

FPY Covariances

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Overview of cumulative fission product yield covariance development

- Combination of data and BeoH (LANL-developed deterministic fission fragment decay code) through a Kalman filter optimization
 - Optimization using cumulative fission product yields, average prompt/delayed neutron multiplicities
 - Data currently taken from EXFOR (A. Mattera, BNL, is correcting EXFOR data for updated nuclear structure information and providing data that is not in EXFOR)
 - Model stiffness is being addressed to ensure FPYs can be reproduced to the needed accuracy
- Covariances are calculated at discrete incident neutron energies
 - Kalman covariances scaled by the χ^2/N (to EXFOR experimental data)
 - Initial impact of diagonal uncertainties vs full correlations is being investigated (A. Sonzogni, et al., BNL)
- Discussions on the covariance format are still ongoing (more tomorrow)

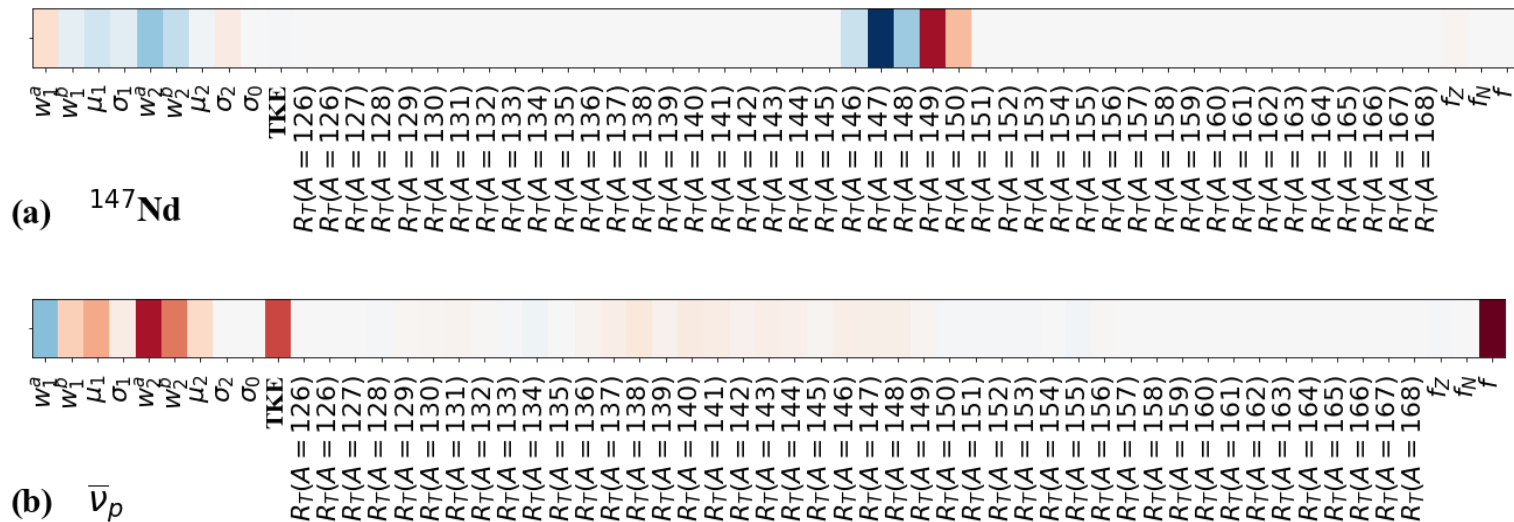
Fission product yield covariances status

- ^{252}Cf spontaneous fission
 - Bulk fitting has been performed
 - Covariances are calculated
- ^{235}U neutron induced fission - thermal to 20 MeV
 - Bulk fitting has been performed up to 20 MeV
 - Covariances calculated up to 20 MeV
- ^{238}U neutron induced fission – thermal to 20 MeV
 - Bulk fitting has been performed up to ~12 MeV (third-chance fission opening)
 - Covariances calculated up to ~12 MeV
- ^{239}Pu neutron induced fission – thermal to 20 MeV
 - Bulk fitting has been performed up to 20 MeV
 - Covariances calculated up to 20 MeV

All calculations shown here are preliminary! Improvements are still being made.

An overview using $^{252}\text{Cf}(\text{sf})$

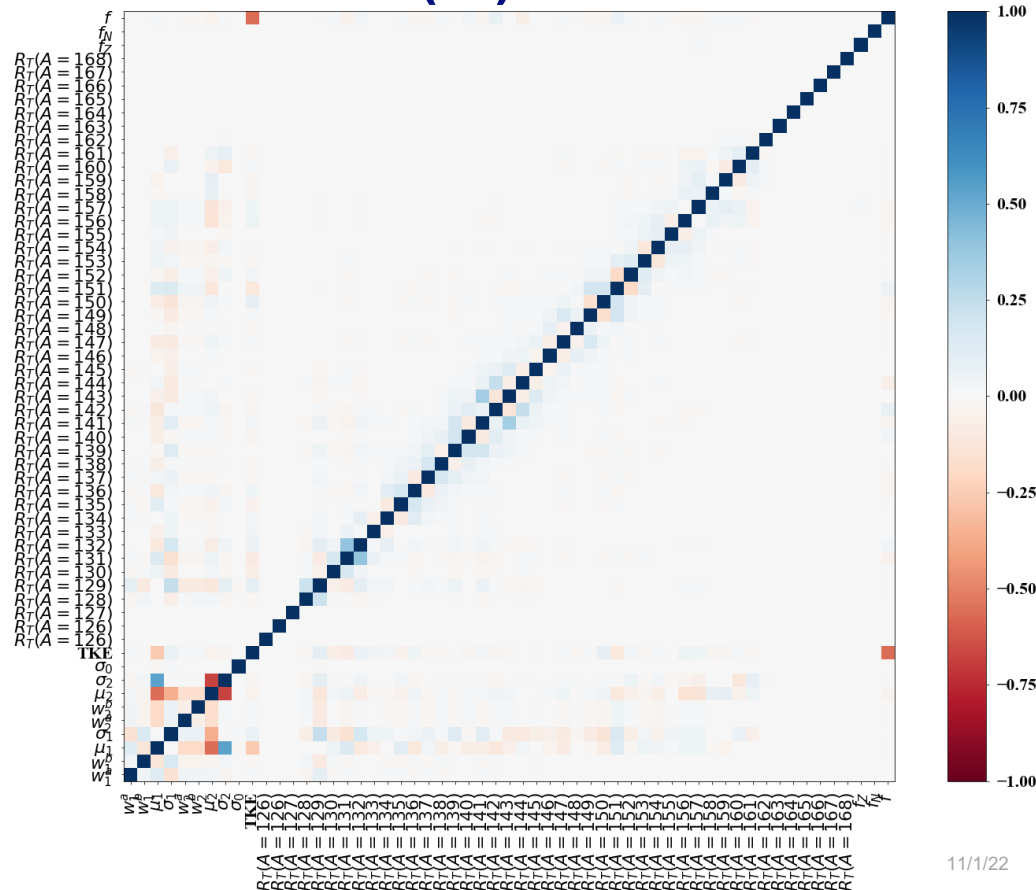
Parameter sensitivities for ^{147}Nd
cumulative FPY and prompt
average neutron multiplicity



