

ECCE
kinematic reco, Sivers, Collins and
unpol TMD studies

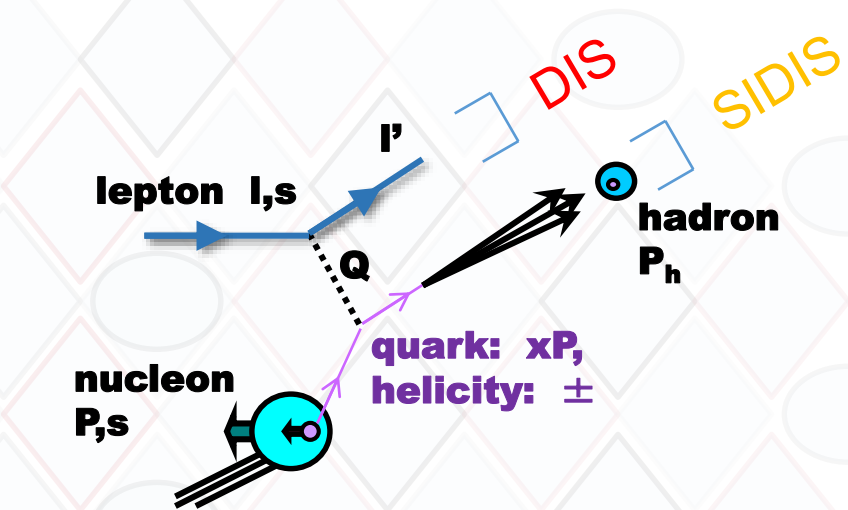
**Project detector SIDIS
meeting**

April 27, 2022

Ralf Seidl (RIKEN)

Exp. Physics analysis strategy

- For any (SI)DIS analysis:
 1. Find **DIS** kinematics: easiest case via scattered lepton l' (other methods include hadronic final state)
 2. Calculate **DIS** variables: x, y, Q^2, W^2, ϕ_S (around virtual photon in proton rest frame, wrt to scattering plane)
 3. Select DIS events (typically $Q^2 > 1 \text{ GeV}^2, W^2 > 10 \text{ GeV}^2, 0.01 < y < 0.95$)
 4. Search for final state hadrons \rightarrow **SIDIS**
 5. Calculate **SIDIS** variables: z, P_{hT} (wrt to virtual photon in proton rest frame), ϕ_h (around virtual photon in proton rest frame, wrt to scattering plane)



$$q = l - l' \quad \text{Momentum transfer}$$

$$Q^2 = -q^\mu q_\mu$$

$$x = \frac{Q^2}{2p \cdot q} \quad \text{Parton momentum fraction*}$$

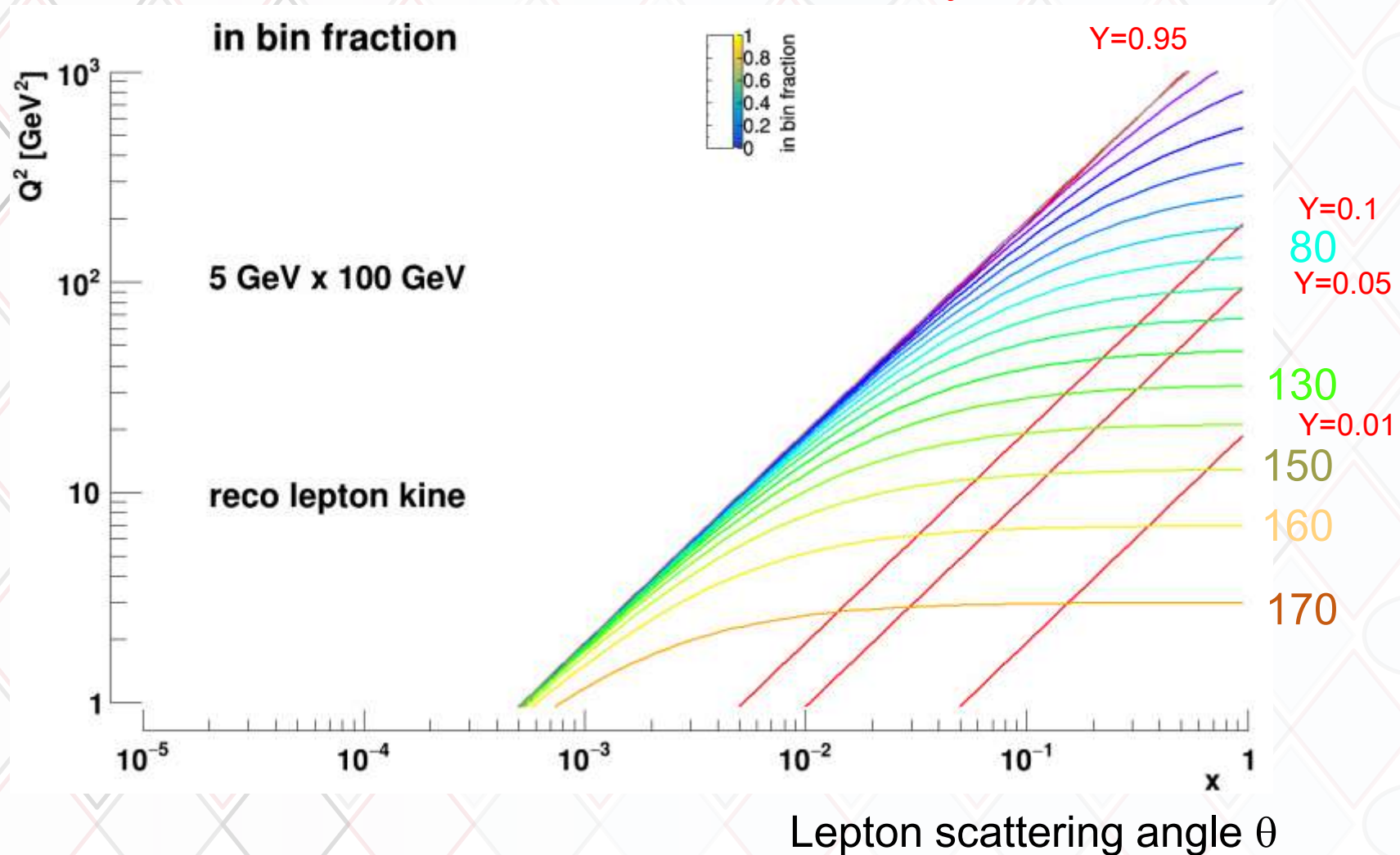
$$y = \frac{q \cdot p}{l \cdot p} \quad \text{Inelasticity}$$

$$W^2 = M_p^2 + (1 - x)Q^2/x \quad \text{Mass of had final state}$$

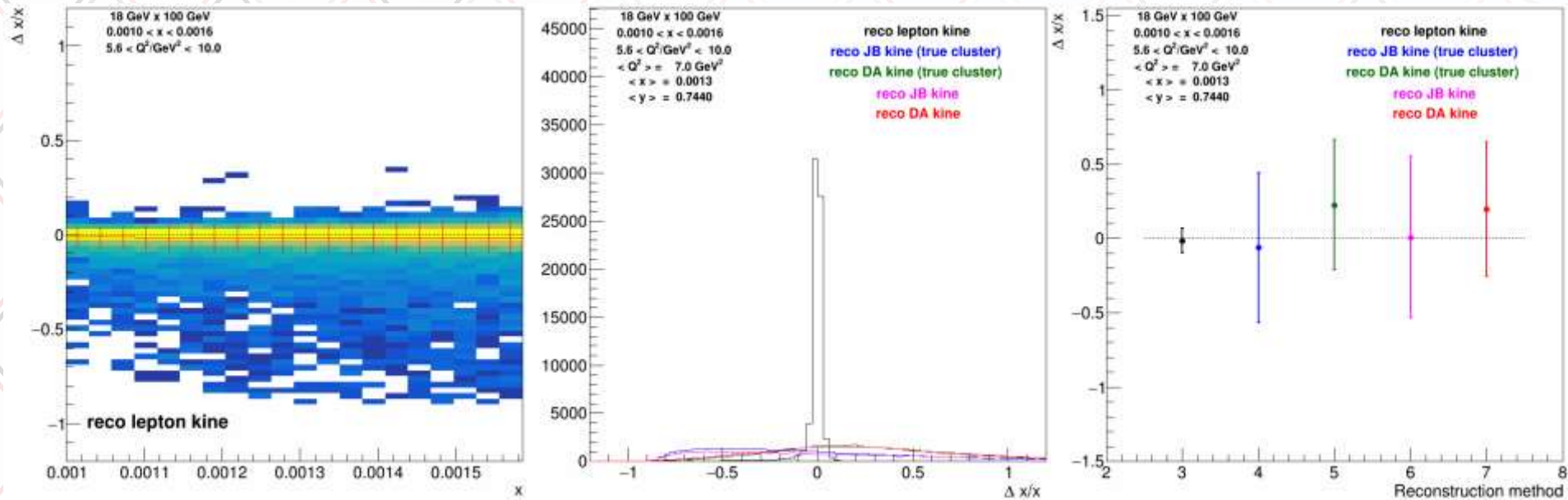
$$z = \frac{p \cdot P_h}{p \cdot q} \quad \text{SIDIS hadron momentum fraction}$$

DIS kinematic regions

Inelasticity
 $y = 1 - E'/E \sin^2 \theta/2$

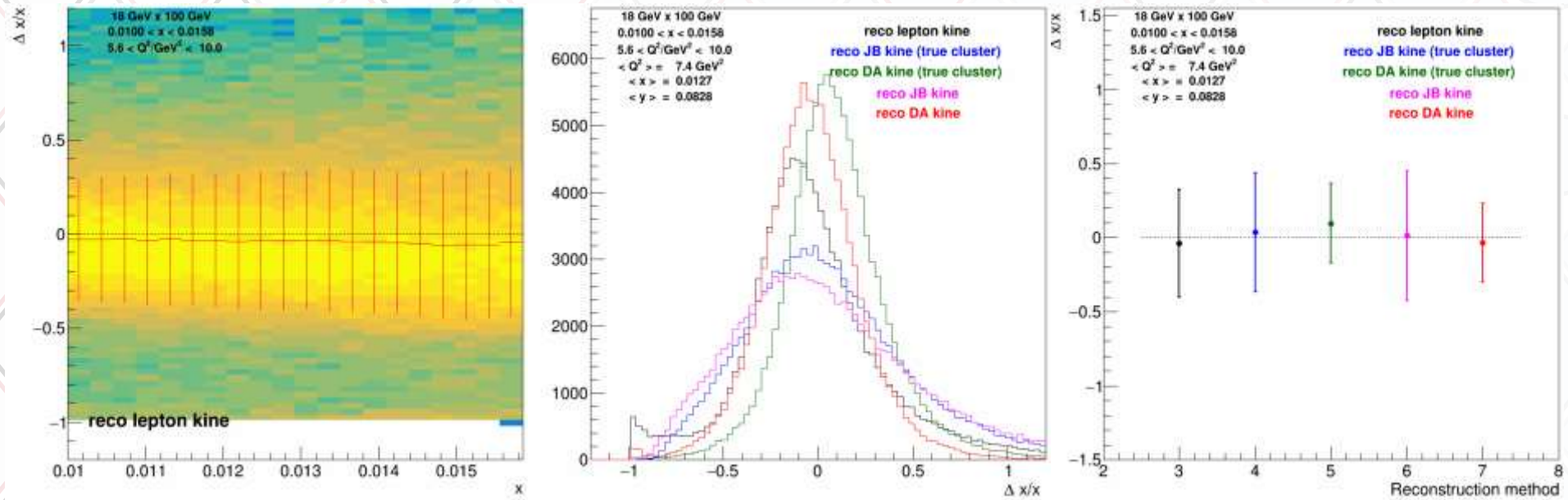


Kinematic reco example plots (x, high y)



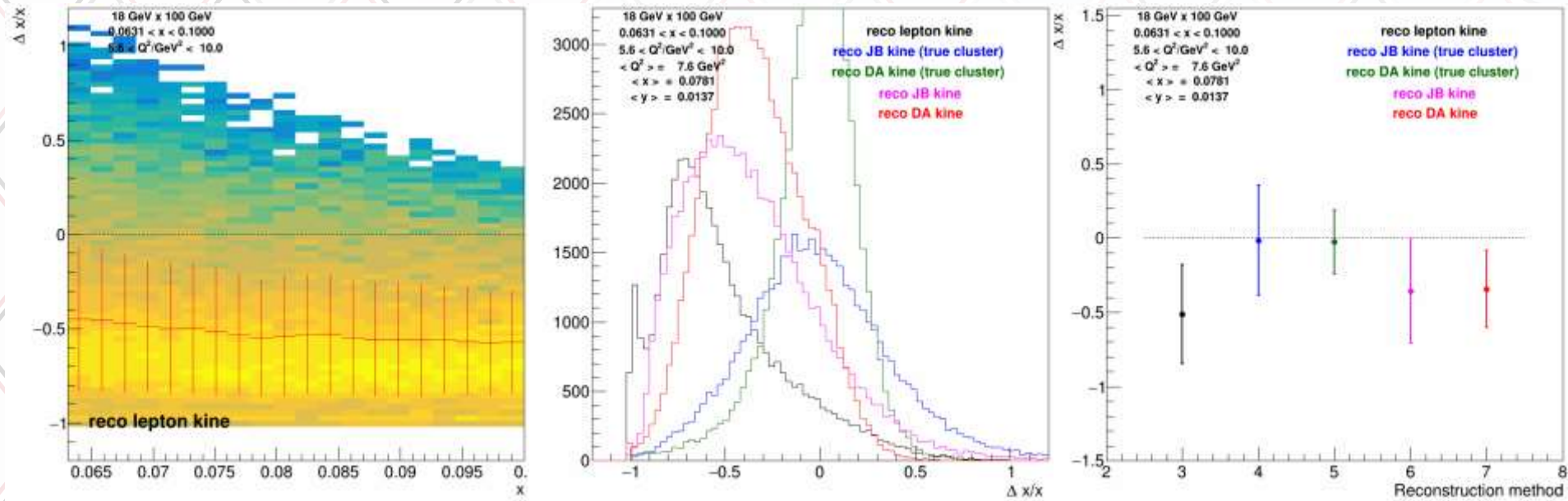
1. $(var_{reco} - var_{true} / var_{true})$ distributions as a function of variable/x/z in one x-Q2 bin
2. $(var_{reco} - var_{true} / var_{true})$ distribution in one x-Q2 bin
3. Mean and width for various reconstruction methods

