

IR2 Requirements for DVCS and $DV\pi^0P$

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Mar 18th 2021

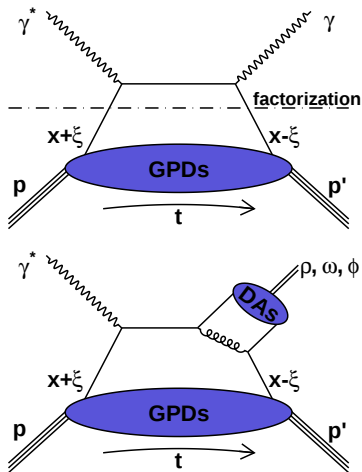


Theory Context



Deep Exclusive Scattering

Generalized Parton Distributions



$$\gamma^* p \rightarrow \gamma p', \gamma^* p \rightarrow \rho p', \omega p', \phi p'$$

Bjorken regime :

$$Q^2 \rightarrow \infty, x_B \text{ fixed}$$

$$t \text{ fixed} \ll Q^2, \xi \rightarrow \frac{x_B}{2-x_B}$$

$$\frac{P^+}{2\pi} \int dy^- e^{ixP^+y^-} \langle p' | \bar{\psi}_q(0) \gamma^+ (1 + \gamma^5) \psi(y) | p \rangle$$

$$= \bar{N}(p') \left[H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) i\sigma^{+\nu} \frac{\Delta_\nu}{2M} + \tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \gamma^5 \frac{\Delta^+}{2M} \right] N(p)$$

spin	N no flip	N flip
q no flip	H	E
q flip	$\tilde{H}$	$\tilde{E}$

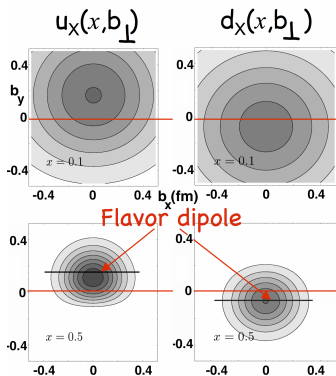
3-D Imaging conjointly in transverse impact parameter **and** longitudinal momentum

GPDs and Transverse Imaging

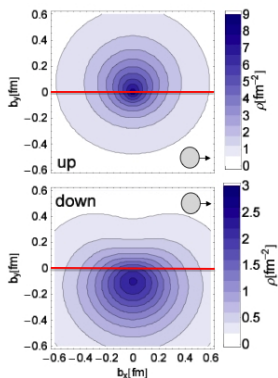
(x_B, t) correlations

$$q_{\mathbf{x}}(x, \vec{b}_{\perp}) = \int \frac{d^2 \vec{\Delta}_{\perp}}{(2\pi)^2} \left[H(x, 0, t) - \frac{E(x, 0, t)}{2M} \frac{\partial}{\partial b_y} \right] e^{-i \vec{\Delta}_{\perp} \cdot \vec{b}_{\perp}}$$

Target polarization



Lattice calculation



GPDs and Energy Momentum Tensor

(x, ξ) correlations

Form Factors accessed via second x-moments :

$$\langle p' | \hat{T}_{\mu\nu}^q | p \rangle = \bar{N}(p') \left[M_2^q(t) \frac{P_\mu P_\nu}{M} + J^q(t) \frac{i(P_\mu \sigma_{\nu\rho} + P_\nu \sigma_{\mu\rho}) \Delta^\rho}{2M} + d_1^q(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{5M} \right] N(p)$$

Angular momentum distribution

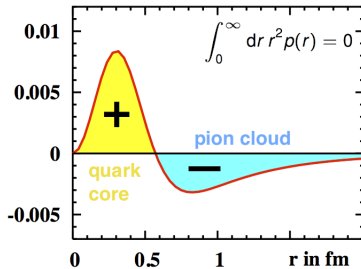
$$J^q(t) = \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

Mass and force/pressure distributions

$$M_2^q(t) + \frac{4}{5} d_1(t) \xi^2 = \frac{1}{2} \int_{-1}^1 dx x H^q(x, \xi, t)$$

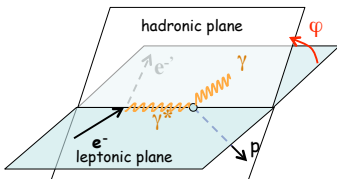
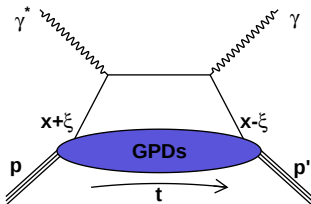
$$d_1(t) = 15M \int d^3\vec{r} \frac{j_0(r\sqrt{-t})}{2t} p(r)$$

Distribution of pressure
 $r^2 p(r)$ in GeV fm^{-1}



Deeply Virtual Compton Scattering

The cleanest GPD probe at low and medium energies



$$ep \rightarrow ep\gamma$$

$$\sigma(ep \rightarrow ep\gamma) \propto \left| \text{DVCS} + \text{BH} \right|^2$$

(a) (b) (c)

Diehl, Gousset, Pire, Ralston (1997)

