

# Proton internal structure

Nobuo Sato



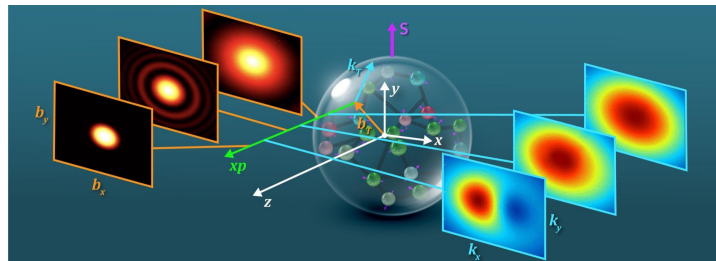
Sep. 22, 2022

Advancing the understanding of non-perturbative QCD using energy flows

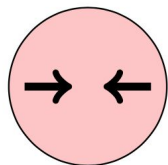


# Motivations

- **Synthesis of 3D tomography/nuclear imaging:** quantum correlation functions (QCFs)
  - hadron structure (PDFs, TMDs, GPDs, HT, ...)
  - hadronization (FFs, TMDFFs)
- **Test of universality & theory predictive power**
  - systematic improvements (resummation, evolution, HO calculations)
  - synergy with lattice calculations (Bayesian priors)
  - identification of regions of phase space where existing theory framework is applicable (phenomenology)
- **Opportunities**
  - origin of proton spin
  - quark and gluon tomography
  - structure of proton sea (strangeness / antimatter asymmetry)
  - origin of nuclear EMC effect
  - precision EW physics (Weinberg angle)
  - ...

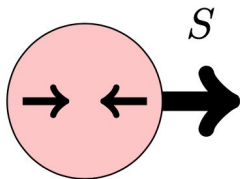


# Collinear Spin structures



$$f = f_{\rightarrow} + f_{\leftarrow}$$

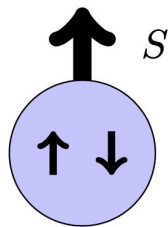
$$\langle N | \bar{\psi}_i(0, w^-, \mathbf{0}_T) \gamma^+ \psi_i(0) | N \rangle$$



$$\Delta f = f_{\rightarrow} - f_{\leftarrow}$$

Helicity distribution

$$\langle N | \bar{\psi}_i(0, w^-, \mathbf{0}_T) \gamma^+ \gamma_5 \psi_i(0) | N \rangle$$



$$\delta_T f = f_{\uparrow} - f_{\downarrow}$$

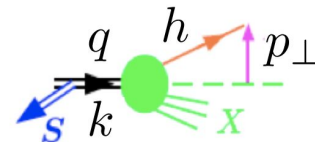
Transversity

$$\langle N | \bar{\psi}_i(0, w^-, \mathbf{0}_T) \gamma^+ \gamma_{\perp} \gamma_5 \psi_i(0) | N \rangle$$

# TMD Spin structures

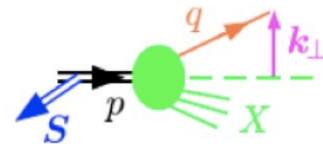
Sivers '89

$$f_{q/h^\uparrow}(x, \vec{k}_\perp, \vec{S}) = f_{q/h}(x, k_\perp^2) - \frac{1}{M} f_{1T}^{\perp q}(x, k_\perp^2) \vec{S} \cdot (\hat{P} \times \vec{k}_\perp)$$


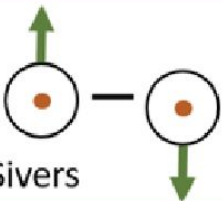
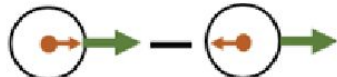
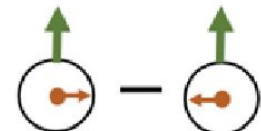



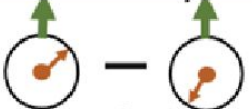


Collins '92

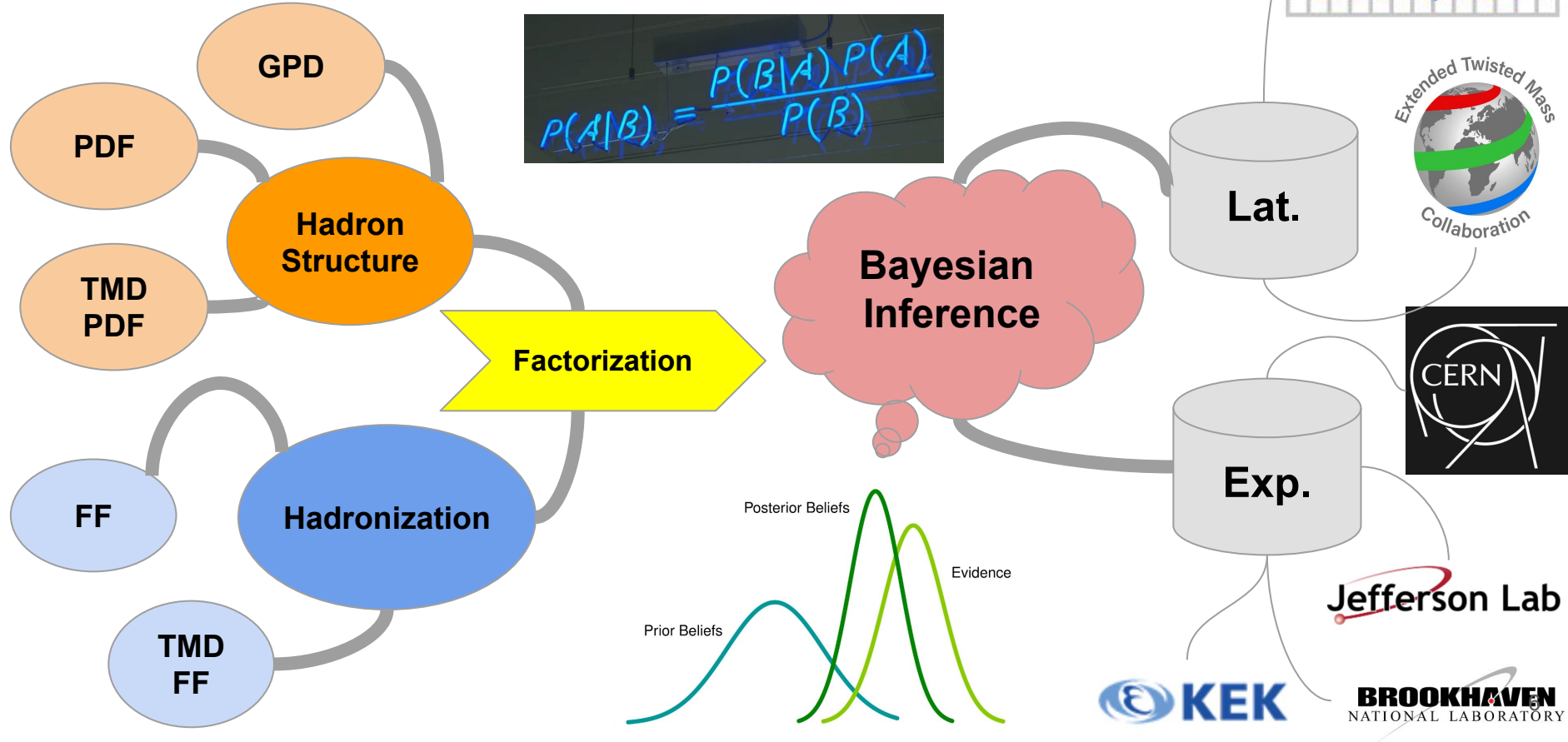
$$D_{q/h}(z, \vec{p}_\perp, \vec{s}_q) = D_{q/h}(z, p_\perp^2) + \frac{1}{zM_h} H_1^{\perp q}(z, p_\perp^2) \vec{s}_q \cdot (\hat{k} \times \vec{p}_\perp)$$





