

Probing gluonic structure in diffractive J/ψ production

Mark Strikman, PSU



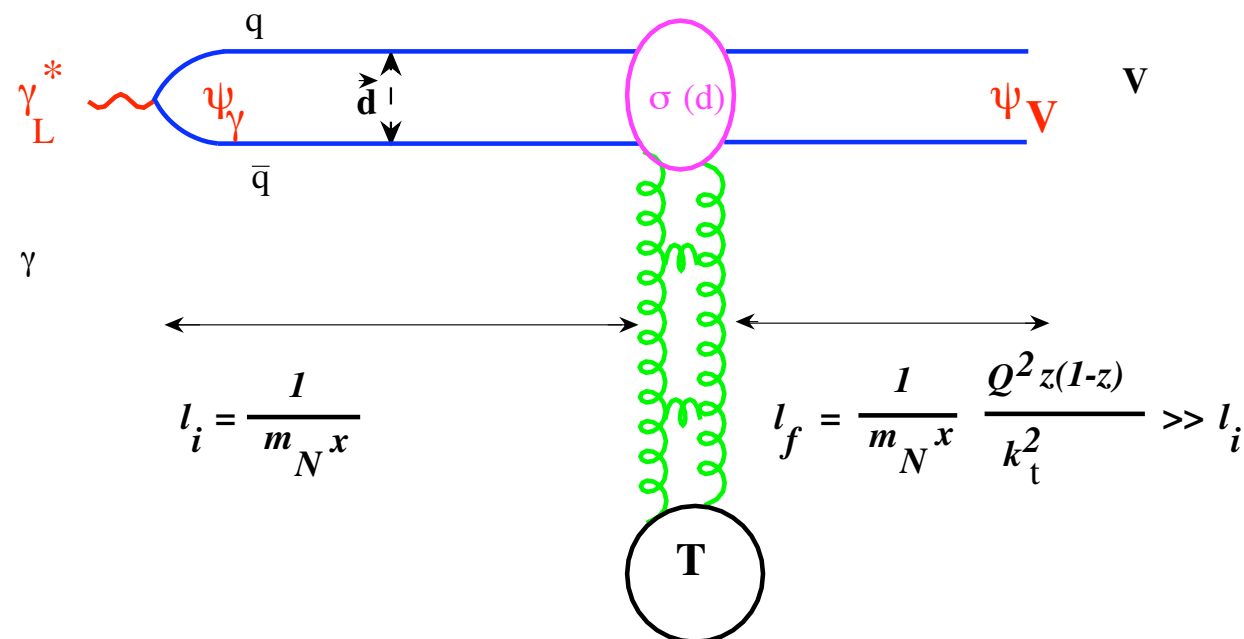
Workshop “Physics Opportunities with Heavy
Quarkonia at the EIC” October 26, 2021

Outline

- ❖ Exclusive VM production in DIS- lessons from HERA
- ❖ Theory of the Leading twist shadowing
- ❖ Coherent J/ψ production off heavy and light nuclei
- ❖ Remarks on incoherent diffraction

Vector meson diffractive production: Theory and HERA data

Space-time picture of Vector meson production at small x in the target rest frame



\Rightarrow Similar to the $\pi + T \rightarrow 2jets + T$ process, $A(\gamma_L^* + p \rightarrow V + p)$ at $p_t = 0$ is a convolution of the light-cone wave function of the photon $\Psi_{\gamma^* \rightarrow |q\bar{q}\rangle}$, the amplitude of elastic $q\bar{q}$ - target scattering, $A(q\bar{q}T)$, and the wave function of vector meson, ψ_V : $A = \int d^2d \psi_{\gamma^*}^L(z, d) \sigma(d, s) \psi_V^{q\bar{q}}(z, d)$.

The leading twist parameter free answer is *BFGMS94*

$$\left. \frac{d\sigma_{\gamma^* N \rightarrow V N}^L}{dt} \right|_{t=0} = \frac{12\pi^3 \Gamma_{V \rightarrow e^+ e^-} M_V \alpha_s^2(Q) \eta_V^2 \left| \left(1 + i \frac{\pi}{2} \frac{d}{d \ln x}\right) x G_T(x, Q^2) \right|^2}{\alpha_{EM} Q^6 N_c^2}$$

. Here, $\Gamma_{V \rightarrow e^+ e^-}$ is the decay width of $V \rightarrow e^+ e^-$;

$$\eta_V \equiv \frac{1 \int \frac{dz d^2 k_t}{z(1-z)} \Phi_V(z, k_t)}{2 \int dz d^2 k_t \Phi_V(z, k_t)} \rightarrow 3 \quad |_{Q^2 \rightarrow \infty}$$

Note: In the leading twist $d=0$ in $\psi_V(z, d)$. Finite b effects in the meson wave function is one of the major sources of the higher twist effects.

$$\begin{array}{ccc} \text{energy denominator} & \frac{1}{Q^2 + \frac{m^2 + k_t^2}{z(1-z)}} & \xrightarrow{\text{operator of interaction}} \left(\frac{1}{Q^2 + \frac{m^2 + k_t^2}{z(1-z)}} \right)^4 \\ & & \text{m- quark mass} \\ & \xrightarrow{\quad} \frac{Q^2}{(\mu^2 + Q^2)^4} \rightarrow \frac{1}{Q^6} \\ & \mu^2 \geq m_V^2 & \end{array}$$

A QCD dipole model of J/ψ production - aims to account more accurately for geometry

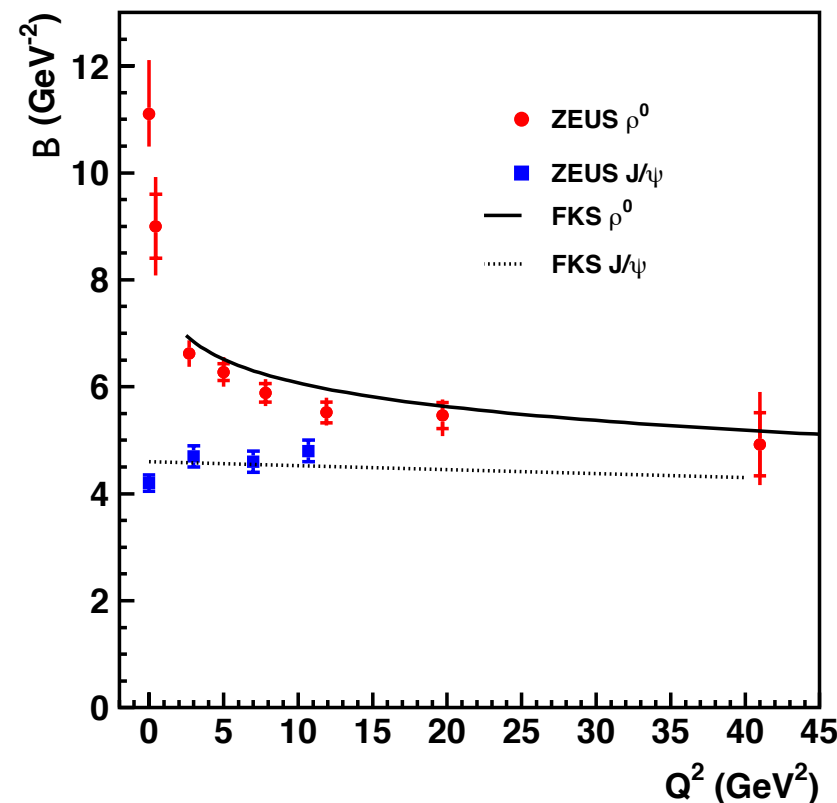
$$A(\gamma + p \rightarrow J/\psi + p) = \int d^2 d \psi_{\gamma \rightarrow c\bar{c}}(z, d) \sigma_{tot}(c\bar{c}, p) \psi_{J/\psi}(z, d)$$

