

Data analysis for the detection efficiency

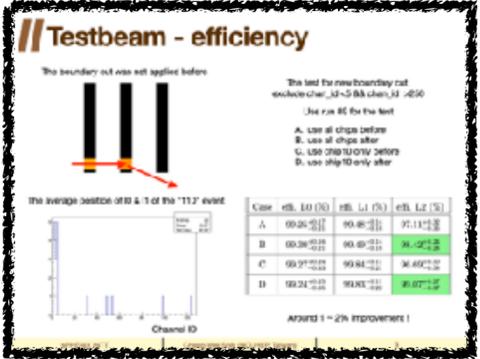
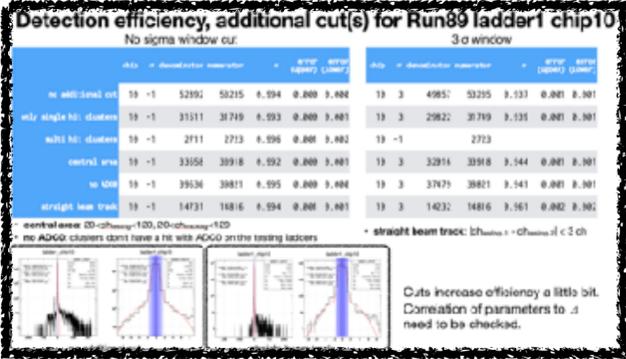
G. Nukazuka (RBRC)

Past reports:

- I. [Jan/27/2022](#) (clone hits)
- II. [Feb/24/2022](#) (BCO grouping, clustering)
- III. [Mar/17/2022](#) (alignment)
- IV. [Mar/24/2022](#) (detection efficiency)

Issue: Analyzer dependence of the detection efficiency

Detection efficiency analysis of Run89 were done by Chen-Wei, Miu, and me. The results without the sigma window cut to the residual distributions were consistent while with 3-sigma window cut look inconsistent.



No sigma window cut

3 σ window

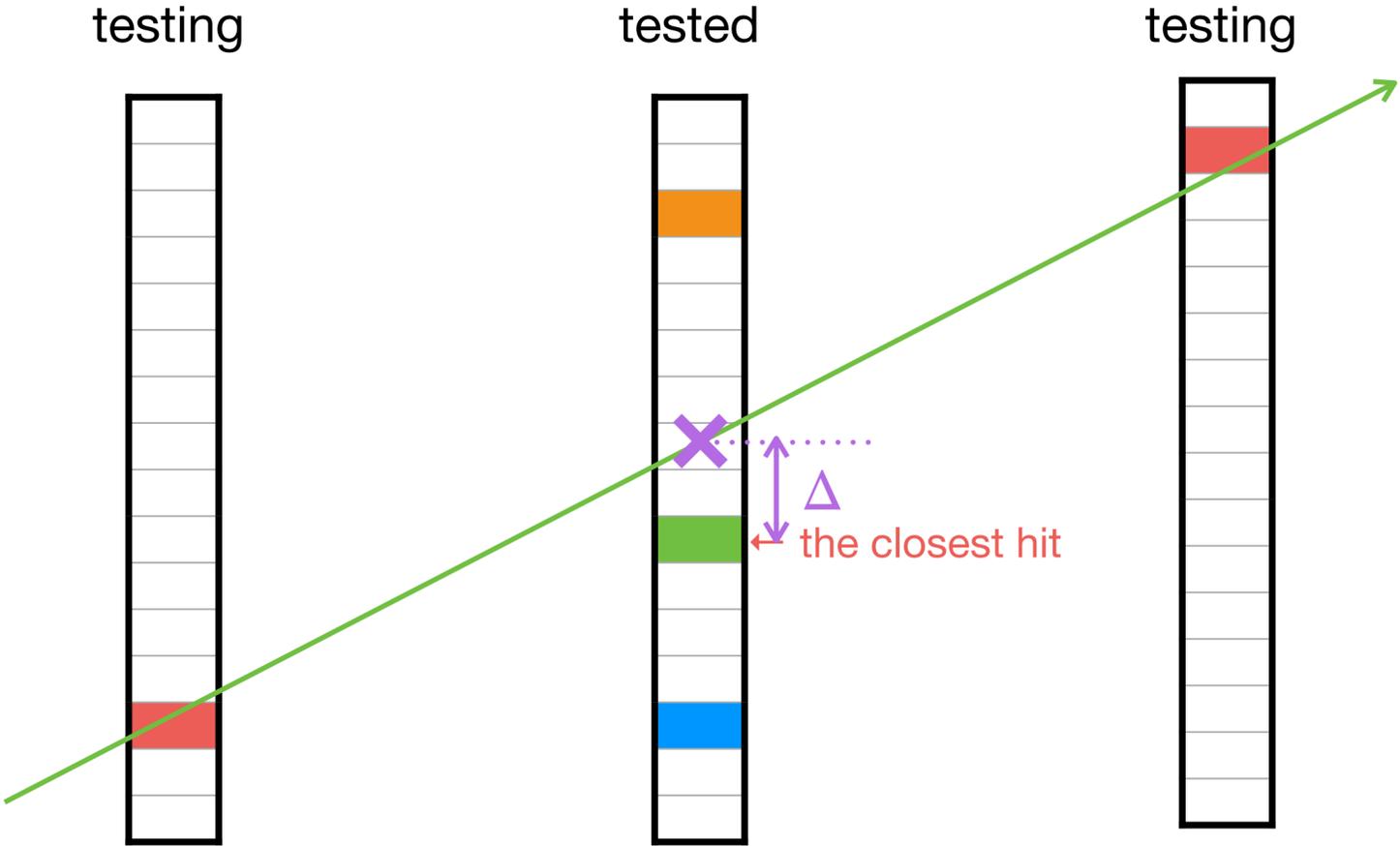
	No sigma window cut					3 σ window				
	chip	σ	ϵ Ladder 0	ϵ Ladder 1	ϵ Ladder 2	chip	σ	ϵ Ladder 0	ϵ Ladder 1	ϵ Ladder 2
Genki, no additional cut	10	-1	0.994	0.994	0.954	10	3	0.940	0.937	0.894
Genki, straight beam track	10	-1	0.981	0.994	0.963	10	3	0.883	0.961	0.921
Chen-Wei, ELPH poster						all	3	0.993	0.995	0.971
Chen-Wei, new (3/24)						10	3	0.992	0.998	0.991
Miu	10	-1	0.995	0.994	0.996	10	3	0.977	0.984	0.969

The difference must be understood.

Issue: Analyzer dependence, tracking methods

From the conversation with Chen-Wei after the INTT meeting last week, I think got the point which made the difference.

Geometrical determination (Genki, Miu)

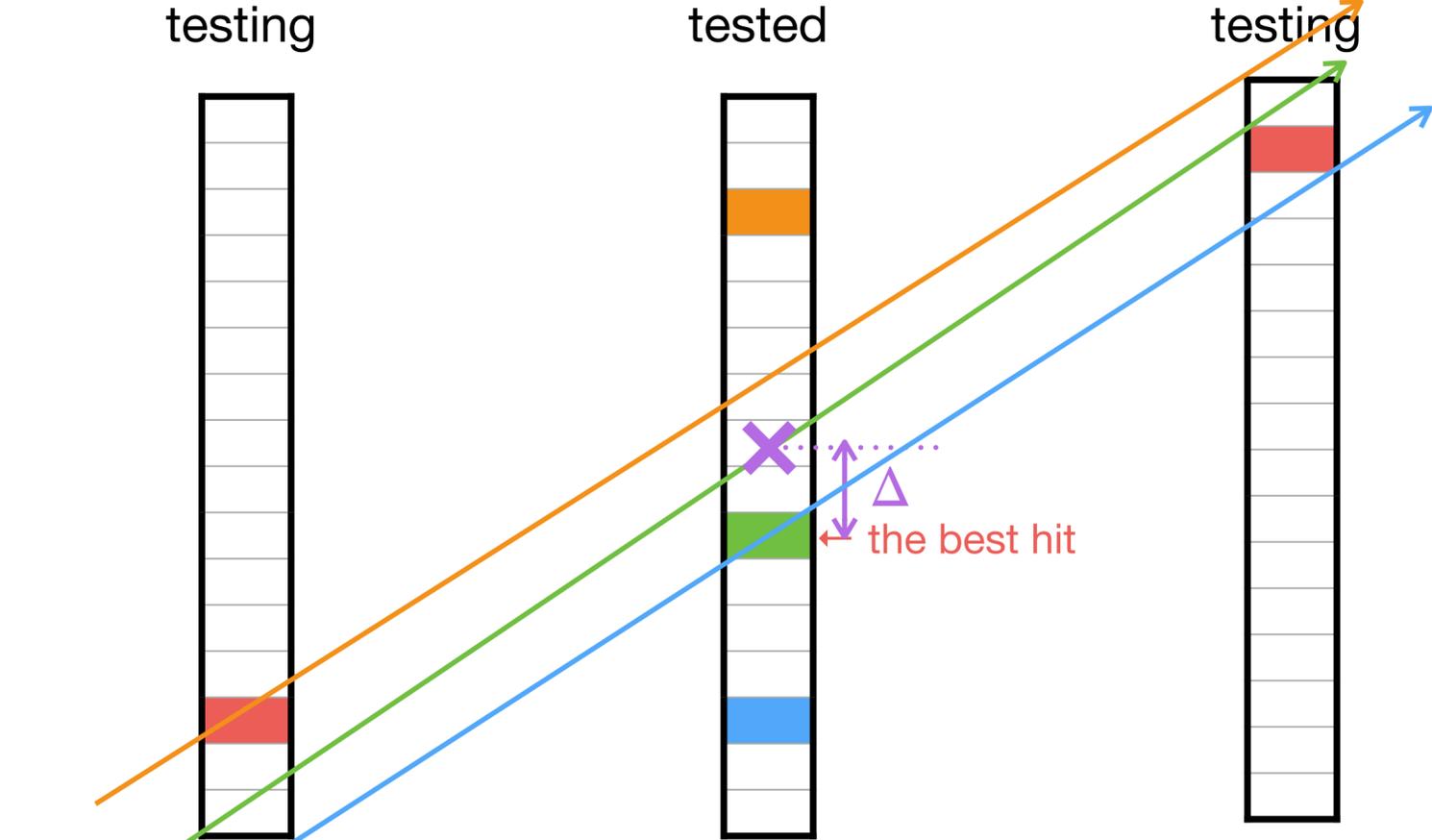


A cluster on each testing ladder are used for tracking. The track can be determined uniquely:

$$y = ax + b \quad \text{and} \quad p_1 = (x_1, y_1) \ \& \ p_2 = (x_2, y_2)$$

The closest hit on the tested ladder to the predicted position by tracking is treated as a candidate.

