Time-reversal odd side of a jet

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in collaboration with Xiaohui Liu, Hongxi Xing, and Manman Wang

based on

X. Liu and H. Xing, arXiv:2104.03328 [hep-ph], and work in progress

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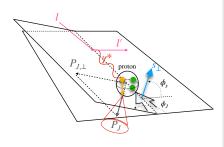
2nd PSQ@EIC Meeting

MOTIVATION

- 3D structure of proton were studied typically using
 - semi-inclusive hadron production
 [Mulders, Tangerman (1996), Brodsky, Hwang, Schmidt (2002),
 Bacchetta et al. (2007)]
 - jet production/hadron in jet
 [Kang, Metz, Qiu, Zhou (2011), Liu, Ringer, Vodelsang, Yuan (2019),
 Kang, Lee, Shao, Zhao (2021)]
- Jet was thought to be able to probe only a subset of TMD PDFs (4 out of 8 at leading twist).
- This work: Investigate possibility of probing all TMD PDFs with jet.

Inclusive jet production in DIS

Consider $l + p(P, S) \rightarrow l' + J(P_J) + X$

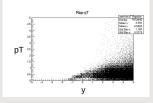


This is like SIDIS, but replace a hadron by a jet.

[Gutierrez-Reyes, Scimemi, Waalewijn, Zoppi (2018)]

Jets at EIC

• A lot of statistics at small p_T in the forward region.



- $\begin{array}{l} \bullet \quad \text{Focus on the region} \\ \Lambda_{\rm QCD} \sim |P_{J\perp}| \ll Q. \\ \text{This is unlike LHC, for which only} \\ \text{jets with } |P_{J\perp}| \gg \Lambda_{\rm QCD} \text{ are of} \\ \text{interest.} \end{array}$
- Still get jets if we use jet algorithms that involve energy (i.e. spherically-invariant jet algorithm [Cacciari, Salam, Soyez (2012)]) instead of k_T . Low p_T ($\sim \Lambda_{\rm QCD}$) and low Q^2 ($\sim 10-100~{\rm GeV}^2$) is not a problem.

FACTORIZATION

• Factorization from SCET: $\sigma = H \otimes \Phi \otimes \mathcal{J}$ H: hard function, Φ : TMD PDFs, \mathcal{J} : TMD jet functions (JFs)

$$\Phi^{ij}(x, p_T) = \int \frac{dy^- d^2 \mathbf{y}_T}{(2\pi)^3} e^{ip \cdot y} \langle P | \bar{\chi}_n^j(0) \chi_n^i(y) | P \rangle|_{y^+ = 0}$$

$$\mathcal{J}^{ij}(z, k_T) = \frac{1}{2z} \sum_X \int \frac{dy^- d^2 \mathbf{y}_T}{(2\pi)^3} e^{ik \cdot y} \langle 0 | \chi_{\bar{n}}^i(y) | JX \rangle \langle JX | \bar{\chi}_{\bar{n}}^j(0) | 0 \rangle|_{y^- = 0}$$

• TMD PDFs and TMD JFs encoded in azimuthal asymmetries:

$$\begin{split} \frac{d\sigma}{dxdydzd\psi d\phi_J dP_J^2} &= \frac{\alpha^2}{xyQ^2} \left\{ \left(1 - y + \frac{y^2}{2}\right) F_{UU,T} + (1 - y) \cos(2\phi_J) F_{UU}^{\cos(2\phi_J)} \right. \\ &\quad + S_{\parallel} (1 - y) \sin(2\phi_J) F_{UL}^{\sin(2\phi_J)} + S_{\parallel} \lambda_e y \left(1 - \frac{y}{2}\right) F_{LL} \\ &\quad + |S_{\perp}| \left[\left(1 - y + \frac{y^2}{2}\right) \sin(\phi_J - \phi_S) F_{UT,T}^{\sin(\phi_J - \phi_S)} + (1 - y) \sin(\phi_J + \phi_S) F_{UT}^{\sin(\phi_J + \phi_S)} \right. \\ &\quad + (1 - y) \sin(3\phi_J - \phi_S) F_{UT}^{\sin(3\phi_J - \phi_S)} \right] + |S_{\perp}| \lambda_e y \left(1 - \frac{y}{2}\right) \cos(\phi_J - \phi_S) F_{LT}^{\cos(\phi_J - \phi_S)} \end{split}$$

 ${\it F}$'s contain convolutions of TMD PDFs and TMD JFs.