		Nucleon Polarization		
		Unpolarized	Longitudinal	Transverse
Quark Polarization	Unpolarized	$f_1$  Number Density		$f_{1T}^\perp$  Sivers
	Longitudinal		$g_1$  Helicity	$g_{1T}^\perp$  Worm-Gear T
	Transverse	$h_1^\perp$  Boer-Mulders	$h_{1L}^\perp$  Worm-Gear L	<div> <math>h_1</math>             Transversity         </div> <div> <math>h_{1T}^\perp</math>             Pretzelosity         </div>

# A holistic approach to global analysis



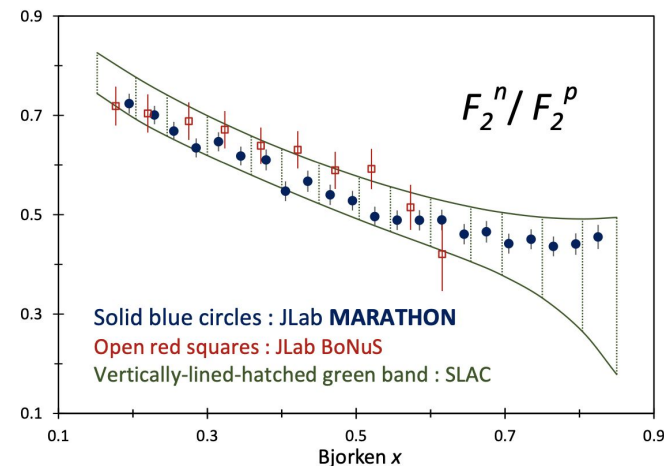
# Outline

1. Isovector EMC effect with MARATHON data
2. Sea asymmetry with SeaQuest and STAR data
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6. Meson structure

## High Energy Physics – Experiment

[Submitted on 12 Apr 2021]

# Measurement of the Nucleon $F_2^n/F_2^p$ Structure Function Ratio by the Jefferson Lab MARATHON Tritium/Helium-3 Deep Inelastic Scattering Experiment



Theory input

Experimental measurement

$$\frac{F_2^n}{F_2^p} = \frac{2\mathcal{R}_{ht} - F_2^h/F_2^t}{2F_2^h/F_2^t - \mathcal{R}_{ht}}$$

↔



## High Energy Physics – Experiment

[Submitted on 12 Apr 2021]

Measurement of the Nucleon  $F_2^n/F_2^p$  Structure Function  
by the Jefferson Lab MARATHON Tritium  
Inelastic Scattering Experiment

High Energy Physics – Phenomenology

[Submitted on 14 Apr 2021]

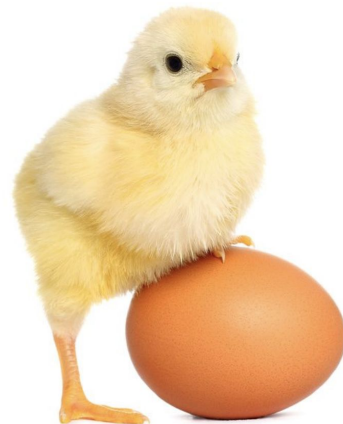
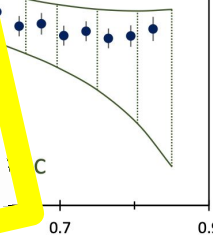
Isovector EMC effect from global QCD analysis with  
MARATHON data

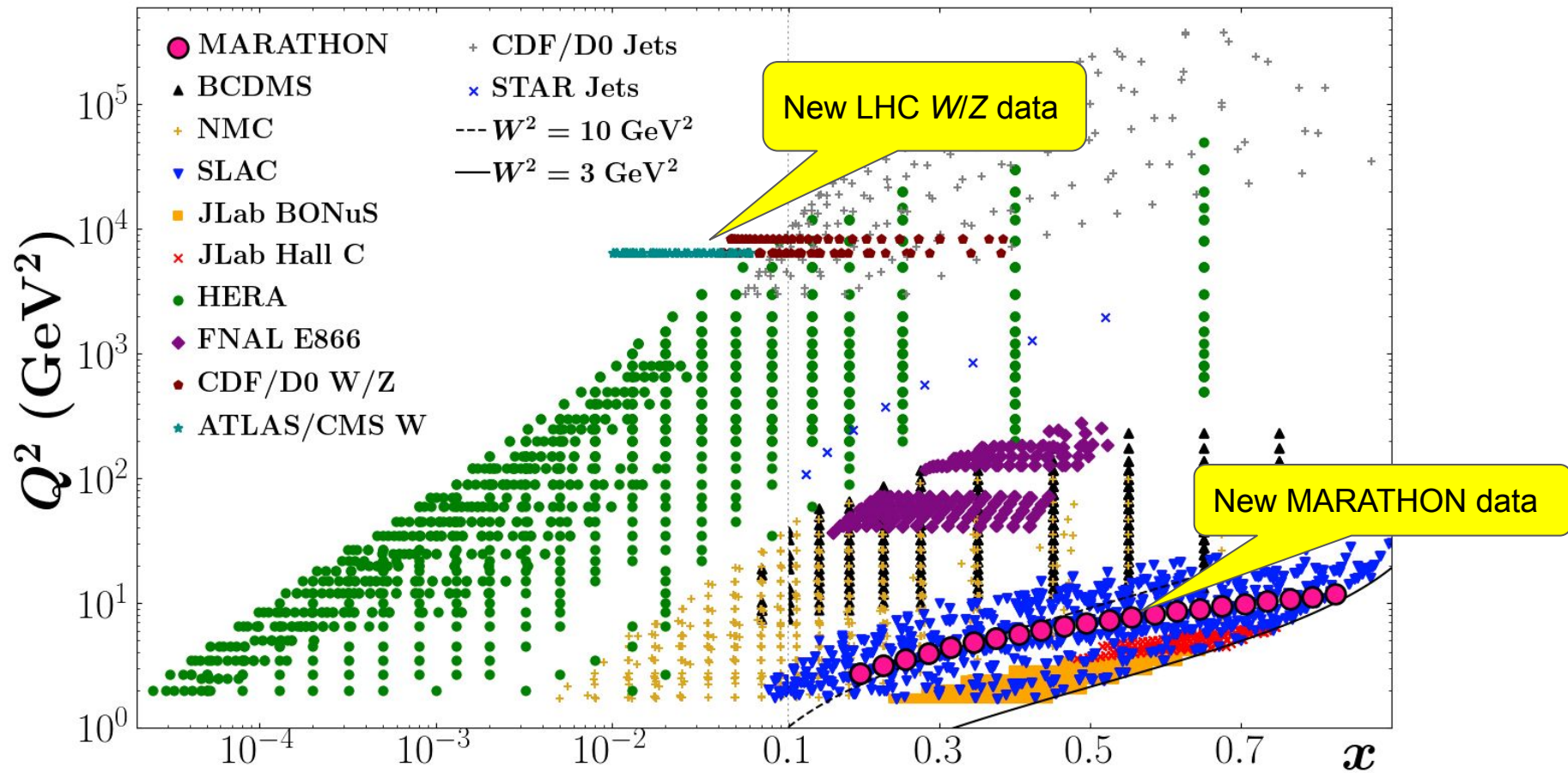
C. Cocuzza, C. E. Keppel, H. Liu, W. Melnitchouk, A. Metz, N. Sato, A. W. Thomas

