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Exotic Heavy Meson Spectroscopy and Strucutre with EIC – August 15, 2022 – Stony Brook



BEPCII @ IHEP

electron-positron collider $E_{cm} = 2 - 4.95 \text{ GeV}$ Luminosity = $10^{33} \text{ cm}^{-2}\text{s}^{-1}$

BESIII @ BEPCII



BESIII Datasets





 $\left(4\right)$

Outline of the results

- Z states:
 - Charged Z_{cs}
 - Neutral Z_{cs}

- X states:
 - Search for X(3872) $\rightarrow \pi^{_0}\chi_{_{c0}}$
 - χ_{c1} direct production

- Y states:
 - ψ(3823)
 - $\pi^+\pi^-D\overline{D}$ and ψ(3843) new
 - π⁺π⁻ψ(2S)
 - K^+K^-J/ψ
 - $\pi^+\pi^-J/\psi$
 - Open charm final states
 - Light hadron final states

And one search on the connection among these states



Search for "strange" partner of the Z_c(3900)

Discovered in the process $e^+e^- \rightarrow K^+(D_sD^* + D^*_sD)$ by studying the K⁺ recoil mass

$$\mathcal{F}_{j}(M) \propto \left| \frac{\sqrt{q \cdot p_{j}}}{M^{2} - m_{0}^{2} + im_{0}(f\Gamma_{1}(M) + (1 - f)\Gamma_{2}(M))} \right|^{2}$$

$$j = 1 \rightarrow Z_{cs} \rightarrow D_{s}D^{*}; j = 2 \rightarrow Z_{cs} \rightarrow D^{*}_{s}D^{*}$$

$$m_{\text{pole}}[Z_{cs}(3985)^{-}] = (3982.5^{+1.8}_{-2.6} \pm 2.1) \text{ MeV}/c^2,$$

 $\Gamma_{\text{pole}}[Z_{cs}(3985)^{-}] = (12.8^{+5.3}_{-4.4} \pm 3.0) \text{ MeV}.$

(one of the) First candidate of open strangeness charged exotic





Neutral partner of Z_{cs} (3985) useful to assess their nature

Studied with partial reconstruction method in K₂ recoil mass

$$\begin{split} R &= \left| \frac{1}{M^2 - m_0^2 + im_0(f \cdot \Gamma_1(M) + (1 - f) \cdot \Gamma_2(M))} \right|^2 \\ R_1 &= R \cdot q \cdot p_1, \\ R_2 &= R \cdot q \cdot p_2, \\ \Gamma_1(M) &= \Gamma_0 \cdot \frac{p_1}{p_1^*} \cdot \frac{m_0}{M}, \\ \Gamma_2(M) &= \Gamma_0 \cdot \frac{p_2}{p_2^*} \cdot \frac{m_0}{M}, \end{split}$$

Evidence at 4.6 σ level. Compatible with isospin predictions

			Mass (MeV/c^2)	Widt	h (MeV)	
	$Z_{cs}(3$	$(985)^0$	3992.2 =	$\pm 1.7 \pm 1.6$	7.7^{+2}_{-3}	$\frac{4.1}{3.8} \pm 4.3$	
	$Z_{cs}(3$	$985)^{+}$	3985.2	$^{+2.1}_{-2.0} \pm 1.7$	13.8^{+}_{-}	$\frac{18.1}{5.2} \pm 4.9$	
-							
\sqrt{s} ((MeV)	$\bar{K}^0 Z_c$	$\sigma^{ m Born} imes$	\mathcal{B} (pb) $_{K^{-}Z_{cs}(398)}$	$_{_{35)}+} \lambda$	$\chi^2 \chi^2_{ m total}$	/ndf
4	628	4.4^{+2}_{-2}	$^{.6}_{.2}\pm2.0$	$0.8^{+1.2}_{-0.8} \pm$	$0.6\ 1$.2	
4	641	0.0^{+1}_{-0}	$\frac{16}{10} \pm 0.2$	$1.6^{+1.2}_{-1.1} \pm$	1.3 0	.5	
4	661	2.8^{+1}_{-1}	$\frac{18}{16} \pm 0.6$	$1.6^{+1.3}_{-1.1} \pm$	0.8 0	.3 5.1	$^{\prime}5$
4	682	2.2^{+1}_{-1}	$\frac{12}{10} \pm 0.8$	$4.4^{+0.9}_{-0.8} \pm$	1.4 1	.0	
4	699	7.0^{+2}_{-2}	$\frac{12}{10} \pm 1.8$	$2.4^{+1.1}_{-1.0} \pm$	$1.2 \ 2$.1	



