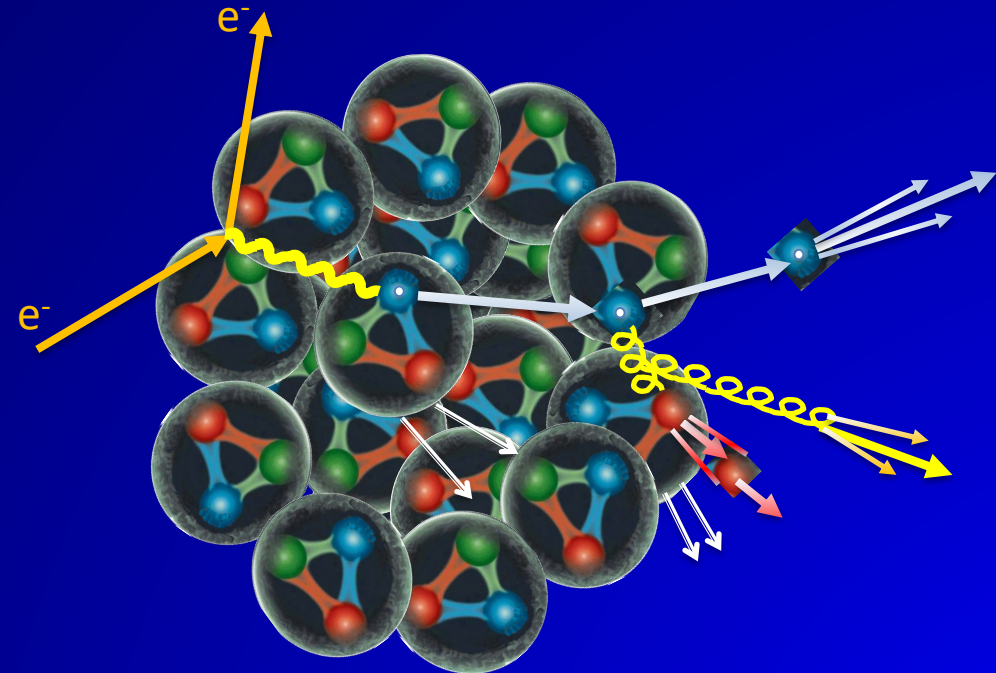
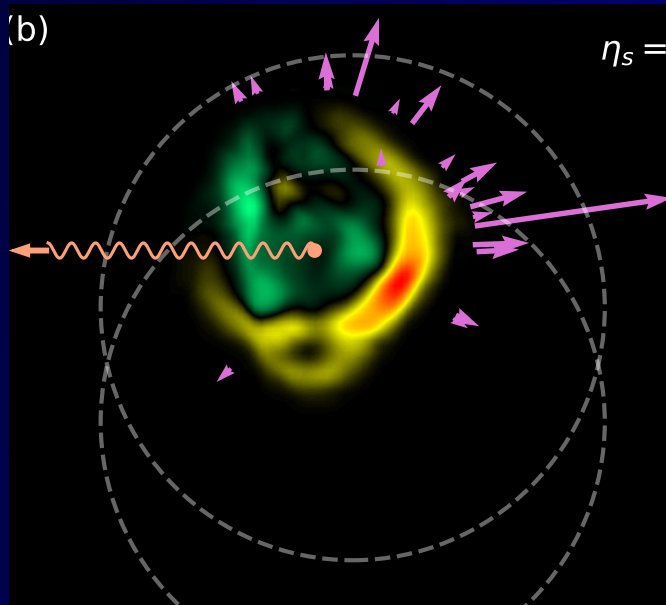


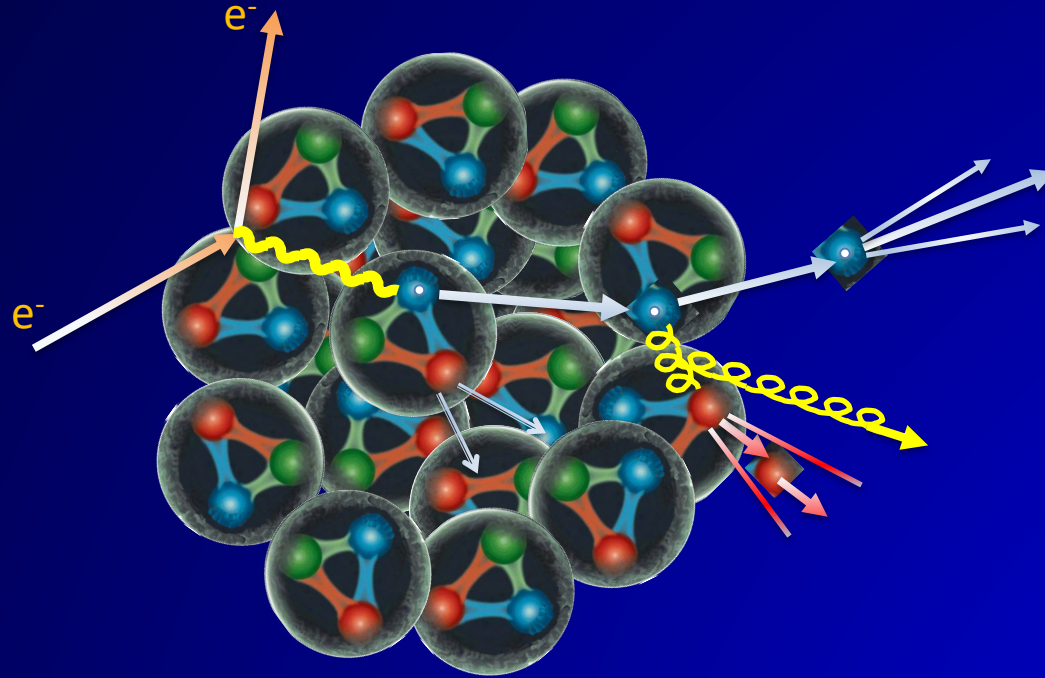
Jet quenching in A+A and e+A Collisions



Xin-Nian Wang

Lawrence Berkeley National Laboratory

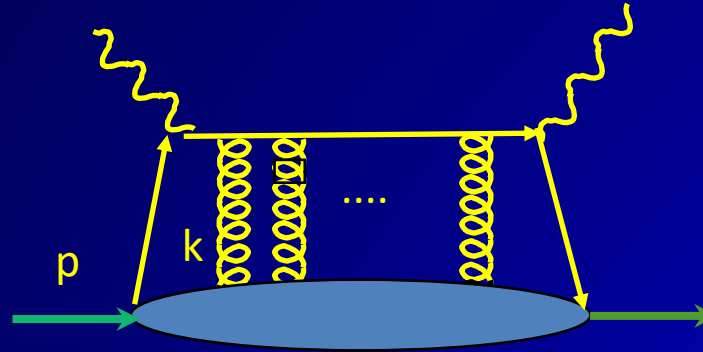
Jet production in DIS off nuclei



Multiple scattering, p_T broadening, parton energy loss, hadronization, hadronic interaction in nuclei

Multiple parton scattering in nuclear medium

$$f_A^q(x, \vec{k}_\perp) = \int \frac{dy^-}{4\pi} \frac{d^2 y_\perp}{(2\pi)^2} e^{ixp^+ y^- - i\vec{k}_\perp \cdot \vec{y}_\perp} \langle A | \bar{\psi}(0) \gamma^+ \mathcal{L}(0, y) \psi(y) | A \rangle$$



Liang, XNW & Zhou, *PRD* 77 (2008) 125010

$$\Delta = \int dy \hat{q}(y)$$

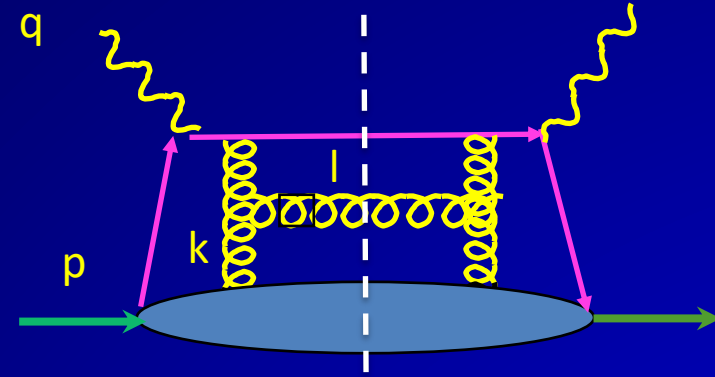
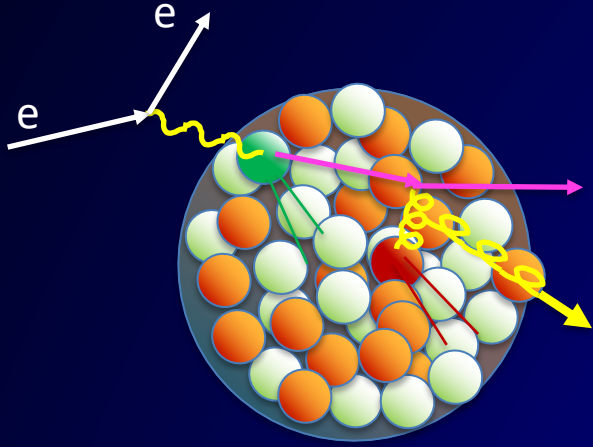
$$f_A^q(x, \vec{k}_\perp) \approx \frac{A}{\pi \Delta} \int d^2 q_\perp \exp \left[-\frac{(\vec{k}_\perp - \vec{q}_\perp)^2}{\Delta} \right] f_N^q(x, \vec{q}_\perp)$$

p_T broadening and Jet transport coefficient:

Saturation scale probed by jet

$$\hat{q}(y) = \frac{4\pi^2 \alpha_s C_R}{N_c^2 - 1} \rho(y) x G(x) |_{x \approx 0} \longleftrightarrow Q_s^2 = \int dy \hat{q}(y)$$