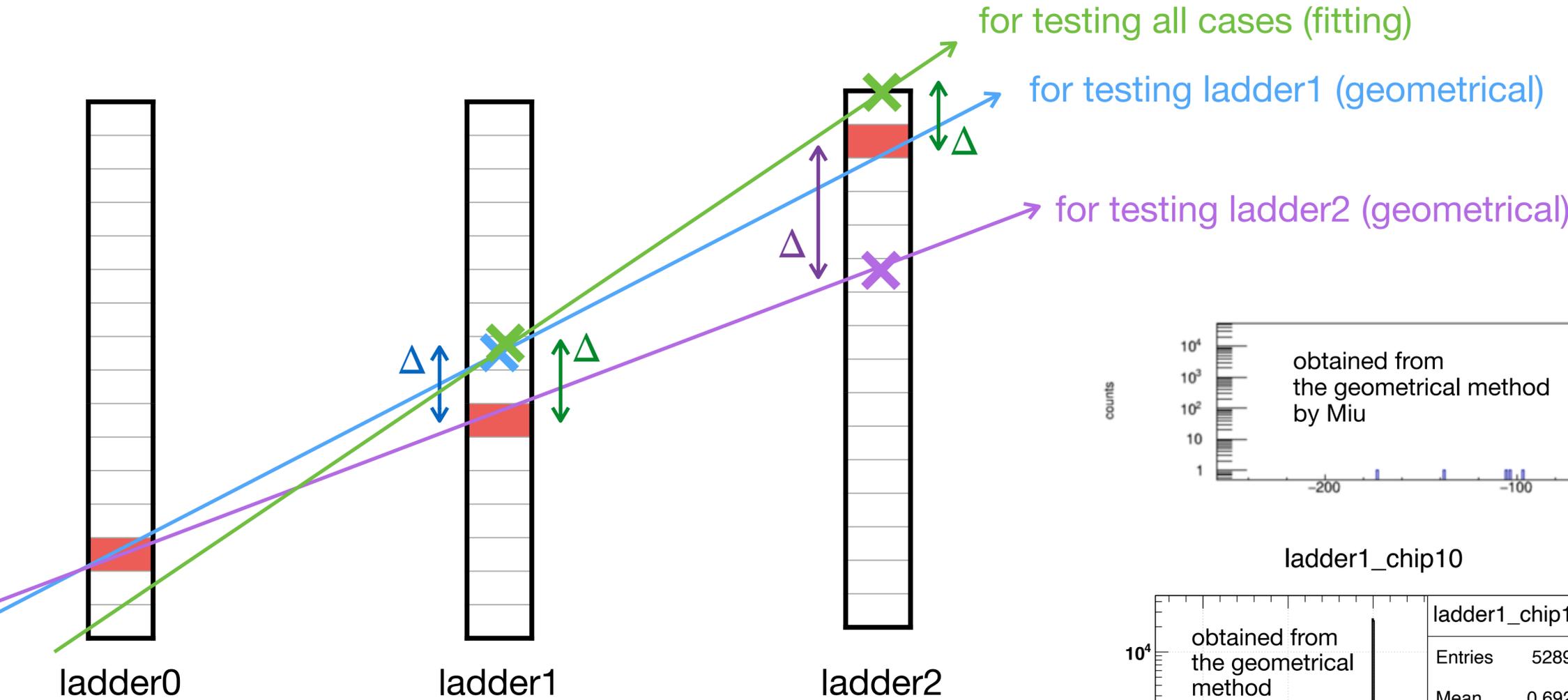
Determination by fitting (Cheng-Wei)



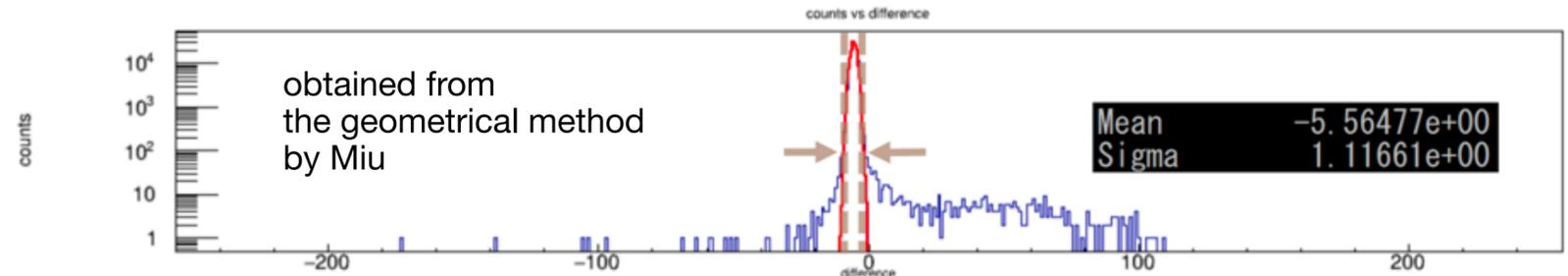
χ^2_{orange} : 17
 χ^2_{green} : 3
 χ^2_{blue} : 24

A cluster on each testing ladder and one of a cluster on the tested are used for tracking. A track is made by fitting to the 3 points with a straight line. The track with the smallest χ^2 is hired.

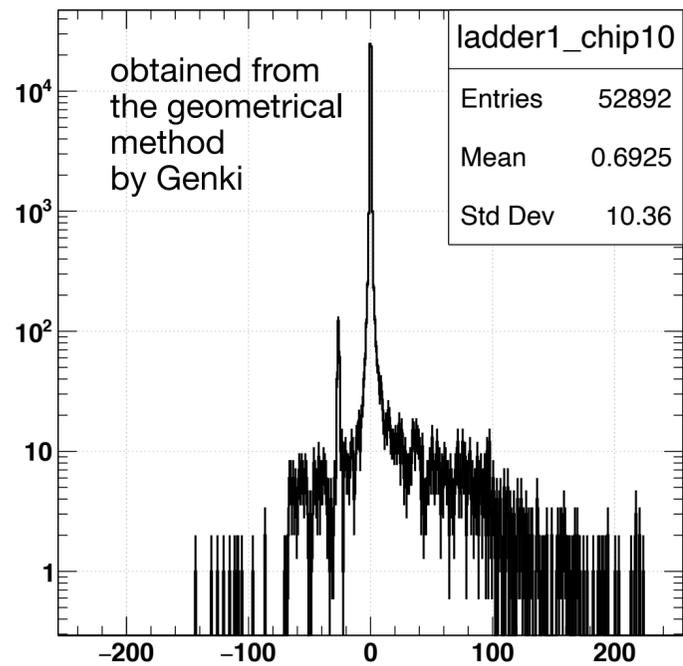
Issue: Analyzer dependence, tracking methods



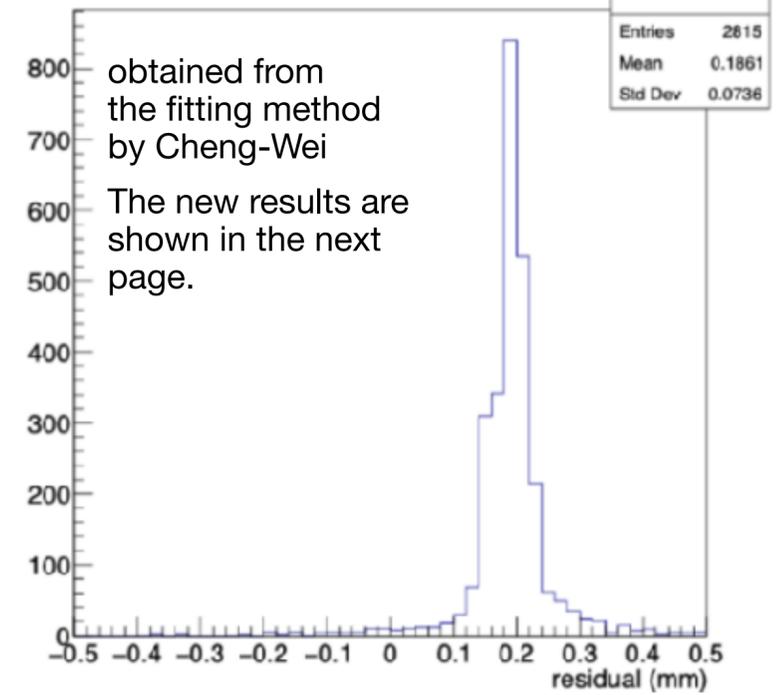
The fitting method always makes a moderate line to all hits.
 The geometrical method never care the tested ladder
 so sometimes overestimates the residual.
 These tracking methods give different residual distributions. It
 means the detection efficiency without the sigma window cut is
 consistent but different with the sigma window.