Slow onset of the LT for cross section both for light and heavy mesons

Slow squeezing of dipole size for light mesons, but early dominance of small dipoles for J/ψ

Universal t-slope: process is dominated by the scattering of quark-antiquark pair in a small size configuration - t-dependence is predominantly due to the transverse spread of the gluons in the nucleon - two gluon nucleon form factor/diagonal gluon GPD $F_g(x,t)$. $d\sigma/dt \propto F_g^2(x,t)$. Onset of universal regime FKS[Frankfurt,Koepf, MS,97] **early for J/ψ late for ρ**

$$r_T \propto \frac{1}{Q} \left(\frac{1}{m_c} \right) \ll r_N$$



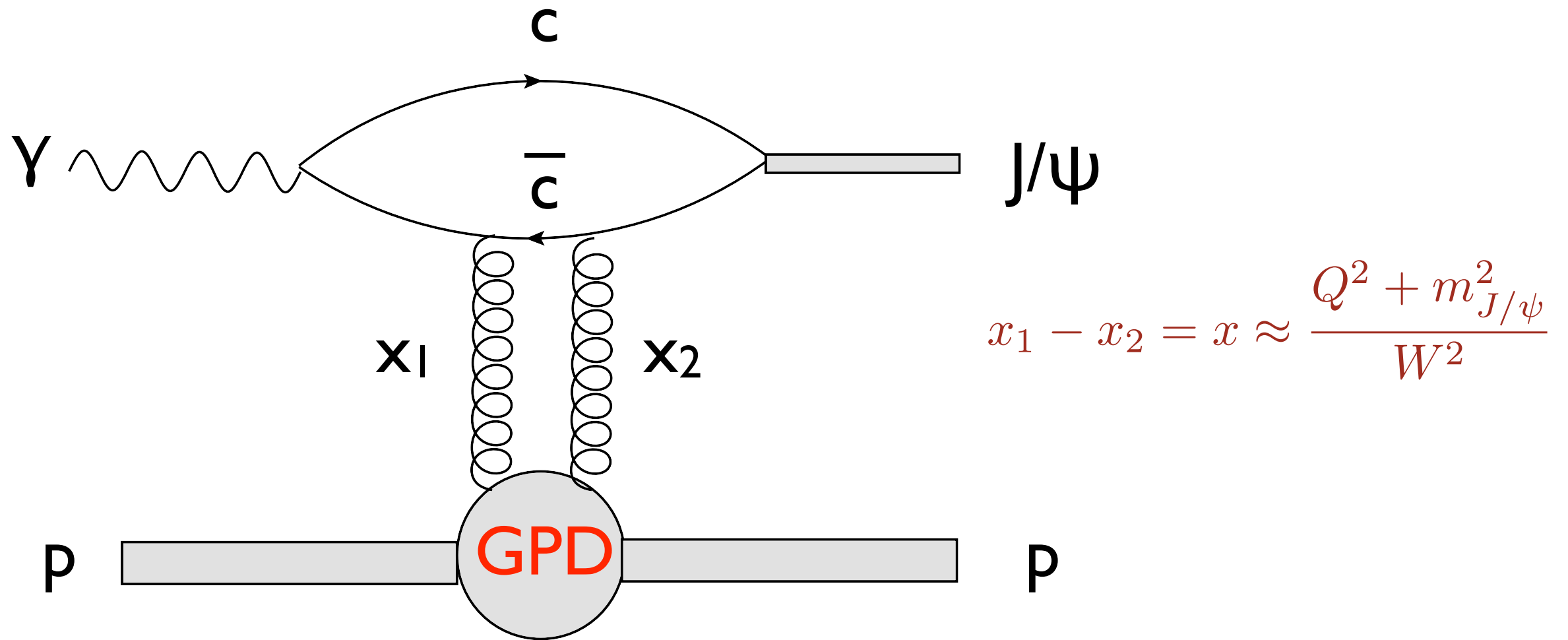
Convergence of the t-slopes, B - $\frac{d\sigma}{dt} = A \exp(Bt)$ of ρ -meson electroproduction to the slope of J/ψ photo(electro)production.

⇒ Transverse distribution of gluons (GPD) can be extracted from $\gamma + p \rightarrow J/\psi + N$

Correction for finite J/ψ size is ~ 10%.

Reminder: transverse spread of gluons enters into description of jet production in pp collisions at the LHC energies

Cavitate: experimentally one can measure only nondiagonal GPD



Analysis of the overlapping integral including Fermi motion of quarks in J/ψ (Koepp et al)