Parton energy loss in nuclear medium



Zhang, Qin and XNW, *PRD* 100 (2019) 7, 074031

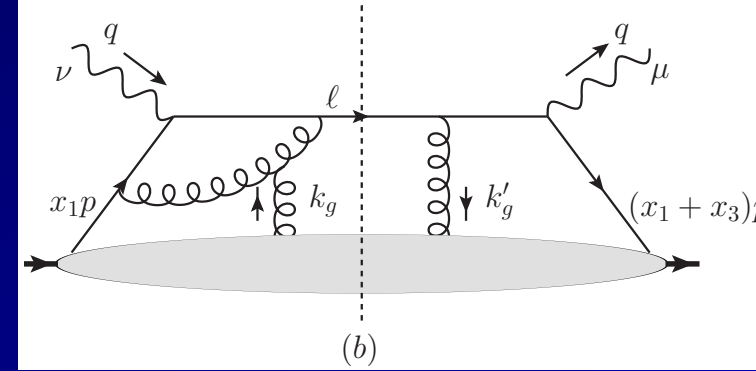
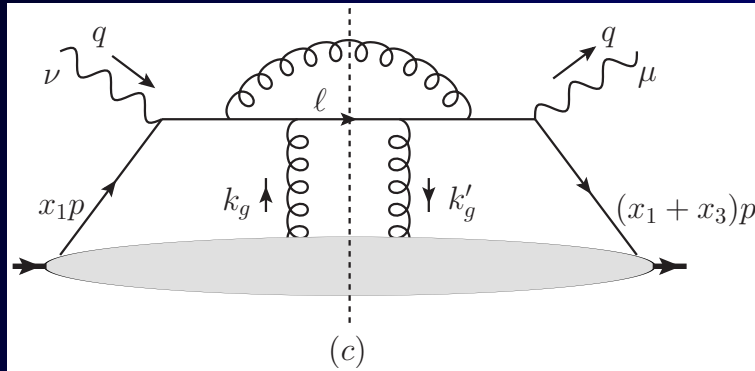
$$\frac{dN_g}{dl_{\perp}^2 dz} = \int_{y^-}^{\infty} dy_1^- \left[\rho_A(y_1^-, \vec{y}_{\perp}) \frac{2\pi\alpha_s}{N_c} \pi \int \frac{dk_{\perp}^2}{(2\pi)^2} \underbrace{\phi_g(0, \vec{k}_{\perp})}_{\text{Nucleon TMD gluon distr.}} \right] \pi \frac{\alpha_s}{2\pi} P_{qg}(z) \frac{C_A}{l_{\perp}^2} \mathcal{N}_g(\vec{l}_{\perp}, \vec{k}_{\perp})$$

Nucleon TMD gluon distr.

$$\mathcal{N}_g^{\text{static+soft}} = \int \frac{d\varphi}{2\pi} \frac{2\vec{k}_{\perp} \cdot \vec{l}_{\perp}}{(\vec{l}_{\perp} - \vec{k}_{\perp})^2} \left(1 - \cos\left[\frac{(\vec{l}_{\perp} - \vec{k}_{\perp})^2}{2q^- z(1-z)} y_1^- \right] \right) \longrightarrow \text{GLV}$$

τ_f Formation time of the gluon emission y_1^- / τ_f

Factorization and qhat of the cold & hot medium



- Cancellation of **soft-collinear** divergence
- Factorization of **the collinear** divergence

Kang, Wang, Xing & Wang, *PRL* 112, 102001(2014);
PRD 94 (2016) 11; *PRD* 94 (2016) 7, 074038

$$\frac{d\langle k_{\perp}^2 \sigma \rangle_{\text{NLO}}}{dz_h} = \sigma_0 D_h(z, \mu_f^2) \otimes H_{\text{NLO}}(x, x_B, Q^2, \mu_f^2) \otimes T_{qg}(x, x_1, x_2, \mu_f^2)$$

$$\frac{\partial}{\partial \ln \mu_f^2} T_{qg}(x_B, 0, 0, \mu_f^2) = \frac{\alpha_s}{2\pi} \int_{x_B}^1 \frac{dx}{x} \left[\mathcal{P}_{qg \rightarrow qg} \otimes T_{qg} + P_{qg}(\hat{x}) T_{gg}(x, 0, 0, \mu_f^2) \right]$$

$$T_{qg}(x_B, 0, 0, \mu_f^2) \implies \hat{q} \implies \hat{q}(E, Q^2) \quad \text{for both DIS and DY}$$

CoLBT-hydro

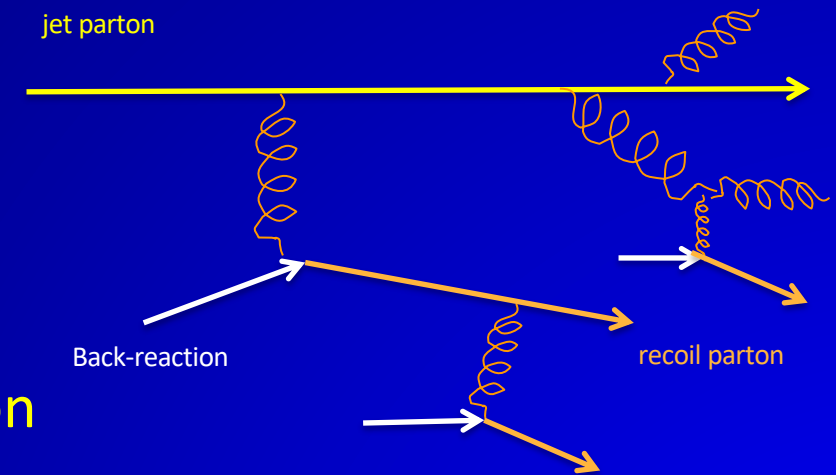
(Coupled Linear Boltzmann Transport hydro)

Concurrent and coupled evolution of bulk medium and jet showers

$$\partial_\mu T^{\mu\nu}(x) = j^\nu(x) \quad j^\nu(x) = \sum_i p_i^\nu \delta^{(4)}(x - x_i) \theta(p_{cut}^0 - p \cdot u)$$

$$p \cdot \partial f(p) = -C(p) \quad (p \cdot u > p_{cut}^0)$$

- LBT for energetic partons (jet shower and recoil)
- Hydrodynamic model for bulk and soft partons: CLVisc
- Parton coalescence (thermal-shower)+ jet fragmentation
- Hadron cascade using UrQMD



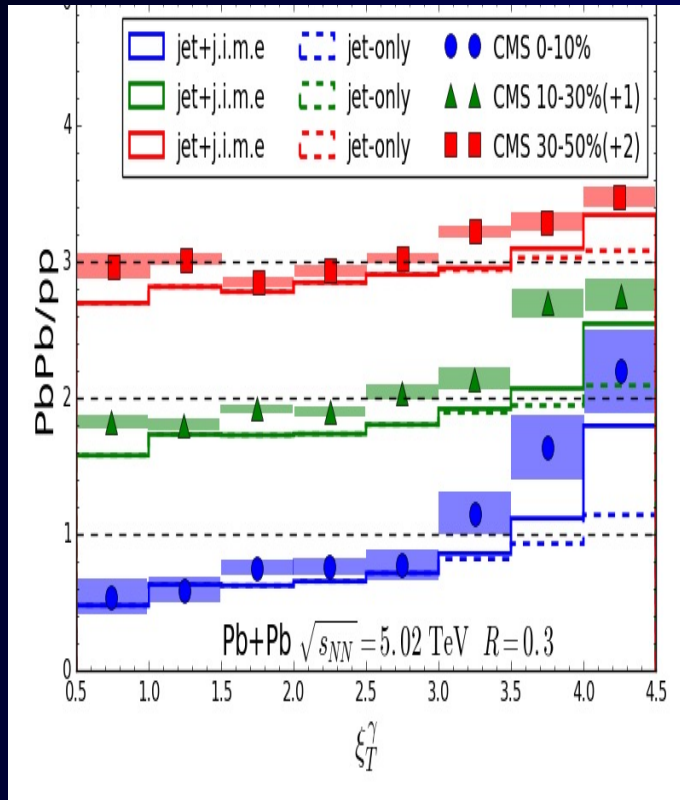
Phys. Lett. B 777 (2018) 86, *Phys. Lett. B* 810 (2020) 135783, e-Print: [2101.05422](https://arxiv.org/abs/2101.05422)

Phys. Rev. C 96 (2017) 3, 034903, *Phys. Lett. B* 777 (2018) 255-259, *Phys. Rev. C* 98 (2018) 021901, *Phys. Rev. Lett.* 122 (2019) 25, 252302, *Phys. Rev. C* 99 (2019) 5, 054911, *Phys. Rev. Lett.* 125 (2020) 12, 122301

Jet quenching in heavy-ion collisions

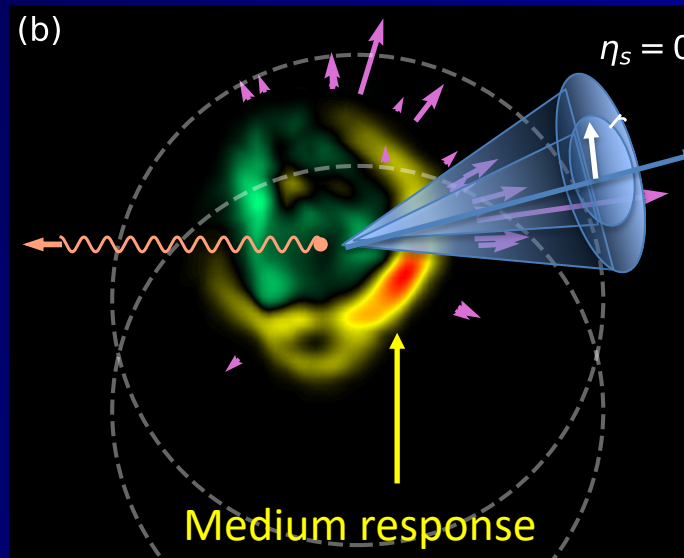
Luo *et al*, Phys. Lett. B 782 (2018) 707-716