ladder1_chip10



layer1 Y axis residual



Issue: Analyzer dependence, trying the fitting method

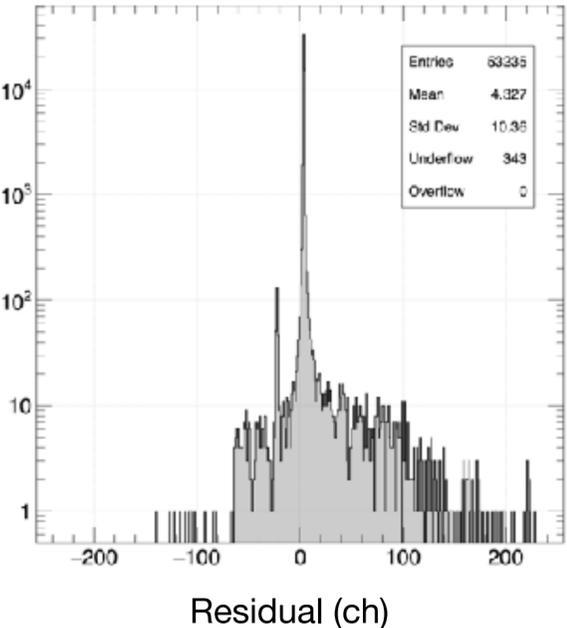
Run89

Geometrical method

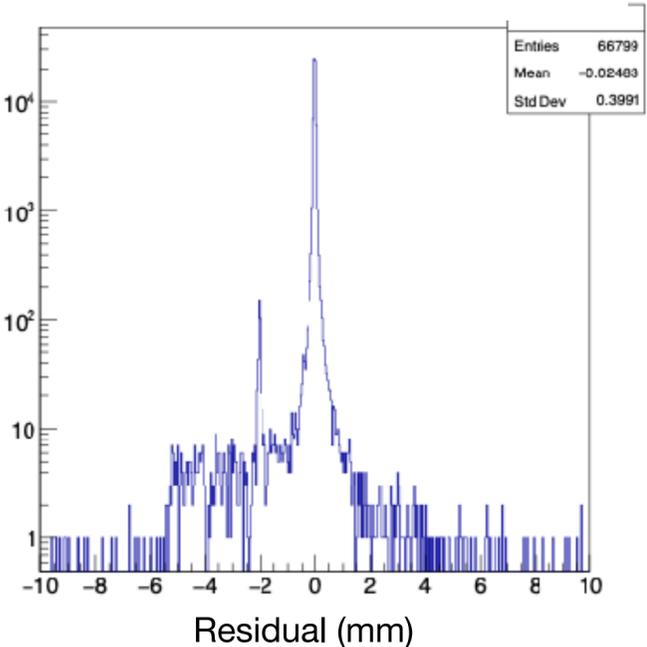
Fitting method

ladder1, chip10

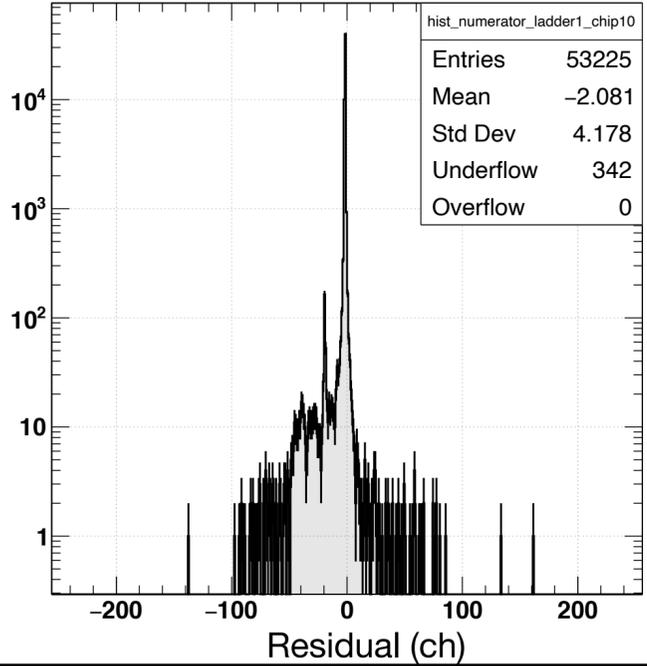
Genki



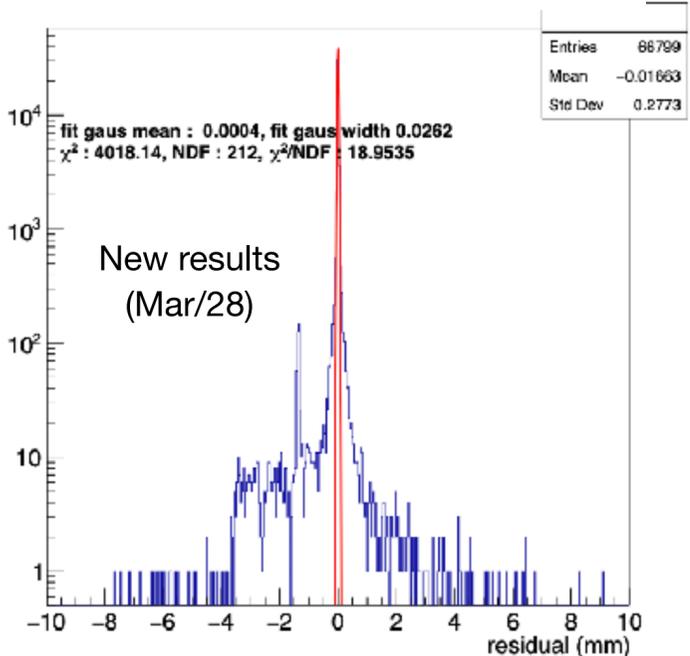
Chen-Wei



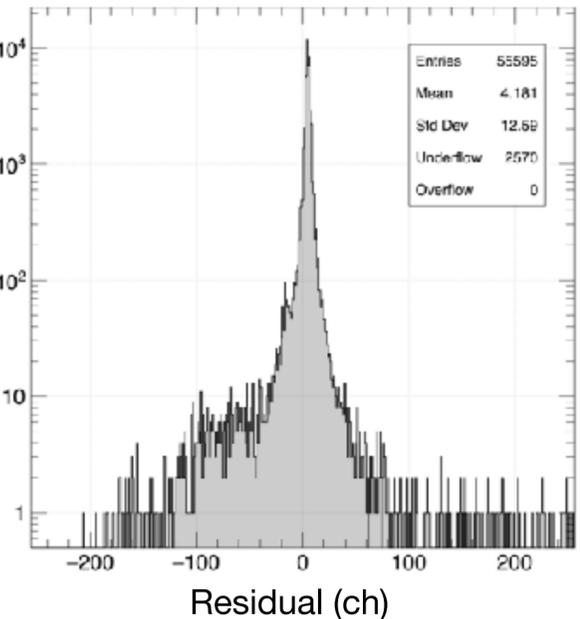
Genki



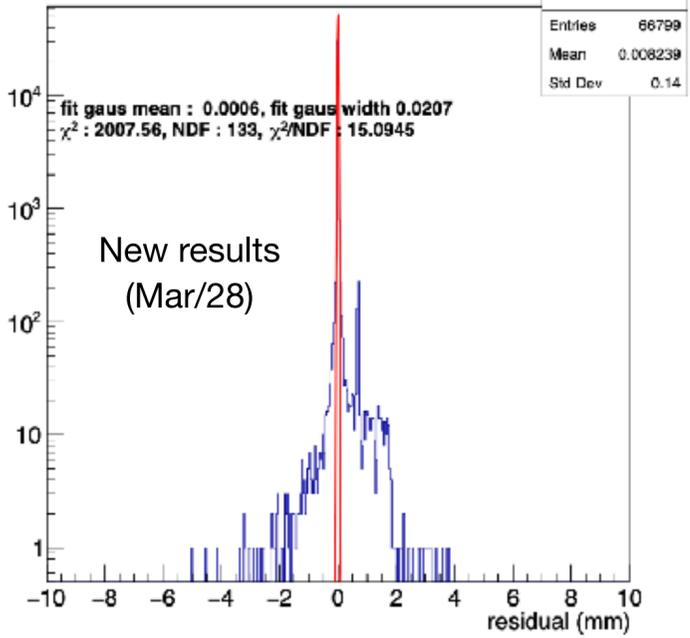
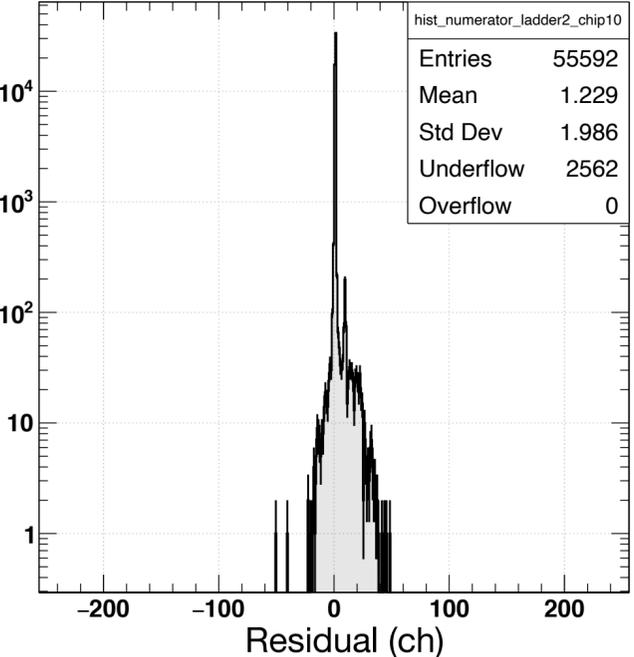
Chen-Wei



ladder2, chip10



Note:
 Genki → Cheng-wei: 256 ch ~ 20 mm
 Cheng-Wei → Genki: 10 mm ~ 128 ch



Note: My plots are updated from the ones sent to the INTT mailing list. There were bugs.

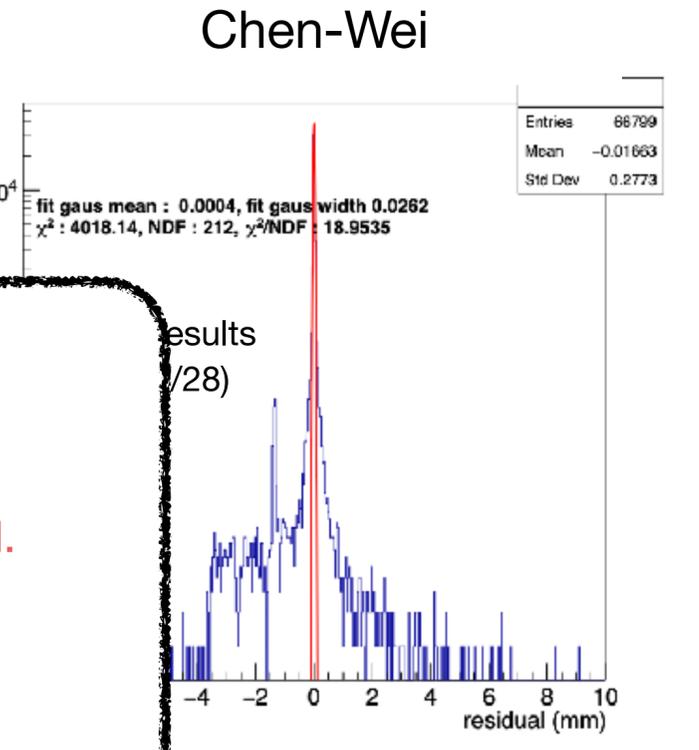
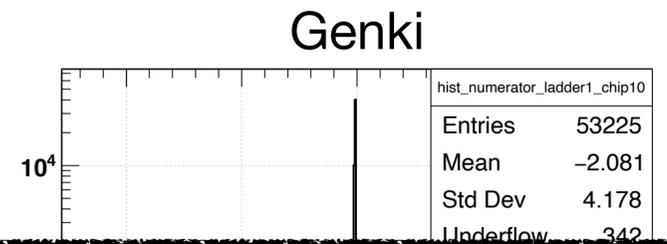
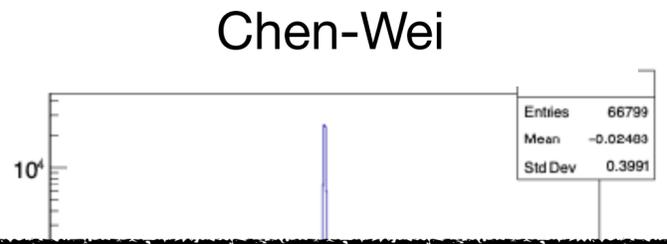
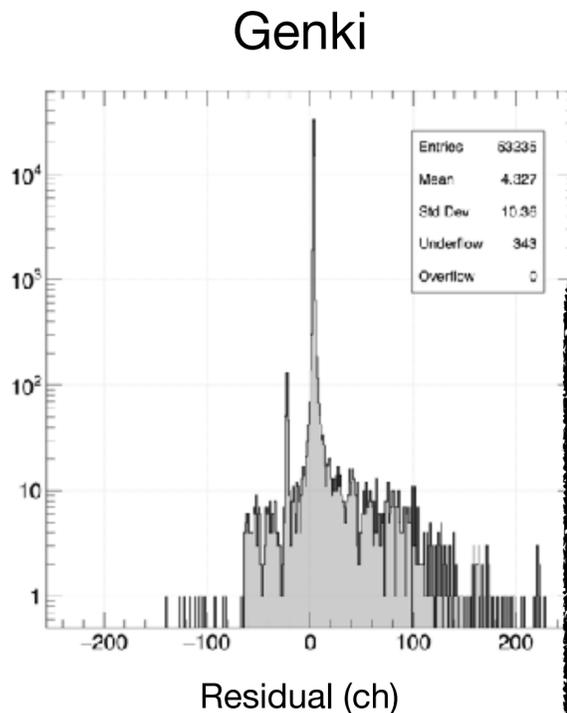
Issue: Analyzer dependence, trying the fitting method

Run89

Geometrical method

Fitting method

ladder1, chip10

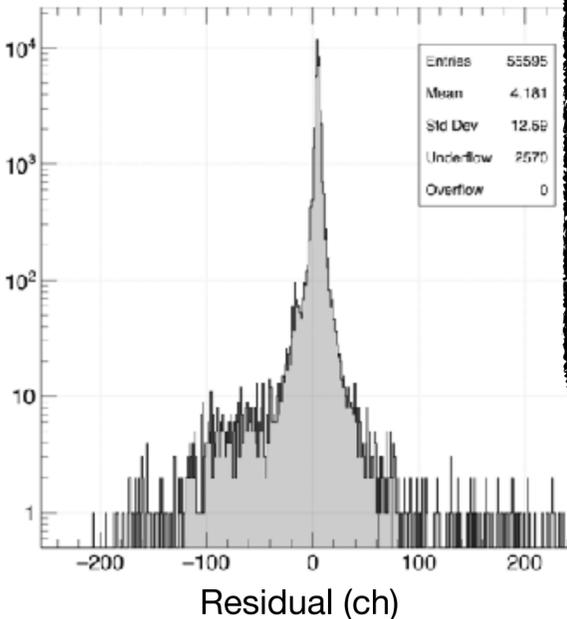


Genki's results:
 Residual distributions using the methods are different as expected.
 The flat background seen in the geometrical method is quite small in the fitting method.
 The positions of the satellite peak in ladder2 towards in opposite directions. I don't understand why...