$$x_1/x_2 \sim 2 \div 3$$

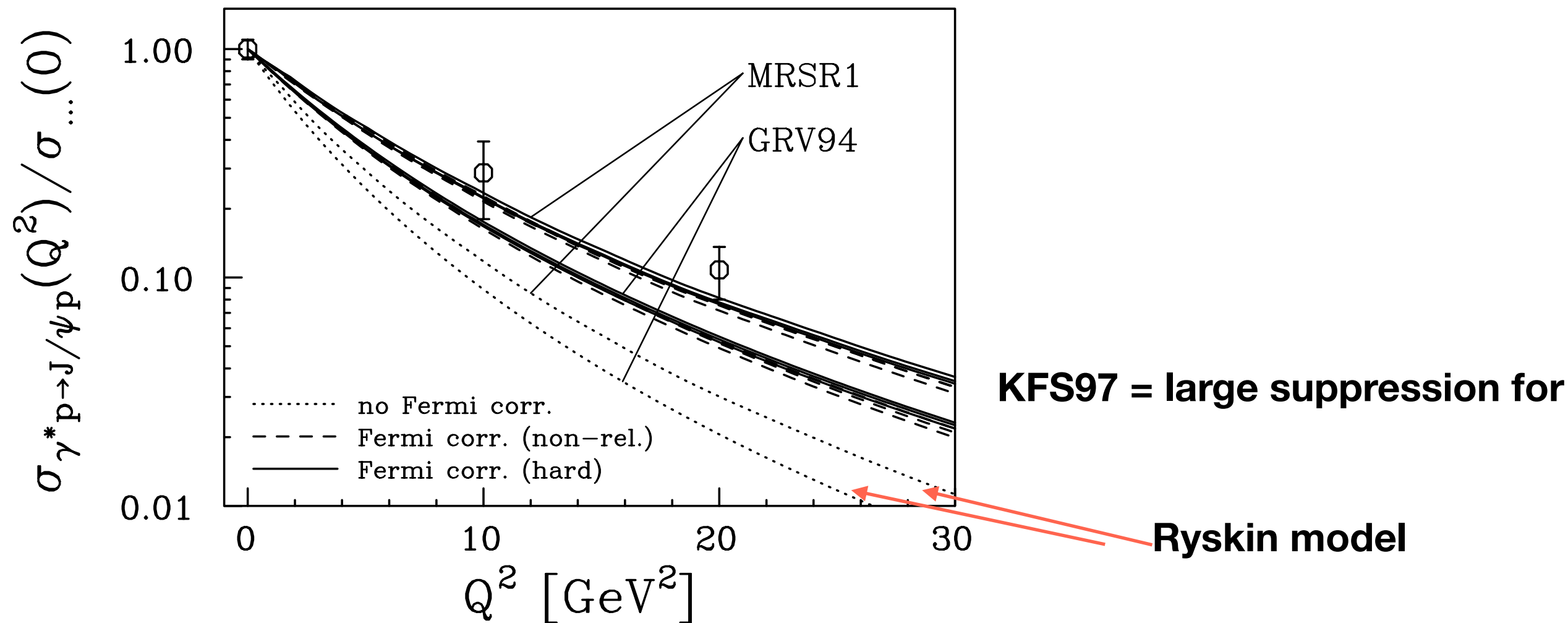
$$x_{eff} = (x_1 + x_2)/2 \sim x$$

In many models Fermi motion is neglected and x_2 is assumed to be 0.

Open questions in exclusive J/psi production

a) How safe it is to neglect Fermi motion of quarks

- Confirmation of the presence of the Fermi suppression factor $T(Q^2)$ in Q^2 dependence of J/ψ production:



b) Relation between NR and LC wave functions LC wave function of quarkonium

Normalization of light cone wave function through f_V does not contain, α_S (Brodsky & Lepage), while in nonrelativistic model there is a Barbiery factor

$$1 - 16\alpha_s/3\pi \sim 0.5$$

suggests presence of large $c\bar{c}g$ component in charmonia

c) what is the value of m_c and how it evolves with resolution?

Charmonium models: $m_c > m_{J/\psi}/2$; pQCD $< m_{J/\psi}/2$



These processes cannot be used so far for extraction of the absolute value of gluon density. However since J/ψ is a compact probe, ratios for different targets are mostly unaffected.

Hard diffraction - J/ψ meson production

- **exclusive production: $\gamma + p (A) \rightarrow J/\psi + p (A)$**

Issues: gluon pdfs and gpd's, gluon shadowing

most popular now (will focus on this process)

- **quasielastic $\gamma + p (A) \rightarrow J/\psi + Y$ at $t=0$**

Issues: color fluctuations in nucleons and nuclei; gluon shadowing

- **$\gamma + p (A) \rightarrow J/\psi$ (large t) + rapidity gap + Y**

Issues: BFKL at $-t > 1 \text{ GeV}^2$

- **$\gamma + p (A) \rightarrow J/\psi(x_F < 0.8) + X$**

for p -- neutrons in proton fragmentation region, ZDC signal for A decay

