

Dynamically groomed jet radius in heavy-ion collisions

(towards sPHENIX predictions)

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Based on JHEP07 (2021) 020 and PRD 105-11 (2022)

Jet substructure observables

- Jet substructure in small collision systems (pp , e^+e^-):
 - Large variety of techniques: mMDT, SoftDrop, ...
Dasgupta, Fregoso, Marzani, Salam, 1307.0007, Larkoski, Marzani, Soyez, Thaler, 1402.2657
 - Many applications: boosted objects tagging, precision determination of α_s, \dots
- Jet substructure in AA collisions:
 - Vacuum baseline under pQCD control.
 - Tuned to be sensitive to specific medium effects.

Dynamically groomed jet angle

- Good pQCD control, but plagued by large NP corrections at low p_t .
- Sensitivity to the coherence angle of the medium θ_c .
- Can help to constrain jet quenching models.

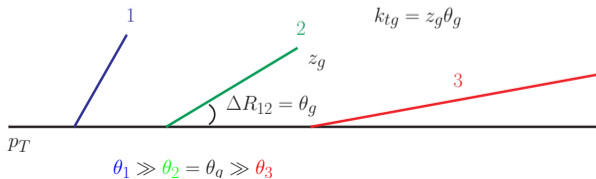
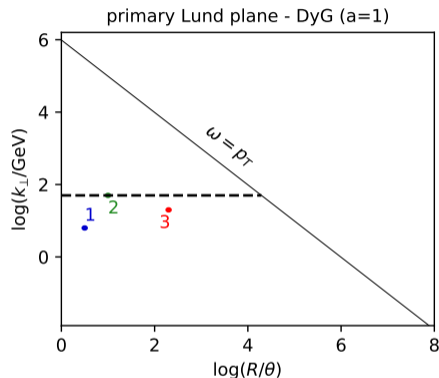
Dynamically groomed distributions

Dynamical grooming techniques proposed by

Mehtar-Tani, Soto-Ontoso, Tywoniuk, 1911.00375

Definition

- Tag the hardest declustering in all the C/A sequence, with hardness measure $\kappa^{(a)} = z(1-z)p_t(\Delta R/R)^a$.
- Then measure the $k_{tg} = z\Delta R/R$ or $\theta_g = \Delta R$ of this branching.



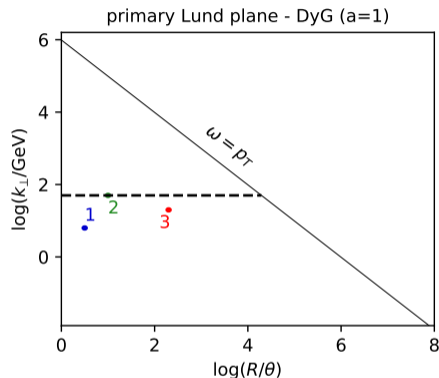
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- Contrary to Soft Drop, only one free parameter $a \Rightarrow$ easier to systematically study the grooming parameter dependence.
- Grooming condition is set on a “jet-by-jet” basis.

All order k_{tg} calculation in pp

- Cumulative distribution:

$$\Sigma(k_{tg}) = \frac{1}{\sigma_0} \int_0^{k_{tg}} dk'_{tg} \frac{d\sigma^{(a)}}{dk'_{tg}}$$

- Contrary to many jet observables, the log resummation **does not exponentiate**:

Catani, Trentadue, Turnock, B. Webber, 1993

$$\Sigma(k_{t,g}) = 1 - \bar{\alpha} \ln^2 \left(\frac{1}{k_{t,g}} \right) + \frac{1+a+a^2}{6a} \bar{\alpha}^2 \ln^4 \left(\frac{1}{k_{t,g}} \right) + \mathcal{O}(\bar{\alpha}^3)$$

- The log accuracy is then defined at the level of Σ :

$$\Sigma(k_{tg}) = \sum_{n=0}^{\infty} \alpha_s^n \sum_{m=0}^{2n} c_{nm} \ln^m(k_{tg}),$$

Def.: N^pDL accuracy $\Leftrightarrow c_{nm}$ known $\forall n$ and $2n-p \leq m \leq 2n$.

