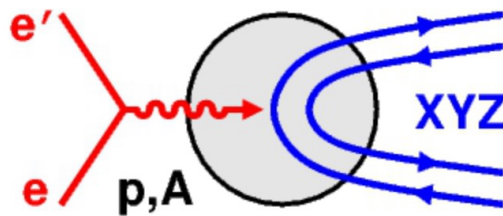


Inclusive productions of hidden/double-charm states at electron-proton facilities

Feng-Kun Guo

Institute of Theoretical Physics, CAS



Exotic heavy meson spectroscopy and structure with EIC

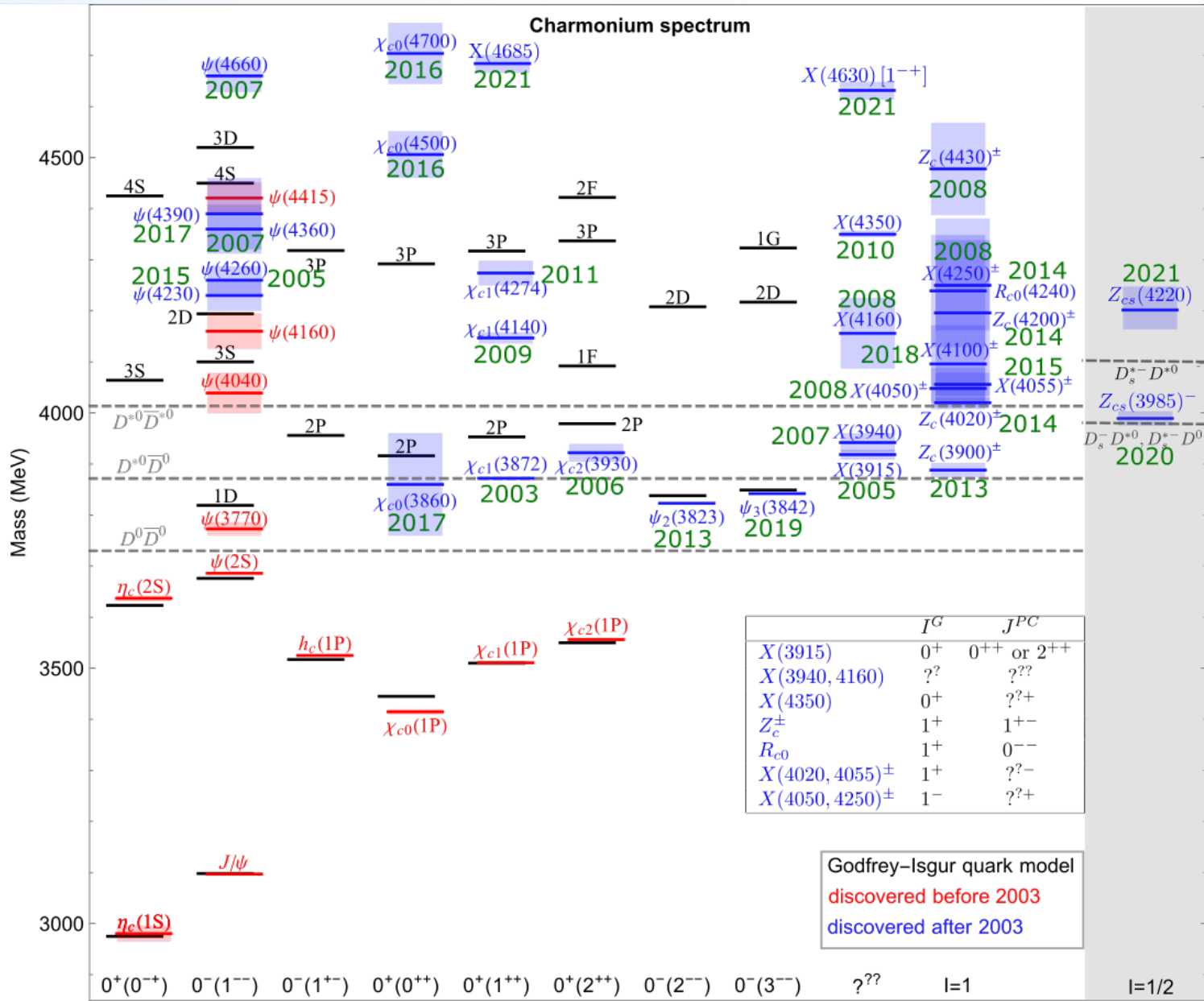
15-19 August 2022

Based on

Z. Yang, FKG, Semi-inclusive lepto-production of hidden-charm exotic hadrons, arXiv:2107.12247;

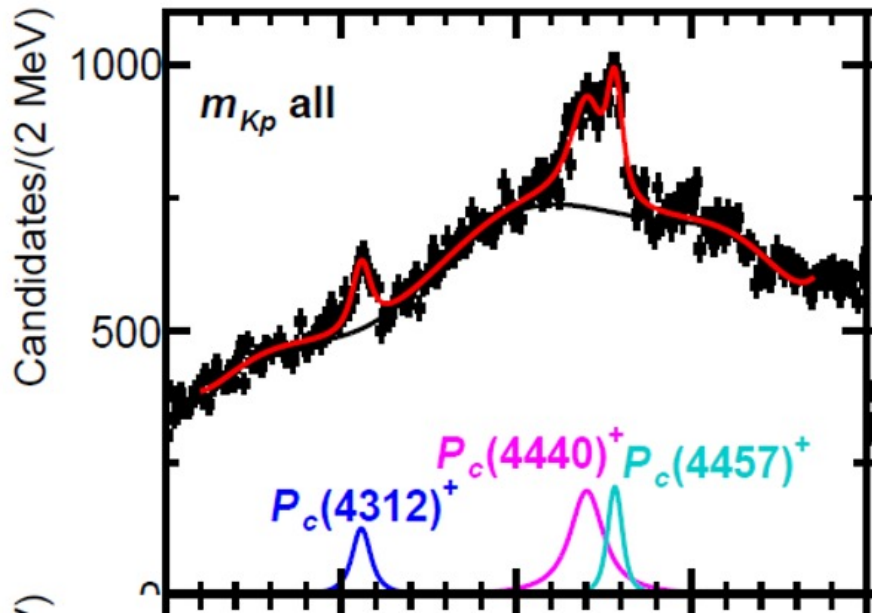
P.-P. Shi, FKG, Z. Yang, Semi-inclusive electroproduction of hidden-charm and double-charm hadronic molecules, arXiv:2208.02639

Hidden-charm states



Hidden-charm and double-charm states

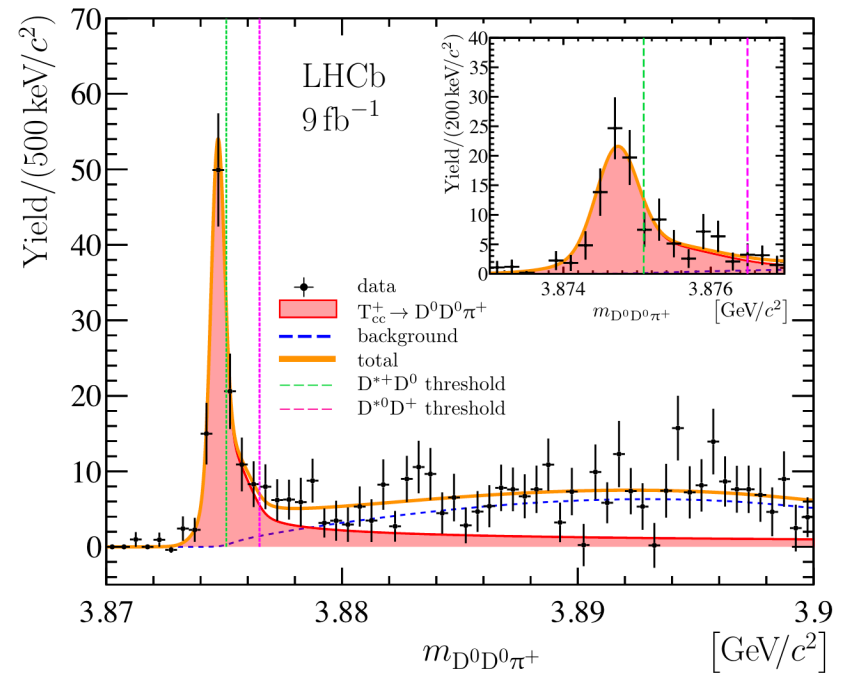
Hidden-charm P_c LHCb (2015, 2019)



$$\Lambda_b^0 \rightarrow J/\psi p K^-$$

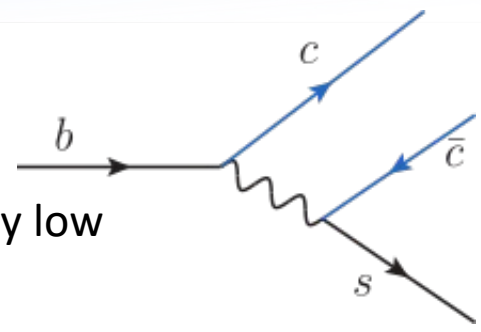
- Internal structure not understood
- Many structures are near threshold; candidates of hadronic molecules