exclusive production: $\gamma (\gamma^*) + A \rightarrow J/\psi + A$

In the leading twist (LT) approximation for $t=0$

$$\left. \frac{\sigma (\gamma + A \rightarrow J/\psi + A)}{\sigma (\gamma + p \rightarrow J/\psi + p)} \right|_{t=0} = [g_A(x, \mu^2)/g_p(x, \mu^2)]^2$$

**EIC: detailed studies using
a range of nuclei, $x \geq 0.5 \cdot 10^{-3}$**

**LHC: ultraperipheral heavy ion collisions
using Pb nuclei, So far the best
measurements are for $x > 0.5 \cdot 10^{-3}$.
In the future $x \sim 10^{-5}$ can be probed.**

Run 3: $y=0 \rightarrow x = 0.5 \cdot 10^{-3}$

Basic guiding features of QCD relevant for diffraction in QCD

- a) cross section of a small dipole off a proton/ nucleus interaction is small, proportional to area of dipole occupied by color, and to gluon density of target and hence grows with decrease of x .

$$\sigma(q\bar{q}T) = \frac{\pi^2}{3} r_{tr}^2 x g_T(x, Q^2 = \lambda/r_t^2) \alpha_s(Q^2)$$

—> factorization theorem for exclusive meson production (Collins, Frankfurt and MS 1997)

- b) Diffraction in DIS is the leading twist effect - (formal proof Collins 1998)

 rescatterings of a small dipole off several nucleons are not suppressed by power of r_t^2

 qualitative difference from eikonal: n -th rescattering is suppressed by Q^{2n}

theory of leading twist parton shadowing (Frankfurt, Guzey, MS - 1989 - 1998- 2012)

Note that discussion is simple in the nucleus rest frame but possible also in the fast/ nucleus reference frame



Fundamental feature of QCD: ratio $\frac{\sigma_{inel\ diff}}{\sigma_{el}}$

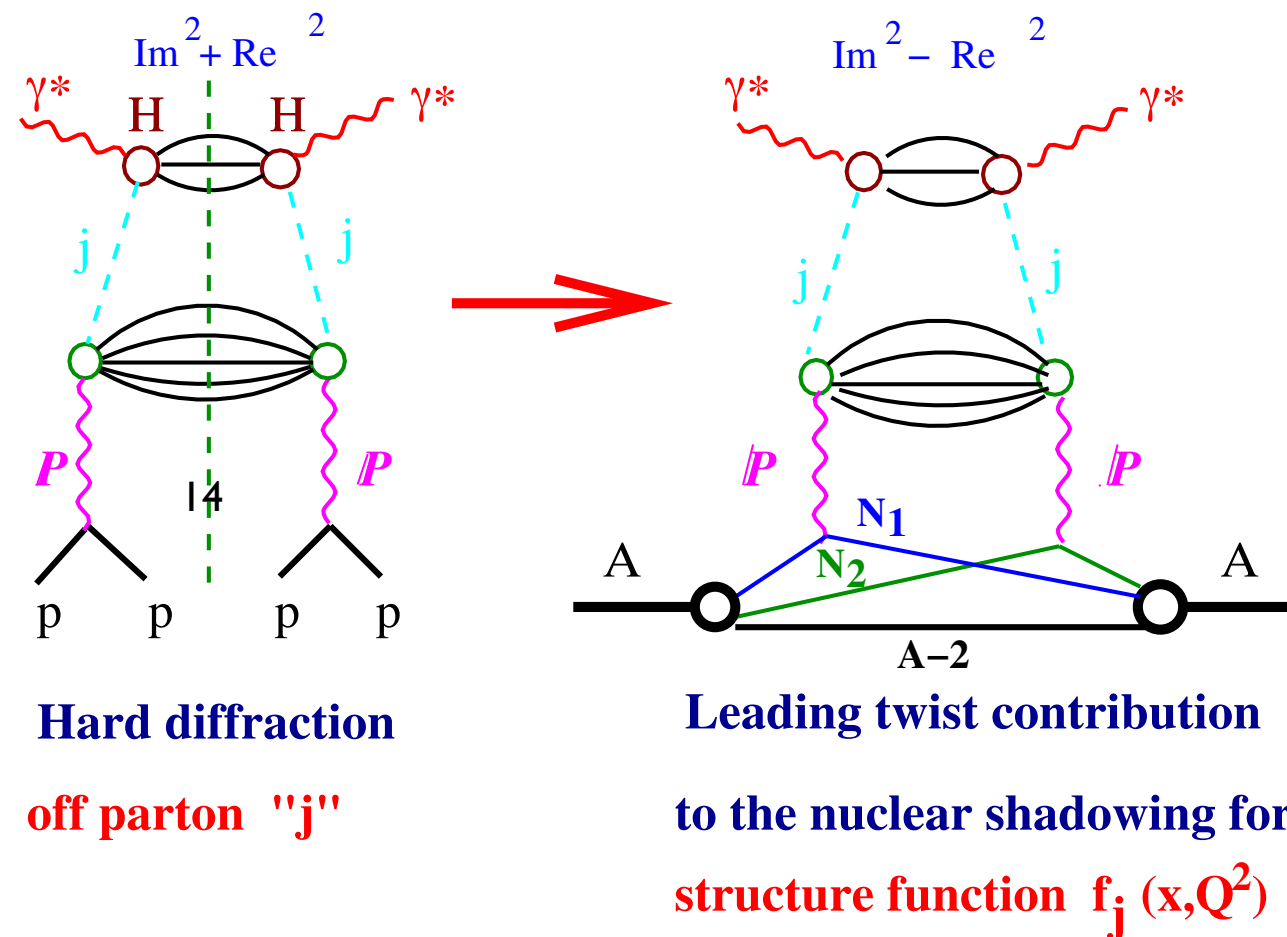
is **small** and decreasing with energy for **soft interactions** (pp)