Cumulative FPYs, prompt and delayed $\langle \nu \rangle$ including in the optimization.
The data (for fits discussed in this talk) are taken from EXFOR.

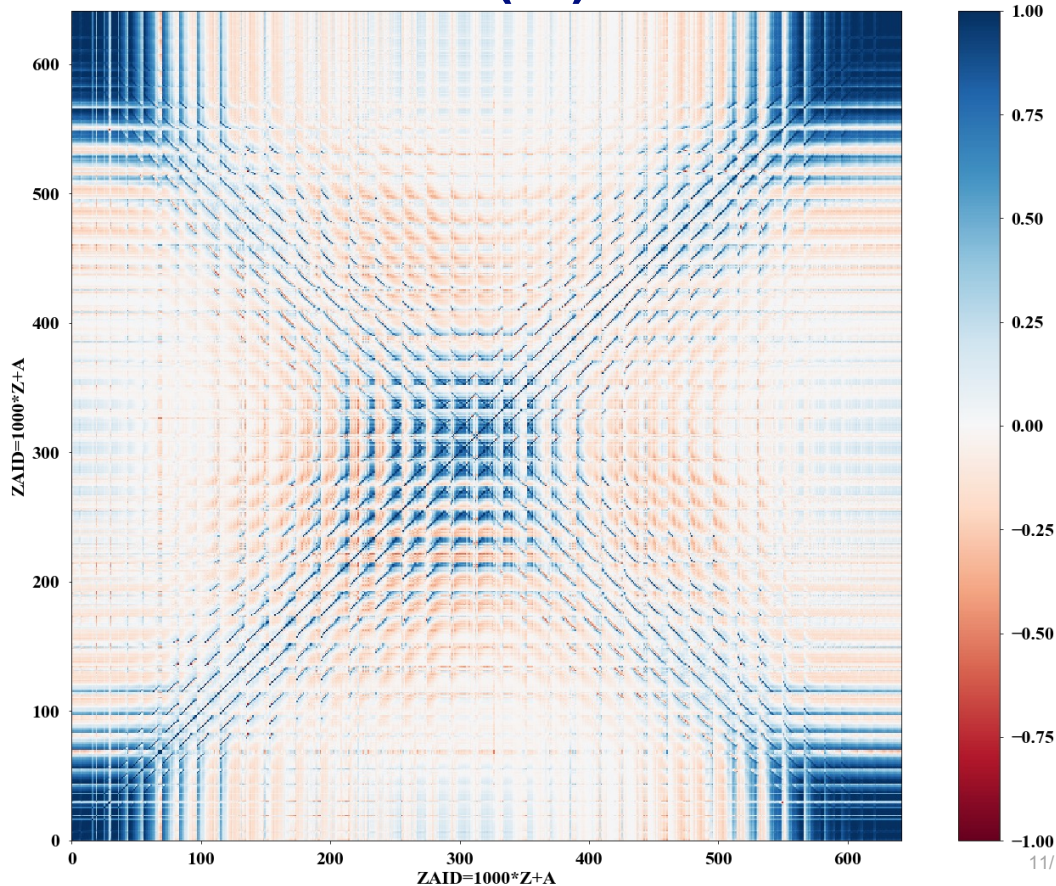
Parameter covariance matrix for $^{252}\text{Cf}(\text{sf})$

- Most parameters are uncorrelated ($R_T(A)$ values only impact a few FPYs each, most correlations are along the diagonal)
- $Y(A)$ parameters are more highly correlated (first 9 parameters)
- TKE and f are highly anti-correlated (mainly through prompt $\langle v \rangle$)