Belitsky, Müller, Kirchner (2002, 2010)

$$A_{LU} = \frac{d^4\sigma^{\rightarrow} - d^4\sigma^{\leftarrow}}{d^4\sigma^{\rightarrow} + d^4\sigma^{\leftarrow}} \stackrel{\text{twist-2}}{\approx} \frac{\alpha \sin \phi}{1 + \beta \cos \phi}$$

$$\alpha \propto \text{Im} \left(F_1 \mathcal{H} + \xi G_M \tilde{\mathcal{H}} - \frac{t}{4M^2} F_2 \mathcal{E} \right)$$

$$\mathcal{H}(\xi, t) = i\pi H(\xi, \xi, t) + \mathcal{P} \int_{-1}^1 dx \frac{H(x, \xi, t)}{x - \xi}$$

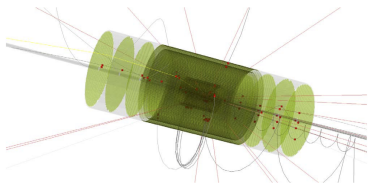
$$A_{UL} \propto \text{Im} \left(F_1 \tilde{\mathcal{H}} + \xi G_M \mathcal{H} + G_M \frac{\xi}{1 + \xi} \mathcal{E} + \dots \right) \sin \phi$$



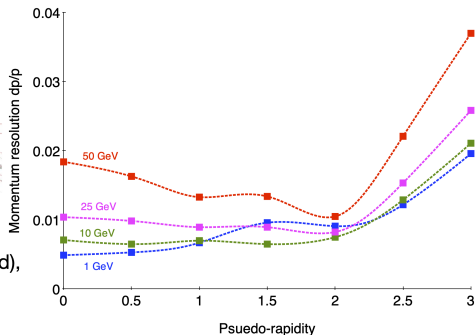
IR2 Studies



EIC Si Tracker Concept



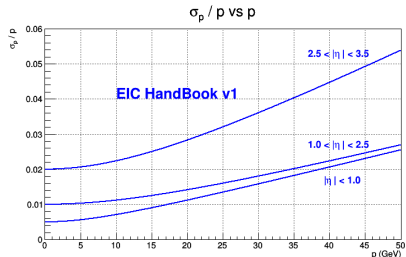
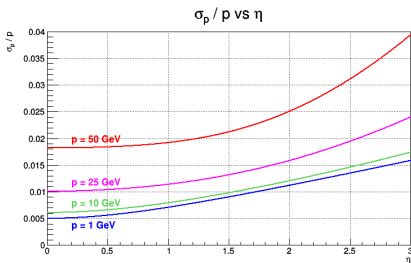
- 6 barrel layers,
- 6 tapered disks x 2 (forward, backward),
- $r_{\text{outer}} \sim 0.45\text{m}$, $-1.22\text{m} < z < 1.22\text{m}$,
- $\sim 15\text{m}^2$ area; $\sim 10\text{m}^2$ barrel, $\sim 5\text{m}^2$ disks



April 9, 2020 - JLab-LBNL EIC discussion

Ernst Sichtermann

Si Tracker Resolutions Parameterization



EIC Handbook Parameterizations:

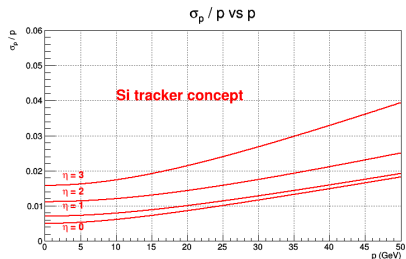
$$2.5 < |\eta| < 3.5 \implies \frac{\sigma_p}{p} = 0.1\% p \oplus 2\%$$

$$1.0 < |\eta| < 2.5 \implies \frac{\sigma_p}{p} = 0.05\% p \oplus 1\%$$

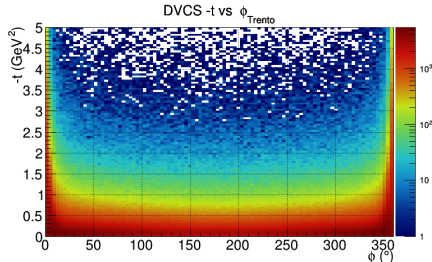
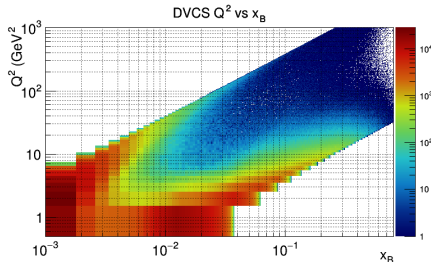
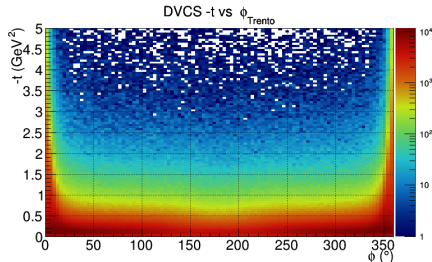
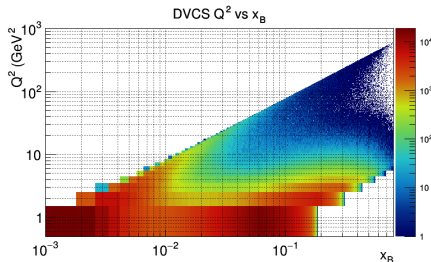
$$|\eta| < 1.0 \implies \frac{\sigma_p}{p} = 0.05\% p \oplus 0.5\%$$

Si concept Parameterization:

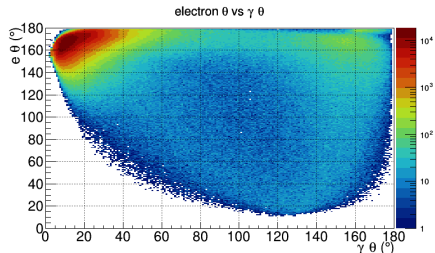
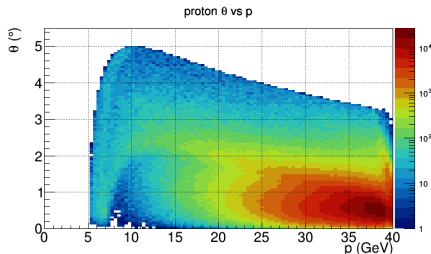
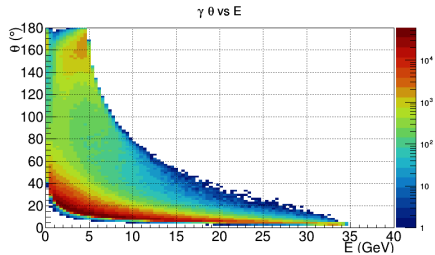
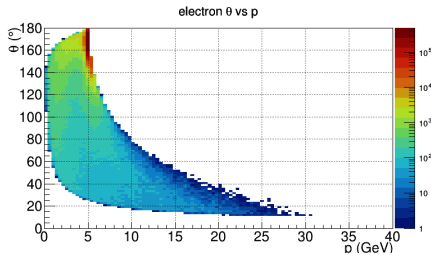
$$\frac{\sigma_p}{p} = 0.5\% \oplus 0.0035\% p \oplus 0.5\% \eta \oplus 7 \times 10^{-5} p \eta^2$$



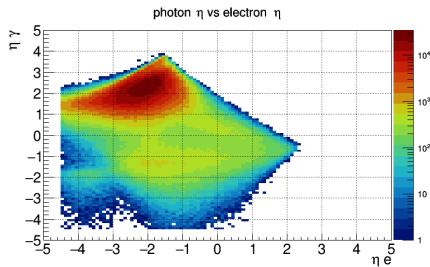
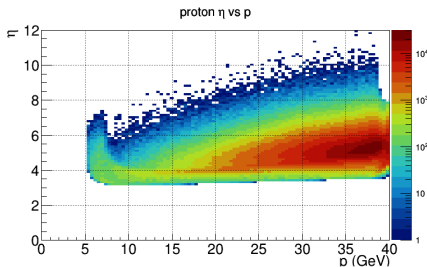
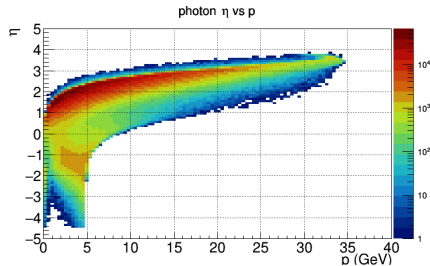
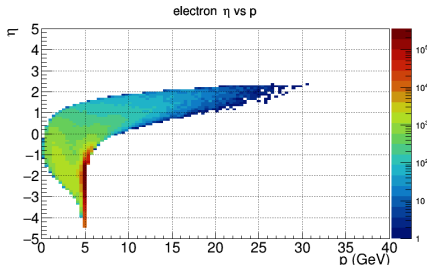
Coverage $5 \times 40 \text{ GeV}^2$ and $10 \times 100 \text{ GeV}^2$



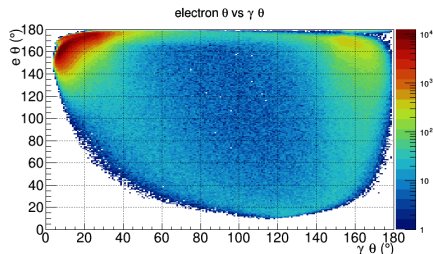
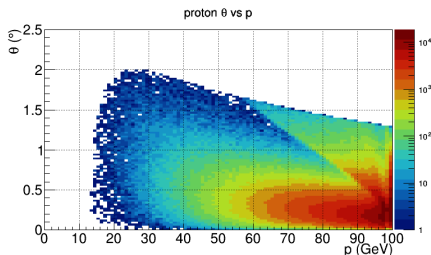
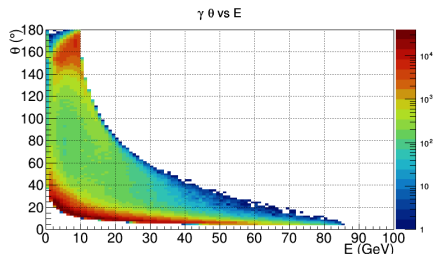
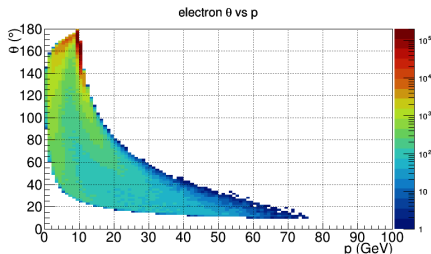
Kinematics $5 \times 40 \text{ GeV}^2$



