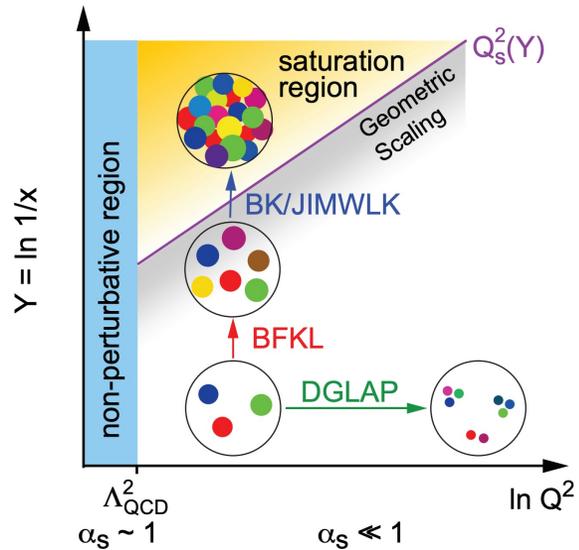
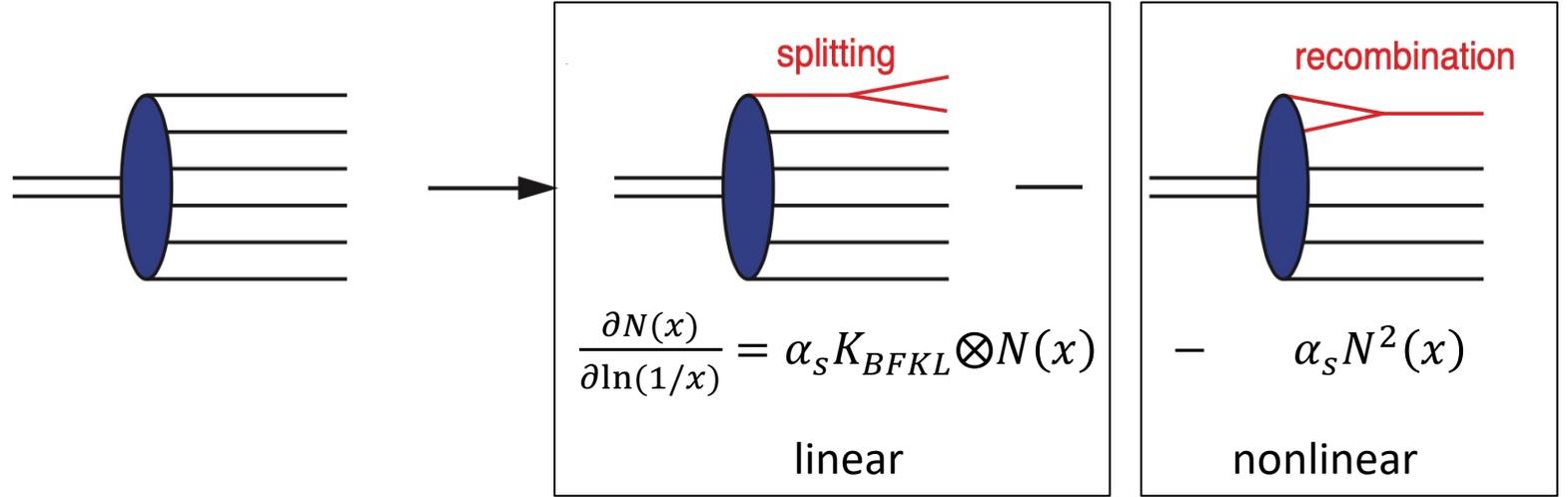
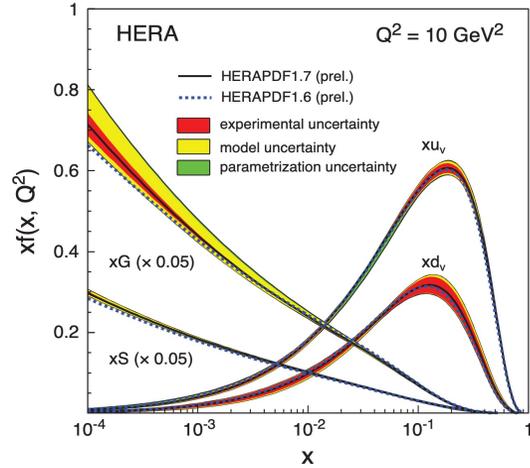


Probing nonlinear gluon effects by forward di-hadron correlations

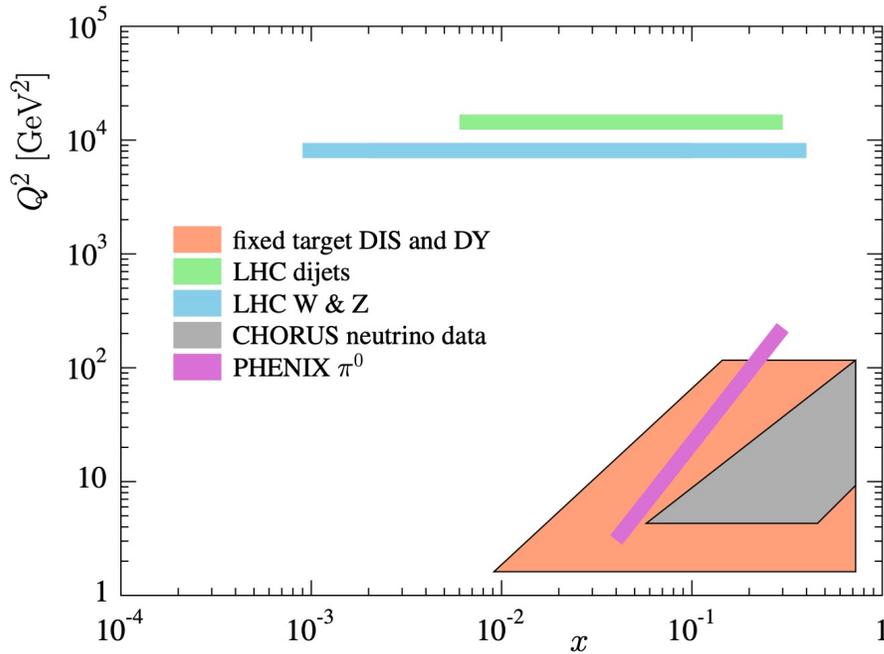
Xiaoxuan Chu, BNL
RBRC Seminar, April 28th 2022

Gluon saturation

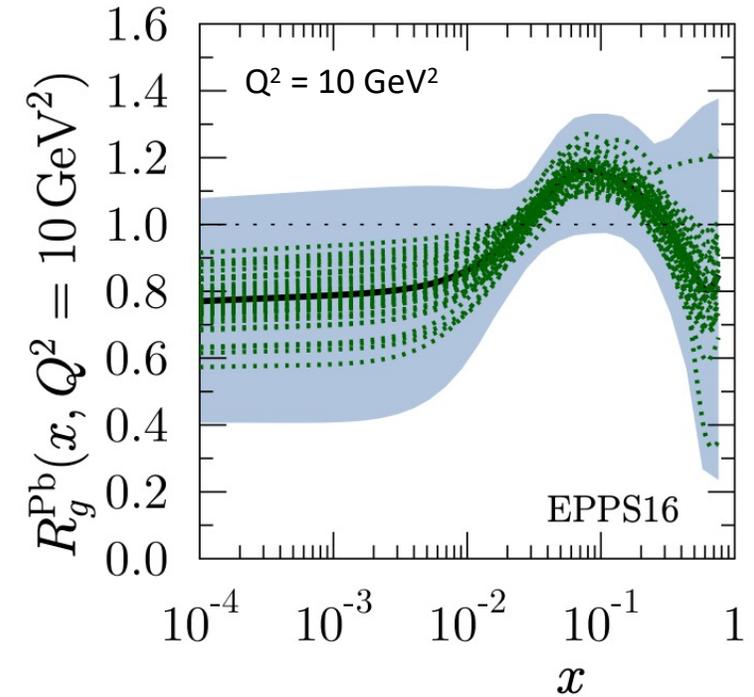
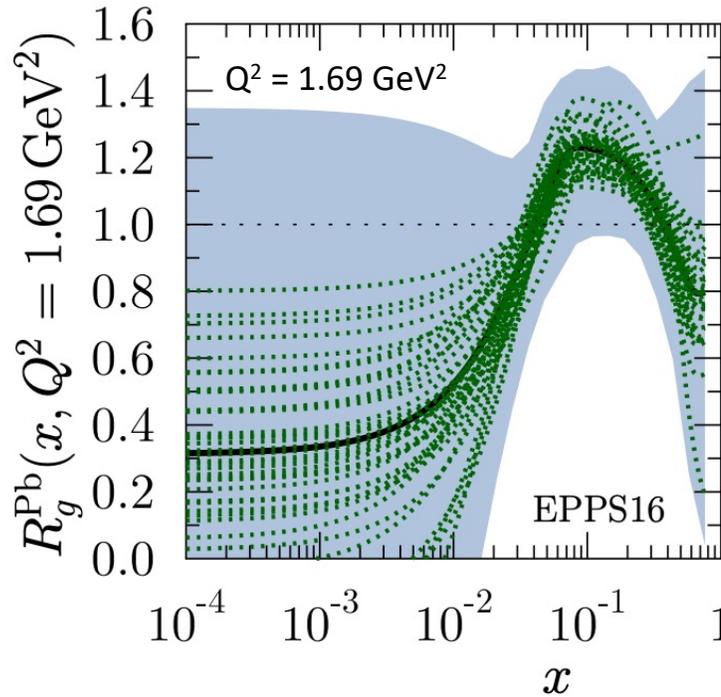


- Gluon density rapidly increases at small x : gluon splitting \rightarrow BFKL \rightarrow linear evolution
- Nonlinear gluon effect: gluon recombination \rightarrow BK \rightarrow non-linear evolution
- Gluon saturation ($Q^2 < Q_s^2$): gluon recombination = gluon splitting
- Nuclear gluon distributions at saturation region?

Current knowledge of nPDFs



K.J.Eskola et al., EPJC (2017) 77:163

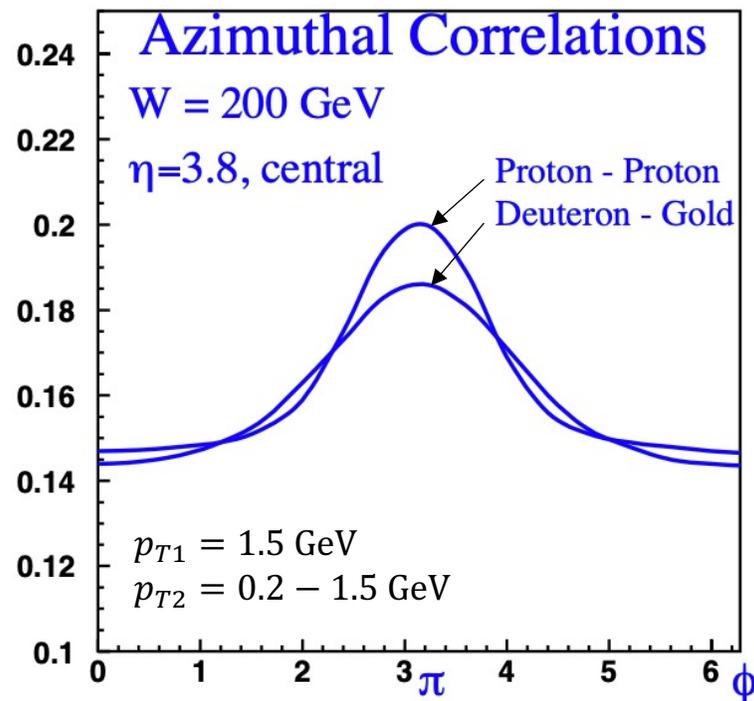


- EPPS16:

- LHC data in p+Pb collisions \rightarrow low x but high Q^2
- DIS, DY and PHENIX π^0 data: low/moderate Q^2
- x and Q^2 evolution behavior of suppression \rightarrow cold nuclear matter (CNM) effect
- Nuclear gluon distributions have large uncertainty at small x , moderate Q^2 and low Q^2 \rightarrow further inputs from RHIC data

Di-hadron measurement in d+Au

- **CGC** successfully predicted the strong **suppression of the hadron inclusive yields** in d+Au relative to p+p, by gluon saturation effects
- **Di-hadron** as another observable provides further test, was first proposed by D. Kharzeev, E. Levin and L. McLerran from NPA 748 (2005) 627-640



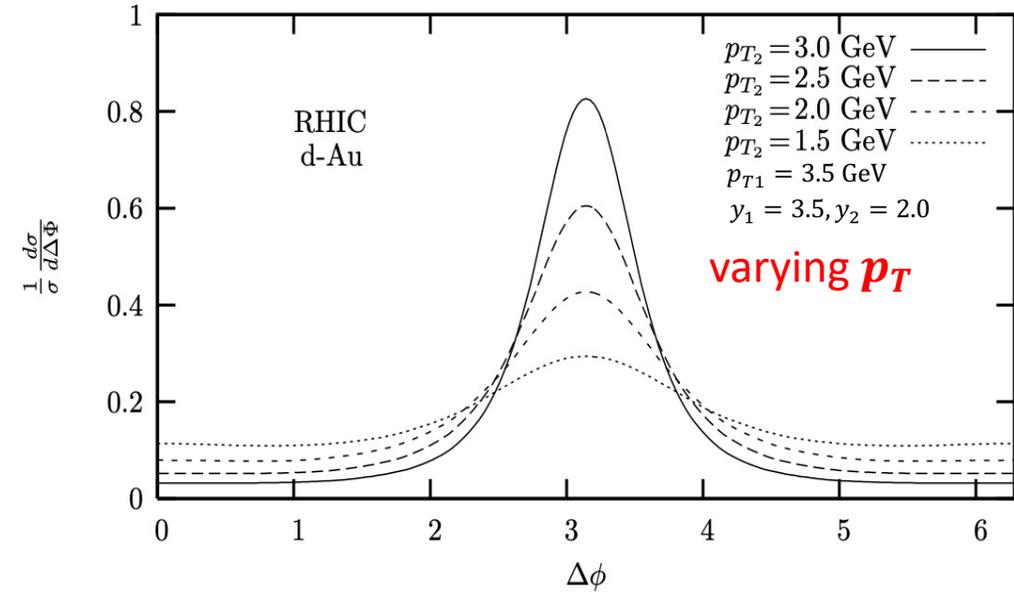
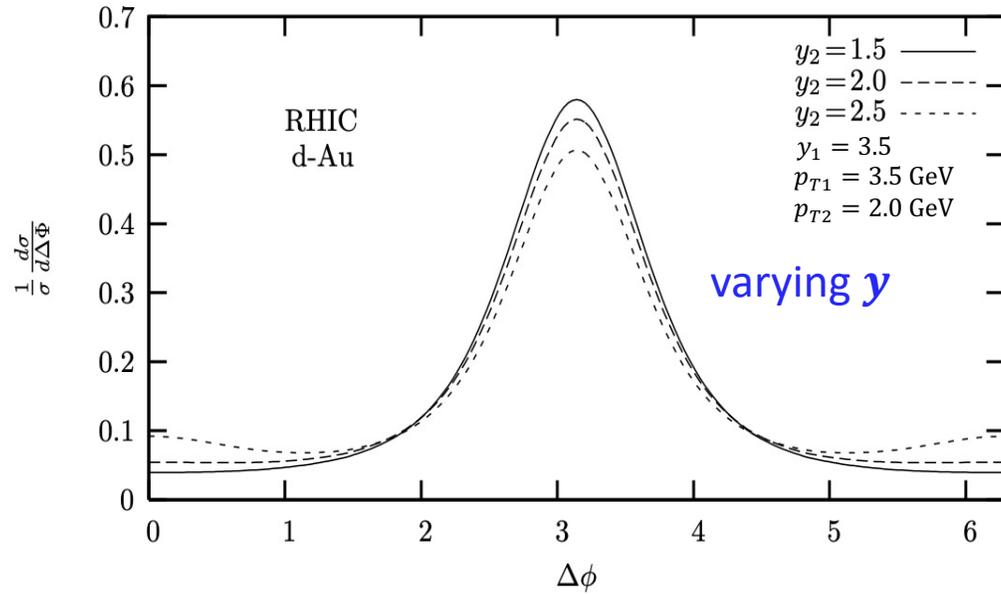
Deletion of away-side peak in d+A relative to p+p as saturation feature