Double-charm T_{cc} LHCb (2021)



Current experiments for the hidden-charm particles

- B-factories



- From **ISR processes**

- Cross sections and selection efficiency are relatively low

- From **B decays with $b \rightarrow sc\bar{c}$**

- Energy region limited: $< m_B - m_K \approx 4.8$ GeV

- Final states with 3 or more hadrons: $B \rightarrow K\psi\phi, K\psi\omega, K\psi\pi\pi, \dots$

Often **difficult due to multi-hadron final states** to get unambiguous properties of broad resonances

- Hadron colliders

- From **Λ_b decays with $b \rightarrow sc\bar{c}$**

- Energy region limited: $< m_{\Lambda_b} - m_{\Lambda} \approx 4.8$ GeV

- Final states with 3 or more hadrons

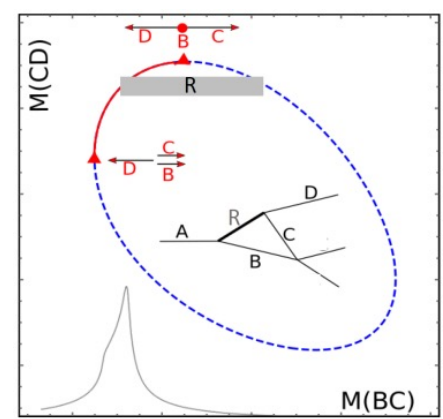
- Prompt productions: high background

- BESIII

- Energy so far $\lesssim 4.96$ GeV, to be upgraded to 5.6 GeV

- Low production rates (radiative transition) for $C = +$ states

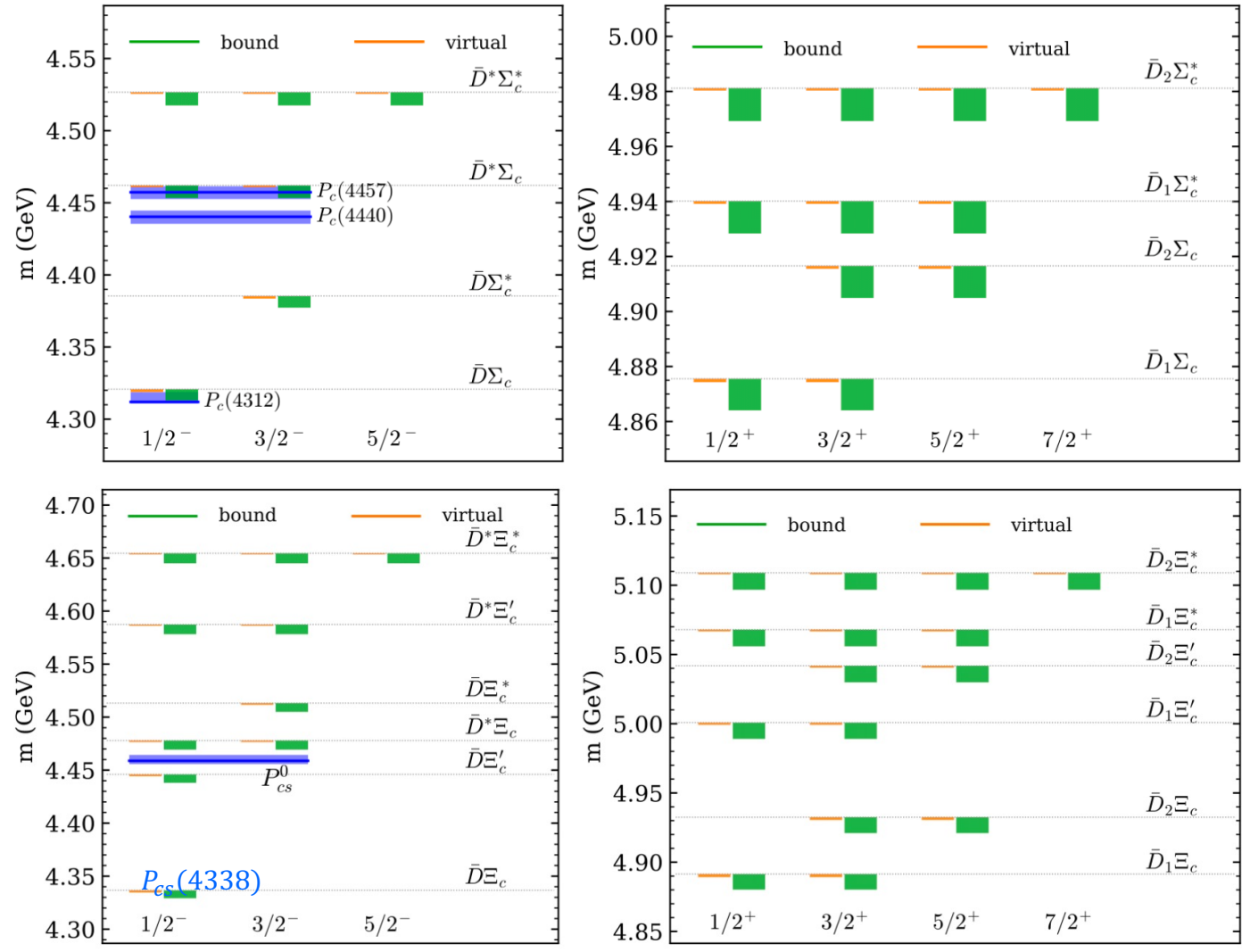
- Luminosity: less than $1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ above 4 GeV



More hadronic molecules are expected

- Survey of hadronic molecular spectrum with a simple vector-exchange model
- Hidden-charm hadronic molecules

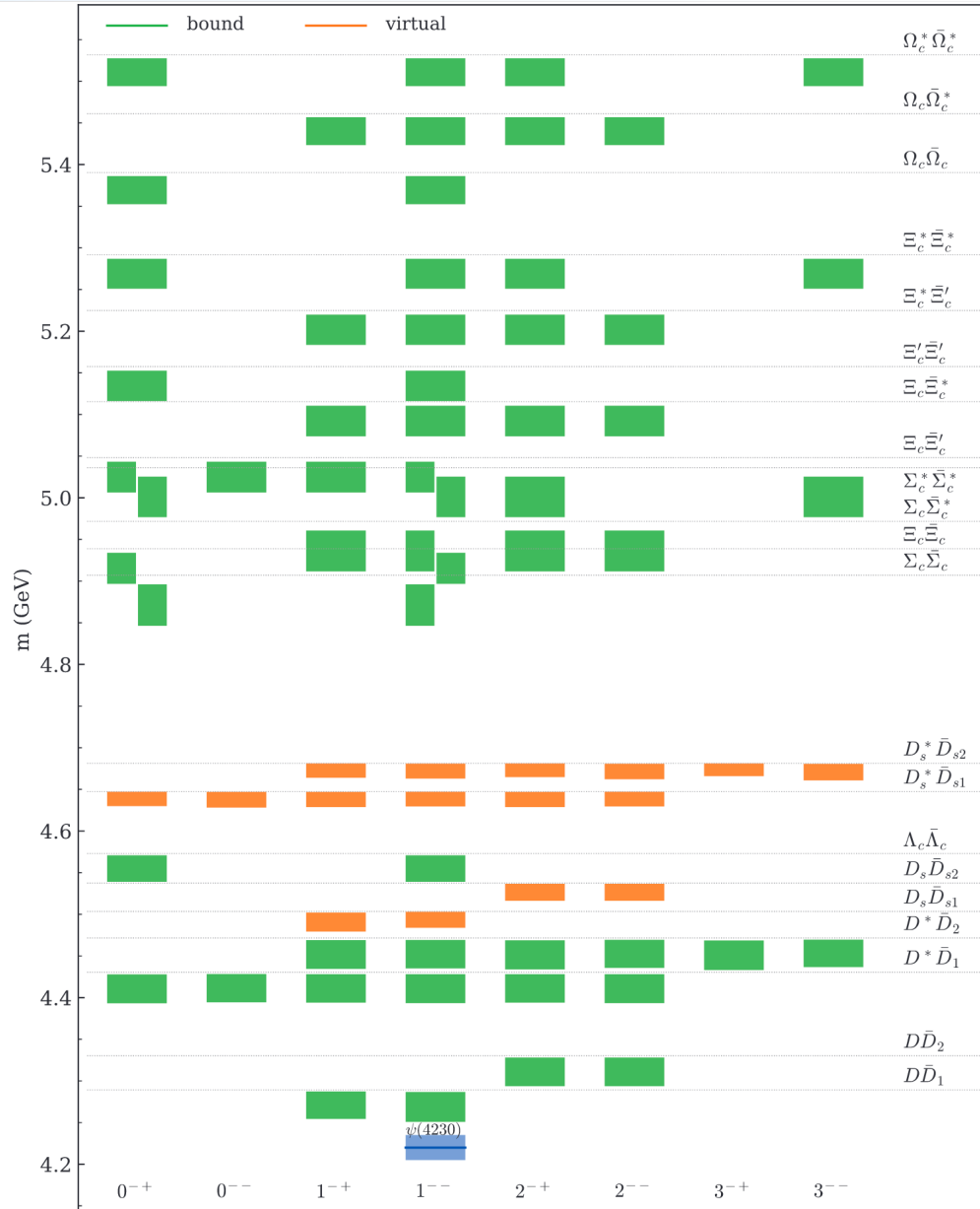
X.-K. Dong, FKG, B.-S. Zou, *Progr.Phys.*41 (2021) 65