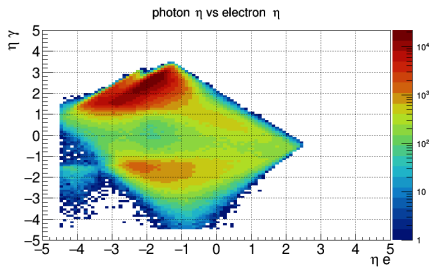
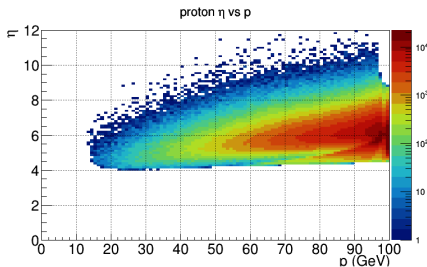
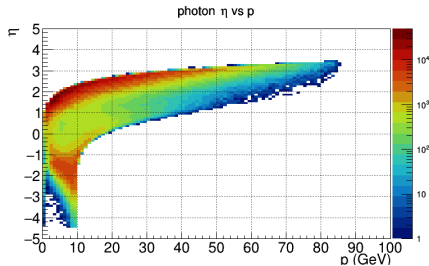
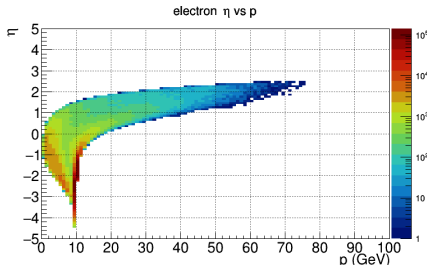
Kinematics $5 \times 40 \text{ GeV}^2$



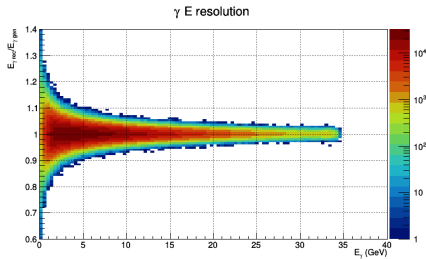
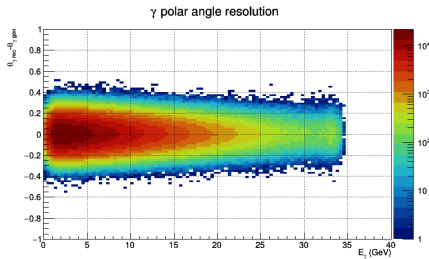
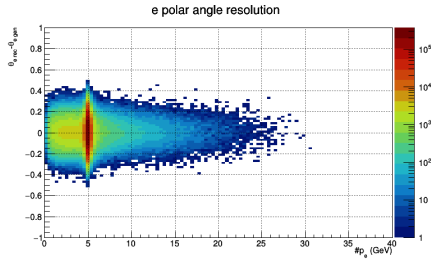
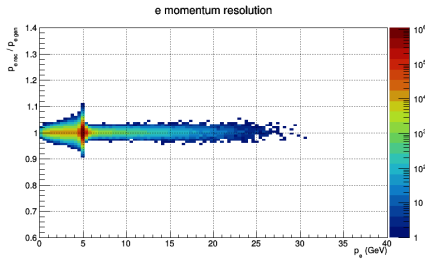
Kinematics $10 \times 100 \text{ GeV}^2$



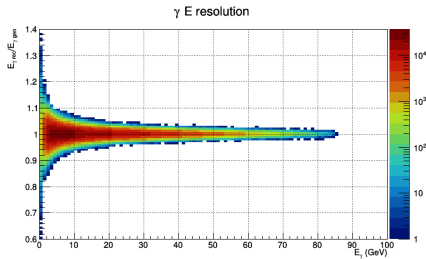
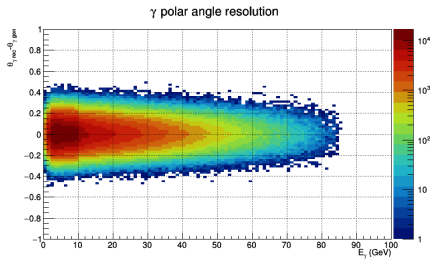
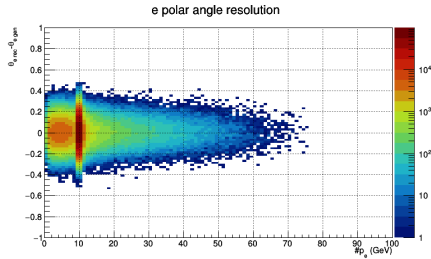
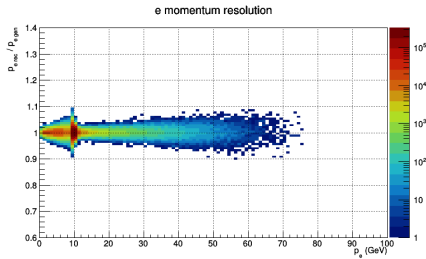
Kinematics $10 \times 100 \text{ GeV}^2$