γ -jet fragmentation function



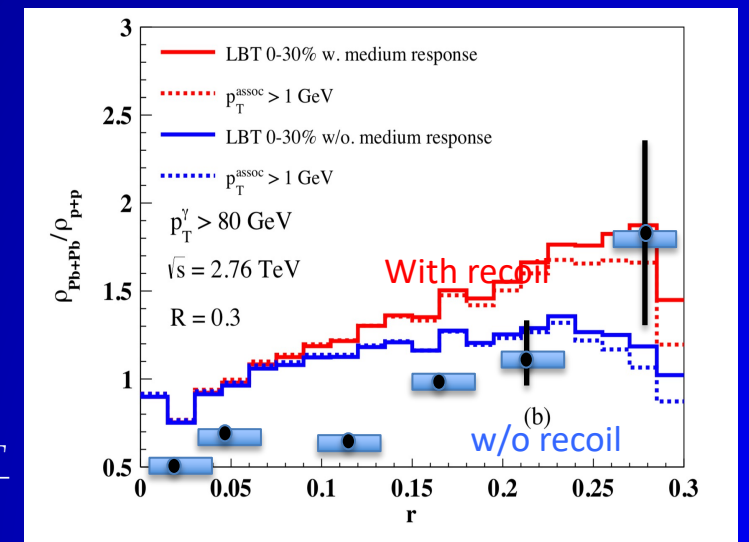
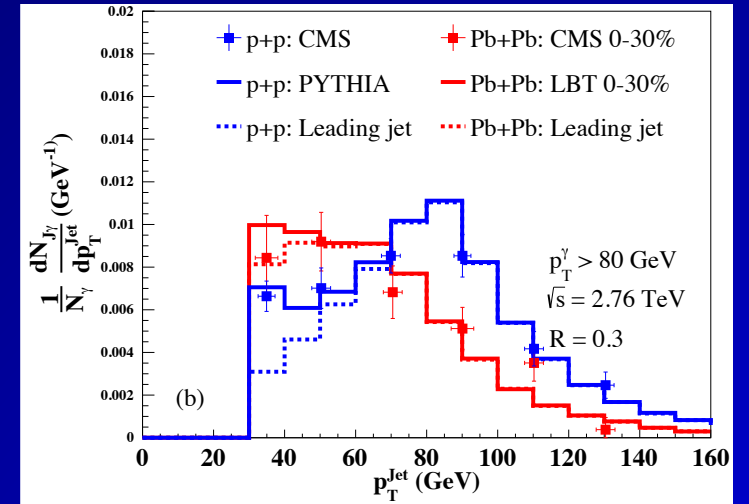
Chen, *et al.*, Phys. Lett. B 810 (2020)

γ -jet asymmetry

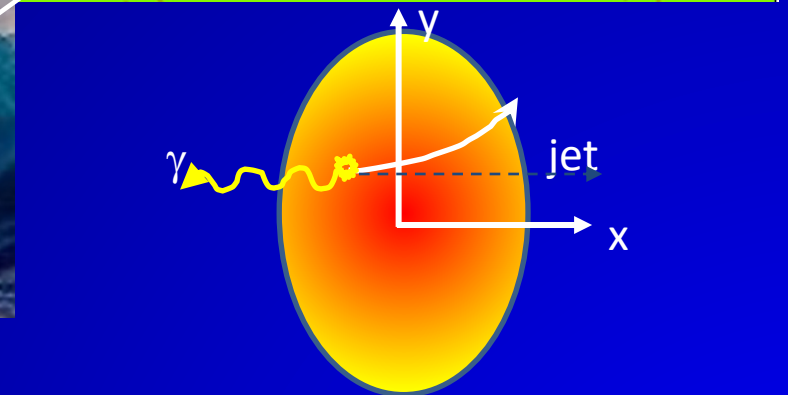
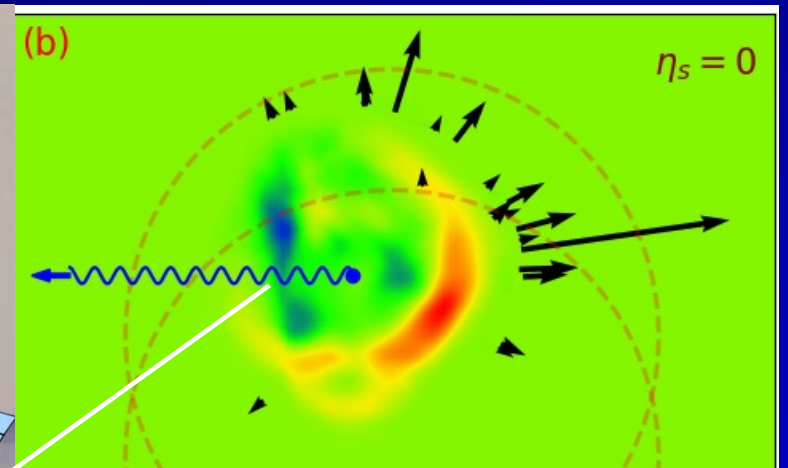
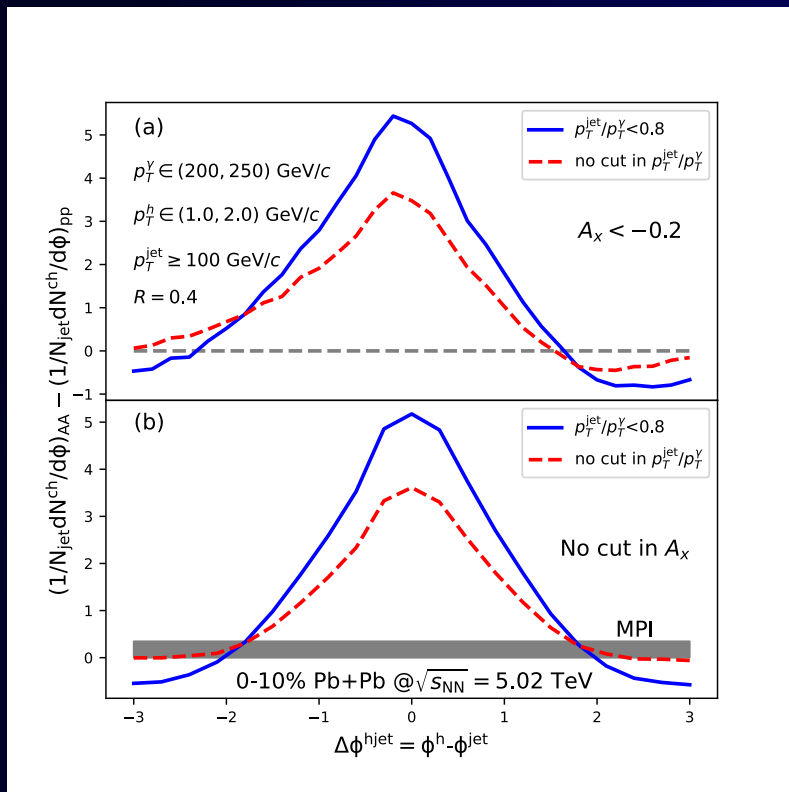


γ -jet profile

$$\rho(r) = \frac{1}{E_T} \frac{dE_T}{dr}$$



Enhancing the diffusion wake



$$A_{E\perp}^{\vec{n}} = \frac{\int d^3r d^3p f_a(\vec{p}, \vec{r}) \vec{p}_T \cdot \vec{n}}{\int d^3r d^3p f_a(\vec{p}, \vec{r})}$$

e-Print: 2101.05422

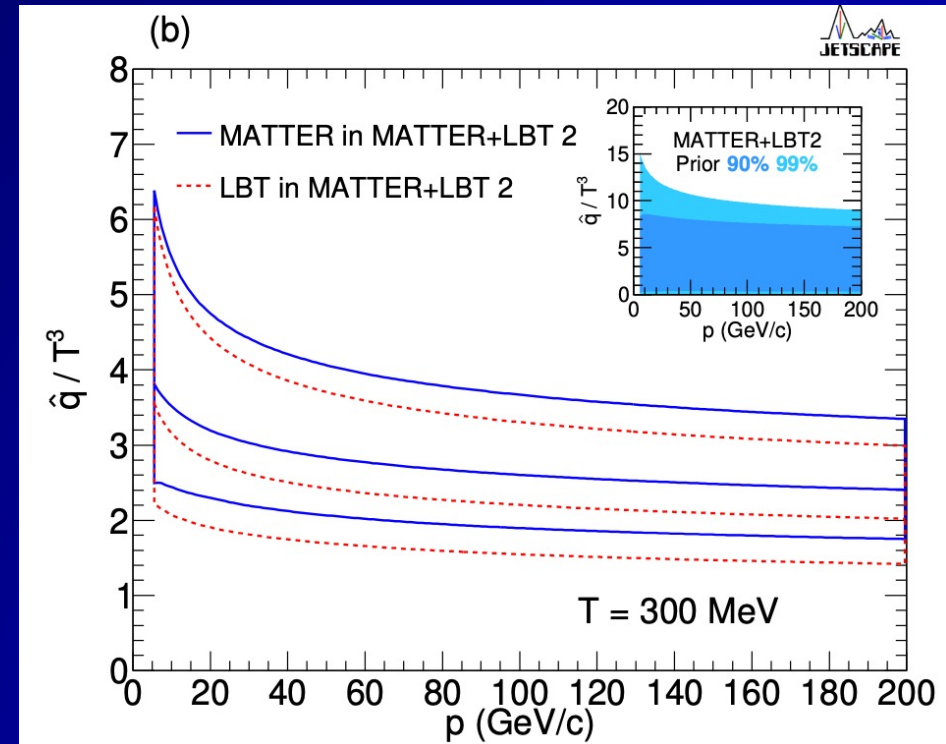
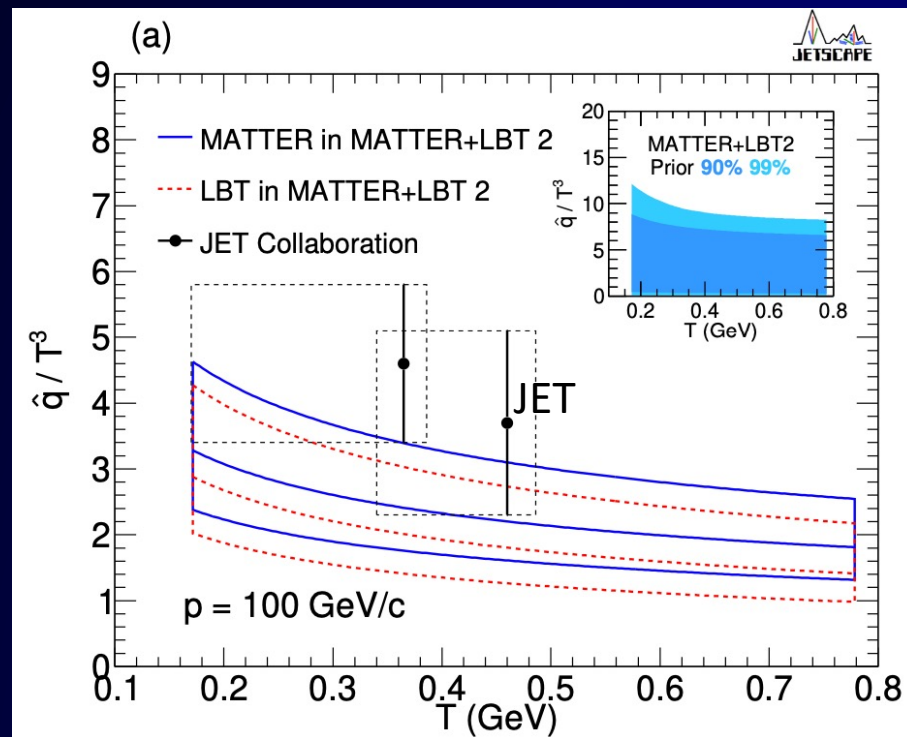
3D jet tomography