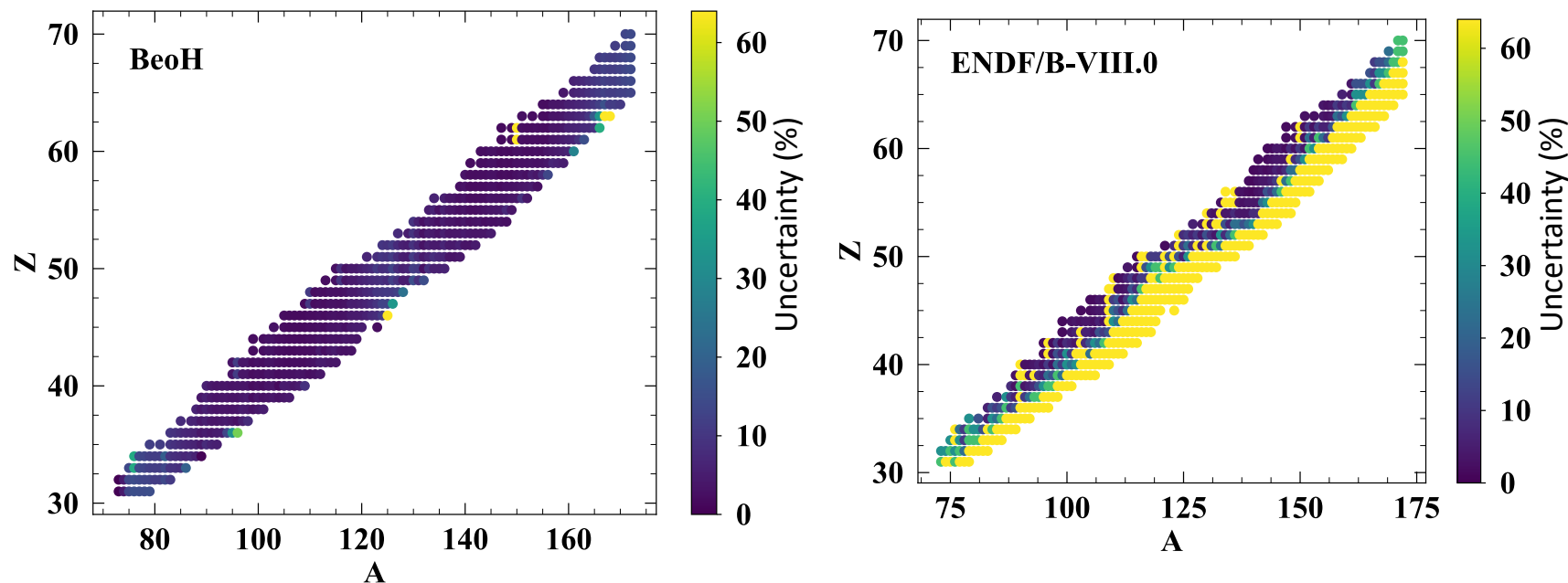
Cumulative FPY correlations for $^{252}\text{Cf}(\text{sf})$

Cumulative FPYs are largely uncorrelated (from the inclusion of $R_T(A)$) but we see blocks of higher correlations.



$$F = CPC^T$$

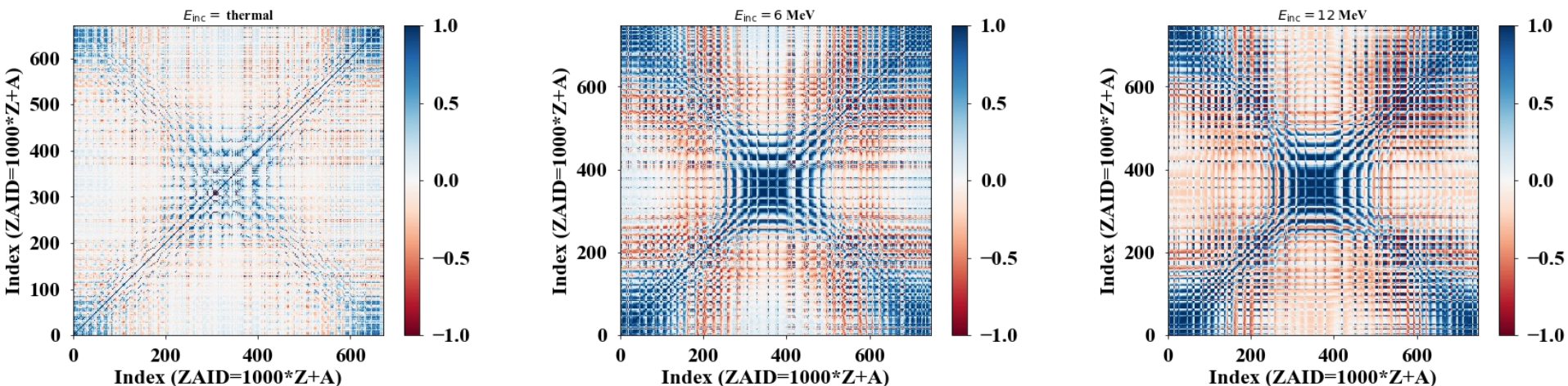
Comparison between preliminary BeoH and ENDF/B-VIII.0 relative uncertainties for $^{252}\text{Cf}(\text{sf})$



