NNLO jets in in polarized DIS

Ignacio Borsa, Daniel de Florian, Iván Pedron*



Universidad Nacional de San Martín





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Factorization theorem

$$\sigma = \sum_{a} \int f_a(z, \mu_F^2) \hat{\sigma}_a \left(\alpha_s(\mu_R), \mu_F, \mu_R \right) dz + \mathcal{O}\left(\frac{\Lambda_{QCD}}{Q}\right)_{\text{Power corrections}}$$
PDFs Partonic cross section (perturbative)
$$\sigma_a = \sigma_a^{(0)} + \frac{\alpha_s}{2\pi} \sigma_a^{(1)} + \left(\frac{\alpha_s}{2\pi}\right)^2 \sigma_a^{(2)} + \left(\frac{\alpha_s}{2\pi}\right)^3 \sigma_a^{(3)} + \dots$$
LO NLO NNLO N3LO
• Accurate predictions require refinement of both perturbative

and non-perturbative pieces

• Perturbative convergence depends on scale, observable, phase space region, etc.



Inclusive observables!!



- Important corrections in differential observables as new regions of phase space become available
- At higher orders uncertainties can still be larger than experimental errors (HERA)

- Reduced scale dependence
- Residual dependence on μ_R and μ_F provides an estimate of the missing higher order corrections
- Reliable predictions in regions where there is good convergence

Currie, Gehrmann, Glover, Huss, Niehues, Vogt (2018)



- New channels may become available at higher orders (e.g, gluons in DIS)
- Parton luminosity can provide large correction (interplay with non-perturbative PDFs)
- QCD jet acquire structure at higher orders
- Better matching with experiments as more partons are considered



Currie, Gehrmann, Glover, Huss, Niehues, Vogt (2018)

HIGH ORDER JET CALCULATIONS IN POLARIZED DIS

Theory status for **polarized** jet production in DIS:

- Not much interest in fixed-target experiments
- NLO single jet production (polarized N-jetiness)

Boughezal, Petriello, Xing (2018)

• NLO dijet production (polarized dipole subtraction)

Photon - Borsa, De Florian, IP (2020) NC and CC - Borsa, De Florian, IP (2021)

• NNLO single jet production (polarized dipoles + P2B)

Photon - Borsa, De Florian, IP (2020) NC and CC - Borsa, De Florian, IP (in preparation)

SUBTRACTION METHODS

Beyond LO, IR singularities that arise in virtual contributions are cancelled against those from real emission diagrams (KNL Theorem)



This only gets worse beyond NLO due to overlapping singularities and mixed real-virtual contributions!

The main idea of **subtraction methods** is to extract the singularities without performing the full integration over the phase space of the real emission processes

DIPOLE SUBTRACTION (NLO)

One of the **general** NLO subtraction methods. The goal is to use a counterterm A that both

- Reproduces IR divergent behaviour of the real emission
- Is simple enough to be analytically integrated to cancel the IR divergences of the virtual contribution

$$\sigma^{NLO} = \int_{m+1} \left[\left(d\sigma^R \right)_{\epsilon=0} - \left(d\sigma^A \right)_{\epsilon=0} \right] + \int_m \left[d\sigma^V + \int_1 d\sigma^A \right]_{\epsilon=0}$$

The counterms are **process independent**, and are based on the factorization formulae:

$$d\sigma^A = \sum_{\text{dipoles}} d\sigma^B \otimes dV_{\text{dipole}}$$

Catani, Seymour (1996)



POLARIZED DIPOLE SUBTRACTION (NLO)

One of the **general** NLO subtraction methods. The goal is to use a counterterm A that both

- Reproduces IR divergent behaviour of the real emission
- Is simple enough to be analytically integrated to cancel the IR divergences of the virtual contribution

$$\sigma^{NLO} = \int_{m+1} \left[\left(d\sigma^R \right)_{\epsilon=0} - \left(d\sigma^A \right)_{\epsilon=0} \right] + \int_m \left[d\sigma^V + \int_{\Gamma} \frac{d\sigma^A}{d\sigma^A} \right]_{\epsilon=0}$$

The counterms are **process independent**, and are based on the factorization formulae: Differences only

$$d\Delta\sigma^A = \sum_{\text{dipoles}} d\Delta\sigma^B \otimes dV_{\text{dipole}}$$

Catani, Seymour (1996) - Borsa, De Florian, IP (2020)



