

# Anomalies and $L_\mu - L_\tau$

Julian Heeck

DWQ@25

12/15/2021



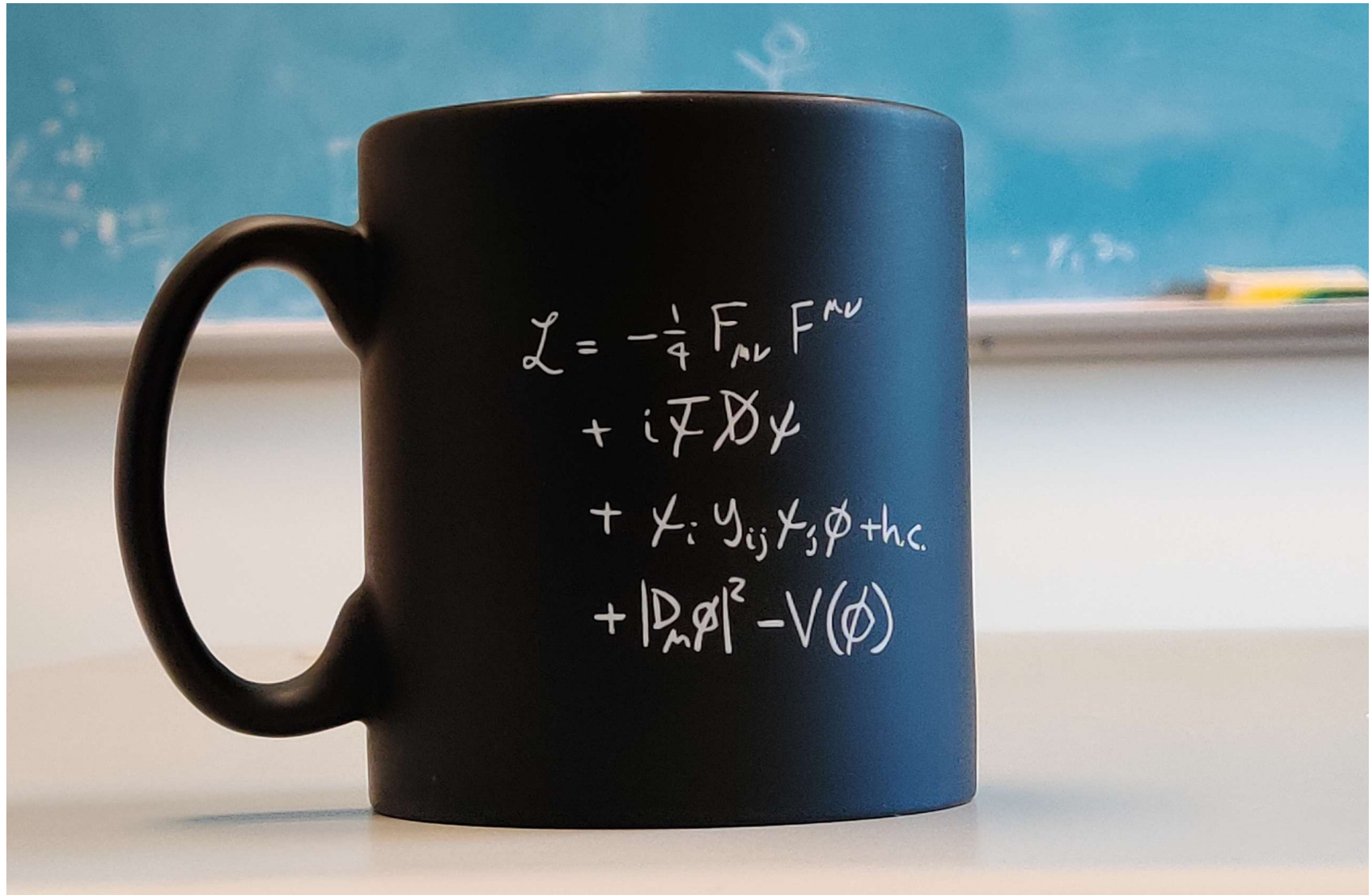
UNIVERSITY  
*of* VIRGINIA

# Elementary particles

	<p>mass → <math>\approx 2.3 \text{ MeV}/c^2</math></p> <p>charge → <math>2/3</math></p> <p>spin → <math>1/2</math></p> <p><b>u</b></p> <p>up</p>	<p>mass → <math>\approx 1.275 \text{ GeV}/c^2</math></p> <p>charge → <math>2/3</math></p> <p>spin → <math>1/2</math></p> <p><b>c</b></p> <p>charm</p>	<p>mass → <math>\approx 173.07 \text{ GeV}/c^2</math></p> <p>charge → <math>2/3</math></p> <p>spin → <math>1/2</math></p> <p><b>t</b></p> <p>top</p>	<p>mass → <math>0</math></p> <p>charge → <math>0</math></p> <p>spin → <math>1</math></p> <p><b>g</b></p> <p>gluon</p>	<p>mass → <math>\approx 126 \text{ GeV}/c^2</math></p> <p>charge → <math>0</math></p> <p>spin → <math>0</math></p> <p><b>H</b></p> <p>Higgs boson</p>
BARYONS/ QUARKS	<p>mass → <math>\approx 4.8 \text{ MeV}/c^2</math></p> <p>charge → <math>-1/3</math></p> <p>spin → <math>1/2</math></p> <p><b>d</b></p> <p>down</p>	<p>mass → <math>\approx 95 \text{ MeV}/c^2</math></p> <p>charge → <math>-1/3</math></p> <p>spin → <math>1/2</math></p> <p><b>s</b></p> <p>strange</p>	<p>mass → <math>\approx 4.18 \text{ GeV}/c^2</math></p> <p>charge → <math>-1/3</math></p> <p>spin → <math>1/2</math></p> <p><b>b</b></p> <p>bottom</p>	<p>mass → <math>0</math></p> <p>charge → <math>0</math></p> <p>spin → <math>1</math></p> <p><b><math>\gamma</math></b></p> <p>photon</p>	
		<p>mass → <math>0.511 \text{ MeV}/c^2</math></p> <p>charge → <math>-1</math></p> <p>spin → <math>1/2</math></p> <p><b>e</b></p> <p>electron</p>	<p>mass → <math>105.7 \text{ MeV}/c^2</math></p> <p>charge → <math>-1</math></p> <p>spin → <math>1/2</math></p> <p><b><math>\mu</math></b></p> <p>muon</p>	<p>mass → <math>1.777 \text{ GeV}/c^2</math></p> <p>charge → <math>-1</math></p> <p>spin → <math>1/2</math></p> <p><b><math>\tau</math></b></p> <p>tau</p>	<p>mass → <math>91.2 \text{ GeV}/c^2</math></p> <p>charge → <math>0</math></p> <p>spin → <math>1</math></p> <p><b>Z</b></p> <p>Z boson</p>