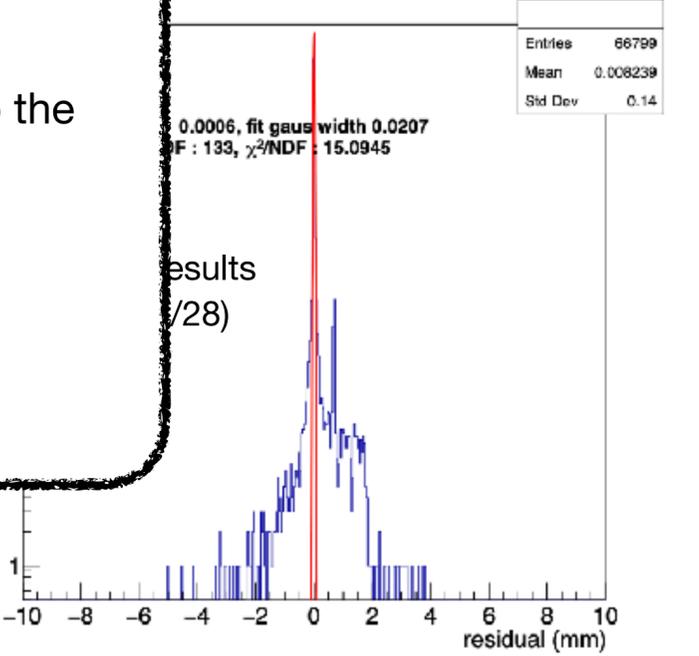
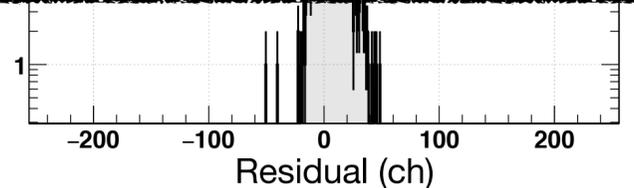
Cheng-Wei's new results:
 New results were obtained using Genki's data having no clone hits.
 The fitting method creates narrower distribution than the geometrical method.
 The satellite peak exists for all plots. They were not seen in the previous results (due to the scale of the y-axis?).

Genki's vs Cheng-Wei's
 Results look consistent.

ladder2, chip10

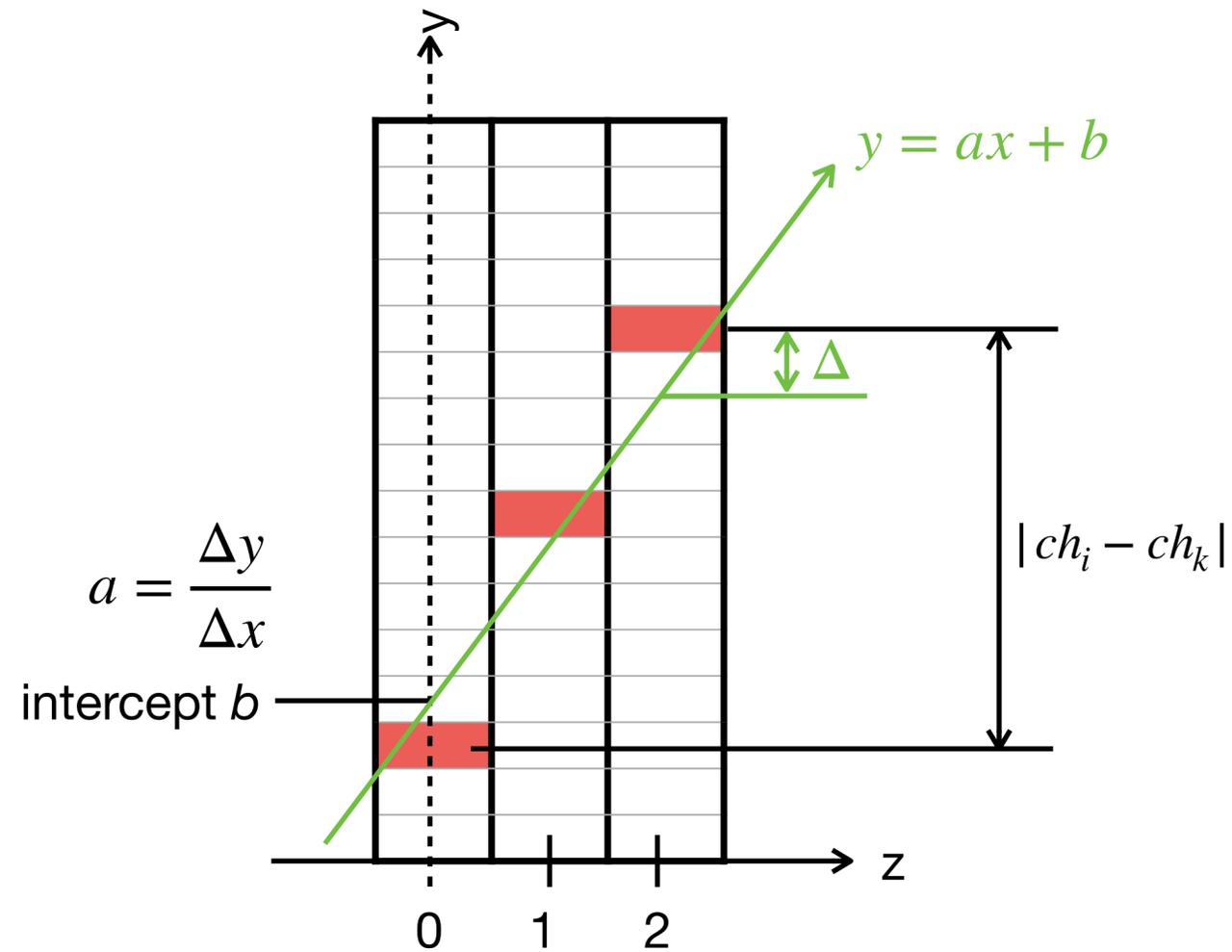


Genki → Cheng-wei: 256 ch ~ 20 mm
 Cheng-Wei → Genki: 10 mm ~ 128 ch



Issue: Analyzer dependence, track slope cut

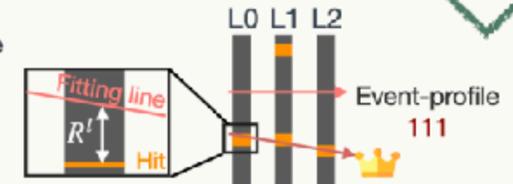
As far as I understand, a requirement of small track slope is included in Chen-Wei's analysis. The largest value required to the slope is the same as the 3- σ window cut.



slope: channel difference when moving from a ladder to the next ladder
intercept: position at ladder0

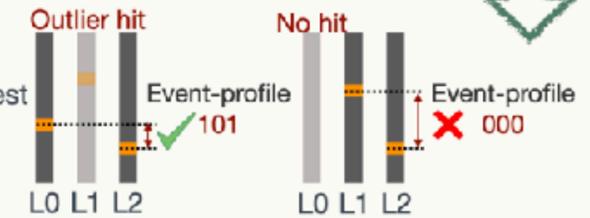
Algorithm-1

1. Fit all combinations and pick up the one with minimum χ^2 / NDF
2. Check the residual (R^i) of each layer
3. If $<$ tolerance \rightarrow event-profile 111
4. If $>$ tolerance \rightarrow algorithm-2 is applied



Algorithm-2

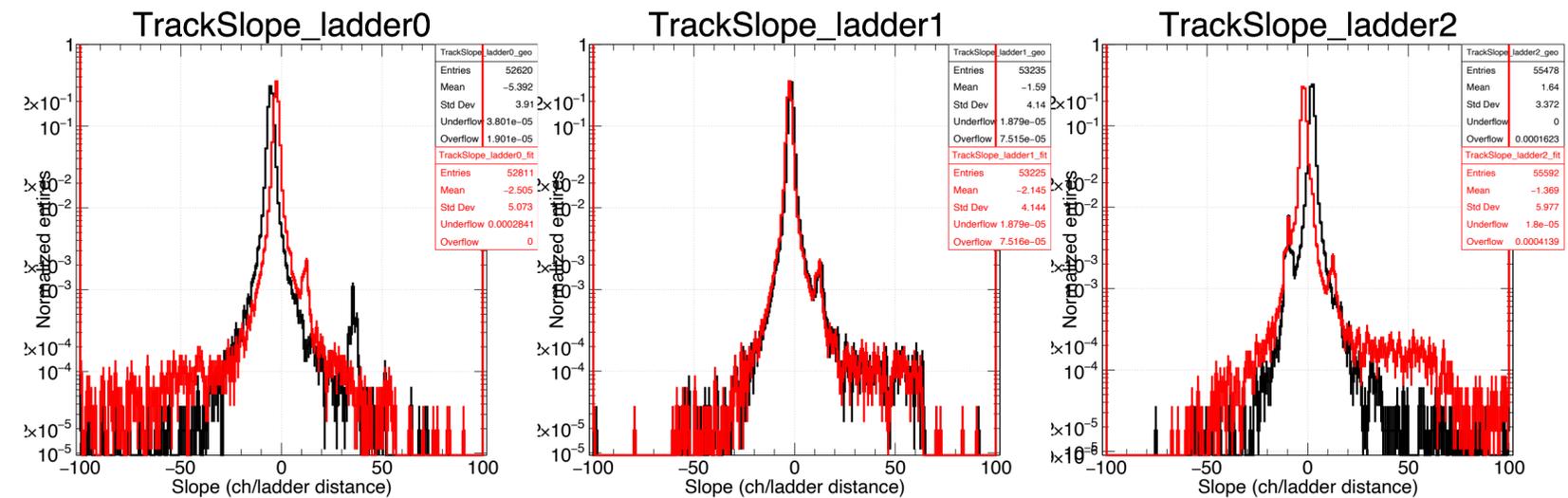
1. Ignore the layer with no/outlier hit
2. Check the position difference of the rest 2 layers, and assign the event profile
3. If $<$ tolerance \rightarrow 110, 101, 011
4. If $>$ tolerance \rightarrow 000



Cheng-Wei,
ELPH2022

- Geometrical method
- Fitting method

Run89, chip10



Track slope distributions

Again, there are some discrepancy between the 2 methods, and I need to take time to investigate it...

Issue: Analyzer dependence, track slope cut to the residual dists.