HIGH ORDER JET CALCULATIONS IN POLARIZED DIS

	Inclusive cross section	Single-Jet (Lab Frame)	Di-jet (Breit Frame)	22
$lpha_S^0$	$q\gamma^* o q$	$q\gamma^* \to q$		7
$lpha_S^1$	$q\gamma^* \rightarrow q$ 1 loop $q\gamma^* \rightarrow qg$ $g\gamma^* \rightarrow q\bar{q}$ NI	$q\gamma^* \to q 1 \text{ loop} \\ q\gamma^* \to qg \\ g\gamma^* \to q\bar{q}$	$\begin{array}{c} q \gamma^* ightarrow q g \\ g \gamma^* ightarrow q ar q \end{array}$	Kanna Journee
α_S^2	$\begin{array}{ccc} q\gamma^* \to q & 2 \operatorname{loops} \\ q\gamma^* \to qg & 1 \operatorname{loop} \\ g\gamma^* \to q\bar{q} & 1 \operatorname{loop} \\ q\gamma^* \to qgg \\ q\gamma^* \to qgg \\ q\gamma^* \to qq\bar{q} \\ g\gamma^* \to q\bar{q}g \end{array} \qquad $	$q\gamma^* \rightarrow q 2 \text{ loops}$ $q\gamma^* \rightarrow qg 1 \text{ loop}$ $g\gamma^* \rightarrow q\bar{q} 1 \text{ loop}$ $q\gamma^* \rightarrow qgg$ $q\gamma^* \rightarrow qq\bar{q}$ $g\gamma^* \rightarrow qq\bar{q}$	$\begin{array}{ccc} q\gamma^* \to qg & 1 \ \text{loop} \\ g\gamma^* \to q\bar{q} & 1 \ \text{loop} \\ q\gamma^* \to qgg \\ q\gamma^* \to qq\bar{q} \\ g\gamma^* \to q\bar{q}g \\ g\gamma^* \to q\bar{q}g \end{array}$	Conservation Conse

(From Borsa)

HIGH ORDER JET CALCULATIONS IN POLARIZED DIS

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α_S^2	$\begin{array}{ccc} q\gamma^* \to q & 2 \operatorname{loops} \\ \overline{q\gamma^* \to qg} & 1 \operatorname{loop} \\ g\gamma^* \to q\bar{q} & 1 \operatorname{loop} \\ q\gamma^* \to qgg \\ q\gamma^* \to qgg \\ q\gamma^* \to qq\bar{q} \\ g\gamma^* \to q\bar{q}g \end{array} $	$\begin{array}{ccc} q\gamma^* \to q & 2 \operatorname{loops} \\ q\gamma^* \to qg & 1 \operatorname{loop} \\ g\gamma^* \to q\bar{q} & 1 \operatorname{loop} \\ q\gamma^* \to qgg \\ q\gamma^* \to qgg \\ q\gamma^* \to qq\bar{q} \\ \textbf{LO} & g\gamma^* \to q\bar{q}g \end{array}$	$\begin{array}{ccc} q\gamma^* \to qg & 1 \ \text{loop} \\ g\gamma^* \to q\bar{q} & 1 \ \text{loop} \\ q\gamma^* \to qgg \\ q\gamma^* \to qq\bar{q} \\ g\gamma^* \to qq\bar{q} \\ g\gamma^* \to q\bar{q}g \end{array}$	Leese and Leese Le

(From Borsa)

NNLO - PROJECTION TO BORN (P2B)

P2B provides the **fully differential** cross section of an observable given that we know

- The inclusive cross section at that order
- The exclusive cross section of that observable + 1 jet at one order below



Cacciari, Dreyer, Karlberg, Salam, Zanderighi (2015)

NNLO - PROJECTION TO BORN (P2B)



NNLO - PROJECTION TO BORN (P2B)

IN OUR CASE:

We compute the polarized **NNLO cross section for 1-jet**, using our <u>NLO calculation for 2-jets</u> (<u>dipoles</u>) and the <u>NNLO inclusive</u> <u>cross sections</u> that are already available



$$d\sigma_{1jet}^{\text{NNLO}} = d\sigma_{2jet}^{\text{NLO}} - d\sigma_{2jet,\text{P2B}}^{\text{NLO}} + d\sigma_{1jet}^{\text{NNLO, incl}}$$
Dipoles van Neerven, Zijlstra (1994)

NLO DIJETS IN POLARIZED DIS (BREIT FRAME)