Banfi, Salam, Zanderighi, 2005

All order k_{tg} calculation in pp PC, Soto-Ontoso, Takacs, 2103.06566

$$\Sigma(k_{t,g}) = \int_0^1 dz \int_0^1 d\theta \tilde{P}(z, \theta) \Delta(\kappa|a) \Theta(k_{t,g} - z\theta)$$

with

$$\tilde{P}(z, \theta) = \left[\frac{2\alpha_s^{2\ell}(z\theta Q) C_i}{\pi z \theta} - 2C_i C_A \frac{\pi^2}{3} \left(\frac{\alpha_s}{2\pi} \right)^2 \frac{\ln(z)}{z} \right] \Theta(e^{-B_i} - z), \text{ and } \ln \Delta(\kappa|a) = - \int_{z\theta^a \geq \kappa} \tilde{P}(z, \theta)$$

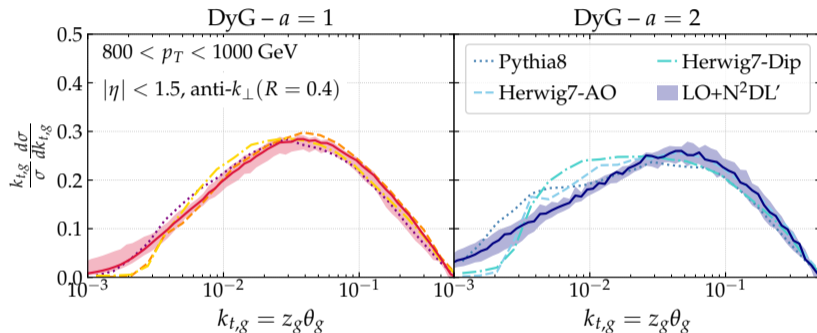
The physical effects that come into play at N²DL:

- ✓ **Hard collinear splittings**
- ✓ **Running coupling corrections at two loops**
- ✓ **Non global configurations** Dasgupta, Salam, 2001
- ✗ **No “clustering” logarithms!** Kang, Lee, Liu, Ringer, 2019, Lifson, Salam, Soyez, 2020
- ✓ C_1 term \Rightarrow requires a $\mathcal{O}(\alpha_s)$ matching.

N²DL resummation matched to LO

PC, Soto-Ontoso, Takacs, 2103.06566

Comparison to parton-level MCs

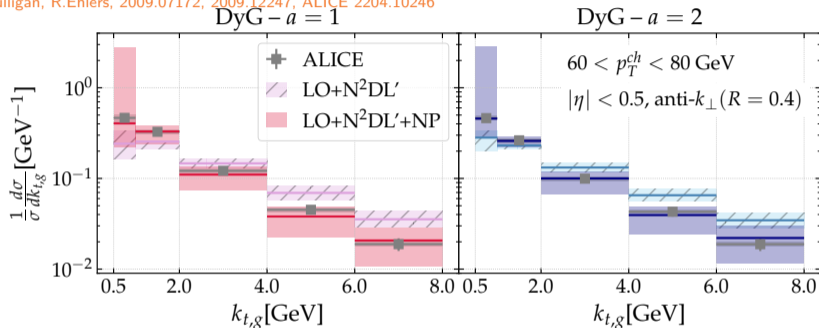


Comments

- Good agreement with parton-level MCs.
- Small differences due to sub-leading effects at N²DL.
- Importance at low $k_{t,g}$ of the infrared cut in the MC parton shower.

Comparison to ALICE data

J. Mulligan, R.Ehlers, 2009.07172, 2009.12247, ALICE 2204.10246



Comments

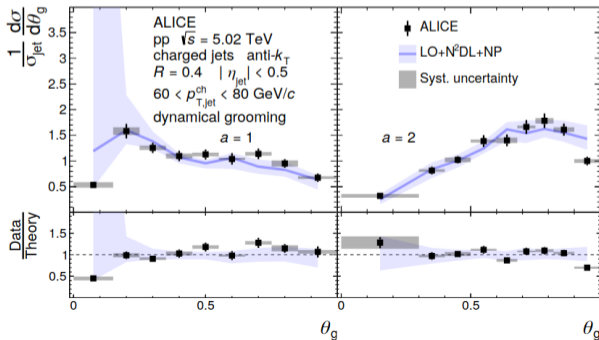
- At such low p_t , hadronization corrections are large.
- Good agreement once a NP factor determined from MCs is included.