Kinematic reco example plots (x, med y)



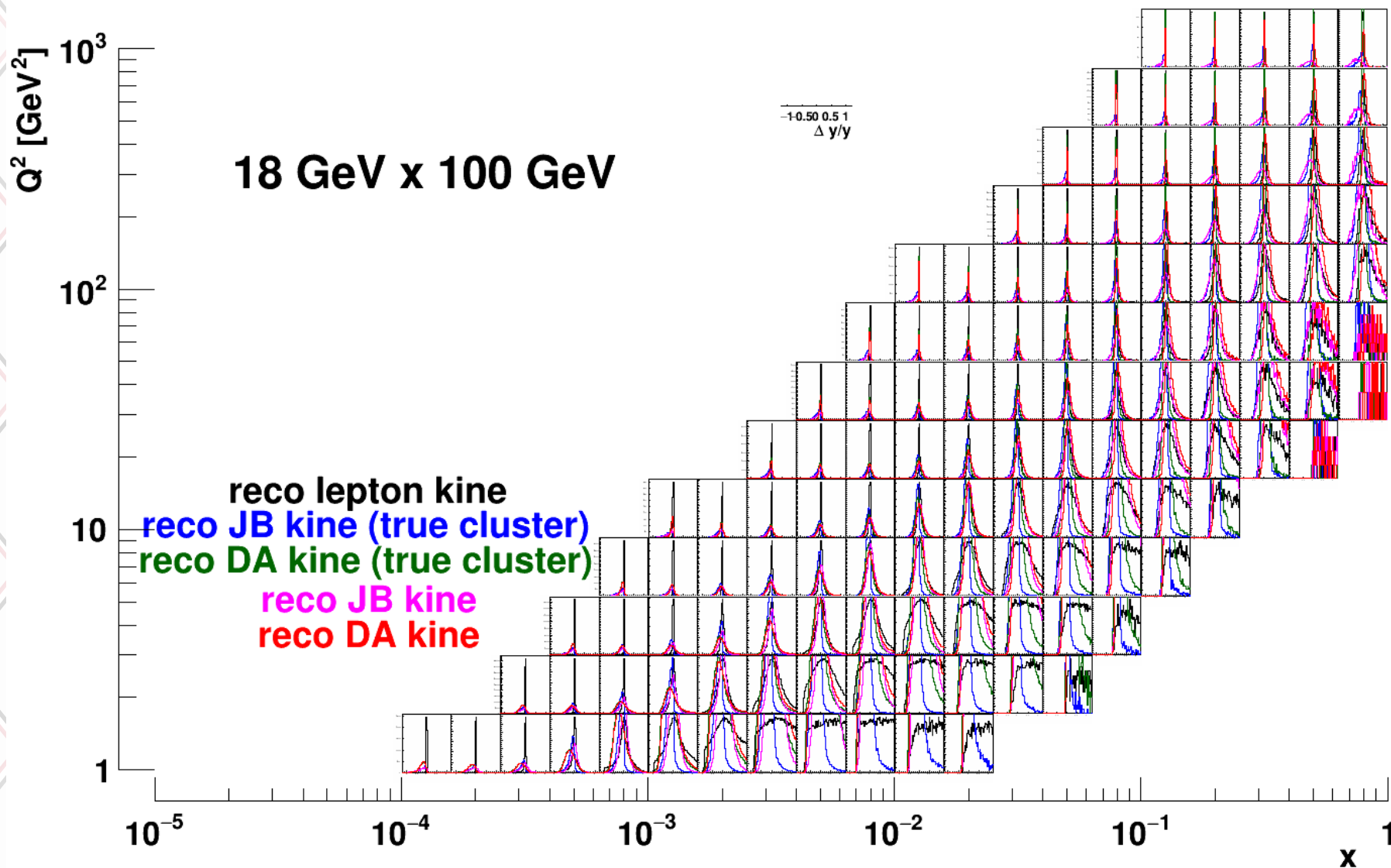
- At medium y all resolutions similar,

Kinematic reco example plots (x, low y)

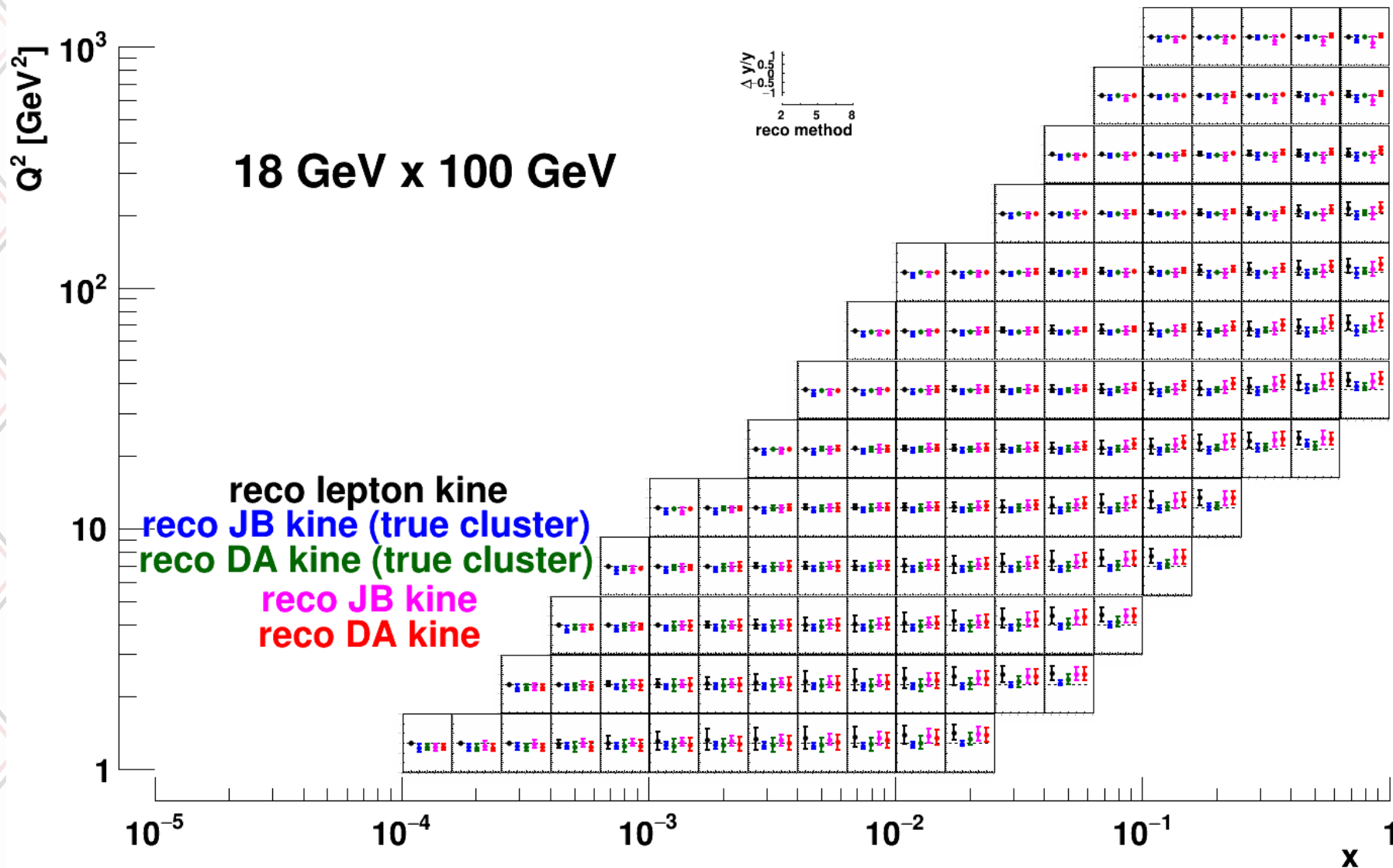


- Low y , lepton shifted and wide, hadronic methods better

Accumulated resolutions

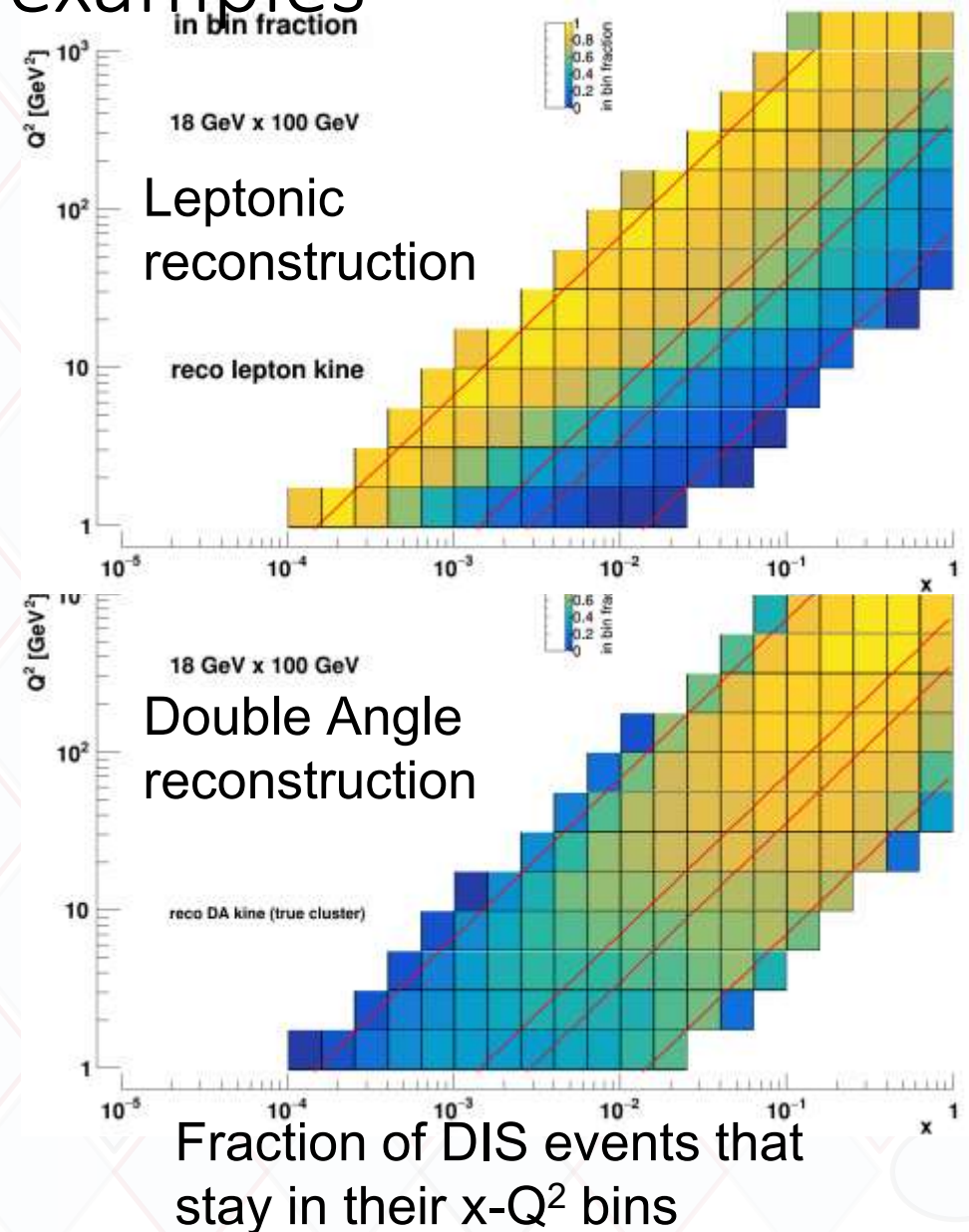


All γ resolution widths and means



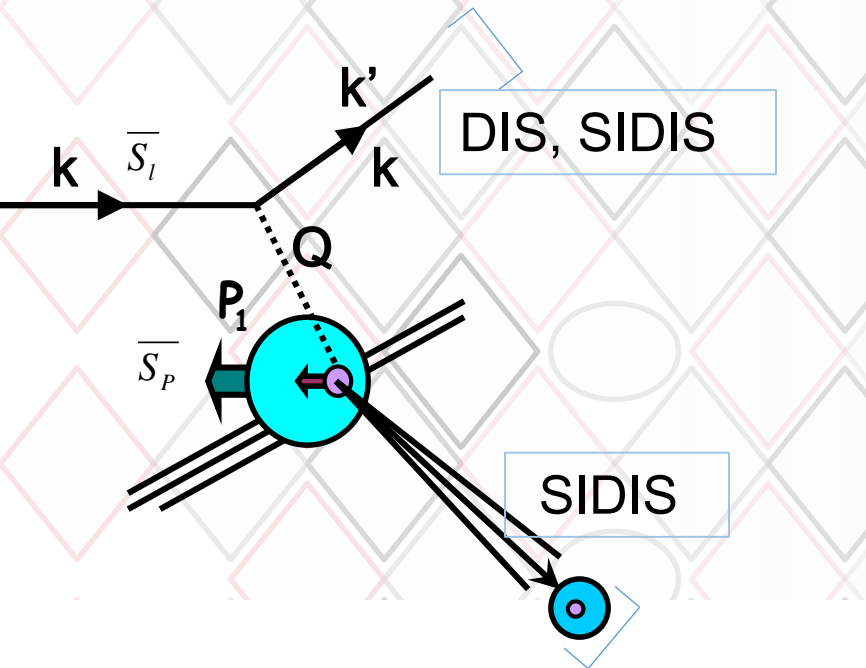
DIS kinematic reconstruction examples

- Full Pythia6+GEANT simulations of the ECCE detector used for various (SI)DIS kinematic resolutions and for various reconstruction methods (lepton, Jaquet-Blondel, Double Angle, etc)
- x and y resolutions suffer from lepton method at lower y, partially recoverable in double angle method (hybrid of scattered lepton + hadronic final state)