LEPTONS	<p>mass → <math>&lt; 2.2 \text{ eV}/c^2</math></p> <p>charge → <math>0</math></p> <p>spin → <math>1/2</math></p> <p><b><math>\nu_e</math></b></p> <p>electron neutrino</p>	<p>mass → <math>&lt; 0.17 \text{ MeV}/c^2</math></p> <p>charge → <math>0</math></p> <p>spin → <math>1/2</math></p> <p><b><math>\nu_\mu</math></b></p> <p>muon neutrino</p>	<p>mass → <math>&lt; 15.5 \text{ MeV}/c^2</math></p> <p>charge → <math>0</math></p> <p>spin → <math>1/2</math></p> <p><b><math>\nu_\tau</math></b></p> <p>tau neutrino</p>	<p>mass → <math>80.4 \text{ GeV}/c^2</math></p> <p>charge → <math>\pm 1</math></p> <p>spin → <math>1</math></p> <p><b>W</b></p> <p>W boson</p>	

[wikipedia]

# Interactions



# Symmetries of the Standard Model

- Rephasing lepton and quark fields:

$$\begin{aligned} & U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} \\ & = \\ & U(1)_{B+L} \times U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e} . \end{aligned}$$

# Symmetries of the Standard Model

- Rephasing lepton and quark fields:

$$U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau}$$

=

$$\cancel{U(1)_{B+L}} \times U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e} \cdot$$

- **Broken** non-perturbatively, but unobservable. [['t Hooft, PRL '76](#)]
- True accidental global symmetry:

$$U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e} \cdot$$

# Symmetries of the Standard Model

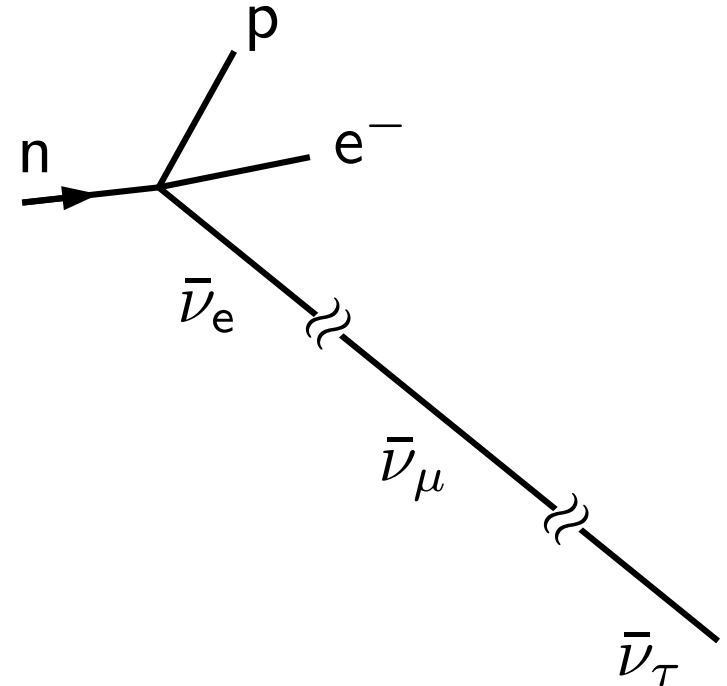
- True accidental global symmetry:

$$U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e} .$$

- A subgroup  $U(1)_{L_\alpha - L_\beta}$  can be **gauged** without any new particles!  
[Foot '91; He, Joshi, Lew, Volkas, '91]
- With 3  $N_R$ , the entire  $U(1)^3$  can be gauged. [Araki, JH, Kubo, '12]
  - Gauging global SM symmetry gives **neutrino masses**, but no mixing angles...

# Neutrino oscillations = flavor violation

- Observations of  $\nu_\alpha \rightarrow \nu_\beta$  prove that  $M_\nu \neq 0$  and  $U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}$  is **broken!**
- Charged lepton flavor violation will occur, not clear how fast.
- B-L could still be **unbroken** if neutrinos are Dirac. [\[JH, 1408.6845\]](#)
  - B-L often broken to get seesaw.