More hadronic molecules are expected

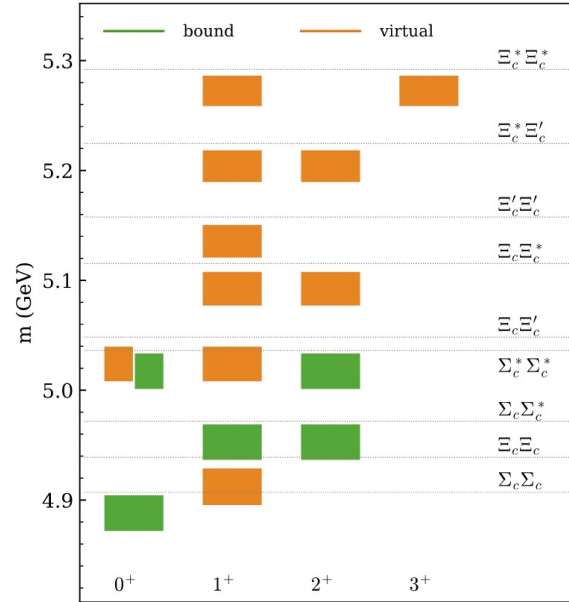
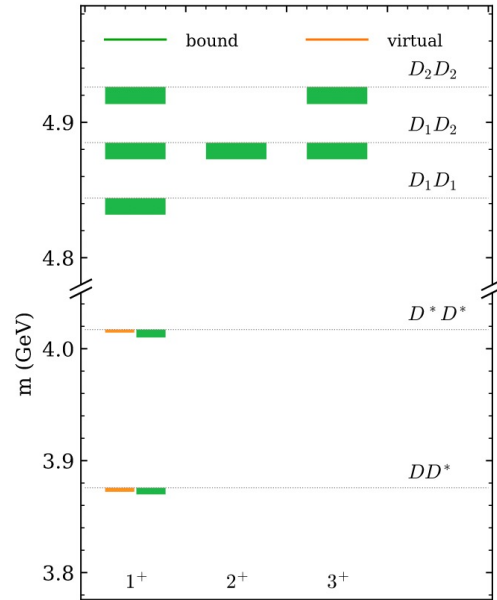
- Hidden-charm hadronic molecules

X.-K. Dong, FKG, B.-S. Zou,
 Progr.Phys.41 (2021) 65



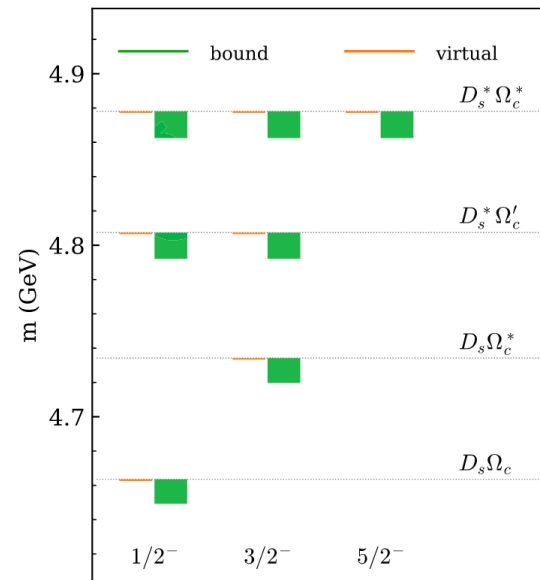
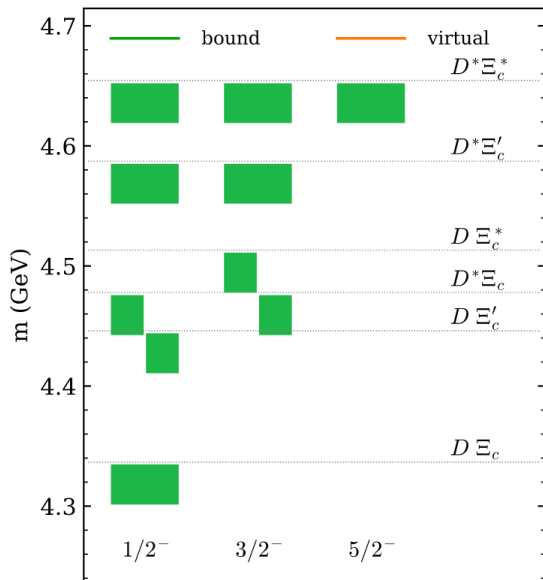
➤ High-luminosity experiments covering the energy range above 5 GeV are needed