$$\frac{F_2^n}{F_2^p} = \frac{2\mathcal{R}_{ht} - F_2^h/F_2^t}{2F_2^h/F_2^t - \mathcal{R}_{ht}}$$



$$F_2^n/F_2^p$$







# Insights from mean field theory

Mineo, Bentz, Ishii, Thomas,  
Yazaki ('04)

$$\hat{H}_q = \hat{h}_q + V_0 \hat{Q}$$

$$V^\mu = (V_0, \mathbf{0})$$

constant mean vector  
field acting on a quark  
in the nuclear medium

$$q(x) = \frac{p^+}{p^+ - V^+} q_0 \left( \frac{p^+}{p^+ - V^+} x - \frac{V_q^+}{p^+ - V^+} \right)$$

PDF in the absence of a vector potential

# Phenomenological approach

$$\tilde{q}_{N/A}(x, p^2) = q_N(x) + v(p^2)\delta q_{N/A} + \dots$$
$$\downarrow$$
$$v(p^2) = (p^2 - M^2)/M^2$$

$$F_2^{N(\text{on})}(x, Q^2) = \left( \sum_q [C_q \otimes q_N^+] + [C_g \otimes g_N] \right) \times \left( 1 + \frac{C_N^{\text{HT}}(x)}{Q^2} \right)$$

$$F_2^{N/A(\text{off})}(x, Q^2) = \left( \sum_q [C_q \otimes \delta q_{N/A}] \right) \times \left( 1 + \frac{C_N^{\text{HT}}(x)}{Q^2} \right)$$

# Nuclear impulse approximation

$$F_2^{A(\text{on})}(x, Q^2) = \sum_N \left[ f^{N/A} \otimes F_2^{N(\text{on})} \right]$$

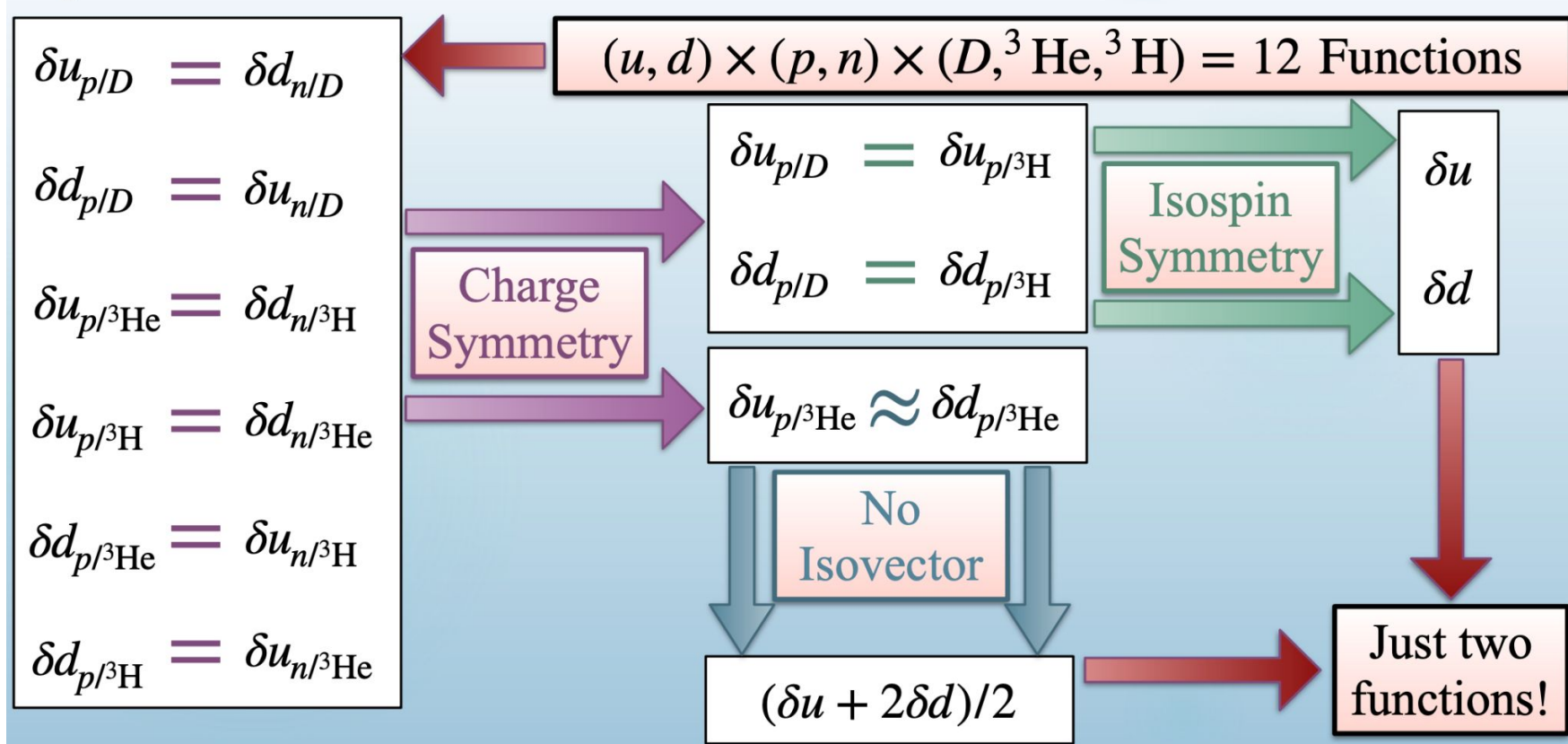
$$F_2^{A(\text{off})}(x, Q^2) = \sum_N \left[ \tilde{f}^{N/A} \otimes F_2^{N/A(\text{off})} \right]$$