He, Pang & XNW, *PRL* 125 (2020) 12, 122301

Effect of flow: Sadofyev, Sievert & Vitev 2104.09513

Jet transport coefficient

JETSCAPE: Combine the evolving Monte Carlo simulators and fluid dynamic models
Statistical analysis package using advanced Bayesian techniques (MADA)



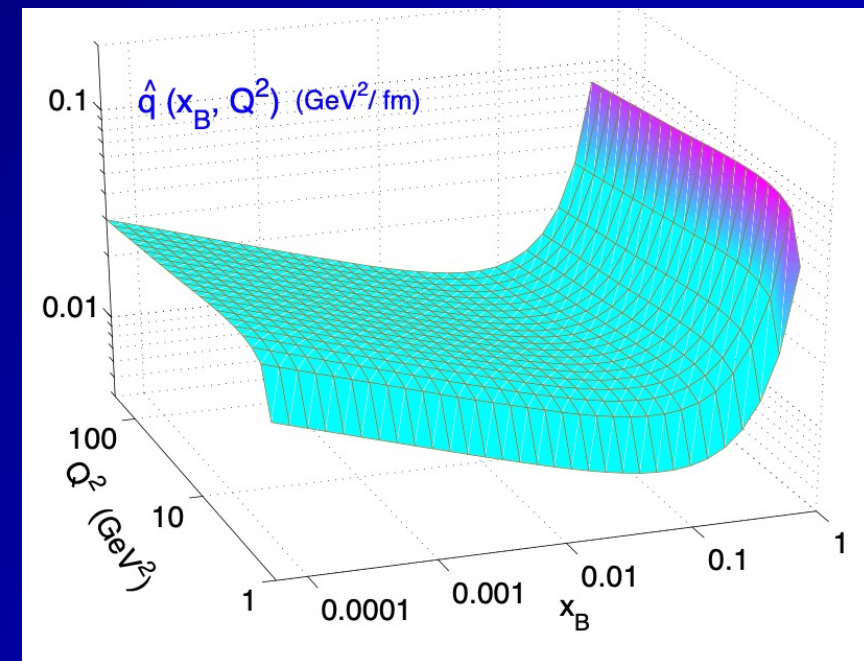
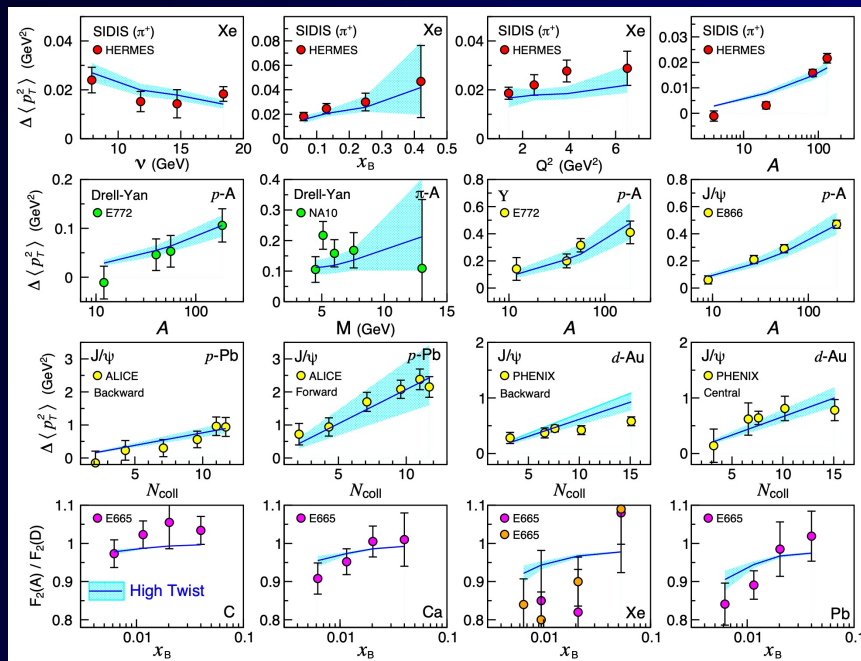
JET: *Phys. Rev. C* 90 (2014) 1, 014909

JETSCAPE: e-Print: [2102.11337](https://arxiv.org/abs/2102.11337)

Jet transport coefficient in nuclei

A global extraction of the jet transport coefficient in nuclei

$$\hat{q}_0 \approx 0.02 \text{ GeV}^2/\text{fm}$$



Data on: DIS, SIDIS(π), Drell-Yan, J/ψ (pA), Y (pA)

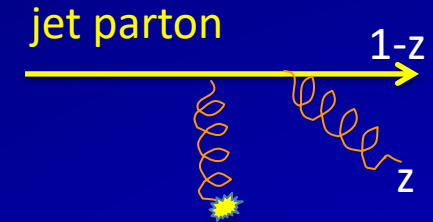
Ru, Kang, Wang, Xing & Zhang *PRD* 103 (2021) 3, L031901

Yuanyuan Zhang & XNW [2104.04520](#)

Suppression of leading hadrons

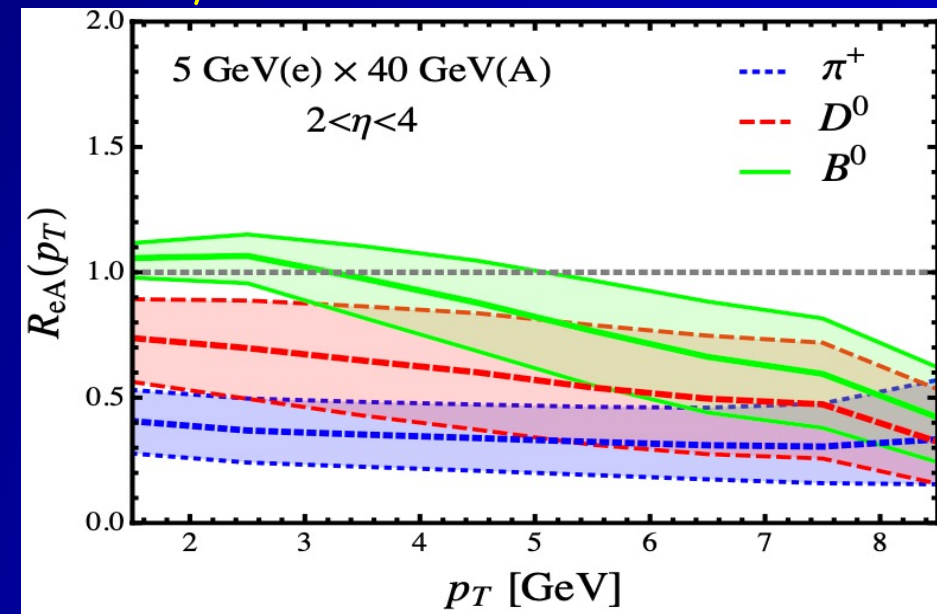
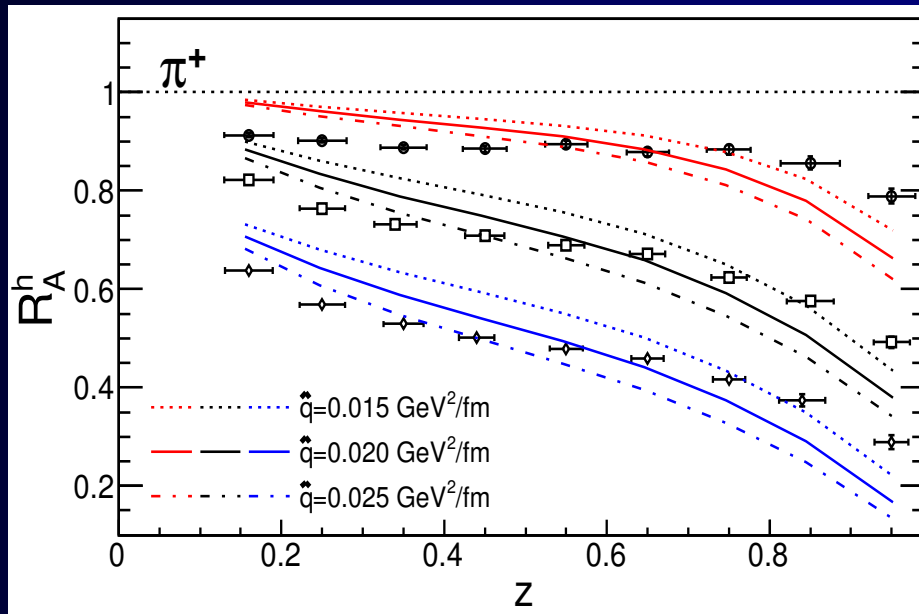
Medium induced splitting function (fractional energy loss distribution)

$$\Delta \tilde{P}_{a \rightarrow ag}(z) \approx \frac{2C_A \alpha_s}{\pi} \int dx \hat{q}(x) \int \frac{d\ell_{\perp}^2}{\ell_{\perp}^4} P(z) \sin^2 \frac{\ell_{\perp}^2 (x - x_0)}{4z(1-z)E}$$