More hadronic molecules are expected



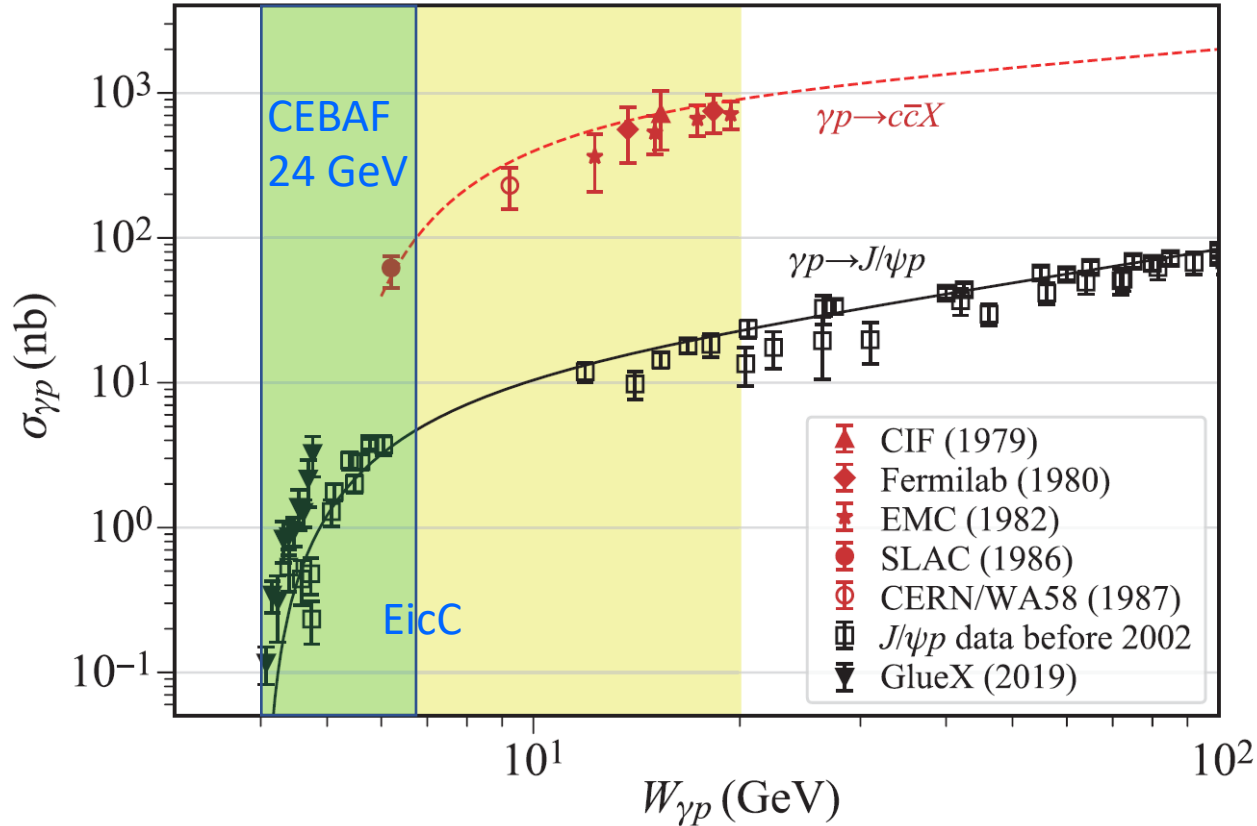
- Double-charm hadronic molecules

X.-K. Dong, FKG, B.-S. Zou, CTP73 (2021) 125201



Photoproduction: charm

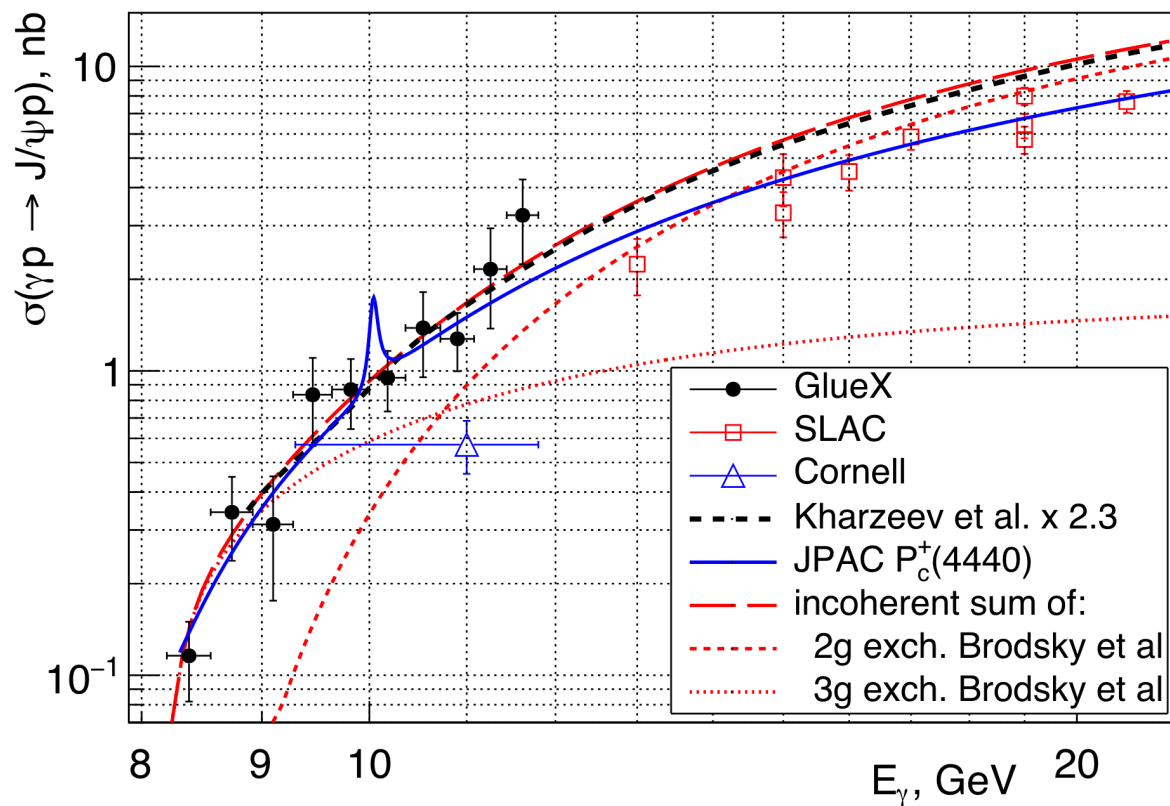
Figure from D. P. Anderle et al., Front.Phys. 16 (2021) 64701



- Leptoproduction: cross sections are roughly two orders of magnitude (α) smaller
- Many more open-charm hadrons D and Λ_c

Near-threshold J/ψ production at GlueX

No evidence of P_c in the J/ψ photoproduction at GlueX

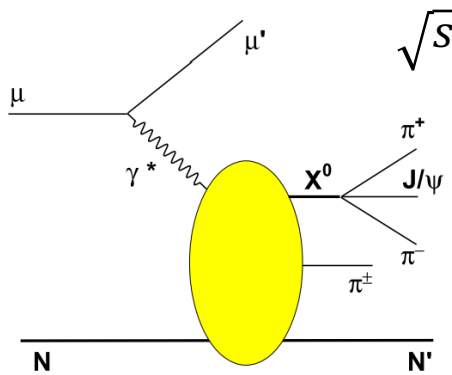


GlueX, PRL 122 (2019) 222001

Hidden-charm exotics at COMPASS

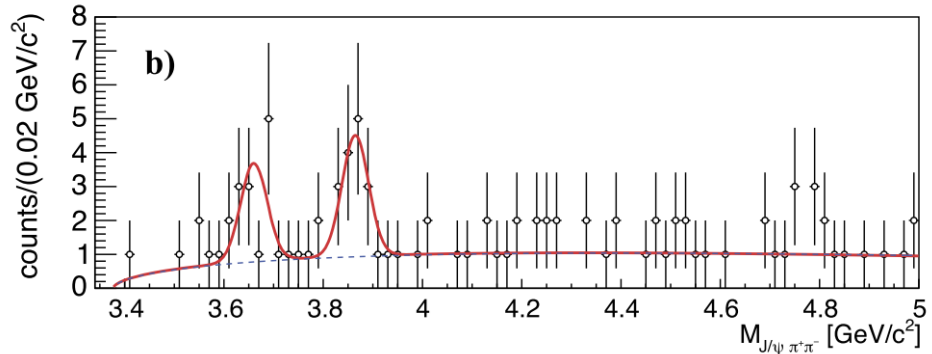
- Observation of $\tilde{X}(3872)$ in $\gamma^* N \rightarrow X^0 \pi^\pm N'$ with 4.1σ

COMPASS, PLB783(2018)334

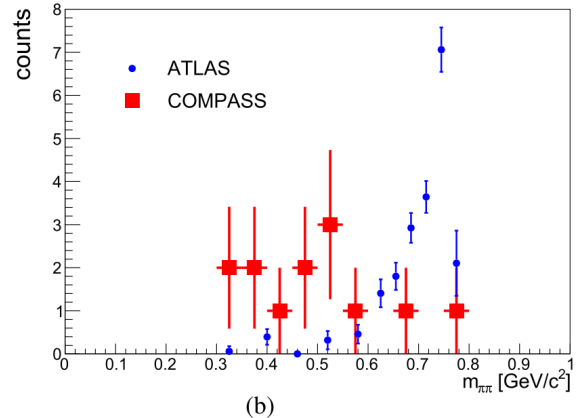
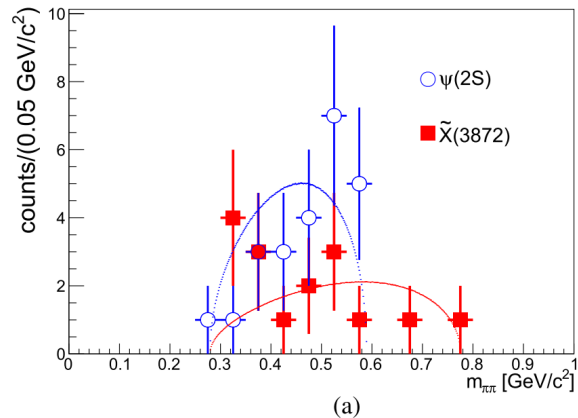