New ψ_2 (3823) decay mode

PRD 103 (2021) 9, L091102

Search for additional experimental evidence of $\psi_2(3823)$ to confirm its status of $\psi_2(1^3D_2)$ in $e^+e^- \rightarrow \pi^+\pi^-\psi_2(3823)$

Based on 19 fb⁻¹ between 4.1 and 4.7 GeV

Channel	$N^{\psi_2(3823)}$	$\frac{\mathcal{B}(\psi_2(3823) \to \dots)}{\mathcal{B}(\psi_2(3823) \to \gamma \chi_{c1})}$
$\gamma\chi_{c1}$	63.1 ± 8.5	
$\gamma\chi_{c2}$	$8.8^{+4.3}_{-3.4}$	$0.28^{+0.14}_{-0.11} \pm 0.02$
$\pi^+\pi^- J/\psi$	< 21.0	< 0.06
$\pi^0\pi^0 J/\psi$	< 10.0	< 0.11
$\eta J/\dot{\psi}$	< 9.8	< 0.14
$\pi^0 J/\psi$	< 5.6	< 0.03
$\gamma\chi_{c0}$	< 6.3	< 0.24

Consistent with theoretical prediction Lower than theoretical prediction

PRD 55, 4001 (1997), PRL 89, 162002 (2002), PRD 67, 014027 (2003), PRD 69, 054008 (2004), PRD 72, 054026 (2005), PRD 79, 094004 (2009), Front. Phys. 11, 11402 (2016), PRD 95, 034026 (2017), Int. J. Mod. Phys. A 32, 1750035 (2017)

Search for ψ_2 (3823) and ψ_3 (3842) production mode



Search for new production mode of $\psi_{_2}$ and $\psi_{_3}$ can help to establish their nature

Evidence of $\pi^0\pi^0\psi_2(3823)$, $\psi_2(3823) \rightarrow \gamma\chi_{c1}$. Ratio with charged pions mode confirms isospin simmetry.

$$\frac{\sigma(e^+e^- \to \pi^0 \pi^0 \psi_2(3823))}{\sigma(e^+e^- \to \pi^+ \pi^- \psi_2(3823))} = (0.64^{+0.22}_{-0.20} \pm 0.05)$$

No signal of $\pi^+\pi^-\psi_3$ (3842)

$\pi \pi \psi_2$ (3823) lineshape and ψ_2 (3823) mass



 $M[\psi_2(3823)] = 3823.12 \pm 0.43 \pm 0.13 \text{ MeV}/c^2$

U.L. width (< 2.9 MeV) will help constrains potential models

Study the internal structure of Y states by measuring their coupling with D-wave charmonia

 ψ_2 (3823) candidates reconstructed in $\gamma \chi_{c1.2}$

Parameters	Solution I	Solution II
$M[R_1]$	4406.9 \pm	17.2 ± 4.5
$\Gamma_{ m tot}[R_1]$	128.1 ± 3	37.2 ± 2.3
$\Gamma_{\mathrm{e^+e^-}}\mathcal{B}_1^{R_1}\mathcal{B}_2$	$0.36 \pm 0.10 \pm 0.03$	$0.30 \pm 0.09 \pm 0.03$
$M[R_2]$	$4647.9 \pm$	8.6 ± 0.8
$\Gamma_{ m tot}[R_2]$	33.1 ± 1	8.6 ± 4.1
$\Gamma_{\mathrm{e^+e^-}}\mathcal{B}_1^{R_2}\mathcal{B}_2$	$0.24 \pm 0.07 \pm 0.02$	$0.06 \pm 0.03 \pm 0.01$
ϕ	$267.1 \pm 16.2 \pm 3.2$	$-324.8 \pm 43.0 \pm 5.7$

Two resonances hypothesis favored:

- to single resonance by 2.6σ
- to only continuum one by more than 50

Second largest BF of Y(4660)

ππDD lineshape

ArXiv: 2203.05815

Study the 4-body final state to search for clues about vector resonance in the region 4-4.7 GeV. 3 subprocesses (PHSP, $\pi\pi\psi(3770)$, D₁(2420)D)

Fit to 37 energy values. Partial reconstruction method (one $D \rightarrow K\pi\pi$, one in recoil mass).