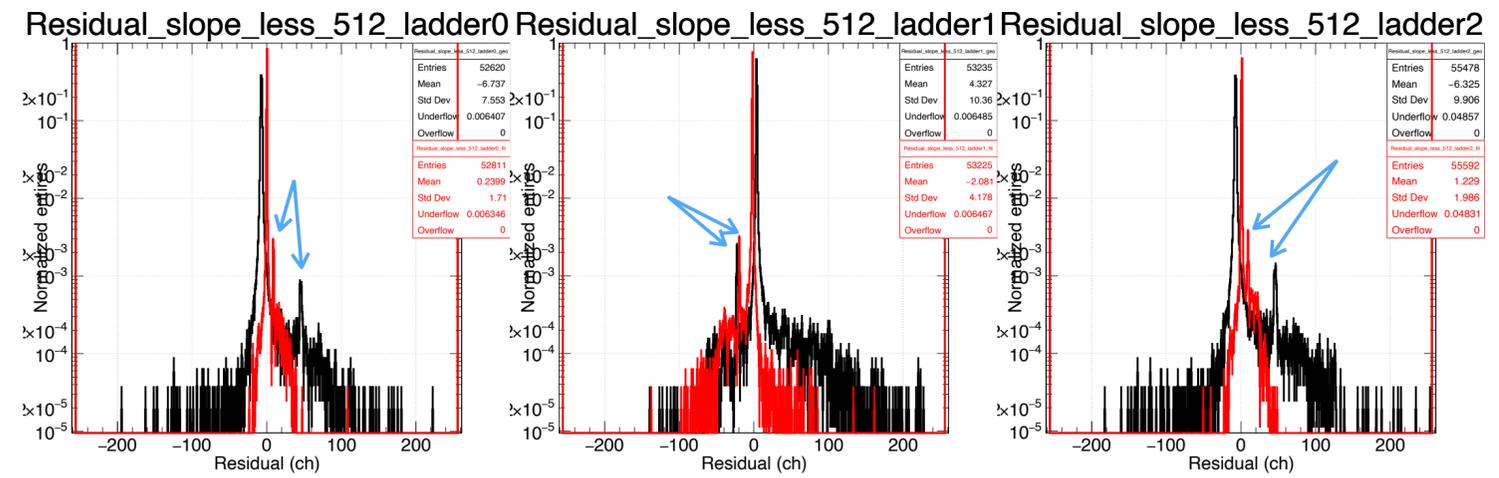
Run89, chip10

Ladder0

Ladder1

Ladder2

No slope cut

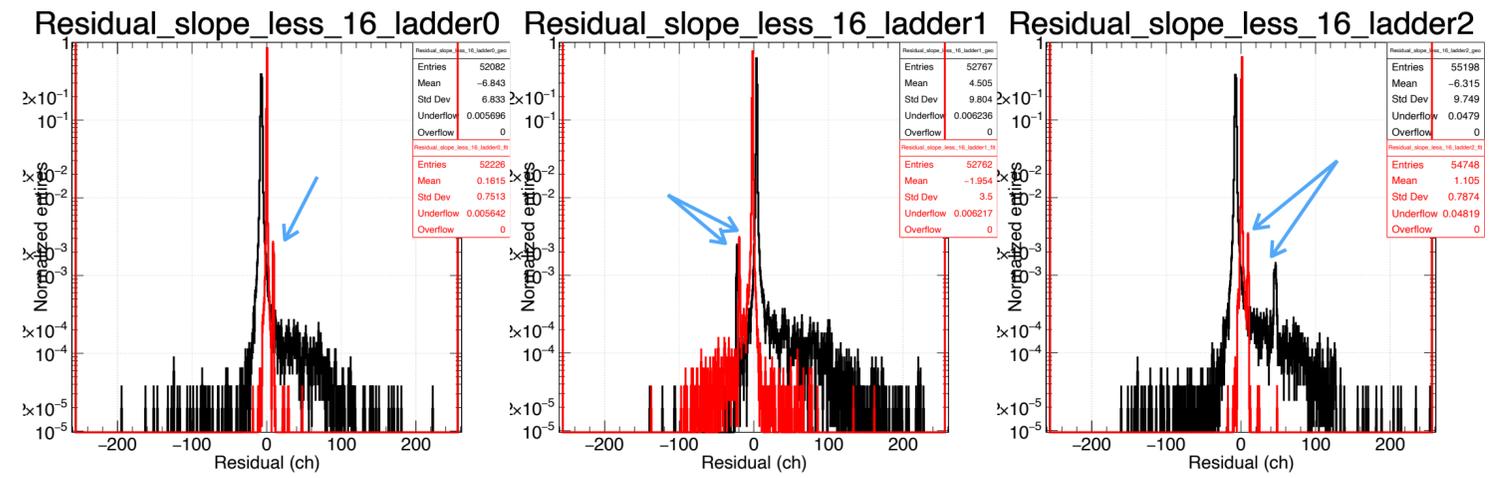


The track slope cut $|\text{slope}| < 16$ narrows the distributions.

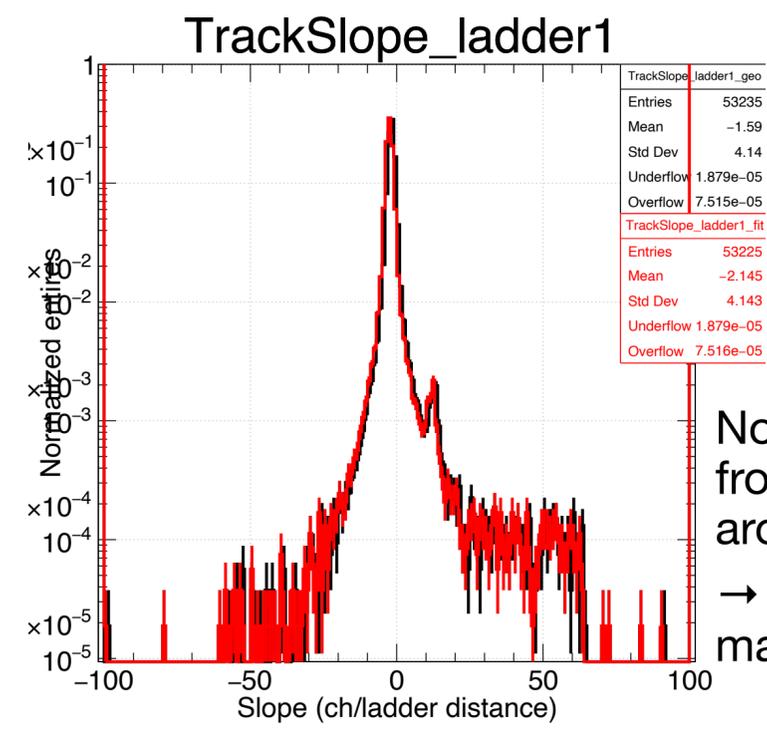
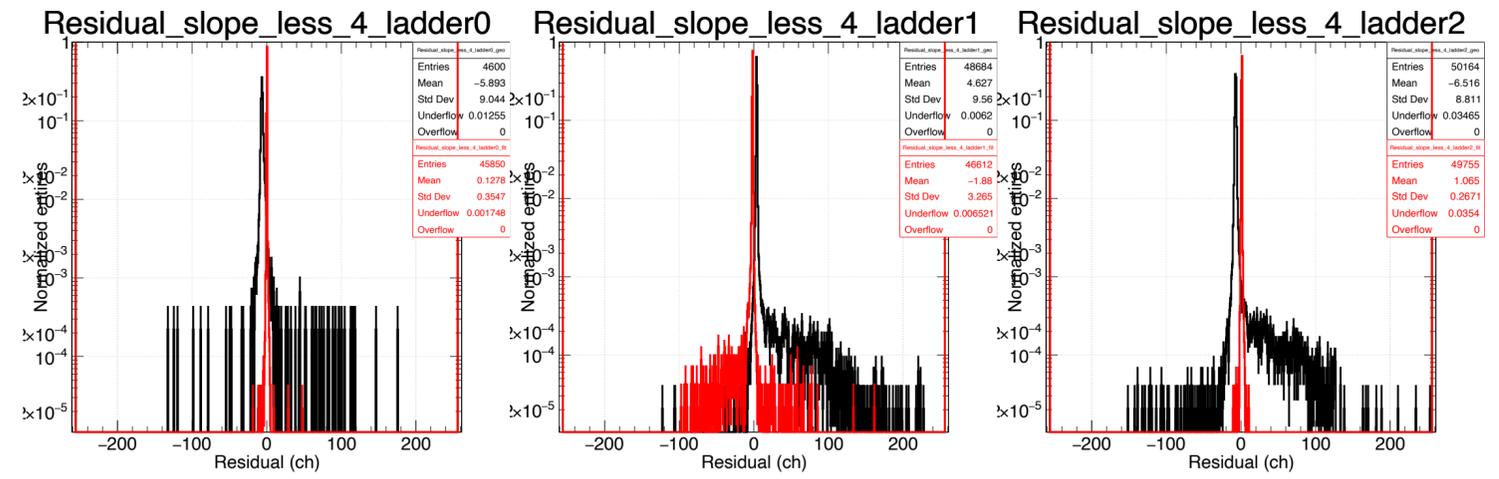
The track slope cut $|\text{slope}| < 4$ completely removes the satellite peak for all cases. It's not due to less statistics because the height of the peak is not so affected.

Chen-Wei applied $|\text{slope}| < 3$ in my understanding. This cut doesn't improve my results somehow. Since the track slope distribution is not centered, I tried selecting events around the mean value (How large is fine?).

$|\text{slope}| < 16$



$|\text{slope}| < 4$

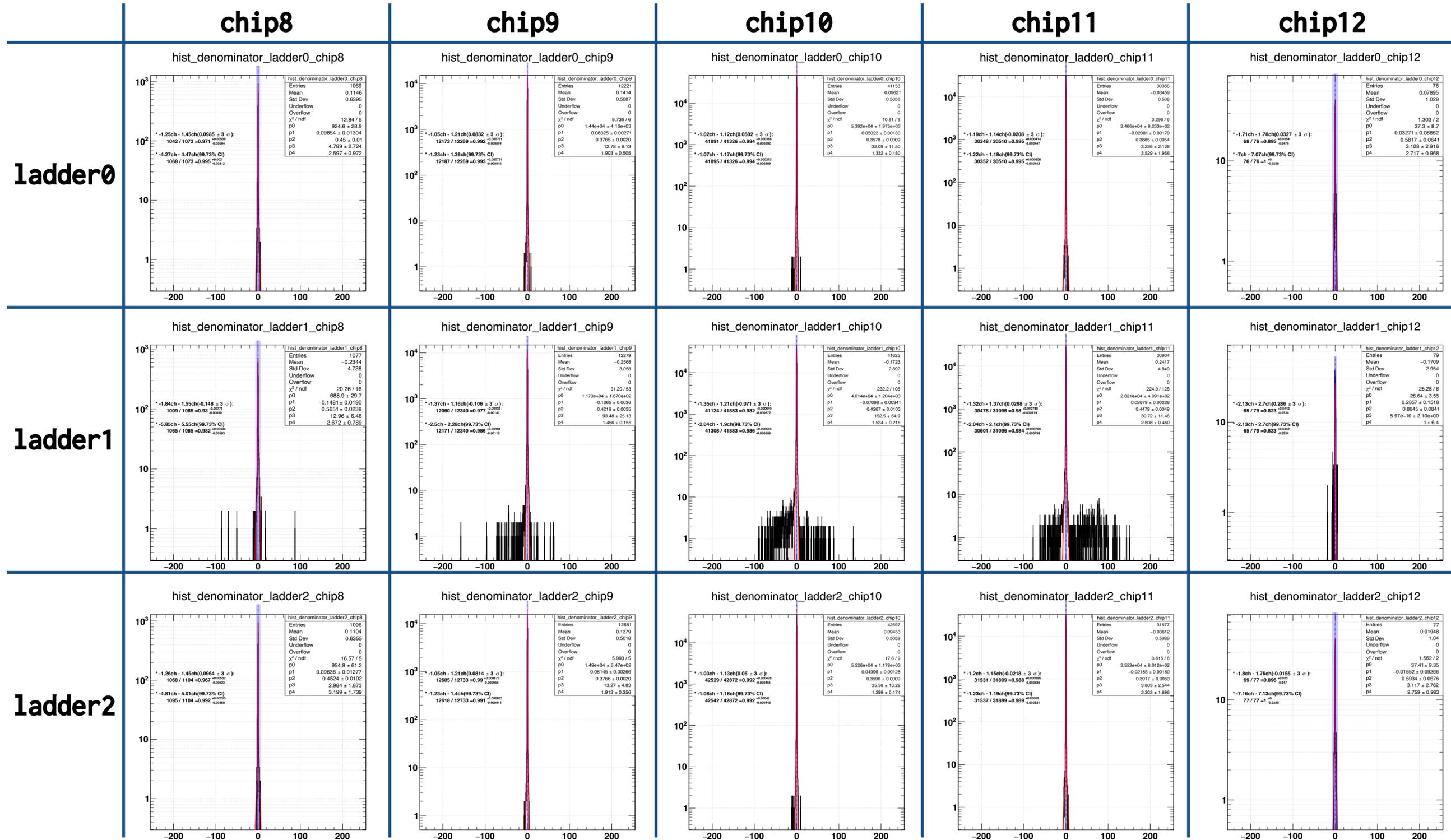


Note: Track slope distribution from MC data distributes around 0.