large (> 1) ($\propto Q^2/Q_0^2$) and increasing with energy for **small dipoles interactions** (DIS)

Theoretical expectations for shadowing in the LT limit

Combining Gribov theory of shadowing and pQCD factorization theorem for diffraction in DIS allows to calculate LT shadowing for **all parton densities** (FS98)
(instead of calculating F_{2A} only)

Theorem: In the low thickness limit the leading twist nuclear shadowing is unambiguously expressed through the nucleon diffractive parton densities: $f_j^D(\frac{x}{x_{\mathbb{P}}}, Q^2, x_{\mathbb{P}}, t)$:



Coherent J/ψ production - update (Guzey, Kryshen, Zhalov, MS 2020)

Theory (Frankfurt, Guzey, MS): Leading twist theory of nuclear shadowing expressing shadowing through LT diffractive PDFs. Alternative - fitting small x data - very limited sample

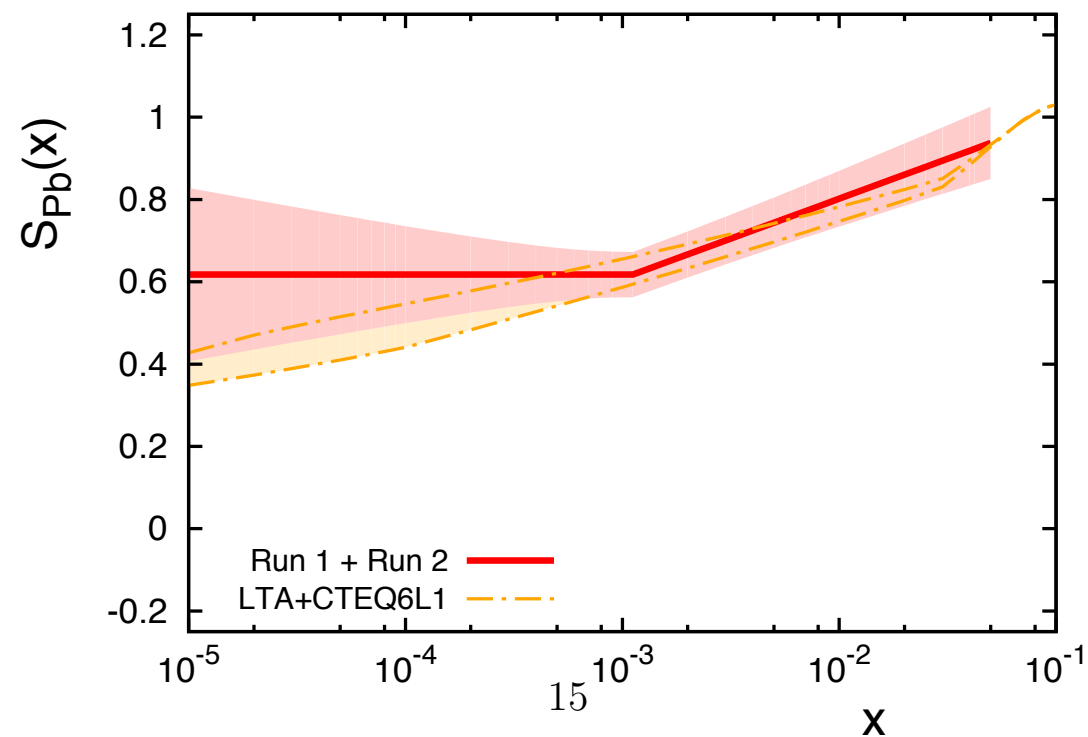
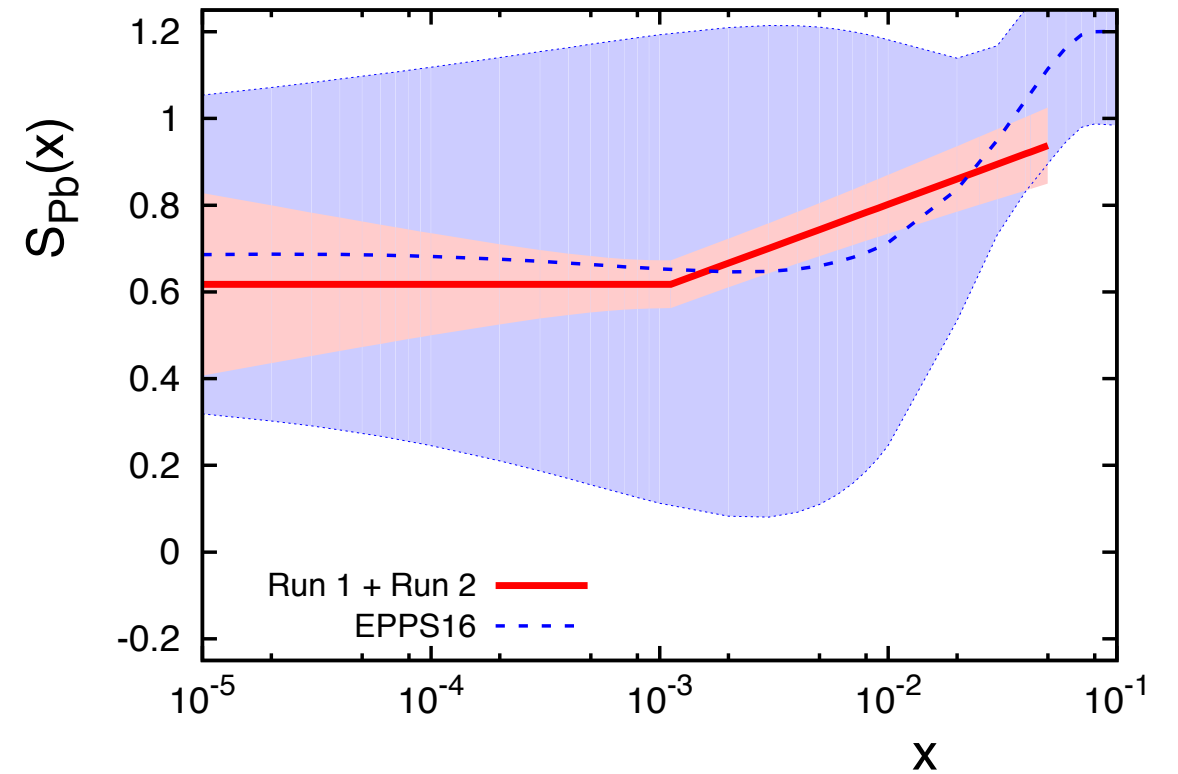
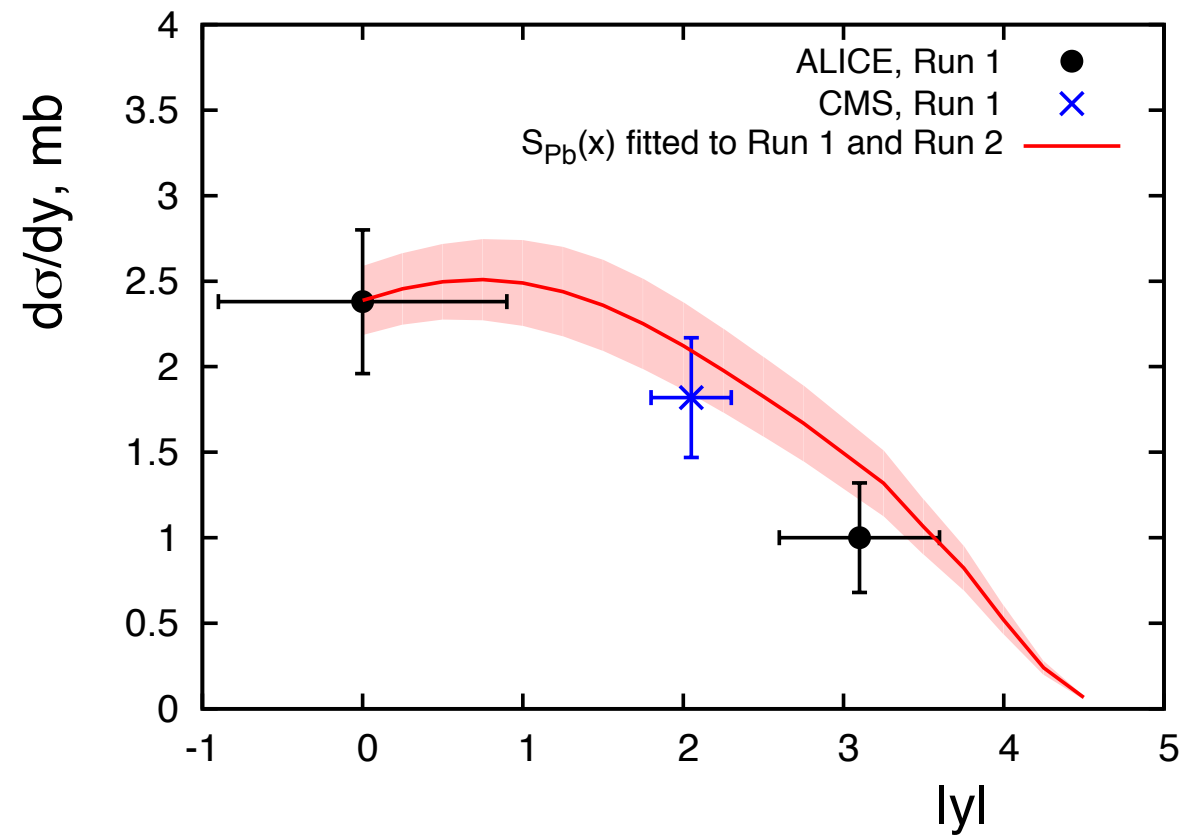
Predicted correctly shadowing for J/ψ in UPC. Use new LHC data to go below **y=0, x=m_{J/ψ} /2E_N**