A piecewise approach is used to fit neutron-induced fission reactions

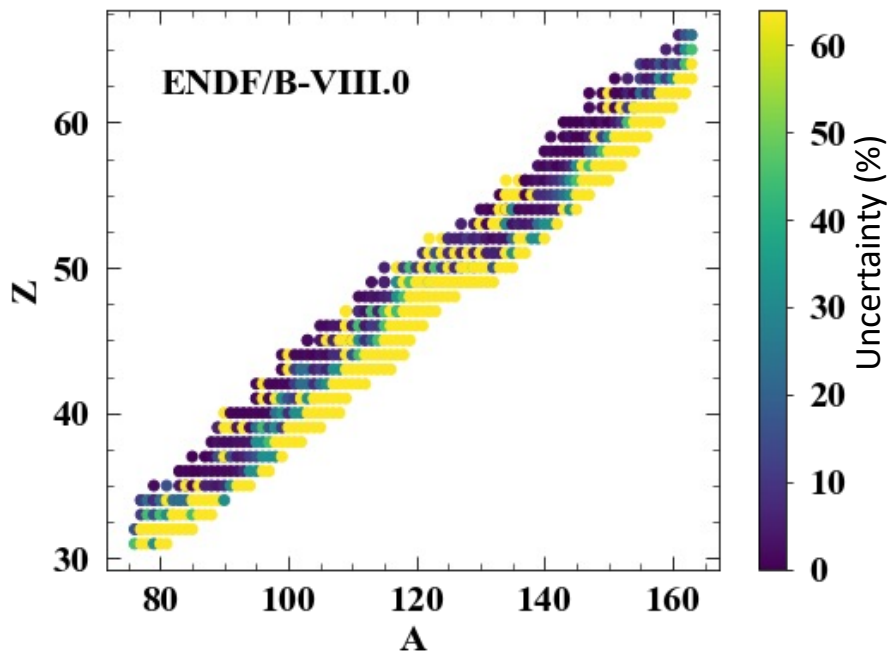
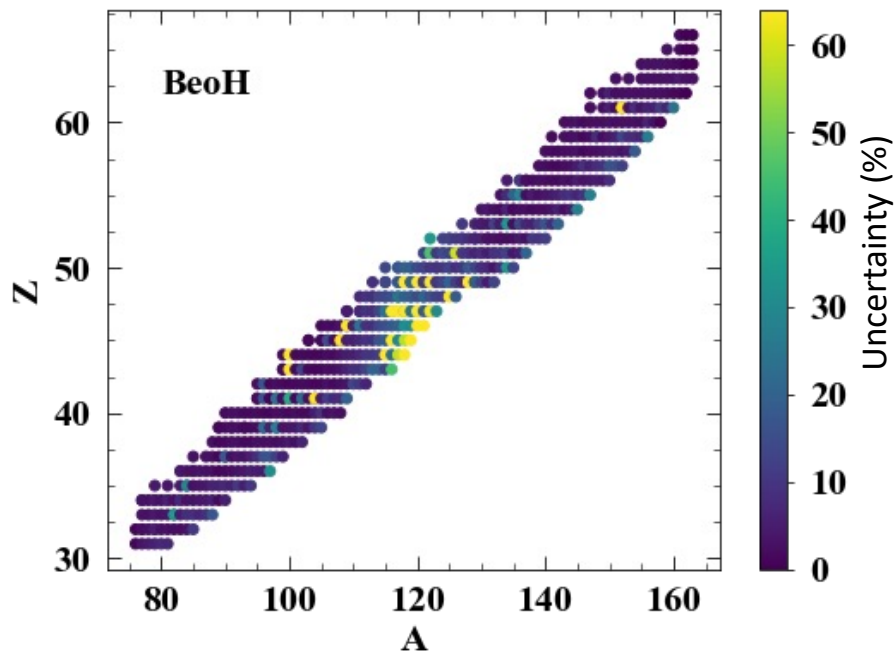
- First-chance parameters fit then fixed, second-chance parameters fit then fixed, third-chance parameters fit then fixed.
- Excitation energy sharing parameters only fit in the first-chance energy region – then kept the same for the other compounds (initial optimizations are to $\nu(A)$, most of the data is below 6 MeV incident neutron energy).
- Fourth-chance fission generally only contributes on the order of a few percent up to 20 MeV and little data to no data are available in this region; parameters are taken from CGMF and held constant.
- This approach possibly raises some questions about how to calculate uncertainties and covariances consistently.

$^{239}\text{Pu}(n,f)$ correlations matrices are being developed at discrete energies from thermal to 20 MeV



Because parameters in the fourth-chance energy region are currently not fit, we currently use the covariance matrix from the highest energy point in the third-chance region for the covariances up to 20 MeV.

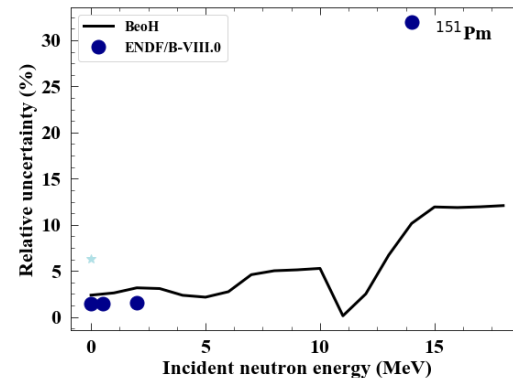
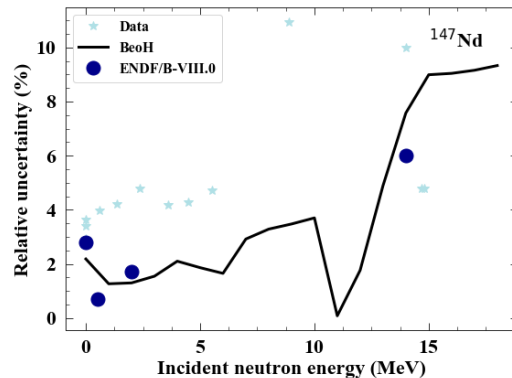
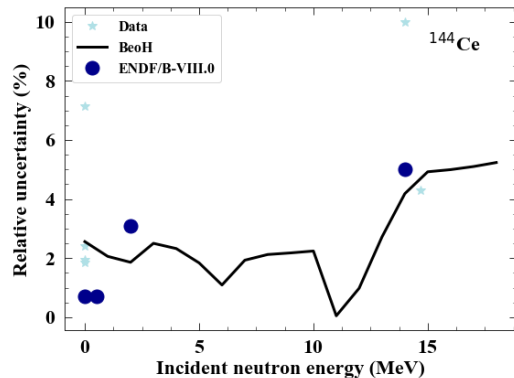
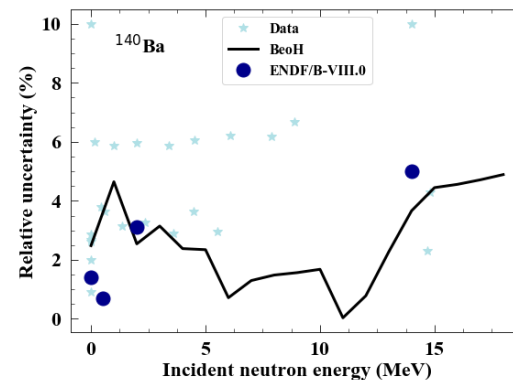
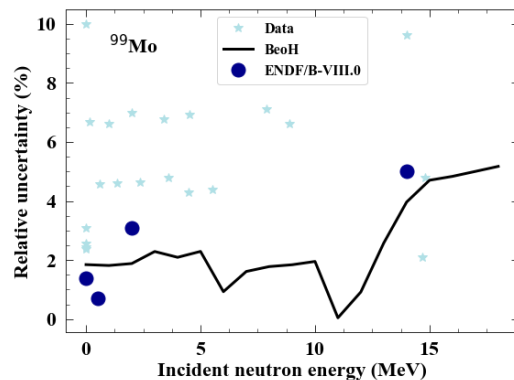
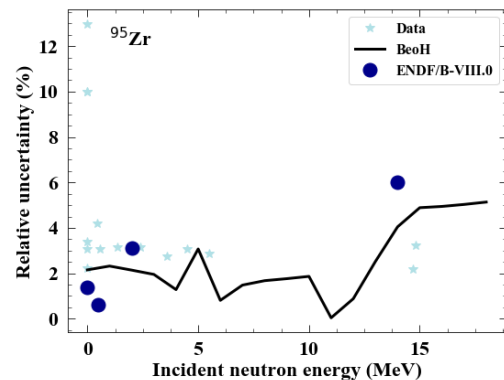
Comparison of relative percent uncertainties for $^{239}\text{Pu}(n,f)$ at thermal