$$\sqrt{s_{\gamma N}} \in [8, 18] \text{ GeV}$$

$$M_{\tilde{X}} = (3860.4 \pm 10.0) \text{ MeV}$$



- The $\pi\pi$ invariant mass suggests $C(\tilde{X}) = -1$



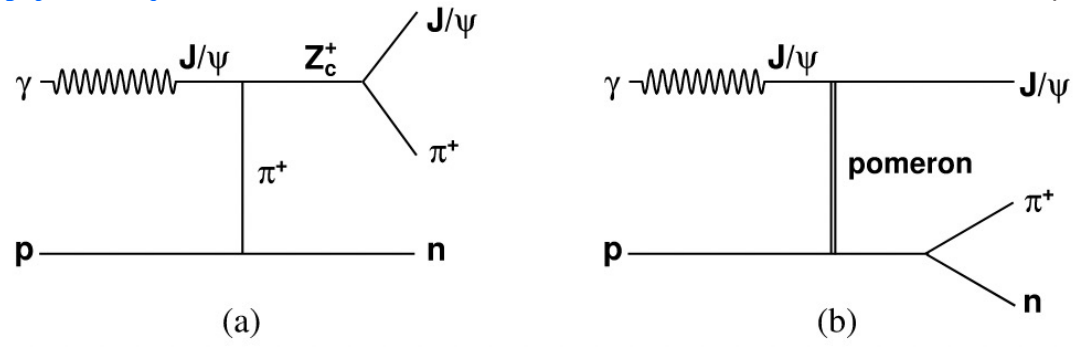
- Cross sections: $\sigma(\gamma N \rightarrow \tilde{X} \pi N') \times B(\tilde{X} \rightarrow J/\psi \pi^+ \pi^-) = (71 \pm 28 \pm 39) \text{ pb}$

$$\sigma(\gamma N \rightarrow X(3872) N') \times B(X(3872) \rightarrow J/\psi \pi^+ \pi^-) < 2.9 \text{ pb (CL = 90\%)}$$

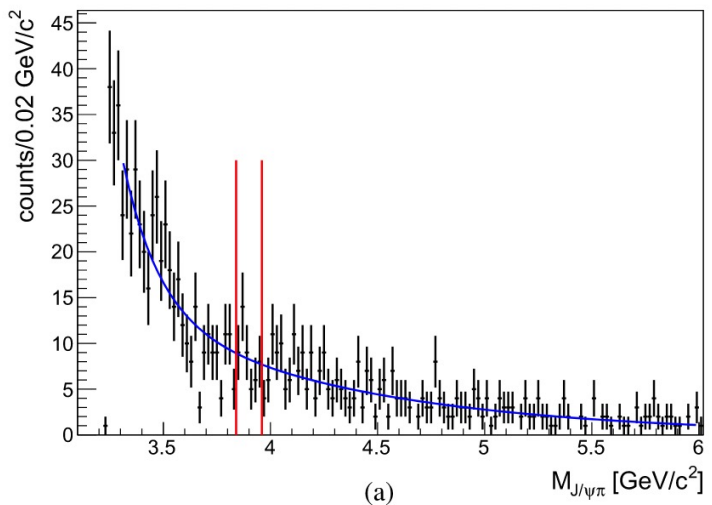
Hidden-charm exotics at COMPASS

- No evidence of $Z_c(3900)$ seen

COMPASS, PLB742(2015)330



$$\mu^+ N \rightarrow \mu^+ Z_c^\pm(3900) N \rightarrow \mu^+ J/\psi \pi^\pm N \rightarrow \mu^+ \mu^+ \mu^- \pi^\pm N \quad \sqrt{s_{\gamma N}} \in [7, 19] \text{ GeV}$$



- Cross sections:

$$BR(Z_c^\pm(3900) \rightarrow J/\psi \pi^\pm) \times \sigma_{\gamma N \rightarrow Z_c^\pm(3900) N} \Big|_{\langle \sqrt{s_{\gamma N}} \rangle = 13.8 \text{ GeV}} < 52 \text{ pb}$$

Coupled-channel effects

- Open-charm channels easier to be produced than $J/\psi p$; thresholds nearby

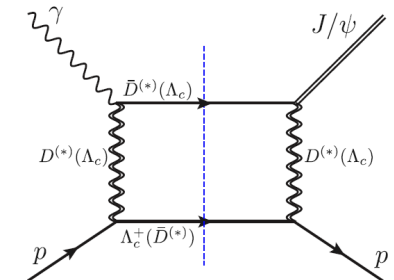
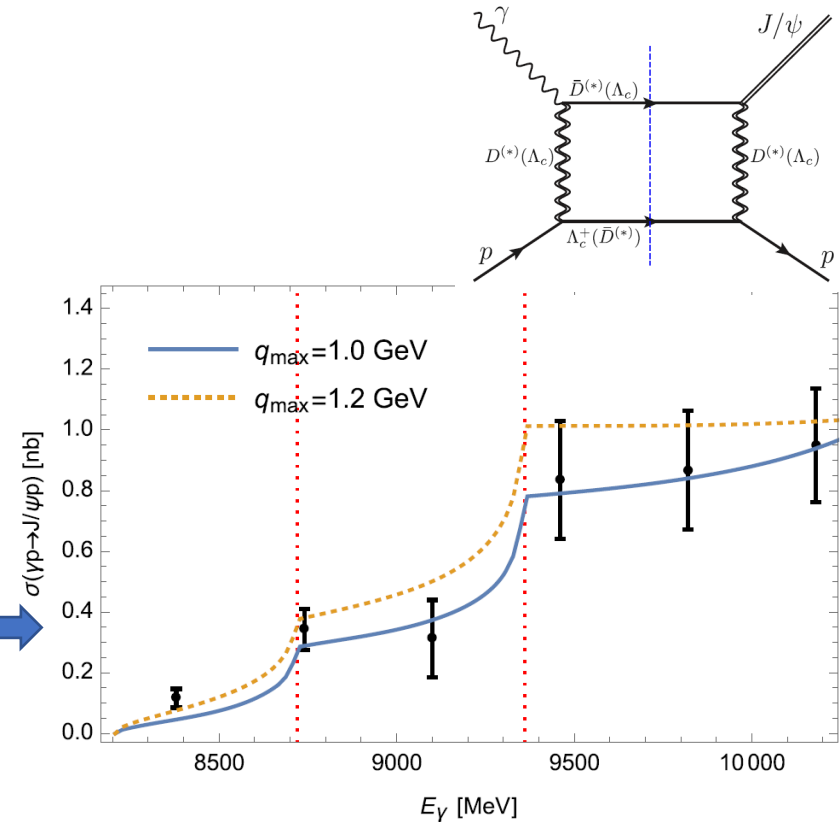
M.-L. Du, V. Baru, FKG, C. Hanhart, U.-G. Meißner, A. Nefediev, I. Strakovsky, EPJC80(2020)1053

+

Unitarity: $J/\psi p \rightarrow J/\psi p$ enters w/o VMD, but cannot be singled out

$$\left\{ \begin{array}{l} \Lambda_c^+ + \bar{D}^- : 2286 + 1865 = 4151 \text{ MeV} \\ J/\psi + p : 3097 + 938 = 4035 \text{ MeV} \end{array} \right.$$

- Estimated cross section w/ couplings taken from literature
- Unique prediction: **cusps at $\Lambda_c \bar{D}^{(*)}$ thresholds**

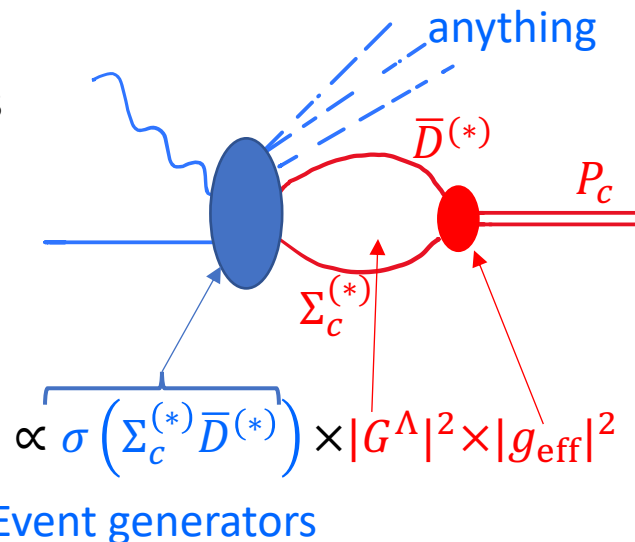


- The same mechanism for $J/\psi p \rightarrow J/\psi p$ leads to small scattering length; need to compare with the scattering length from gluon exchanges (ongoing):

$$\left| a^{J=1/2} \right| = 0.2 \dots 3.1 \text{ mfm}, \quad \left| a^{J=3/2} \right| = 0.2 \dots 3.0 \text{ mfm},$$

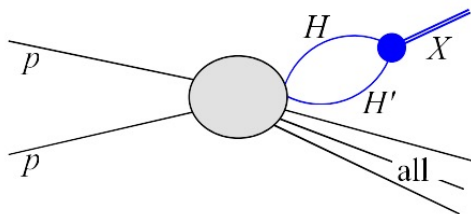
Cross section estimates

- Order-of-magnitude estimates of **inclusive** lepto-production of near-threshold **hadronic molecules**
- The cross section can be estimated as e.g., for P_c states