SIDIS Kinematics

Detect also final-state hadron(s) and make use of flavor, etc. sensitivity of Fragmentation functions

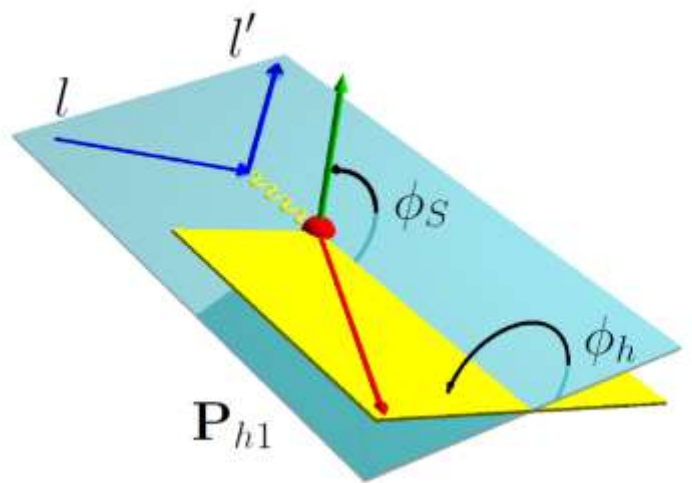


z: Fractional hadron momentum wrt to parton momentum ($0 < z < 1$)

P_{hT} : transverse hadron momentum wrt to virtual photon (convolution over intrinsic transverse momenta of PDFs and FFs)

ϕ_S : Azimuthal angle of nucleon (transverse) spin wrt to scattering plane, along virtual photon axis

ϕ_h : Azimuthal angle of hadron wrt to scattering plane, along virtual photon axis



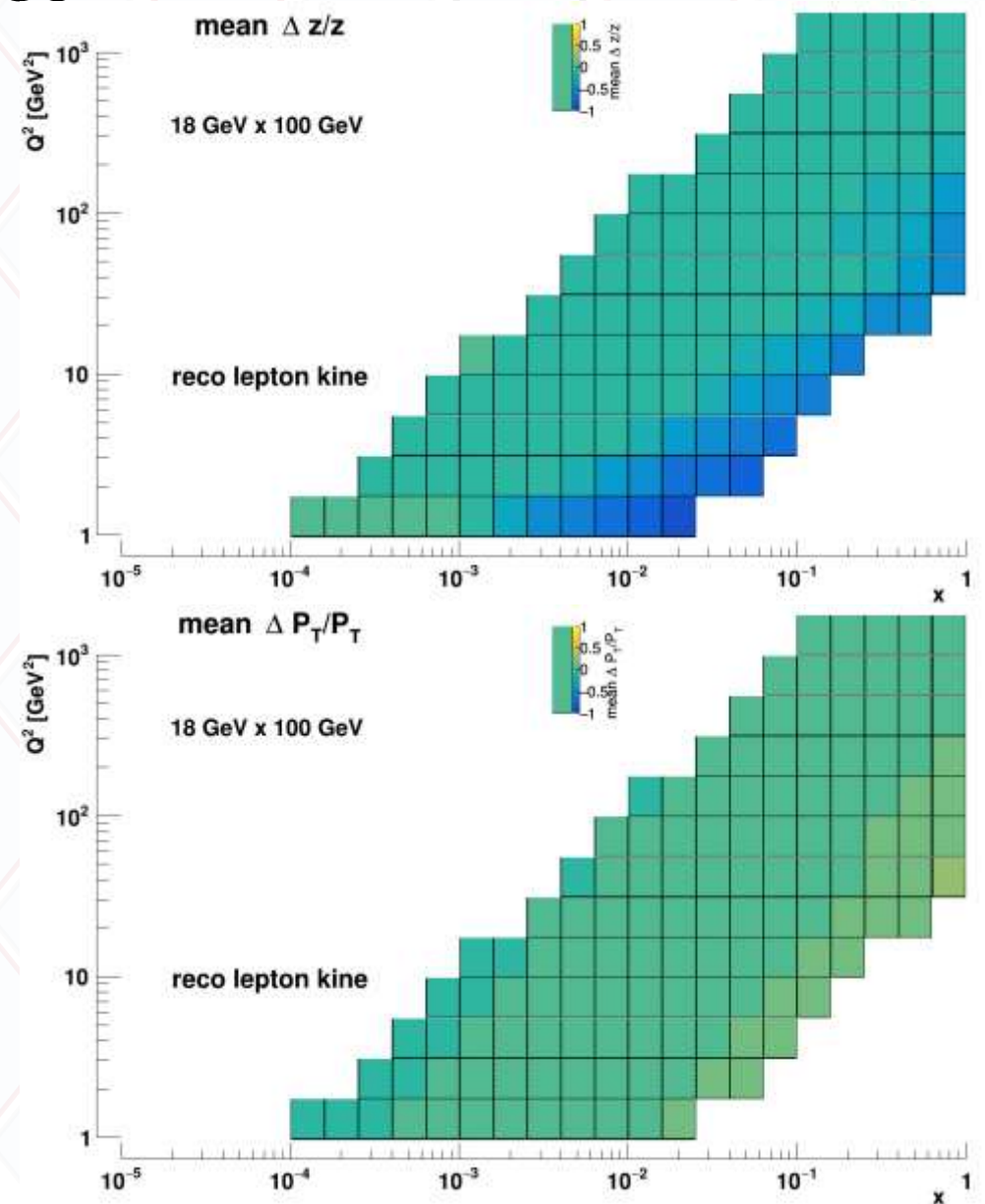
$$\frac{d^6\sigma}{dx dQ^2 dz dP_{hT} d\phi_S d\phi_h} \propto \sum_{q, \bar{q}}^{LO} e_q^2 q(x, Q^2, k_t) \otimes D_{1,q}^h(z, Q^2, p_t)$$

- Transverse momentum and angles rely also on correct boost to hadron rest system
- Current fragmentation: related to struck quark
- Target fragmentation: related to nucleon remnant

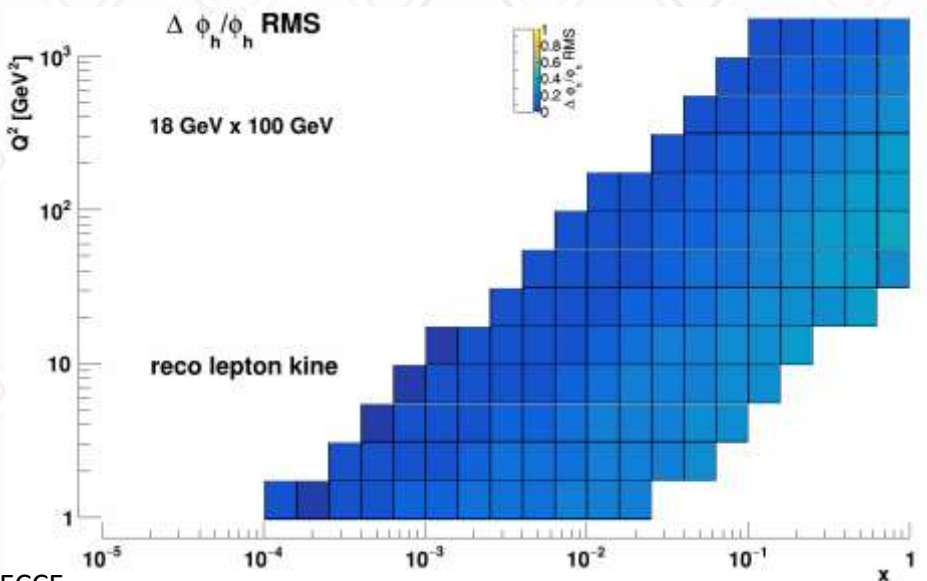
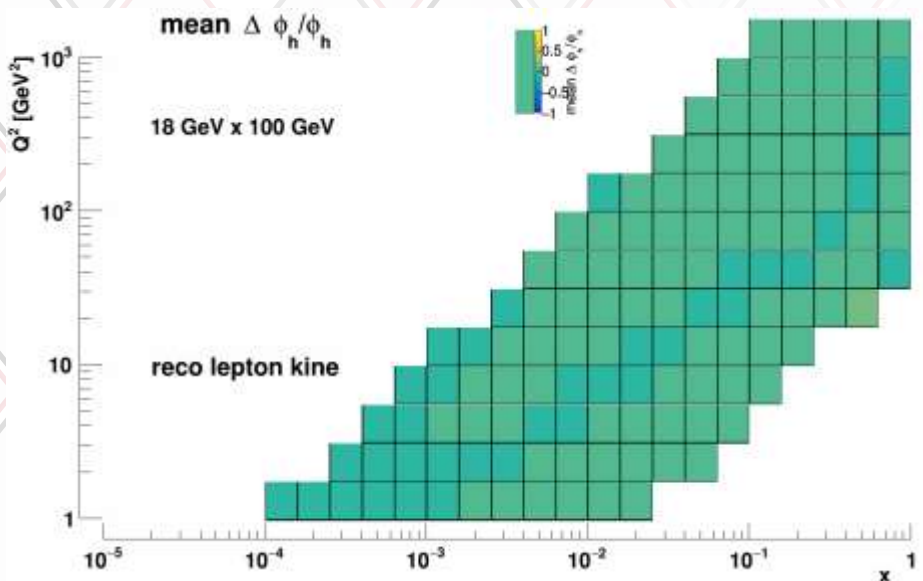
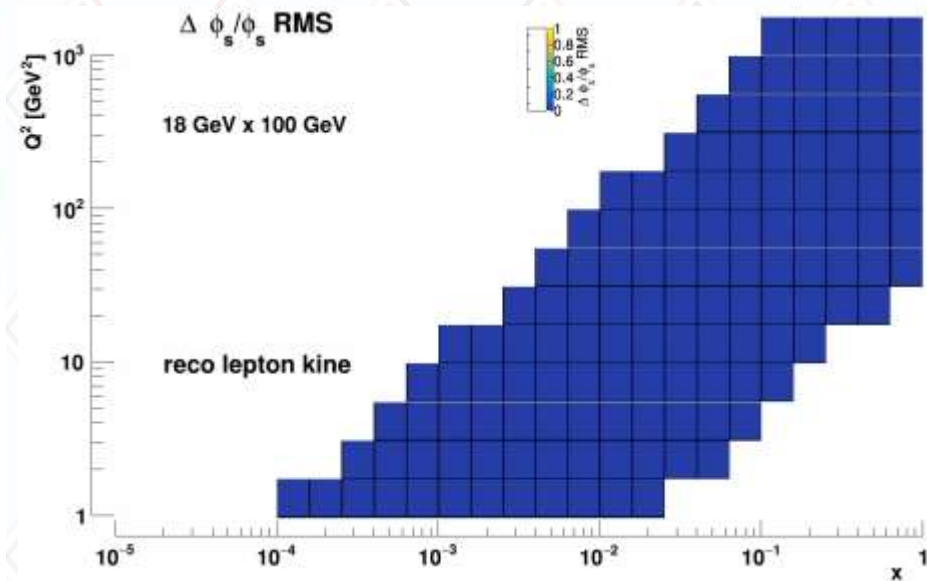
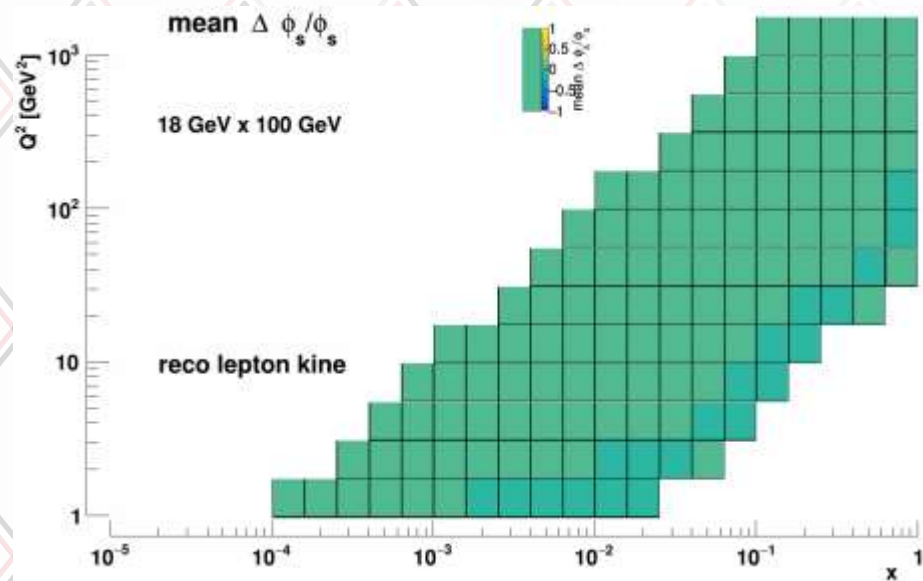


