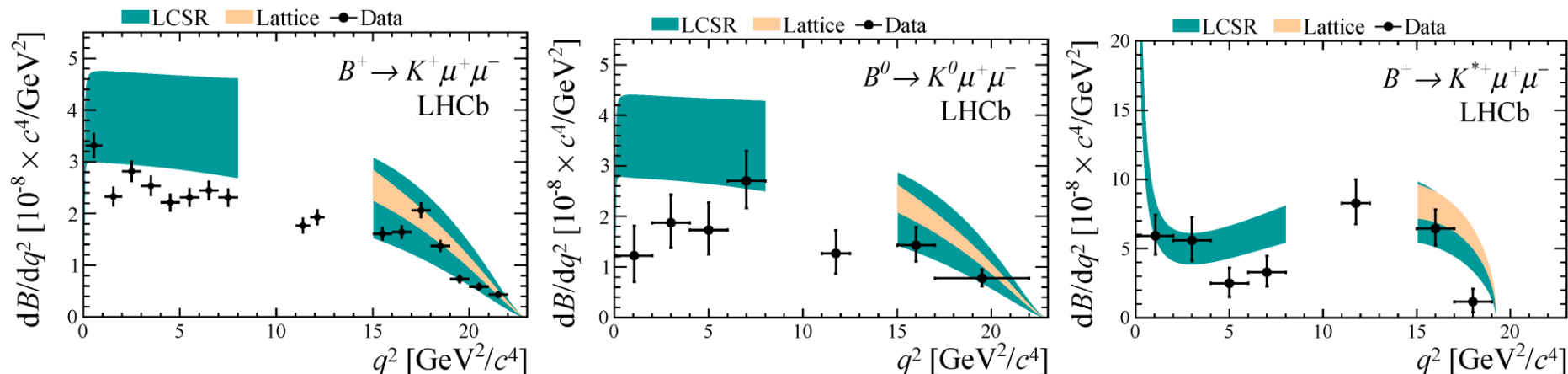
[4.0-6.0] and [6.0-8.0] GeV²/c⁴ bins both 2.9 σ .

The combined deviation is 3.7 σ .

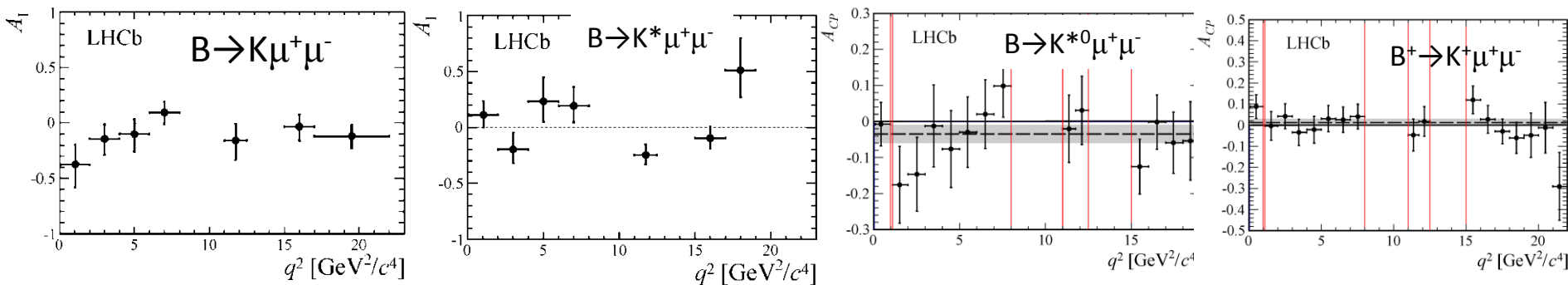
Other coefficients C compatible with SM.

$B \rightarrow K^{(*)} \mu^+ \mu^-$ branching fractions, A_{CP} and A_I asymmetries

JHEP 06 (2014) 133; JHEP 09 (2014) 177



Branching fractions seem to be consistently lower than SM predictions

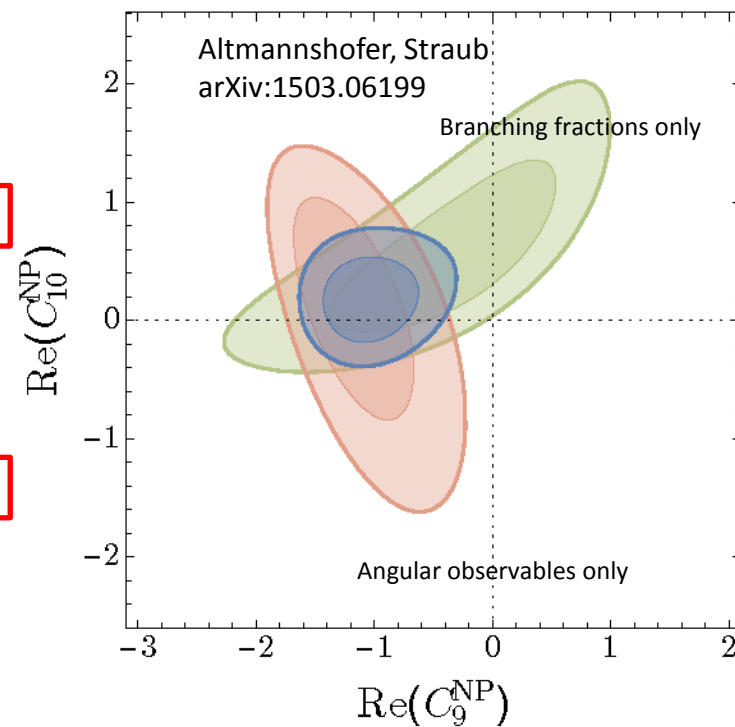


Isospin Asymmetries A_I and CP Asymmetries A_{CP} are in agreement with SM

Interpreting the results

Example of a global fit to multiple measurements from many experiments with coefficients allowed to float one by one.