Note: self normalization ($\Delta\phi$ distribution normalized by N_{pair})

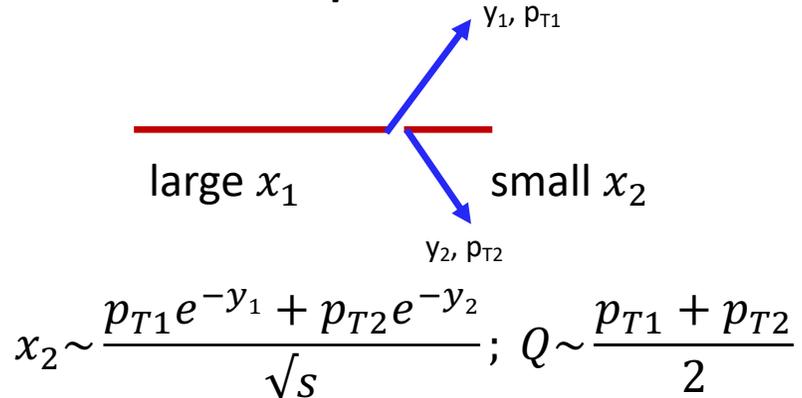
- Following theoretical predictions on di-hadron:

Saturation signatures on p_T and y

C. Marquet in NPA 796, 41 (2007)



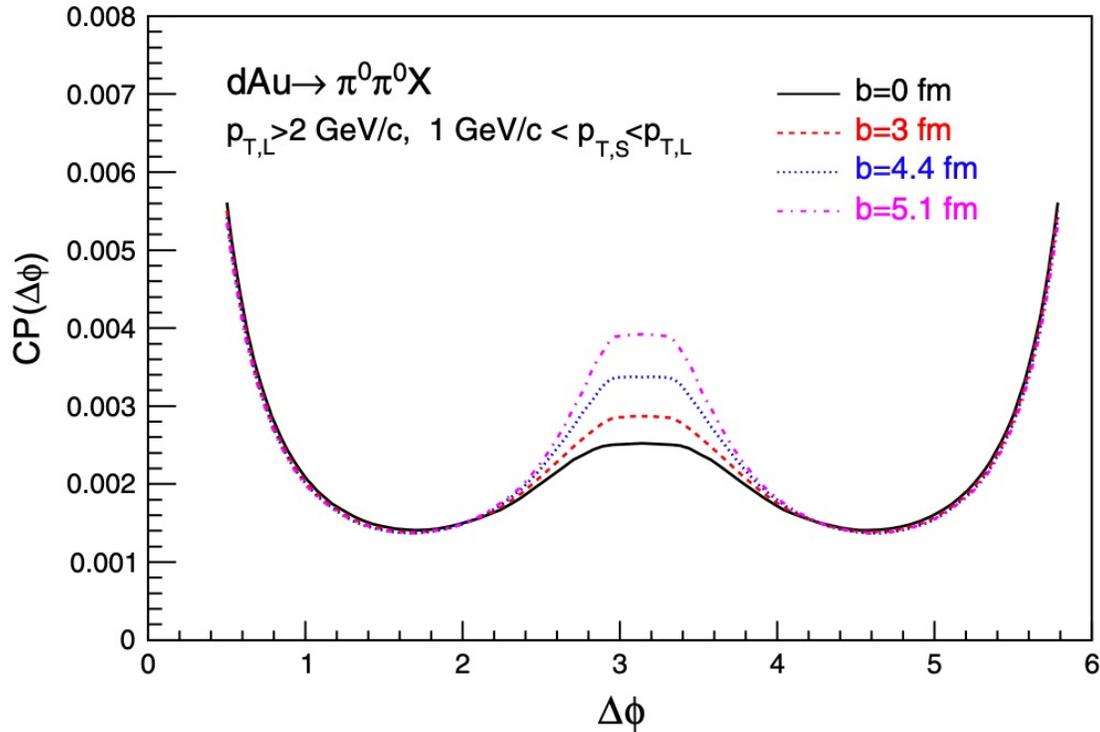
Forward di-parton kinematics



- Correlation suppressed as x_2 decreases
 - x (and Q^2) scanned by varying p_T and y
- Note: $\Delta\phi$ distribution normalized by N_{trig}

Saturation signatures on b and A

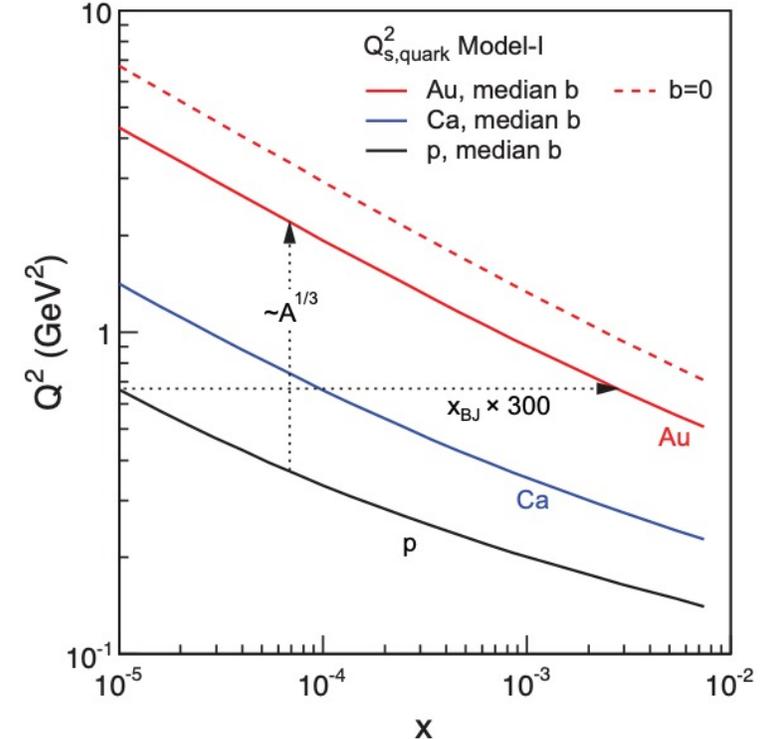
J. L. Albacete and C. Marquet, PRL 105, 162301 (2010)



$Q_s \propto T_A(b) \propto 1/b$:
 smaller b , larger $Q_s \rightarrow$ easier to reach saturation region

[Woods-Saxon potential: \$T_A\(b\)\$](#)

arXiv: 1212.1701



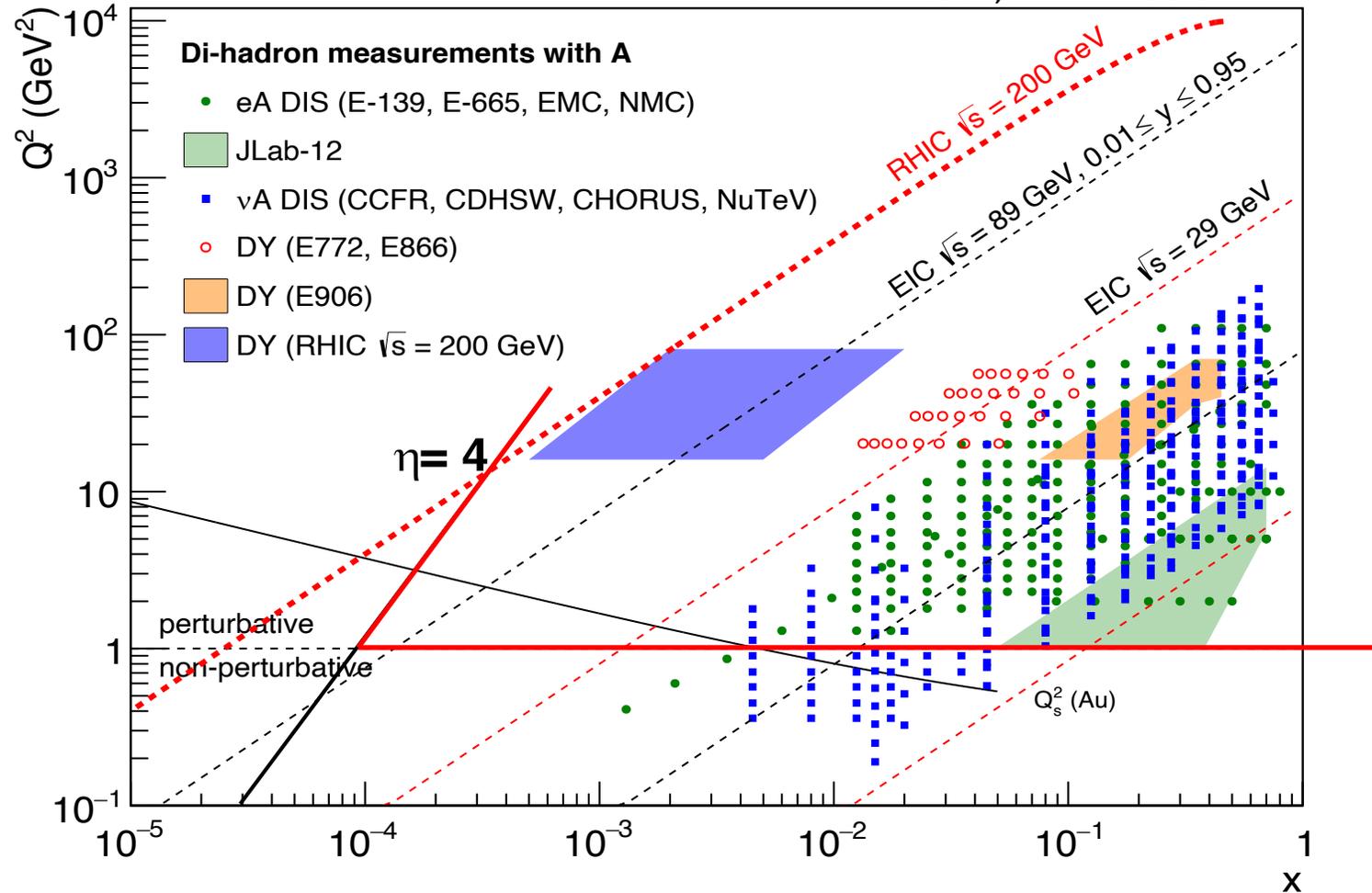
$Q_s \propto A^{1/3}$:
 Larger A , larger $Q_s \rightarrow$ easier to reach saturation region

Do we observe the nonlinear gluon dynamics signatures from recent STAR p+p, p+A, and d+A data?

- **p+p, p+Al, and p+Au collisions:** STAR, arXiv: 2111.10396
 - d+Au collisions: STAR preliminary results

STAR data in $x - Q^2$ phase space

R. Abdul Khalek et al., arXiv:2103.05419

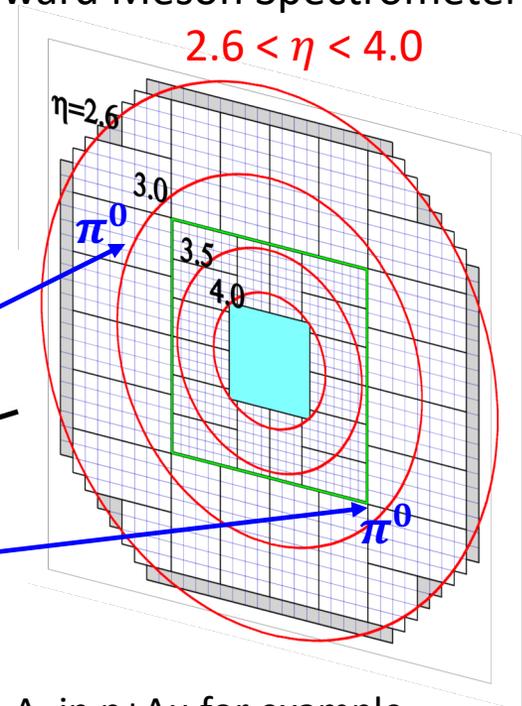


STAR data can access linear-nonlinear transition region

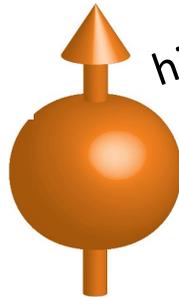
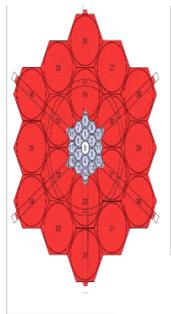
Di- π^0 measurement at STAR

- **p+p, p+Al, p+Au and d+Au** collisions at $\sqrt{s_{NN}} = 200$ GeV
- $NN \rightarrow \pi^0 + \pi^0 + X$, π^0 detected by FMS with $2.6 < \eta < 4.0$
- **Event activity (E.A.):** energy deposition at BBC describes the degree of the p+A collisions
- **Observable:** $C(\Delta\phi) = \frac{N_{pair}(\Delta\phi)}{N_{trig} \times \Delta\phi_{bin}}$, $\pi^0_{trig} \rightarrow$ higher p_T

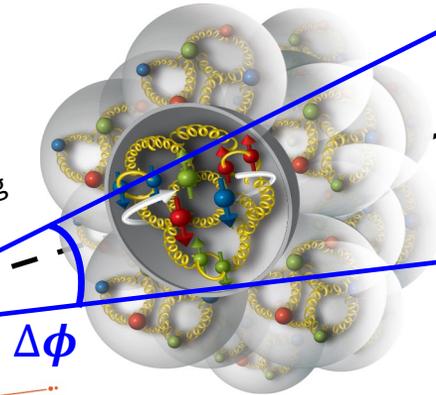
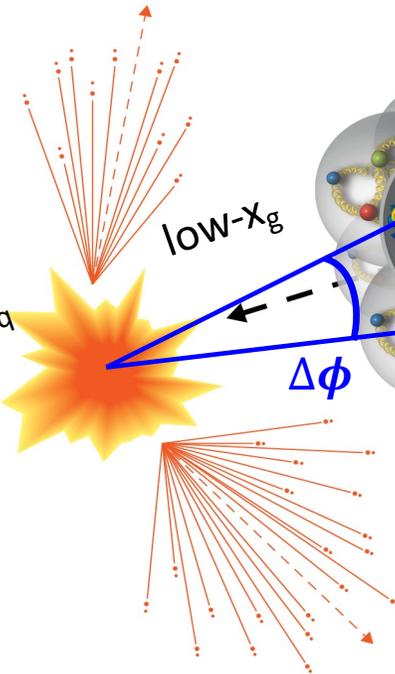
Forward Meson Spectrometer (FMS)



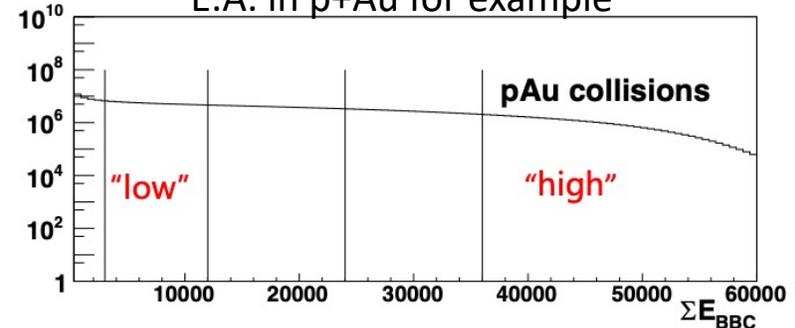
Beam beam counter (BBC)
(inner BBC: $-5 < \eta < -3.3$)



