

# Status of the updated FPY evaluation for $^{252}\text{Cf}(\text{sf})$ , $^{235,238}\text{U}(\text{n},\text{f})$ , and $^{239}\text{Pu}(\text{n},\text{f})$

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Mumpower, W. Haecck, N. Gibson, A.  
Mattera, and A. Sonzogni.

# Evaluation methodology for fission product yields

- Combination of experimental data and model calculations through a Kalman filter optimization
  - Includes new experimental data, including recent effort to measure short-lived FPY and energy-dependent values
  - BeoH – LANL-developed, Hauser-Feshbach fission fragment decay code (e.g. PRC 103, 014615 (2021) and references therein)
  - Updated experimental FPY data with most recent structure information and updated decay data (consistency between independent and cumulative FPY with decay data)
- Covariances are calculated consistently from the Kalman filter (see talk during Wednesday's covariance session)
- R-values are not currently included in the fitting procedure but are instead being used for validation

# Optimization details

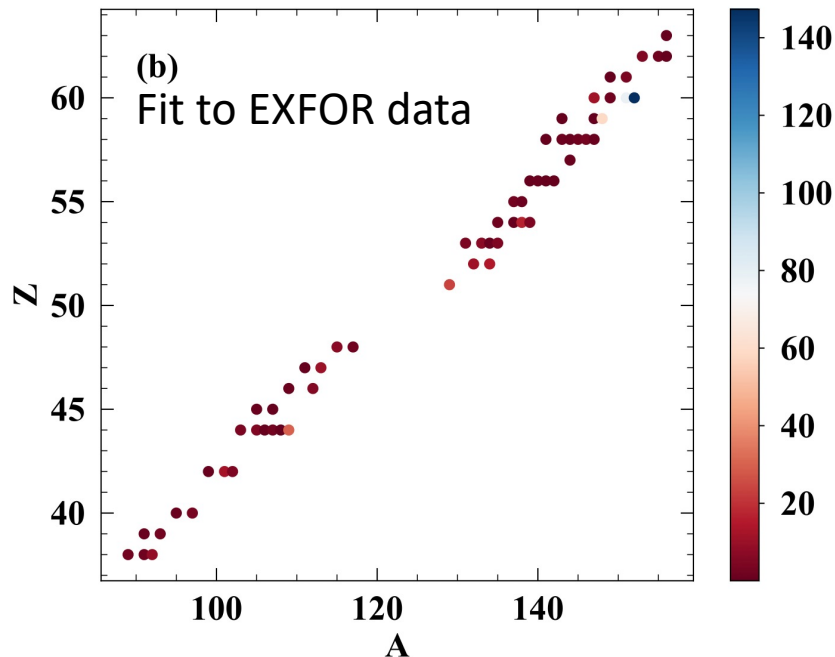
- Prompt and delayed average neutron multiplicity included in the optimization to further constrain input parameters that are not well-constrained by the cumulative fission product yields
- Currently, data from EXFOR is being used, which has been nominally curated to remove some discrepant data
  - Templates of experimental uncertainties should be used
  - BNL is sending revised FPY values based on current structure data and data that is not included in EXFOR (A. Mattera),  $^{238}\text{U}(n,f)$  received already
  - BNL has shared updated decay data, which will be incorporated (A. Sonzogni)
  - Comparison against data used in previous LANL/England and Rider evaluation has to be done
- We first perform a bulk optimization to experimental cumulative FPYs (current status); next, tuning will be undertaken to ensure that our model is not too rigid to reproduce all important data (in progress)

# Fission product yield evaluations under development

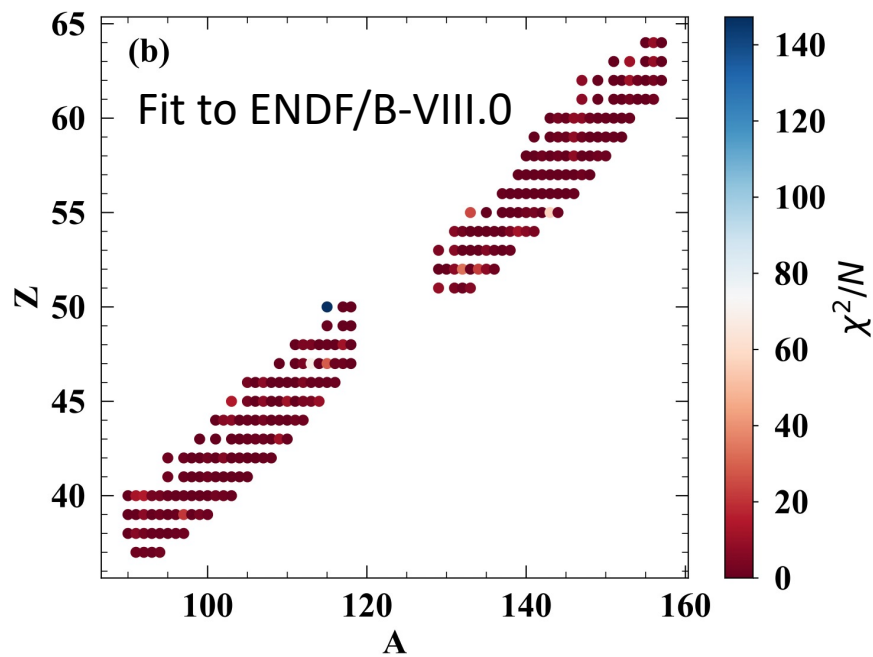
- $^{252}\text{Cf}$  spontaneous fission
  - Bulk fitting has been performed
  - Covariances are calculated
- $^{235}\text{U}$  neutron induced fission - thermal to 20 MeV
  - Bulk fitting has been performed up to 20 MeV
  - Covariances calculated up to 20 MeV
- $^{238}\text{U}$  neutron induced fission – thermal to 20 MeV
  - Bulk fitting has been performed up to ~12 MeV (third-chance fission opening)
  - Covariances calculated up to ~12 MeV
- $^{239}\text{Pu}$  neutron induced fission – thermal to 20 MeV
  - Bulk fitting has been performed up to 20 MeV
  - Covariances calculated up to 20 MeV

All calculations shown here are preliminary! Improvements are still being made.