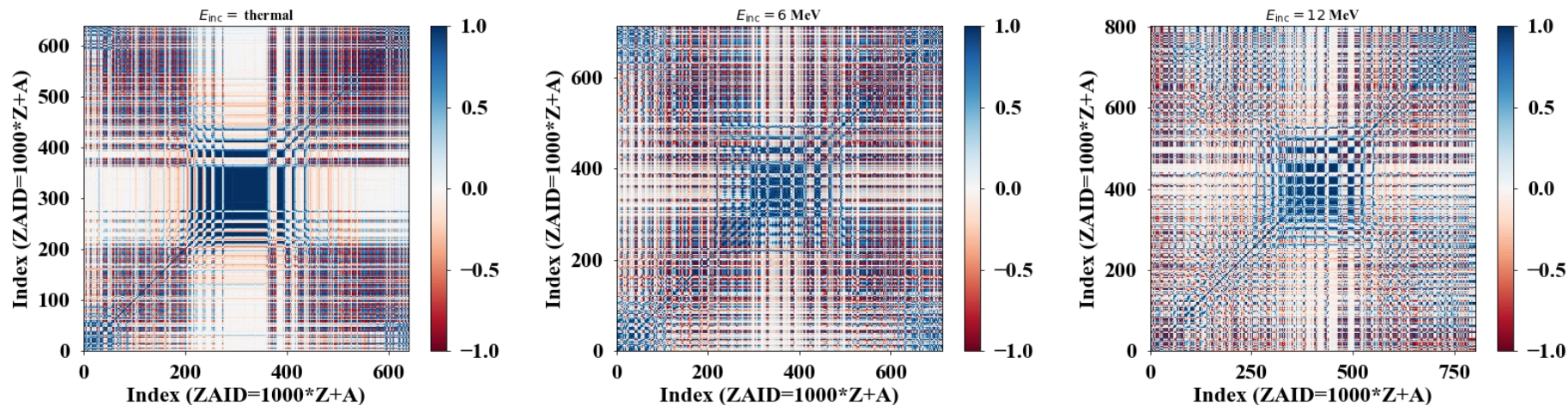
$^{239}\text{Pu}(n,f)$ thermal cumulative FPY percent uncertainty comparison

$^{239}\text{Pu}(n_{\text{th}},f) Y_c(A,Z)$	ENDF/B-VIII.0	IRDFF-II	Present (prelim)
^{95}Zr	1.4%	1.1%	2.2%
^{99}Mo	1.4%	0.7%	1.8%
^{103}Ru	2.0%	2.1%	1.7%
^{106}Ru	2.0%	2.3%	2.2%
^{137}Cs	64.0%	1.22%	10.2%
^{140}Ba	1.4%	1.1%	2.5%
^{144}Ce	0.7%	0.9%	2.6%

$^{239}\text{Pu}(n,f)$ relative uncertainties for select cumulative FPY

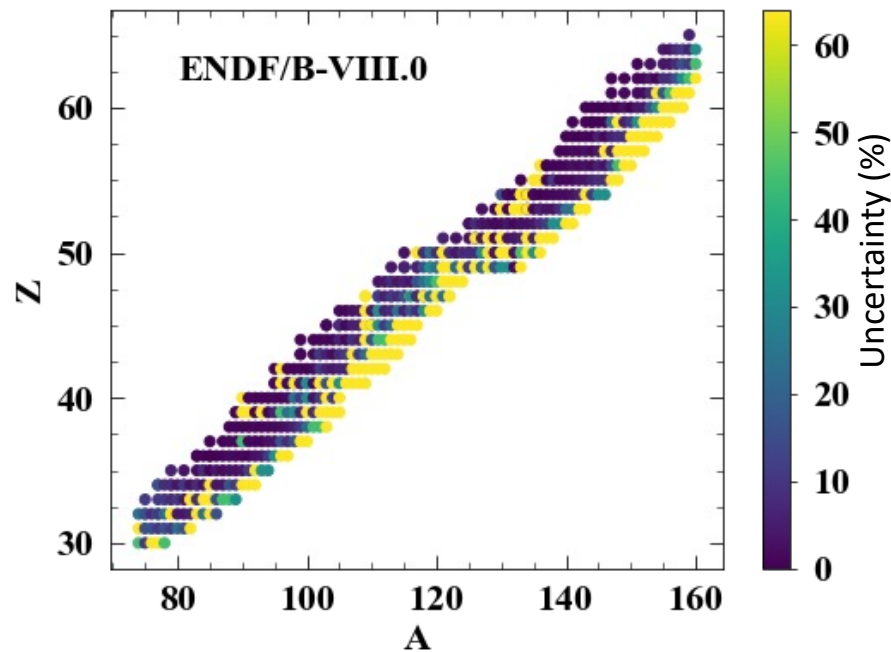
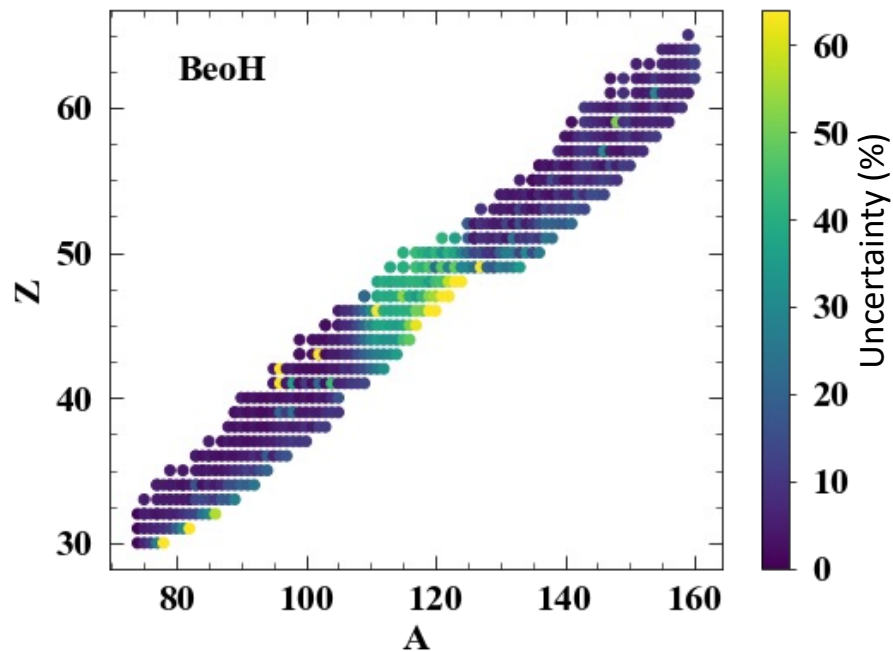