Example of resolutions studies

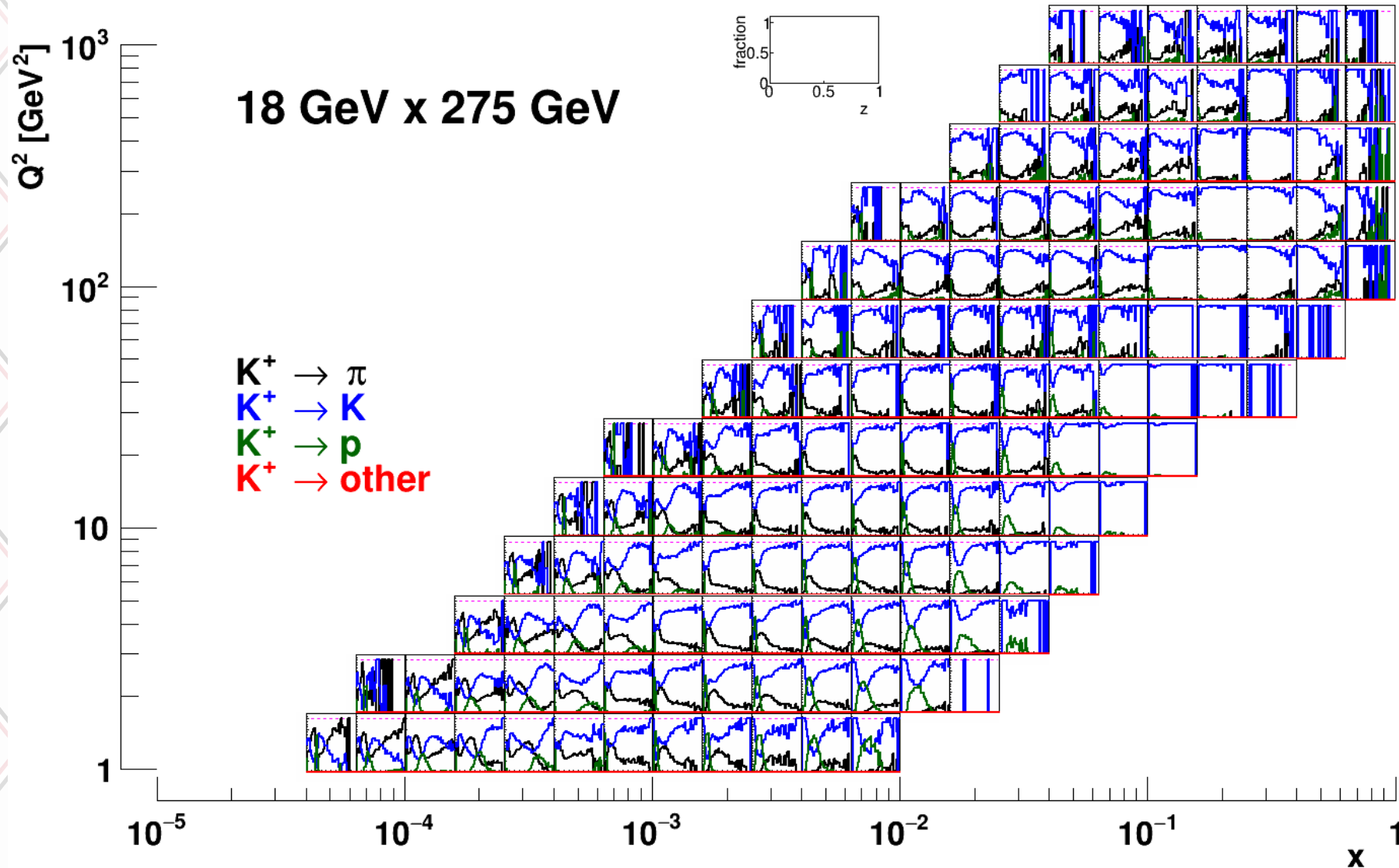
- Full Pythia6+GEANT simulations of the ECCE detector for various (SI)DIS kinematic resolution and reconstruction methods:
 - z resolution suffers in lepton method at lower y, partially recoverable in double angle method
 - p_T and azimuthal angles ϕ_h , ϕ_S very robust



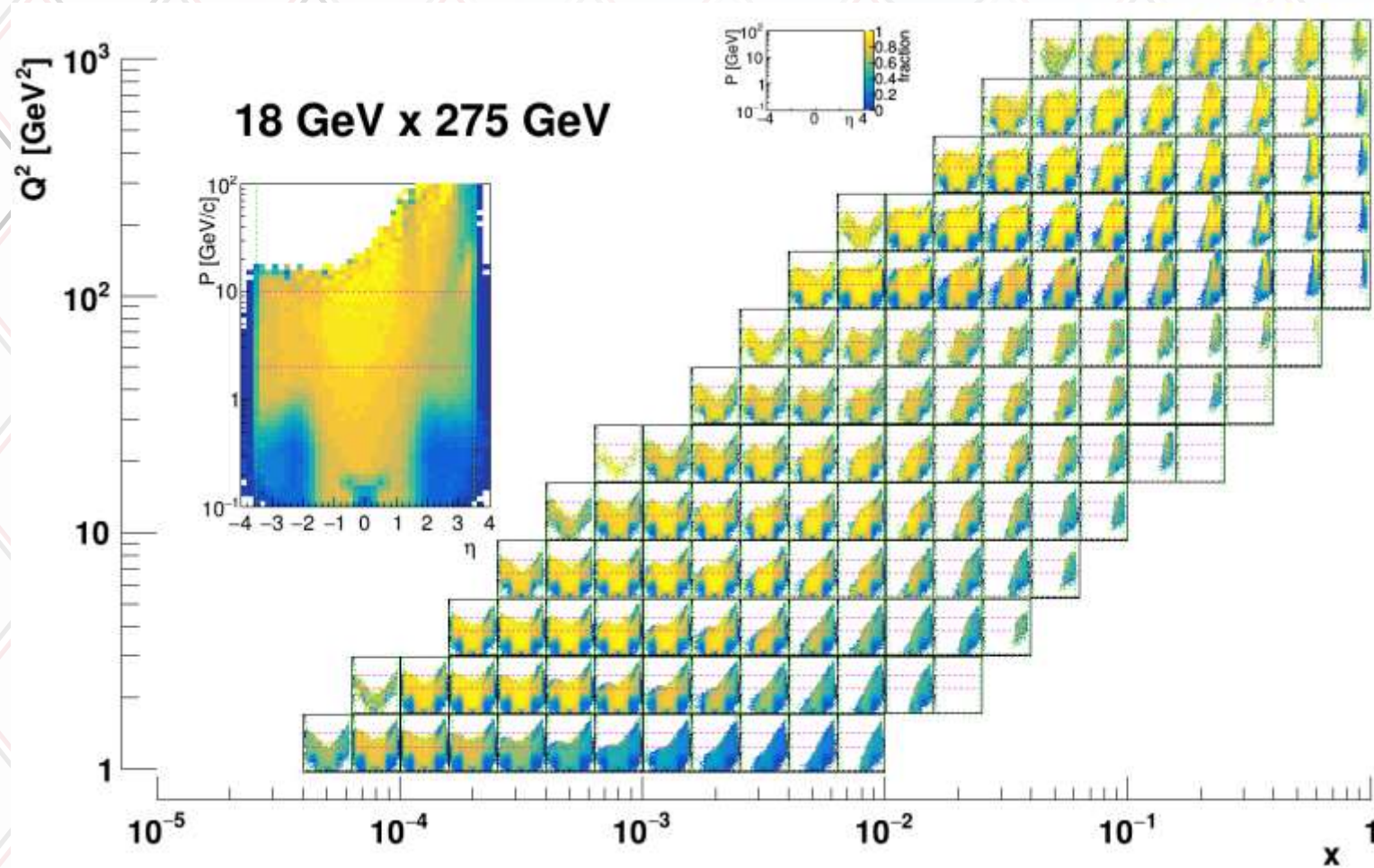
Azimuthal angles



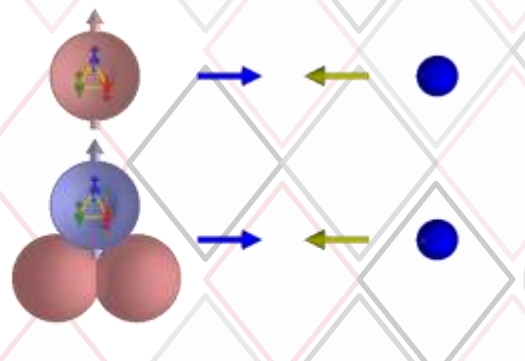
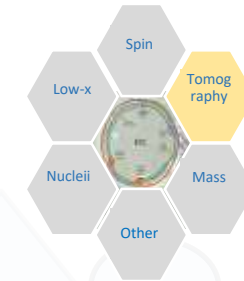
PID efficiencies (fast PID based on dRICH, DIRC, and mRICH)



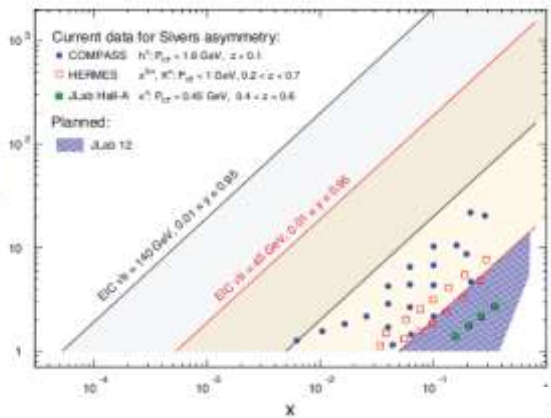
Hadron acceptance



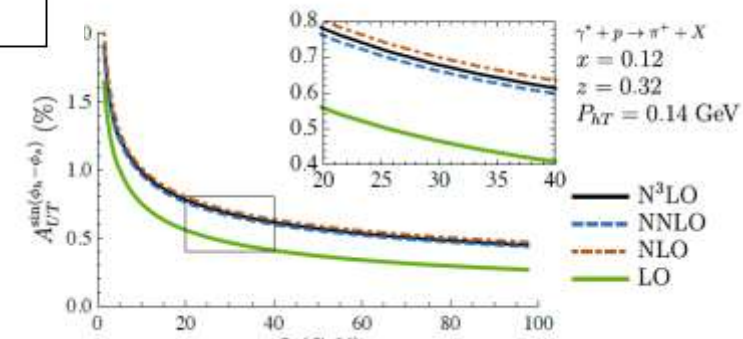
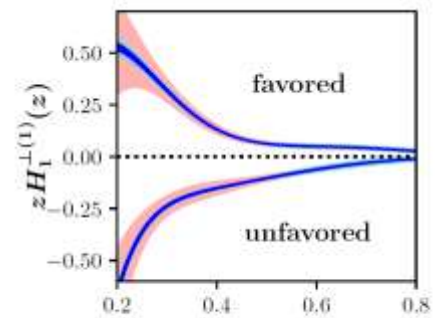
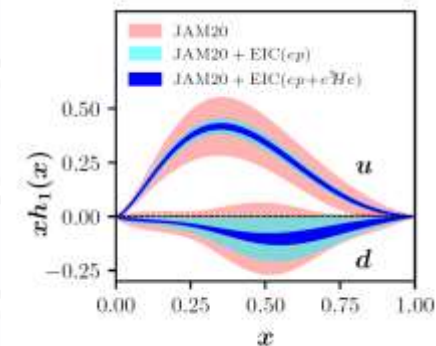
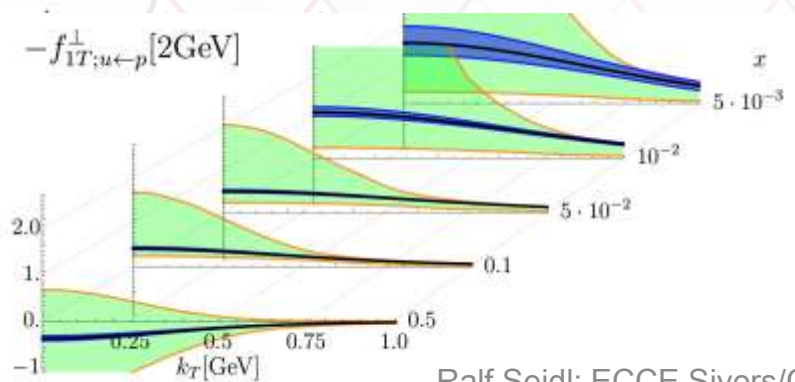
Motivation: 3D Transverse spin and momentum structure



Deliverables	Observables	What we learn	Stage I	Stage II
Sivers & unpolarized TMD quarks and gluon	SIDIS with Transverse polarization; di-hadron (di-jet)	Quantum Interference & Spin-Orbital correlations	3D Imaging of quarks valence+sea	3D Imaging of quarks & gluon; $Q^2 (P_{hT})$ range QCD dynamics
Chiral-odd functions: Transversity; Boer-Mulders	SIDIS with Transverse polarization	3 rd basic quark PDF; novel hadronization effects	valence+sea quarks	$Q^2 (P_{hT})$ range for detailed QCD dynamics