Coeff.	best fit	1σ	2σ	$\sqrt{\chi_{\text{b.f.}}^2 - \chi_{\text{SM}}^2}$	p [%]
C_7^{NP}	-0.04	$[-0.07, -0.01]$	$[-0.10, 0.02]$	1.42	2.4
C_7'	0.01	$[-0.04, 0.07]$	$[-0.10, 0.12]$	0.24	1.8
C_9^{NP}	-1.07	$[-1.32, -0.81]$	$[-1.54, -0.53]$	3.70	11.3
C_9'	0.21	$[-0.04, 0.46]$	$[-0.29, 0.70]$	0.84	2.0
C_{10}^{NP}	0.50	$[0.24, 0.78]$	$[-0.01, 1.08]$	1.97	3.2
C_{10}'	-0.16	$[-0.34, 0.02]$	$[-0.52, 0.21]$	0.87	2.0
$C_9^{\text{NP}} = C_{10}^{\text{NP}}$	-0.22	$[-0.44, 0.03]$	$[-0.64, 0.33]$	0.89	2.0
$C_9^{\text{NP}} = -C_{10}^{\text{NP}}$	-0.53	$[-0.71, -0.35]$	$[-0.91, -0.18]$	3.13	7.1
$C_9' = C_{10}'$	-0.10	$[-0.36, 0.17]$	$[-0.64, 0.43]$	0.36	1.8
$C_9' = -C_{10}'$	0.11	$[-0.01, 0.22]$	$[-0.12, 0.33]$	0.93	2.0



Angular analysis of $B \rightarrow K^{*0} e^+ e^-$

- Can go to lower effective q^2 than $K^{*0} \mu^+ \mu^-$: $0.002 - 1.12 \text{ GeV}^2/c^4$
- Some NP models predict significant right-handed photons.

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\cos\theta_\ell d\cos\theta_K d\tilde{\phi}} = \frac{9}{16\pi} \left[\frac{3}{4}(1 - F_L) \sin^2\theta_K + F_L \cos^2\theta_K + \left(\frac{1}{4}(1 - F_L) \sin^2\theta_K - F_L \cos^2\theta_K \right) \cos 2\theta_\ell + \frac{1}{2}(1 - F_L) A_T^{(2)} \sin^2\theta_K \sin^2\theta_\ell \cos 2\tilde{\phi} + (1 - F_L) A_T^{\text{Re}} \sin^2\theta_K \cos\theta_\ell + \frac{1}{2}(1 - F_L) A_T^{\text{Im}} \sin^2\theta_K \sin^2\theta_\ell \sin 2\tilde{\phi} \right]. \quad (1.1)$$

$\tilde{\phi} = \phi + \pi \text{ if } \phi < 0$

$$F_L = \frac{|A_0|^2}{|A_0|^2 + |A_{||}|^2 + |A_{\perp}|^2}$$

$$A_T^{(2)} = \frac{|A_{\perp}|^2 - |A_{||}|^2}{|A_{\perp}|^2 + |A_{||}|^2}$$

$$A_T^{\text{Re}} = \frac{2\text{Re}(A_{||L} A_{\perp L}^* + A_{||R} A_{\perp R}^*)}{|A_{||}|^2 + |A_{\perp}|^2}$$