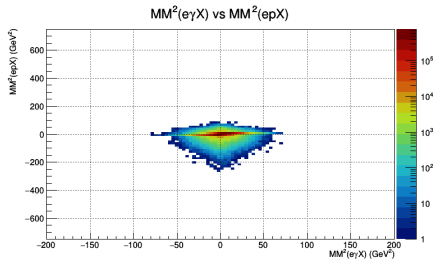
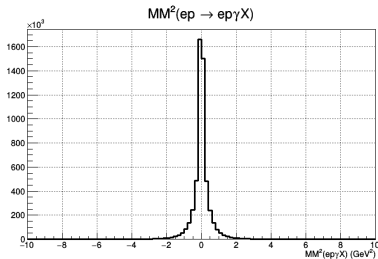
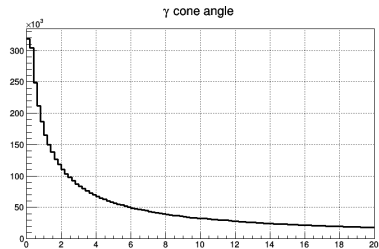
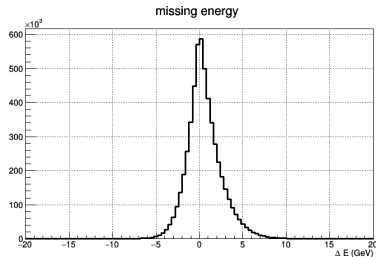
Input Resolutions $5 \times 40 \text{ GeV}^2$



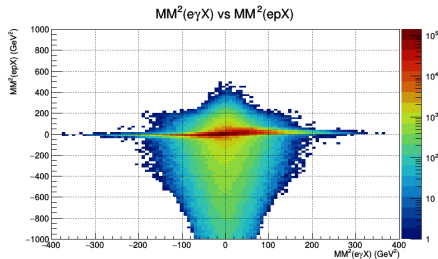
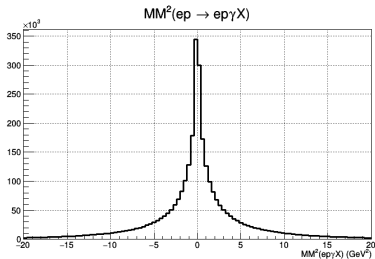
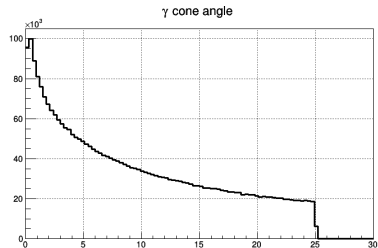
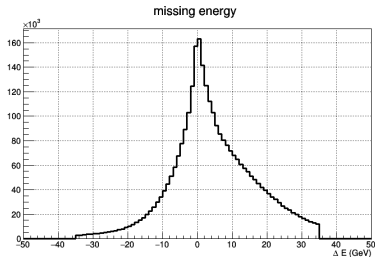
Input Resolutions $10 \times 100 \text{ GeV}^2$



Input Resolutions $5 \times 40 \text{ GeV}^2$



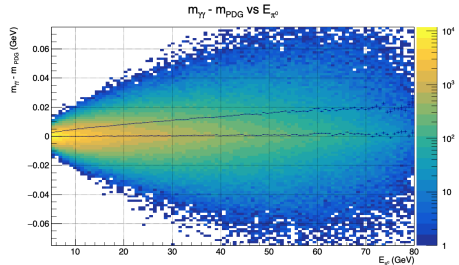
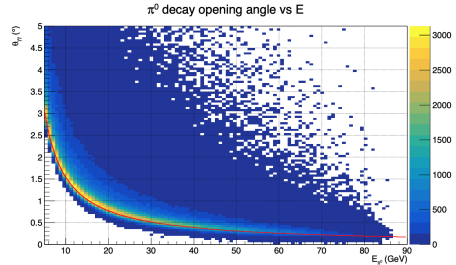
Input Resolutions $10 \times 100 \text{ GeV}^2$



ECal granularity DVCS / π^0 separation

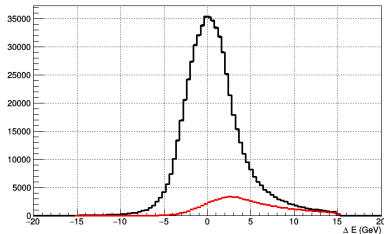
Photon angular resolution is essential to discriminate clusters at high energies
Both θ and ϕ have $\sigma \sim 0.05^\circ < 1$ mrad