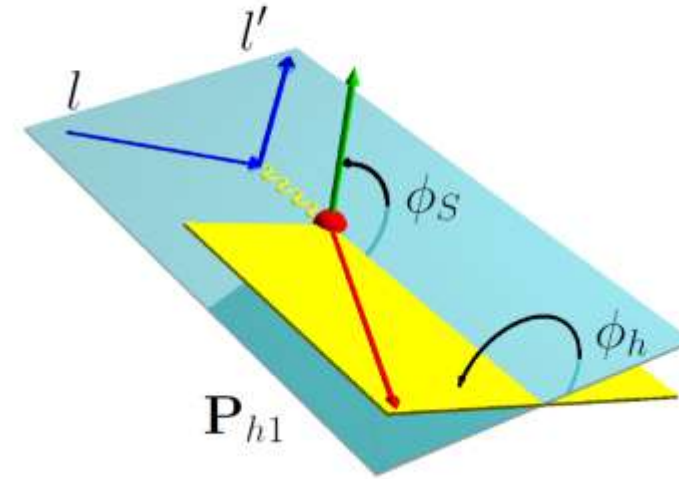


From EIC Yellow Report:



Motivation

- Unpolarized TMD distribution and Fragmentation functions are the baseline for all polarized TMD measurements
- Relevant even to heavy boson production (H, W, Z) at LHC
- Also relevant to low-x physics
- Scale dependence in TMD regime still poorly known (as TMD evolution contains non-perturbative parts)
- Understanding the regions of applicability between TMD, collinear frameworks and target fragmentation, etc



- SIDIS sensitive to convolution of intrinsic transverse momenta from PDF and FF
- Unlike jets (PDF only), detected SIDIS pions/kaons/etc provide flavor sensitivity

ECCE simulation setup and binning

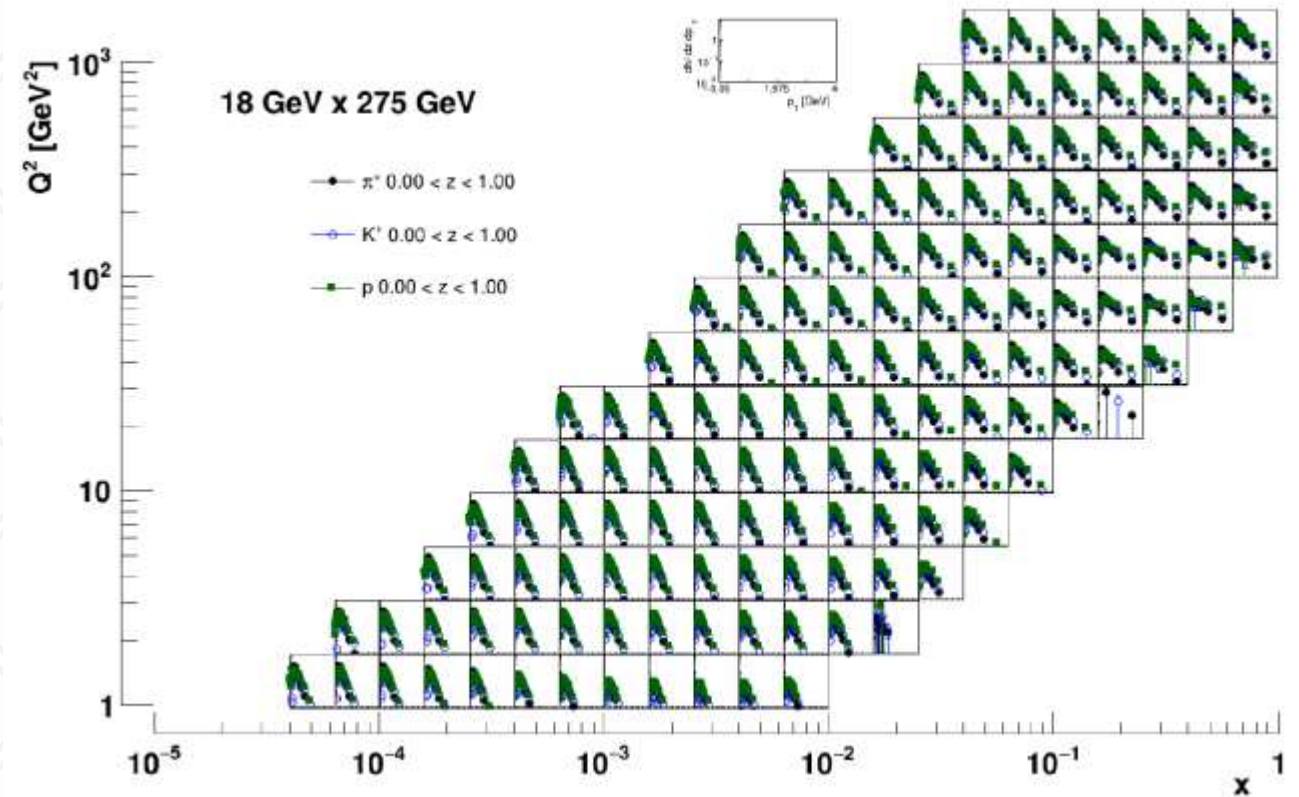
- pythiaRHIC (Pythia 6) simulations for e+p collisions at 4 energies similar to YR
- Generator output simulated through GEANT4 (prop4)
- Analyzed via slightly modified EventEvaluator TTrees
- Scattered lepton ($|\eta| < 3.5$) DIS kinematic reconstruction using reco track momenta (assuming perfect eID)
- DIS cuts: $0.01 < y < 0.95$, $Q^2 > 1$, $W^2 > 10 \text{ GeV}^2$
- SIDIS cuts: pions and kaons ($|\eta| < 3.5$), using true PID (assuming successful unfolding)
- $25 \times 13 \times 12 \times 12$ kinematic bins (x, Q^2, z, P_T)

Energy	Q^2 range	events	Luminosity (fb^{-1})
18x275	1 - 100	38.71M	0.044
	> 100	3.81M	1.232
18x100	1 - 100	14.92M	0.022
	> 100	3.72M	2.147
10x100	1 - 100	39.02M	0.067
	> 100	1.89M	1.631
5x41	1 - 100	39.18M	0.123
	> 100	0.96M	5.944

Kinematic variable	Bin boundaries
x	$1.0 \times 10^{-5}, 1.59 \times 10^{-5}, 2.51 \times 10^{-5}, 3.98 \times 10^{-5}, 6.31 \times 10^{-5},$ $1.0 \times 10^{-4}, 1.59 \times 10^{-4}, 2.51 \times 10^{-4}, 3.98 \times 10^{-4}, 6.31 \times 10^{-4},$ $1.0 \times 10^{-3}, 1.59 \times 10^{-3}, 2.51 \times 10^{-3}, 3.98 \times 10^{-3}, 6.31 \times 10^{-3},$ $1.0 \times 10^{-2}, 1.59 \times 10^{-2}, 2.51 \times 10^{-2}, 3.98 \times 10^{-2}, 6.31 \times 10^{-2},$ $1.0 \times 10^{-1}, 1.59 \times 10^{-1}, 2.51 \times 10^{-1}, 3.98 \times 10^{-1}, 6.31 \times 10^{-1},$ 1.0
Q^2	$1.0 \times 10^0, 1.78 \times 10^0, 3.16 \times 10^0, 5.62 \times 10^0,$ $1.0 \times 10^1, 1.78 \times 10^1, 3.16 \times 10^1, 5.62 \times 10^1,$ $1.0 \times 10^2, 1.78 \times 10^2, 3.16 \times 10^2, 5.62 \times 10^2,$ $1.0 \times 10^3, 1.0 \times 10^4$
z	0., 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0
P_T	0, 0.05, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0, 1.5, 2.0, 4.0

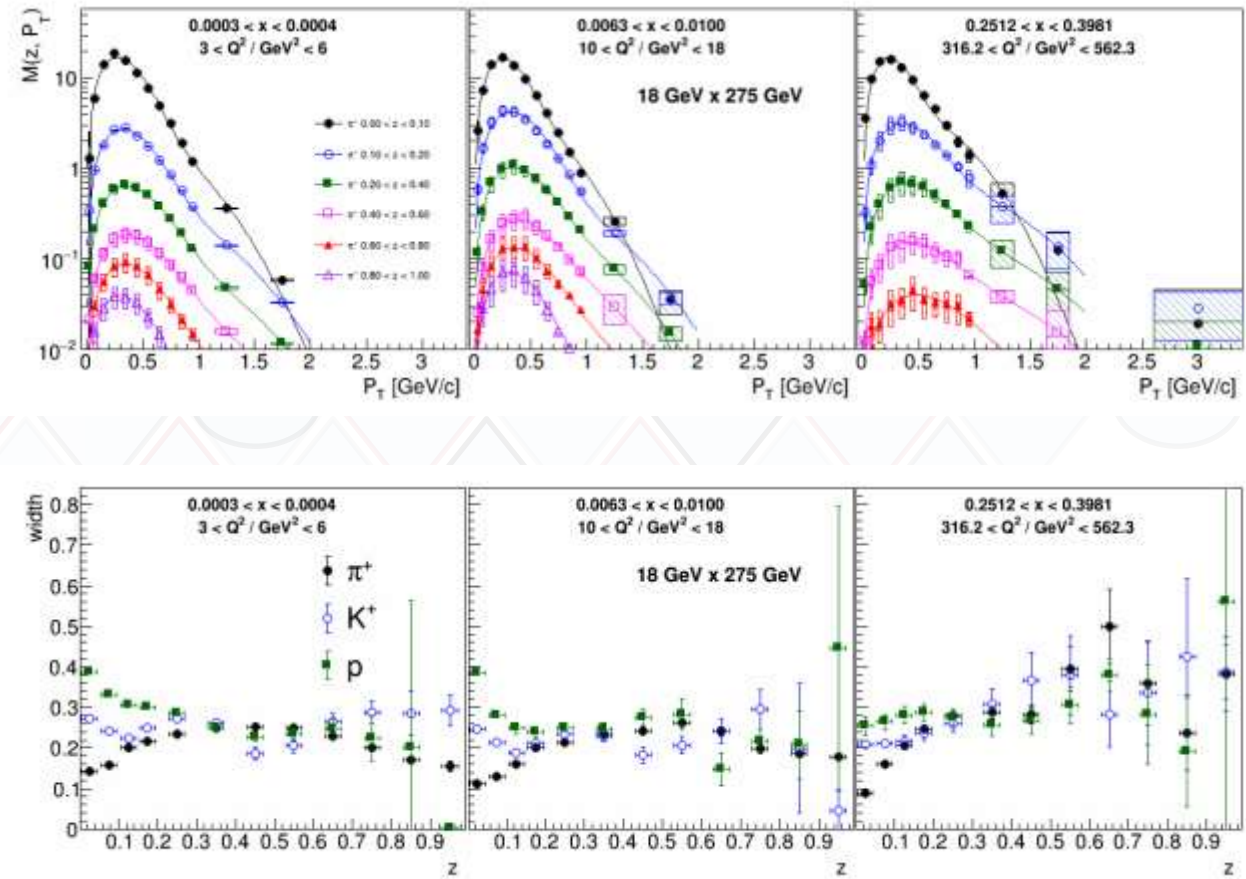
All Multiplicities at highest energies

- Pion, kaon and proton multiplicities shown in all x - Q^2 bins as a function of P_T (integrated over z)



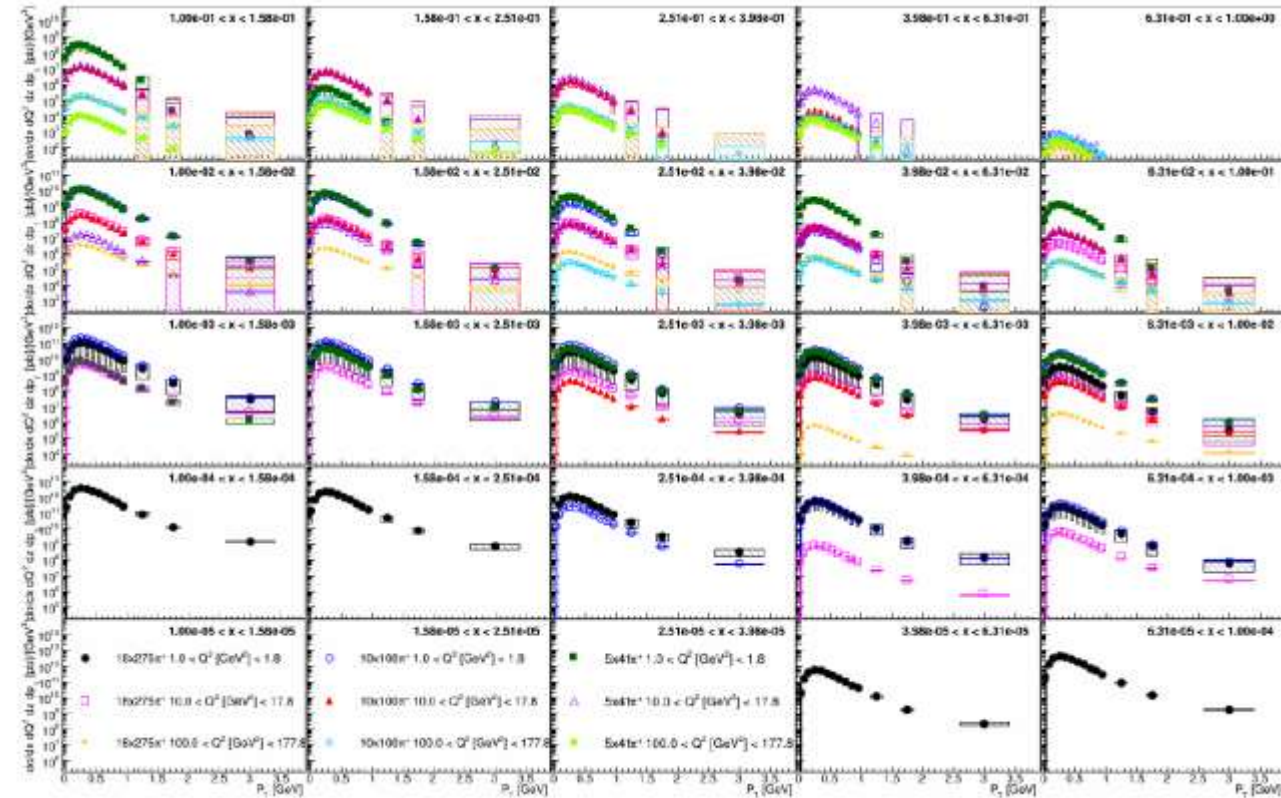
z-dependence of multiplicities and widths