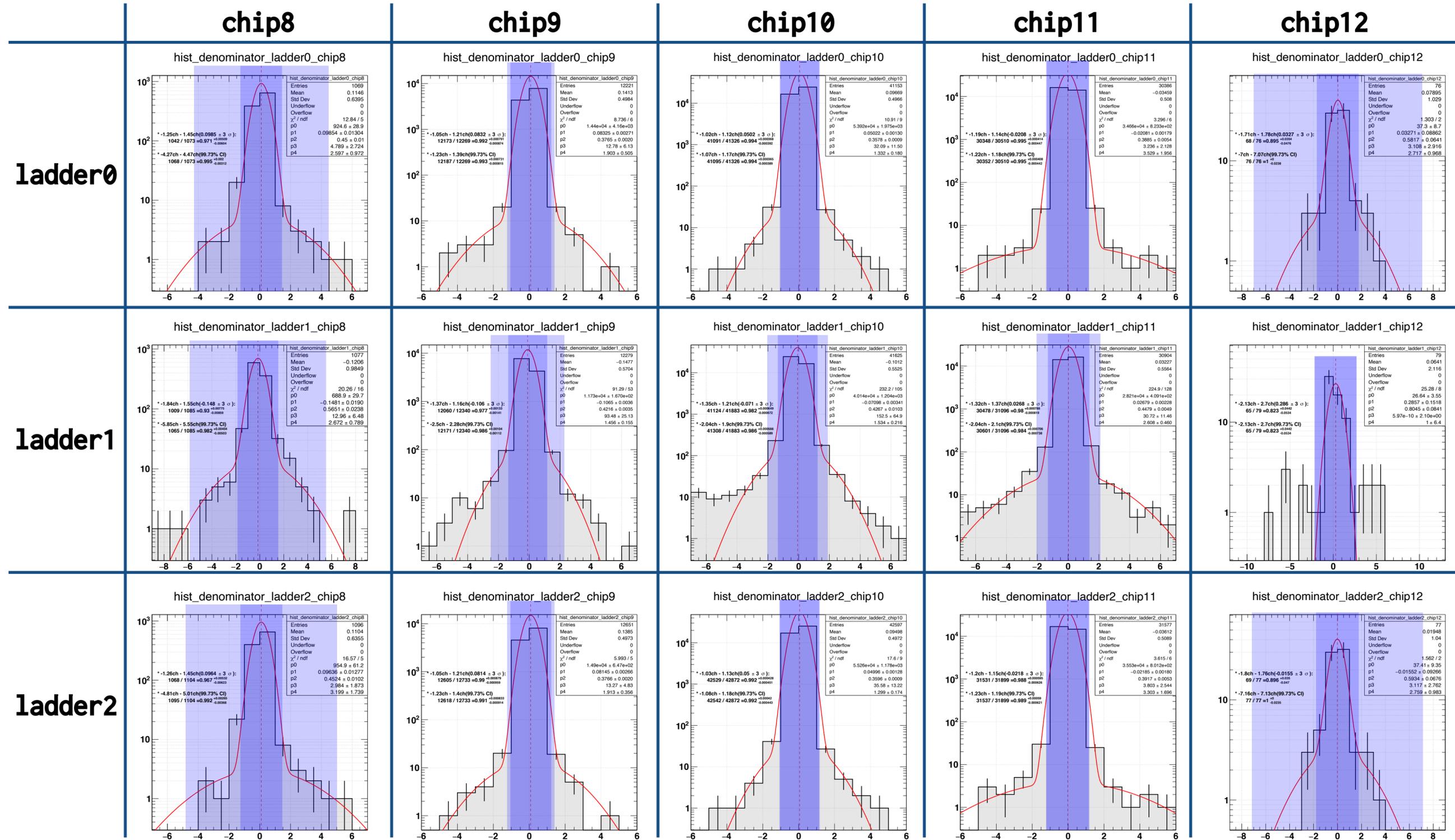
→ My analysis codes don't make a bias.

The satellite peaks are strongly suppressed by the slope cut.