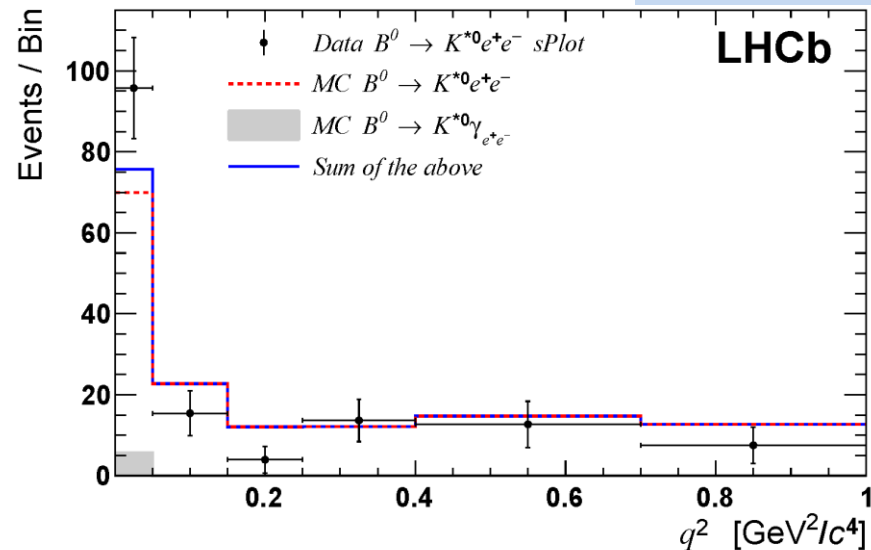
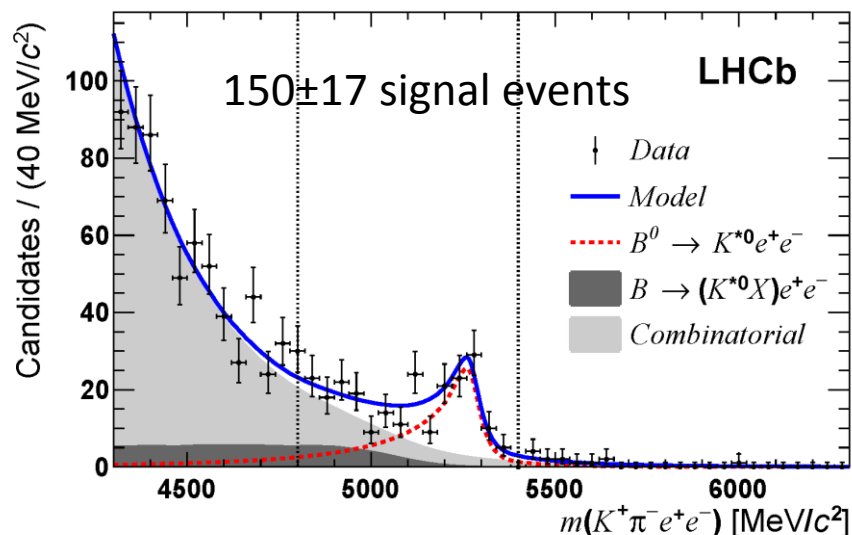
$$A_T^{\text{Im}} = \frac{2\text{Im}(A_{||L} A_{\perp L}^* + A_{||R} A_{\perp R}^*)}{|A_{||}|^2 + |A_{\perp}|^2},$$

- F_L expected to be small
- A_T sensitive to C_7' (right-handed photon):

$$A_T^{(2)}(q^2 \rightarrow 0) = \frac{2\text{Re}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2}, A_T^{\text{Im}}(q^2 \rightarrow 0) = \frac{2\text{Im}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2}, A_T^{\text{Re}} = \frac{4A_{FB}}{3(1 - F_L)}$$

- Extract F_L , $A_T^{(2)}$, A_T^{Im} , and A_T^{Re} in q^2 range $[0.002, 1.12] \text{ GeV}^2$ from ML fit to $(\cos\theta_K, \cos\theta_\ell, \tilde{\phi}, m(K^+ \pi^- e^+ e^-))$.

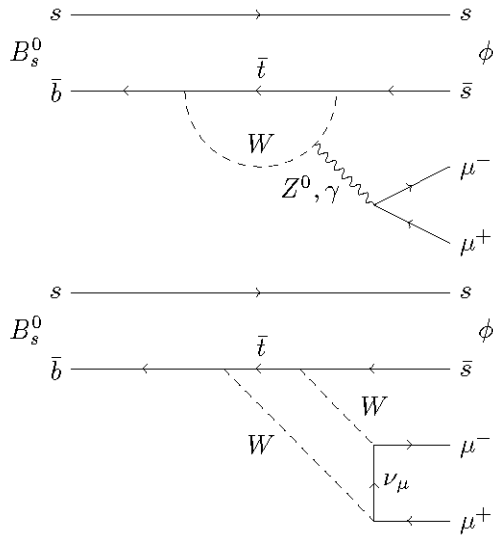
Angular analysis of $B \rightarrow K^{*0} e^+ e^-$



Observable	Measured	SM Prediction
F_L	$+0.16 \pm 0.06 \pm 0.03$	$+0.10^{+0.11}_{-0.05}$
$A_T^{(2)}$	$-0.23 \pm 0.23 \pm 0.05$	$+0.03^{+0.05}_{-0.04}$
A_T^{Re}	$+0.10 \pm 0.18 \pm 0.05$	$-0.15^{+0.04}_{-0.03}$
A_T^{Im}	$+0.14 \pm 0.22 \pm 0.05$	$(-0.2 \pm 1.2) \times 10^{-4}$

Consistent with SM predictions (Jaeger et al. JHEP 05 (2013) 043)