- Top: Explicit z dependence of select pion multiplicities in 3 x-Q² bins, including the double-Gaussian fits
- Bottom: behavior of the narrow Gaussian widths vs z for pions, kaons and protons
- Small z discrepancies likely due to target fragmentation



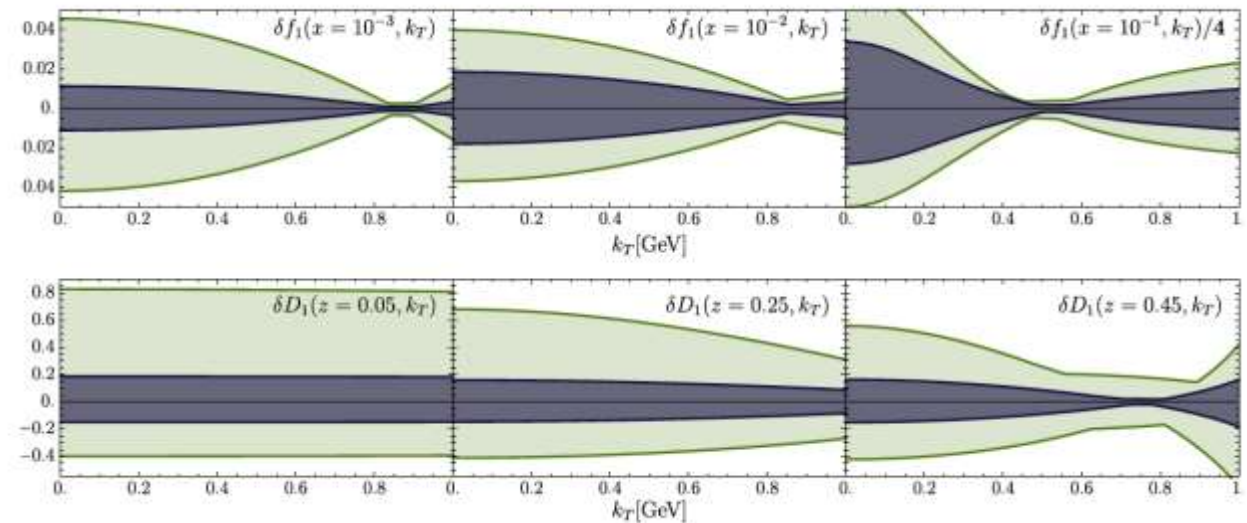
Combination of several collision energies

- Z-integrated PT dependent cross sections for several x and Q² bins and various collision energies



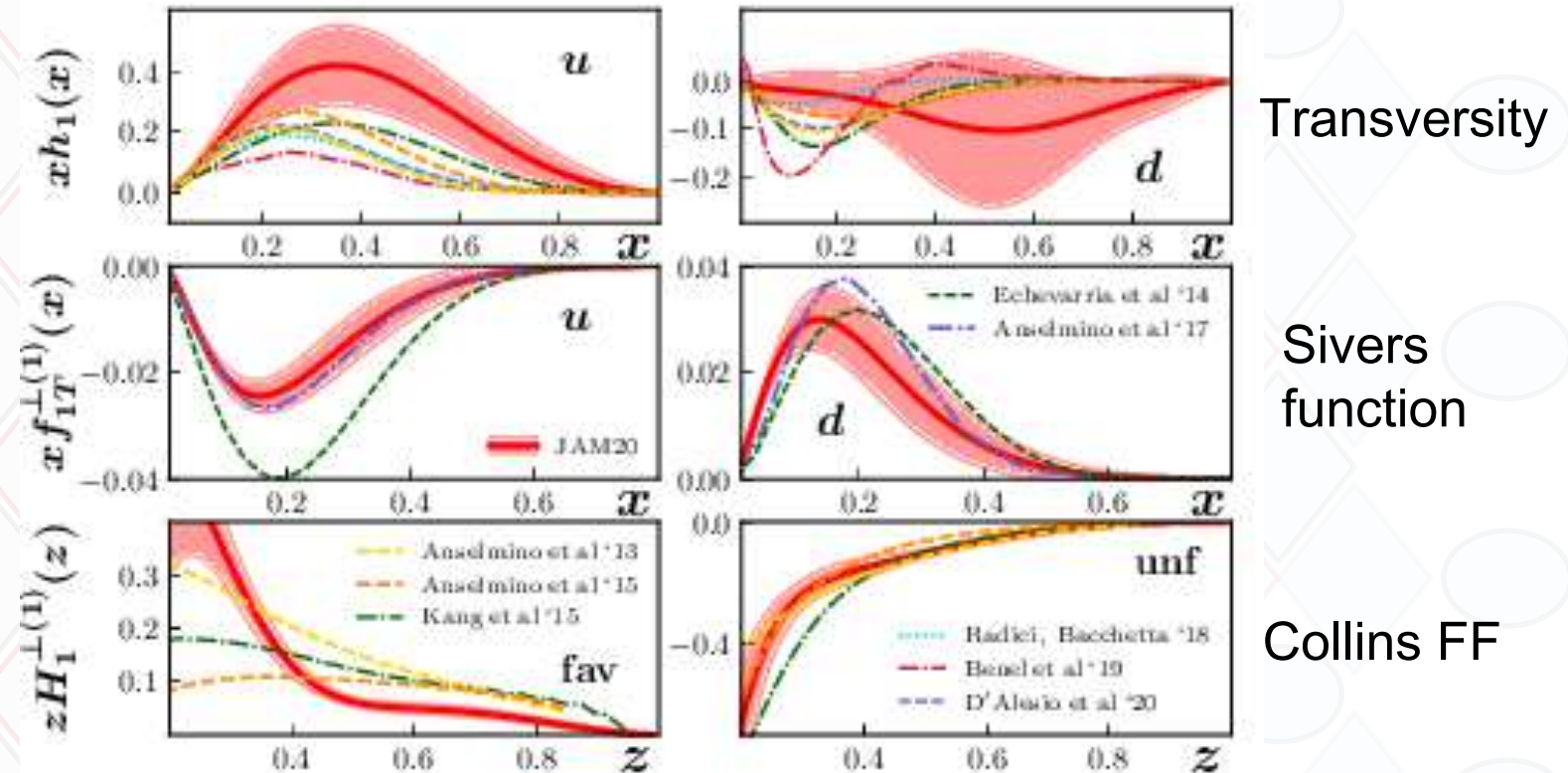
Impact for unpolarized TMD functions

- Similar to YR impact studies following the latest SV global fit (<https://arxiv.org/abs/1912.06532>) for the unpolarized TMDs based on the existing SIDIS +DY data
- Impact figure still that from YR, needs to be replaced (but little differences expected)



Current knowledge on these functions

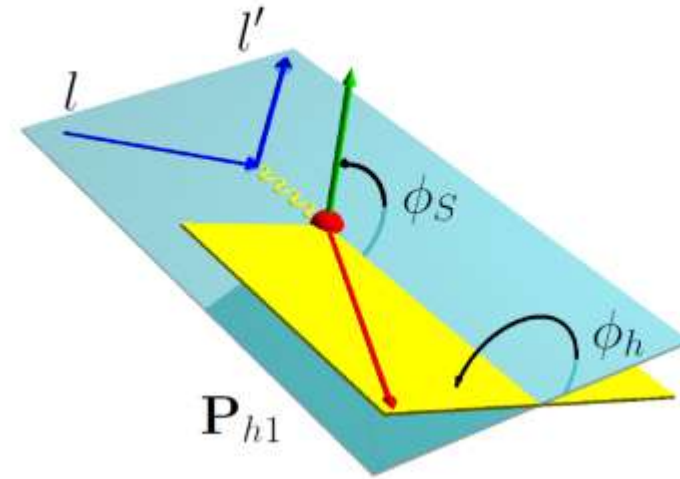
- Only valence quark
Sivers and Transversity functions known at this time with substantial uncertainties
- Experimentally covered range $0.01 < x < 0.3$
- So far no sensitivity to sea quarks and gluons* and lower x



[Camarota et al, PRD 102 \(2020\) 054002](#)

Experimental access to transversity and Sivers function

- Both functions are accessible as different azimuthal modulations in transversely polarized SIDIS of single hadrons
- Other TMD PDFs are similarly accessible via different modulations and spin orientations (though often higher twist effects present)
- Gluon Sivers via di-jet/di-HF TSSAs (only partially studied in ECCE so far → needs to be addressed soon)



$$A_{UT}^{\sin(\phi_h + \phi_S)}(x, z, P_T) \propto \mathbf{S}_T \frac{\sum_{q, \bar{q}} e_q^2 \delta q(x, k_t) \otimes H_1^\perp(z, p_t)}{\sum_{q, \bar{q}} e_q^2 q(x, k_t) \otimes D_1(z, p_t)}$$

$$A_{UT}^{\sin(\phi_h - \phi_S)}(x, z, P_T) \propto \mathbf{S}_T \frac{\sum_{q, \bar{q}} e_q^2 f_{1T}^{\perp, q}(x, k_t) \otimes D_1(z, p_t)}{\sum_{q, \bar{q}} e_q^2 q(x, k_t) \otimes D_1(z, p_t)}$$

ECCE simulation setup and binning

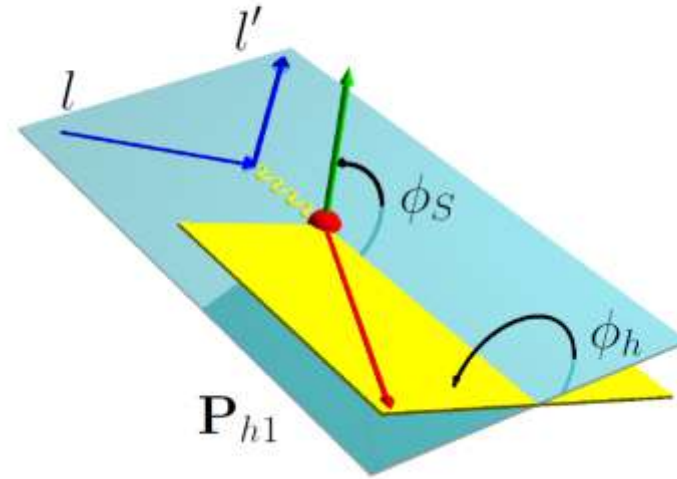
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- Generator output simulated through GEANT4 (prop4)
- Analyzed via slightly modified EventEvaluator TTrees
- Scattered lepton ($|\eta| < 3.5$) DIS kinematic reconstruction using reco track momenta (assuming perfect eID)
- DIS cuts: $0.01 < y < 0.95$, $Q^2 > 1$, $W^2 > 10 \text{ GeV}^2$
- SIDIS cuts: pions and kaons ($|\eta| < 3.5$), using true PID (assuming successful unfolding)
- Initially $12 \times 8 \times 12 \times 12$ kinematic bins (x, Q^2, z, P_T) and 16×16 azimuthal bins

Energy	Q^2 range	events	Luminosity (fb^{-1})
18x275	1 - 100	38.71M	0.044
	> 100	3.81M	1.232
18x100	1 - 100	14.92M	0.022
	> 100	3.72M	2.147
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	> 100	0.96M	5.944

Kinematic variable	Bin boundaries
x	$1.0 \times 10^{-4}, 2.154 \times 10^{-4}, 4.641 \times 10^{-4},$ $1.0 \times 10^{-3}, 2.154 \times 10^{-3}, 4.641 \times 10^{-3},$ $1.0 \times 10^{-2}, 2.154 \times 10^{-2}, 4.641 \times 10^{-2},$ $1.0 \times 10^{-1}, 2.154 \times 10^{-1}, 4.641 \times 10^{-1},$ 1.0×10^0
Q^2	$1.0 \times 10^0, 3.162 \times 10^0,$ $1.0 \times 10^1, 3.162 \times 10^1,$ $1.0 \times 10^2, 3.162 \times 10^2,$ $1.0 \times 10^3, 3.162 \times 10^3,$ 1.0×10^4
z	0, 0.05, 0.1, 0.15, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0
P_T	0, 0.05, 0.1, 0.2, 0.3, 0.5, 0.7, 0.9, 1.2, 1.5, 1.8, 2.4, 4.0