**Are the U(1) symmetries not interesting if they're broken?**

Majorana mass matrix  $\mathcal{M}_\nu = U \text{diag}(m_1, m_2, m_3) U^T$  in special cases:

- ① **Normal hierarchy** ( $m_1 \simeq 0$ ) and best-fit values (phases zero):

$$\mathcal{M}_\nu \simeq \begin{pmatrix} 0.37 & 0.75 & 0.24 \\ \cdot & 2.47 & 2.11 \\ \cdot & \cdot & 2.99 \end{pmatrix} 10^{-2} \text{ eV} \sim \begin{pmatrix} 0 & 0 & 0 \\ 0 & \times & \times \\ 0 & \times & \times \end{pmatrix} \leftarrow L_e$$

- ② **Inverted hierarchy** ( $m_3 \simeq 0$ ) and  $\alpha = \pi/2$ :

$$\mathcal{M}_\nu \simeq \begin{pmatrix} 1.84 & -3.11 & 3.22 \\ \cdot & -0.14 & 0.88 \\ \cdot & \cdot & -1.77 \end{pmatrix} 10^{-2} \text{ eV} \sim \begin{pmatrix} 0 & \times & \times \\ \times & 0 & 0 \\ \times & 0 & 0 \end{pmatrix} \leftarrow L_e - L_\mu - L_\tau$$

- ③ **Quasi-degenerate** ( $m_{1,2,3} \simeq 1 \text{ eV}$ ) and  $\beta = \pi/2$ :

$$\mathcal{M}_\nu \simeq \begin{pmatrix} 0.96 & -0.20 & -0.22 \\ \cdot & 0.11 & -0.97 \\ \cdot & \cdot & -0.07 \end{pmatrix} \text{ eV} \sim \begin{pmatrix} \times & 0 & 0 \\ 0 & 0 & \times \\ 0 & \times & 0 \end{pmatrix} \leftarrow L_\mu - L_\tau$$



- Three interesting zeroth order approximations:

$$\mathcal{M}_\nu^{L_e} \sim \begin{pmatrix} 0 & 0 & 0 \\ 0 & \times & \times \\ 0 & \times & \times \end{pmatrix}, \quad \mathcal{M}_\nu^{L_e - L_\mu - L_\tau} \sim \begin{pmatrix} 0 & \times & \times \\ \times & 0 & 0 \\ \times & 0 & 0 \end{pmatrix}, \quad \mathcal{M}_\nu^{L_\mu - L_\tau} \sim \begin{pmatrix} \times & 0 & 0 \\ 0 & 0 & \times \\ 0 & \times & 0 \end{pmatrix}$$

[G. Branco, W. Grimus, L. Lavoura, *NPB* (1989); S. Choubey, W. Rodejohann, *EPJC* 40 (2005)]

- Normal, inverted, quasi-degenerate hierarchy might hint at “weakly broken”  $B - 3L_e$ ,  $B + 3(L_e - L_\mu - L_\tau)$ ,  $L_\mu - L_\tau$



makes it anomaly free

[JH, Rodejohann, 1203.3117]

- Connection of  $L_\mu - L_\tau$  to **neutrino mass anomaly**.
- Pressure on quasi-degenerate regime from cosmology bounds on  $\Sigma m_\nu$ . [Asai et al, 1811.07571]

# Symmetries of the Standard Model

- True accidental global symmetry:

$$U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e} .$$

- With 3  $N_R$ , the entire  $U(1)^3$  can be gauged.
- First see the  $Z'$  with largest  $g'$  or smallest mass, coupled to

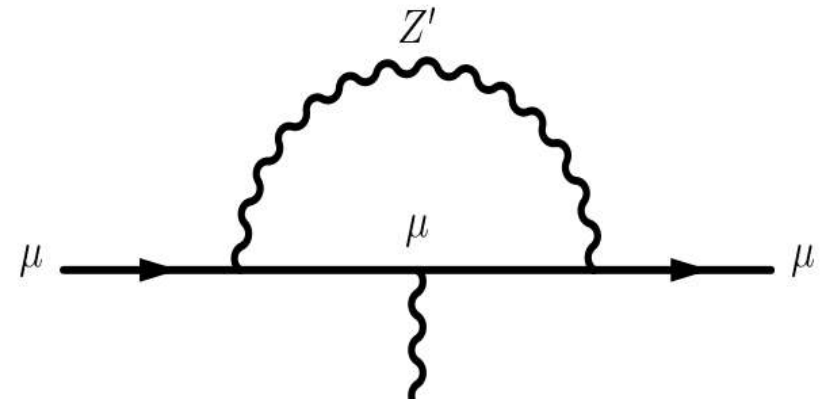
$$a(B - L) + b(L_\mu - L_\tau) + c(L_\mu + L_\tau - 2L_e) .$$

- Pheno dominated by electron coupling, except for  $a=c=0$ !