$$S_{Pb}(x) = \sqrt{\frac{\sigma_{\gamma A \rightarrow J/\psi A}(W_{\gamma p})}{\sigma_{\gamma A \rightarrow J/\psi A}^{\text{IA}}(W_{\gamma p})}} = g_A(x, \mu)/g_p(x, \mu)$$

$$\left(\frac{d\sigma_{AA \rightarrow J/\psi AA}(\sqrt{s_{NN}}, y)/dy}{d\sigma_{AA \rightarrow J/\psi AA}^{\text{IA}}(\sqrt{s_{NN}}, y)/dy} \right)^{1/2}$$

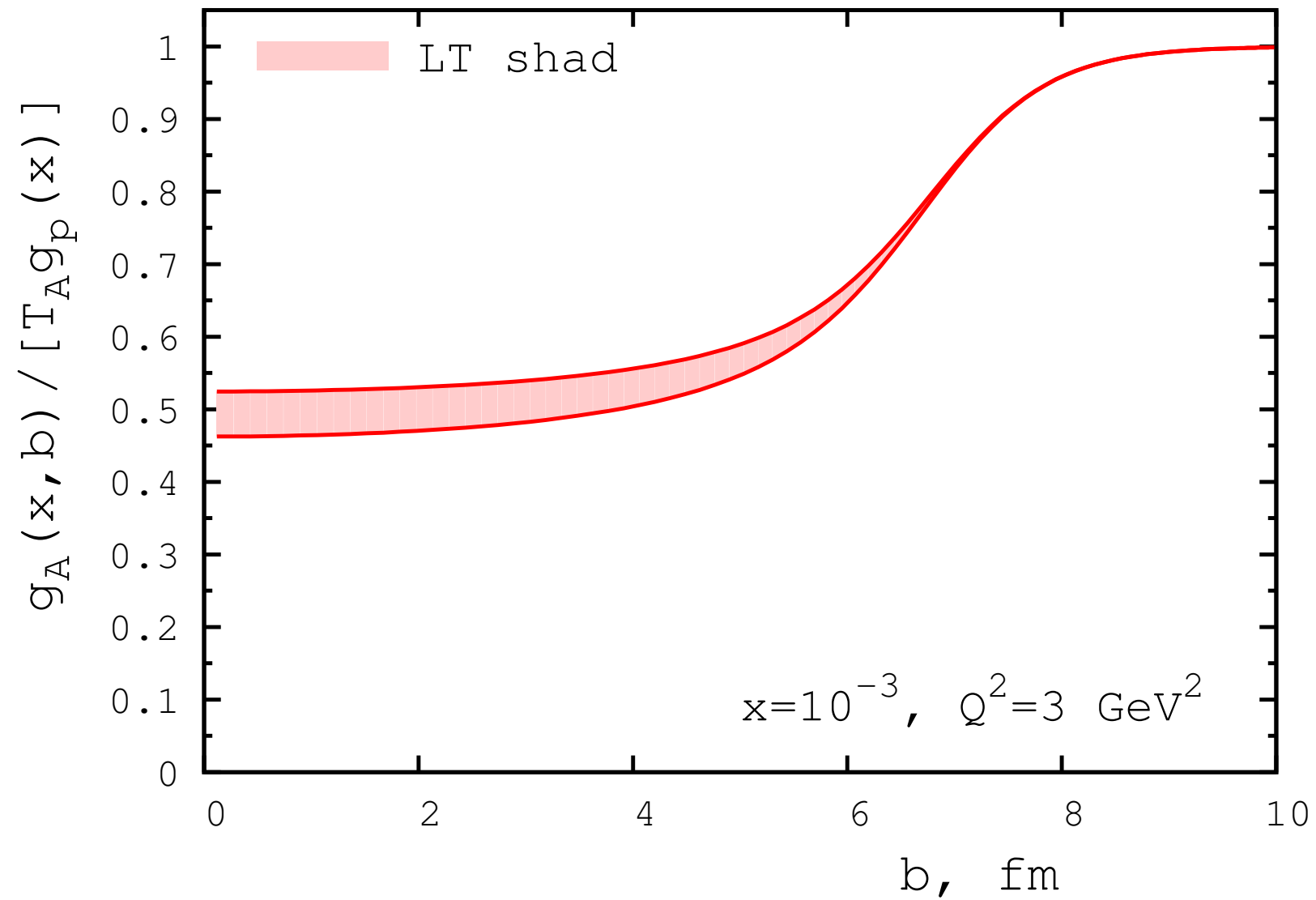
$$= \left(\frac{N_{\gamma/A}(W_{\gamma p}^+) S_{Pb}^2(x_+) \sigma_{\gamma A \rightarrow J/\psi A}^{\text{IA}}(W_{\gamma p}^+) + N_{\gamma/A}(W_{\gamma p}^-) S_{Pb}^2(x_-) \sigma_{\gamma A \rightarrow J/\psi A}^{\text{IA}}(W_{\gamma p}^-)}{N_{\gamma/A}(W_{\gamma p}^+) \sigma_{\gamma A \rightarrow J/\psi A}^{\text{IA}}(W_{\gamma p}^+) + N_{\gamma/A}(W_{\gamma p}^-) \sigma_{\gamma A \rightarrow J/\psi A}^{\text{IA}}(W_{\gamma p}^-)} \right)^{1/2}$$

where $x_{\pm} = M_{J/\psi}^2 / W_{\gamma p}^{\pm 2}$

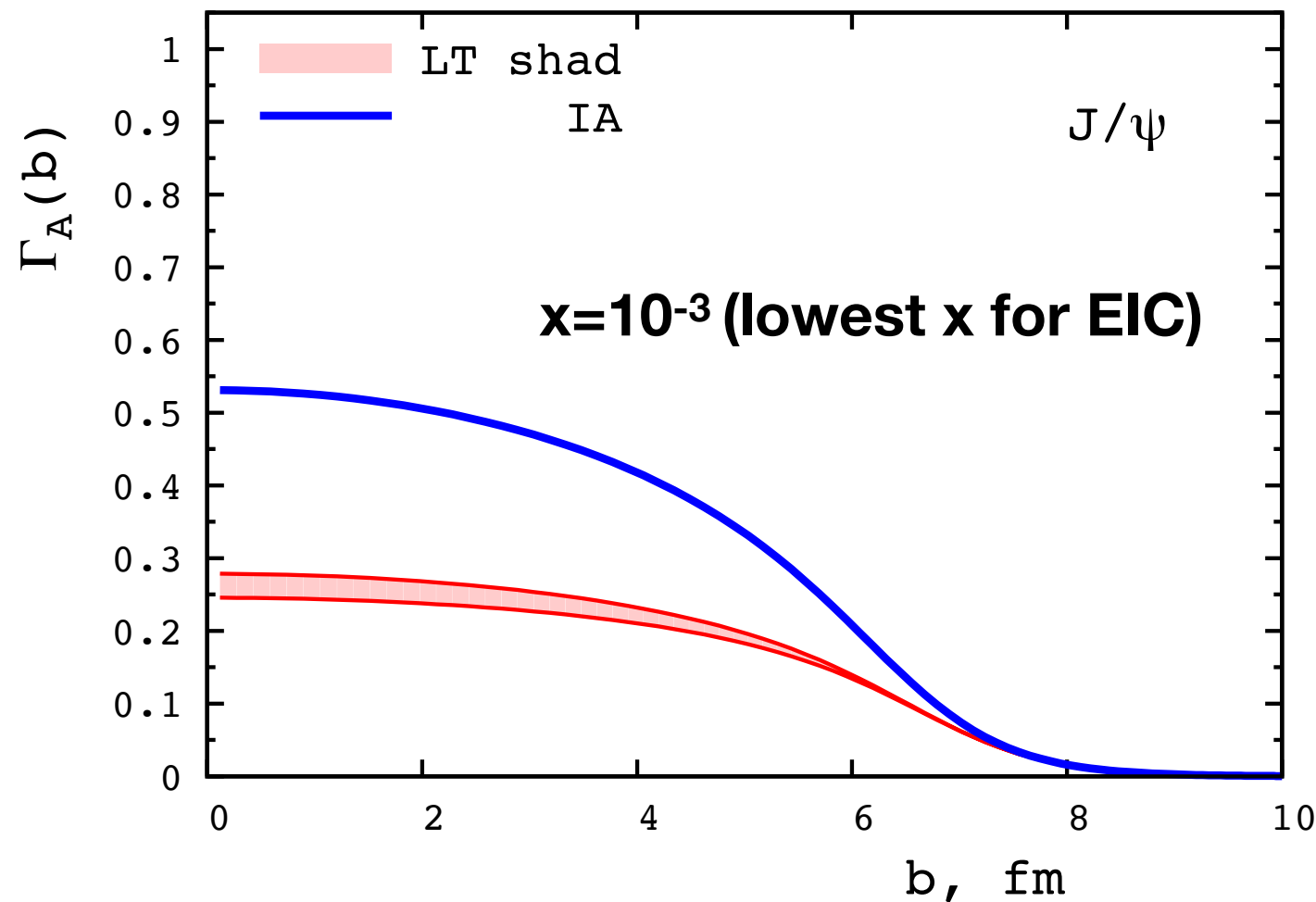


Our prediction (orange dashed dot) for $x=10^{-4}$ is bit below the range. Necessary to figure out the reasons for discrepancy between LHCb and ALICE & study impact parameter dependence of the J/ψ yield

we also predicted increase of t -dependence of coherent J/ψ production as compared to impulse approximation



Leading twist gluon shadowing in impact parameter space for coherent J/ψ photoproduction on Pb as a function of $|\vec{b}|$.



The scattering amplitude in impact parameter space $\Gamma_A(b)$ for coherent J/ψ photoproduction on Pb as a function of $|\vec{b}|$.