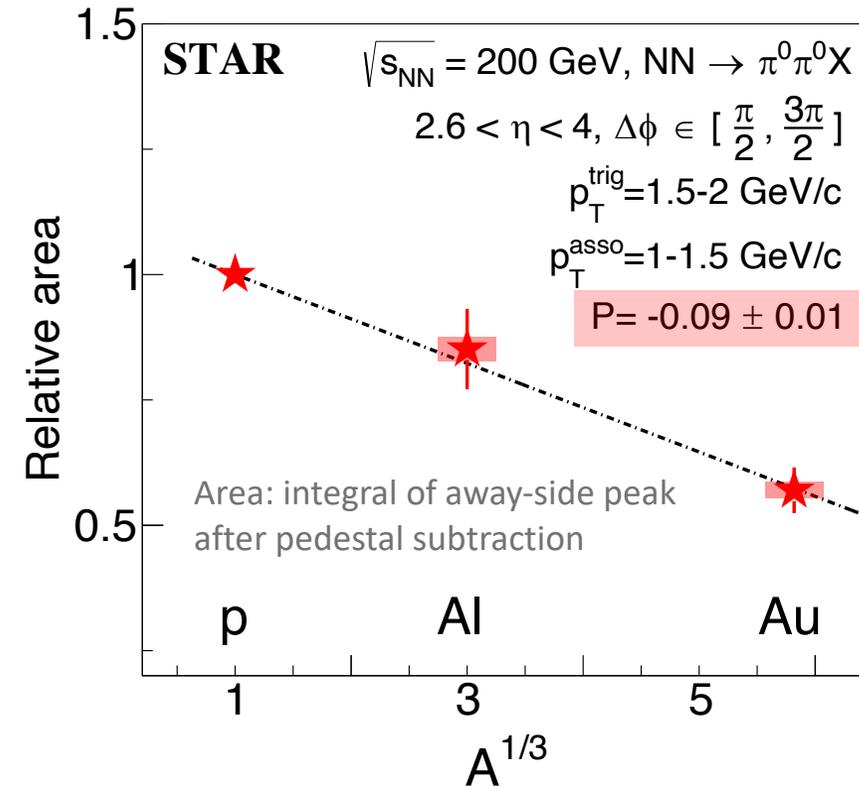
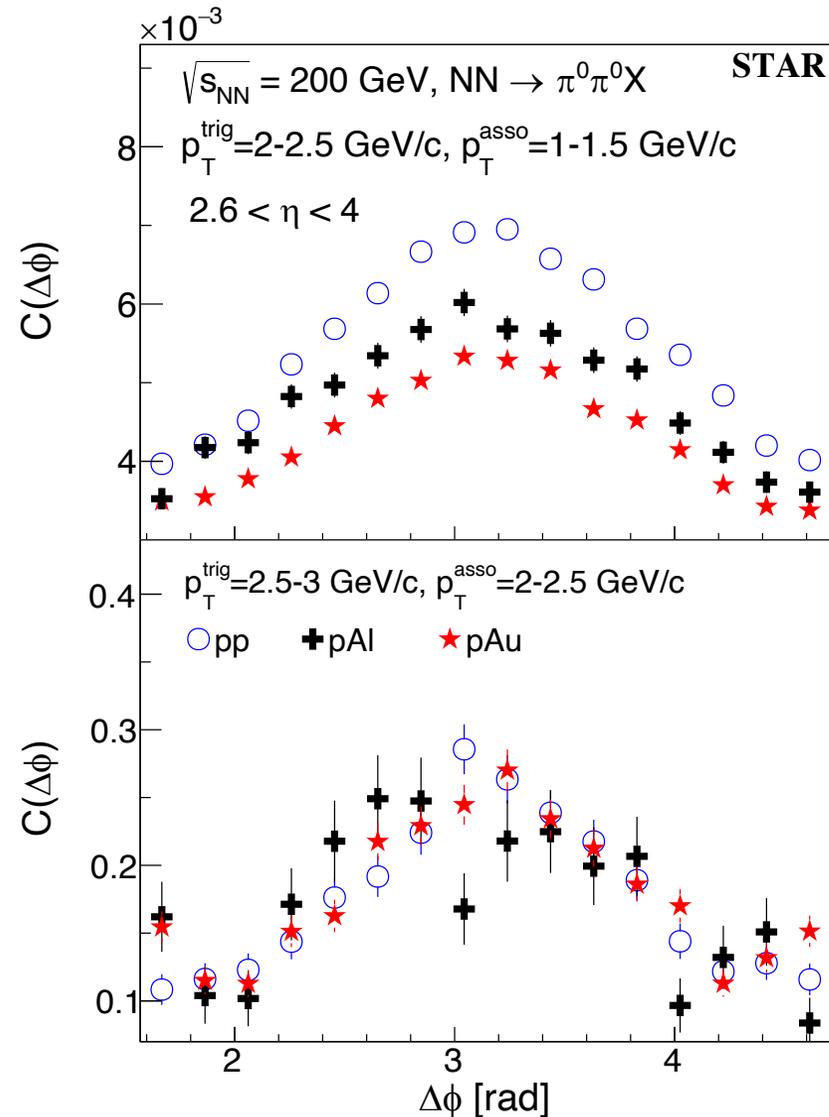
high- x_a



E.A. in p+Au for example

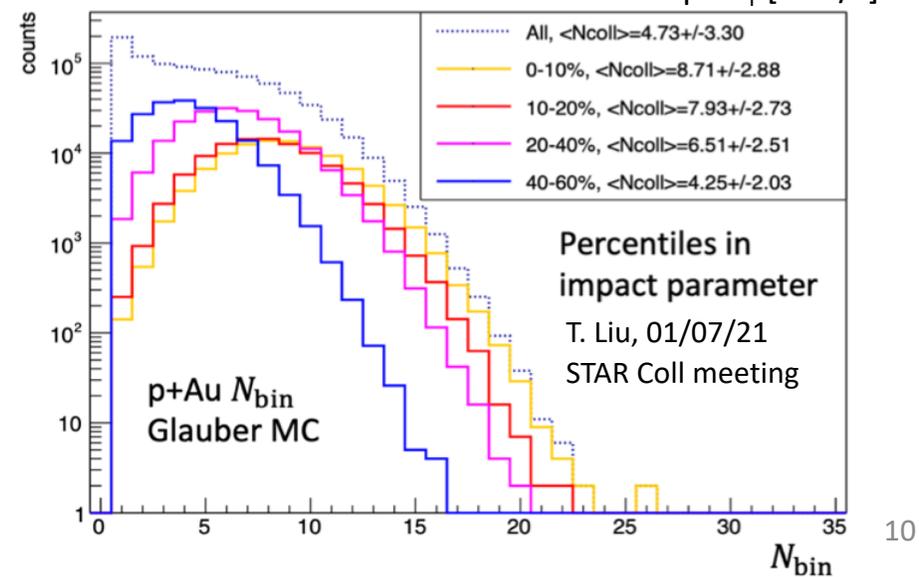
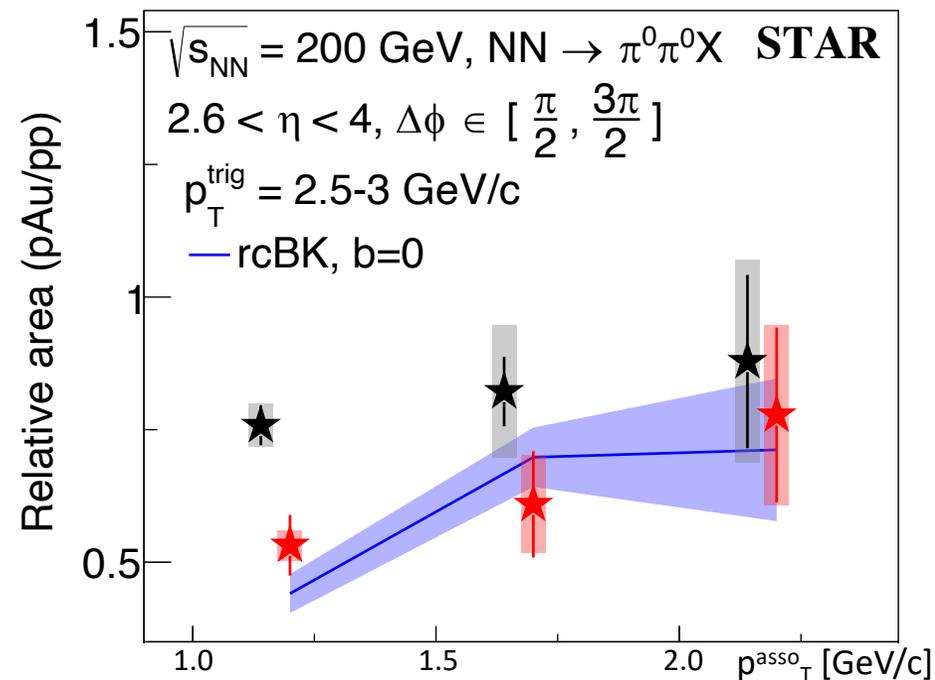
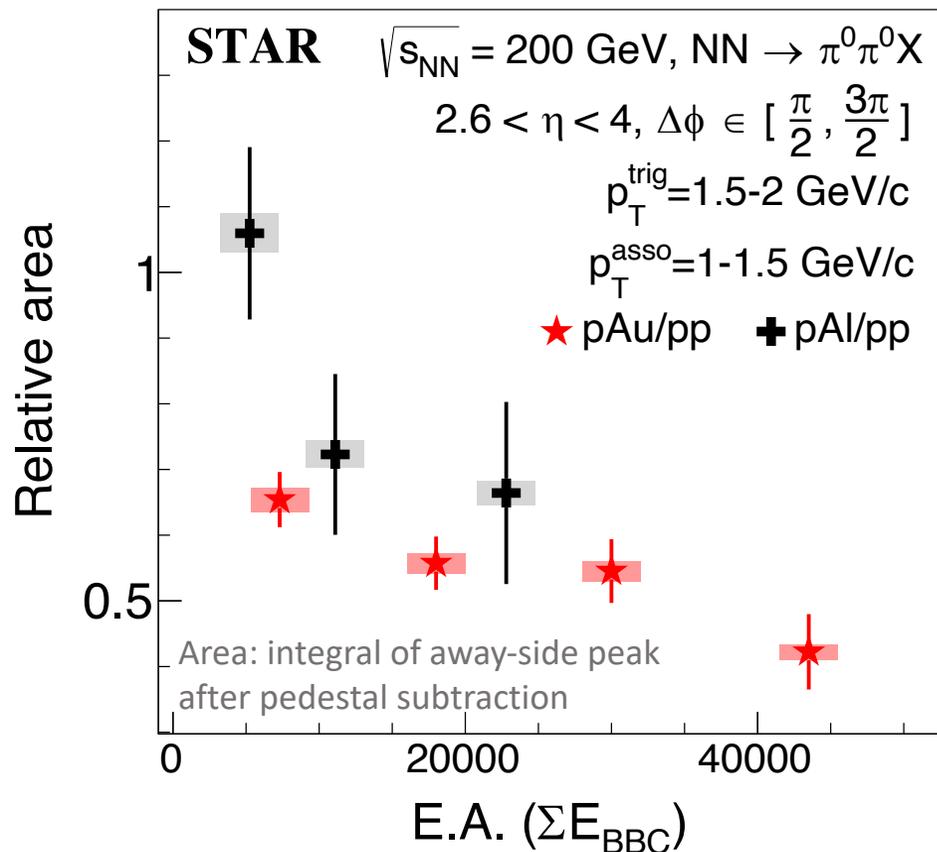


p_T and A dependence



- Suppression at low p_T not high p_T
- Fixed p_T (smallest p_T) bin $\rightarrow x - Q^2$ phase space is fixed, suppression is dominantly affected by various A:
 - Suppression linearly depends on $A^{1/3}$
 - Slope from the fitting = -0.09 ± 0.01

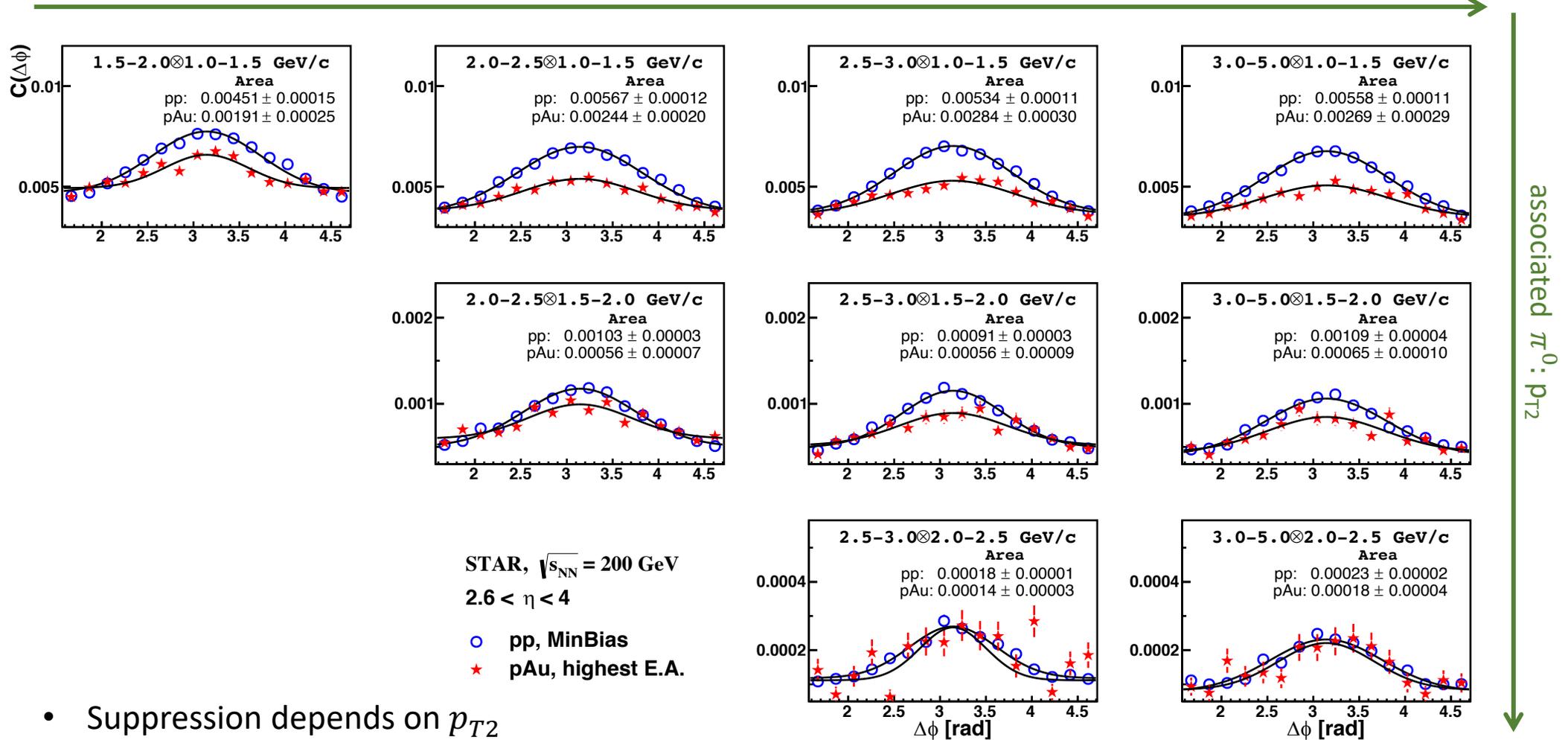
E.A. dependence



- Suppression increases with E.A., highest E.A. data is consistent with predictions at $b = 0$
- Traditional definition of centrality doesn't work well for small systems: what is the variable best correlated with b in small systems?