Modified frag function & hadron spectra: $\tilde{D}_{c/h}(z_h) \approx [P_{a \rightarrow ag}(z) + \Delta \tilde{P}_{a \rightarrow ag}(z)] \otimes D_{a/h}(z_h)$

$$\hat{q}_0 \approx 0.02 \text{ GeV}^2/\text{fm}$$

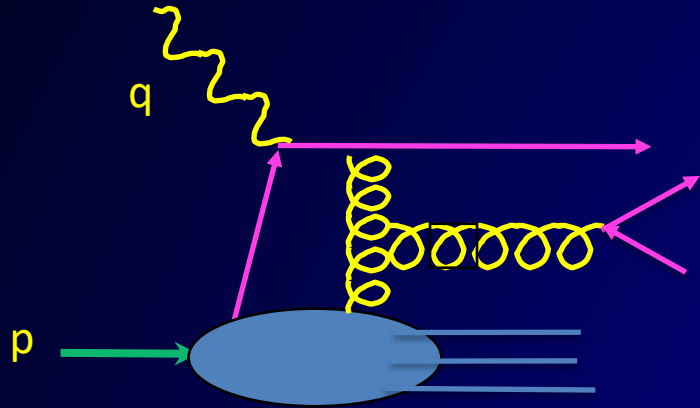


Chang, Deng & XNW *PRC* 89 (2014) 3, 034911

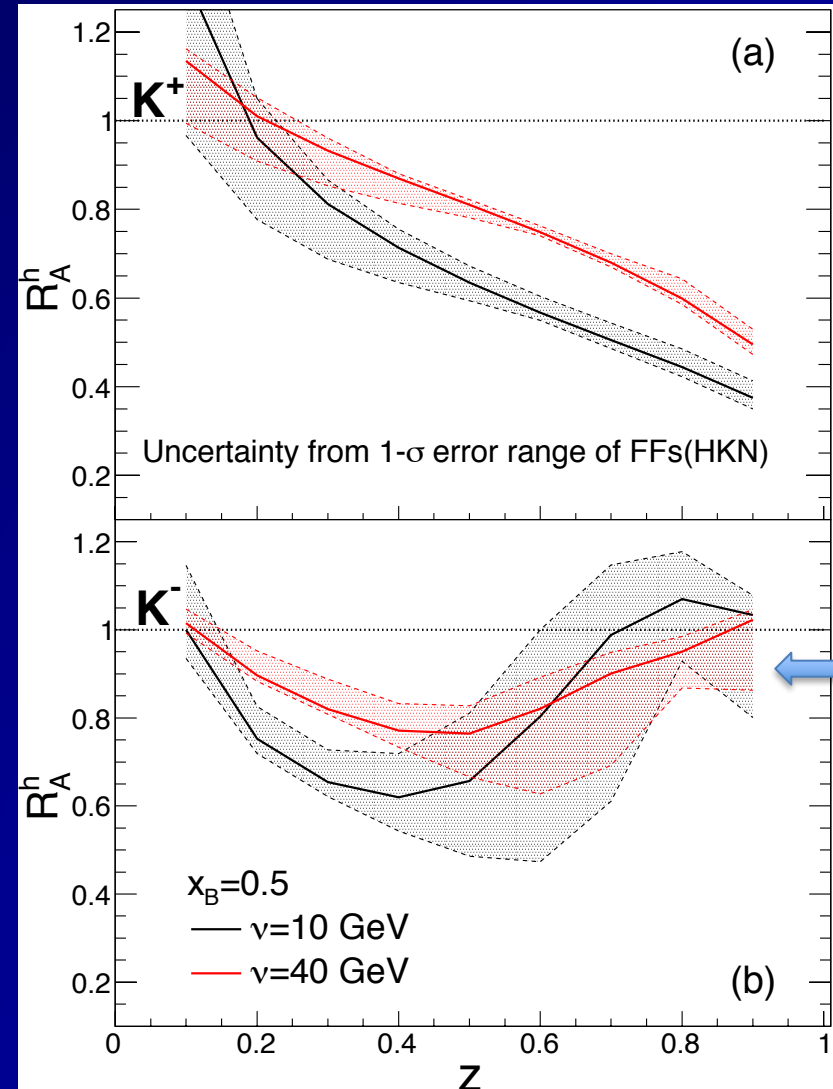
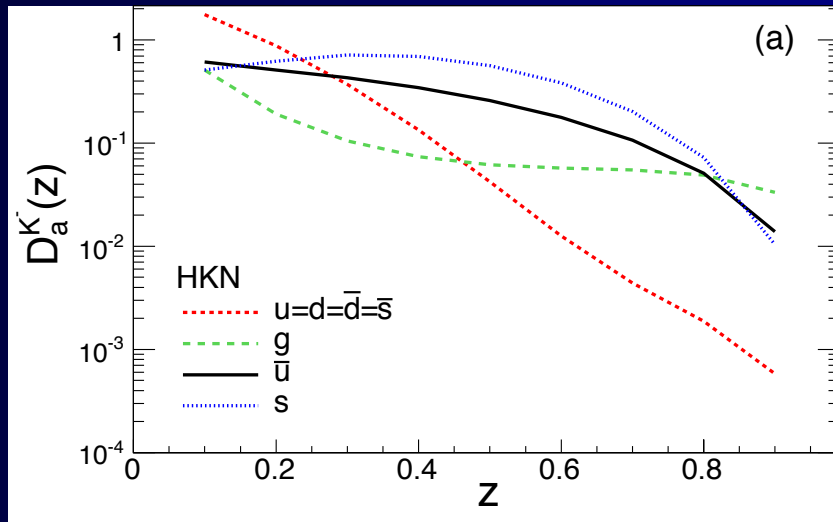
Li, Liu & Vitev, *PLB* 816 (2021) 136261



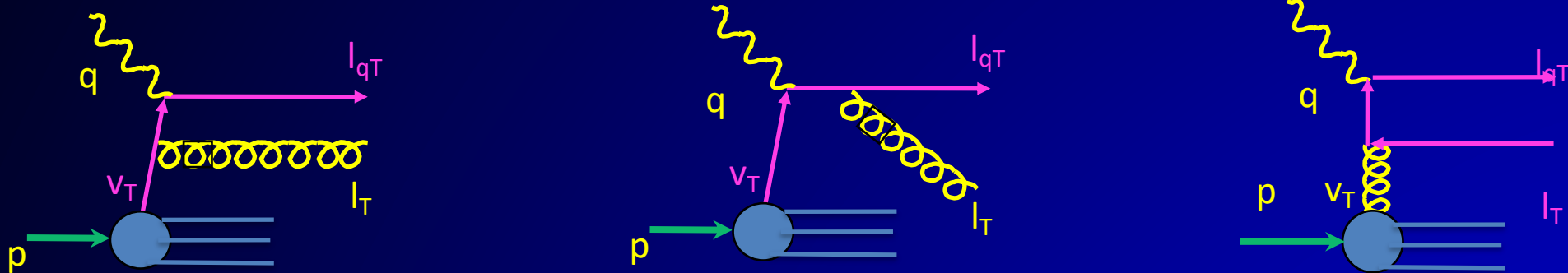
Flavor conversion in eA SIDIS



Chang, Deng & XNW, PRC 92 (2015) 5, 055207



Dijets production in DIS



TMD quark distribution: $f_q^A(x_B, \vec{v}_\perp)$

LO leading order contribution at large x_B

$$v_\perp = |\vec{l}_\perp + \vec{l}_{q\perp}|$$

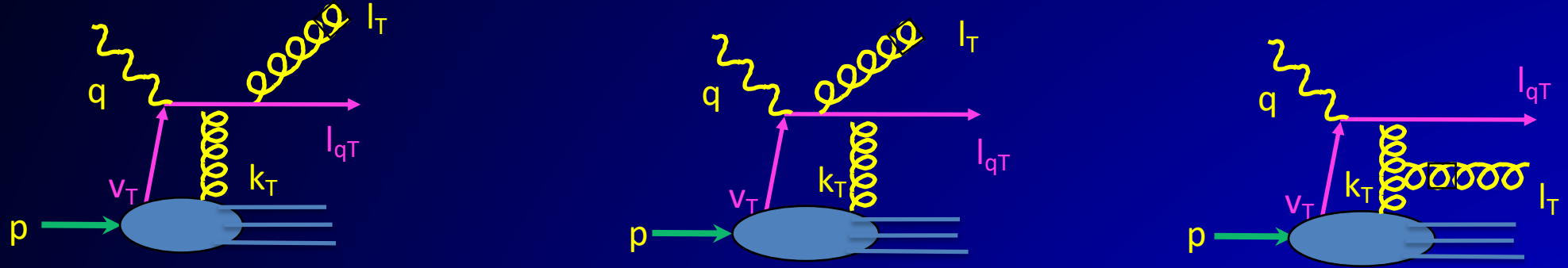
$$\downarrow$$

$$\sqrt{l_\perp^2 + l_{q\perp}^2 + 2l_\perp l_{q\perp} \cos \Delta\phi}$$

$$\frac{d\hat{\sigma}_S}{dx_B dQ^2 dz d^2l_\perp d^2l_{q\perp}} = \sigma_0 \frac{\alpha_s}{2\pi} \frac{1+z^2}{1-z} f_q^A(x_B, \vec{v}_\perp) \frac{C_F}{[\vec{l}_\perp - (1-z)(\vec{l}_\perp + \vec{l}_{q\perp})]^2}$$