The Dynamically groomed θ_g distribution

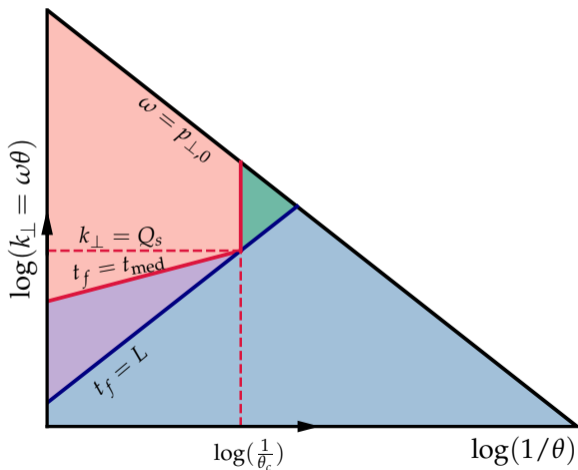
- The opening angle θ_g of the splitting is measured: only Sudakov safe.
- N²DL resummation achieved by taking the limit of IRC safe distributions:

$$\Sigma(z_g) = \lim_{c \rightarrow 0} \int_0^1 dz \int_0^1 d\theta \tilde{P}(z, \theta) \Delta(\kappa|a) \Theta(z_g - z\theta^c)$$

- Comparison to ALICE data: [ALICE 2204.10246](#)



Modification of the phase space in heavy-ion collisions



- In-medium constraint: $k_{\perp}^2 \geq \hat{q}t_f$.

- Out-medium condition: $t_f \geq L$.

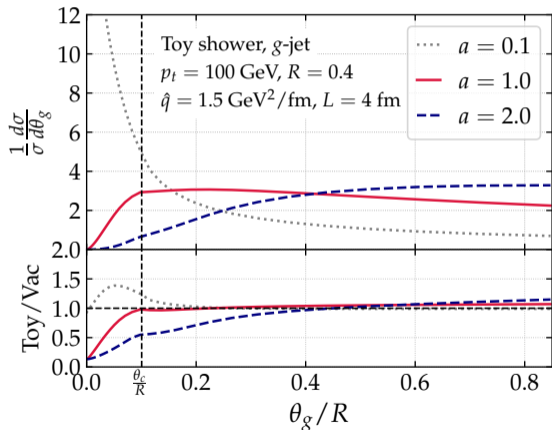
- **NB: because of color coherence, emissions "inside" with $t_f \leq L$ is not modified if**

$$\theta \leq \theta_c = 2/\sqrt{\hat{q}L^3}$$

- Phase-space at RHIC: lower p_{t0} , lower $\hat{q} \Rightarrow$ the green region shrinks.

Analytic toy calculation

Relatively hard intrajet medium-induced emissions



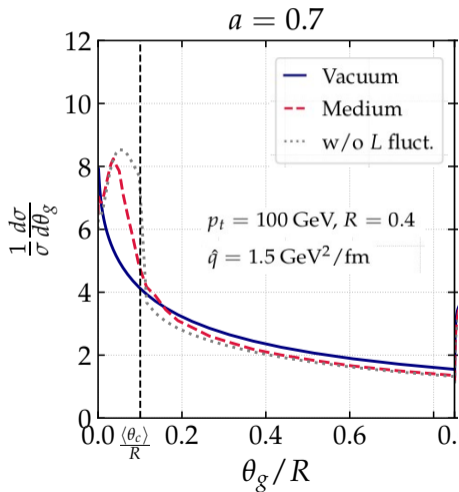
- DyG can select a semi-hard MIEs inside the jet.
- From the factorization:

$$\tilde{P}_{\text{vac}}(z, \theta) \rightarrow \tilde{P}_{\text{vac}}(z, \theta) + \underbrace{\bar{\alpha}_s \sqrt{\frac{\hat{q} L^2}{z^3 p_t}} \mathcal{B}(z, \theta)}_{\sim \text{BDMPS-Z}}$$

- Minimal angle of semi-hard MIEs,
 $\theta \sim Q_s/\omega_c \sim \theta_c \Rightarrow$ transition around θ_c .

Analytic toy calculation

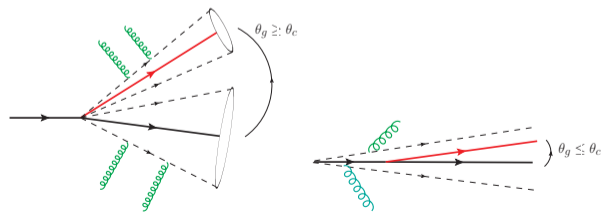
θ_c dependent large angle energy loss:



- Coherence angle $\theta_c \sim 2/\sqrt{\hat{q}L^3}$ measures resolution power of the medium.