Full p_T picture

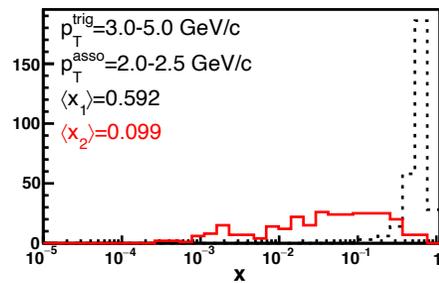
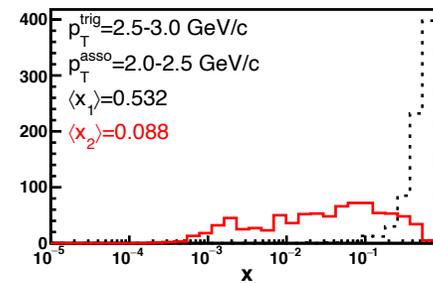
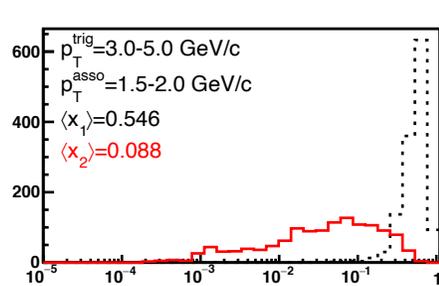
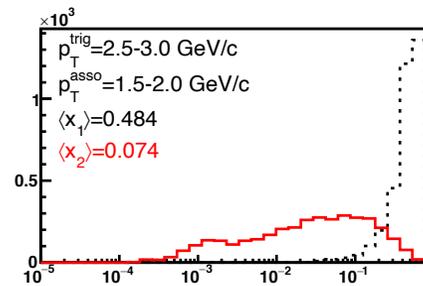
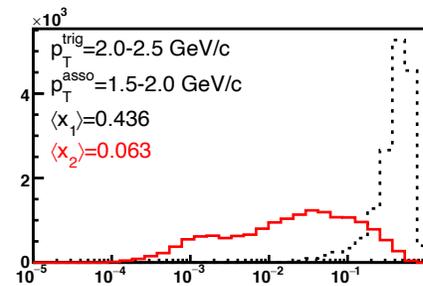
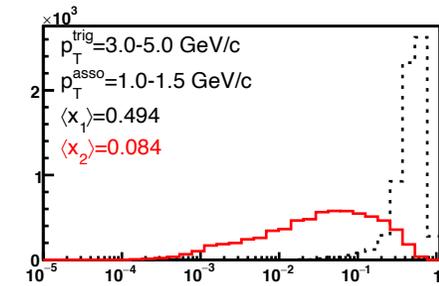
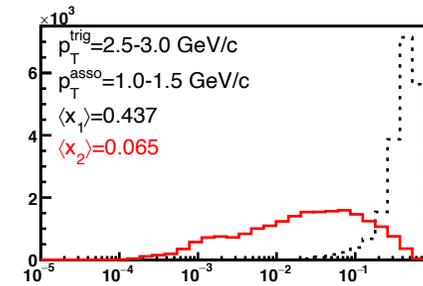
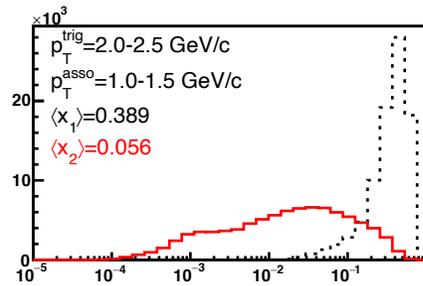
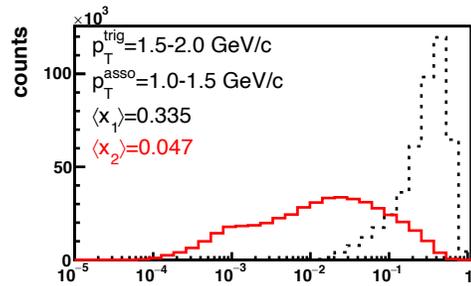
trigger π^0 : p_{T1}



- Suppression depends on p_{T2}
- At fixed p_{T2} , suppression rarely depends p_{T1}

Simulated x

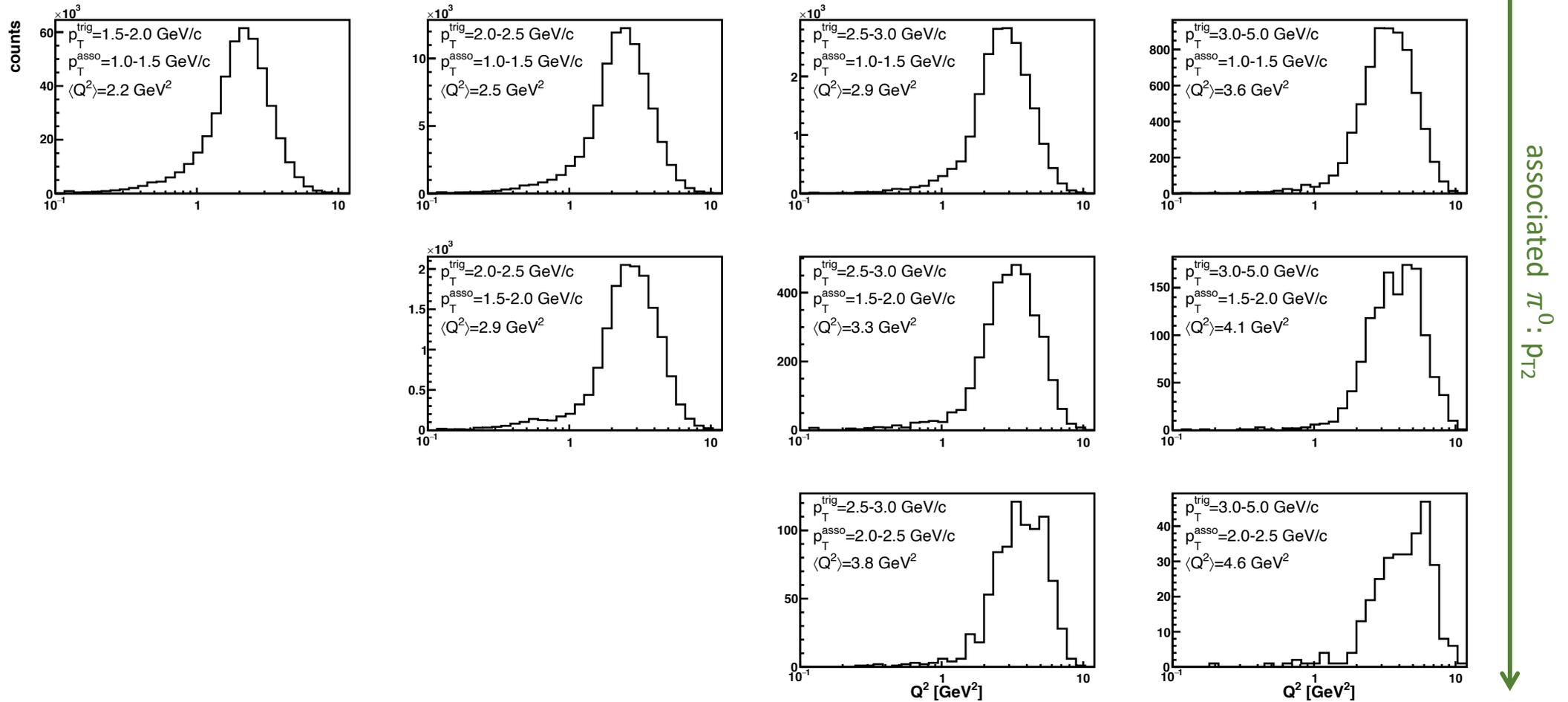
trigger π^0 : p_{T1}



associated π^0 : p_{T2}

Simulated Q^2

trigger π^0 : p_{T1}

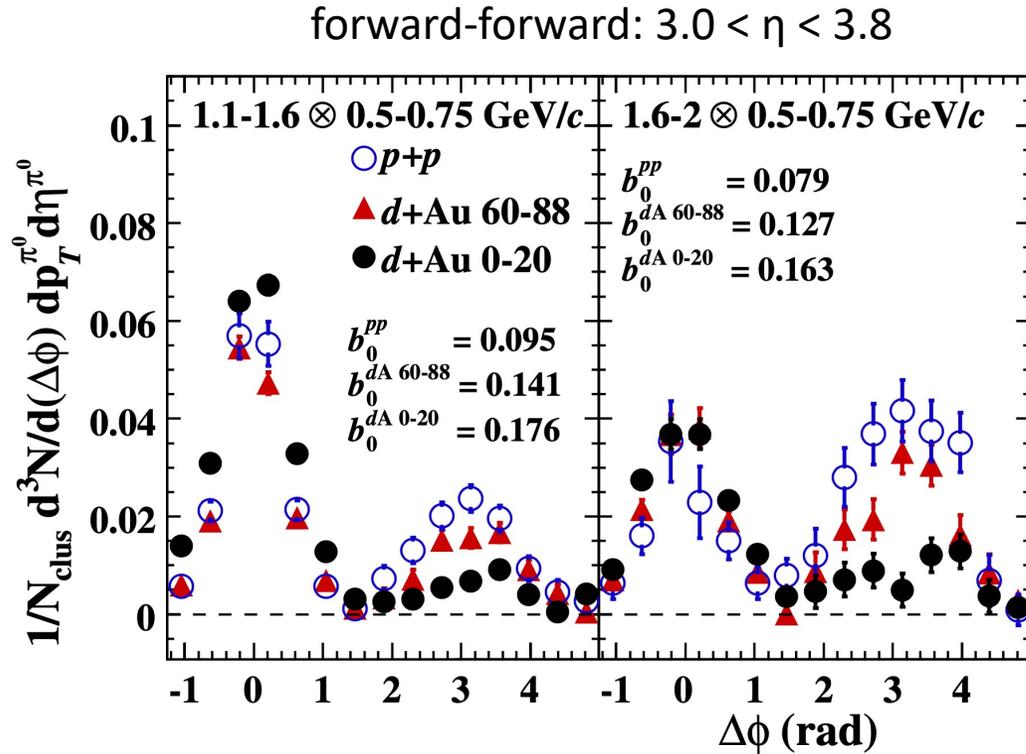


Do we observe the nonlinear gluon dynamics signatures from recent STAR p+p, p+A, and d+A data?

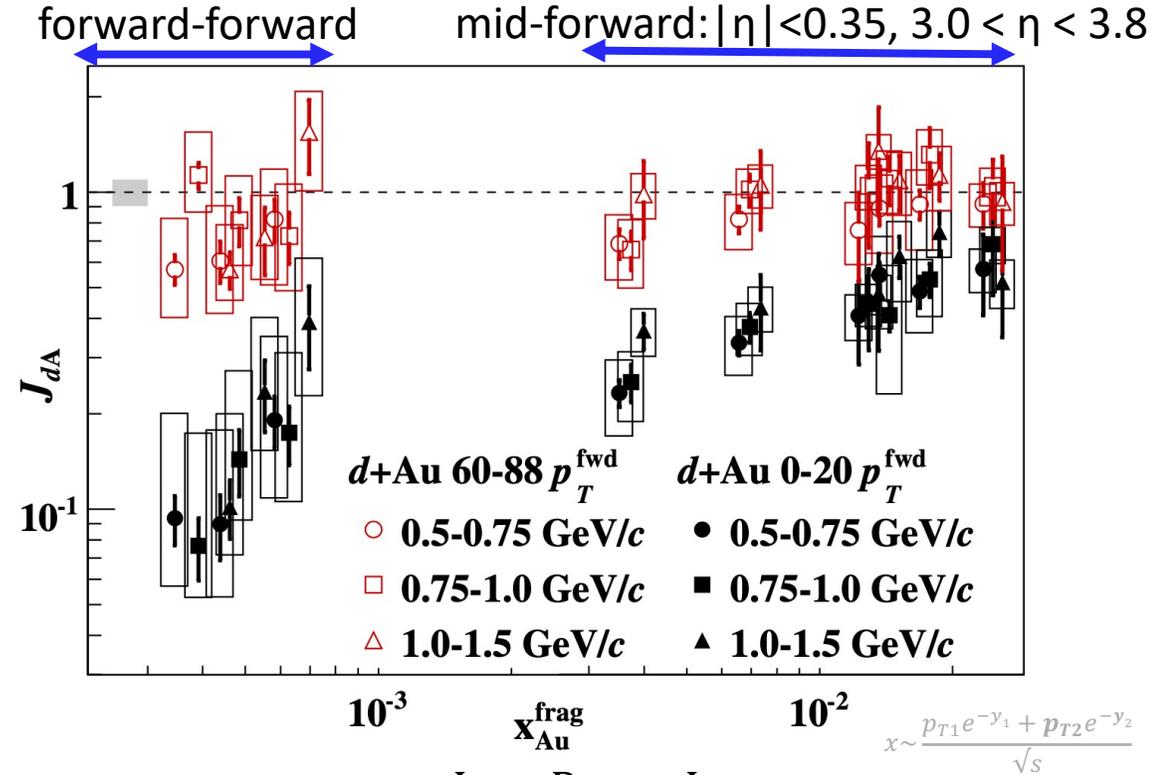
- **p+p**, p+Al, and **p+Au collisions**: STAR, arXiv: 2111.10396
 - **d+Au collisions**: STAR preliminary results

PHENIX data

PHENIX, PRL 107, 172301 (2011)



Note: $\Delta\phi$ distribution normalized by N_{trig}



$$J_{dA} = R_{dAu} \times I_{dAu}$$

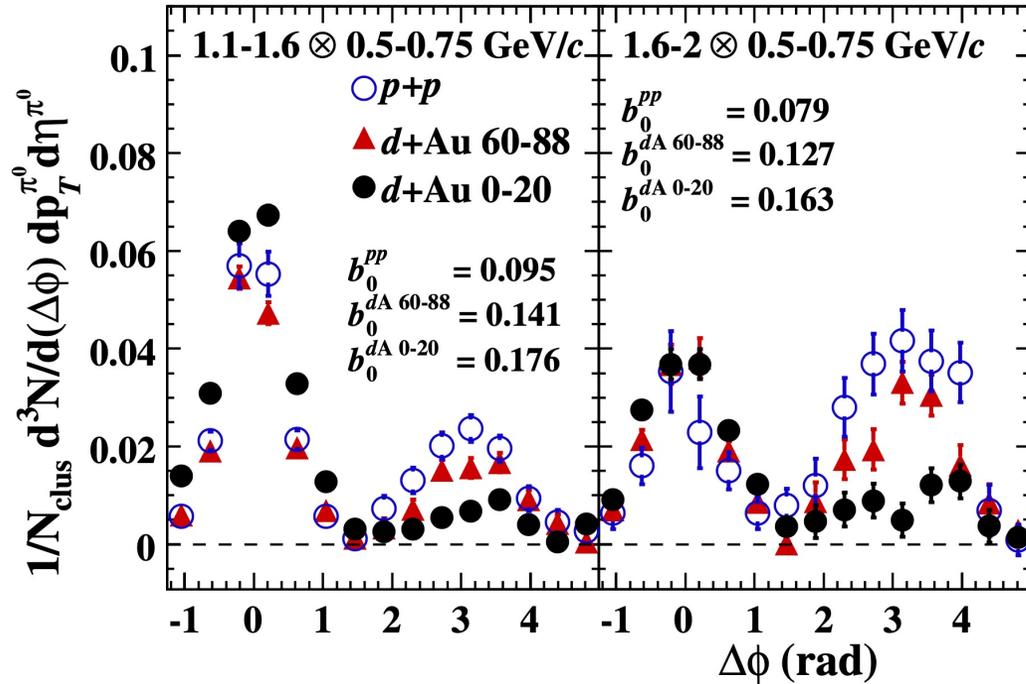
I_{dAu} : area ratio dAu/pp \rightarrow what STAR measured