Evidence of $\pi\pi\psi_3$ (3843)

ArXiv: 2203.05815

Search for spin-3 partner of $\psi(3770)$ and $\psi(3823)$ in its DD decay. More stringent requirements on the selection criteria



Signal shape extracted using $e^+e^- \rightarrow f_0(500)\psi(3843)$ MC

Combining all dataset in 4.6-4.7 GeV evidence of $\pi\pi\psi$ (3843) at 4.2 σ level

$e^+e^- \rightarrow \pi\pi\psi(2S)$

PRD 104 (2021) 5, 052012

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Extension of a previous work (PRD 96, 032004 (2017))

New measurement up to 4.7 GeV, with addition of new final state.

Confirmed both Y(4220) and Y(4390) contribution

First observation of Y(4660) at BESIII thanks to the center of mass upgrade!

BaBar: PRD 89, 111103 (2014) Belle: PRD 91, 112007 (2015)

Y(4220) - Y(43xx) - Y(4660) PRD 10

PRD 104 (2021) 5, 052012



Status of the Y(4220)/Y(43xx) measurements

As observed in ππψ(2S) Belle: PRD 91, 142002 (2007) BaBar: PRD 89, 111103 (2014)

New structures in $e^+e^- \rightarrow KKJ/\psi$ cross section

ArXiv: 2204.07800

First observation of Y(4230) in KKJ/ψ

$$0.02 < \frac{\mathcal{B}(Y(4230) \to K^+ K^- J/\psi)}{\mathcal{B}(Y(4230) \to \pi^+ \pi^- J/\psi)} < 0.26$$

New structure Y(4500) observed for first time!

Y(4500) compatible with: - 5S/4D mixing

- $D_{t}\overline{D}_{t}$ hadronic molecule
- lattice ccss structure

	15 (Gev)	(Gev)		
	Parameters	Solution I	Solution II	
	$M({ m MeV})$	4225.3 ± 2	2.3 ± 21.5	
Y(4230)	$\Gamma_{tot}({ m MeV})$	$72.9 \pm 6.$	$.1 \pm 30.8$	
	$\Gamma_{ee}\mathcal{B}(\mathrm{eV})$	$0.42 \pm 0.04 \pm 0.15$	$0.29 \pm 0.02 \pm 0.10$	
	$M({ m MeV})$	4484.7 ± 1	3.3 ± 24.1	
Y(4500)	$\Gamma_{tot}({ m MeV})$	111.1 ± 30	0.1 ± 15.2	
	$\Gamma_{ee}\mathcal{B}(eV)$	$1.35 \pm 0.14 \pm 0.06$	$0.41 \pm 0.08 \pm 0.13$	
phase angle	$\varphi(\mathrm{rad})$	$1.72 \pm 0.09 \pm 0.52$	$5.49 \pm 0.35 \pm 0.58$	



Update of $e^+e^- \rightarrow \pi \pi J/\psi$

arXiv:2206.08554

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Update of previous measurements with a total of 23/fb between 3.77 and 4.70 GeV



Clear observation of two resonances. Data around 4. GeV favor BW rather than exponential parametrization. Large flactuation at 3.8713 - X(3872)



Update of

 $e^+e^- \rightarrow \pi\pi J/\psi - II_{arXiv:2206.08554}$

Fit with a third resonance yields to a better description of the data.

Tested four models: (a) free \rightarrow solution compatible with ψ (4415) (b) free \rightarrow solution compatible with Y(4500) (c) fixed to ψ (4415) (d) fixed to Y(4500)

Impact on "known" resonances: - Stable results for Y(4220) - Large differences for Y(4320)

More data are needed in the 4.4 – 4.6 GeV region

PRD 104 (2021) 032012



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JHEP 2022, 155 (2022)



 $e^+e^- \rightarrow D^*D^{(*)}$

15.7 fb $^{\mbox{-}1}$ collected between 4.085 and 4.6 GeV

Reconstructed $D^{*+} \rightarrow \pi^+ D^0$ and $D^0 \rightarrow K^-\pi^+$.

D^{(*)-} inferred kinematically

Good agreement with existing measurements

Confirmed structure at 4.39 GeV in D^*D^*

Results can provide information to improve Eur. Phys. J. C81 (2021) 83



XYZ to light hadrons: $e^+e^- \rightarrow$ hadrons

PRD 104 (2021) 11, 112009

At present, charmonium(-like) states above 4 GeV has not been observed decaying into light hadrons.