# 2001: $(g-2)_\mu$

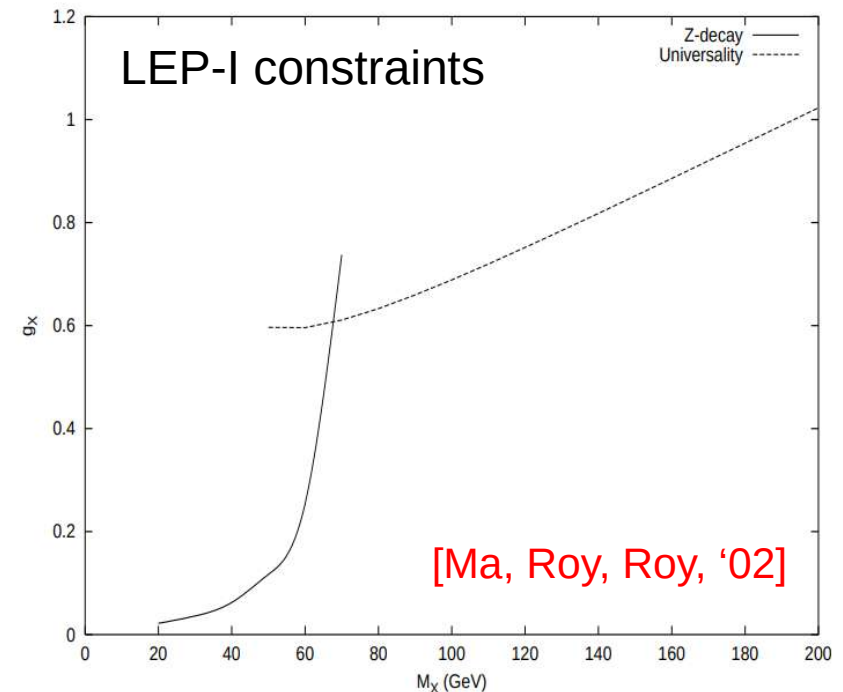
- Quickly realized that  $L_\mu - L_\tau$   $Z'$  can explain BNL result.

[Baek, Deshpande, He, Ko, '01; Ma, Roy, Roy, '02]



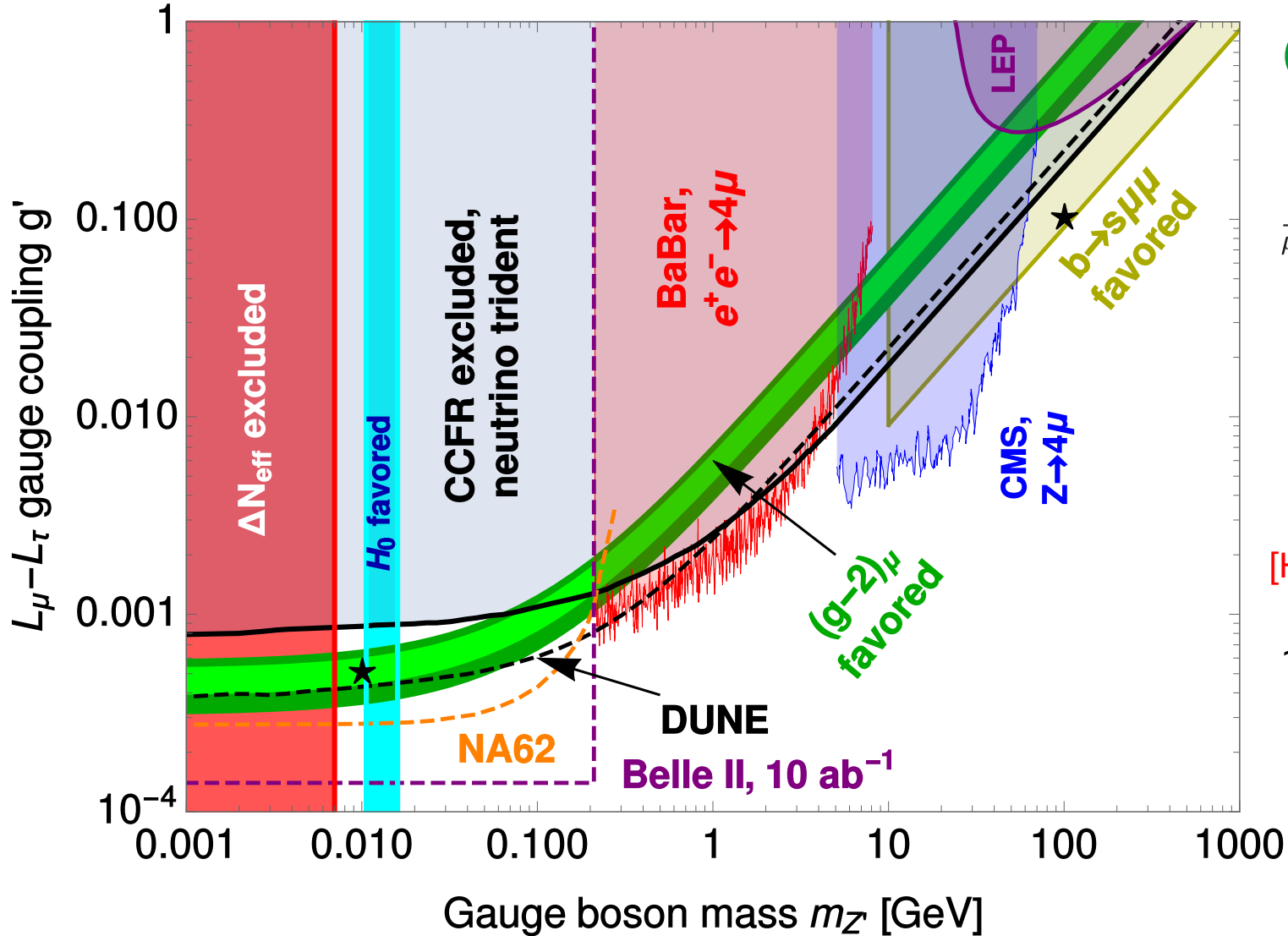
- Back then, *many* other simple models worked, but  $L_\mu - L_\tau$  has survived for 20 years.

- While initially almost unconstrained due to vanishing first-generation couplings, it has now been pushed into a corner.