Sivers/Collins measurements in SIDIS

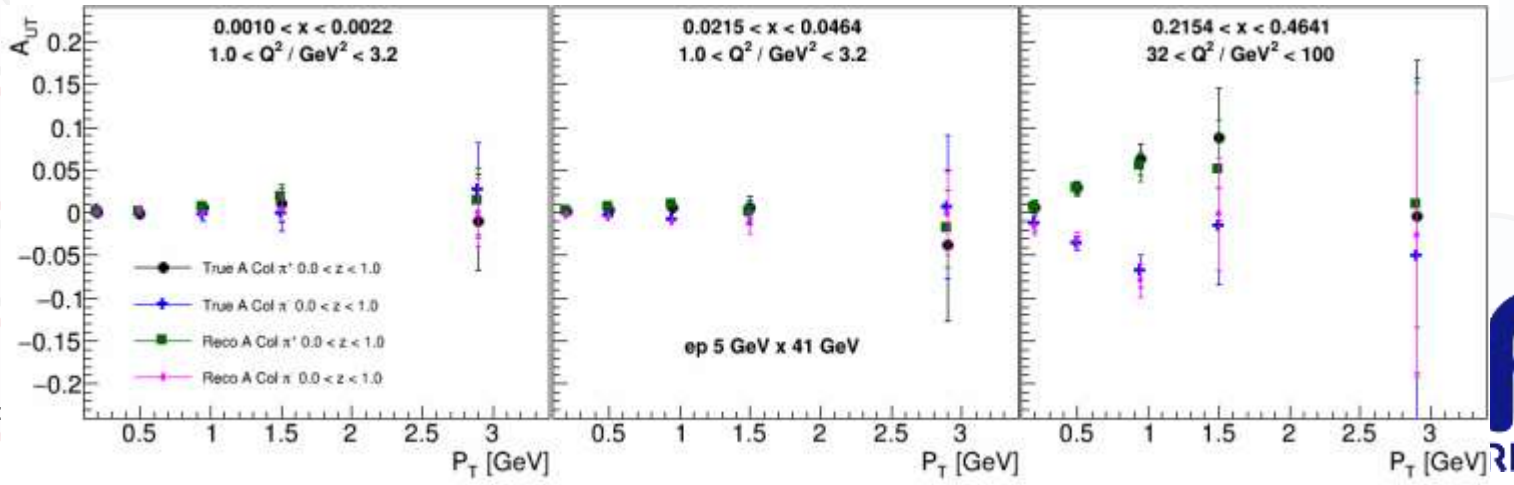
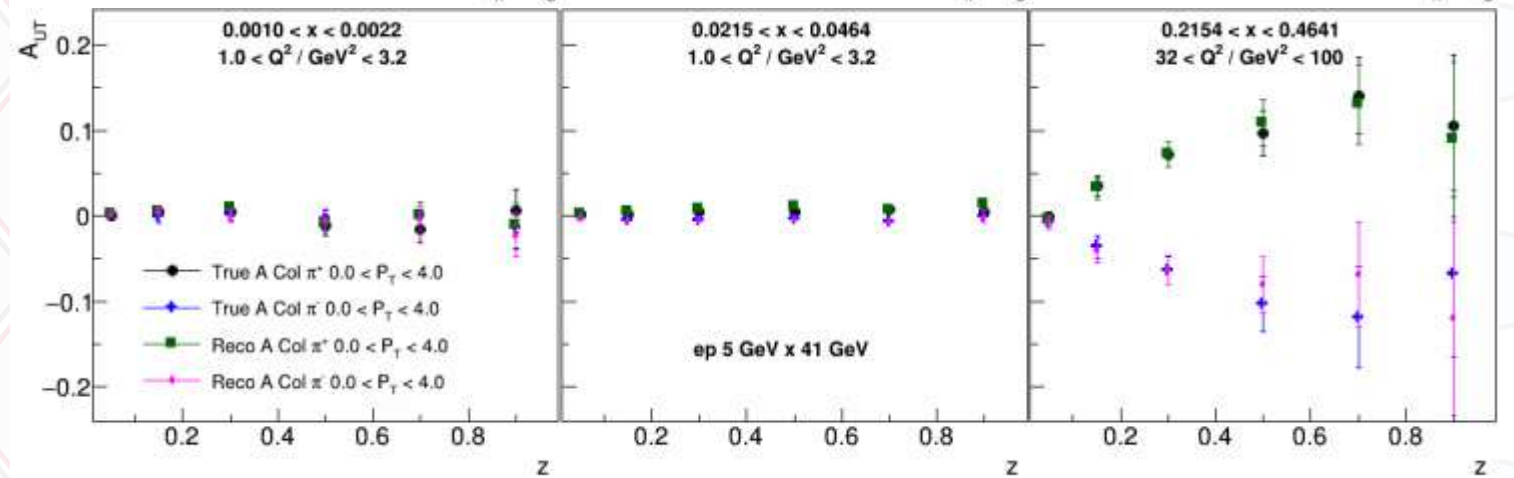
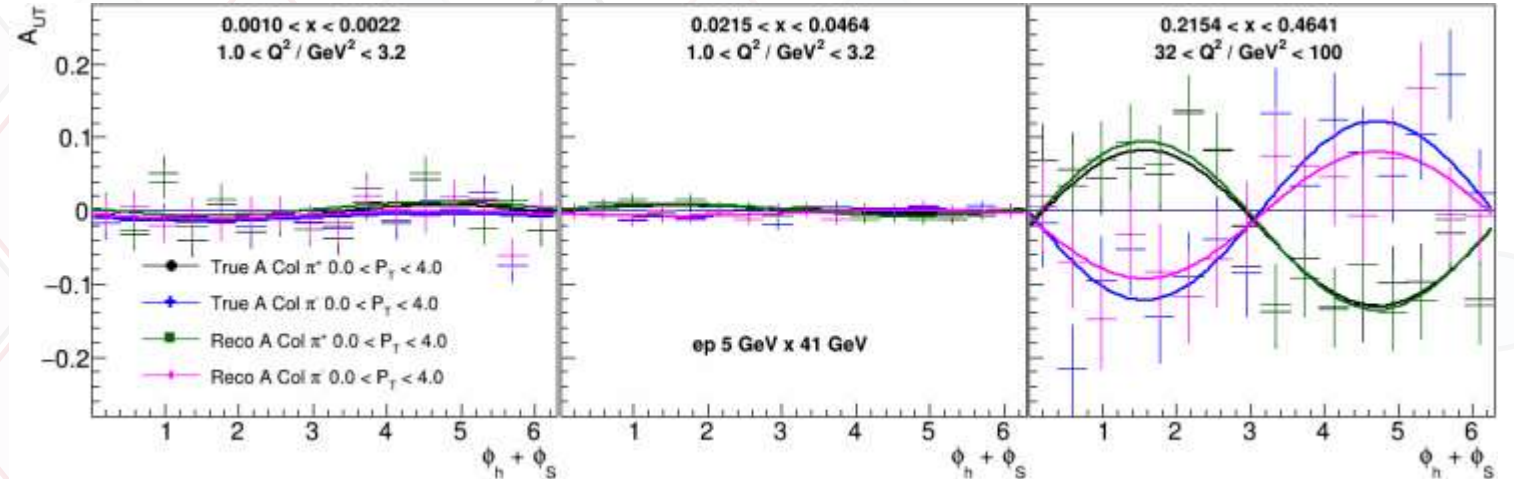
- Reweight events according to true parton flavor q , hadron h , x , z , Q^2 , P_{hT} , azimuthal angles and random spin orientation
- $ep^\uparrow \rightarrow e'hX$
- A_{UT} asymmetries (Unpolarized lepton beam, Transversely polarized target)
- Different azimuthal modulations related to Sivers effect ($\sin(\phi - \phi_s)$) and Collins effect ($\sin(\phi + \phi_s)$)
- Fit simultaneously in the reconstructed events and calculate asymmetries



- Input structure functions (polarized and unpolarized) from Torino global fits (arXiv:0812.4366, arXiv:0805.2677) as in <https://github.com/prokudin/tmd-parametrizations/>

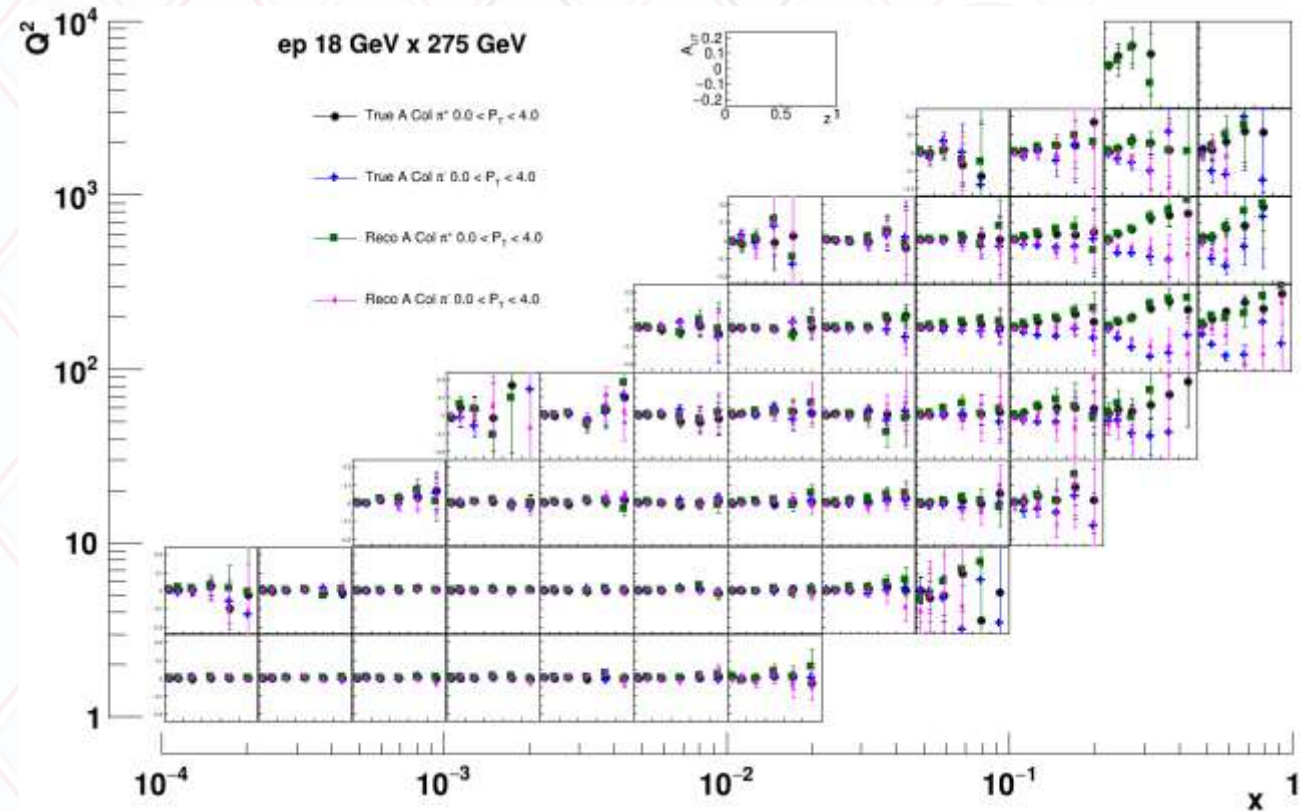
Example figures

- Examples in 3 x and Q^2 bins: on top for the Collins angular combination for charged pions true and reconstructed in an intermediate z bin
- Lower figures: same, either projected vs z or vs P_T



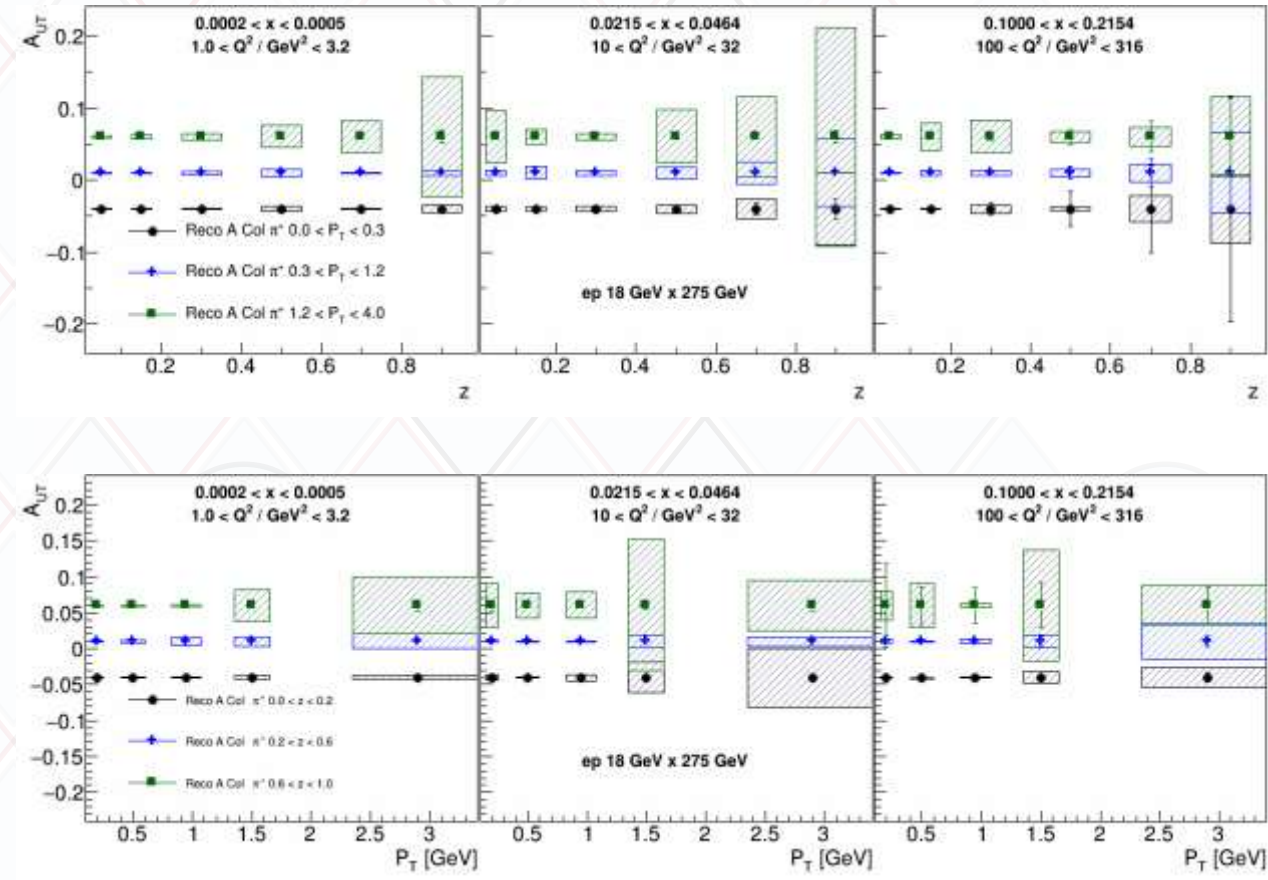
Collins asymmetries at highest energies

- Example of the level of reconstruction and uncertainties give the simulated statistics
- Nonzero asymmetries well reproduced at higher x
- Opposite sign for π^+/π^- seen as expected
- High precision at lower (yet hardly measured) x