Angular Analysis and dB/dq^2 of $B_s \rightarrow \phi \mu^+ \mu^-$

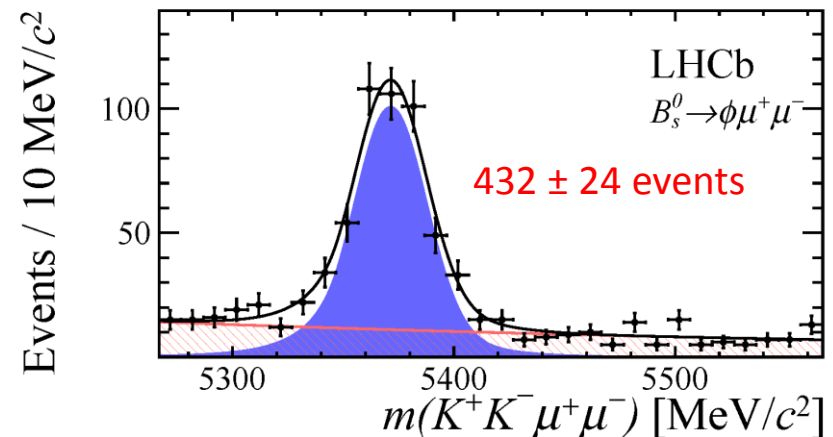
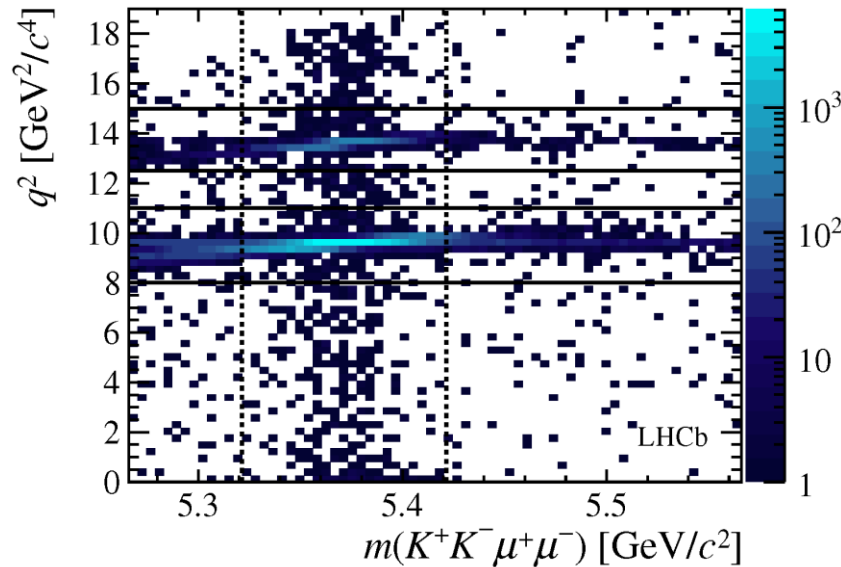


$$\frac{1}{\text{d}\Gamma/\text{d}q^2 \text{d}\cos\theta_l \text{d}\cos\theta_K \text{d}\Phi} \frac{\text{d}^3\Gamma}{\text{d}\Gamma/\text{d}q^2 \text{d}\cos\theta_l \text{d}\cos\theta_K \text{d}\Phi} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ \left. + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l - F_L \cos^2 \theta_K \cos 2\theta_l \right. \\ \left. + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\Phi + S_4 \sin 2\theta_K \sin 2\theta_l \cos \Phi \right. \\ \left. + A_5 \sin 2\theta_K \sin \theta_l \cos \Phi + A_6 \sin^2 \theta_K \cos \theta_l \right. \\ \left. + S_7 \sin 2\theta_K \sin \theta_l \sin \Phi + A_8 \sin 2\theta_K \sin 2\theta_l \sin \Phi \right. \\ \left. + A_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\Phi \right].$$