Gluon shadowing changes regime of interaction for $x \sim 10^{-3}$ and small b from close to black (probability to interact inelastically)

$$1 - (1 - \Gamma)^2 = 0.77 \text{ to gray } 1 - (1 - \Gamma)^2 = 0.45$$

To reach the black limit $x \sim 10^{-5}$ is necessary

why heavy nucleus did not help significantly?

Where is $A^{1/3}$ factor?

nucleus is much more dilute than proton + gluon shadowing

$$\frac{Q_{sA}^2}{Q_{sN}^2} = A \frac{R_{gN}^2}{R_A^2} \frac{g_A(x, Q^2)}{A g_N(x, Q^2)}$$

$$R_{gN}^2(x = 10^{-3}) = 0.6 \text{ fm}^2$$

$$Q_{sA}^2(b = 0)/Q_{sN}^2 = T_A(b = 0) \cdot S_A(x, b = 0) \cdot 2R_{gN}^2 = 1.2$$

A~200

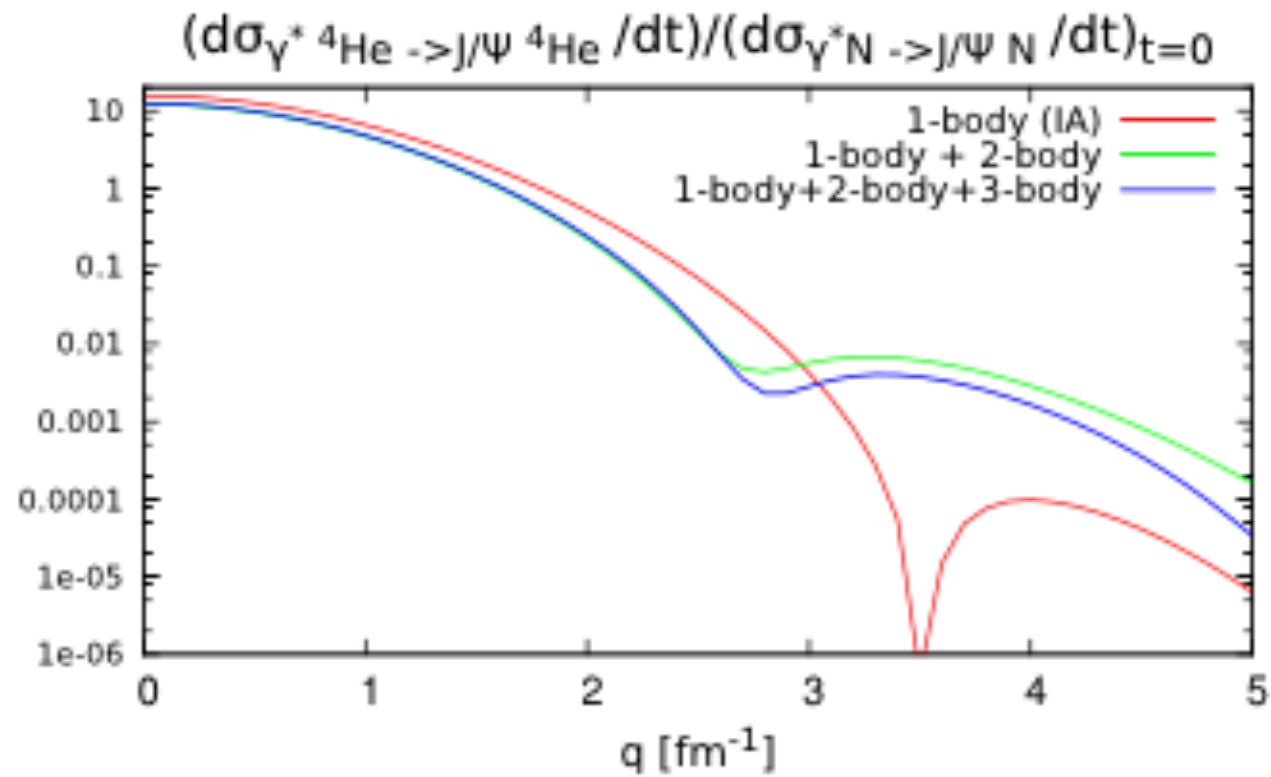
compare: $Q_{\text{sat}}^2 = 1 \text{ GeV}^2$ for proton at $x=10^{-4}$ (Jamal Jalilian-Marian 2021)

New opportunity at EIC - light nuclei. Allows to measure interaction with exactly 2, 3 nucleons

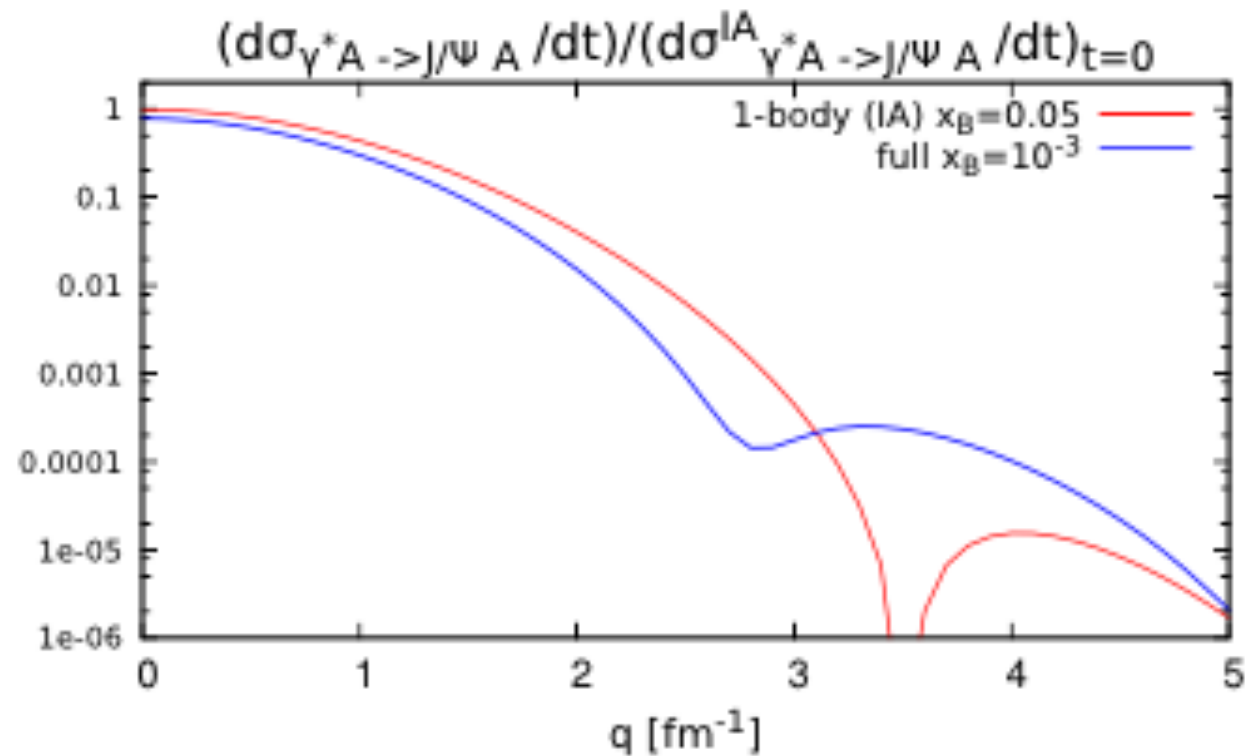
Shadowing for heavy nuclei involves interactions with 2, 3, 4, ... nucleons with individual terms canceling each other. Difficult to separate interactions with 2, 3 nucleons and perform critical tests of the models. For the lightest nuclei (^4He , ^3He) only interactions with 1 & 2 & 3 nucleons contribute.