- **Away-side correlation:** suppression dependence on rapidity and centrality is studied by PHENIX

Note: $\Delta\phi$ distribution normalized by N_{trig}

Other thoughts for PHENIX data

forward-forward: $3.0 < \eta < 3.8$



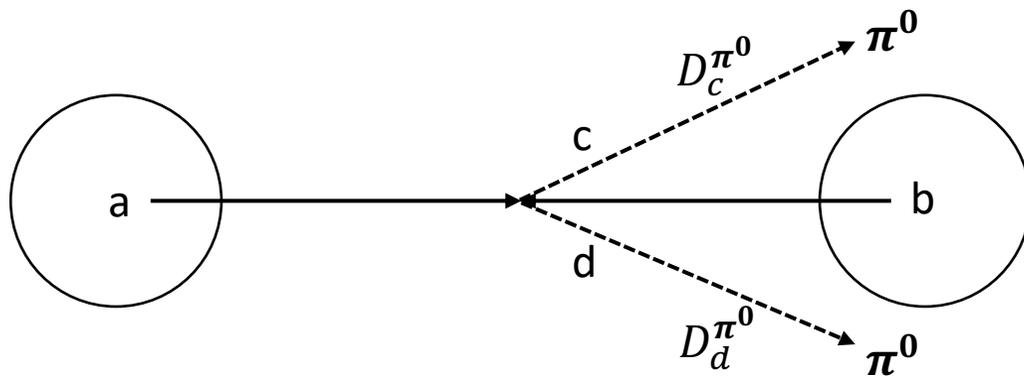
Low p_T	Pedestal ratio (central dAu/pp): 1.9
High p_T	Pedestal ratio (central dAu/pp): 2.1

- **Pedestal:** high pedestal in d+Au; ratio(d+Au/pp) tends to increase with p_T
PRD 83, 034029 (2011) → double parton interactions (**DPS**) in d+Au? → correlation is also affected by DPS?
- **Motivation of performing the similar measurement at STAR** → Impact of DPS in d+Au; complementary studies

Di- π^0 from SPS/DPS

M. Strikman and W. Vogelsang,
PRD 83, 034029 (2011)

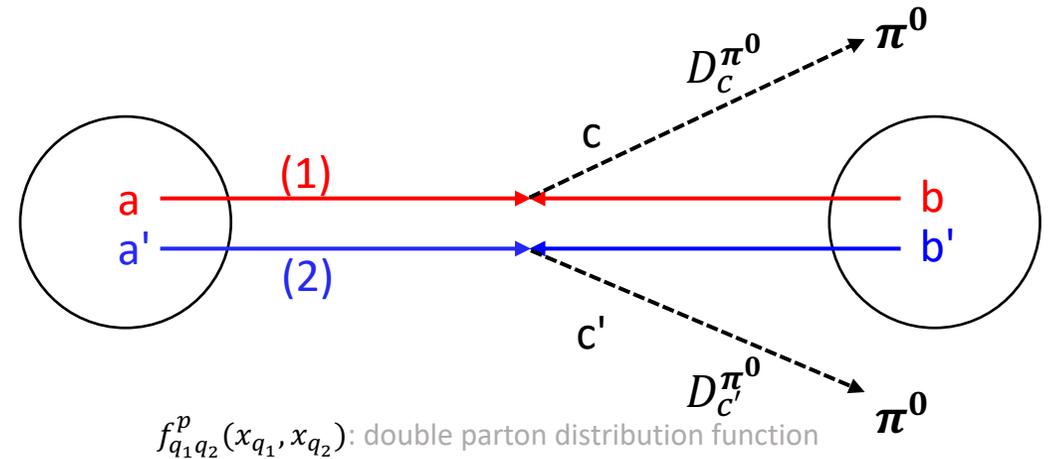
Single parton scattering (SPS) in pp: $a+b \rightarrow c+d+X$



Leading-twist (LT) mechanism

$$\sigma_{LT} \propto f_a^p(x_a) \otimes f_b^p(x_b) \otimes \sigma^{ab \rightarrow cdX} \otimes D_c^{\pi^0} \otimes D_d^{\pi^0}$$

Double parton scattering (DPS) in pp: $a+b \rightarrow c+X$ and $a'+b' \rightarrow c'+X$



$f_{q_1 q_2}^p(x_{q_1}, x_{q_2})$: double parton distribution function

$$\sigma_{double} \propto f_{aa'}^p(x_a, x_{a'}) \otimes f_{bb'}^p(x_b, x_{b'})$$

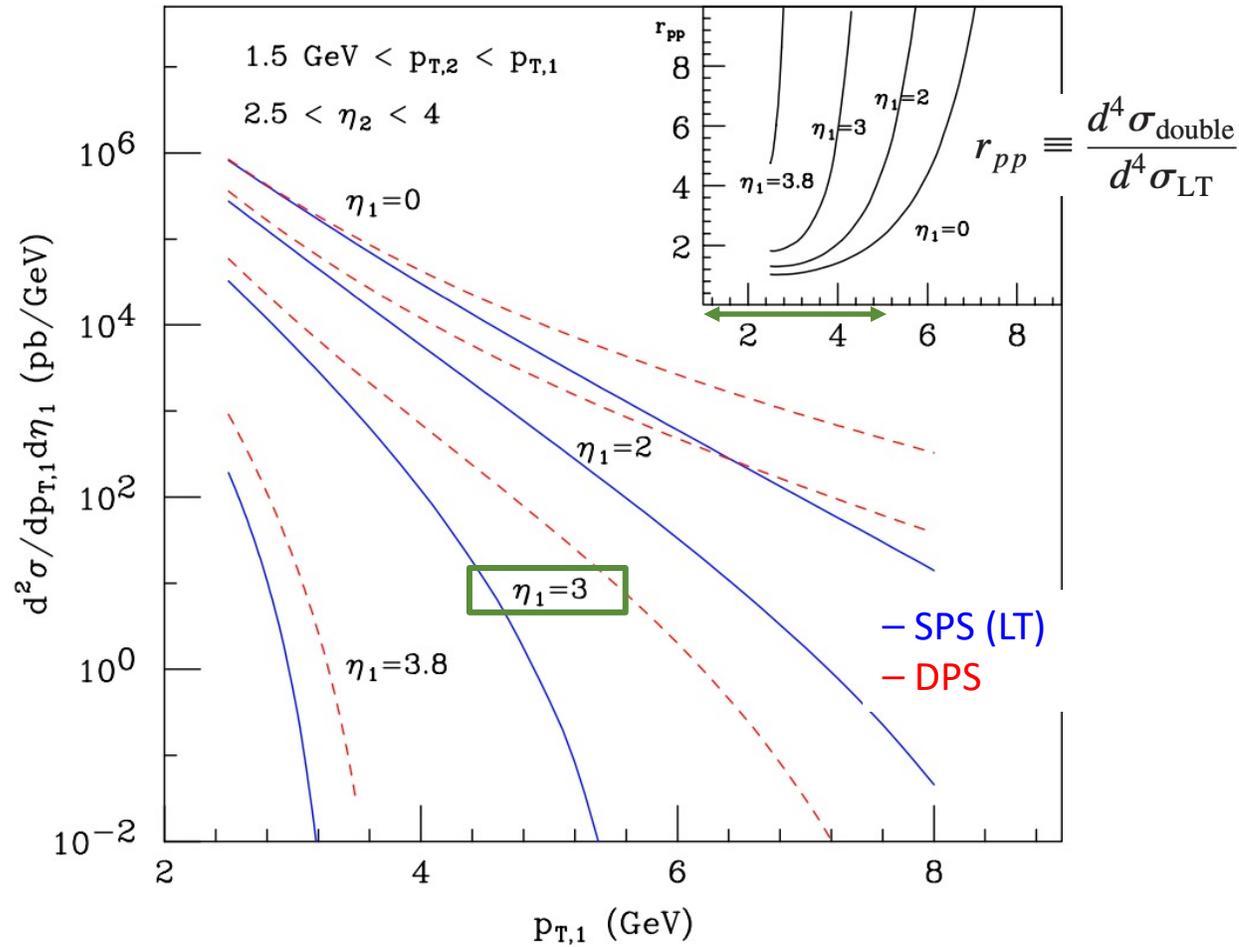
$$\otimes \sigma^{ab \rightarrow cX} \otimes D_c^{\pi^0} \quad (1)$$

$$\otimes \sigma^{a'b' \rightarrow c'X'} \otimes D_{c'}^{\pi^0} \quad (2)$$

If q_1, q_2 correlated: $f_{q_1 q_2}^p(x_{q_1}, x_{q_2}) \neq f_{q_1}^p(x_{q_1}) f_{q_2}^p(x_{q_2})$

If q_1, q_2 uncorrelated: $f_{q_1 q_2}^p(x_{q_1}, x_{q_2}) = f_{q_1}^p(x_{q_1}) f_{q_2}^p(x_{q_2})$

DPS dominates at forward rapidities

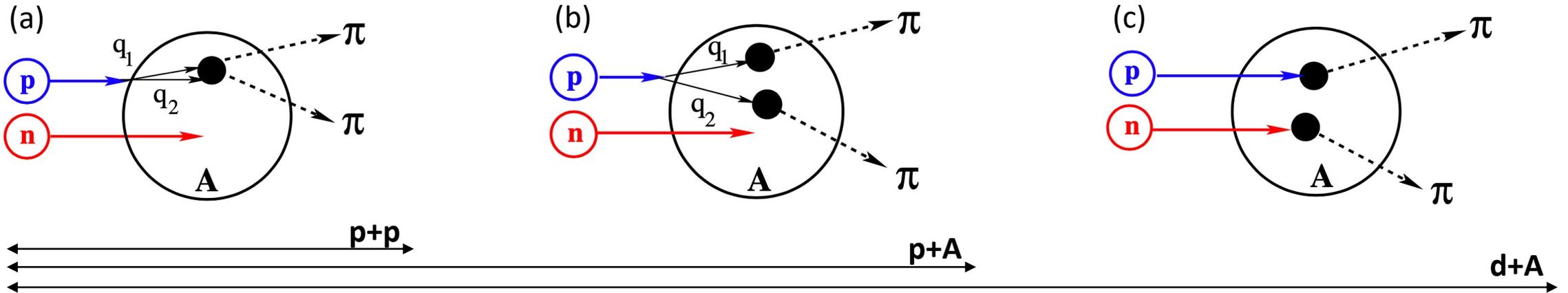


- DPS is enhanced and not negligible at high rapidities
- Green box and arrow represent the kinematics STAR data can reach

DPS in d+Au?

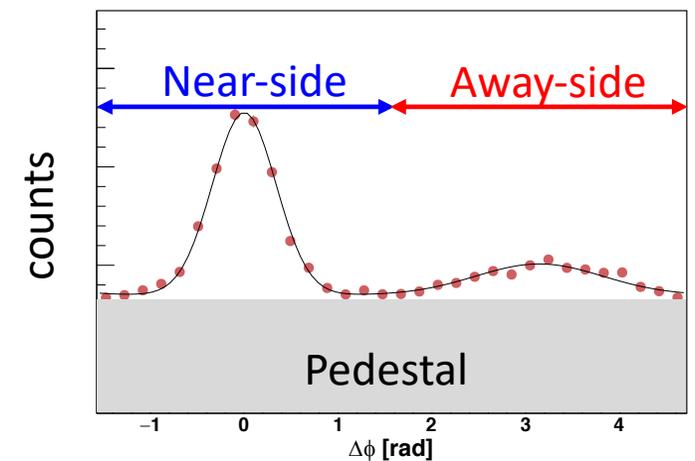
M. Strikman and W. Vogelsang,
PRD 83, 034029 (2011)

Examples contribution of DPS

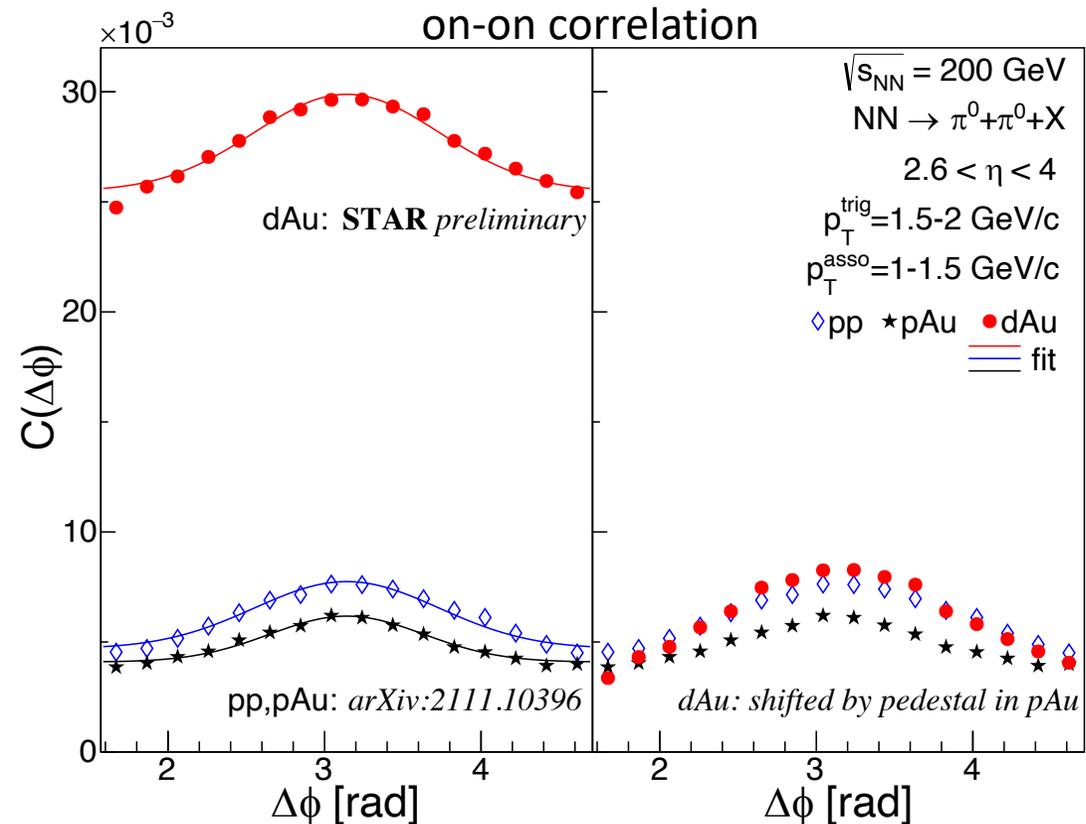
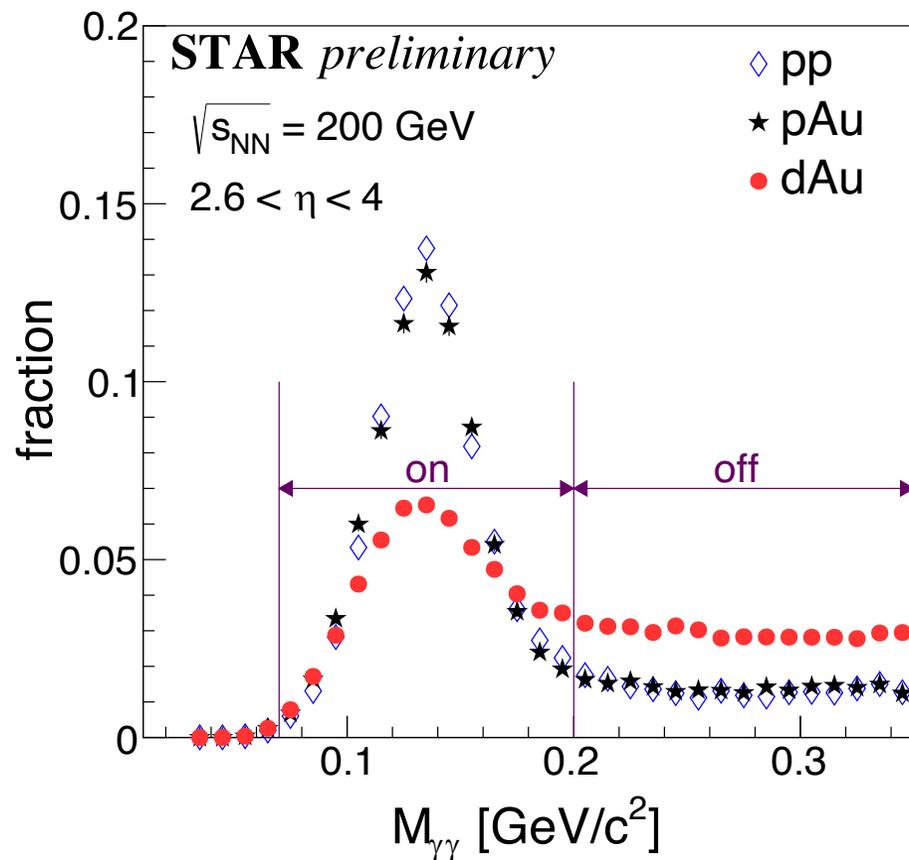