BESIII reports a list of additional final state useful to add information



Evidence of $\psi(4040) \rightarrow 5\pi$ at 3.6 σ significance Presented also upper limits for Y(4220)

Mass and width fixed to PDG

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XYZ to light hadrons: $e^+e^- \rightarrow \Lambda \overline{\Lambda}$



First evidence of $\psi(3770) \rightarrow \Lambda\overline{\Lambda}$ decay, BF at least one order of magnitude larger than predicted.

Only U.L. for other charmonium-like states

Study of charmonium-like decay to baryons provide insight:

- on the resonances nature
- on the electromagnetic structure of the baryons

Predictions based on scaling as electronic coupling gives $B \sim 5 \times 10^{-7}$ at $\psi(3770)$



Search for X(3872) $\rightarrow \pi^{0}\chi_{c0}$ and X(3872) $\rightarrow \pi\pi\chi_{c0}$

To understand the nature of X(3872), verify prediction to test the *charmonium-ness* of the state

Ratio	Central Value (Upper Limit)
$\frac{\mathcal{B}(X(3872) \to \pi^0 \chi_{c0})}{\mathcal{B}(X(3872) \to \pi^+ \pi^- J/\psi)}$	$1.70^{+0.55}_{-0.75} \pm 0.40 \; (3.6)$
$\frac{\mathcal{B}(X(3872) \to \pi^0 \chi_{c0})}{\mathcal{B}(X(3872) \to \pi^0 \chi_{c1})}$	$1.9^{+1.2}_{-0.7} \pm 0.5 \ (4.4)$
$\frac{\mathcal{B}(X(3872) \rightarrow \pi^+\pi^-\chi_{c0})}{\mathcal{B}(X(3872) \rightarrow \pi^+\pi^-J/\psi)}$	$0.06^{+0.24}_{-0.23} \pm 0.12 \ (0.68)$
$\frac{\mathcal{B}(X(3872) \to \pi^0 \pi^0 \chi_{c0})}{\mathcal{B}(X(3872) \to \pi^+ \pi^- J/\psi)}$	$-0.55^{+0.53}_{-0.42} \pm 0.33 \ (1.7)$

Using also PRL122 202001 (2019)

Upper limits (90% C.L.) still not conclusive. New statistics will be collected with BEPCII-U



$\chi_{c1}(1P)$ direct production

ArXiv: 2203.13782



Similar approach for X(3872). Paper in preparation! Study of $e^+e^- \rightarrow \gamma J/\psi$ to extract interference pattern

First observation (5 σ) of χ_{c1} direct production at e⁺e⁻ collider



Electronic width same order of magnitude with theoretical calculation



Connections

The process $e^+e^- \rightarrow \pi^0 Z_c$; $Z_c \rightarrow \gamma X(3872)$ can be useful:

- Study connections among the XYZ states

- Improve the measurement of the X(3872) mass, as proposed in PRD 102, 114041 (2020)



BEPCII-U

Chin.Phys.C 44 (2020) 4, 040001



Accelerator upgrade:

- center of mass maximum energy up to 5.6 GeV

- 3 times the present luminosity in XYZ region

Planned in 2024 with also new inner tracker based on cylindrical GEM



Additional Materials

Update of $e^+e^- \rightarrow \pi\pi J/psi$





Parameter	Solution I	Solution II	Solution III	Solution IV
$\Gamma^{\rm ee}_{3770}\mathcal{B}(R_{3770})$		0.6 ± 0.1	(0.3 ± 0.1)	
$M(R_0)(p_0)$		3905.5 ± 30	$0.1 (4.4 \pm 0.3)$	
$\Gamma_0^{\rm tot}(R_0)(p_1)$		346.0 ± 48.5 ((2)	$2.7 \pm 0.6) \times 10^{-3}$)	
$\Gamma_0^{\rm ee} \mathcal{B}(R_0)$	5.5 ± 0.5 ()	6.9 ± 0.7 ()	$8.3 \pm 0.6 ()$	10.5 ± 0.9 ()
$M(R_1)$		4221.4 ± 1.5	(4220.1 ± 1.2)	
$\Gamma_1^{\rm tot}(R_1)$		41.8 ± 2.9	(43.6 ± 2.6)	
$\Gamma_1^{\rm ee}\mathcal{B}(R_1)$	$1.7 \pm 0.2 \; (1.7 \pm 0.2)$	$8.2 \pm 0.9 \ (8.6 \pm 0.5)$	$3.0 \pm 0.5 \; (2.5 \pm 0.3)$	$14.6 \pm 1.2 \ (12.7 \pm 0.8)$
$M(R_2)$		4297.5 ± 12.1	(4316.2 ± 12.4)	
$\Gamma_2^{\rm tot}(R_2)$		126.6 ± 16.7	(124.3 ± 18.0)	
$\Gamma_2^{\rm ee} \mathcal{B}(R_2)$	$1.2 \pm 0.3 \; (0.7 \pm 0.2)$	$2.3 \pm 0.8 \; (1.1 \pm 0.3)$	$15.6 \pm 2.1 \; (15.0 \pm 1.2)$	$30.2 \pm 3.3 \; (23.6 \pm 2.9)$
ϕ_1	$-3.7 \pm 5.4 \ (-24.3 \pm 3.0)$	$-124.6 \pm 11.7 \; (78.8 \pm 5.1)$	$87.7 \pm 21.9 \; (-88.0 \pm 12.1)$	$-33.5 \pm 11.2 \; (15.1 \pm 7.8)$
ϕ_2	$79.6 \pm 18.5 \; (106.4 \pm 16.5)$	$35.8 \pm 27.2 \; (-184.6 \pm 15.1)$	$-104.7\pm26.9\;(179.5\pm9.1)$	$-148.7\pm4.5\;(-112.5\pm6.2)$
χ^2/ndf		54.0/40) (57.3/41)	



Update of

$e^+e^- \rightarrow \pi\pi J/psi - II$

Parameter	Result I	Result II
$M(R_1)$	$4221.0 \pm 1.6~(4220.3 \pm 1.6)$	$4219.8 \pm 1.3 (4219.1 \pm 1.2)$
$\Gamma_1^{\rm tot}(R_1)$	$41.0\pm3.0~(42.3\pm3.0)$	$45.4 \pm 2.8 \ (46.3 \pm 2.5)$
$M(R_2)$	$4293.7 \pm 13.1~(4304.8 \pm 18.8)$	$4345.8 \pm 28.4 \ (4357.9 \pm 20.2)$
$\Gamma_2^{\rm tot}(R_2)$	$152.4 \pm 23.9 (144.3 \pm 31.5)$	$130.1\pm20.7(107.9\pm25.6)$
$M(R_2)$	$4405.6 \pm 4.5 (4405.0 \pm 6.7)$	$4471.1 \pm 36.2 \ (4550.9 \pm 16.9)$
$\Gamma_3^{\rm tot}(R_3)$	$9.1 \pm 2.5 \ (8.7 \pm 4.9)$	$159.7 \pm 97.0~(211.8 \pm 132.8)$
χ^2/ndf	40.1/36 (44.8/37)	47.6/36 (48.7/37)
Significance	$4.0\sigma (3.6\sigma)$	2.1σ (2.7 σ)
Parameter	Result III	Result IV
$\begin{tabular}{c} \hline Parameter \\ \hline M(R_1) \end{tabular}$	Result III 4223.9 ± 1.4 (4219.6 ± 1.3)	Result IV 4220.2 ± 1.3 (4219.4 ± 1.1)
$\begin{tabular}{ c c } \hline Parameter \\ \hline $M(R_1)$ \\ $\Gamma_1^{tot}(R_1)$ \\ \hline \end{tabular}$	Result III $4223.9 \pm 1.4 \ (4219.6 \pm 1.3)$ $42.2 \pm 3.2 \ (44.3 \pm 2.7)$	Result IV $4220.2 \pm 1.3 (4219.4 \pm 1.1)$ $44.5 \pm 2.9 (45.3 \pm 2.5)$
$\begin{tabular}{ c c c } \hline \hline Parameter \\ \hline $M(R_1)$ \\ \hline $\Gamma_1^{tot}(R_1)$ \\ \hline $M(R_2)$ \\ \hline \end{tabular}$	Result III 4223.9 ± 1.4 (4219.6 ± 1.3) 42.2 ± 3.2 (44.3 ± 2.7) 4308.5 ± 17.6 (4333.2 ± 23.2)	Result IV $4220.2 \pm 1.3 \ (4219.4 \pm 1.1)$ $44.5 \pm 2.9 \ (45.3 \pm 2.5)$ $4328.58 \pm 18.9 \ (4347.1 \pm 14.5)$
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