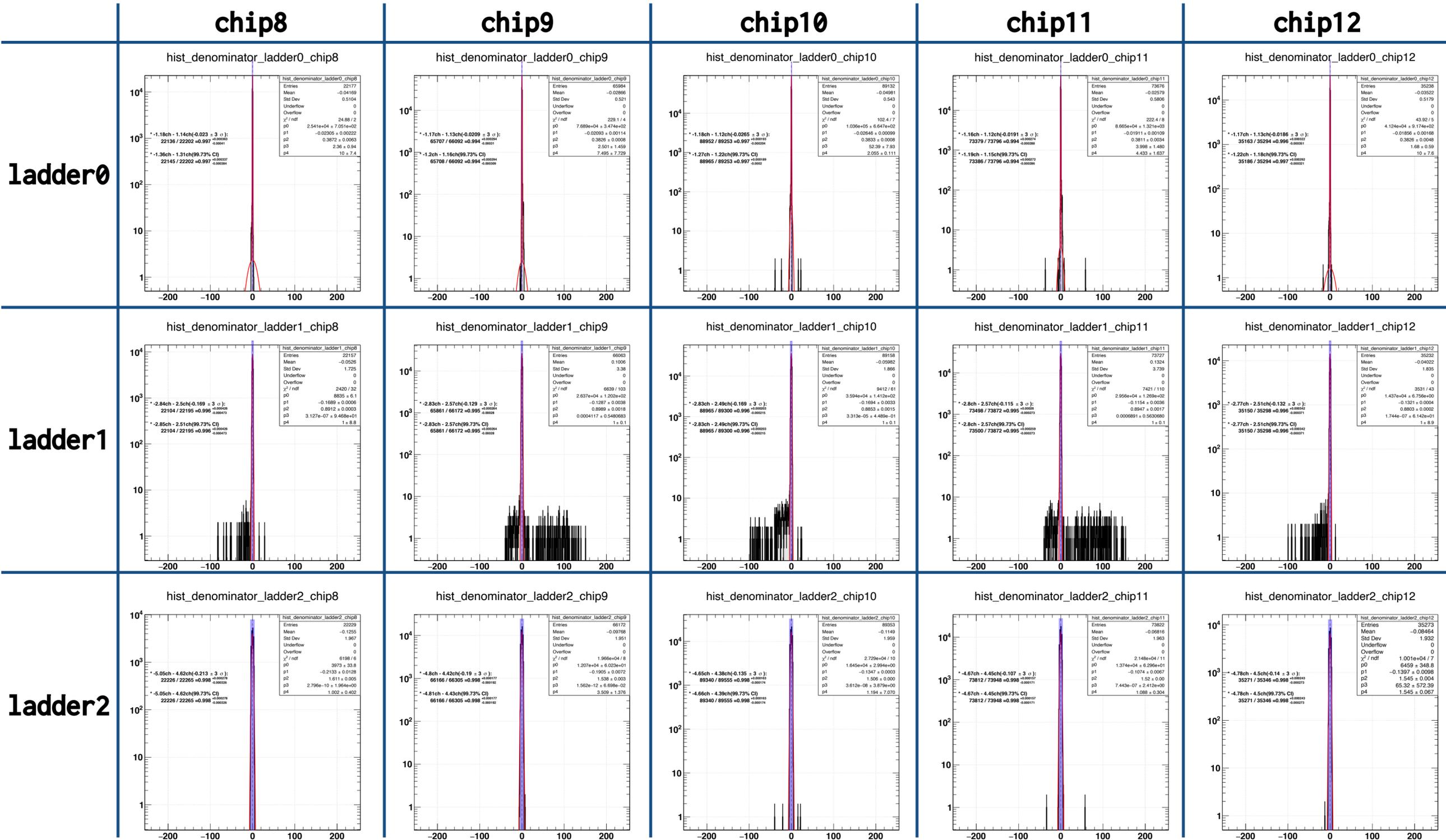
Residuals, Whole range



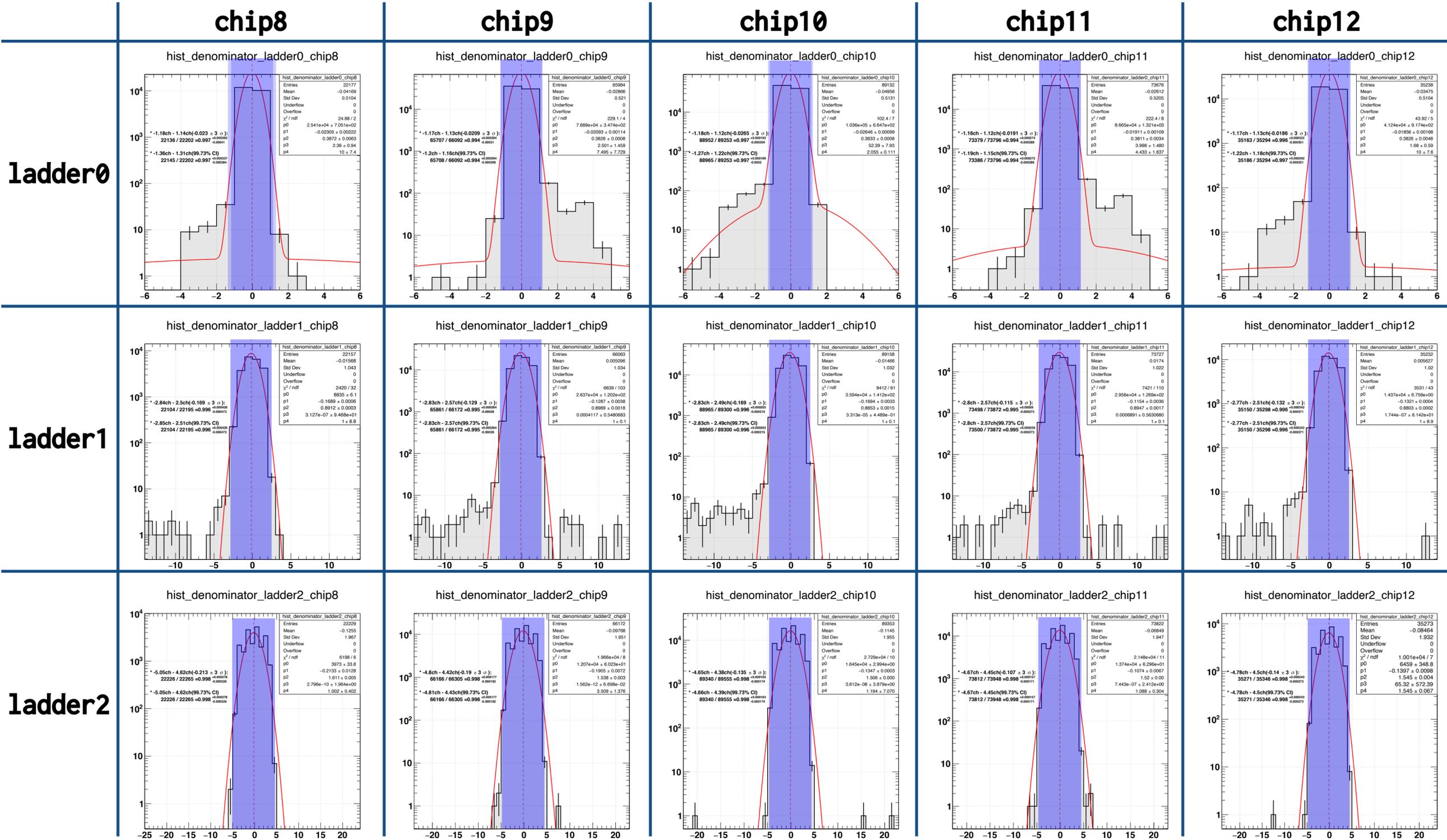
Residuals, Zoomed



MC, Residuals, Whole range



MC, Residuals, Zoomed



Issue: Analyzer dependence, Detection efficiency with Fitting method

Ladder0

Ladder1

Ladder2

Chip	σ	#hits found	#track	ϵ	Upper error	Lower error
8	-1	1069	1073	0.996	0.002	0.003
8	3	1042	1073	0.971	0.005	0.006
9	-1	12221	12269	0.996	0.001	0.001
9	3	12173	12269	0.992	0.001	0.001
10	-1	41153	41326	0.996	0.000	0.000
10	3	41091	41326	0.994	0.000	0.000
11	-1	30386	30510	0.996	0.000	0.000
11	3	30348	30510	0.995	0.000	0.000
12	-1	76	76	1.000	0.000	0.024
12	3	68	76	0.895	0.035	0.048
all	-1	84905	85254	0.996		
all	3	84722	85254	0.994		

Chip	σ	#hits found	#track	ϵ	Upper error	Lower error
8	-1	1077	1085	0.993	0.003	0.004
8	3	1009	1085	0.930	0.008	0.009
9	-1	12279	12340	0.995	0.001	0.001
9	3	12060	12340	0.977	0.001	0.001
10	-1	41625	41883	0.994	0.000	0.000
10	3	41124	41883	0.982	0.001	0.001
11	-1	30904	31096	0.994	0.000	0.000
11	3	30478	31096	0.980	0.001	0.001
12	-1	79	79	1.000	0.000	0.023
12	3	65	79	0.823	0.044	0.053
all	-1	85964	86483	0.994		
all	3	83727	85398	0.980		

Chip	σ	#hits found	#track	ϵ	Upper error	Lower error
8	-1	1096	1104	0.993	0.002	0.004
8	3	1068	1104	0.967	0.005	0.006
9	-1	12651	12733	0.994	0.001	0.001
9	3	12605	12733	0.990	0.001	0.001
10	-1	42597	42872	0.994	0.000	0.000
10	3	42529	42872	0.992	0.000	0.000
11	-1	31577	31899	0.990	0.001	0.001
11	3	31531	31899	0.988	0.001	0.001
12	-1	77	77	1.000	0.000	0.024
12	3	69	77	0.896	0.035	0.047
all	-1	87998	88685	0.992		
all	3	87802	88685	0.990		

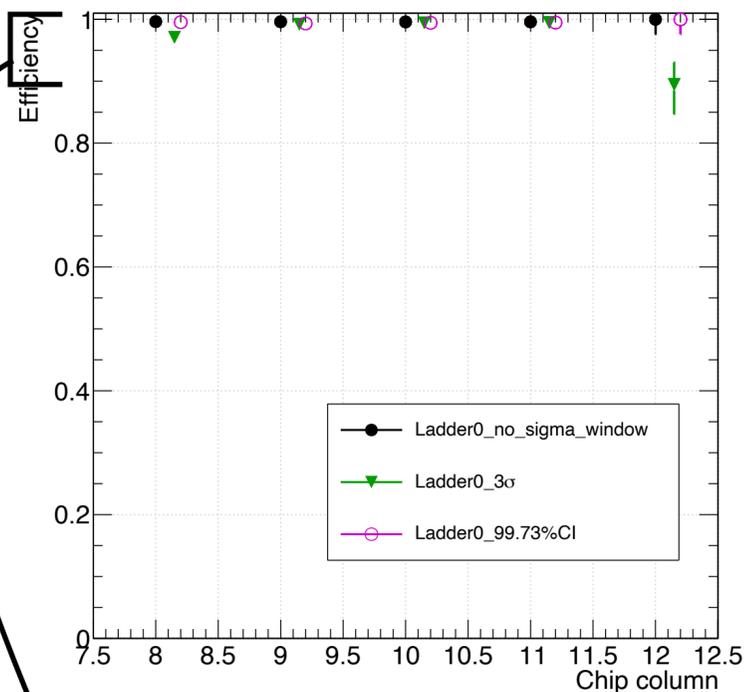
Note: 10<ch_{testing} is not used

Note2: The results sent to the mailing list required “-3<slope<-1” while these are required “-4.3<slope<-0.3”

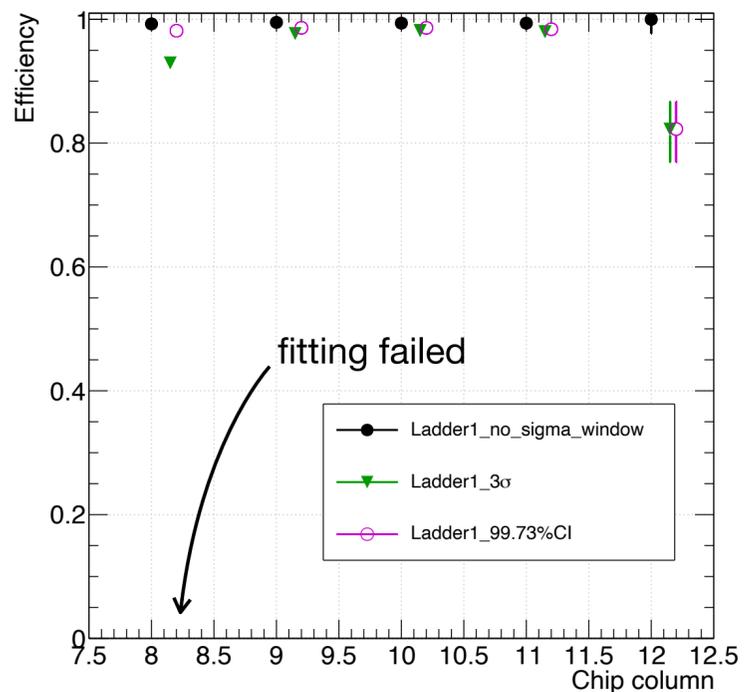
Issue: Analyzer dependence, Detection efficiency with Fitting method