 $xp = (\frac{Q}{2}, 0, 0, \frac{Q}{2})$ EIC KINEMATICS: Ep = 275 GeV q = (0, 0, 0, -Q)Fe = 18 GeV $(\frac{Q}{2}, 0, 0, -\frac{Q}{2})$ KINEMATICAL CUTS: $p_{T,1}^B > 5 \text{ GeV},$ 0.2 < y < 0.6, $p_{T,2}^B > 4 \text{ GeV},$ $25\,{\rm GeV}^2 < Q^2 < 2500\,{\rm GeV}^2$ $|\eta^L| < 3.5,$ DSSV14 MC (polarized) - PDF4LHC15 (unpolarized) NLO PDFs: SCALES: $\mu_F^2 = \mu_R^2 = \frac{1}{2}(Q^2 + \langle p_T^B \rangle_2^2) \equiv \mu_0^2$ (dynamical) JET ALGORITHM: anti-Kt, R = 0.8

Asymmetrical Pt cuts to improve perturbative stability!

$$M_{12} = \sqrt{(p_1 + p_2)^2} \qquad \eta^* = \frac{1}{2} |\eta_1^B - \eta_2^B|$$
$$\langle p_T \rangle_2 = \frac{1}{2} (p_{T,1}^B + p_{T,2}^B) \qquad \xi_2 = x(1 + \frac{M_{12}^2}{Q^2})$$

UNPOLARIZED CASE

- Significant NLO corrections (K factors above 1.5)
- Strong scale dependence (7point variation)
- Perturbative instabilities due to regions of phase space forbidden at LO (M12 > 10 GeV)



$$M_{12} = \sqrt{(p_1 + p_2)^2} \qquad \eta^* = \frac{1}{2} |\eta_1^B - \eta_2^B|$$

$$\langle p_T \rangle_2 = \frac{1}{2} (p_{T,1}^B + p_{T,2}^B) \qquad \xi_2 = x(1 + \frac{M_{12}^2}{Q^2})$$

POLARIZED CASE

- Significant NLO corrections
- Strong scale dependence (can be bigger than PDFs errors!)
- Perturbative instabilities due to forbidden regions at LO
- Different shape/size of corrections respect to the unpol case (see asymmetries)
- Shift in dijet momentum fraction



$$\begin{split} M_{12} &= \sqrt{(p_1 + p_2)^2} & \eta^* = \frac{1}{2} |\eta_1^B - \eta_2^B \\ \langle p_T \rangle_2 &= \frac{1}{2} (p_{T,1}^B + p_{T,2}^B) & \xi_2 = x (1 + \frac{M_{12}^2}{Q^2}) \end{split}$$

POLARIZED CASE

- Cancellation between quark and gluon channels at low Q2
- Also, there is a shift in the quark contribution at low Q2
- Good perturbative convergence at high Q2



$$M_{12} = \sqrt{(p_1 + p_2)^2} \qquad \eta^* = \frac{1}{2} |\eta_1^B - \eta_2^B|$$

$$\langle p_T \rangle_2 = \frac{1}{2} (p_{T,1}^B + p_{T,2}^B) \qquad \xi_2 = x(1 + \frac{M_{12}^2}{Q^2})$$

ASYMMETRIES

- Reduction in double spin asymmetries due to quark-gluon channel cancellation, particularly in pseudorapidity distribution
- Shift in dijet momentum fraction



• EW boson introduce vector and axial couplings

$$-ie \gamma^{\mu} \left(C_V + C_A \gamma^5 \right)$$

• In the case of neutral currents, we also have Z/photon interference

The presence of γ^5 in the HVBM scheme of dimensional regularization adds further complications:

VERTEX SYMMETRIZATION IN D-DIMENSIONS

$$-ie\left(C_V + C_A \gamma^5\right) \rightarrow -ie\left(C_V \gamma^{\mu} + C_A \tilde{\gamma^{\mu}} \gamma^5\right)$$

FINITE SUBTRACTION DUE TO UV DIVERGENCES

$$(\Delta)C_T = \alpha_s \ 4C_F \ d(\Delta)\hat{\sigma}_{\text{axial}}^{\text{LO}}$$

The possible results of the differents fermion traces depend only on whether there is an odd or even number of $~\gamma^5$

- Trivial in real emission diagrams (4-dimensional)
- Only valid in virtual diagrams after symmetrization and finite subtraction (d-dimensional)

Since spin projectors also add γ^5 , we can reuse polarized matrix elements for unpolarized parity violating pieces (PV), and vice versa!