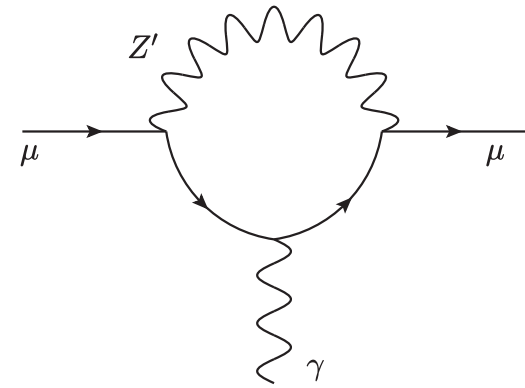


# Current $Z'$ constraints

[JH, Garani, 1906.10145]



$(g-2)_\mu$ :

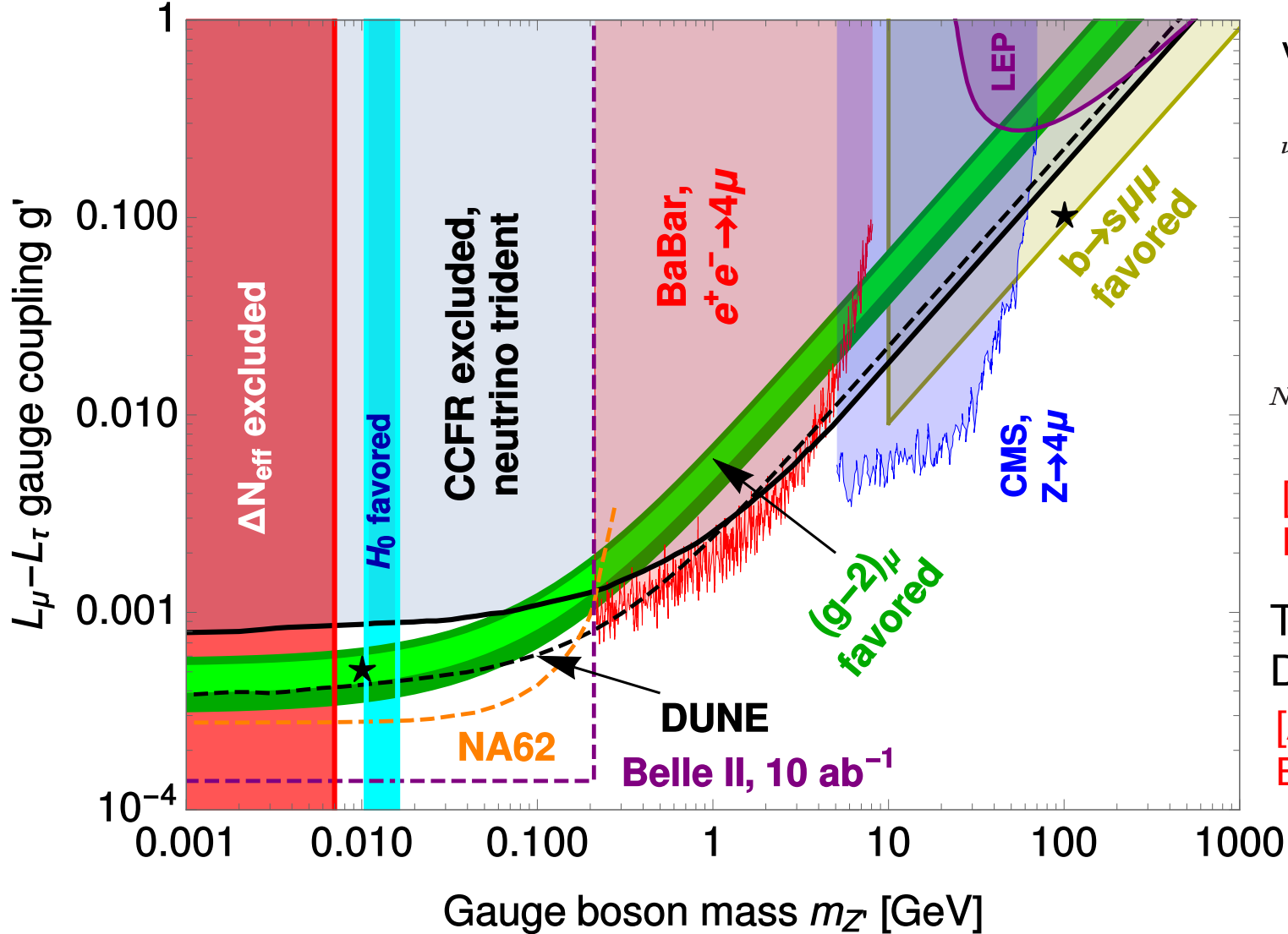


[He, Joshi, Lew, Volkas, '91]

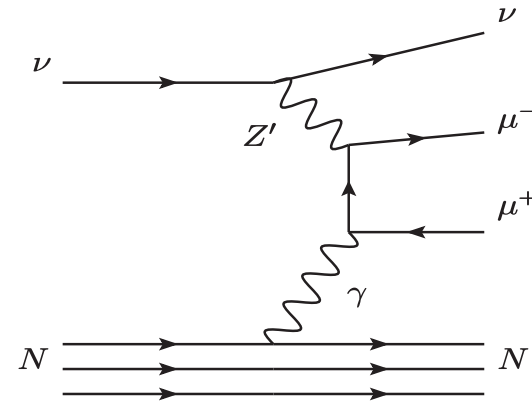
$\sim 4\sigma$  deviation!