# $^{252}\text{Cf}(\text{sf})$ cumulative FPY data overview (taken from EXFOR, FPY>1%)



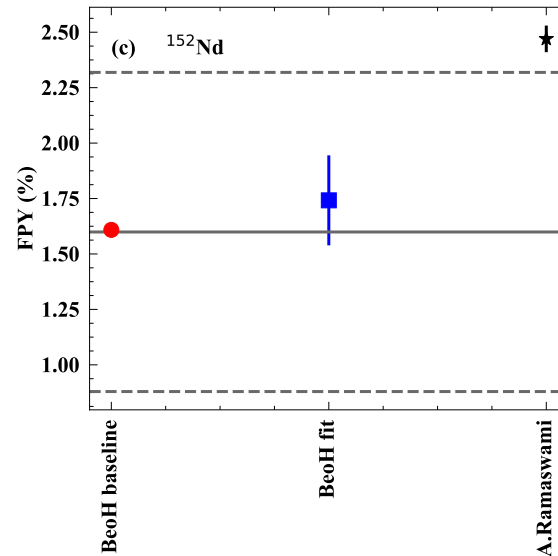
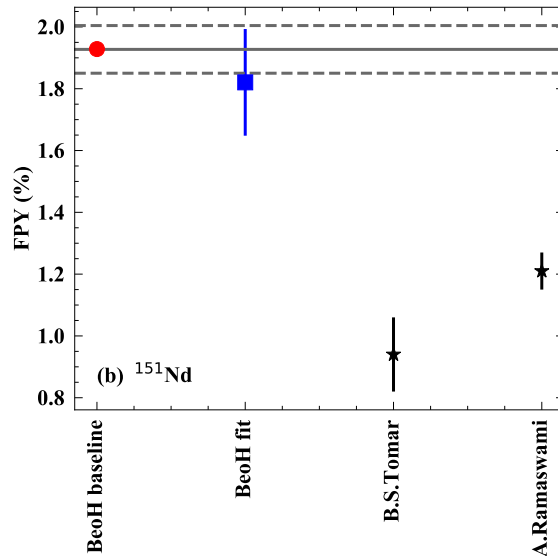
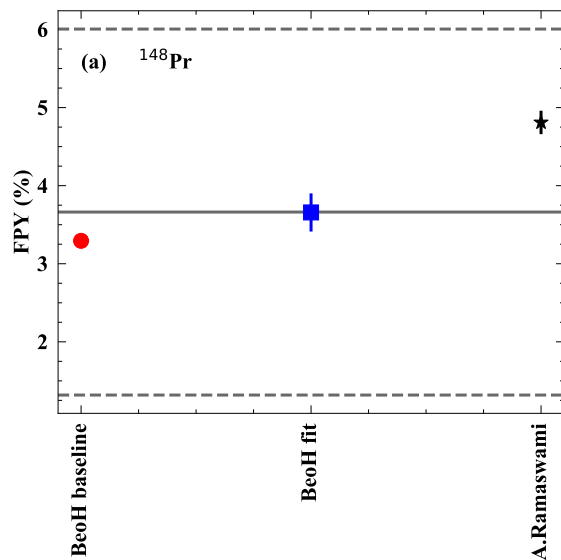
$$\chi^2/N = 6.16$$



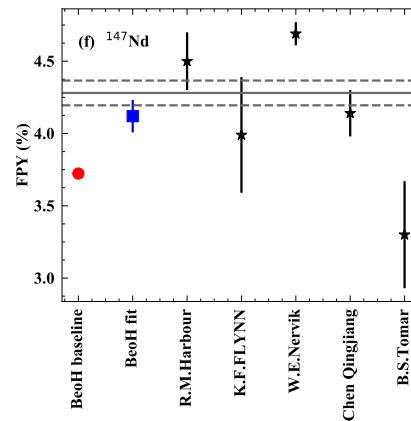
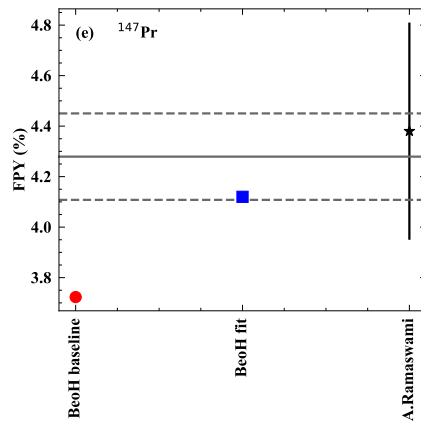
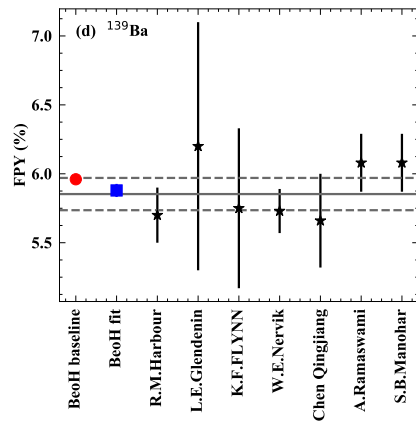
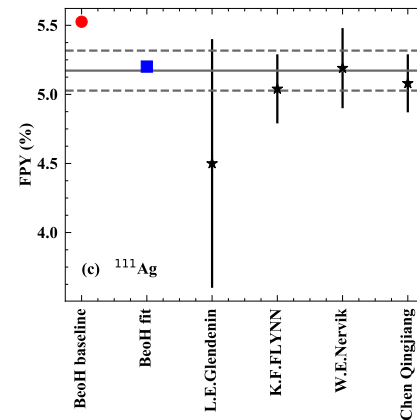
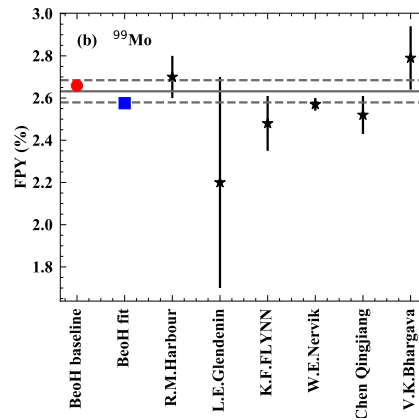
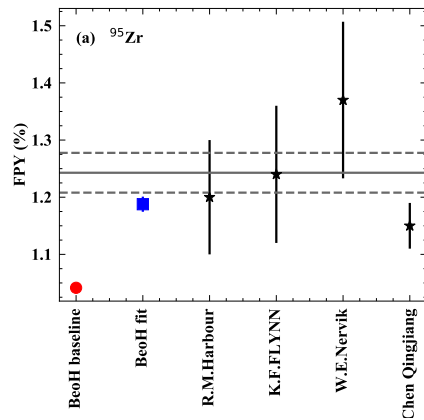
$$\chi^2/N = 11.82$$