 $\hat{\sigma}_q = \hat{\sigma}_q^{PV} + \hat{\sigma}_q^{NPV}$

VALID FOR $q+W/Z \rightarrow q, q+W/Z \rightarrow q+g \text{ and } q+W/Z \rightarrow q+g+g$ (up to NNLO)

AND THE GLUON CHANNELS?



No analogous relation for polarized NPV gluon channel. **However, PV terms with initial gluon cancel due to charge conjugation arguments** (antisymmetric in quark-antiquark crossing)

SPECIAL CASE - TRIANGLE DIAGRAMS



Triangles only in Z exchange, but they cancel out if the two members of each weak isospin doublet are considered

Also, in the particular 4 quark channel we can use properties similar to those of the previous slides, depending on each particular case $q + W/Z \rightarrow q + q' + \bar{q'}$

NLO DIJETS IN DIS (NEUTRAL CURRENTS)

$$M_{12} = \sqrt{(p_1 + p_2)^2} \qquad \eta^* = \frac{1}{2} |\eta_1^B - \eta_2^B|$$

$$\langle p_T \rangle_2 = \frac{1}{2} (p_{T,1}^B + p_{T,2}^B) \qquad \xi_2 = x(1 + \frac{M_{12}^2}{Q^2})$$

UNPOLARIZED CASE

- Contribution of the Z boson in very small, and comes mainly due to interference with photon
- 10% only at Q2 ~ 2000 GeV
- Q2 does not reach high enough values at EIC for Z



NLO DIJETS IN DIS (NEUTRAL CURRENTS)

$$M_{12} = \sqrt{(p_1 + p_2)^2} \qquad \eta^* = \frac{1}{2} |\eta_1^B - \eta_2^B|$$

$$\langle p_T \rangle_2 = \frac{1}{2} (p_{T,1}^B + p_{T,2}^B) \qquad \xi_2 = x(1 + \frac{M_{12}^2}{Q^2})$$

POLARIZED CASE

- Stronger contribution in polarized cross section due to channel cancellation
- Parity violating pieces only in quark channel
- This overall improves the asymmetries (~10%), but mainly at high Q2 and



NLO DIJETS IN DIS (CHARGED CURRENTS)

$$M_{12} = \sqrt{(p_1 + p_2)^2} \qquad \eta^* = \frac{1}{2} |\eta_1^B - \eta_2^B|$$

$$\langle p_T \rangle_2 = \frac{1}{2} (p_{T,1}^B + p_{T,2}^B) \qquad \xi_2 = x(1 + \frac{M_{12}^2}{Q^2})$$

UNPOLARIZED CASE

- Massive propagator suppression at low Q2
- Q2 and dijet momentum fraction are related
- Same perturbative instabilities as in photon exchange



NLO DIJETS IN DIS (CHARGED CURRENTS)

$$M_{12} = \sqrt{(p_1 + p_2)^2} \qquad \eta^* = \frac{1}{2} |\eta_1^B - \eta_2^B|$$
$$\langle p_T \rangle_2 = \frac{1}{2} (p_{T,1}^B + p_{T,2}^B) \qquad \xi_2 = x(1 + \frac{M_{12}^2}{Q^2})$$

POLARIZED CASE

- Polarized x-sec not as suppressed compared to NC
- Parity-violating piece of x-sec is more relevant (due to couplings)



NLO DIJETS IN DIS (CHARGED CURRENTS)



NNLO SINGLE JET IN POLARIZED DIS (LAB FRAME)

EIC KINEMATICS: Ep

$$Ep = 275 \text{ GeV}$$

$$Ee = 18 \text{ GeV}$$

 $075 0 \cdot 1/$

Lab Frame needed for P2B!

KINEMATICAL CUTS:

 $\begin{array}{ll} 0.04 < y < 0.95, & 5 \, {\rm GeV} < p_T^L < 36 \, {\rm GeV}, \\ 25 \, {\rm GeV}^2 < Q^2 < 1000 \, {\rm GeV}^2 & |\eta^L| < 3, \end{array}$

NLO PDFs:

DSSV14 MC (polarized) - PDF4LHC15 (unpolarized)

SCALES:

JET ALGORITHM:

 $\mu_F^2 \;=\; \mu_R^2 \;=\; Q^2 \;\equiv\; \mu_0$

anti-Kt, R = 0.8

NLO SINGLE JET IN DIS (PHOTON)