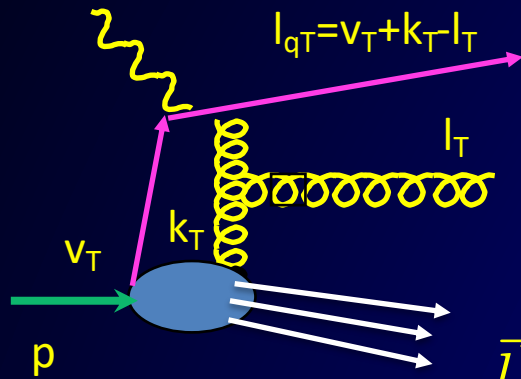
Angular correlation of dijets with fixed l_T and l_{qT}

Dijets from double scattering in EIC



$$\begin{aligned}
 \frac{d\hat{\sigma}_D}{dx_B dQ^2 dz d^2l_\perp d^2l_{q\perp}} &= \sigma_0 \frac{1+z^2}{1-z} \frac{\alpha_s^2}{N_c} \int dy_1^- \rho(y_1^-, \vec{y}_{N\perp}) d^2\vec{v}_\perp \frac{d^2\vec{k}_\perp}{(2\pi)^2} f_q^A(x_B, \vec{v}_\perp) \frac{\phi(0, \vec{k}_\perp)}{k_\perp^2} \\
 &\otimes \delta^2(\vec{l}_\perp + \vec{l}_{q\perp} - \vec{k}_\perp - \vec{v}_\perp) \left\{ C_F \mathcal{N}_{\text{coh}}(\vec{l}_\perp, \vec{l}_{q\perp}, \vec{k}_\perp, \vec{v}_\perp) \right. \\
 &+ \frac{1}{N_c} \mathcal{N}_{\text{qLPM}}(\vec{l}_\perp, \vec{l}_{q\perp}, \vec{k}_\perp, \vec{v}_\perp) \left(1 - \cos \frac{[\vec{l}_\perp - (1-z)\vec{v}_\perp]^2}{2p^+ q^- z(1-z)} p^+ y_1^- \right) \\
 &\left. + C_A \mathcal{N}_{\text{gLPM}}(\vec{l}_\perp, \vec{l}_{q\perp}, \vec{k}_\perp, \vec{v}_\perp) \left(1 - \cos \frac{[\vec{l}_\perp - (1-z)\vec{v}_\perp - \vec{k}_\perp]^2}{2p^+ q^- z(1-z)} p^+ y_1^- \right) \right\}
 \end{aligned}$$

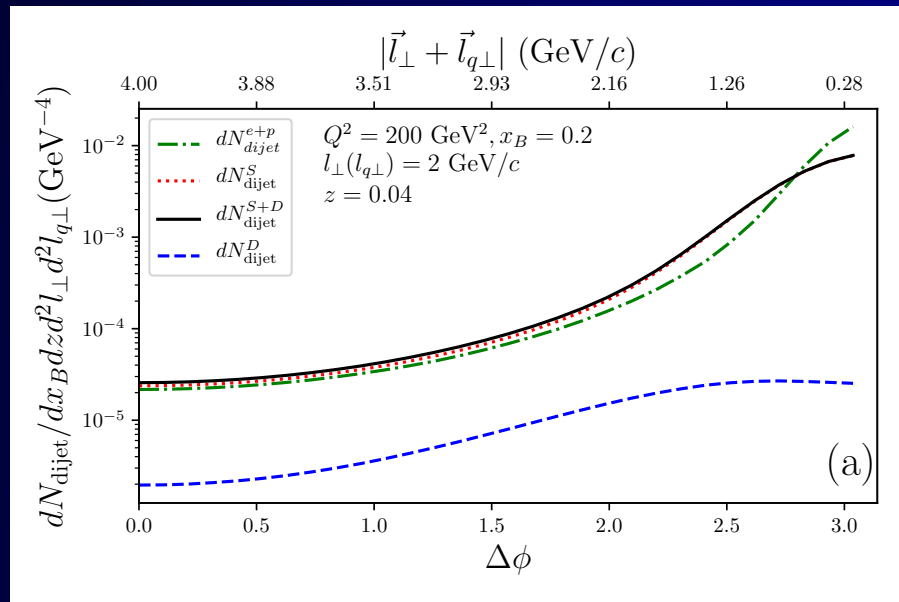
Nuclear modification of dijets & TMD pdf at EIC



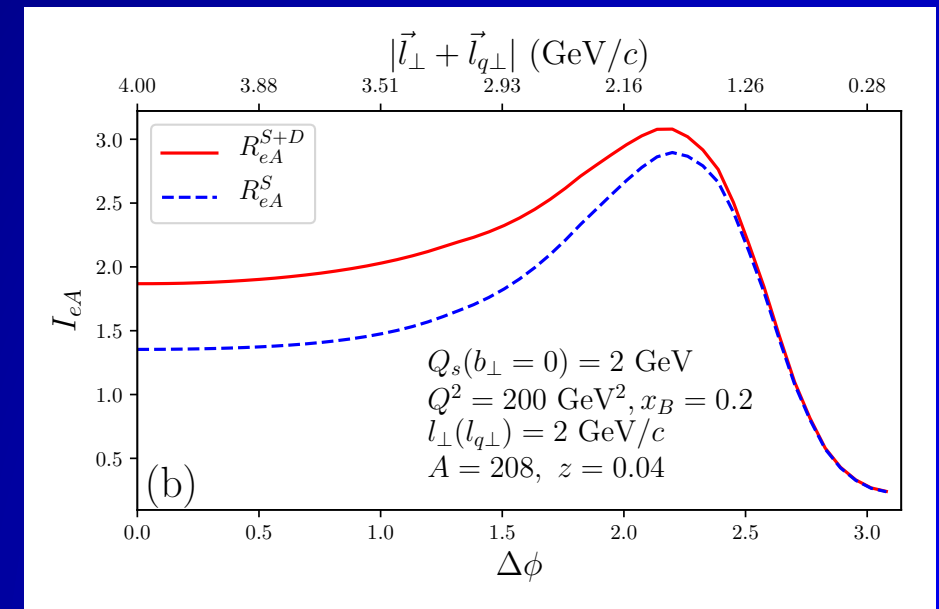
$$\frac{d\hat{\sigma}_D}{dx_B dQ^2 dz d^2l_\perp d^2l_{q\perp}} = \sigma_0 \frac{1+z^2}{1-z} \frac{\alpha_s^2}{N_c} \int dy_1^- \rho(y_1^-, \vec{y}_{N\perp})$$

$$\otimes \int d^2\vec{v}_\perp \int \frac{d^2\vec{k}_\perp}{(2\pi)^2} f_q^A(x_B, \vec{v}_\perp) \frac{\phi(0, \vec{k}_\perp)}{k_\perp^2} \mathcal{N}_g(\vec{l}_\perp, \vec{l}_{q\perp}, \vec{k}_\perp, \vec{v}_\perp)$$

$$\vec{l}_\perp + \vec{l}_{q\perp} = \vec{k}_\perp + \vec{v}_\perp$$



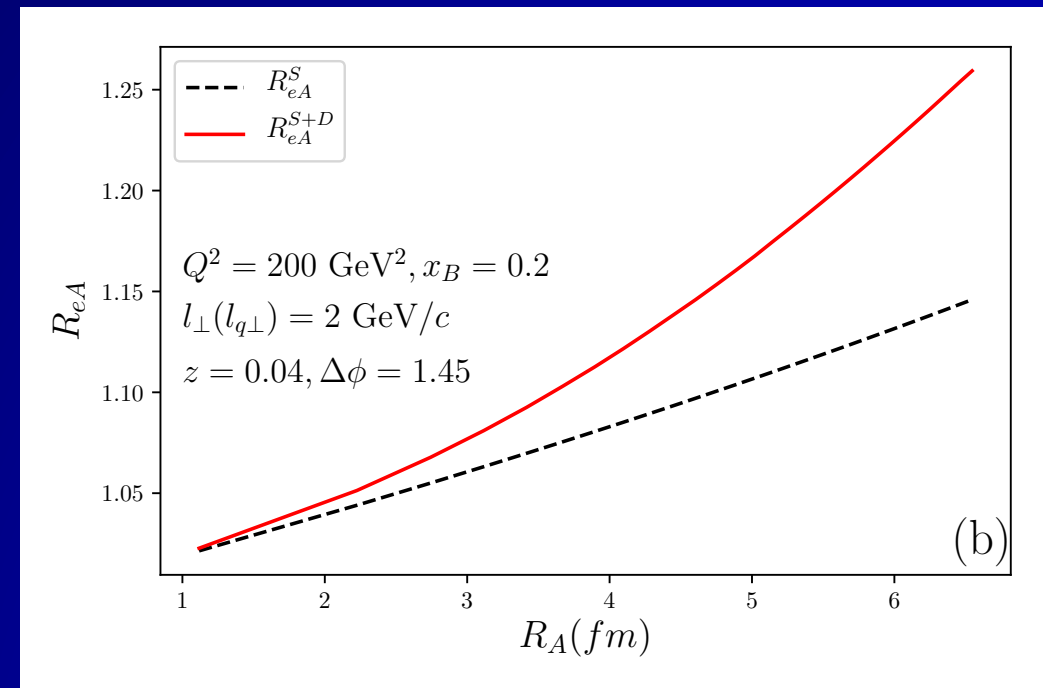
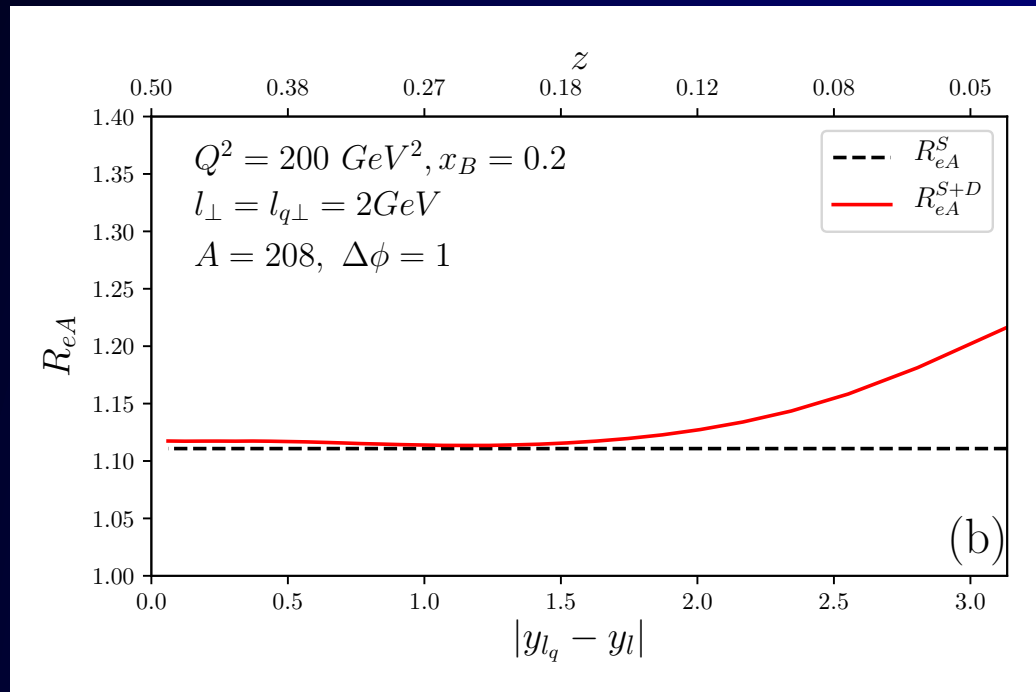
$$\Delta\sigma_{e+p}/A\sigma_{e+p}$$