The remainder of this talk focuses on fits to experimental data.

Large  $\chi^2$  values for  $^{252}\text{Cf}(\text{sf})$  are from a few FPYs (which agree well with ENDF/B-VIII.0 despite being fit to data)



# Overall, reasonable agreement between data, ENDF/B-VIII.0, and present work mean cumulative FPY values

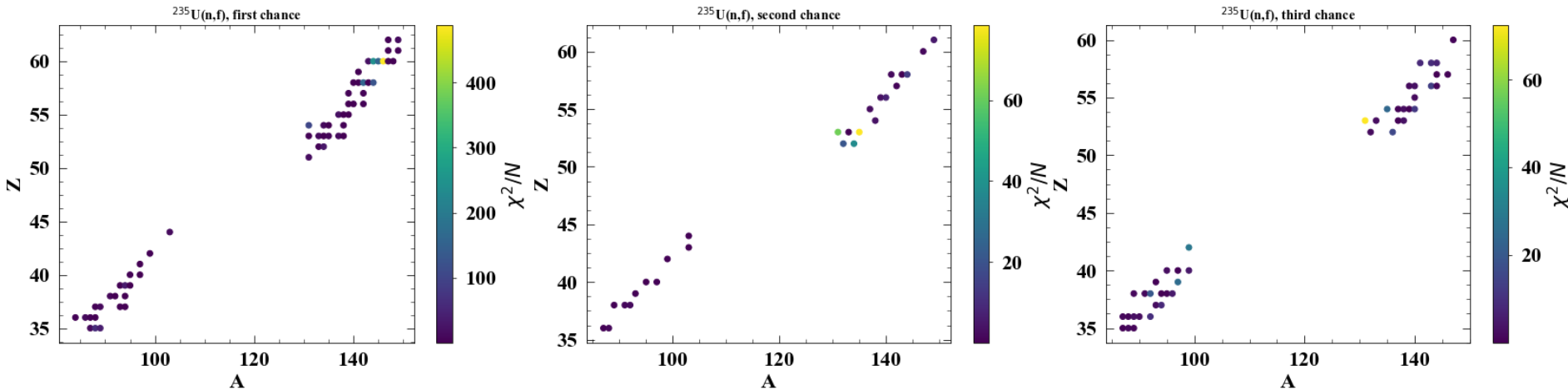


# A piecewise approach is used to fit neutron-induced fission reactions

- First-chance parameters fit then fixed, second-chance parameters fit then fixed, third-chance parameters fit then fixed.
- Excitation energy sharing parameters only fit in the first-chance energy region – then kept the same for the other compounds (initial optimizations are to  $\nu(A)$ , most of the data is below 6 MeV incident neutron energy).
- Fourth-chance fission generally only contributes on the order of a few percent up to 20 MeV and little data to no data are available in this region; parameters are taken from CGMF and held constant.
- This approach possibly raises some questions about how to calculate uncertainties and covariances consistently.



# $^{235}\text{U}(n,f)$ cumulative FPY data overview (taken from EXFOR, FPY>1%)

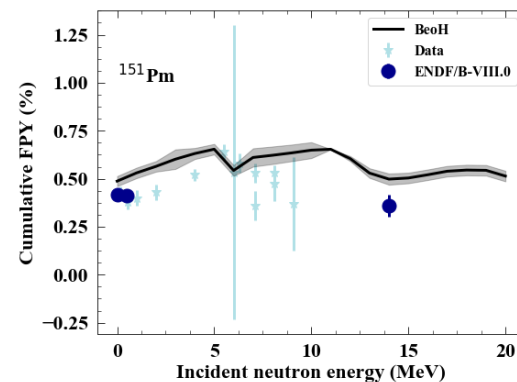
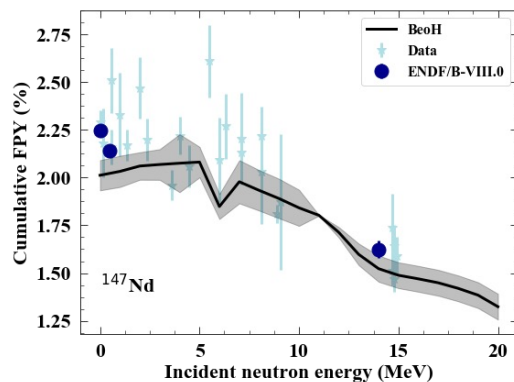
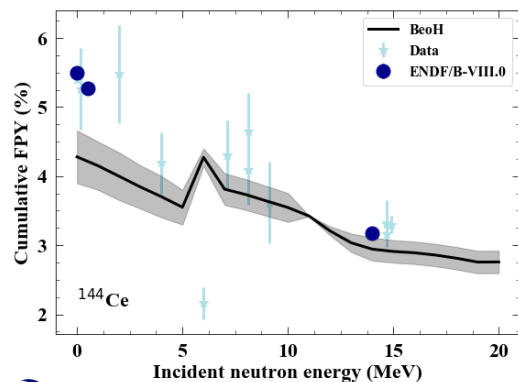
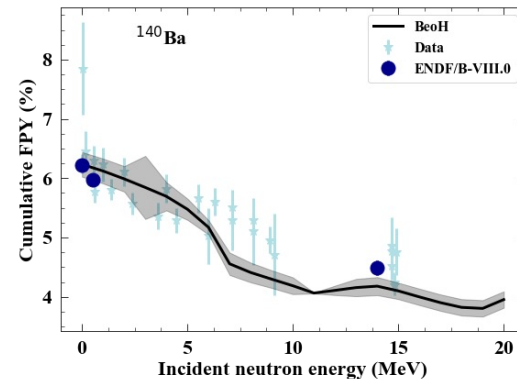
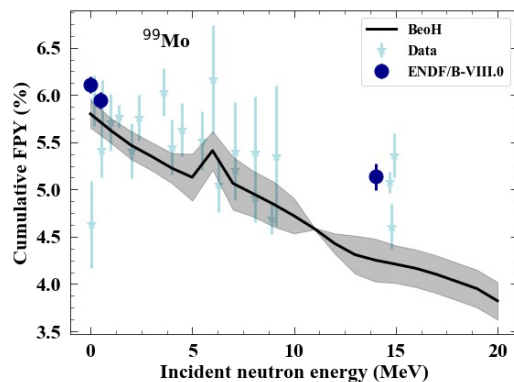
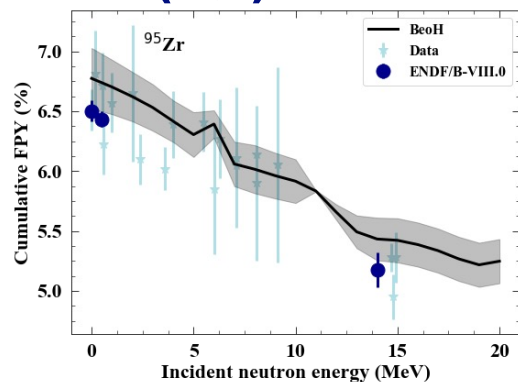