Comparison of p+p, p+Au and d+Au \rightarrow study the individual source of DPS

- **Compare pedestal:** DPS provides an explanation of higher pedestal in d+Au
- **Compare away-side correlation \rightarrow window open to studies of double parton distributions in nucleons:**
 - q_1, q_2 correlated: DPS enhances the correlation
 - q_1, q_2 uncorrelated: DPS will only enhance pedestal



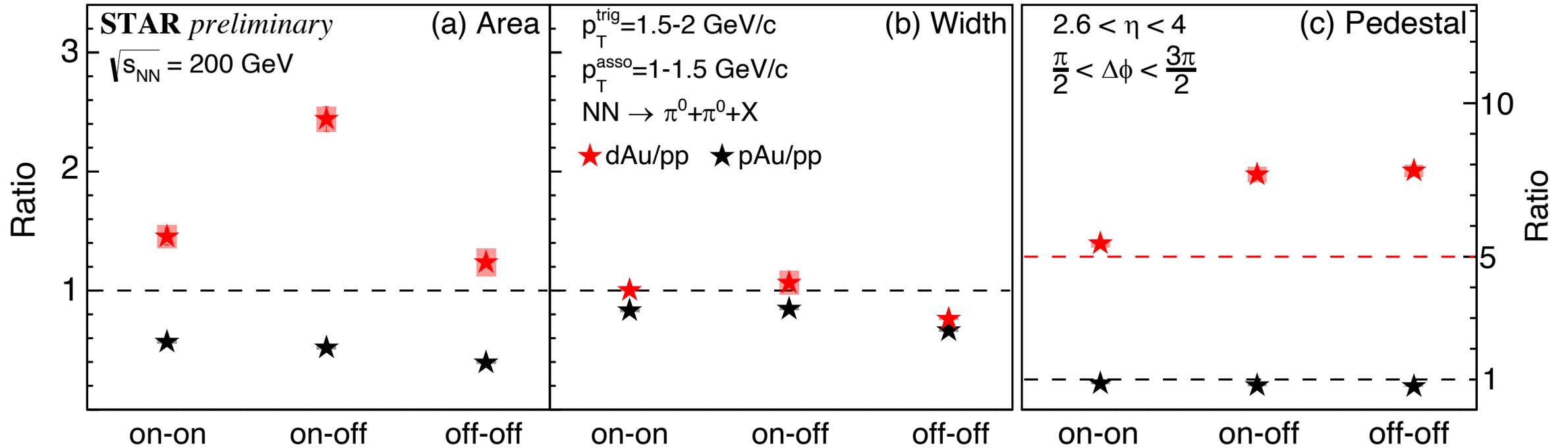
p+p, p+Au and d+Au comparison



S/(S+B)	STAR	PHENIX (PhD thesis)
p+p	82%	81%
d+Au	58%	73%

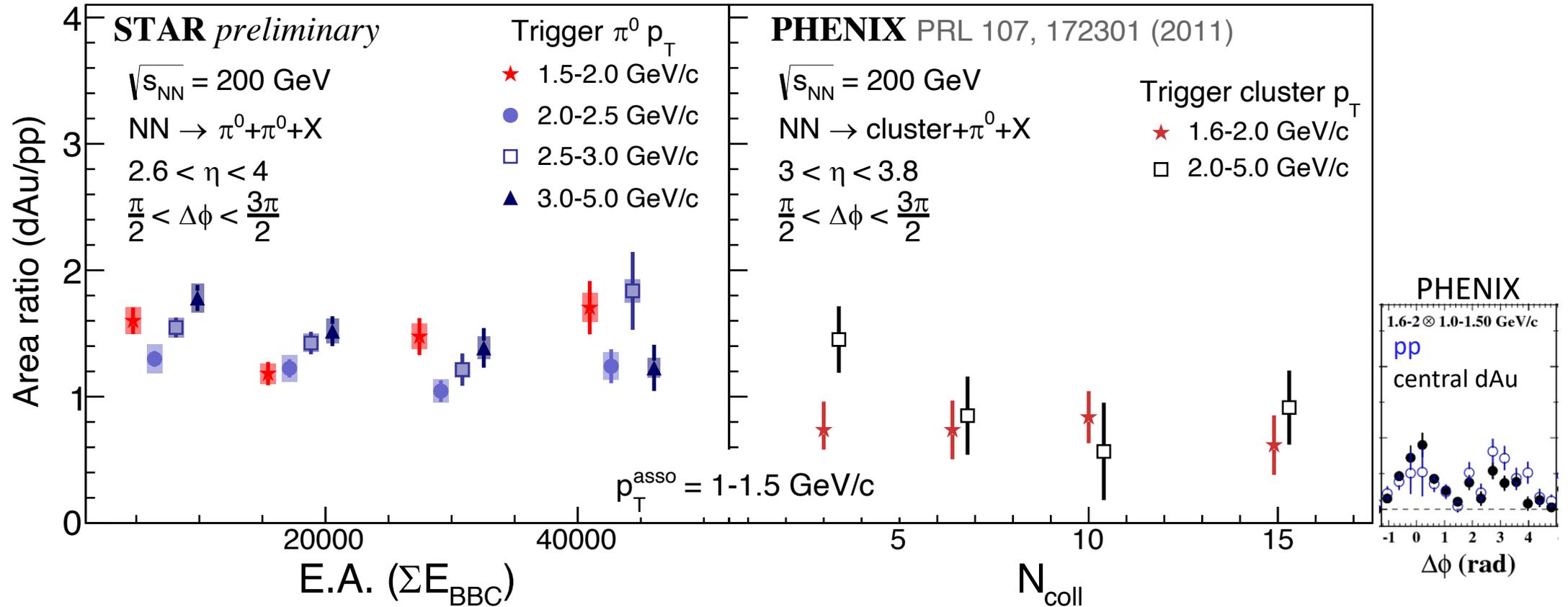
- π^0 PID: much higher background in d+Au than p+p (Au)
- Very high pedestal: d+Au > 5 times higher compared to p+p (Au)
- Away-side: enhancement in d+Au compared to p+Au

Combinatoric contributions in d+Au



- Area: contribution from off mass window is high in d+Au
 - not fair to directly compare d+Au and p+p without background subtraction, but we don't fully understand the background correlation
 - potential enhancement lead by DPS can not be determined so far...
- Width: roughly stable in three collision systems → no broadening
- Pedestal: d+Au/p+p > 5; d+Au/p+p ~ 1 → no DPS in p+Au, but is there DPS in d+Au?

E.A. dependence in d+Au

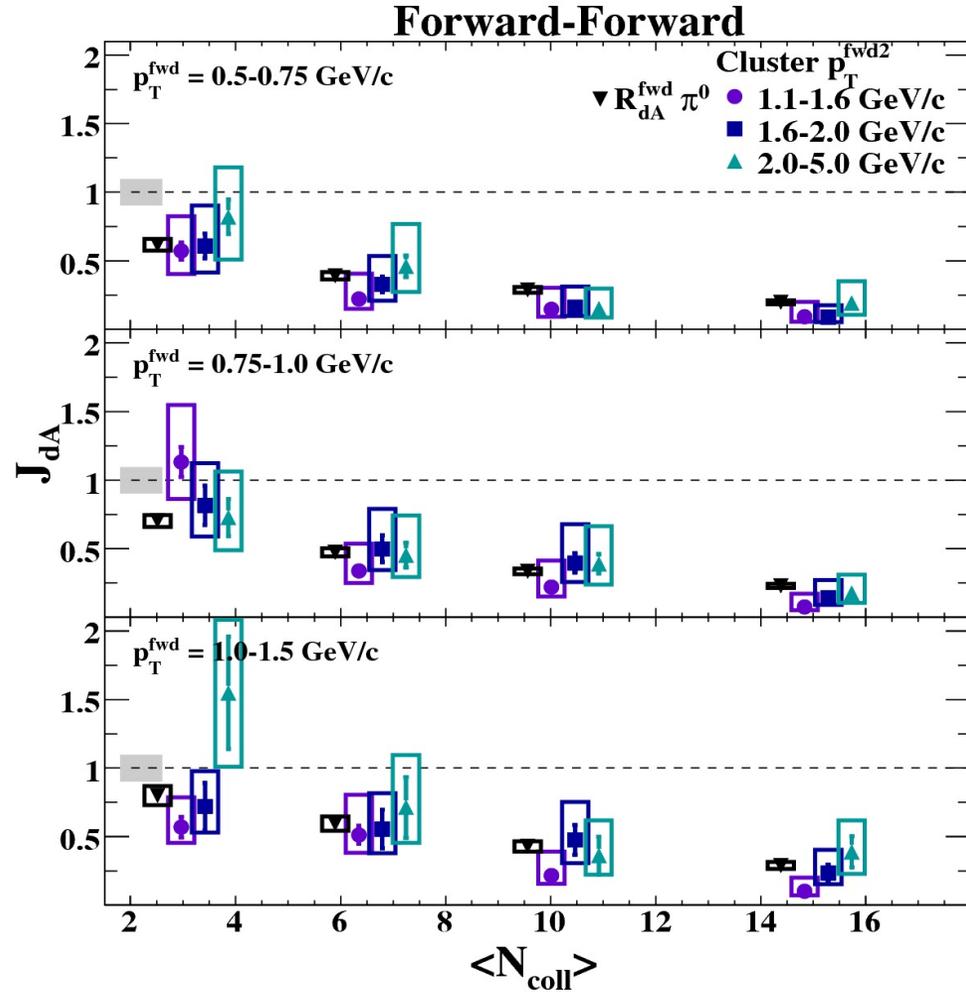


- In the overlapping p_T range of two collaborations, no suppression or E.A. dependence in d+Au relative to p+p
- Suppression exits at very low p_T at PHENIX, where STAR cannot reach

How to describe suppression?

PHENIX, PRL 107, 172301

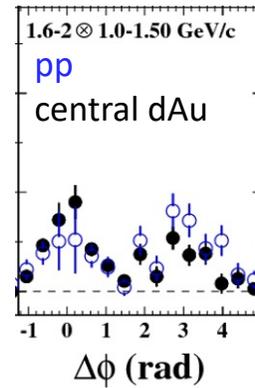
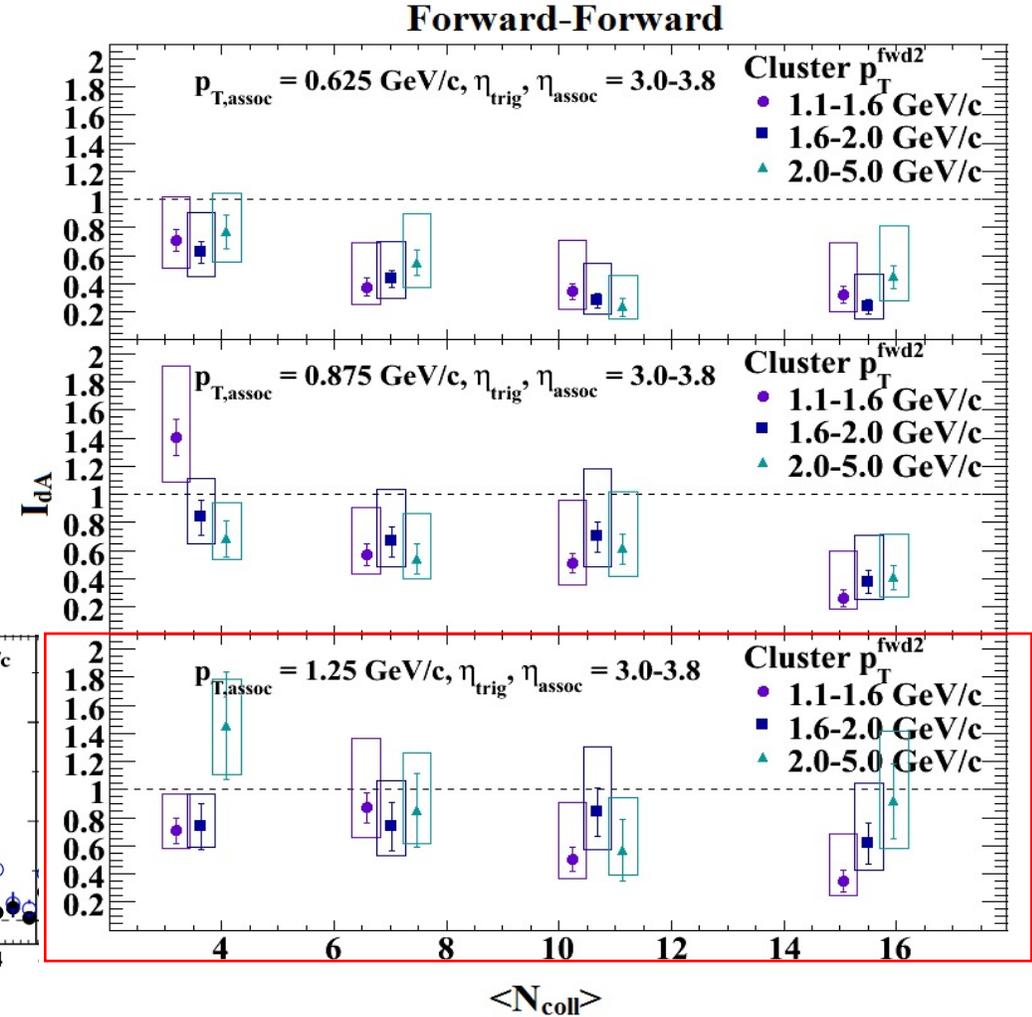
[PhD thesis](#)