POLARIZED CASE

- Improved convergence at NNLO (K-factors)
- Shift towards larger rapidities and lower Pt, as the emission of extra partons populates those regions
- Strong scale dependence at low Q2 and x due to kinematical cuts in Pt and y
- This is further enhanced in the polarized case due to channel cancellations



NLO SINGLE JET IN DIS (PHOTON)

Asymmetries

- Cancellations in the polarized cross section lead to small asymmetries (~ 2%)
- Significant corrections in the asymmetries, even at NNLO

$$A_{LL} = \frac{\Delta \sigma}{\sigma}$$



PARITY VIOLATING STRUCTURE FUNCTION (P2B)

The F_3 unpolarized structure functions is known to NNLO (van Neerven, Zijlstra (1992)), but the polarized equivalent g_4 and g_5 are not available

We get the NNLO g_4 and g_5 from F_2 and F_1 due to the previous arguments. Initial gluon contributions are not a problem since they cancel out, and we can safely ignore Z triangle terms

$$\begin{split} W^{i}_{\mu\nu} &= \left(-g_{\mu\nu} + \frac{q_{\mu}q_{\nu}}{q^{2}}\right) \left[F^{i}_{1}(x,Q^{2}) - \frac{h}{2} \ g^{i}_{5}(x,Q^{2})\right] \\ &+ \frac{\left(p_{\mu} - \frac{p \cdot q}{q^{2}}q_{\mu}\right) \left(p_{\nu} - \frac{p \cdot q}{q^{2}}q_{\nu}\right)}{p \cdot q} \left[F^{i}_{2}(x,Q^{2}) - \frac{h}{2} \ g^{i}_{4}(x,Q^{2})\right] \\ &- i\epsilon_{\mu\nu\alpha\beta} \frac{q^{\alpha}p^{\beta}}{2p \cdot q} \left[F^{i}_{3}(x,Q^{2}) + h \ g^{i}_{1}(x,Q^{2})\right], \end{split}$$

$$\begin{split} L_{\gamma}^{\mu\nu} &= 2 \left(-k \cdot k' g^{\mu\nu} + k^{\mu} k'^{\nu} + k'^{\mu} k^{\nu} - i \lambda \epsilon^{\mu\nu\alpha\beta} k_{\alpha} k'_{\beta} \right), \\ L_{z}^{\mu\nu} &= \left(g_{V}^{e} + e \lambda g_{A}^{e} \right)^{2} L_{\gamma}^{\mu\nu}, \\ L_{\gamma/z}^{\mu\nu} &= \left(g_{V}^{e} + e \lambda g_{A}^{e} \right) L_{\gamma}^{\mu\nu}, \\ L_{W}^{\mu\nu} &= \left(1 + e \lambda \right)^{2} L_{\gamma}^{\mu\nu}, \end{split}$$

NNLO SINGLE JET IN DIS (NEUTRAL CURRENTS)

UNPOLARIZED CASE

 Contribution of the Z boson in very small, and comes mainly due to interference with photon

 Overall good convergence of the perturbative series



NNLO SINGLE JET IN DIS (NEUTRAL CURRENTS)

POLARIZED CASE

- Enhanced contribution at high Q2, x and pt
- This enhancement translated into spin asymmetries



NNLO SINGLE JET IN DIS (CHARGED CURRENTS)

UNPOLARIZED CASE

- Massive propagator suppression at low Q2
- Pt^2 in proportional to Q2 at LO, leading to large corrections
- Shifted towards higher x and Q2



NNLO SINGLE JET IN DIS (CHARGED CURRENTS)

POLARIZED CASE

- Massive propagator suppression at low Q2
- Pt² in proportional to Q2 at LO, leading to large corrections
- Shift towards higher values of Q2, x, pt and rapidity when compared to unpolarized case



SUMMARY

• Higher order corrections are fundamental piece in the high precision description of observables, and they will be instrumental in the description of proton spin.

We presented:

- NNLO calculation of polarized single-jet production, in both Neutral and Charged Current DIS.
- As an ingredient of the P2B method, we also calculated the NLO dijet production in both processes.
- Increased perturbative convergence, but still showing sizable corrections and scale dependance.
- Sizable correction to asymmetries (no cancellation of higher order effects)

YOU CAN NOW GO GRAB A COFFEE



NLO DIJETS IN DIS (NEUTRAL CURRENTS)



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Asymmetries



Asymmetries