Corresponding invariant mass resolution
 ~ 5 to 20 MeV

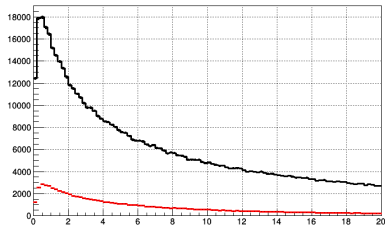


DVCS π^0 separation 5 GeV $\times$ 40 GeV

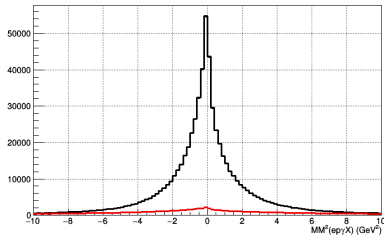
missing energy



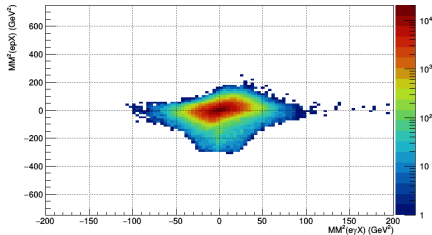
γ cone angle



$MM^2(ep \rightarrow e\gamma X)$

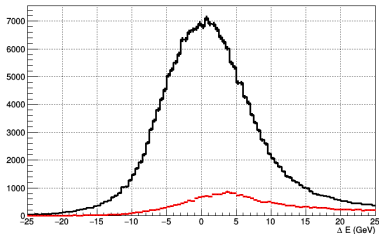


$MM^2(e\gamma X)$ vs $MM^2(epX)$

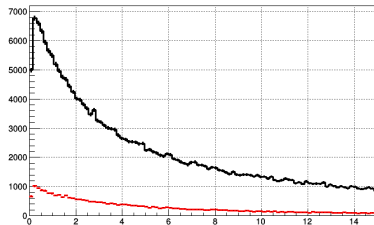


DVCS π^0 separation 10 GeV $\times$ 100 GeV

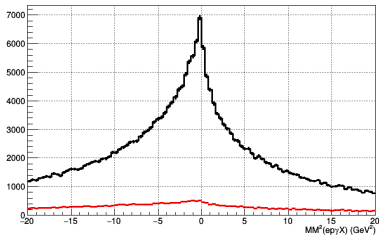
missing energy



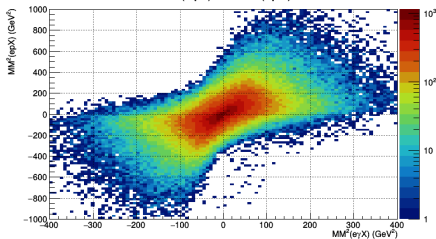
γ cone angle



$MM^2(ep \rightarrow e\gamma X)$

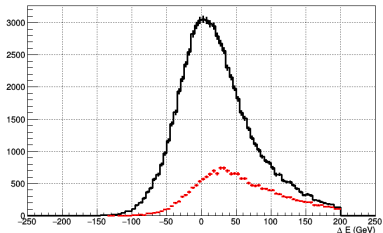


$MM^2(e\gamma X)$ vs $MM^2(epX)$

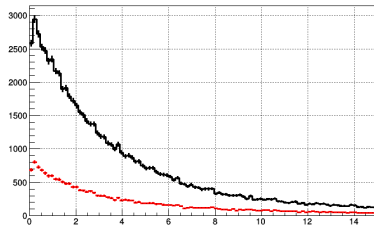


DVCS π^0 separation 18 GeV $\times$ 275 GeV

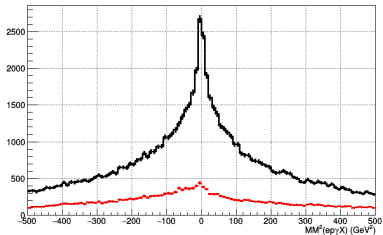
missing energy



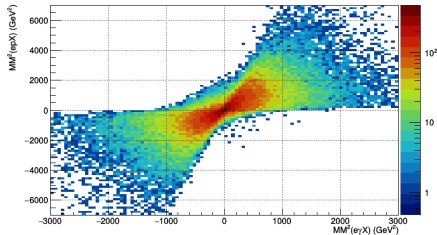
γ cone angle



$MM^2(ep \rightarrow e\gamma X)$



$MM^2(e\gamma X)$ vs $MM^2(epX)$



EIC CFF Extraction Study

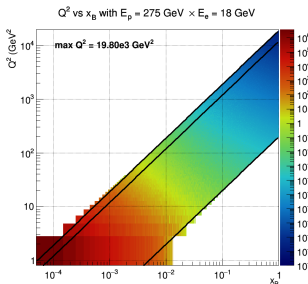


EIC proton DVCS Observables

	$\int \mathcal{L}$	Observables	$A_{e,p}$
unpolarized	200 fb^{-1}	σ	A_{LU}
L polarized	100 fb^{-1}	A_{UL}	A_{LL}
T polarized	100 fb^{-1}	A_{UTx}	A_{UTy} A_{LTx} A_{LTy}
e^+	100 fb^{-1}	A^C	A_{LU}^C

$$N_{\text{events}} = \int \mathcal{L} \times \sigma \times \text{KPS}$$

$$\text{KPS} = \Delta x_B \Delta Q^2 \Delta t \Delta \phi$$



$$\frac{\Delta \sigma}{\sigma} = \frac{1}{\sqrt{N_{\text{events}}}} \oplus 5\%$$

$$\Delta A_{LU} = \frac{1}{P_e} \sqrt{\frac{1 - P_e^2 A_{LU}^2}{N}} \oplus 3\%_{\text{relative}} \quad P_e = 70\%$$

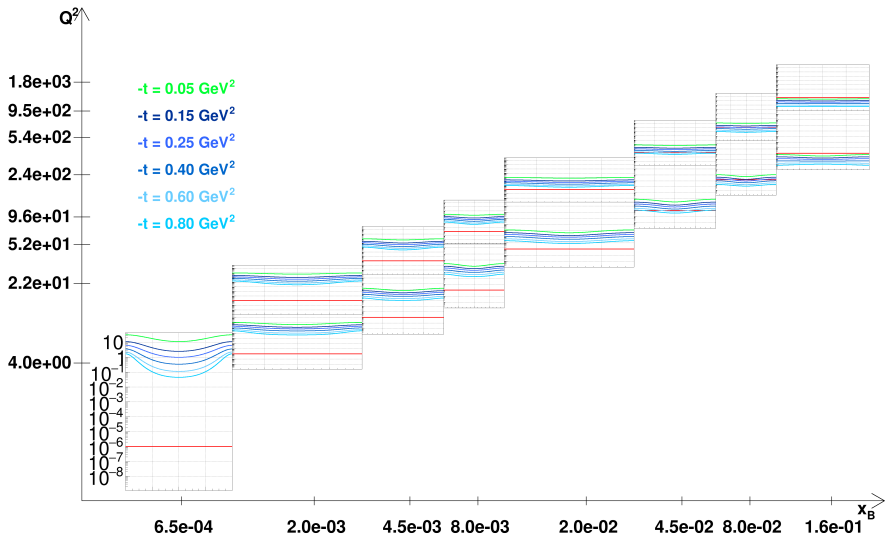
$$\Delta A_{UL} = \frac{1}{P_p} \sqrt{\frac{1 - P_p^2 A_{UL}^2}{N}} \oplus 3\%_{\text{relative}} \quad P_p = 70\%$$