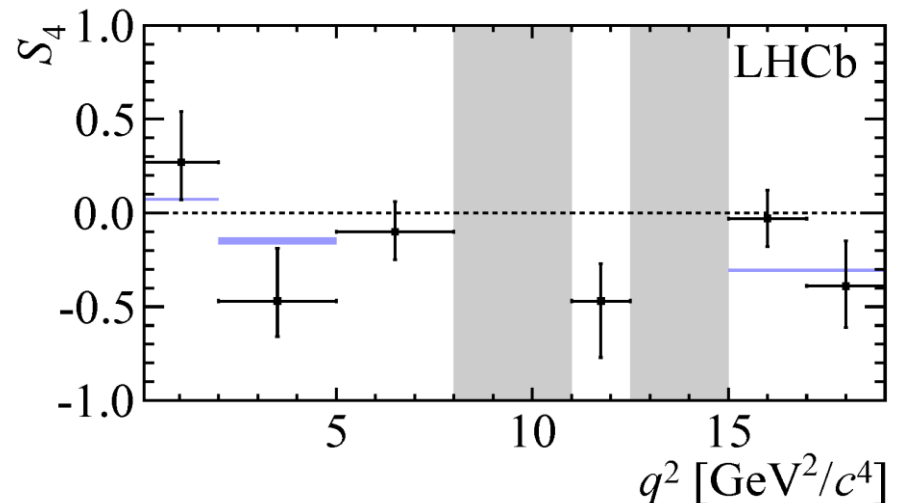
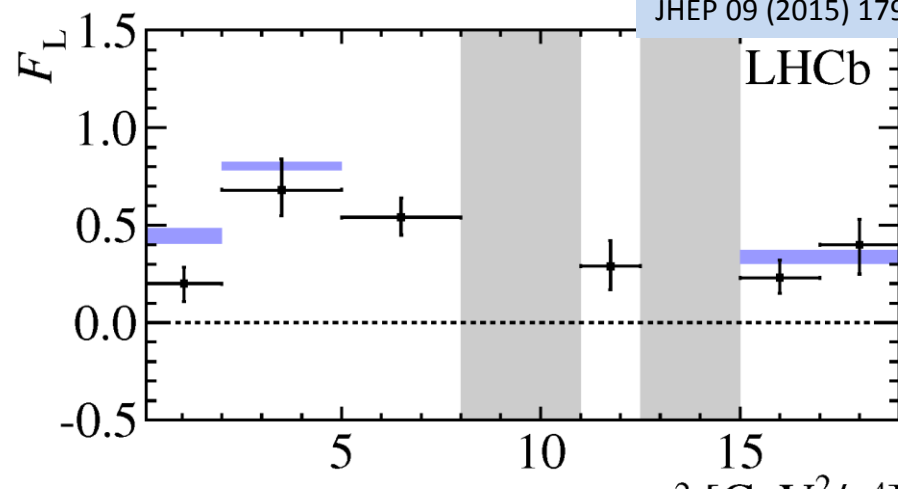
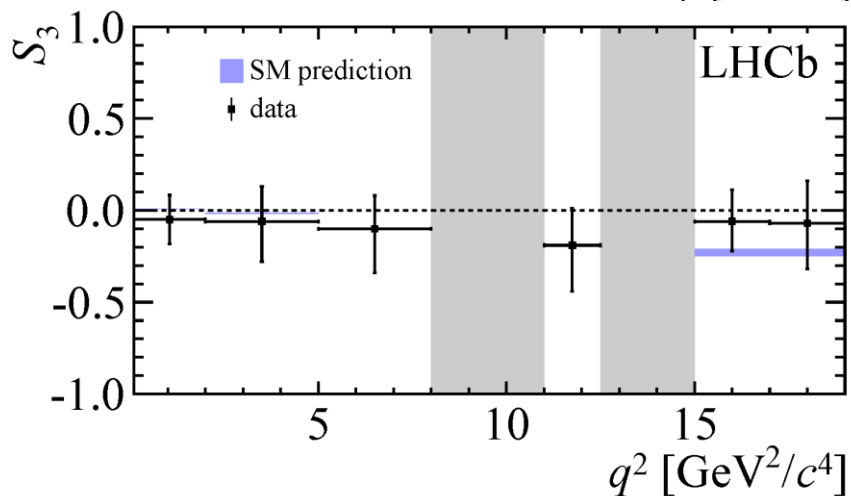
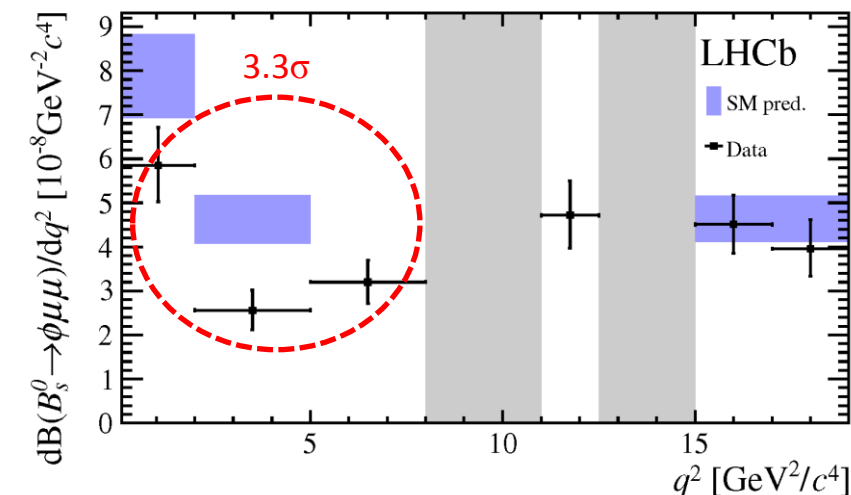
$\phi \rightarrow K^+ K^-$ not flavor specific:

$F_L, S_{3,4,7}$: CP averaged

$A_{5,6,8,9}$: CP asymmetries



Angular Analysis of $B_s \rightarrow \phi \mu^+ \mu^-$



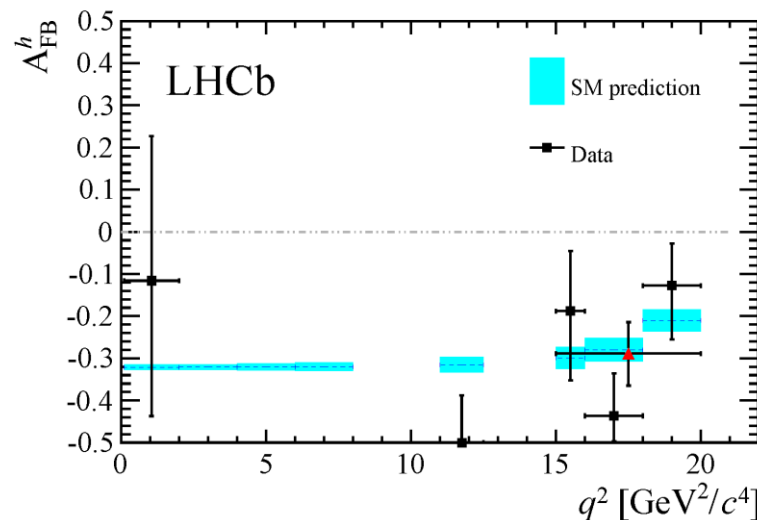
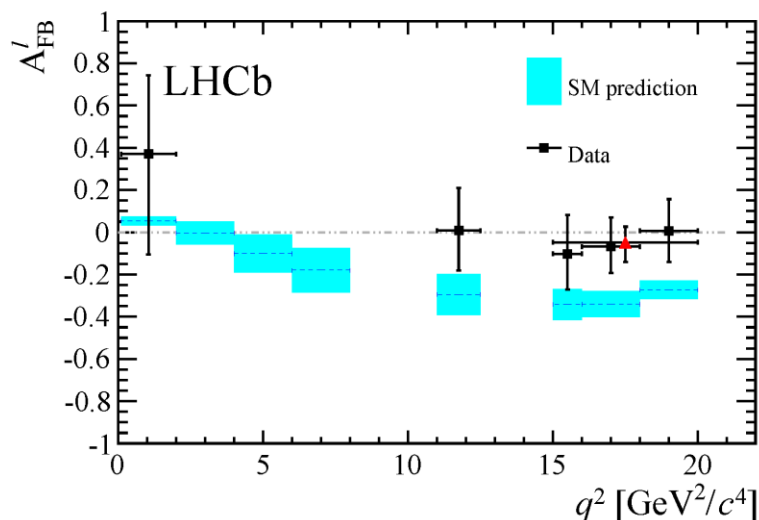
dB/dq^2 disagrees with SM at low q^2 by 3.3σ

F_L , S_3 , S_4 agree with SM predictions.

No SM predictions for other S_i and A_i . If assume SM values near zero, then measurements agree with SM.

Similar to $B \rightarrow K^* l^+ l^-$ but in baryonic mode

Can also look at Forward-Backward asymmetry of the hadron system, A_{FB}^h .



In range $15 < q^2 < 20 \text{ GeV}^2/c^4$:

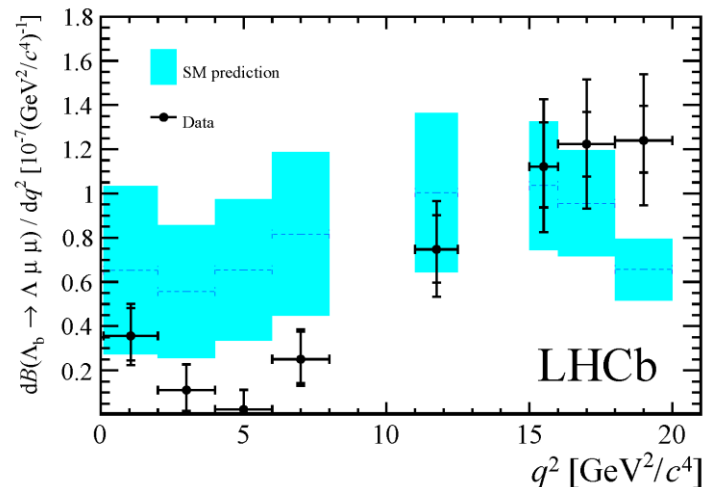
$$\frac{dB(\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-)}{dq^2} = (1.18_{-0.08}^{+0.09} \pm 0.03 \pm 0.27) \times 10^{-7} (\text{GeV}^2/c^4)^{-1}$$