$^{235}\text{U}(n,f)$ correlations matrices are being developed at discrete energies from thermal to 20 MeV



Because parameters in the fourth-chance energy region are currently not fit, we currently use the covariance matrix from the highest energy point in the third-chance region for the covariances up to 20 MeV.

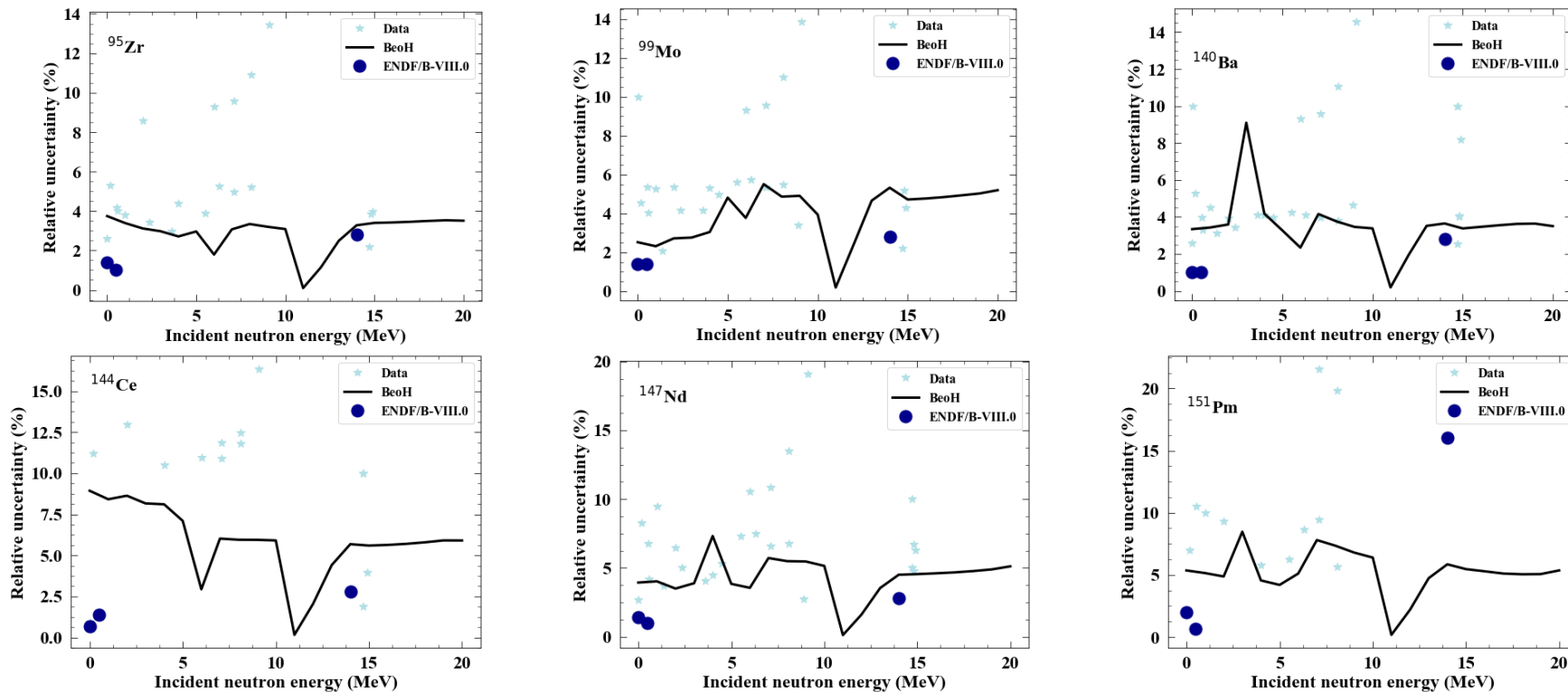
Comparison of relative percent uncertainties for $^{235}\text{U}(n,f)$ at thermal