# Current $Z'$ constraints

[JH, Garani, 1906.10145]



$\nu$  trident:



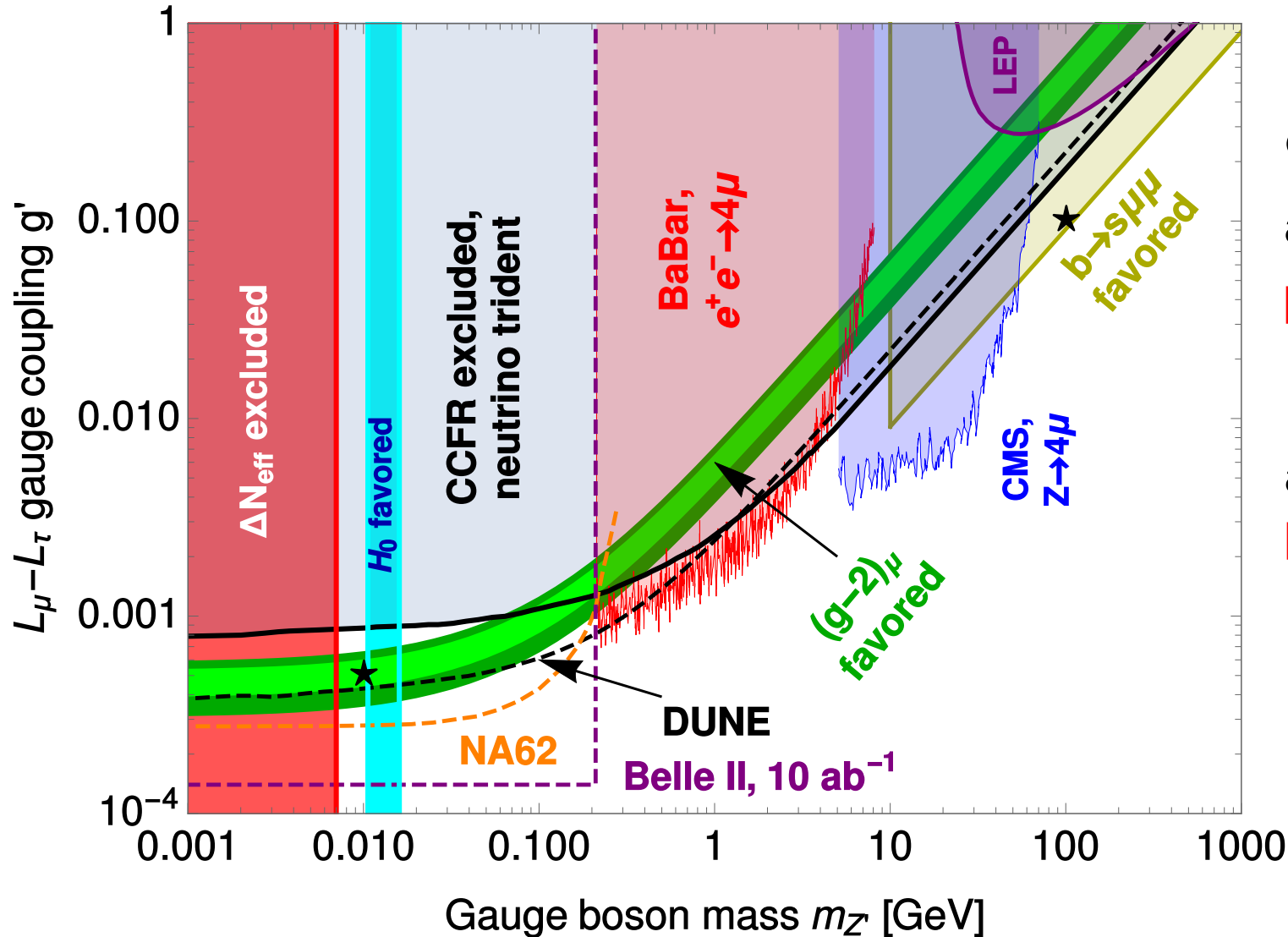
[Altmannshofer, Gori, Pospelov, Yavin, '14]

To be improved by DUNE!

[Altmannshofer++, '19; Ballett++, '19]

# Current $Z'$ constraints

[JH, Garani, 1906.10145]



Invisible  $Z'$ :

$$e^+e^- \rightarrow \mu^+\mu^-Z'$$

at Belle II.

[Jho++, 1904.1305]