$$A_{FB}^l = -0.05 \pm 0.09 \pm 0.03$$

$$A_{FB}^h = -0.29 \pm 0.07 \pm 0.03$$

Results are compatible with SM in high $q^2 > 15 \text{ GeV}^2/c^4$

Results are below SM predictions in low q^2 region

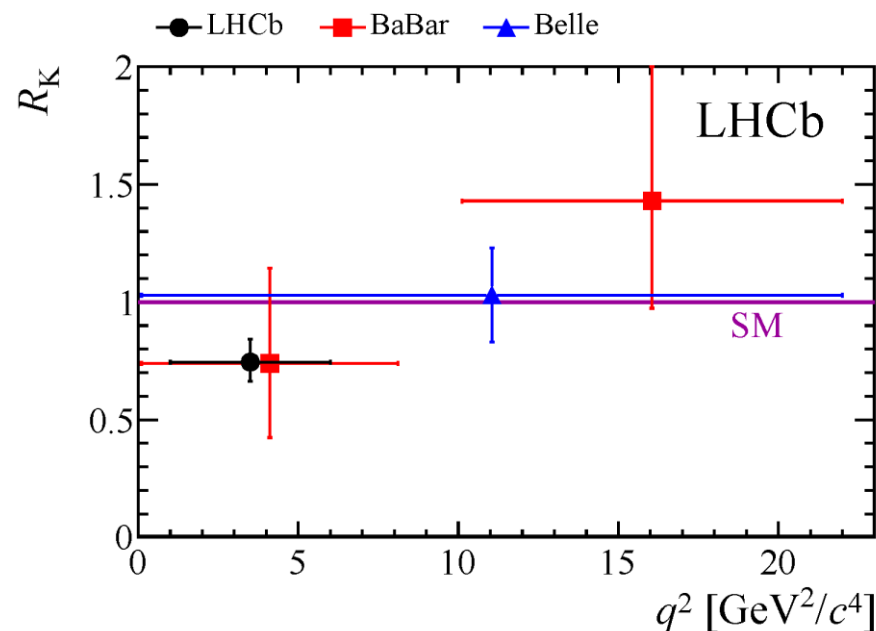
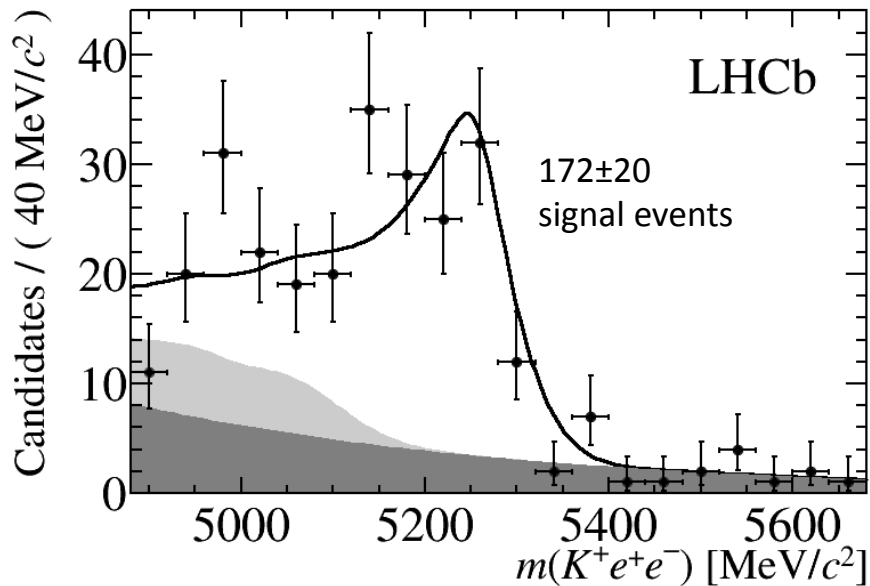


Theoretical uncertainties in branching fraction mostly cancel in ratios.

SM prediction $R_K \approx 1.0 \pm (0.001-0.01)$ depending on corrections.

Extract yields from ML fit to $m(K^+ l^+ l^-)$ spectrum

Use range $1.0 < q^2 < 6.0 \text{ GeV}^2$ as theoretical uncertainties lowest here and for comparison with other experiments.

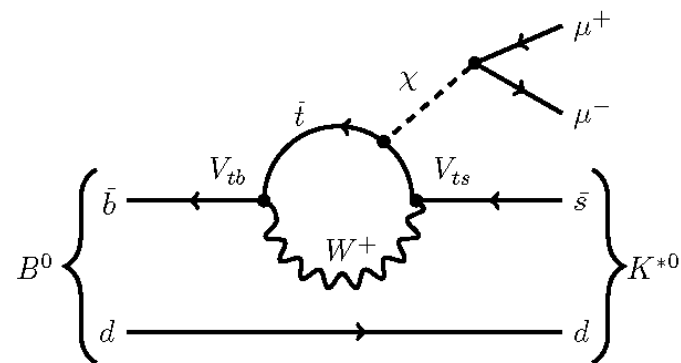
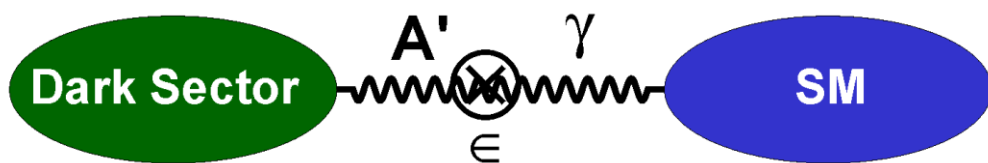


$$R_K = \frac{B(B^+ \rightarrow K^+ \mu^+ \mu^-)}{B(B^+ \rightarrow K^+ e^+ e^-)} = 0.745_{-0.074}^{+0.090} \pm 0.036$$

Ratio is 2.6σ from SM prediction.