Nonrelativistic nucleon  
spectral functions computed  
from quantum Monte Carlo

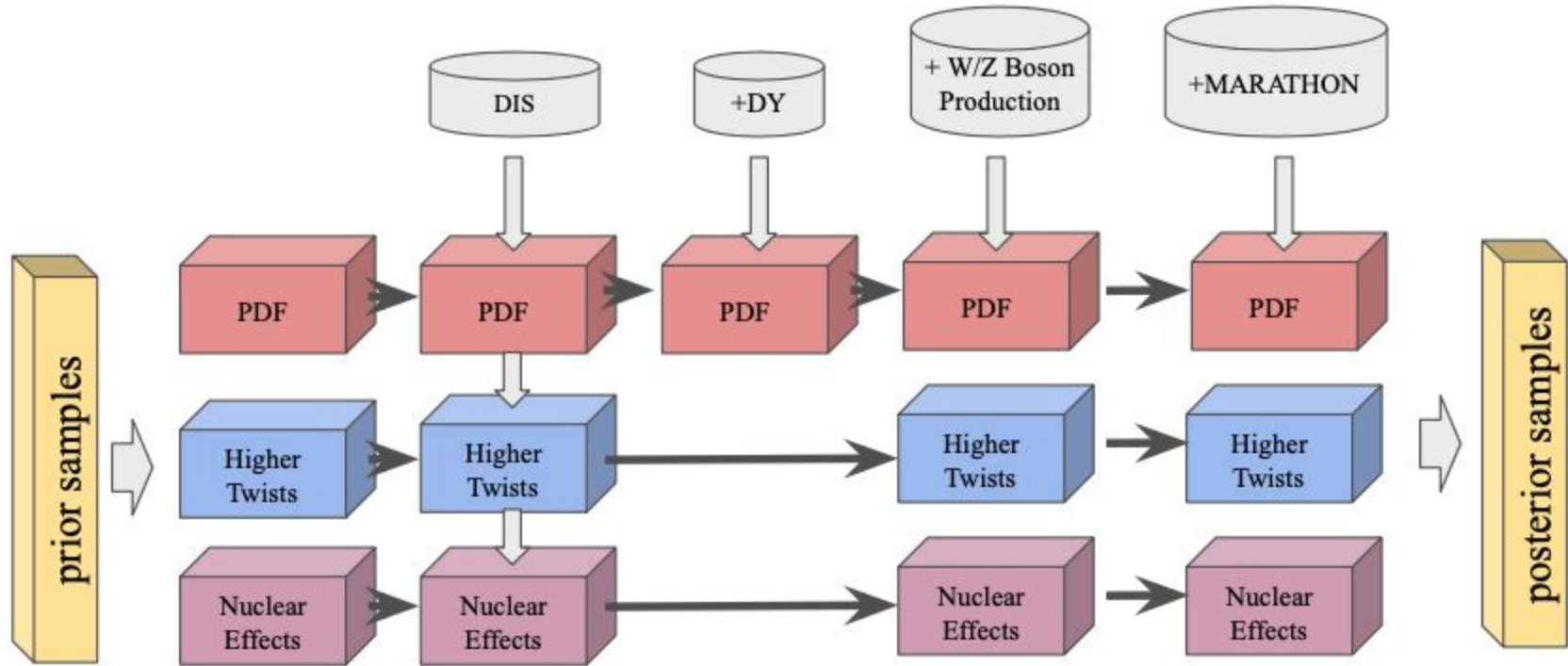
$$f_{ij}^N(y, \gamma) = \int \frac{d^4p}{(2\pi)^4} \mathcal{F}_0^N(\varepsilon, \mathbf{p}) \left(1 + \frac{\gamma p_z}{M}\right) \mathcal{C}_{ij} \delta\left(y - 1 - \frac{\varepsilon + \gamma p_z}{M}\right)$$

$$\tilde{f}_{ij}^N(y, \gamma) = \int \frac{d^4p}{(2\pi)^4} \mathcal{F}_0^N(\varepsilon, \mathbf{p}) \left(1 + \frac{\gamma p_z}{M}\right) \mathcal{C}_{ij} v(p^2) \delta\left(y - 1 - \frac{\varepsilon + \gamma p_z}{M}\right)$$

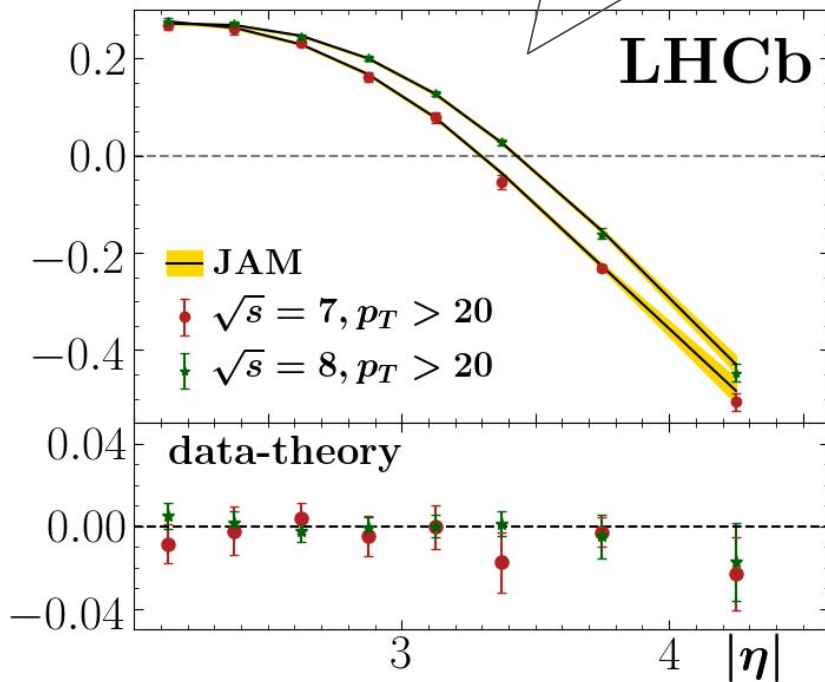
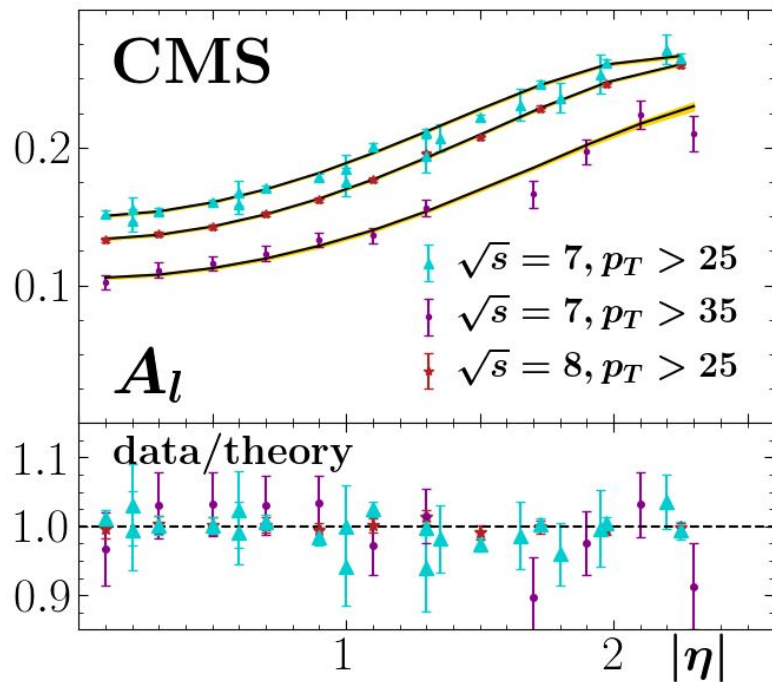
# Symmetries