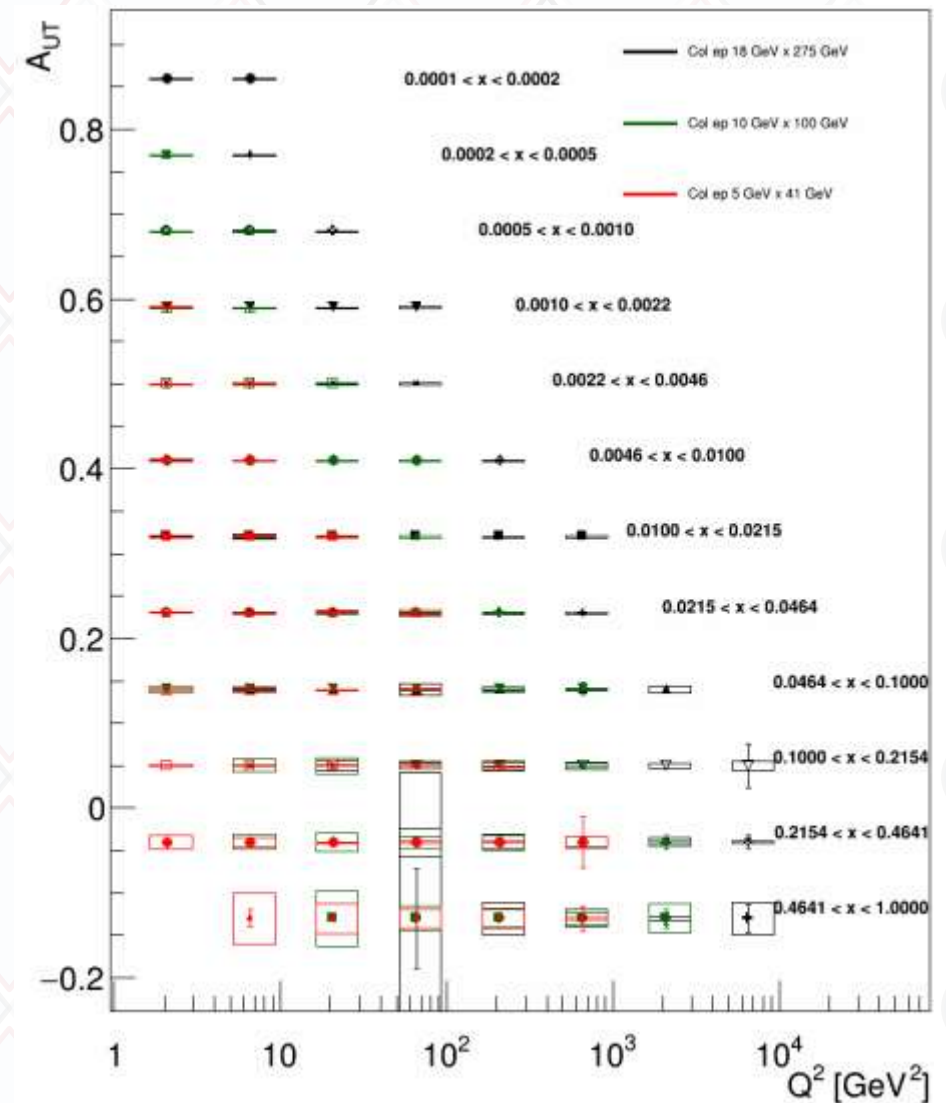
Projections to 10fb^{-1}

- Systematic uncertainties estimated from differences between true and reconstructed asymmetries \rightarrow they are likely largely overestimated since most of the kinematic smearing would be unfolded, but give a sense of where uncertainties still might be larger due to that unfolding



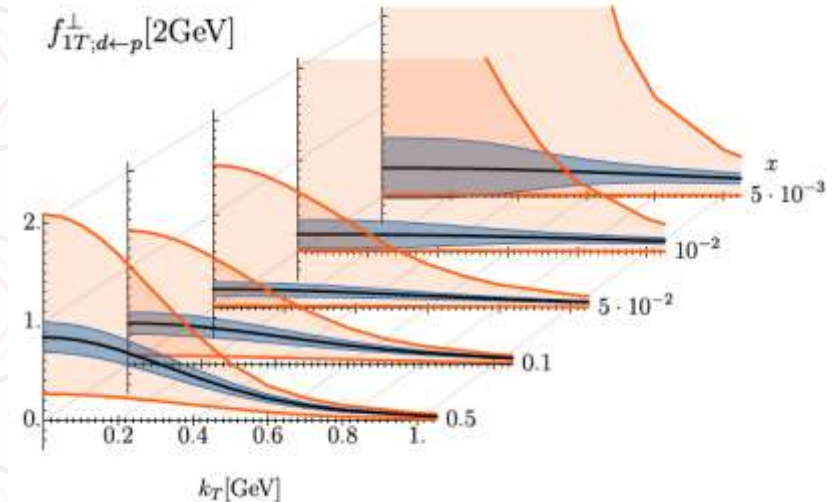
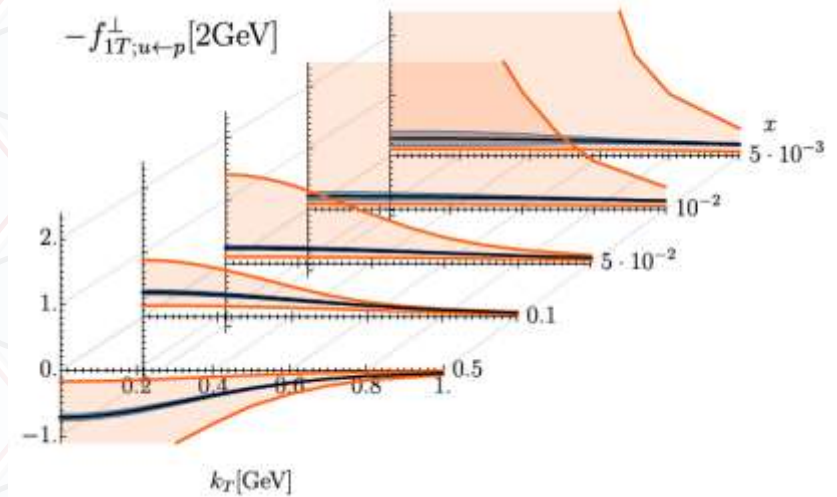
Scale dependence (and interplay of collision energies)

- An example of the expected uncertainties in x and Q^2 to study the scale dependence of the Sivers/Collins asymmetries (as TMD evolution is not very well known/contains other nonperturbative pieces)
- Overlap of the different energies shows how they increase the lever arm
- Note: in future evolution analysis likely more Q^2 bins and maybe not as fine x binning



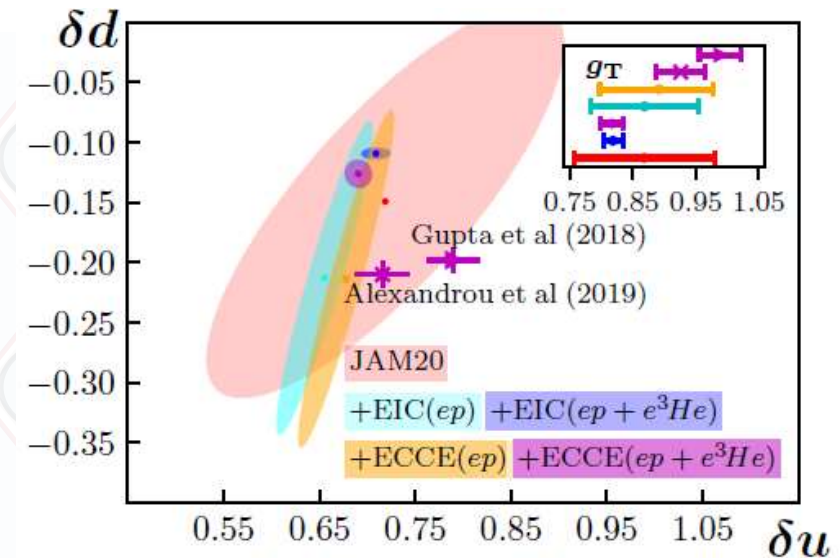
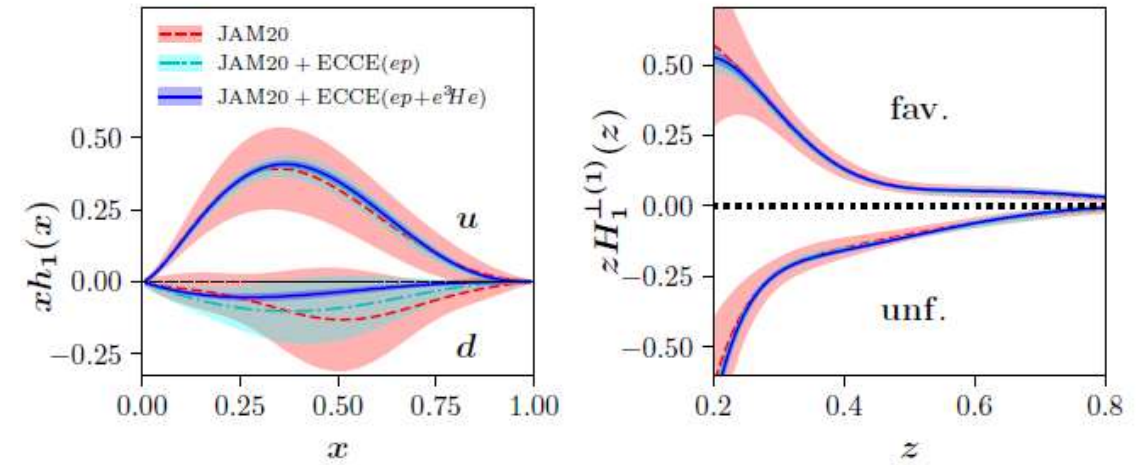
Impact for Sivers functions

- Similar to YR impact studies following the latest BPV global fit (arXiv:2103.03270) for the Sivers function based on the existing SIDIS +DY data
- Uncertainties are shown for current level of knowledge on up/down Sivers functions at various x vs k_T and expected impact from ECCE



Tensor charge impact

- Similar to [Gamberg et al Phys.Lett.B 816 \(2021\) 136255](#) (for YR) use fitting code from latest global fit Cammarota et al arXiv:2002.08384 to extract impact on Transversity, Collins functions and tensor charges
- Together with projected JLAB12 data precision to compare with Lattice results (and check for possible discrepancies)



Summary

- Full GEANT simulations to study the reconstruction of DIS and SIDIS variables using various reconstruction methods (lepton, DA, JB)
- ➔ Follow up with further studies as detector evolves:
 - Add EMCAL info where better for electron DIS reconstruction
 - Add Sigma method, study hadronic methods' tracking vs cluster performance more (currently only clusters if trackless – neutrals)
 - Optimize interplay between best methods
- Unpolarized and Sivers/Collins TMD SIDIS studies performed using full GEANT simulations, impact plots prepared
- ➔ Follow up on these studies as project detector evolves:
 - Improved DIS kinematics reconstruction/different methods
 - consider studying the proper unfolding of kinematic smearing as well as particle identification
 - Radiative effects
 - Consider more explicit TMD evolution studies

DIS Kinematic reconstruction using hadronic Final State:

- JB method: use only hadronic final state

$$y_{JB} = \frac{E_p \sum_h E_h - p_{z,p} \sum_h p_{z,h} - m_p^2}{E_p E_e - p_{z,p} p_{z,e}}$$

$$Q_{JB}^2 = \frac{\sum_h p_{x,h}^2 + \sum_h p_{y,h}^2}{1 - y}$$

$$x_{JB} = \frac{Q^2}{ys}$$

- Double Angle method: use both

$$y_{DA} = \frac{\tan \theta_h / 2}{\tan \theta_e / 2 + \tan \theta_h / 2}$$

$$Q_{DA}^2 = \frac{4E_2^2}{\tan \theta_e / 2 (\tan \theta_e / 2 + \tan \theta_h / 2)}$$

$$x_{DA} = \frac{Q^2}{ys}$$

$$\tan \theta_h / 2 = \frac{\sum_h E_h - \sum_h p_{z,h}}{\sqrt{\sum_h p_{x,h}^2 + \sum_h p_{y,h}^2}}$$