F's: accessible by traditional jet function F's: inaccessible by traditional jet function

TMD PDFs at leading twist

$$\begin{split} \Phi &= \frac{1}{2} \left\{ f_1 \not\!\! n - f_{1T}^\perp \frac{\epsilon_{\alpha\beta} p_T^\alpha S_T^\beta}{M} \not\!\! n + \left(S_L g_{1L} - \frac{p_T \cdot S_T}{M} g_{1T} \right) \gamma_5 \not\!\! n \right. \\ &+ h_{1T} \frac{[S_T^\prime, \not\! n] \gamma_5}{2} + \left(S_L h_{1L}^\perp - \frac{p_T \cdot S_T}{M} h_{1T}^\perp \right) \frac{[p_T^\prime, \not\! n] \gamma_5}{2M} + i h_1^\perp \frac{[p_T^\prime, \not\! n]}{2M} \right\} \end{split}$$

quark hadron	unpolarized	chiral	transverse
U	f_1		h_1^\perp (Boer-Mulders)
L		g_{1L}	h_{1L}^{\perp}
T	f_{1T}^{\perp} (Sivers)	g_{1T}	h_{1T}, h_{1T}^{\perp} (transversity)

[Angeles-Martinez, Bacchetta, Balitsky, Boer, Boglione, Boussarie, Ceccopieri, Cherednikov, Connor et al. (2015)]

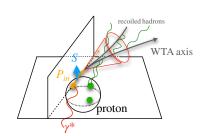
- ullet 8 TMD PDFs at leading twist, functions of x and p_T^2
- T-even: $f_1, g_{1L}, g_{1T}, h_{1T}, h_{1L}^{\perp}, h_{1T}^{\perp}$ T-odd: $f_{1T}^{\perp}, h_{1}^{\perp}$
- 3 functions f_1, g_{1L}, h_{1T} survive after p_T integration giving collinear PDF
- Accessible by traditional jet function: $f_1, g_{1L}, g_{1T}, f_{1T}^{\perp}$

T-ODD JET FUNCTION

- Traditionally, only jets with high p_T ($\gg \Lambda_{\rm QCD}$) were of interest. Production of high- p_T jets is perturbative. Since massless perturbative QCD is chiral-symmetric, only T-even jet functions appear.
- At low p_T ($\sim \Lambda_{QCD}$), the jet is sensitive to nonperturbative physics. In particular, spontaneous chiral symmetry breaking leads to a nonzero T-odd jet function when the jet axis is different from the direction of the fragmenting parton. (This is similar to Collins effect in fragmentation functions of hadrons [Collins (2002)].)

$$\mathcal{J}(z,k_T) = \mathcal{J}_1(z,k_T) \frac{\vec{n}}{2} + i \frac{\mathcal{J}_T(z,k_T)}{2} \frac{\vec{k}_T \vec{n}}{2}$$

- \mathcal{J}_1 : T-even, traditional jet function
- \mathcal{J}_T : T-odd, encodes correlations of quark transverse spin with quark transverse momentum (analogue of Collins function)



Advantages of T-odd jet function

• Universality
Like the T-even \mathcal{J}_1 , T-odd \mathcal{J}_T is process independent.

Flexibility

Flexibility of choosing jet recombination scheme and hence the jet axis

- ⇒ Adjust sensitivity to different nonperturbative contributions
- ⇒ Provide opportunity to "film" the QCD nonperturbative dynamics, if one continuously change the axis from one to another.
- High predictive power
 - Perturbative predictability. Since a jet contains many hadrons, the jet function has more perturbatively calculable degrees of freedom than the fragmentation function. For instance, in the WTA scheme, the z-dependence in the jet function is completely determined:

$$\mathcal{J}(z, k_T, R) = \delta(1 - z)\tilde{J}(k_T) + \mathcal{O}\left(\frac{k_T^2}{P_J^2 R^2}\right)$$

[Gutierrez-Reyes, Scimemi, Waalewijn, Zoppi (2018)]

• Nonperturbative predictability. Similar to the study in [Becher, Bell (2014)], \mathcal{J}_T can be factorized into a product of a perturbative coefficient and a nonperturbative factor. The nonperturbative factor has an operator definition [Vladimirov (2020)], and as a vacuum matrix element can be calculated on the lattice. This is unlike the TMD fragmentation function, which is an operator element of $|h+X\rangle$.