- The method has been used to estimate the X(3872) production at hadron colliders; despite the debates regarding the X(3872) structure, **correct order of magnitude** was reproduced

Artoisenet, Braaten, PRD83(2011)014019; FKG, Meißner, W. Wang, Z. Yang, EPJC74(2014)3063



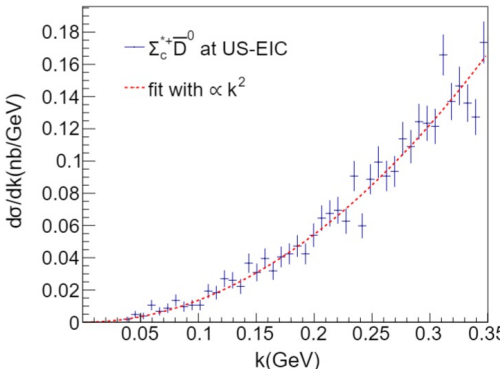
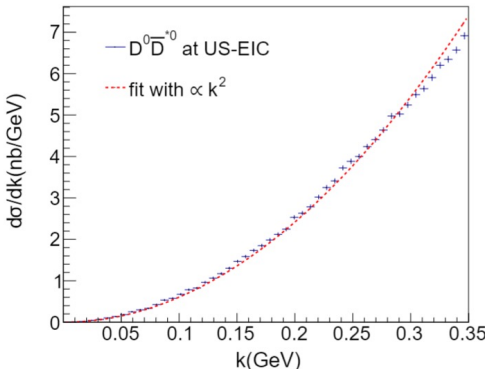
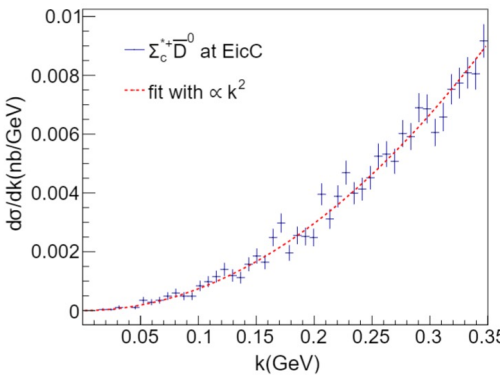
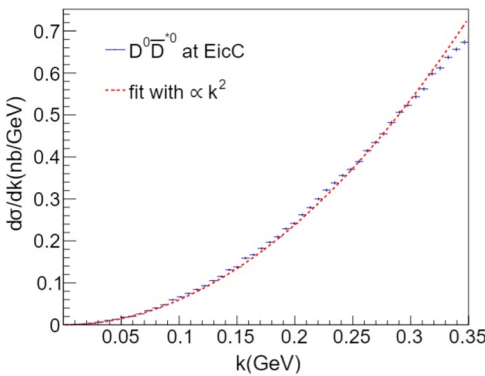
$\sigma(pp/\bar{p} \rightarrow X)$ [nb] Exp.	$\Lambda=0.5$ GeV	$\Lambda=1.0$ GeV
Tevatron 37-115	7 (5)	29 (20)
LHC-7 13-39	13 (4)	55 (15)

Albaladejo, FKG, Hanhart et al., CPC41(2017)121001

Cross section estimates

Z. Yang, FKG, CPC 45 (2021) 123101

- Charm hadron pairs generated using Pythia6.4



- Considered machine configurations

	EicC	EIC	CEBAF (24 GeV)
e^- energy (GeV)	3.5	20	24
proton energy (GeV)	20	250	0
luminosity ($\text{cm}^{-2} \text{s}^{-1}$)	2×10^{33}	10^{34}	10^{36}

Cross section estimates

Z. Yang, FKG, CPC 45 (2021) 123101; P.-P. Shi, FKG, Z. Yang, arXiv:2208.02639

- **Order-of-magnitude estimates** of the semi-inclusive electro-production of hidden/double-charm hadronic molecules (**in units of pb**)

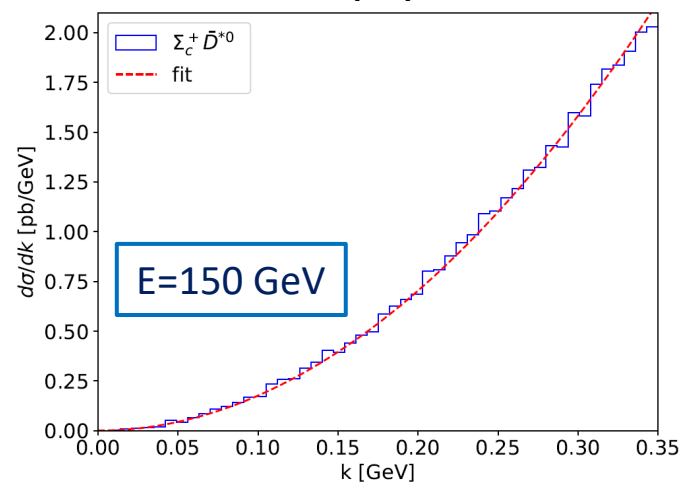
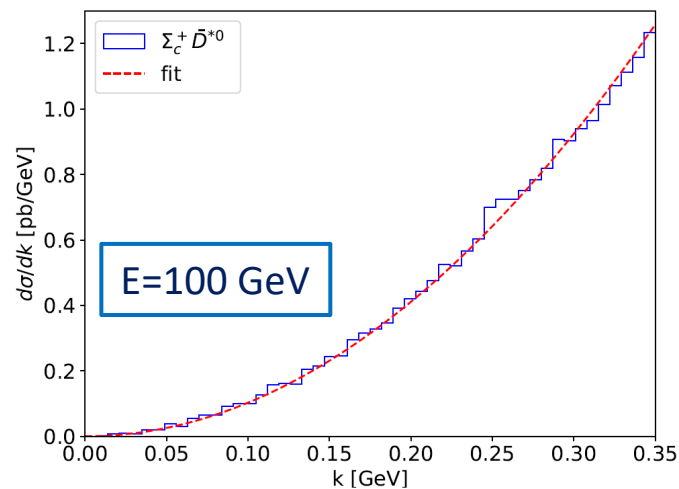
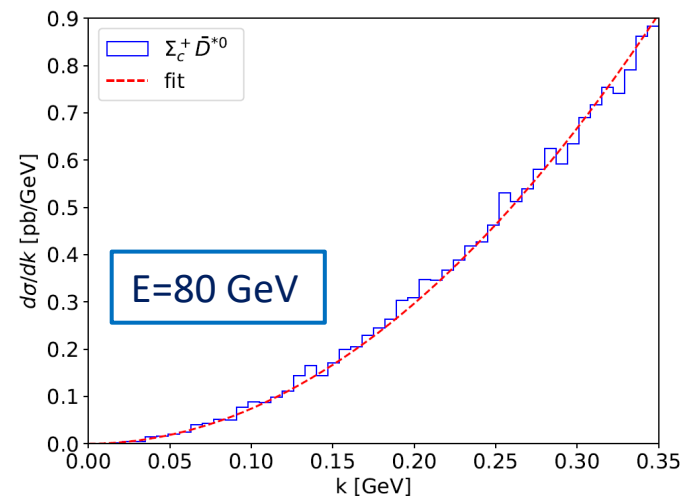
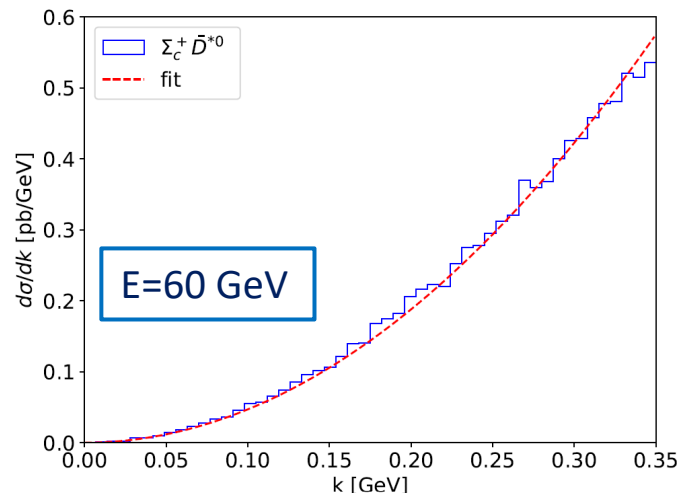
	Constituents	$I, J^{P(C)}$	EicC	EIC
$X(3872)$	$D\bar{D}^*$	$0, 1^{++}$	21(89)	216(904)
$Z_c(3900)^0$	$D\bar{D}^*$	$1, 1^{+-}$	$0.4 \times 10^3 (1.3 \times 10^3)$	$3.8 \times 10^3 (14 \times 10^3)$
Z_{cs}^-	$D^{*0}D_s^-$	$1/2, 1^+$	19(69)	250(900)
$P_c(4312)$	$\Sigma_c\bar{D}$	$1/2, 1/2^-$	0.8(4.1)	15(73)
$P_{cs}(4338)$	$\Xi_c\bar{D}$	$0, 1/2^-$	0.1(1.6)	1.8 (30)
Predicted	$\Lambda_c\bar{\Lambda}_c$	$0, 0^{-+}$	0.3 (3.0)	10 (110)
Predicted	$\Lambda_c\bar{\Sigma}_c$	$1, 0^-$	0.01 (0.12)	0.5 (5.5)
T_{cc}^+	DD^*	$0, 1^+$	$0.3 \times 10^{-3} (1.2 \times 10^{-3})$	0.1 (0.5)

Results for more systems can be found in the above refs.