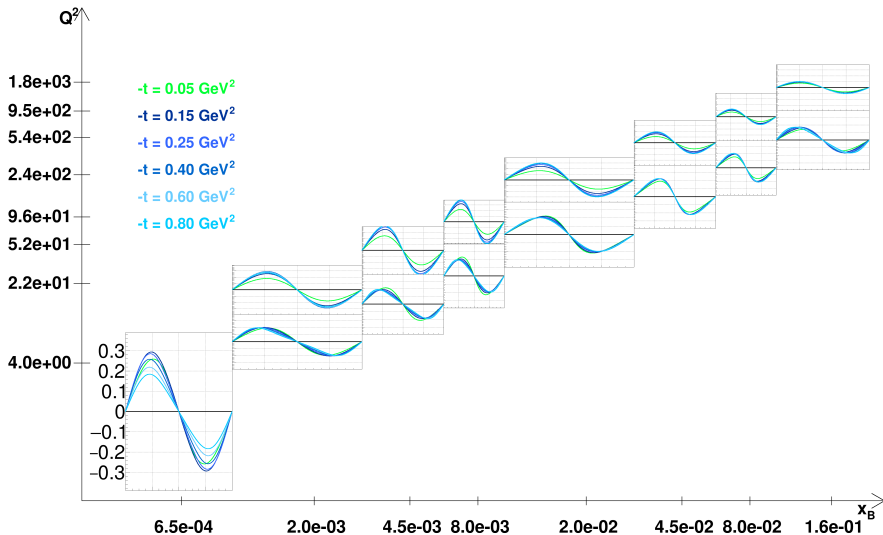
$$\Delta A_{LL} = \frac{1}{P_e P_p} \sqrt{\frac{1 - P_e^2 P_p^2 A_{LL}^2}{N}} \oplus 3\%_{\text{relative}} \oplus 3\%_{\text{relative}}$$

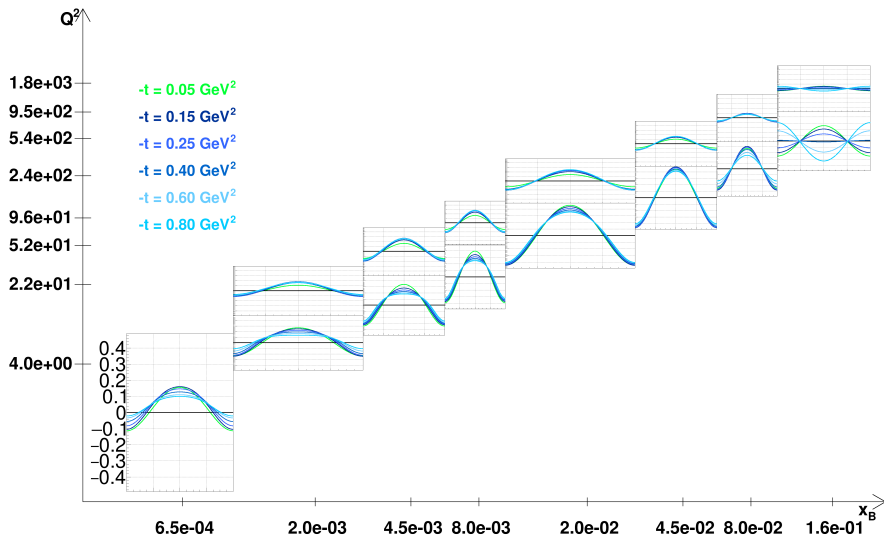
$$\Delta A_C = \sqrt{\frac{1 - A_C^2}{N}} \oplus 3\%_{\text{relative}}$$

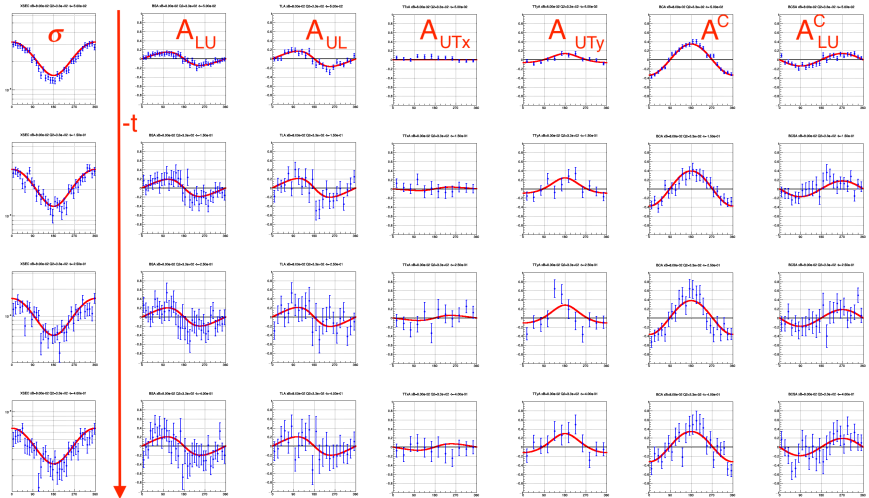
$$\Delta A_{LC} = \frac{1}{P_{e^+}} \sqrt{\frac{1 - P_{e^+}^2 A_{LC}^2}{N}} \oplus 3\%_{\text{relative}} \quad P_{e^+} = 70\%$$