Run89

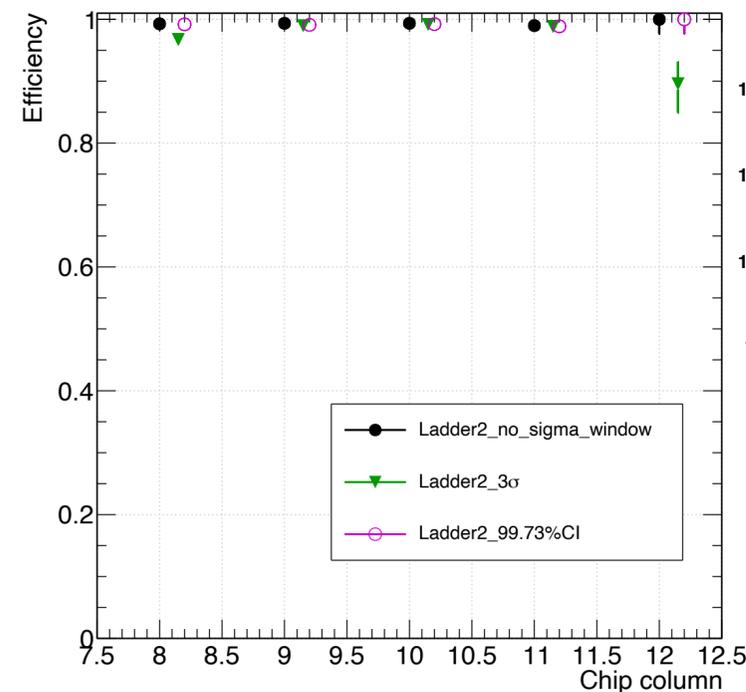
Ladder0



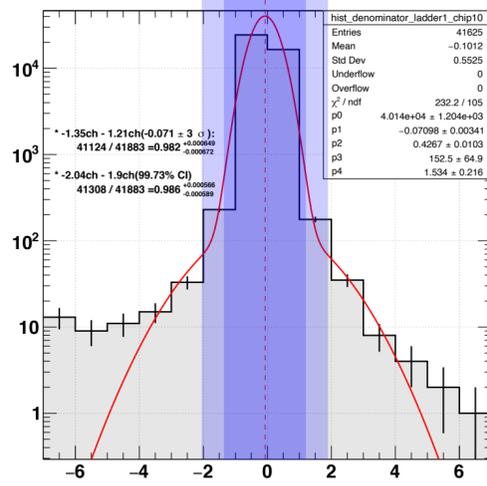
Ladder1



Ladder2

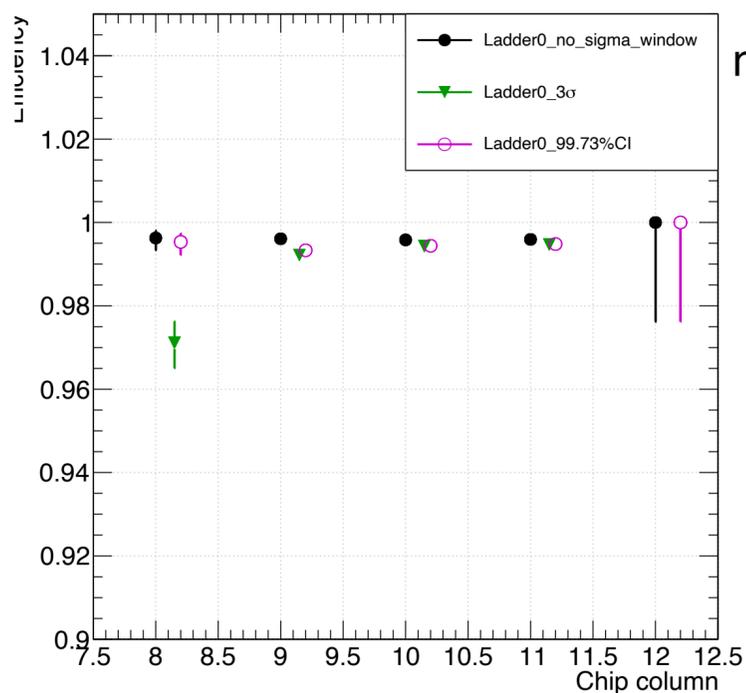


hist_denominator_ladder1_chip10



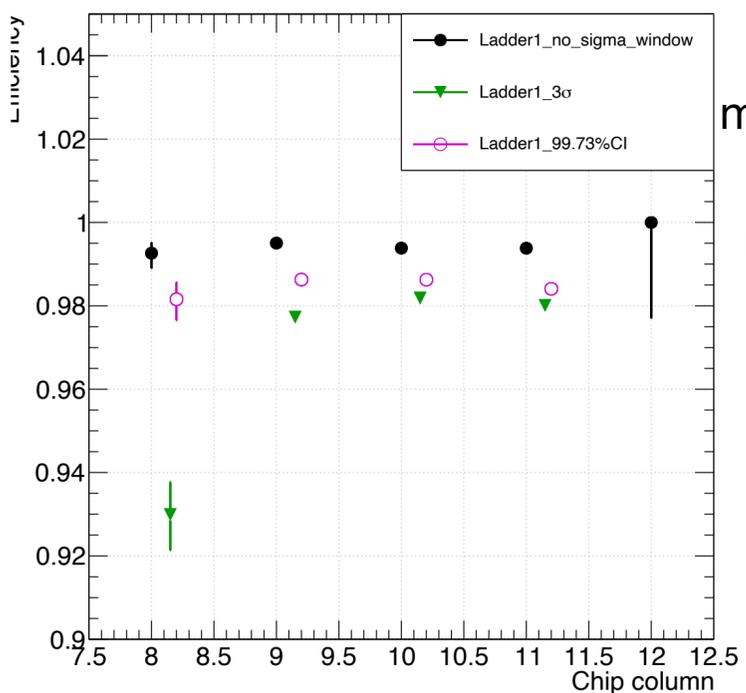
zoomed

Ladder0



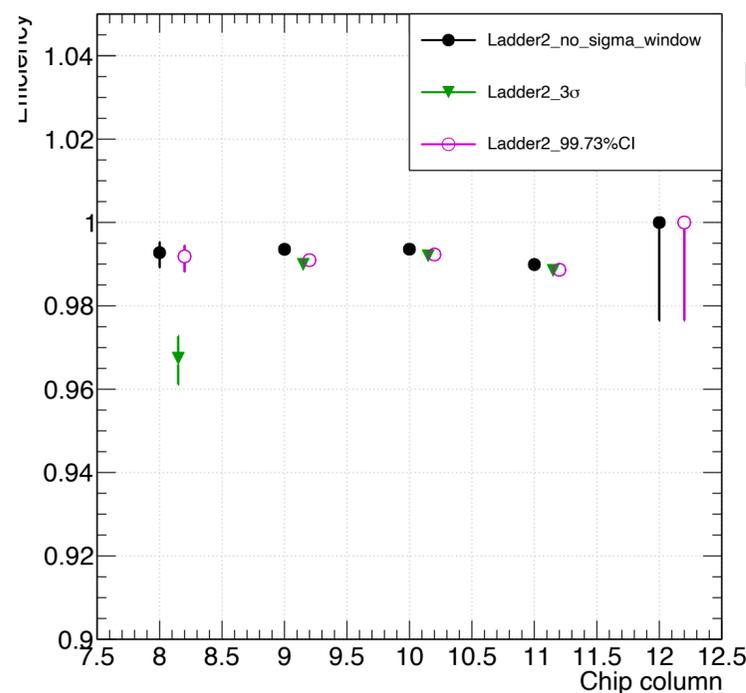
mean of
 3σ
0.994

Ladder1



mean of
 3σ
0.980

Ladder2



mean of
 3σ
0.990

Issue: Analyzer dependence, Detection efficiency, Comparison

Since the track slope distributions from the 2 methods are not the same, comparison of the detection efficiency with the track slope cut is not possible. Comparison with the cut is briefly shown.

Detection efficiency without the sigma window cut

Ladder0

Chip	σ	ϵ Fitting	ϵ Geometrical	Fit. - Geom.	
0	9	-1	99.6%	99.6%	0.04%
0	10	-1	99.6%	99.5%	0.03%
0	11	-1	99.6%	99.6%	0.00%

Ladder1

Chip	σ	ϵ Fitting	ϵ Geometrical	Fit. - Geom.	
1	9	-1	99.5%	99.5%	0.05%
1	10	-1	99.4%	99.4%	0.01%
1	11	-1	99.4%	99.4%	-0.02%

Ladder2

Chip	σ	ϵ Fitting	ϵ Geometrical	Fit. - Geom.	
2	9	-1	99.4%	99.5%	-0.10%
2	10	-1	99.4%	99.4%	-0.02%
2	11	-1	99.0%	99.0%	0.01%

→ No big difference between the 2 methods as expected

Detection efficiency with the 3-sigma window cut

Chip	σ	ϵ Fitting	ϵ Geometrical	Fit. - Geom.	
0	9	3	99.2%	96.3%	2.96%
0	10	3	99.4%	97.0%	2.43%
0	11	3	99.5%	96.7%	2.77%

Chip	σ	ϵ Fitting	ϵ Geometrical	Fit. - Geom.	
1	9	3	97.7%	96.1%	1.63%
1	10	3	98.2%	96.2%	2.02%
1	11	3	98.0%	95.5%	2.52%

Chip	σ	ϵ Fitting	ϵ Geometrical	Fit. - Geom.	
2	9	3	99.0%	95.2%	3.81%
2	10	3	99.2%	95.9%	3.29%
2	11	3	98.8%	95.2%	3.68%

→ Few % of difference!

Issue: Analyzer dependence, Conclusion

Genki tried the fitting method, which have beed hired by Cheng-Wei.

Residual distributions obtained from the fitting method are slightly sharper than ones from the the geometrical method. The track slope cuts suppress the satellite peak drastically, and remove the tail-like structure around the peak especially for the fitting method.

Since much sharper residual distributions are obtained thanks to the fitting method and the track slope cuts, more the 99% efficiency was achieved with the 3-sigma window cut. This is consistent with Chen-Wei's results.

For better results:

- optimization of alignment correction depending on the chips
- consideration of the 3-sigma window cut
- optimization of the stack slope cut

No sigma window cut

	chip	σ	ϵ Ladder 0	ϵ Ladder 1	ϵ Ladder 2
Genki, no additional cut	10	-1	0.994	0.994	0.954
Genki, straight beam track	10	-1	0.981	0.994	0.963
Genki, Fitting method	10	-1	0.996	0.994	0.994
Chen-Wei, ELPH poster					
Chen-Wei, new (3/24)					
Miu	10	-1	0.995	0.994	0.996
Genki, Fitting method, MC	10	-1	0.999	0.998	0.998

3 σ window

	chip	σ	ϵ Ladder 0	ϵ Ladder 1	ϵ Ladder 2
	10	3	0.940	0.937	0.894
	10	3	0.883	0.961	0.921
	10	3	0.994	0.982	0.992
	?	3	0.993	0.995	0.971
	10	3	0.992	0.998	0.991
	10	3	0.977	0.984	0.969
	10	3	0.997	0.996	0.998

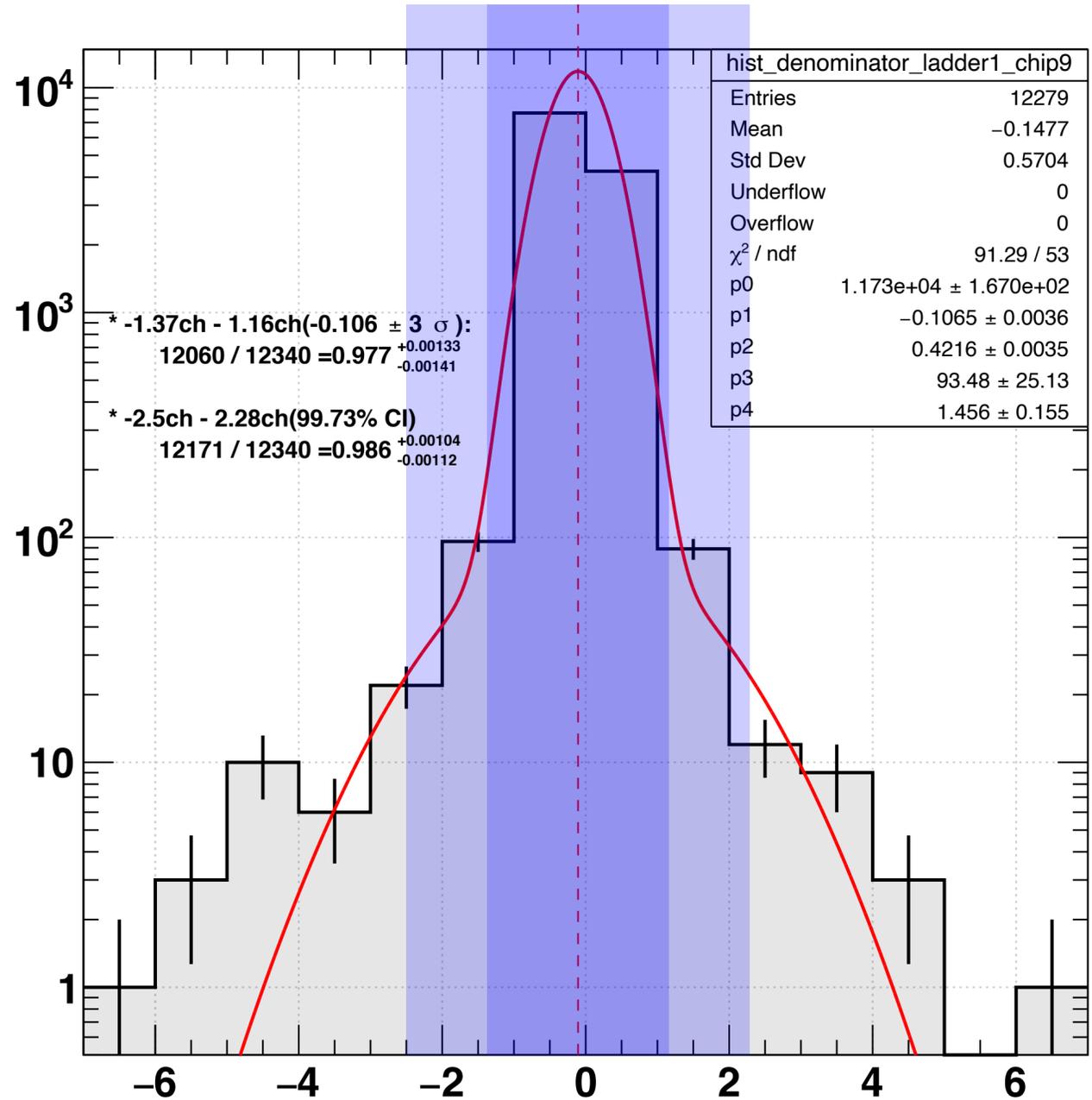
The difference well was understood.

backup

Detection efficiency, to get better results...

Run89, chip10

hist_denominator_ladder1_chip9



```
bool Get3SigmaRange( TF1* f, double& lower, double& upper )
{
    double xmin = f->GetXmin();
    double xmax = f->GetXmax();

    //double mean = f->Mean( xmin, xmax ); // useless, it's fine in CINT.
    double mean = f->GetParameter(1);
    double whole_area = f->Integral( xmin, xmax );

    double division = 1e5;
    double step = (xmax - xmin) / division;

    for( int i=0; i<int(division); i++ )
    {
        double xmin_current = mean - i * step;
        double xmax_current = mean + i * step;

        double area = f->Integral( xmin_current, xmax_current );

        if( area / whole_area > 0.9973 )
        {
            lower = xmin_current;
            upper = xmax_current;
            return true;
        }
    }
    return false;
}
```

I calculated 99.73% of the all area of the fitting function:

$$\left(\int_{\mu-a}^{\mu+a} f(x)dx \right) / S = 0.9973$$

	min	max	denominator	numerator	ϵ
The leading gaussian	-1.37	1.16	12060	12340	0.977
Whole distribution	-2.5	2.28	12171	12340	0.986

Since the residual distributions are not reproduced by a single gaussian, acceptance range for detection efficiency calculation should be modified accordingly, otherwise we underestimate the efficiency. This effort slightly increases the efficiency. For low statistic distributions, it increases the efficiency up to 0.1.