# Multi-step strategy



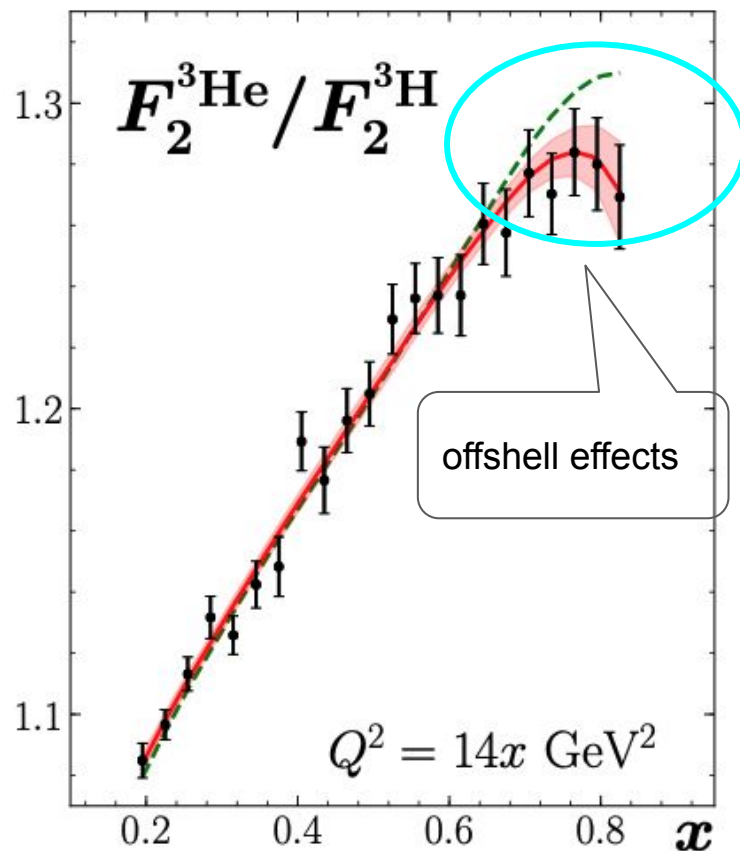
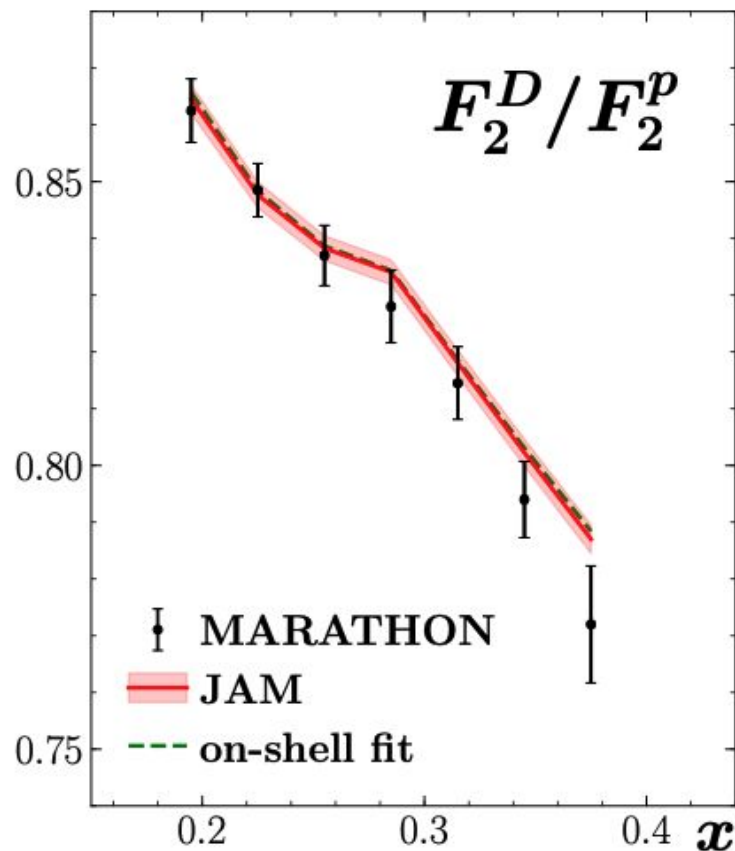
# LHC W data