LPM interference and rapidity & R_A dependence

Gluon splitting formation time:

$$\tau_f = \frac{2Ez(1-z)}{(\vec{l}_\perp - (1-z)\vec{v}_\perp - \vec{k}_\perp)^2}$$

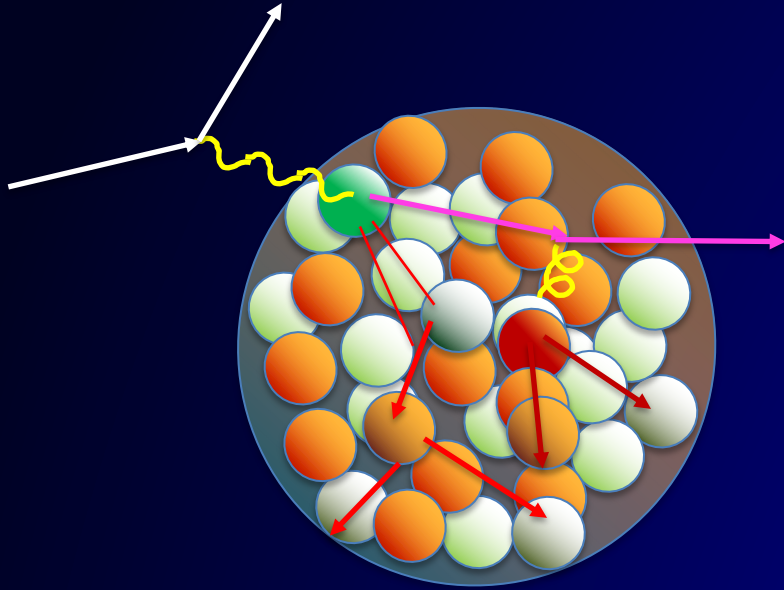


Dijet rapidity gap: $\Delta y = \log \frac{z}{1-z}$

Quadratic nuclear-size dependence due to LPM interference $\frac{\Delta\sigma_{e+A}}{A\sigma_{e+p}} \propto A^{2/3}$

Medium response in nuclei: grey particles

Grey particles: slow recoiling target nucleons due to multiple interaction inside the nucleus

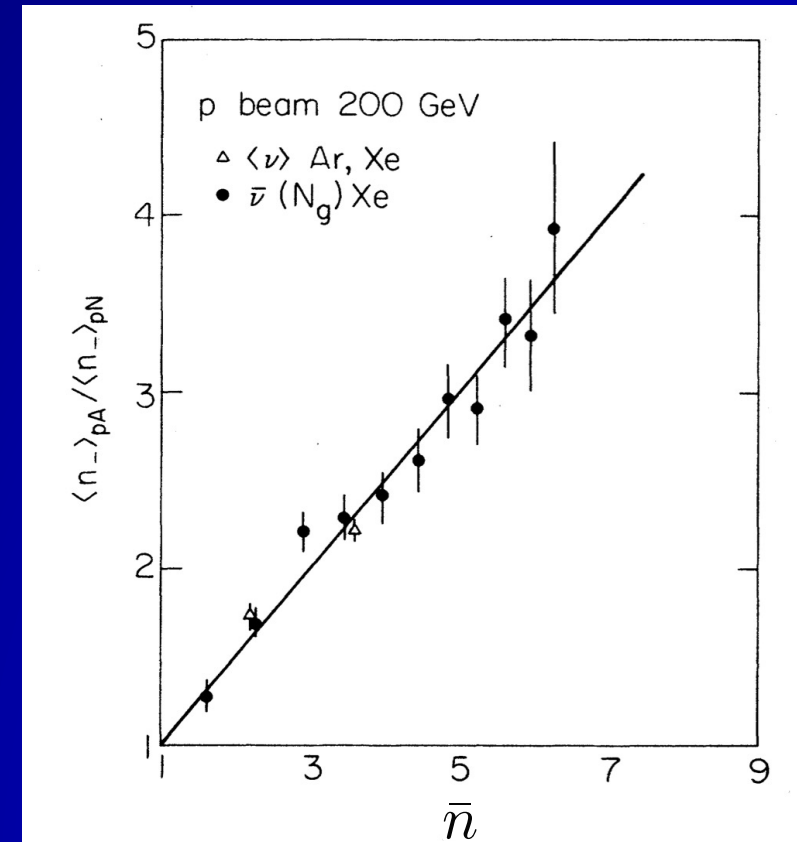


N_{grey} as a trigger for the number of scattering

$$\bar{n} \approx \frac{A\sigma_N}{\sigma_A} \left(\frac{N_{grey}}{\langle N_{grey} \rangle} \right)^{1/2}$$

$$P_n = \binom{N_{grey} + n - 1}{N_{grey}} X^{N_{grey}} (1 - X)^n$$

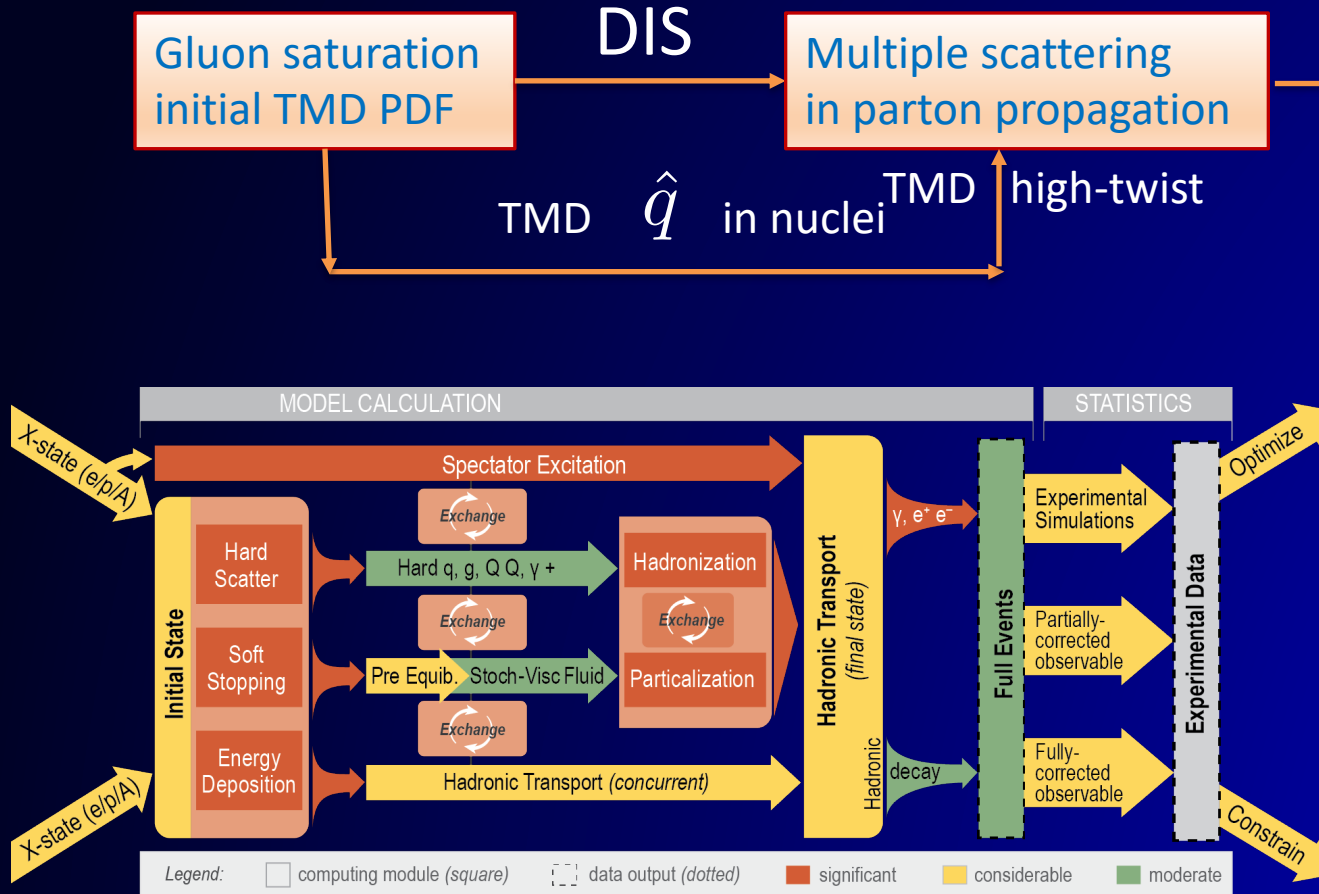
$$X = \frac{\langle N_{grey} \rangle}{\langle n \rangle + \langle N_{grey} \rangle} \quad \langle n \rangle = \frac{A\sigma_N}{\sigma_A}$$