First chance  
 $\chi^2/N = 15.02$

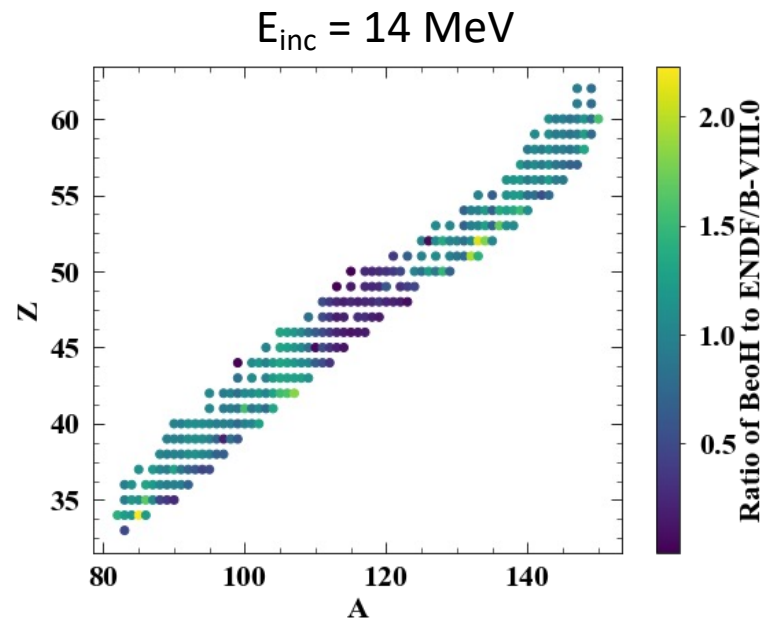
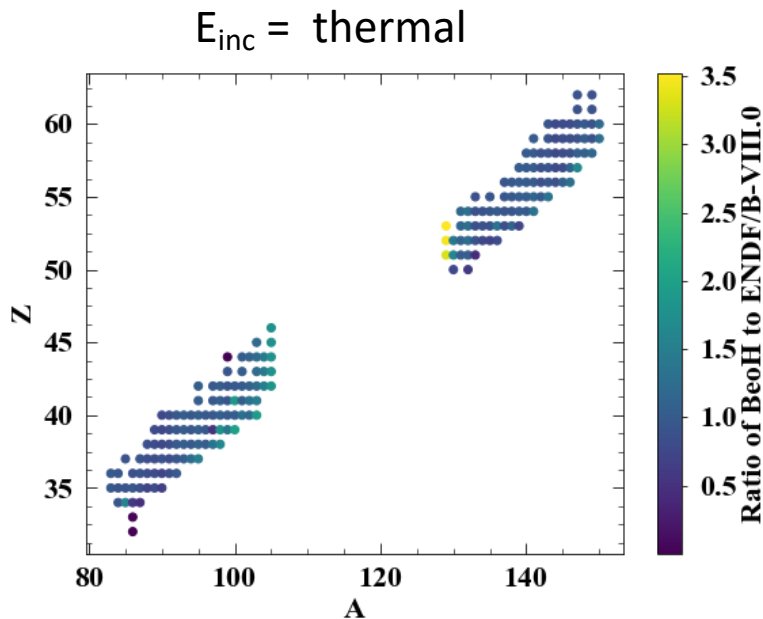
Second chance  
 $\chi^2/N = 7.00$