V. Guzey, M. Renaldi, S. Scopetta, MS, M. Viviani

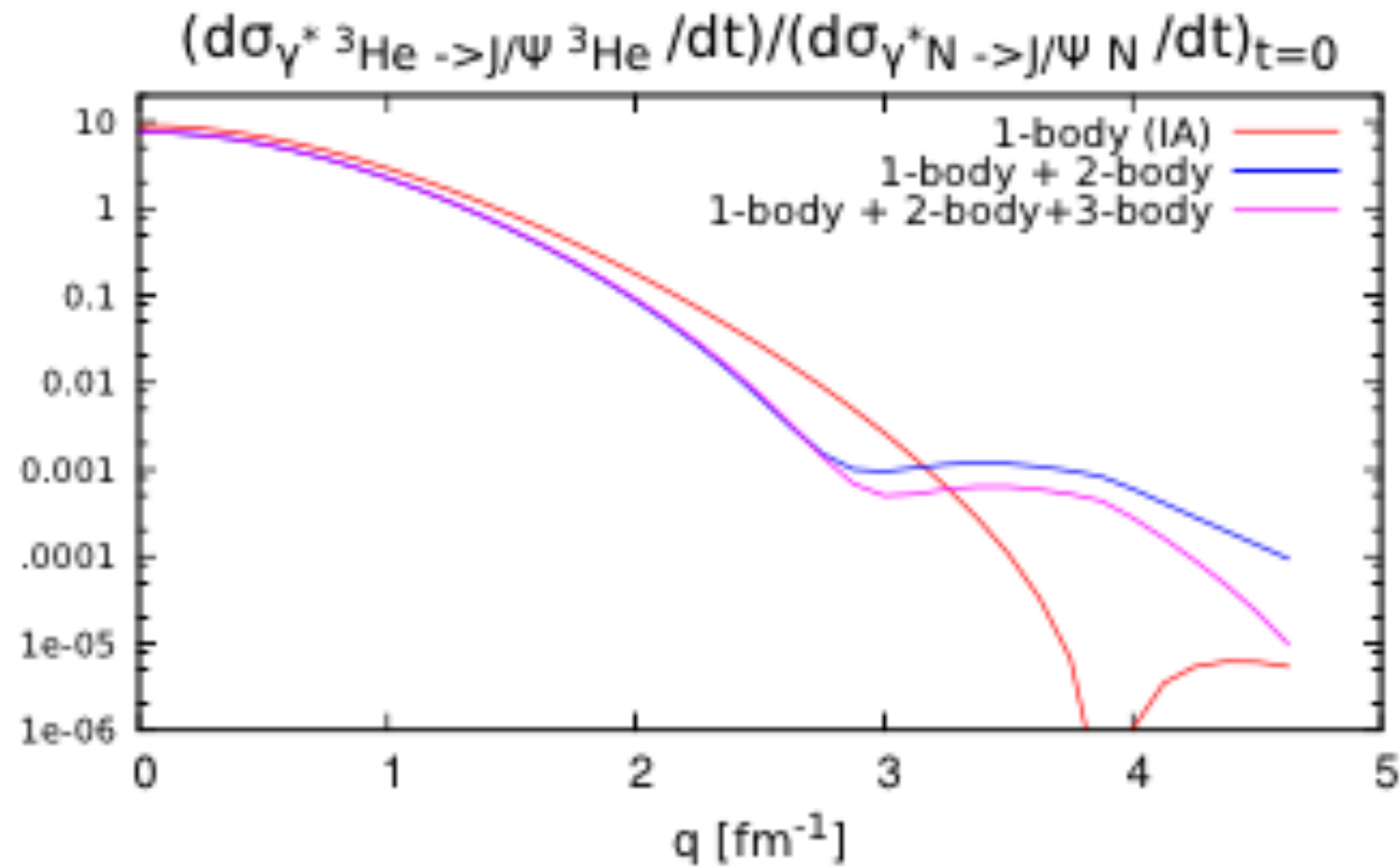
Naively — impulse approximation masks 2 & 3 scattering term. However there is a special feature for $A=3, 4$. One body term which is proportional to form factor goes through zero at moderate t providing window to 2 & 3 contribution. Challenge: calculation of 2, 3, 4 body form factors with realistic ^4He wave functions.



Ratio of the differential cross section for J/Ψ coherent production on ⁴He to the same quantity for the nucleon target at t=0, x=10⁻³.



Prediction: Strong x - dependence of the ratio of the differential cross section for J/Ψ coherent production on ⁴He to the same quantity for the nucleon target at t=0, x=10⁻³ & x=.05



Ratio of the differential cross section for J/Ψ coherent production on ${}^3\text{He}$ to the same quantity for the nucleon target at $t=0$, $x=10^{-3}$

Other directions

- **quasielastic** $\gamma + p (A) \rightarrow J/\psi + Y$ at $t=0$

inelastic diffraction at $t=0$ measures color fluctuations in nucleons

$$\frac{\langle g_N^2(x) \rangle}{g_N^2(x)} = 1 \quad \text{Frankfurt, MS, Treleani, Weiss}$$

for heavy nuclei details of gluon shadowing dynamics

For $-t > 1 \text{ GeV}^2$ - dynamics of parton (gluon) knock out
(minor sensitivity to color fluctuations)

- $\gamma + p (A) \rightarrow J/\psi(\text{large } t) + \text{rapidity gap} + Y$

Issues: **BFKL at $-t > 1 \text{ GeV}^2$, propagation of small dipole through nuclear media**

Conclusions

- **J/ ψ coherent and quasielastic production provide unique probes of the gluon dynamics at in nucleons and nuclei.**
- **Complementarity of EIC and UPC at the LHC**
- **Detector challenges: Low t resolution, separation of inelastic and elastic channels, detection of light nuclei.**

Supplementary slide

Perturbative Pomeron: what is energy dependence cross section in vacuum channel ?

Problem for the study - two large parameters $\ln Q^2$, and $\ln 1/x$.

DIS - both parameters enter (DGLAP); BGKL - only $\ln 1/x$ (scattering of two small dipoles)

BFKL elastic amplitude $f(s) = (s/s_0)^{1+\omega}$

$$\omega_{/P} = a_1 \alpha_S - a_2 \alpha_S^2 + \dots$$

leading log $\omega_{/P} \sim 0.5 \div 0.8$, NLO ~ 0.1 , resummation ~ 0.25

Main reason for small values of $\omega_{/P}$ energy conservation

Promising direction: Rapidity gaps at large t for J/ψ production - squeezing from both ends.

*Can be measured in UPC (pA),
future: EIC, LHeC.*

a simpler process than Mueller and Tung dijet