AZIMUTHAL ASYMMETRY

 $\sin(\phi_J + \phi_s)$ azimuthal asymmetry:

$$A(\zeta, y, \phi_s, \phi_J, P_{J\perp}) = 1 + \epsilon |S_{\perp}| \sin(\phi_J + \phi_s) \frac{F_{UT}}{F_{UU}}$$

- $F_{UT} \sim h_1 \otimes J_T$, probes transversity
- We simulate using Pythia 8.2+StringSpinner [Kerbizi, Loennblad (2021], with jet charge [Kang, Liu, Mantry, Shao (2020)] measured to enhance flavor separation (not mandatory), with EIC kinematics.
- Use the spherically-invariant jet algorithm [Cacciari, Salam, Soyez (2012)]

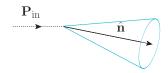
$$d_{ij} = min(E_i^{-2}, E_j^{-2}) \frac{1 - \cos \theta_{ij}}{1 - \cos R}, \quad d_{iB} = E_i^{-2}$$

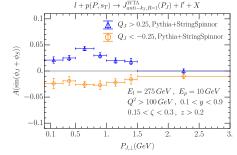
(Conventional anti- k_T algorithms using k_T instead of E not good for low p_T jets)

Change the jet axis from one to another (WTA \rightarrow E-scheme), "film" nonperturbative physics.

WTA scheme:

$$\hat{m{n}}_r = \left\{ egin{array}{ll} \hat{m{n}}_1 \,, & ext{if } E_1 > E_2 \ \hat{m{n}}_2 \,, & ext{if } E_2 > E_1 \end{array}
ight.$$





AZIMUTHAL ASYMMETRY

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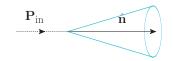
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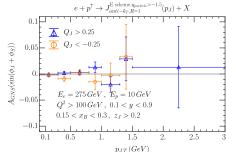
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E-scheme:

$$k_r = k_1 + k_2$$

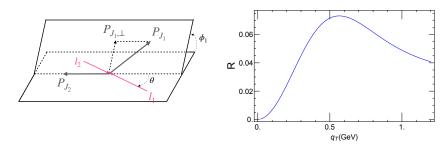




e^+e^- ANNIHILATION

We demonstrate prediction on azimuthal asymmetry in e^+e^- annihilation at $\sqrt{s}=\sqrt{110}$ GeV, with WTA scheme and parametrized nonperturbative Sudakov for $J_T\colon$

$$R^{J_1 J_2} = 1 + \cos(2\phi_1) \frac{\sin^2 \theta}{1 + \cos^2 \theta} \frac{F_T(q_T)}{F_U(q_T)}$$
$$R = 2 \int d\cos \theta \, \frac{d\phi_1}{\pi} \cos(2\phi_1) R^{J_1 J_2}$$

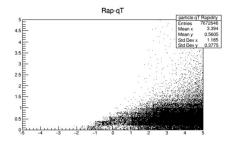


SUMARY AND OUTLOOK

- We introduce the T-odd jet function, which is relevant for low p_T jets, i.e. jets at EIC.
- Using T-odd jet function, together with the traditional T-even one, we can probe all 8 TMD PDFs at leading twist using jets.
- T-odd jet function has the advantages of universality, flexibility, and high predictive power.
- T-odd jet functions provide new input to the global analysis of nonperturbative proton structure.

Thank you.

Backup slides



AZIMUTHAL ASYMMETRY AT LEADING TWIST

Couplings of Φ and $\mathcal J$ encoded in angular distribution:

$$\frac{d\sigma}{dxdydzd\psi d\phi_{J}dP_{J}^{2}} = \frac{\alpha^{2}}{xyQ^{2}} \left\{ \left(1 - y + \frac{y^{2}}{2} \right) F_{UU,T} + (1 - y)\cos(2\phi_{J}) F_{UU}^{\cos(2\phi_{J})} + S_{\parallel}(1 - y)\sin(2\phi_{J}) F_{UL}^{\sin(2\phi_{J})} + S_{\parallel}\lambda_{e}y \left(1 - \frac{y}{2} \right) F_{LL} + |S_{\perp}| \left[\left(1 - y + \frac{y^{2}}{2} \right) \sin(\phi_{J} - \phi_{S}) F_{UT,T}^{\sin(\phi_{J} - \phi_{S})} + (1 - y)\sin(\phi_{J} + \phi_{S}) F_{UT}^{\sin(\phi_{J} + \phi_{S})} + (1 - y)\sin(3\phi_{J} - \phi_{S}) F_{UT}^{\sin(3\phi_{J} - \phi_{S})} \right] + |S_{\perp}|\lambda_{e}y \left(1 - \frac{y}{2} \right) \cos(\phi_{J} - \phi_{S}) F_{LT}^{\cos(\phi_{J} - \phi_{S})}$$