Third chance  
 $\chi^2/N = 7.83$

# Select cumulative FPYs up from thermal to 20 MeV for $^{235}\text{U}(n,f)$

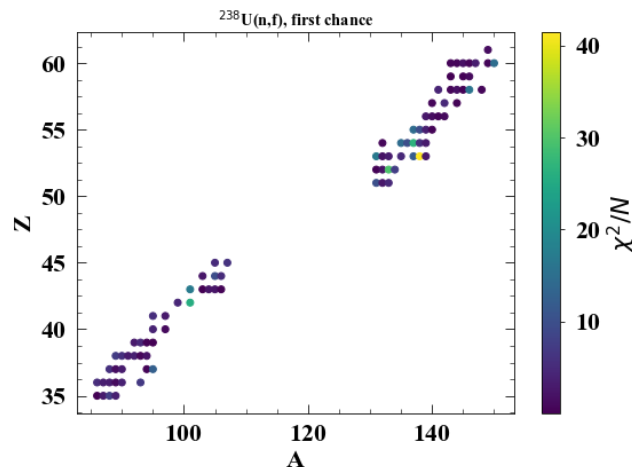


# Reasonable agreement with the current ENDF evaluation

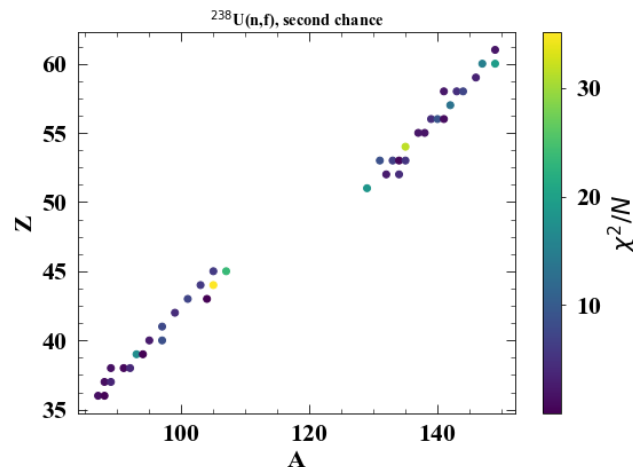


We only plot cumulative FPYs where the ENDF value is  $> 0.5\%$ .  
The discrepancy grows away from the peaks of the distribution.

# $^{238}\text{U}(n,f)$ cumulative FPY data overview (taken from EXFOR, FPY>1%)

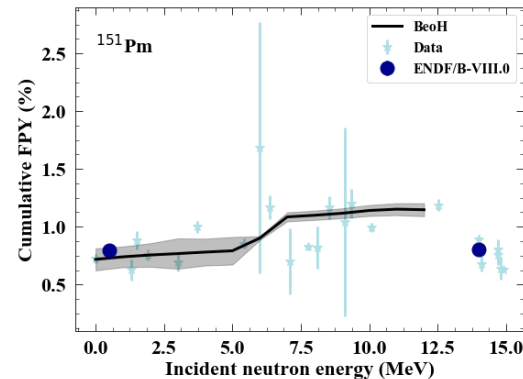
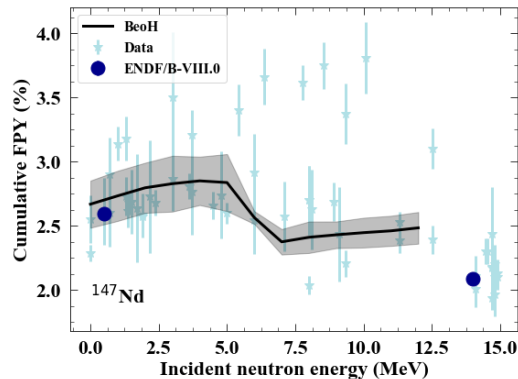
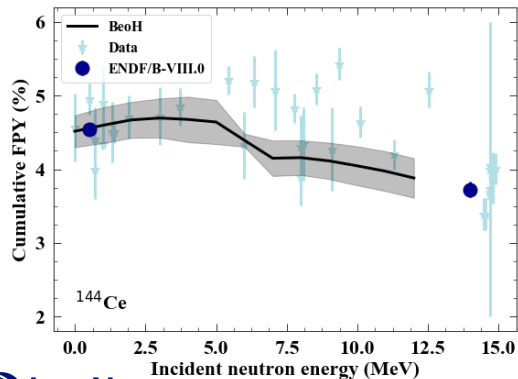
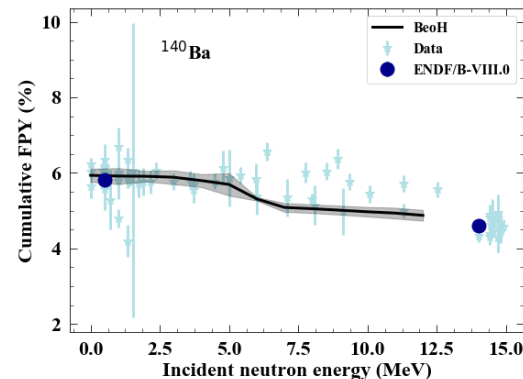
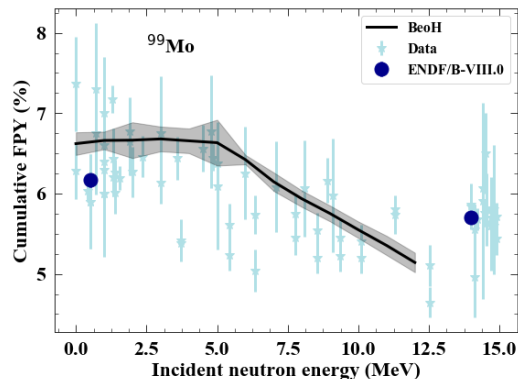
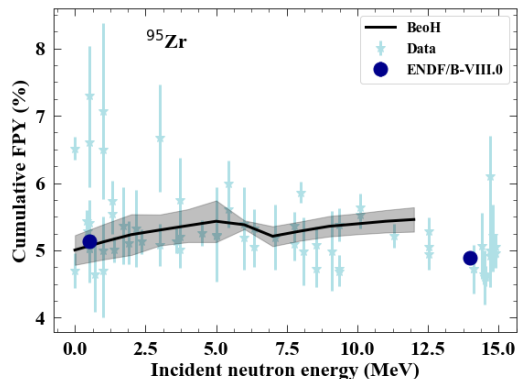