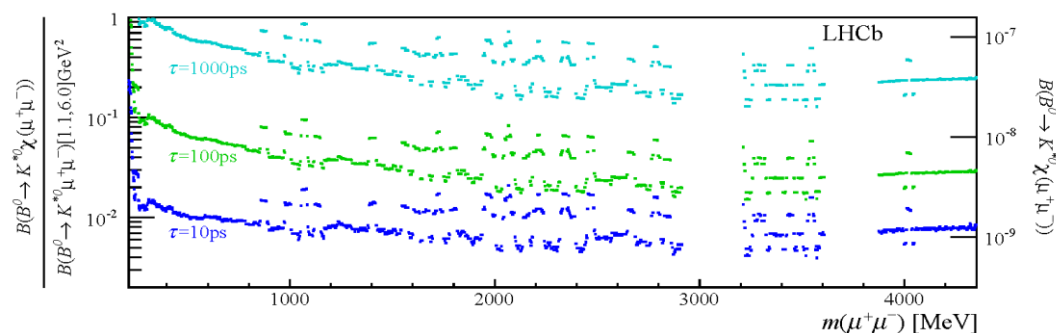
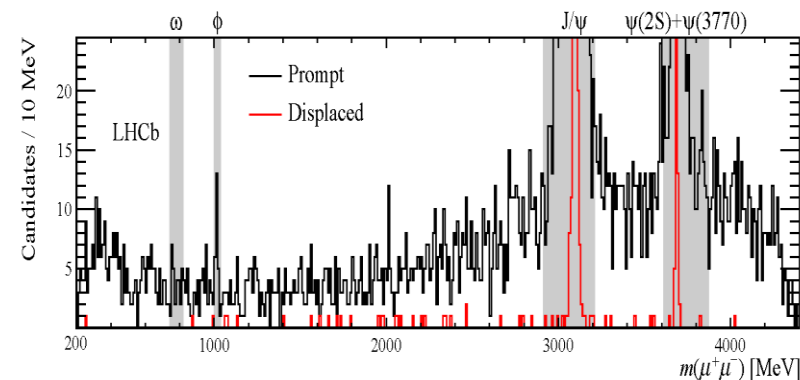
Hidden-Sector Bosons in $B \rightarrow K^{*0} \mu^+ \mu^-$ decays

- With little evidence for ~ 1 TeV scale NP, increased interest in hidden-sector models.
- Postulate a dark matter particle A' interacting feebly with neutral SM particles (H, Z, γ, ν) via mixing of the hidden-sector and SM field with a coupling ε .
- The models have the potential to explain e.g. inflation, baryon asymmetries, suppressed strong-CP, ...



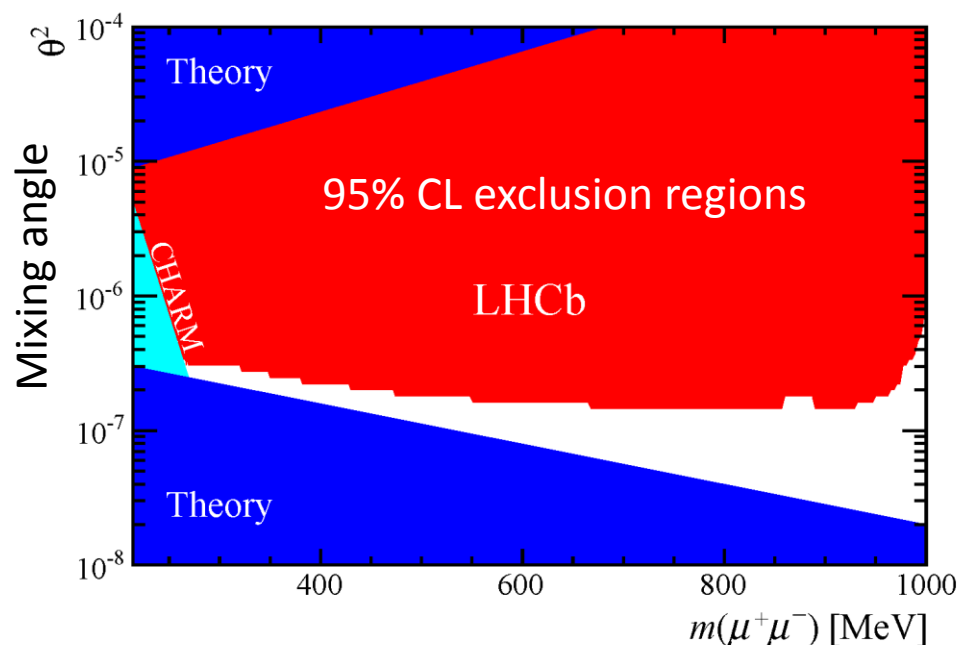
- LHCb has looked for $B^0 \rightarrow K^{*0} \chi$ ($\chi \rightarrow \mu^+ \mu^-$) allowing for different χ lifetimes (lifetime resolution better than 1 ps).
- Normalise branching fraction to prompt $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ in range $1.1 < m^2(\mu^+ \mu^-) < 6.0 \text{ GeV}^2/c^4$.

Hidden-Sector Bosons in $B \rightarrow K^{*0} \mu^+ \mu^-$ decays



Example of constraint on a particular inflaton model with sterile neutrino:

F. Bezrukov and D. Gorbunov, PLB 736 (2014) 494.



Latest LHCb 3 fb^{-1} results are confirming earlier 1 fb^{-1} observations.

Rare $b \rightarrow s$ decays are proving to be intriguing:

2- 3σ deviations from SM in some $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular observables.

Some deviations in dB/dq^2 for $B \rightarrow K l^+ l^-$ decays.

2.6 σ deviation in Lepton Universality in $B^+ \rightarrow K^+ l^+ l^-$ decays.

Results from other experiments, e.g. Belle and BaBar, point in the same direction.

Models that incorporate new physics, e.g. Z' with mass $O(10 \text{ TeV})$, are having some success in explaining deviations.

LHCb is taking more data at higher energy and can expect to continue to improve on precision.