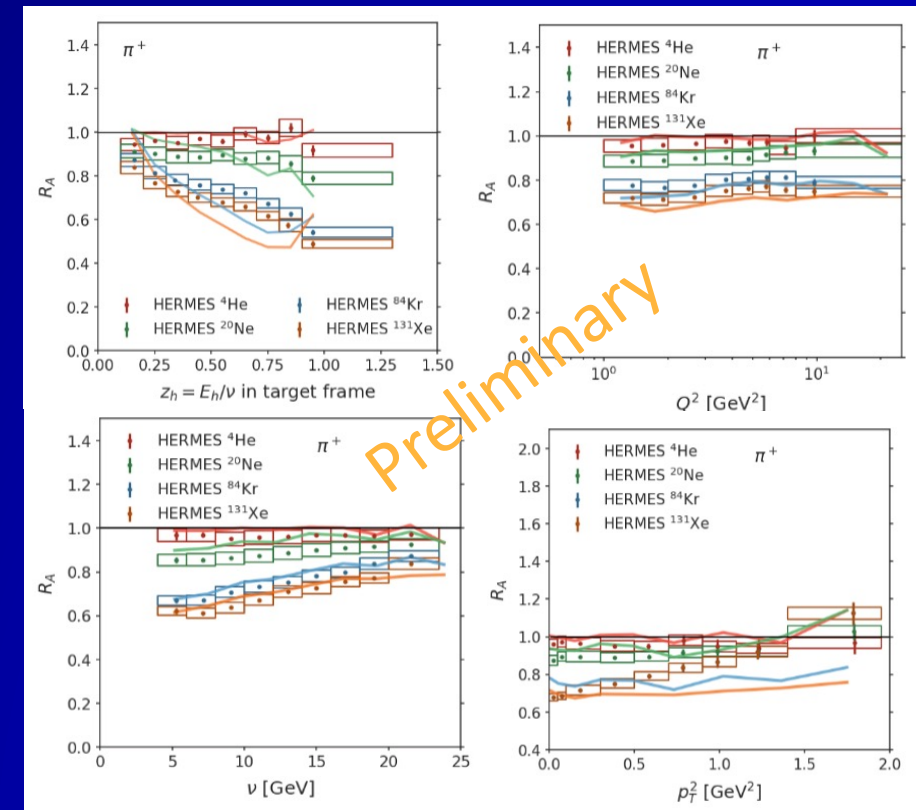
Hwa & XNW, PRD39, 2561 (1989)

e-HIJING (electron Heavy-Ion Jet INteraction Generator)

Weyao Ke (UCB/LBNL), Yayun He (SCNU), Hongxi Xing (SCNU) & XNW



XSCAPE



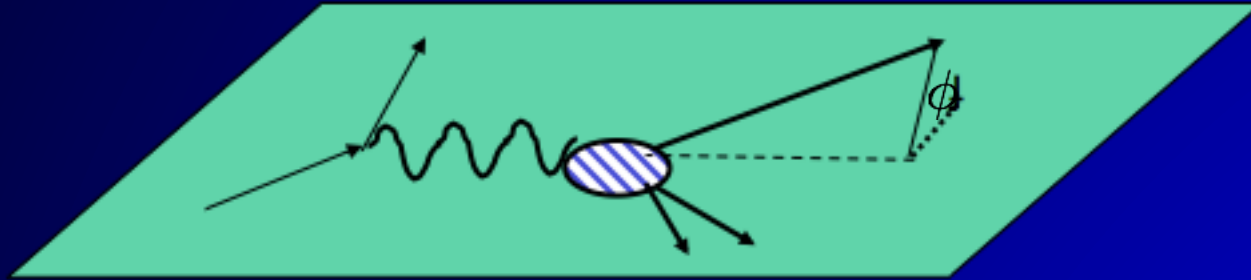
Summary

- Many similarities between jet transport in QGP and cold nuclei
- Generalized high-twist approach for both
 - Jet transport coefficient is related to gluon distribution density in medium
 - LPM effect in induced gluon bremsstrahlung
- Differences
 - $\hat{q} = 1\text{-}2 \text{ GeV}^2/\text{fm}$ vs $\hat{q}=0.02 \text{ GeV}^2/\text{fm}$ in large nuclei
 - Jet induced QGP response vs recoiling nucleons inside nuclei
- Jet medium interaction leads to flavor conversion in SIDIS
- Modification of dijets at EIC can provide information about TMD parton distributions in nuclei

Azimuthal Asymmetry

Gao, Liang & XNW (2010)

$$\langle \cos \phi \rangle_{eA} = \frac{2(2-y)\sqrt{1-y}}{1+(1-y)^2} \frac{k_T}{Q} \frac{x_B f_{A\perp}^q(x_B, k_T)}{f_A^q(x_B, k_T)} \quad k_T \ll Q$$



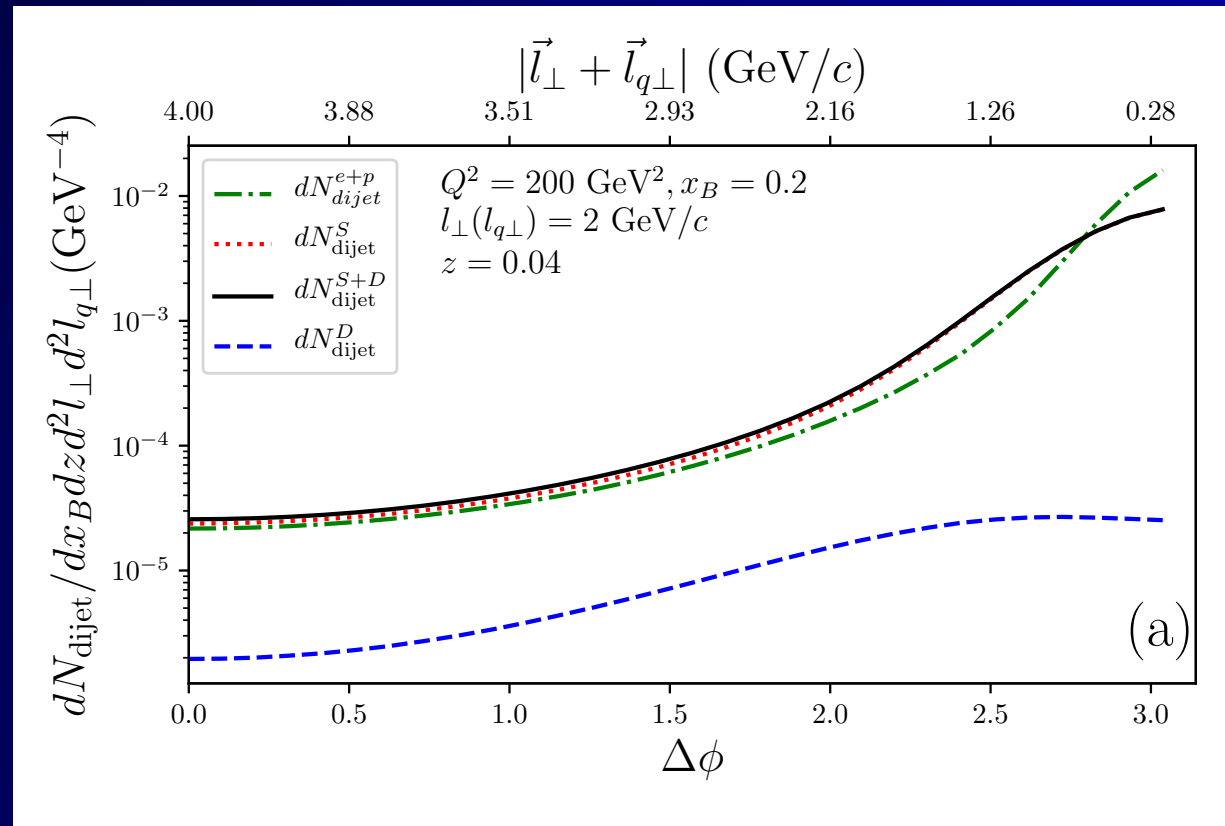
Twist-3 quark matrix elements

$$f_{A\perp}^q(x, k_T) = p^+ \int \frac{dy^-}{4\pi} \frac{d^2 y_\perp}{(2\pi)^2} e^{ixp^+ y^- - i\vec{k}_\perp \cdot \vec{y}_\perp} \langle A | \bar{\psi}(0) \frac{\gamma \cdot k_T}{k_T^2} \mathcal{L}(0, y) \psi(y) | A \rangle$$

$$\frac{\langle \cos \phi \rangle_{eA}}{\langle \cos \phi \rangle_{eN}} \approx \sqrt{\frac{\langle k_T^2 \rangle_N}{\langle k_T^2 \rangle_N + \Delta}}$$

LO dijet angular correlation

$$\frac{d\hat{\sigma}_S}{dx_B dQ^2 dz d^2l_\perp d^2l_{q\perp}} = \sigma_0 \frac{\alpha_s}{2\pi} \frac{1+z^2}{1-z} f_q^A(x_B, \vec{v}_\perp) \frac{C_F}{[\vec{l}_\perp - (1-z)(\vec{l}_\perp + \vec{l}_{q\perp})]^2}$$



Jet quenching in heavy-ion collisions

Multiple scattering

Transverse momentum broadening

Jet 1

Parton energy loss

Jet suppression