First chance  
 $\chi^2/N = 5.22$

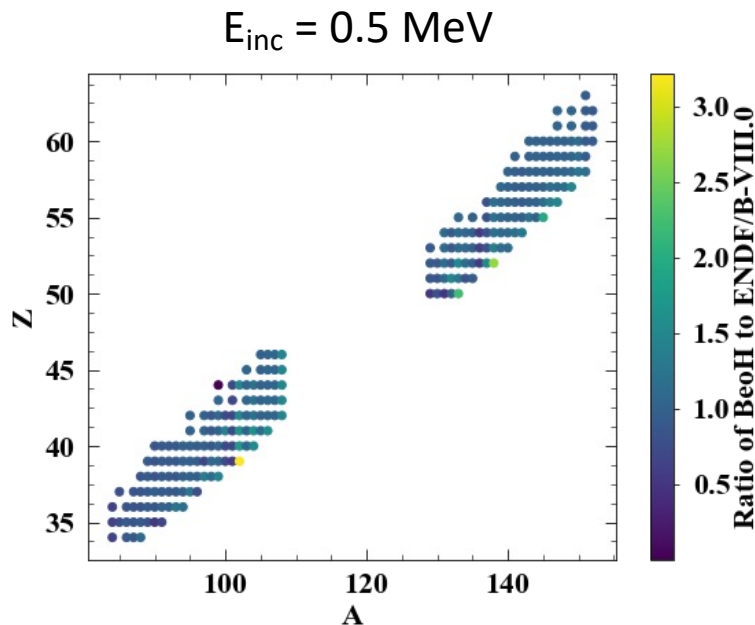


Second chance  
 $\chi^2/N = 7.05$

# Select cumulative FPYs up from thermal to 12 MeV for $^{238}\text{U}(n,f)$

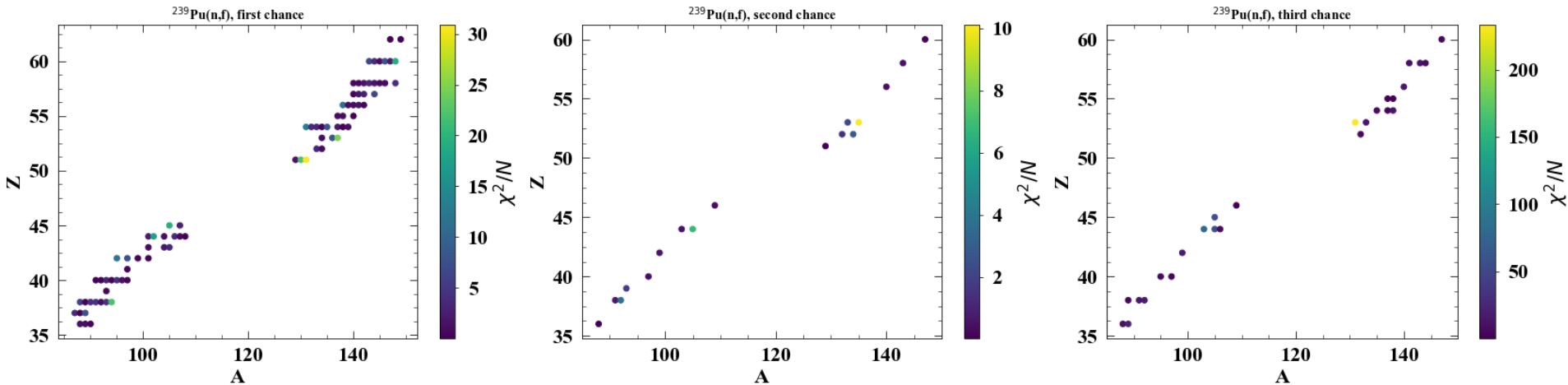


# Reasonable agreement with the current ENDF evaluation



We only plot cumulative FPYs where the ENDF value is  $> 0.5\%$ .  
The discrepancy grows away from the peaks of the distribution.

# $^{239}\text{Pu}(n,f)$ cumulative FPY data overview (taken from EXFOR, FPY>1%)

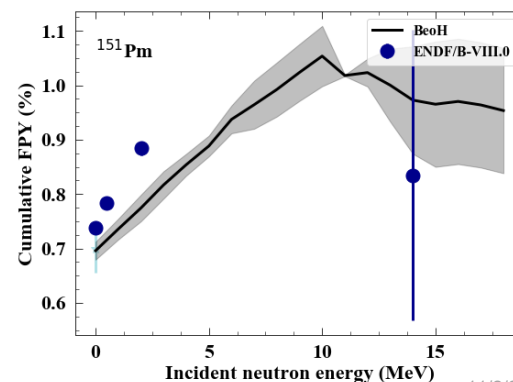
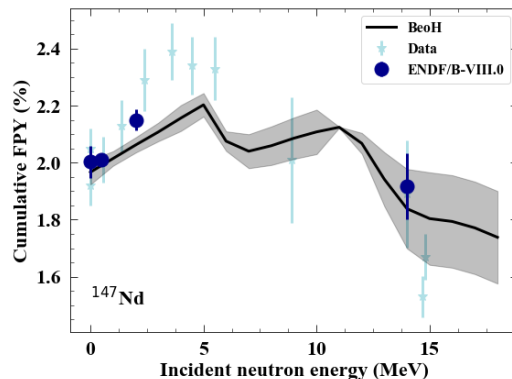
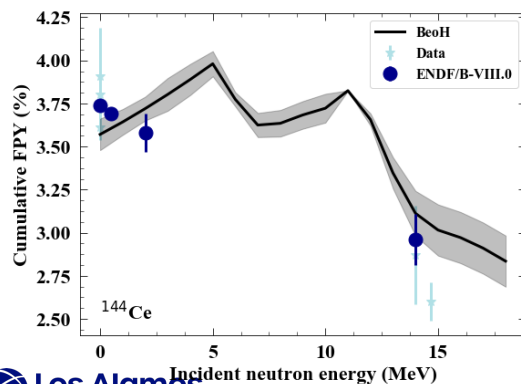
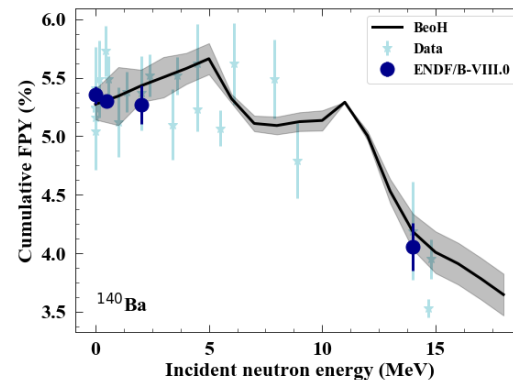
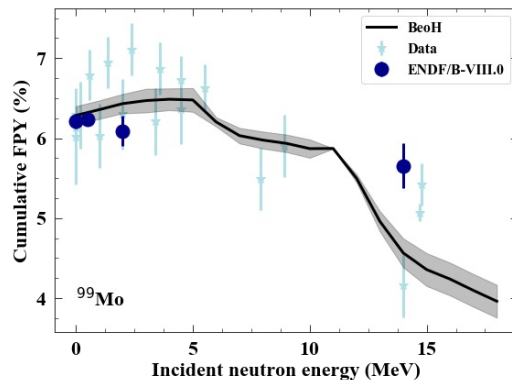
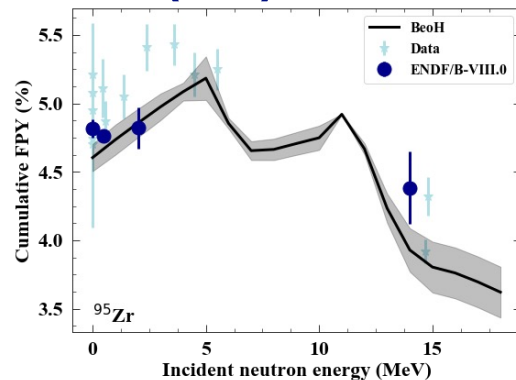