$$J_{dA} = I_{dA} * R_{dAu}$$

$$I_{dA} = \text{area ratio}$$

$$R_{dAu} \sim 2/N_{\text{coll}}$$

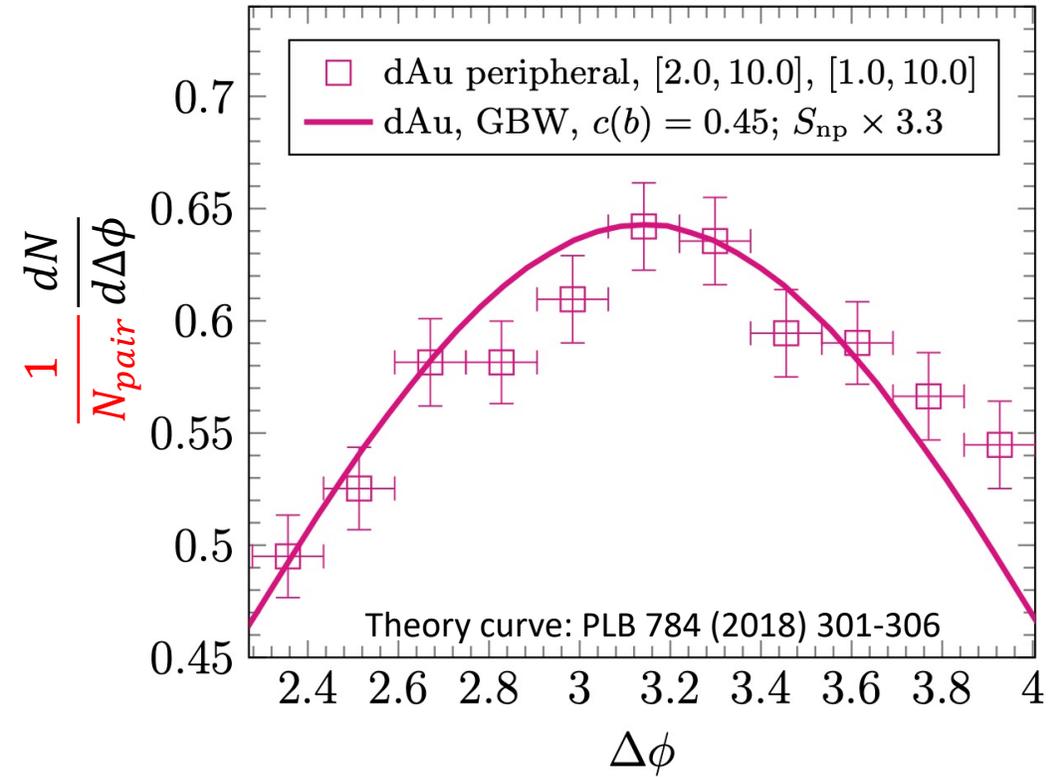
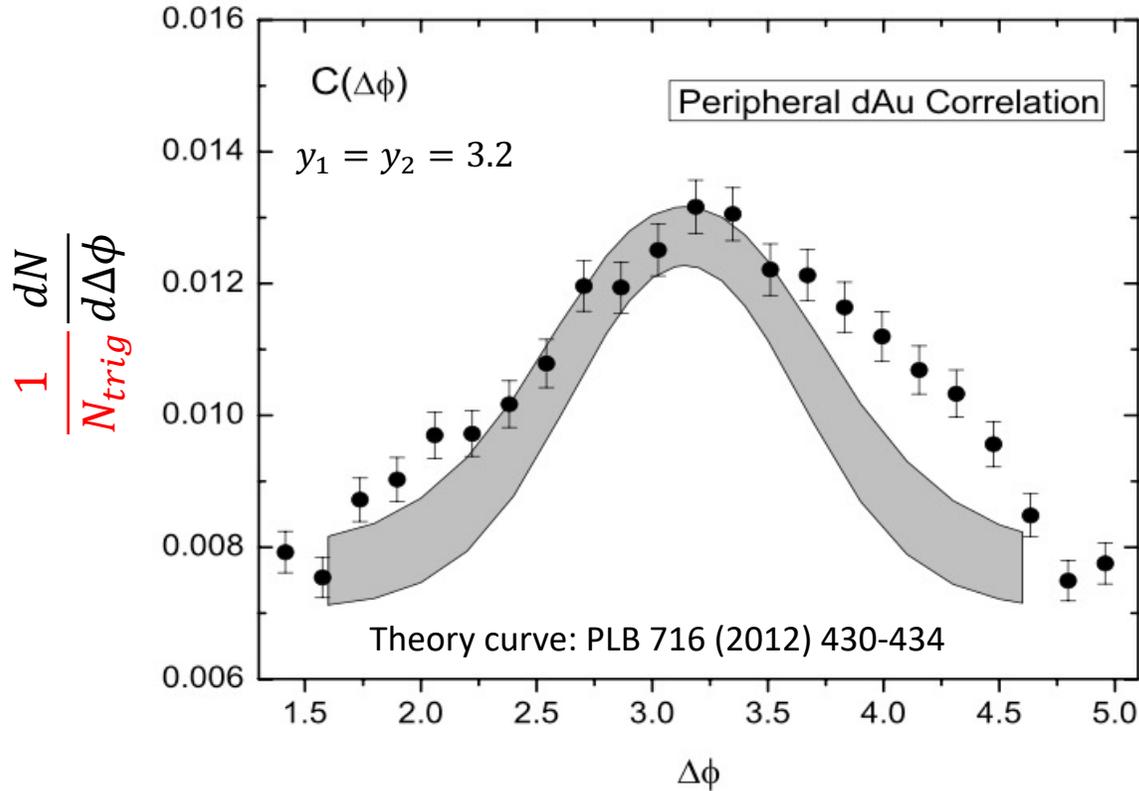


" $J_{dAu} \rightarrow 0.1$ that "10 times suppression observed in central dAu" should be clarified

In fact, in the highest associated p_T bin (red box), no suppression or centrality dependence is observed

How to normalize?

Data: STAR preliminary, NPA 854, 168 (2011); Theory: A. Stasto et al., GBW model for CGC

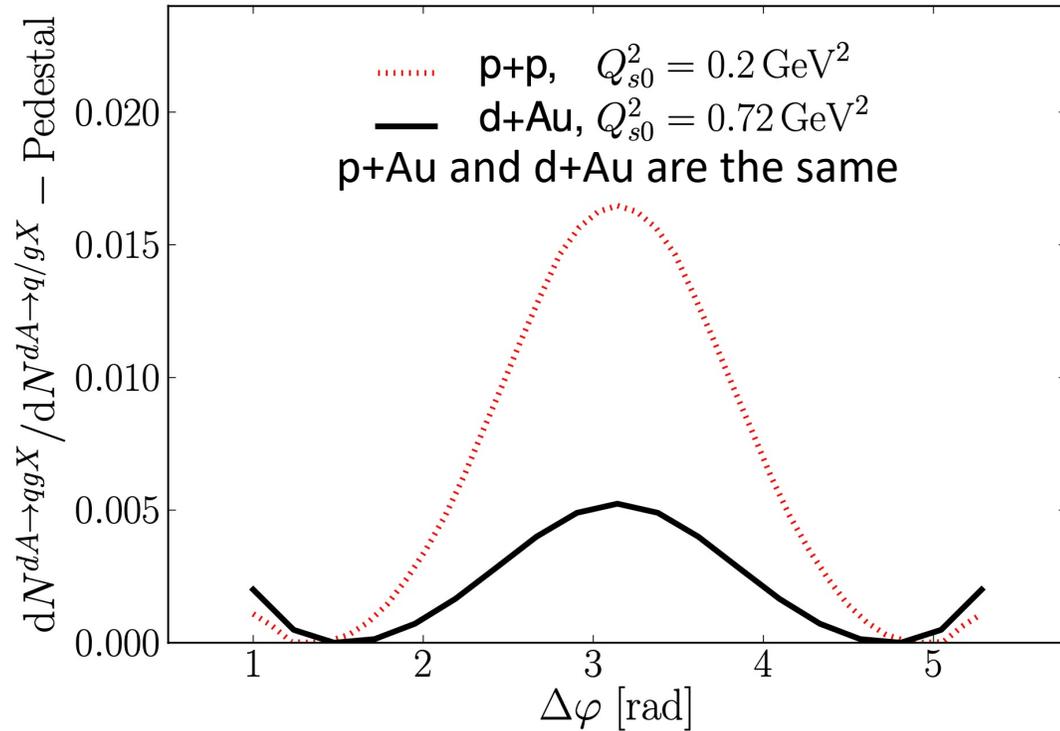


- CGC predictions based on GBW model with Sudakov effects included agrees with data better
- Two ways of normalization used: correlation function normalized by N_{trig} not N_{pair}
 - PLB 716 (2012) 430-434: normalized by N_{trig} , but issues found with p+p normalization
 - PLB 784 (2018) 301-306: normalized by N_{pair} , issues with p+p normalization fixed

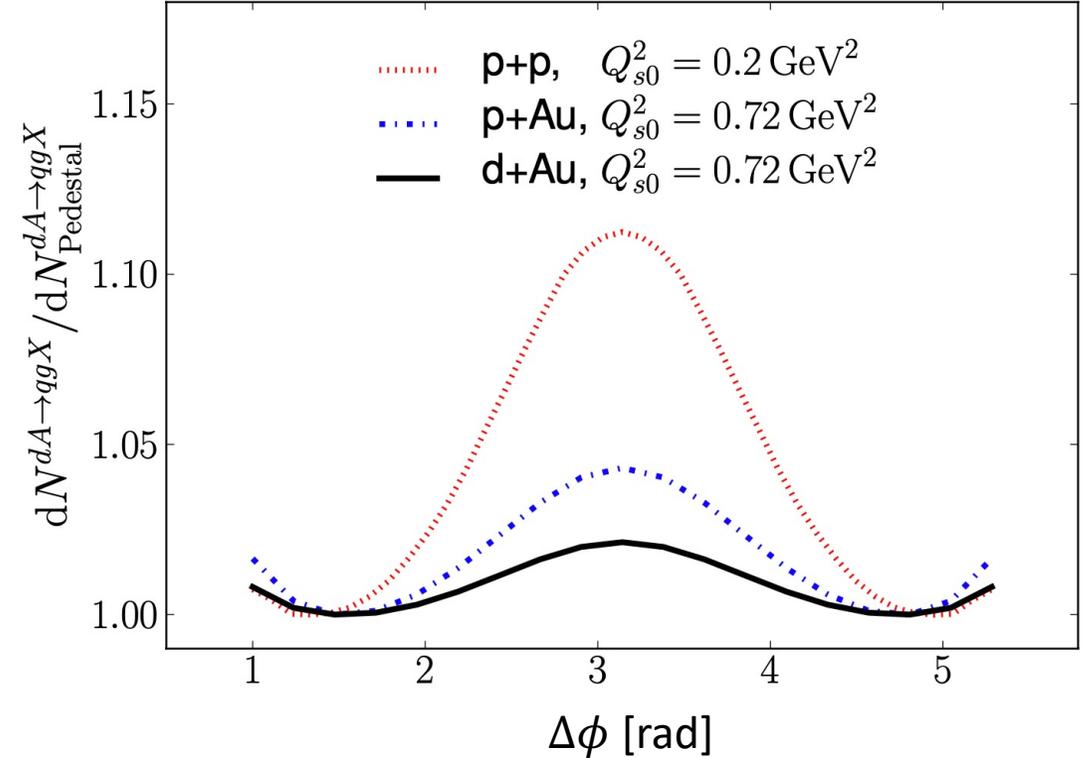
How to normalize?

T. Lappi and H. Mantysaari, NPA 908 (2013) 51-72

$$p_T^{trig} = 2 \text{ GeV}, p_T^{ass} = 1 \text{ GeV}, y_1 = y_2 = 3.4$$

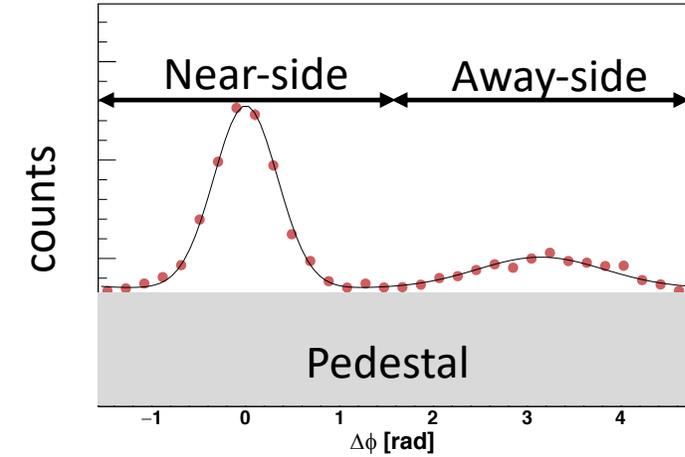


$$p_T^{trig} = 2 \text{ GeV}, p_T^{ass} = 1 \text{ GeV}, y_1 = y_2 = 3.4$$



- For the first time, the pedestal is predicted
- **Independent scattering of two partons** from the probe: $f_{q_1 q_2}^p(x_{q_1}, x_{q_2}) = f_{q_1}^p(x_{q_1}) f_{q_2}^p(x_{q_2})$
- Two ways of normalizations : Left: $\frac{N_{pair}(\Delta\phi)}{N_{trig}}$ – pedestal; right: $\frac{N_{pair}(\Delta\phi)}{N_{pair \text{ from pedestal}}}$

Normalize summary

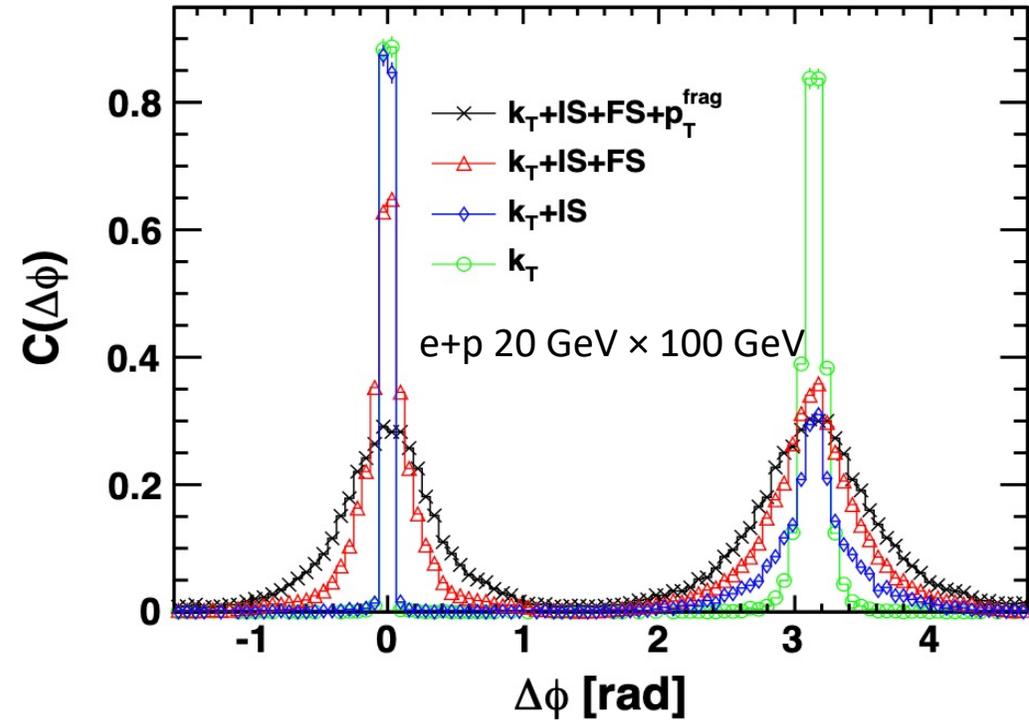
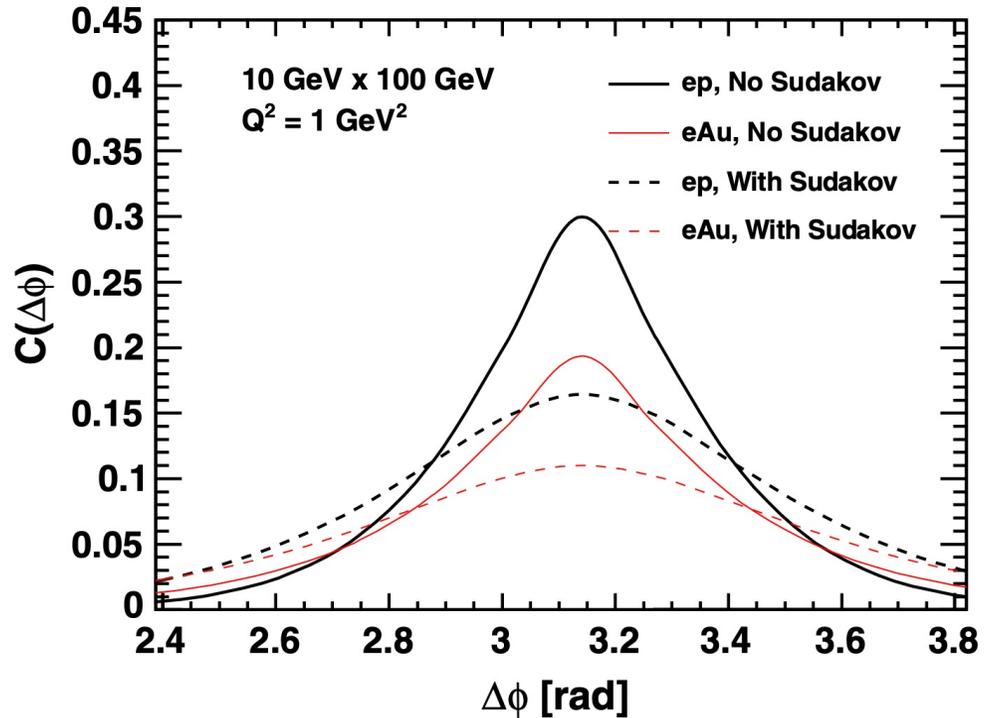