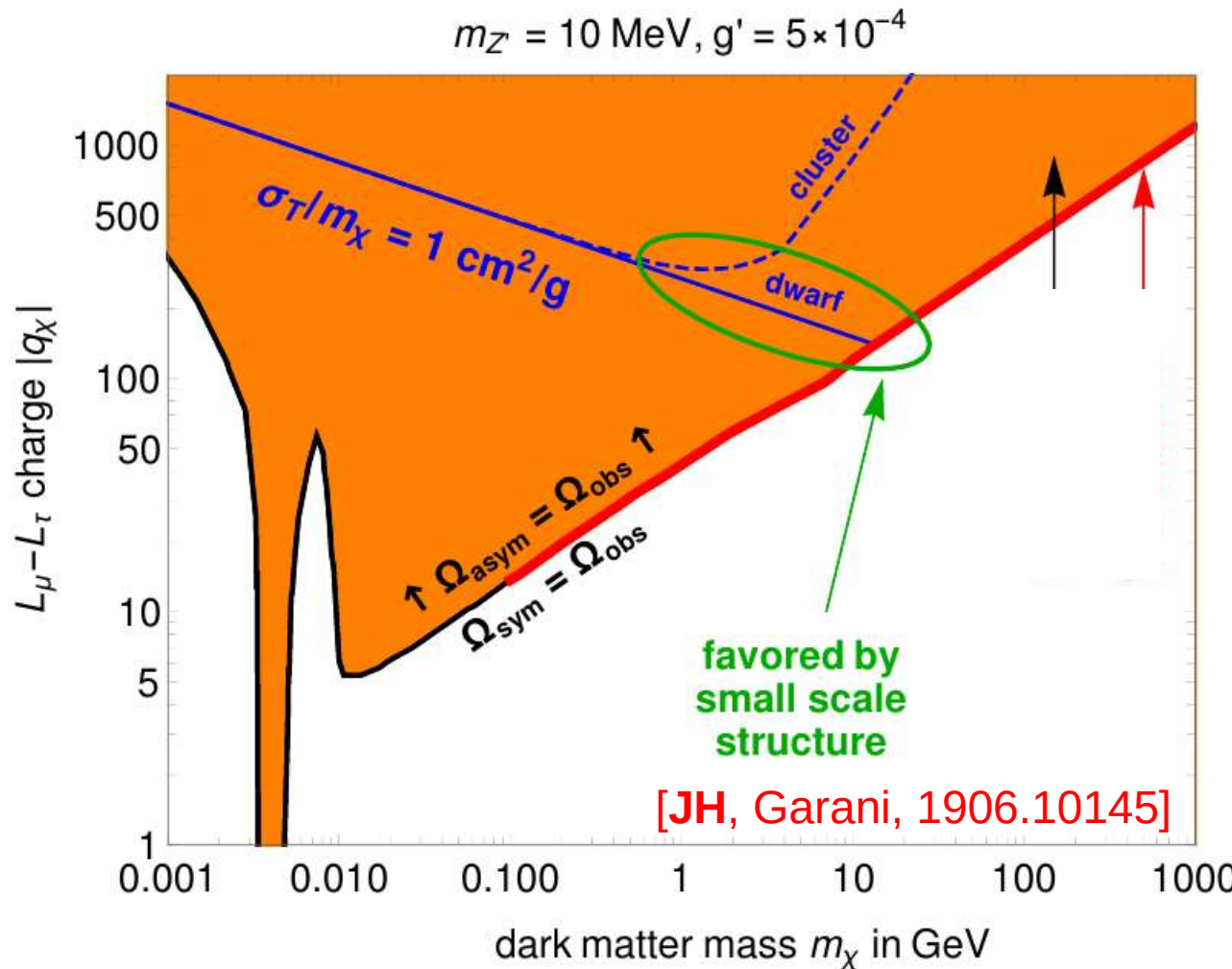
$$K \rightarrow \mu\nu Z'$$

at NA62.

[Krnjaic++, 1902.07715]

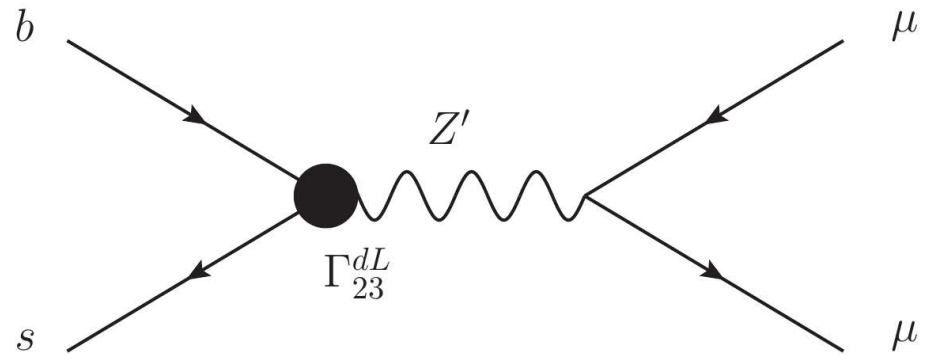
# $L_\mu - L_\tau$ and $g-2$

- Pushed into corner  $10 \text{ MeV} < m_{Z'} < 200 \text{ MeV}$ , probed decisively in near future.
- Light  $Z'$  could be a mediator to a DM sector; can easily generate large **DM self-interaction** cross sections that solve small-scale structure problems.
- DM stability:  $U(1)'$ .



# Non-minimal $L_\mu - L_\tau$

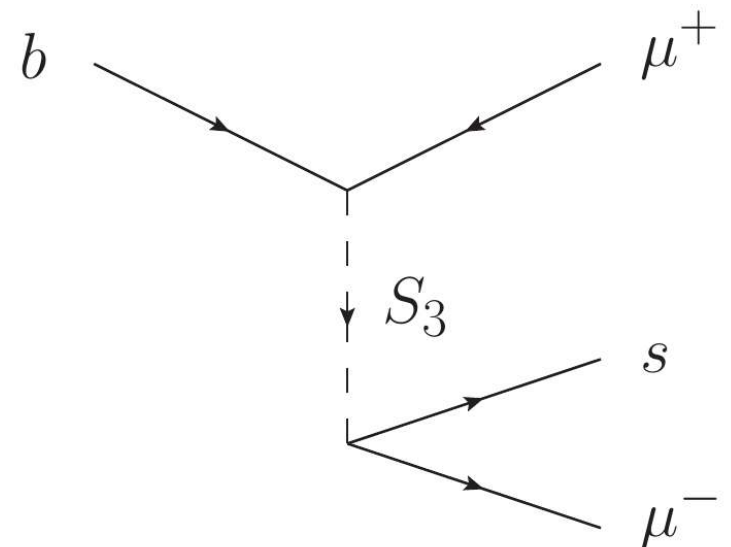
- Can induce additional  $Z'$  couplings, e.g. in the quark sector, via heavy fermions [Altmannshofer, Gori, Pospelov, Yavin, '14] or Higgs fields. [Crivellin, D'Ambrosio, **JH**, PRL & PRD '15]
- Can get  $bs\mu\mu$  operator, explains  $R(K)$  and  $R(K^*)$ !
- LFUV from  $L_\mu - L_\tau$ , but  $Z'$  needs to be heavier than for g-2.
- Predicts deviations in  $b \rightarrow s\tau\tau$  and  $b \rightarrow sv\nu$ , but tough to test.
- Strong constraint from  $B-\bar{B}$  oscillations.