First chance  
 $\chi^2/N = 3.49$

Second chance  
 $\chi^2/N = 2.14$

Third chance  
 $\chi^2/N = 21.65$

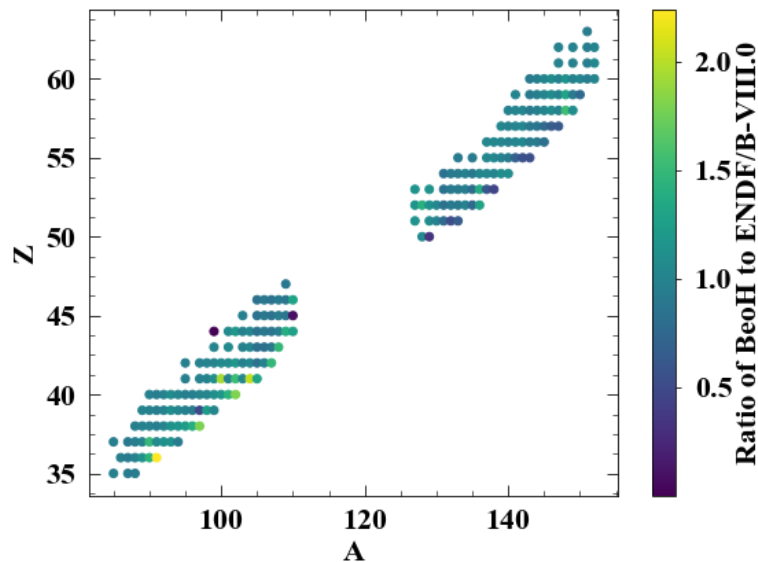
# Select cumulative FPYs up from thermal to 20 MeV for $^{239}\text{Pu}(n,f)$