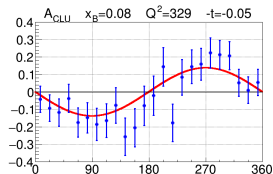
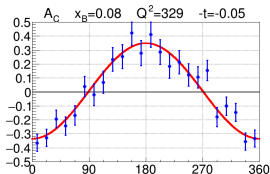
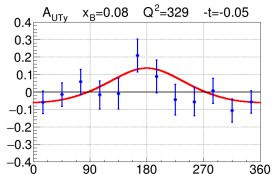
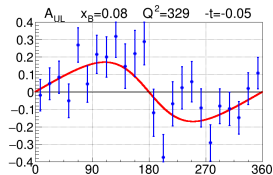
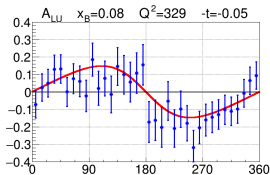
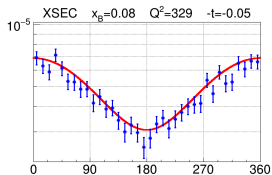






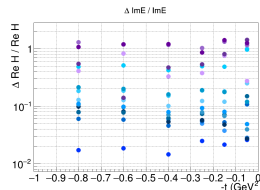
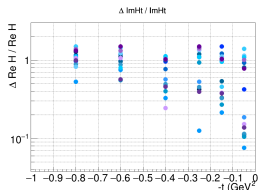
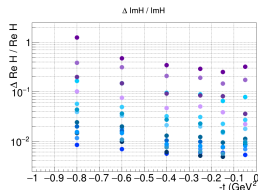
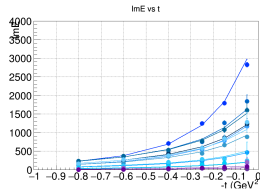
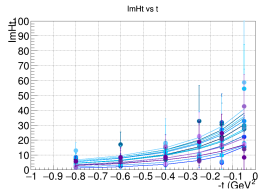
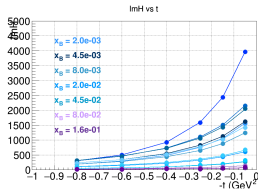


Not shown here: A_{LL} A_{LTx} A_{LTy} are small

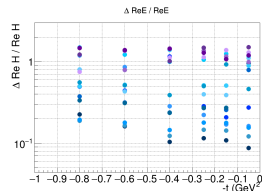
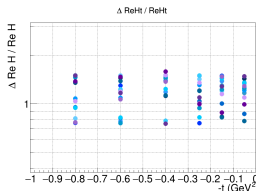
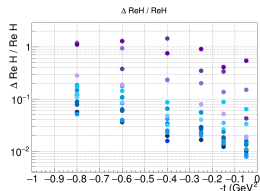
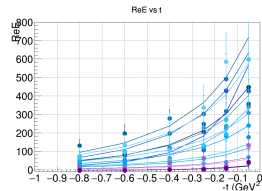
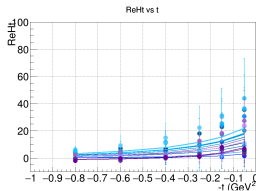
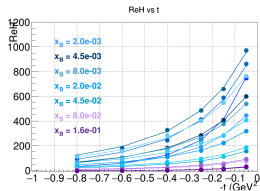


Smearing both statistics and systematics
Fit CFF wth/without to estimate systematics

Locally extracted Im CFF $275 \times 18 \text{ GeV}^2$

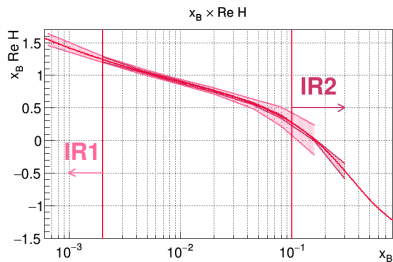
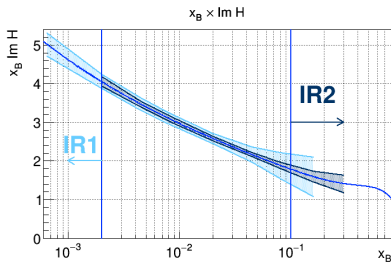


Locally extracted Re CFF $275 \times 18 \text{ GeV}^2$



Complementarity of IR1 and IR2

Local extraction results:



Entering the GPD extraction Precision Era!

Summary, Outlook



Summary, Outlook

- Complementarity between IR1 and IR2
- Conceptual Design for IR2
- Resolutions similar to Handbook v1
- Next Step: implement dispersion relation (global) fit