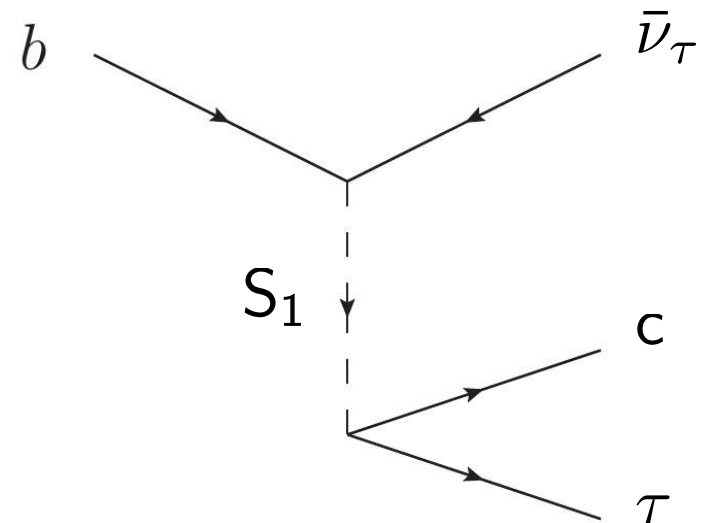
# $L_\mu - L_\tau$ beyond the $Z'$

- Can use  $L_\mu - L_\tau$  (or other flavor  $U(1)'$ ) to forbid or enforce couplings.
- Take leptoquark  $S_3 \sim (\mathbf{3}, \mathbf{3}, -1/3)$ :  $\mathcal{L} = y_{ij} \bar{Q}_i S_3 L_j^c + x_{ij} Q_i Q_j S_3$
- Charge  $S_3 \sim +1$  under  $L_\mu - L_\tau$  to get  $x_{ij} = 0$ ,  $y_{ij} = y_{i\mu}$ .  
 → no more **proton decay**, no **lepton flavor violation**,  
 only coupling to **muons**!
- Perfect for  **$R(K)$**  &  **$R(K^*)$** !  
 [Hambye, **JH**, PRL '18; Davighi, Kirk, Nardecchia, '20; Greljo, Stangl, Thomsen, '21]
- $L_\mu - L_\tau$  global or gauged, just need to break it in neutrino sector.



# $L_\mu - L_\tau$ beyond the $Z'$

- Can use  $L_\mu - L_\tau$  (or other flavor  $U(1)'$ ) to forbid or enforce couplings.
- Take LQ  $S_1 \sim (\mathbf{3}, \mathbf{1}, -1/3)$ :  $\mathcal{L} = y_{ij} \bar{Q}_i S_1 L_j^c + x_{ij} Q_i Q_j S_1 + \dots$
- Charge  $S_1 \sim -1$  under  $L_\mu - L_\tau$  to get  $x_{ij} = 0$ ,  $y_{ij} = y_{i\tau}$ .  
 → no more **proton decay**, no **lepton flavor violation**,  
 only coupling to **tauons**!
- Perfect for  **$R(D)$**  &  **$R(D^*)$** !  
 [Angelescu++, 2103.12504,  
**JH** & Thapa, in preparation]
- $L_\mu - L_\tau$  global or gauged, just need to break it in neutrino sector.



# A simple $L_\mu - L_\tau$ model

- Gauge  $L_\mu - L_\tau$  and break it in neutrino sector to get  $M_\nu$ .
- Add LQ  $S_1 \sim (\mathbf{3}, \mathbf{1}, -1/3)$  with  $L_\mu - L_\tau \sim -1$  to explain  $R(D)$  and LQ  $S_3 \sim (\mathbf{3}, \mathbf{3}, -1/3)$  with  $L_\mu - L_\tau \sim +1$  to explain  $R(K)$ .
  - U(1) eliminates **proton decay** and **lepton flavor violation**.
- $Z'$  in mass range 10-100 MeV explains  $(g-2)_\mu$ .
- Charge new singlet fermions/scalars under  $L_\mu - L_\tau$ .
  - Stability through U(1)'  $\rightarrow$  dark matter!
  - Relic abundance through  $Z'$ .
  - Self-interactions via light  $Z'$  explain **small-scale structure!**

[JH & Thapa, in preparation]

Only  $L_\mu - L_\tau$  can do all this!

# Summary

- Standard Model symmetry/prediction:

$$U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e} .$$

- Easy to gauge any subgroup of this.
- $L_\mu - L_\tau$  special:
  - Only acts on 2<sup>nd</sup> & 3<sup>rd</sup> gen particles → weak constraints.
  - Good flavor symmetry for quasi-degenerate **neutrinos**.
  - Only  $Z'$  left to explain muon  **$g-2$** , soon fully probed.
  - Breaks lepton flavor universality, can explain  **$R(K)$  &  $R(D)$** .

Arguably most useful  $U(1)$ !