Semi-inclusive production at CEBAF 24 GeV

P.-P. Shi, FKG, Z. Yang, arXiv:2208.02639

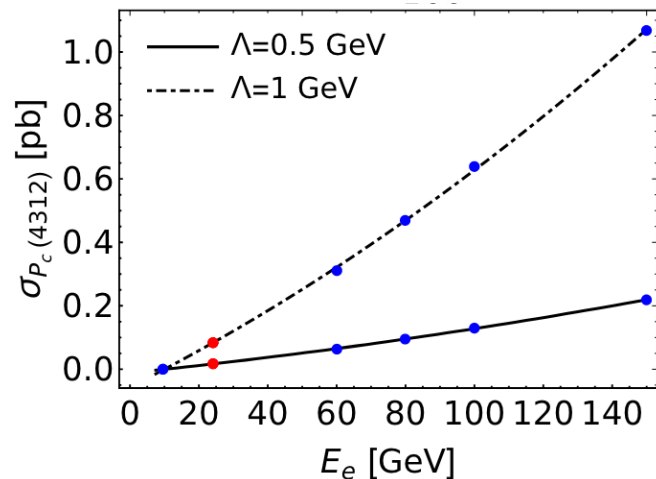
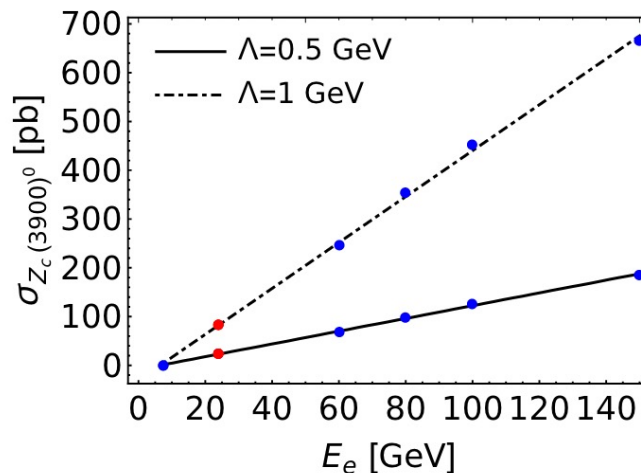
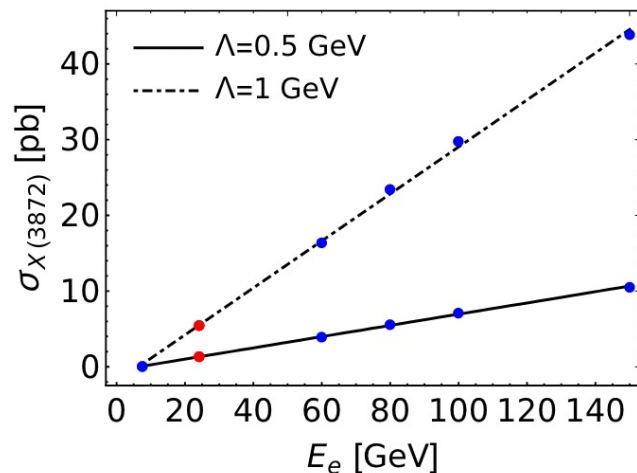
- For beam energy of 24 GeV, the ep c.m. energy: 6.77 GeV; too low for Pythia
- Choose a few higher energy points, and extrapolate the results done to 24 GeV
- Rough **order-of-magnitude** estimates



Semi-inclusive production at CEBAF 24 GeV

P.-P. Shi, FKG, Z. Yang, arXiv:2208.02639

- For beam energy of 24 GeV, the ep c.m. energy: 6.77 GeV; too low for Pythia
- Choose a few higher energy points, and extrapolate the results done to 24 GeV
- Rough **order-of-magnitude** estimates



Semi-inclusive production at CEBAF 24 GeV



P.-P. Shi, FKG, Z. Yang, arXiv:2208.02639

- Order-of-magnitude estimates of the electro-production cross sections with 24 GeV electron beam

	Constituents	$J^{P(C)}$	σ_X/pb
$X(3872)$	$D\bar{D}^*$	1^{++}	1.3 (5.5)
$Z_c(3900)^0$	$D\bar{D}^*$	1^{+-}	23 (82)
$P_c(4312)$	$\Sigma_c\bar{D}$	$1/2^-$	0.02 (0.08)
$P_{cS}(4459)$	$\Xi_c\bar{D}^*$	$3/2^-$	0.005 (0.03)

- Not surprising the GlueX observed no signal of P_c : $\sigma(\gamma p \rightarrow J/\psi p) = \mathcal{O}(1 \text{ nb}) \gg 10^2 \times \sigma(e^- p \rightarrow P_c + \text{anything})$, **much higher statistics is needed**
- With a luminosity of $10^{36} \text{ cm}^{-2}\text{s}^{-1}$, for an integrated luminosity of 10^7 pb^{-1} , **a large number of hidden-charm exotics can be produced**
even after having taken into account branching fractions, e.g., $\mathcal{B}(P_c \rightarrow J/\psi p) = \mathcal{O}(1\%)$, $\mathcal{B}(J/\psi \rightarrow \ell^+\ell^-) = 12\%$



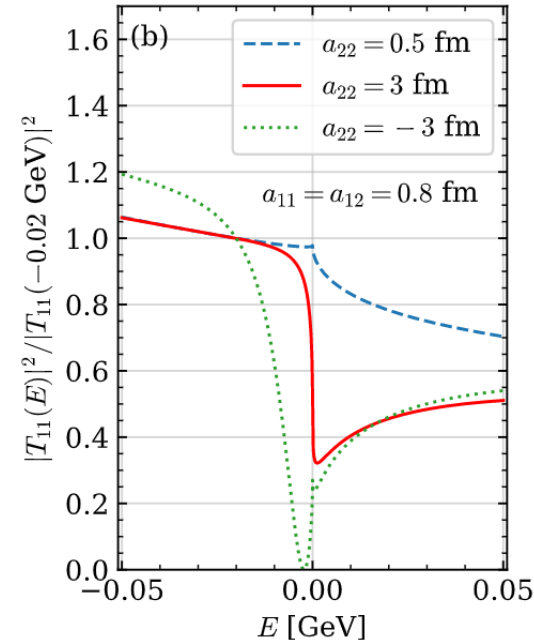
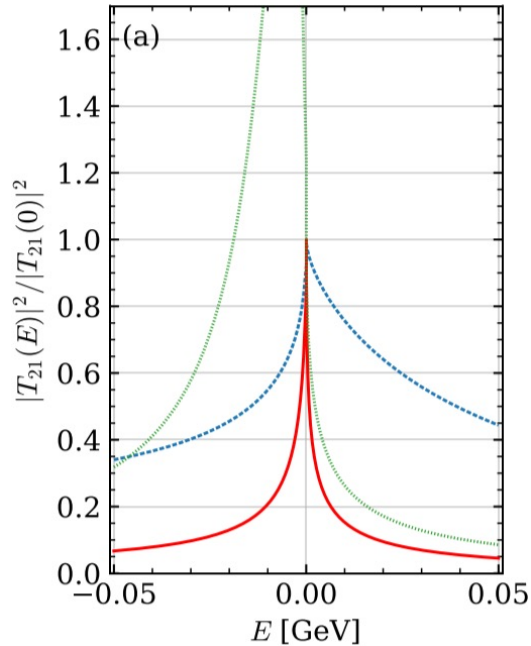
- Future electron-proton machines will be able to contribute a lot to hadron spectroscopy
- A large amount of hidden-charm exotic hadrons can be observed at CEBAF 24 GeV for a luminosity of $10^{36} \text{ cm}^{-2} \text{ s}^{-1}$

Thank you for your attention!