Experimental papers	Normalized by	Systems	Details
STAR	N_{trig}	p+p, p+Al, p+Au, d+Au	Compare area ratio
PHENIX	N_{trig}	p+p, d+Au	Compare area ratio $\times R_{dAu}$

Prediction papers	Normalized by	Systems	Details
1. NPA 748 (2005) 627-640	N_{pair}	p+p, d+Au	N_{pair} for entire $-\frac{1}{2}\pi < \Delta\phi < \frac{3}{2}\pi$ range
2. PLB 716 (2012) 430-434	N_{trig}	p+p, d+Au	same as experiment, issue with p+p
3. PLB 784 (2018) 301-306	N_{pair}	p+p, p+Au, d+Au	N_{pair} for back-to-back region: $\frac{1}{2}\pi < \Delta\phi < \frac{3}{2}\pi$
4. NPA 908 (2013) 51-72	N_{trig}	p+p, p+Au, d+Au	same as experiment
	N_{pair}	p+p, p+Au, d+Au	N_{pair} for pedestal
5. PRL 105, 162301 (2010)	N_{trig}	p+p, d+Au	same as experiment
6. PRD 99, 014002 (2019)	N_{trig}	p+p, p+Au, d+Au	same as experiment, used to compare with STAR data

Future measurement at EIC

L. Zheng et al.,
PRD 89 (2014) 074037



- Away side suppression is a combination of Sudakov (no nuclear dependence) and saturation effects?
- Sudakov effect can be estimated from the suppression at non-saturated region
- Away-side peak mainly affected by initial state parton shower (IS)
- Near-side peak mainly affected by final state parton shower (FS) and fragmentation p_T

Conclusion for theory

- Detailed signatures with back-to-back di-hadron correlation measurement from theory:
 - Suppression can be a consequence of both initial- and final-state effects
 - Initial effect \rightarrow CGC: A, E.A./centrality, p_T , and rapidity dependence predicted
 - Efforts needed to determine an observable correlated best with b for small systems
 - DPS in d+Au: both pedestal and correlation affected?

Conclusion for STAR

- Detailed signatures with back-to-back di-hadron correlation measurement from theory:
 - Suppression can be a consequence of both initial- and final-state effects
 - Initial effect \rightarrow CGC: A, E.A./centrality, p_T , and rapidity dependence predicted
 - Efforts needed to determine an observable correlated best with b for small systems
 - DPS in d+Au: both pedestal and correlation affected?
- p+p, p+Al, and p+Au results from STAR: A, E.A./centrality, p_T , and rapidity dependence observed
- d+Au results from STAR: Challenging to conclude
 - For nonlinear gluon dynamics: high background correlation not fully understood; favors for cleaner p+Au collisions
 - For DPS physics: favors for di-charged hadron correlation in p+p, p+A, and d+A

Clarifications

- Detailed signatures with back-to-back di-hadron correlation measurement from theory:
 - Suppression can be a consequence of both initial- and final-state effects
 - Initial effect \rightarrow CGC: A, E.A./centrality, p_T , and rapidity dependence predicted
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 - DPS in d+Au: both pedestal and correlation affected?
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 - For DPS physics: favors for di-charged hadron correlation in p+p, p+A, and d+A
- Uniform normalization needed
- Background contribution cannot be ignored from the data, be careful with predictions based on the results in d+Au collisions

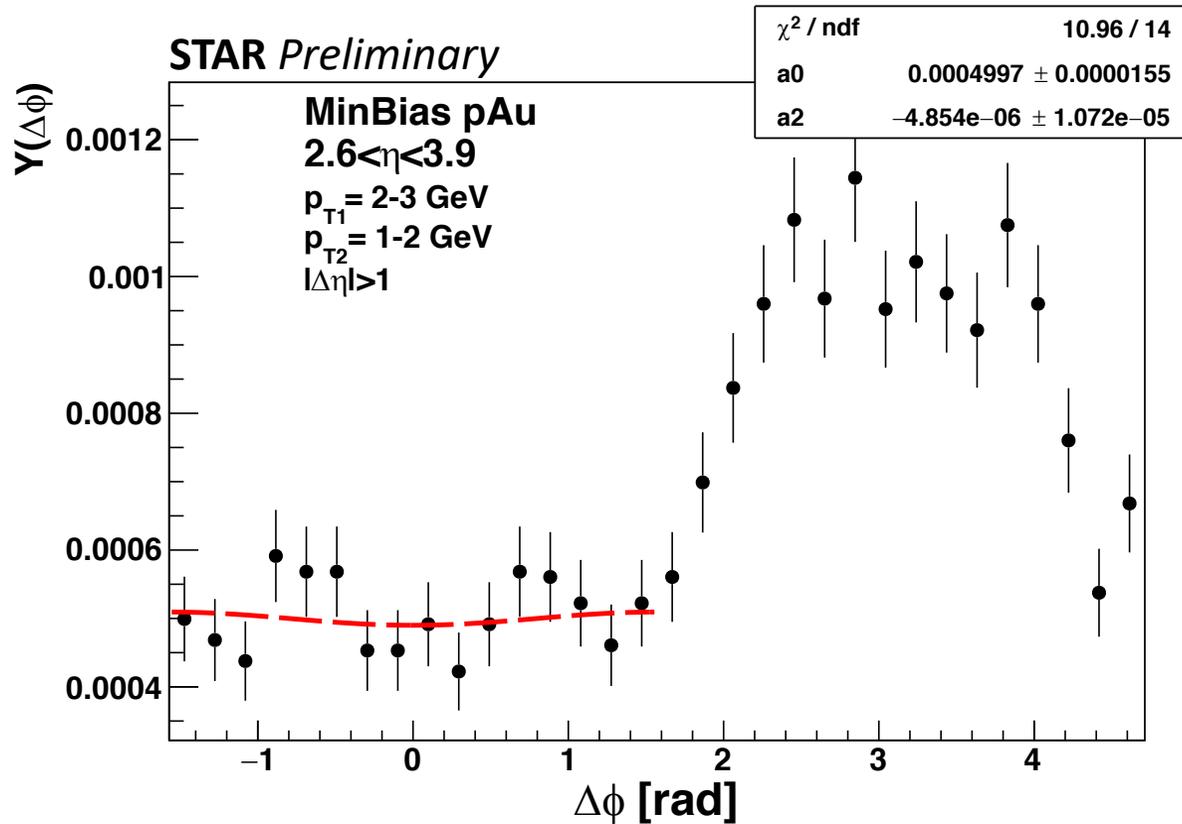
Outlook

- Detailed signatures with back-to-back di-hadron correlation measurement from theory:
 - Suppression can be a consequence of both initial- and final-state effects
 - Initial effect \rightarrow CGC: A, E.A./centrality, p_T , and rapidity dependence predicted
 - Efforts needed to determine an observable correlated best with b for small systems
 - DPS in d+Au: both pedestal and correlation affected?
- p+p, p+Al, and p+Au results from STAR: A, E.A./centrality, p_T , and rapidity dependence observed
- d+Au results from STAR: Challenging to conclude
 - For nonlinear gluon dynamics: high background correlation not fully understood; favors for cleaner p+Au collisions
 - For DPS physics: favors for di-charged hadron correlation in p+p, p+A, and d+A
- Uniform normalization needed
- Background contribution cannot be ignored from the data, be careful with predictions based on the results in d+Au collisions
- Di-charged hadron correlation with STAR Forward Upgrade and EIC:
 - Away-side peak: background correlation controllable \rightarrow probe DPS physics?
 - Near-side peak can be studied: separation of IS, FS and fragmentation p_T ?

Back up

Flow-like correlation

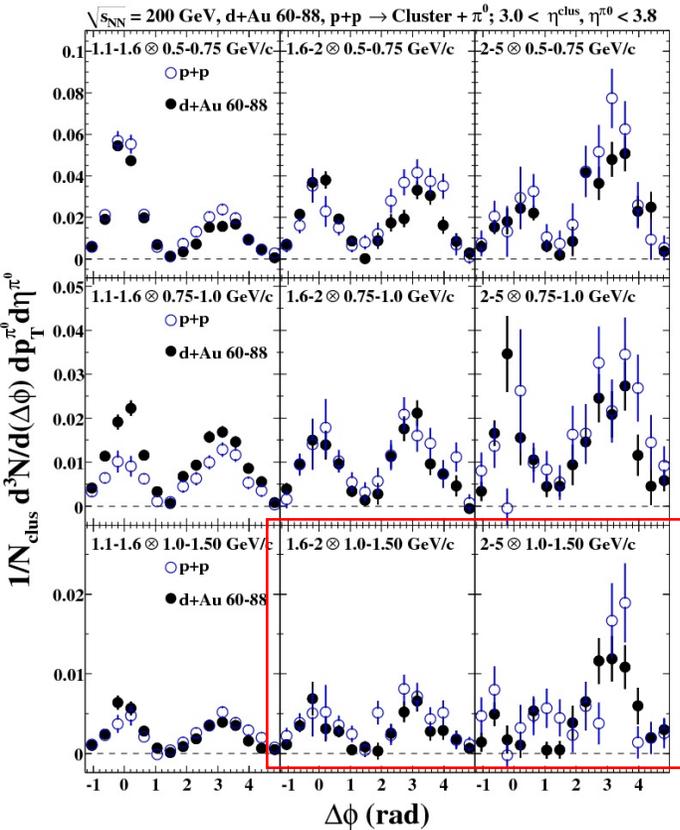
Fit function: $Y(\Delta\phi) = a_0 + 2*a_2 \cos(2\Delta\phi)$



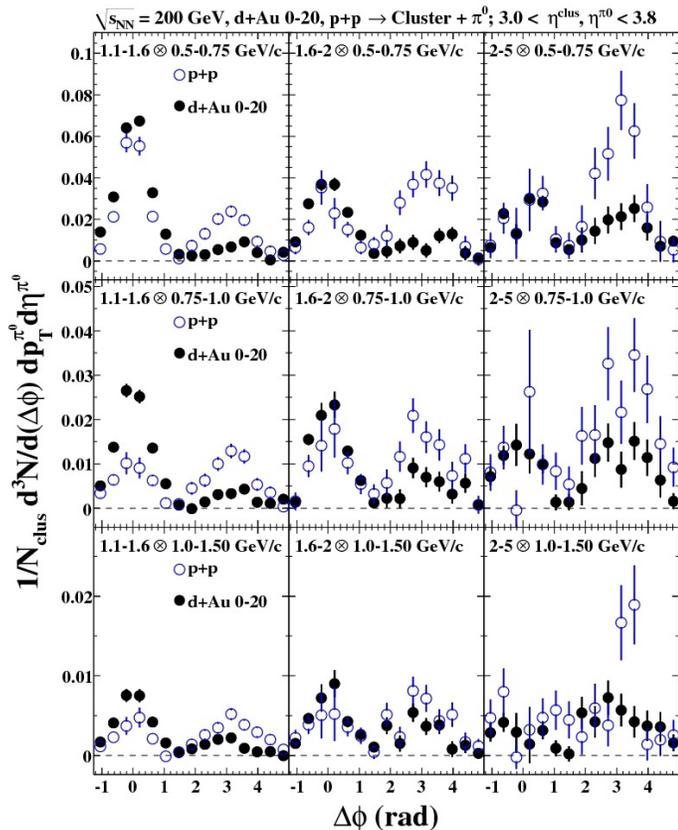
- Flow signal from near side is negligible for the current measurement
- π^0 s at FMS have very high energy; hard to require those two π^0 s not come from the same jet
- Due to limited rapidity coverage of FMS, it's challenging to accurately estimate long range correlation. Even if there is flow, \rightarrow makes suppression stronger
- Saturation stays after flow-like correlation subtraction in pPt at LHCb (Nuclear Physics A 00 (2018) 1–4)

PHENIX data

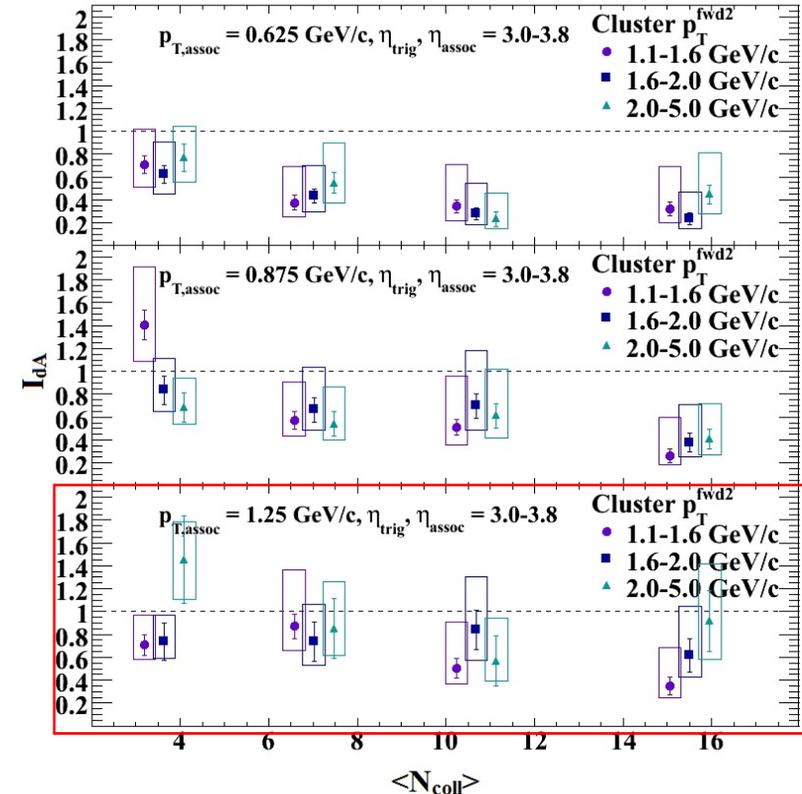
dAu peripheral



dAu central



Forward-Forward



Phys. Rev. Lett. 107, 172301

[PhD thesis for the paper](#)

- PHENIX MPC (Muon Piston Cal) data: forward cluster- π^0 correlation, $3.0 < \eta < 3.8$, the highest p_T bin is the lowest p_T bin at STAR
- I_{dA} is the area ratio of the away side correlation in dAu over pp, the same observable as STAR
- In the highest p_T bin: dAu = pp, no suppression is observed, no centrality dependence either