- $F_{UU,T}, F_{LL}, F_{UT,T}^{\sin(\phi_J \phi_S)}, F_{LT}^{\cos(\phi_J \phi_S)}$: contain T-even parts of Φ and $\mathcal J$
- $F_{UU}^{\cos(2\phi_J)}, F_{UL}^{\sin(2\phi_J)}, F_{UT}^{\sin(\phi_J+\phi_S)}, F_{UT}^{\sin(3\phi_J-\phi_S)}$: contain T-odd parts of Φ and $\mathcal J$

The F's are convolutions of TMD PDFs and jet functions:

$$\mathcal{C}[wfJ] \equiv x \sum e_q^2 \int d^2 \boldsymbol{p}_T \int d^2 \boldsymbol{k}_T \delta^{(2)} \left(\boldsymbol{p}_T + \boldsymbol{q}_T - \boldsymbol{k}_T\right) w(\boldsymbol{p}_T, \boldsymbol{k}_T) f(x, p_T^2) J(z, \boldsymbol{k}_T^2)$$

$$\begin{split} F_{UU,T} &= \mathcal{C}[f_1 \mathcal{J}_1] \,, \quad F_{LL} = \mathcal{C}[g_{1L} \mathcal{J}_1] \\ F_{UT,T}^{\sin(\phi_J - \phi_S)} &= \mathcal{C}\left[-\frac{\hat{\boldsymbol{h}} \cdot \boldsymbol{p}_T}{M} f_{1\perp}^{\perp} \mathcal{J}_1\right] \,, \quad F_{UT,T}^{\cos(\phi_J - \phi_S)} = \mathcal{C}\left[\frac{\hat{\boldsymbol{h}} \cdot \boldsymbol{p}_T}{M} g_{1T} \mathcal{J}_1\right] \,, \\ F_{UU}^{\cos(2\phi_J)} &= \mathcal{C}\left[-\frac{(2(\hat{\boldsymbol{h}} \cdot \boldsymbol{k}_T)(\hat{\boldsymbol{h}} \cdot \boldsymbol{p}_T) - \boldsymbol{k}_T \cdot \boldsymbol{p}_T)}{M} h_1^{\perp} \mathcal{J}_T\right] \\ F_{UL}^{\sin(2\phi_J)} &= \mathcal{C}\left[-\frac{(2(\hat{\boldsymbol{h}} \cdot \boldsymbol{k}_T)(\hat{\boldsymbol{h}} \cdot \boldsymbol{p}_T) - \boldsymbol{k}_T \cdot \boldsymbol{p}_T)}{M} h_{1L}^{\perp} \mathcal{J}_T\right] \\ F_{UT}^{\sin(\phi_J + \phi_S)} &= \mathcal{C}\left[-\hat{\boldsymbol{h}} \cdot \boldsymbol{k}_T h_1 \mathcal{J}_T\right] \\ F_{UT}^{\sin(3\phi_J - \phi_S)} &= \mathcal{C}\left[\frac{2(\hat{\boldsymbol{h}} \cdot \boldsymbol{p}_T)(\boldsymbol{p}_T \cdot \boldsymbol{k}_T) + \boldsymbol{p}_T^2(\hat{\boldsymbol{h}} \cdot \boldsymbol{k}_T) - 4(\hat{\boldsymbol{h}} \cdot \boldsymbol{p}_T)^2(\hat{\boldsymbol{h}} \cdot \boldsymbol{k}_T)}{2M^2} h_{1T}^{\perp} \mathcal{J}_T\right] \end{split}$$

where $\hat{m h} \equiv m P_{J\perp}/|m P_{J\perp}|$ and $h_1 \equiv h_{1T} + rac{m p_T^2}{2M^2}h_{1T}^\perp$