Near-threshold structures

- Nontrivial near-threshold structure for **S-wave short-range attraction**

X.-K. Dong, FKG, B.-S. Zou, PRL126 (2021) 152001



- The same pole could lead to distinct line shapes in different reactions
- Hadronic molecules easily formed in the hidden/double-heavy-flavor region
- Other models also predict higher states

Interaction strengths from light-vector exchanges

X.-K. Dong, FKG, B.-S. Zou, CTP73 (2021) 125201

System	I	S	Thresholds [MeV]	Exchanged particles	F
$D^{(*)}\bar{D}^{(*)}/D^{(*)}D^{(*)}$	1 0	0/0	(3734, 3876, 4017)	ρ, ω	$-\frac{1}{2}, \frac{1}{2}/-\frac{1}{2}, -\frac{1}{2}$ $\frac{3}{2}, \frac{1}{2}/\frac{3}{2}, -\frac{1}{2}$
$D_s^{(*)}\bar{D}^{(*)}/D_s^{(*)}D^{(*)}$	$\frac{1}{2}$	1/1	(3836, 3977, 3979, 4121)	K^*	0/-1
$D_s^{(*)}\bar{D}_s^{(*)}/D_s^{(*)}D_s^{(*)}$	0	0/2	(3937, 4081, 4224)	ϕ	1/-1
$\bar{D}^{(*)}\Lambda_c/D^{(*)}\Lambda_c$	$\frac{1}{2}$	0/0	(4154, 4295)	ω	-1/1
$\bar{D}_s^{(*)}\Lambda_c/D_s^{(*)}\Lambda_c$	0	-1/1	(4255, 4399)	-	0/0
$\bar{D}^{(*)}\Xi_c/D^{(*)}\Xi_c$	1 0	-1/-1	(4337, 4478)	ρ, ω	$-\frac{1}{2}, -\frac{1}{2}/-\frac{1}{2}, \frac{1}{2}$ $\frac{3}{2}, -\frac{1}{2}/\frac{3}{2}, \frac{1}{2}$
$\bar{D}_s^{(*)}\Xi_c/D_s^{(*)}\Xi_c$	$\frac{1}{2}$	-2/0	(4438, 4582)	ϕ	-1/1
$\bar{D}^{(*)}\Sigma_c^{(*)}/D^{(*)}\Sigma_c^{(*)}$	$\frac{3}{2}$ $\frac{1}{2}$	0/0	(4321, 4385, 4462, 4527)	ρ, ω	-1, -1/-1, 1 2, -1/2, 1
$\bar{D}_s^{(*)}\Sigma_c^{(*)}/D_s^{(*)}\Sigma_c^{(*)}$	1	-1/1	(4422, 4486, 4566, 4630)	-	0/0
$\bar{D}^{(*)}\Xi_c^{\prime(*)}/D^{(*)}\Xi_c^{\prime(*)}$	1 0	-1/-1	(4446, 4513, 4587, 4655)	ρ, ω	$-\frac{1}{2}, -\frac{1}{2}/-\frac{1}{2}, \frac{1}{2}$ $\frac{3}{2}, -\frac{1}{2}/\frac{3}{2}, \frac{1}{2}$
$\bar{D}_s^{(*)}\Xi_c^{\prime(*)}/D_s^{(*)}\Xi_c^{\prime(*)}$	$\frac{1}{2}$	-2/0	(4547, 4614, 4691, 4758)	ϕ	-1/1
$\bar{D}^{(*)}\Omega_c^{(*)}/D^{(*)}\Omega_c^{(*)}$	$\frac{1}{2}$	-2/0	(4562, 4633, 4704, 4774)	-	0/0
$\bar{D}_s^{(*)}\Omega_c^{(*)}/D_s^{(*)}\Omega_c^{(*)}$	0	-3/-1	(4664, 4734, 4807, 4878)	ϕ	-2/2
$\Lambda_c\bar{\Lambda}_c/\Lambda_c\Lambda_c$	0	0/0	(4573)	ω	2/-2
$\Lambda_c\Xi_c/\Lambda_c\Xi_c$	$\frac{1}{2}$	1/-1	(4756)	ω/K^*	1, 0/-1, -1
$\Xi_c\Xi_c/\Xi_c\Xi_c$	1 0	0/-2	(4939)	ρ, ω, ϕ	$-\frac{1}{2}, \frac{1}{2}, 1/-\frac{1}{2}, -\frac{1}{2}, -1$ $\frac{3}{2}, \frac{1}{2}, 1/\frac{3}{2}, -\frac{1}{2}, -1$
$\Lambda_c\bar{\Sigma}_c^{(*)}/\Lambda_c\Sigma_c^{(*)}$	1	0/0	(4740, 4805)	ω/K^*	1, 0/-1, -1

Interaction strengths from light-vector exchanges

X.-K. Dong, FKG, B.-S. Zou, CTP73 (2021) 125201

System	I	S	Thresholds [MeV]	Exchanged particles	F
$\Lambda_c \bar{\Xi}'^{(*)} / \Lambda_c \Xi'^{(*)}$	$\frac{1}{2}$	1/ - 1	(4865, 4932)	ω	1/ - 1
$\Lambda_c \bar{\Omega}_c^{(*)} / \Lambda_c \Omega_c^{(*)}$	0	2/ - 2	(4982, 5052)	—	0/0
$\Sigma_c^{(*)} \bar{\Xi}_c^{(*)} / \Sigma_c^{(*)} \Xi_c^{(*)}$	$\frac{3}{2}$ $\frac{1}{2}$	1/ - 1	(4923, 4988)	ρ, ω, K^*	- 1, 1, 0/ - 1, - 1, - 2 2, 1, 0/2, - 1, - 2
$\Xi_c \bar{\Xi}'^{(*)} / \Xi_c \Xi'^{(*)}$	1 0	0/ - 2	(5048, 5115)	ρ, ω, ϕ	$-\frac{1}{2}, \frac{1}{2}, 1/ - \frac{1}{2}, -\frac{1}{2}, -1$ $\frac{3}{2}, \frac{1}{2}, 1/ \frac{3}{2}, -\frac{1}{2}, -1$
$\Xi_c \bar{\Omega}_c^{(*)} / \Xi_c \Omega_c^{(*)}$	$\frac{1}{2}$	1/ - 3	(5165, 5235)	ϕ, K^*	2, 0/ - 2, - 2
$\Sigma_c^{(*)} \bar{\Sigma}_c^{(*)} / \Sigma_c^{(*)} \Sigma_c^{(*)}$	2 1 0	0/0	(4907, 4972, 5036)	ρ, ω	- 2, 2/ - 2, - 2 2, 2/2, - 2 4, 2/4, - 2
$\Sigma_c^{(*)} \bar{\Xi}'^{(*)} / \Sigma_c^{(*)} \Xi'^{(*)}$	$\frac{3}{2}$ $\frac{1}{2}$	1/ - 1	(5032, 5097, 5100, 5164)	ρ, ω, K^*	- 1, 1, 0/ - 1, - 1 - 2 2, 1, 0/2, - 1, - 2
$\Sigma_c^{(*)} \bar{\Omega}_c^{(*)} / \Sigma_c^{(*)} \Omega_c^{(*)}$	0	2/ - 2	(5149, 5213, 5219, 5284)	—	0/0
$\Xi_c' \bar{\Xi}'^{(*)} / \Xi_c' \Xi'^{(*)}$	1 0	0/ - 2	(5158, 5225, 5292)	ρ, ω, ϕ	$-\frac{1}{2}, \frac{1}{2}, 1/ - \frac{1}{2}, -\frac{1}{2}, -1$ $\frac{3}{2}, \frac{1}{2}, 1/ \frac{3}{2}, -\frac{1}{2}, -1$
$\Xi_c' \bar{\Omega}_c^{(*)} / \Xi_c' \Omega_c^{(*)}$	$\frac{1}{2}$	1/ - 3	(5272, 5341, 5345, 5412)	ϕ, K^*	2, 0/ - 2, - 2
$\Omega_c^{(*)} \bar{\Omega}_c^{(*)} / \Omega_c^{(*)} \Omega_c^{(*)}$	0	0/ - 4	(5390, 5461, 5532)	ϕ	4/ - 4