

$$J^\nu = \delta^{\nu+} \rho_p(\mathbf{x}_\perp) \delta(x^-) + \delta^{\nu-} \rho_T(\mathbf{x}_\perp) \delta(x^+)$$