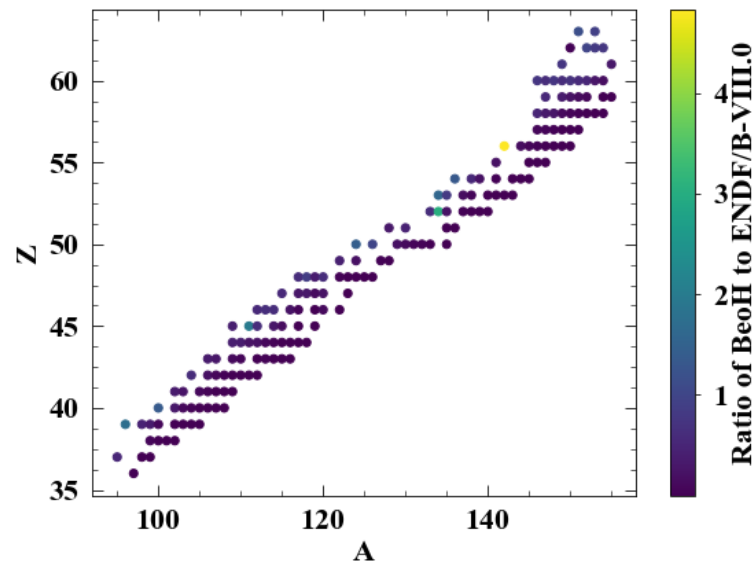


# Reasonable agreement with the current ENDF evaluation

$E_{\text{inc}} = \text{thermal}$

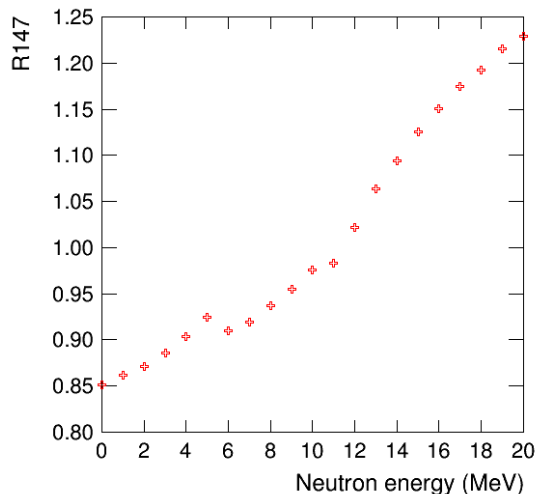


$E_{\text{inc}} = 14 \text{ MeV}$



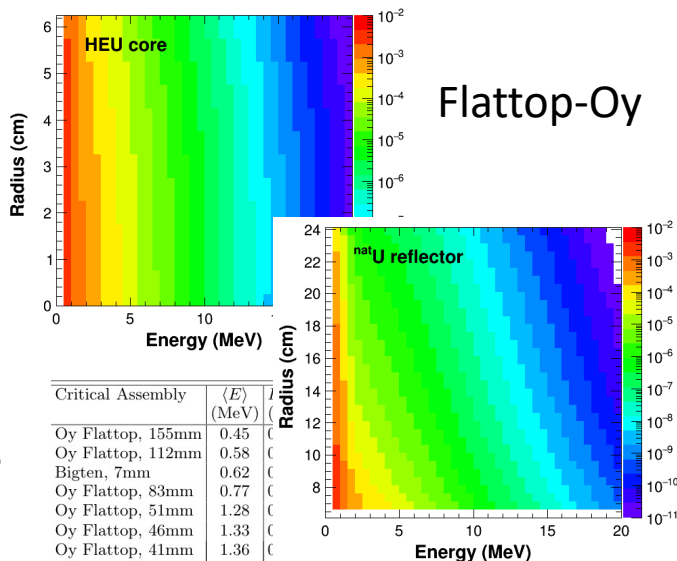
We only plot cumulative FPYs where the ENDF value is  $> 0.5\%$ .  
The discrepancy grows away from the peaks of the distribution.

# A process has been set up to validate select cumulative FPYs with critical assemblies



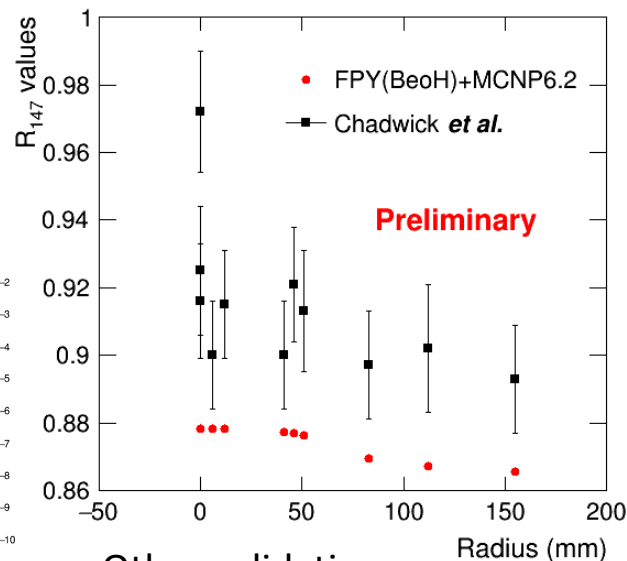
$$R_{147} = \frac{Y_{147}(\text{Pu})}{Y_{147}(\text{U}_{\text{th}})} \frac{Y_{99}(\text{U}_{\text{th}})}{Y_{99}(\text{Pu})}$$

Pu calcs from BeoH;  $\text{U}_{\text{th}}$  from ENDF



Critical Assembly	$\langle E \rangle$ (MeV)	$\langle R \rangle$ (cm)	$\langle R \rangle$ (cm)
Oy Flattop, 155mm	0.45	0.916 ± 0.8%	0.916 ± 0.8%
Oy Flattop, 112mm	0.58	0.927 ± 2.7%	0.927 ± 2.7%
Bigten, 7mm	0.62	0.927 ± 2.7%	0.927 ± 2.7%
Oy Flattop, 83mm	0.77	0.927 ± 2.7%	0.927 ± 2.7%
Oy Flattop, 51mm	1.28	0.927 ± 2.7%	0.927 ± 2.7%
Oy Flattop, 46mm	1.33	0.927 ± 2.7%	0.927 ± 2.7%
Oy Flattop, 41mm	1.36	0.927 ± 2.7%	0.927 ± 2.7%
Oy Flattop, 12mm	1.44	0.927 ± 2.7%	0.927 ± 2.7%
Oy Flattop, 6mm	1.44	0.927 ± 2.7%	0.927 ± 2.7%
Oy Flattop, center	1.44	0.968 ± 3.3%	0.972 ± 1.89%
Oy Flattop, center	1.44	0.929 ± 2.7%	0.925 ± 2.04%
Oy Flattop, center	1.44	0.899 ± 2.7%	0.916 ± 1.88%
Pu Flattop, center	1.68	0.895 ± 2.7%	0.912 ± 2.70%
Pu Flattop, center	1.68	0.927 ± 2.7%	0.944 ± 1.78%
Pu Flattop, center	1.68	—	0.928 ± 1.77%
Pu Jezebel, center	1.88	0.927 ± 3.3%	0.934 ± 2.32%
Average $R$ -value			0.916 ± 0.8%

Flattop-Oy



Other validation:  
Remaining critical assemblies  
SOFIA integrated results  
Dosimetry

M.B. Chadwick, et al., NDS 111, 2923 (2010)

# Covariance format is up for discussion (2 main options)

- Create an MF 38 format (like MF 35) for covariances; move FPY uncertainties out of MF 8 into MF 38 only
  - Pros: consistent with other covariance files, could essentially use the format for MF 35 (little to no new development)
  - Cons: applications that use the current format will have to update to take uncertainties from a new file
- Extend the MF 8 format to include correlations as well as uncertainties
  - Pros: applications can keep their current way of reading uncertainties
  - Cons: new format will have to be developed
- Cross correlations between incident energies would not be included

# Conclusions and path forward

- Independent and cumulative FPYs are being re-evaluated, with covariances, for  $^{252}\text{Cf(sf)}$ ,  $^{235,238}\text{U(n,f)}$ , and  $^{239}\text{Pu(n,f)}$
- Third-chance calculations for  $^{238}\text{U(n,f)}$  are being finished
- Tweaking of BeoH Y(A) shape underway to account for stiffness in the model that currently doesn't consistently calculate important FPYs
- More work on the database and uncertainties:
  - Updated FPY values from BNL
  - Updated decay data from BNL
  - Comparing database from England and Rider evaluation with current fitted data
  - Template of expected experimental uncertainties
  - Calculating R values of critical assemblies