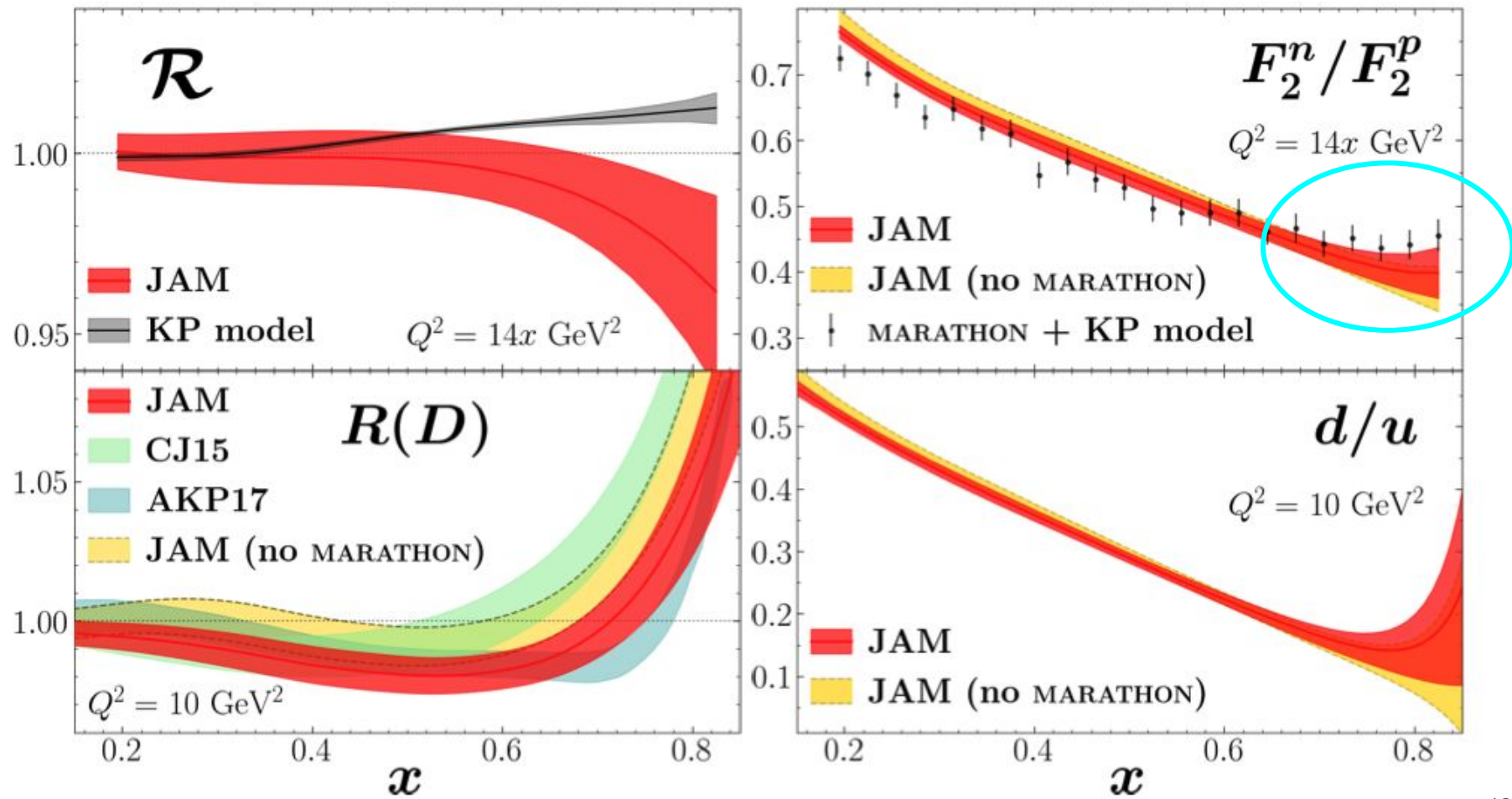


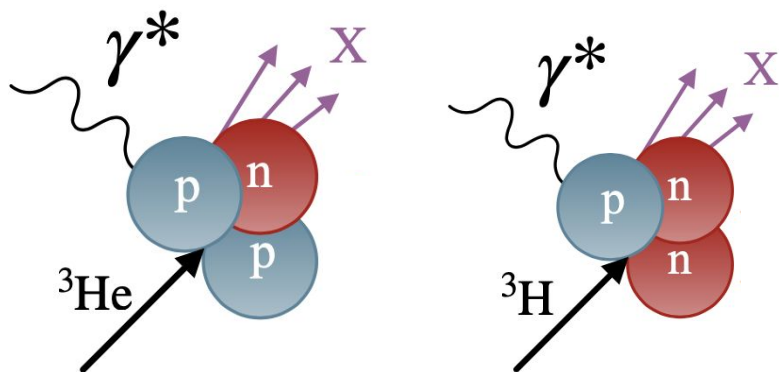
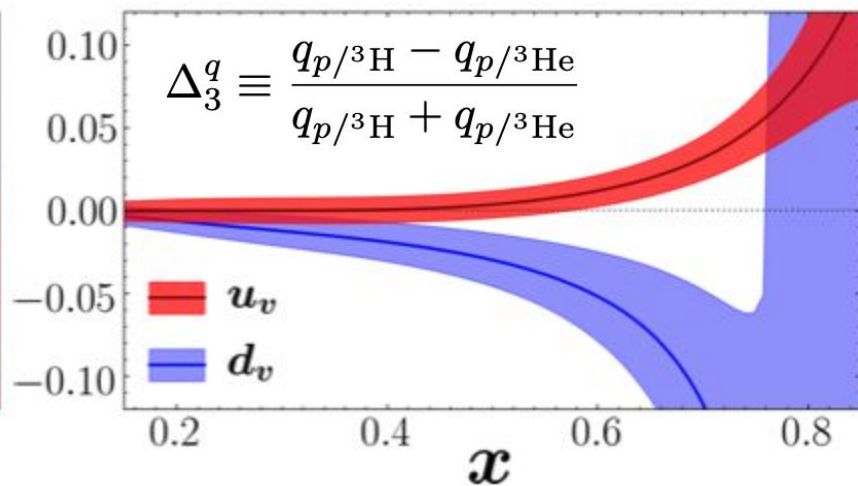
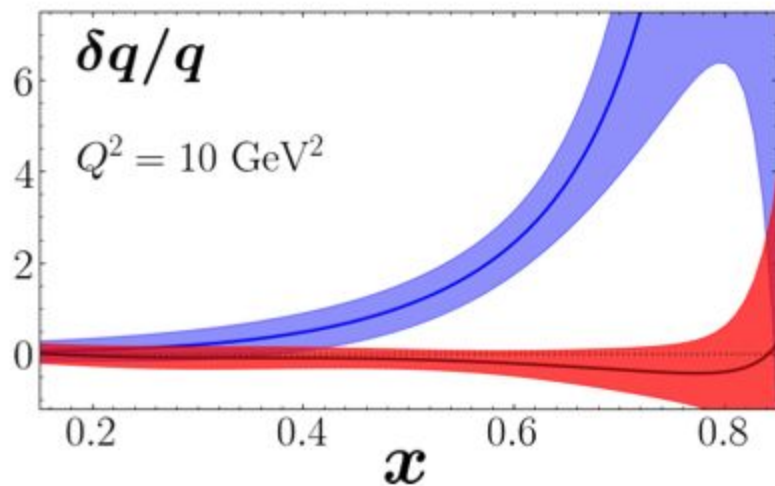
Excellent agreement  
between theory and data



# MARATHON data







- Evidence of different medium modifications for  $u$  and  $d$  quarks
- Naive modeling of nuclear PDFs, e.g.  $u/p/A = d/n/A$  (violates isospin for non-isoscalar  $A$ ) is wrong
- Proposals to explore isovector effects in SIDIS at JLab

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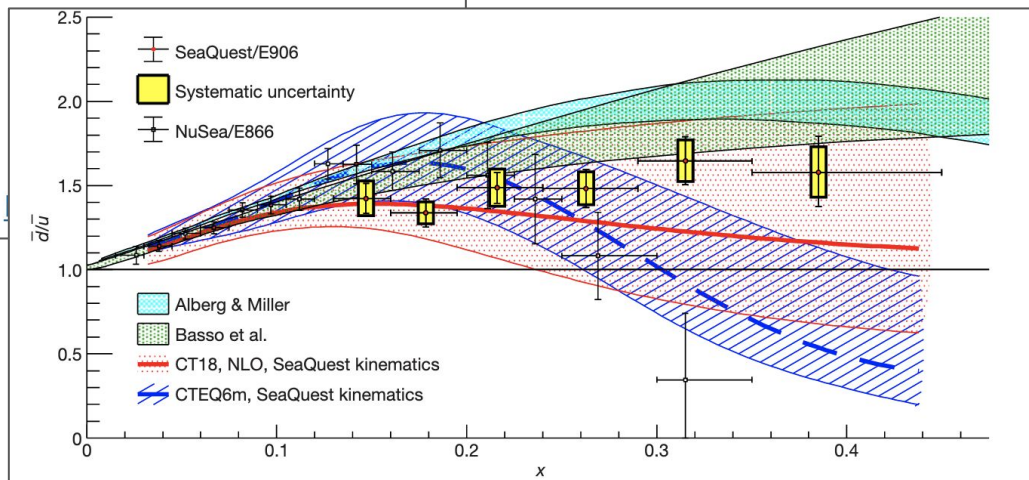
Article | [Published: 24 February 2021](#)

## The asymmetry of antimatter in the proton

[J. Dove](#), [B. Kerns](#), ... [Z. Ye](#) [+ Show authors](#)

[Nature](#) **590**, 561–565 (2021) | [Cite this article](#)

**8942** Accesses | **13** Citations | **290** Altmetric



Measurements of  $W$  and  $Z/\gamma^*$  cross sections and their ratios in  $p + p$  collisions at RHIC

J. Adam *et al.* (STAR Collaboration)

Phys. Rev. D **103**, 012001 – Published 4 January 2021

Article | [Published: 24 February 2021](#)

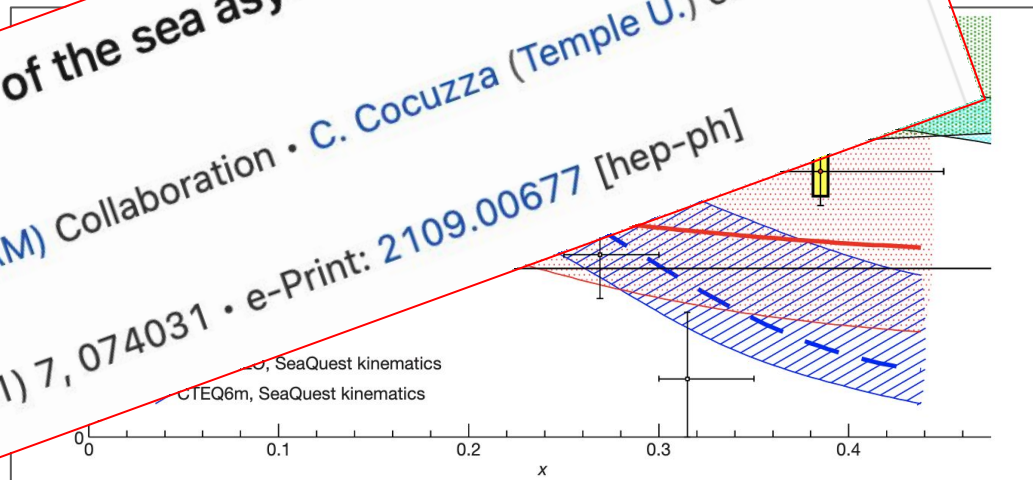
## The asymmetry of antimatter in the

[J. Dove](#), [B. Kerns](#), ... [Z. Ye](#) [+ Show authors](#)