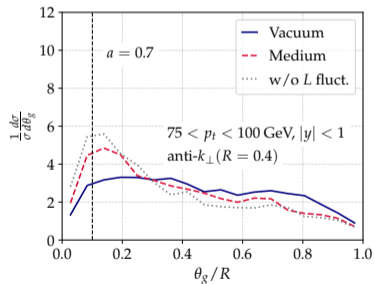
Mehtar-Tani, Salgado, Tywoniuk, 2011 - Casalderrey-Solana, Iancu, 2011

- Jets with $\theta_g \geq \theta_c$ lose more energy.
- θ_g dependent energy loss implemented using quenching weights.



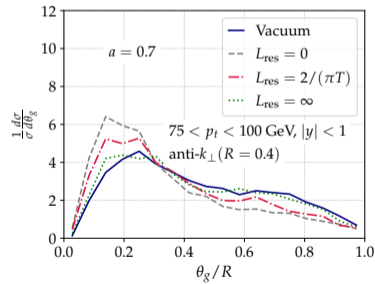
Dependence upon jet quenching model

- Many jet quenching models have a notion of "resolution scale" incorporated.
- Example: L_{res} parameter in the Hybrid strong-weak coupling model.
Casalderrey-Solana, Gulhan, Hulcher, Milhano, Pablos, Rajagopal, 2015-17
- Need for an "orthogonal" observable to discriminate between models.



MC JetMed (weak coupling picture)

PC, Iancu, Mueller, Soyez, 2018



MC Hybrid model (hybrid strong/weak coupling picture)

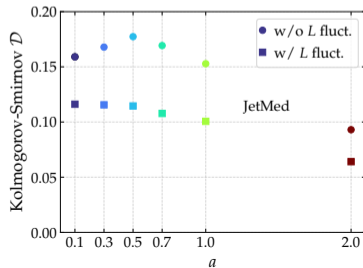
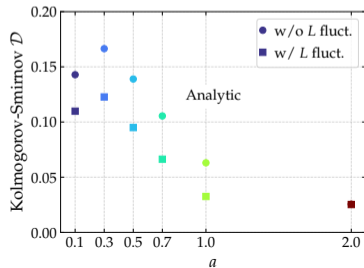
Best experimental set-up

- Kolmogorov-Smirnov distance measures the difference between the medium and vacuum baseline. $KS = \max|\Sigma_{P_b P_b}(\theta_g) - \Sigma_{PP}(\theta_g)|$
- Analytic results confirm our numerical findings.
- "Ideal" set-up:

$$0.5 \lesssim a \lesssim 1 \quad \text{and}$$

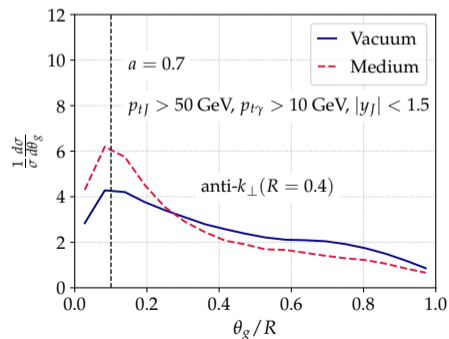
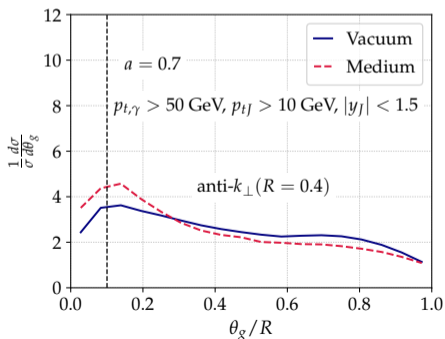
$$R = 0.2$$

reduce medium response and background effects



sPHENIX opportunities: θ_g distribution in γ -jet events

- Theoretical analysis that should be taken with a grain of salt.
- γ -jet events reduce the effect from quark-gluon mixture,
- and help to quantify the selection bias effect. See Brewer, Brodsky, Rajagopal, 2110.13159



Summary

- Analytical calculation of dynamically groomed jet substructure observables, up to N²DL accuracy, supplemented by a LO matching and a Monte-Carlo estimation of NP corrections.
- Good agreement with ALICE data, within the uncertainty.
- In heavy-ion collisions, observable strongly sensitive to the coherence angle θ_c of the plasma, even when selection bias are reduced as in γ -jet events.
- Further studies are necessary to see if a measurement in γ -jet is realistic at RHIC with STAR or sPHENIX.

THANK YOU !