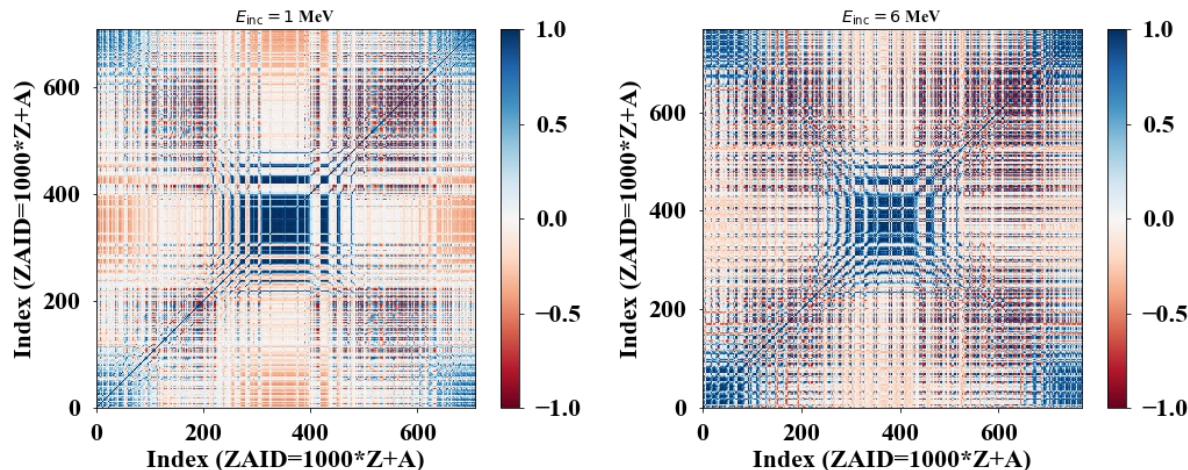
$^{235}\text{U}(n,f)$ thermal cumulative FPY percent uncertainty comparison

$^{235}\text{U}(n_{\text{th}},f) Y_c(A,Z)$	ENDF/B-VIII.0	IRDFF-II	Present (prelim)
^{95}Zr	1.4%	1.0%	3.7%
^{99}Mo	1.4%	1.3%	2.5%
^{103}Ru	1.4%	2.1%	2.2%
^{106}Ru	1.4%	2.3%	7.7%
^{137}Cs	0.5%	1.04%	4.0%
^{140}Ba	1.0%	1.0%	3.3%
^{144}Ce	0.7%	0.9%	8.9%

$^{235}\text{U}(\text{n},\text{f})$ relative uncertainties for select cumulative FPY

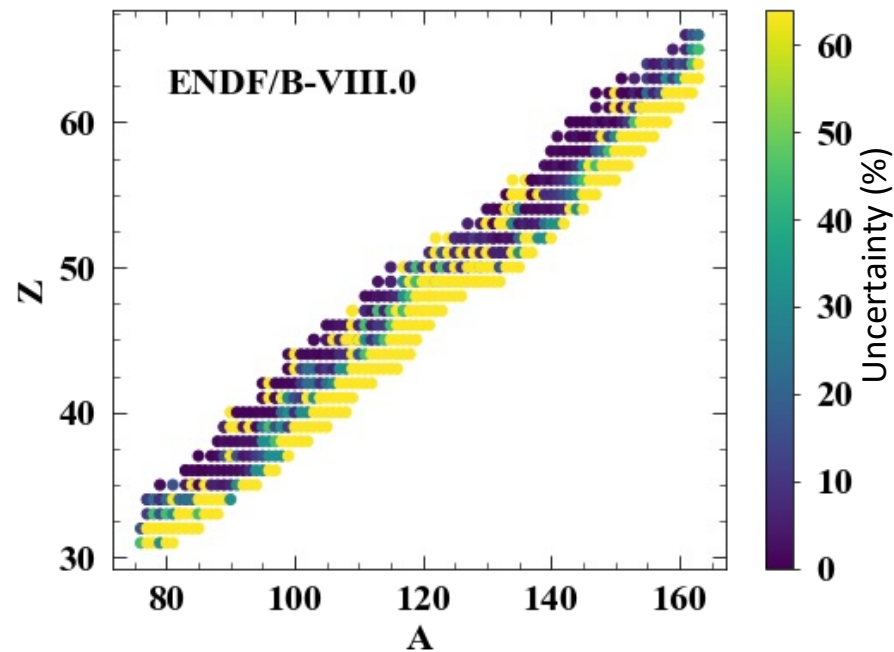
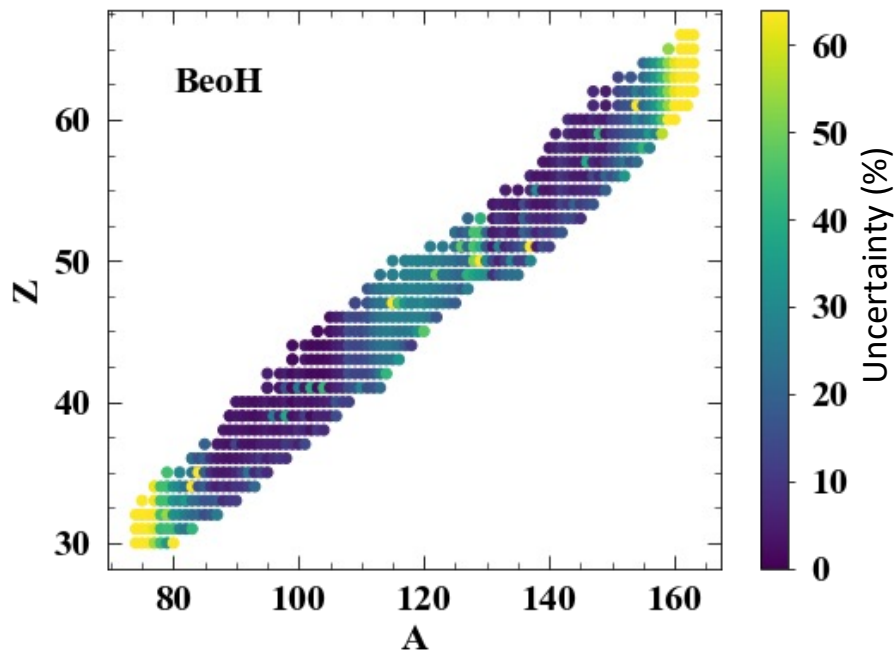


$^{238}\text{U}(n,f)$ correlations matrices are being developed



The optimization of the third-chance parameters is still being performed.