[Nature](#) **590**, 561–565 (2021)

**8942** Accesses

Bayesian Monte Carlo extraction of the sea asymmetry with SeaQuest #7  
and STAR data  
Jefferson Lab Angular Momentum (JAM) Collaboration • C. Cocuzza (Temple U.) et al. (Sep 1, 2021)  
Published in: Phys.Rev.D 104 (2021) 7, 074031 • e-Print: 2109.00677 [hep-ph]

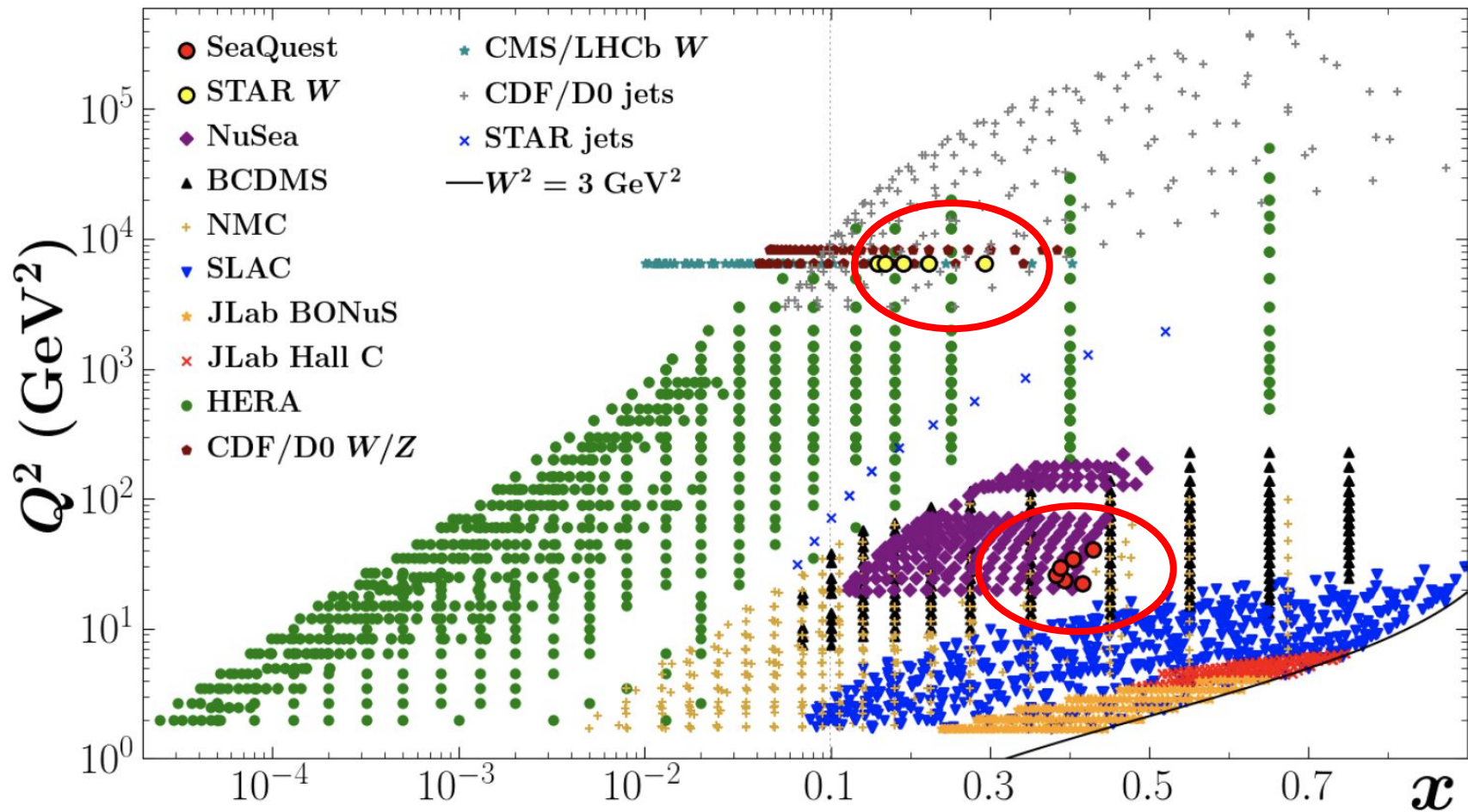


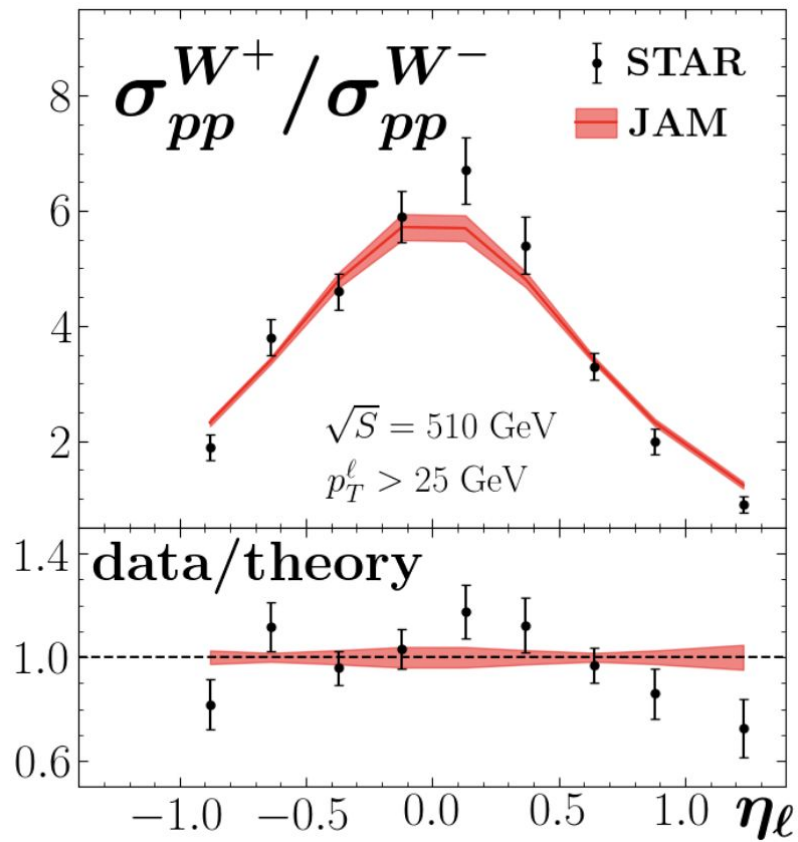
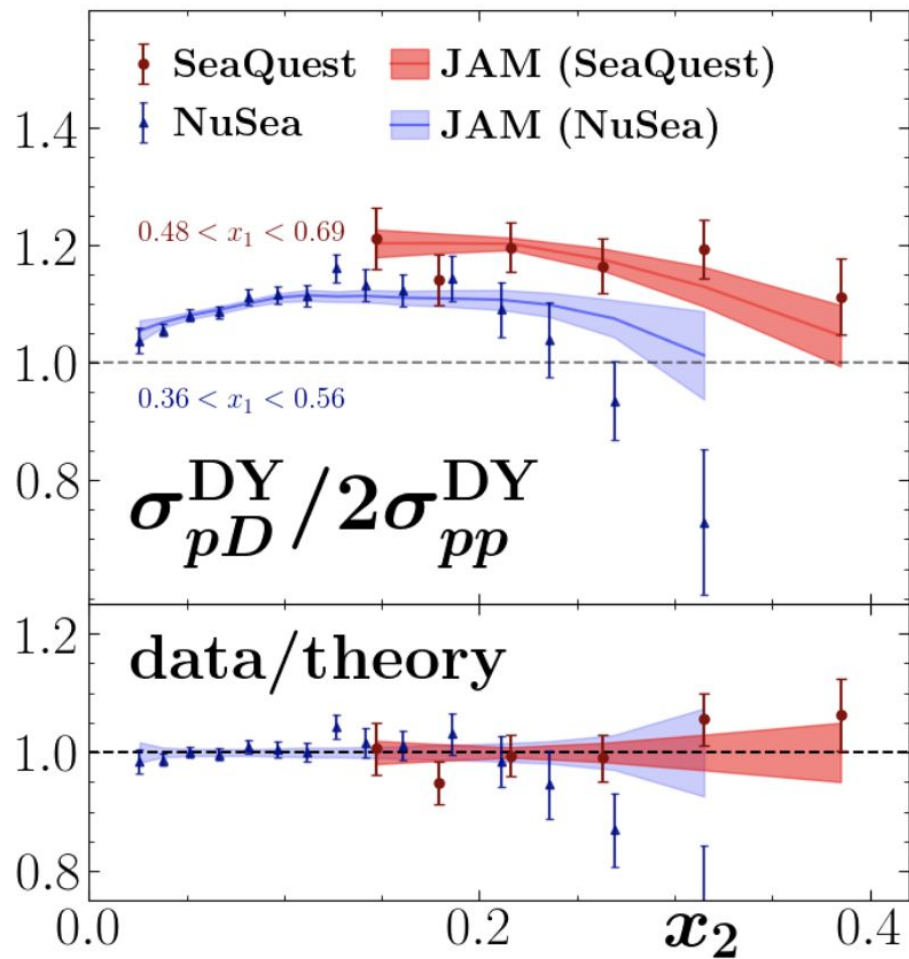