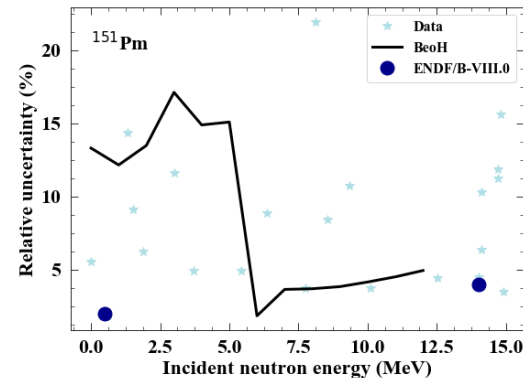
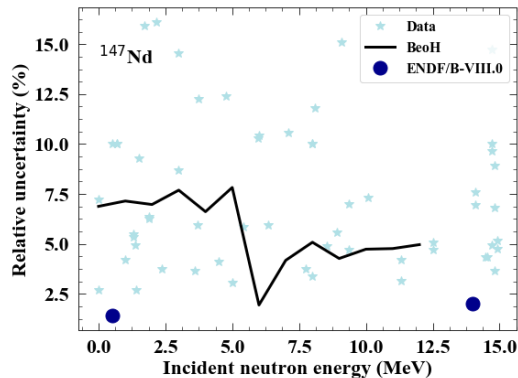
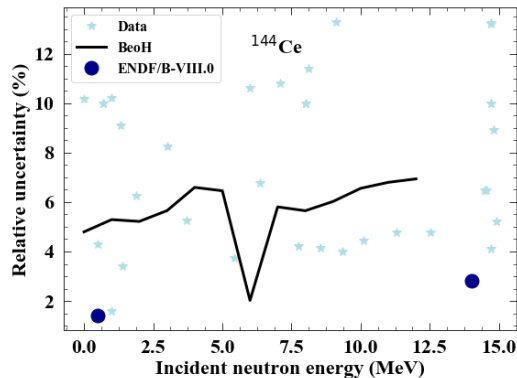
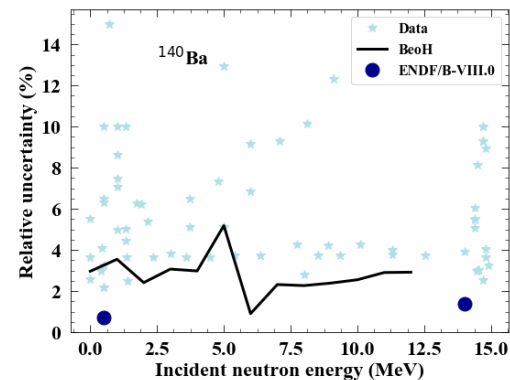
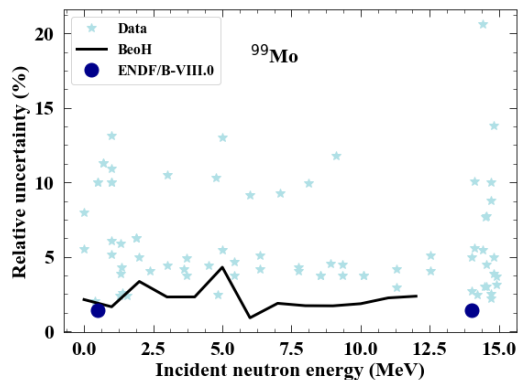
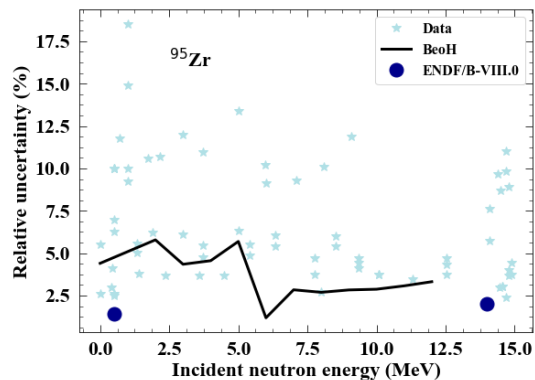
Comparison of relative percent uncertainties for $^{238}\text{U}(n,f)$ at 0.5 MeV



$^{238}\text{U}(n,f)$ 0.5 MeV cumulative FPY percent uncertainty comparison

$^{238}\text{U}(n_{0.5 \text{ MeV}}, f)$ $Y_c(A, Z)$	ENDF/B-VIII.0	IRDFF-II	Present (prelim)
^{95}Zr	1.4%	1.6%	4.8%
^{99}Mo	1.4%	1.6%	1.9%
^{103}Ru	1.4%	1.8%	1.8%
^{106}Ru	1.4%	5.3%	5.1%
^{137}Cs	1.0%	2.33%	6.6%
^{140}Ba	0.7%	1.29%	3.3%
^{144}Ce	1.4%	2.25%	5.0%

$^{238}\text{U}(n,f)$ relative uncertainties for select cumulative FPY



Conclusions and future work

- Covariances are being developed for the FPY re-evaluation, for $^{252}\text{Cf}(\text{sf})$, $^{235,238}\text{U}(\text{n,f})$, and $^{239}\text{Pu}(\text{n,f})$
- For neutron-induced fission, covariances are being developed from thermal to 20 MeV (optimization for $^{238}\text{U}(\text{n,f})$ after ~ 12 MeV still in progress)
- Results shown here are preliminary
 - Further optimization will take place – accounting for model stiffness, new decay data from BNL (Sonzogni), updated FPY values from BNL (Mattera) – which could change correlations and uncertainties
- Here, results for the cumulative FPYs were shown, but we have consistent calculations with independent yields and covariances from BeoH
- Currently, only considering covariances at single incident energies (no cross-energy correlations included)
- Covariance format in ENDF is still under development