Measurement of  $w$  and  $Z/\gamma^*$  cross sections and their ratios in  
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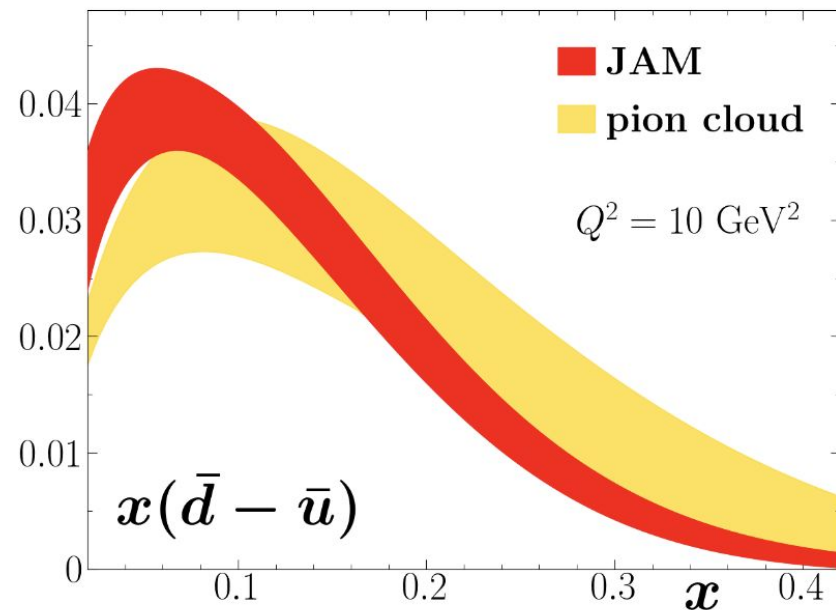
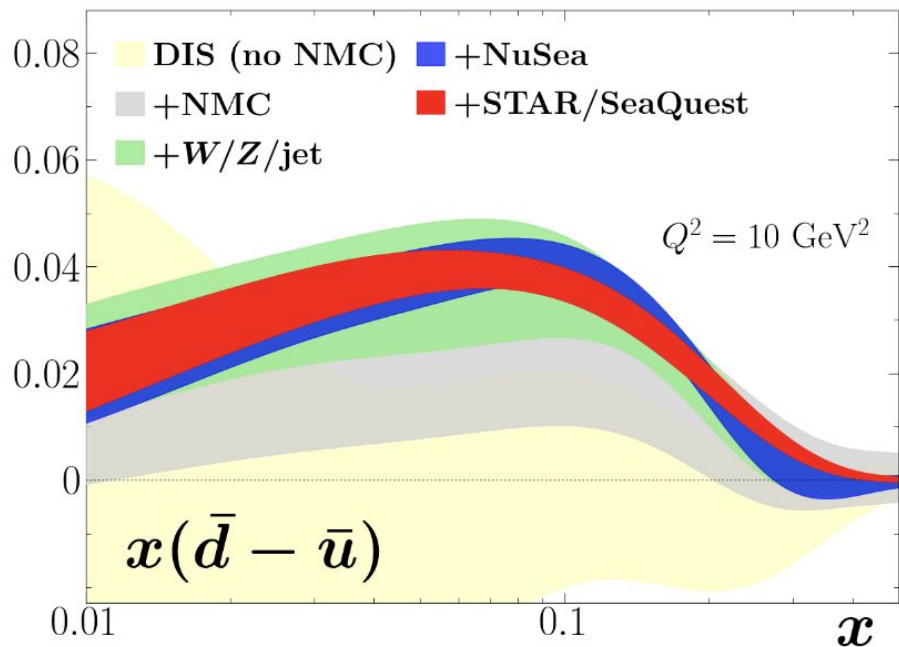
Phys. Rev. D **103**, 012001 – Published 4 January 2021







# The historical progression of sea asymmetry



$$(\bar{d} - \bar{u})(x) = [(f_{n\pi^+} + f_{\Delta^0\pi^+} - f_{\Delta^{++}\pi^-}) \otimes \bar{q}_v^\pi](x)_{25}$$

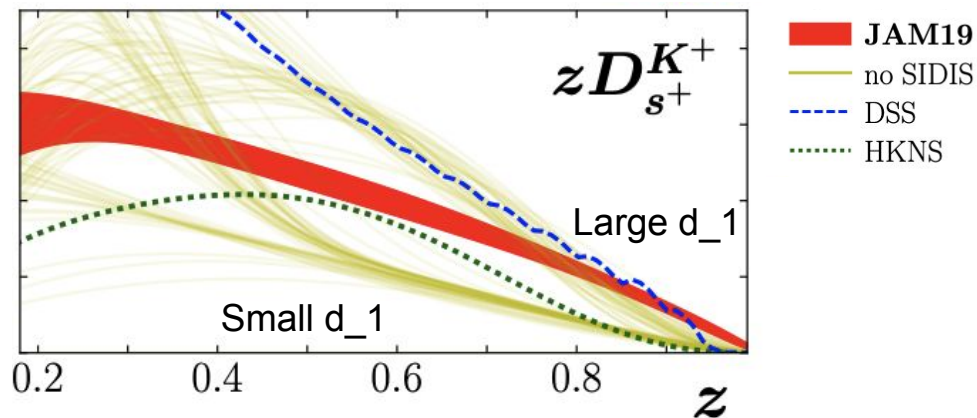
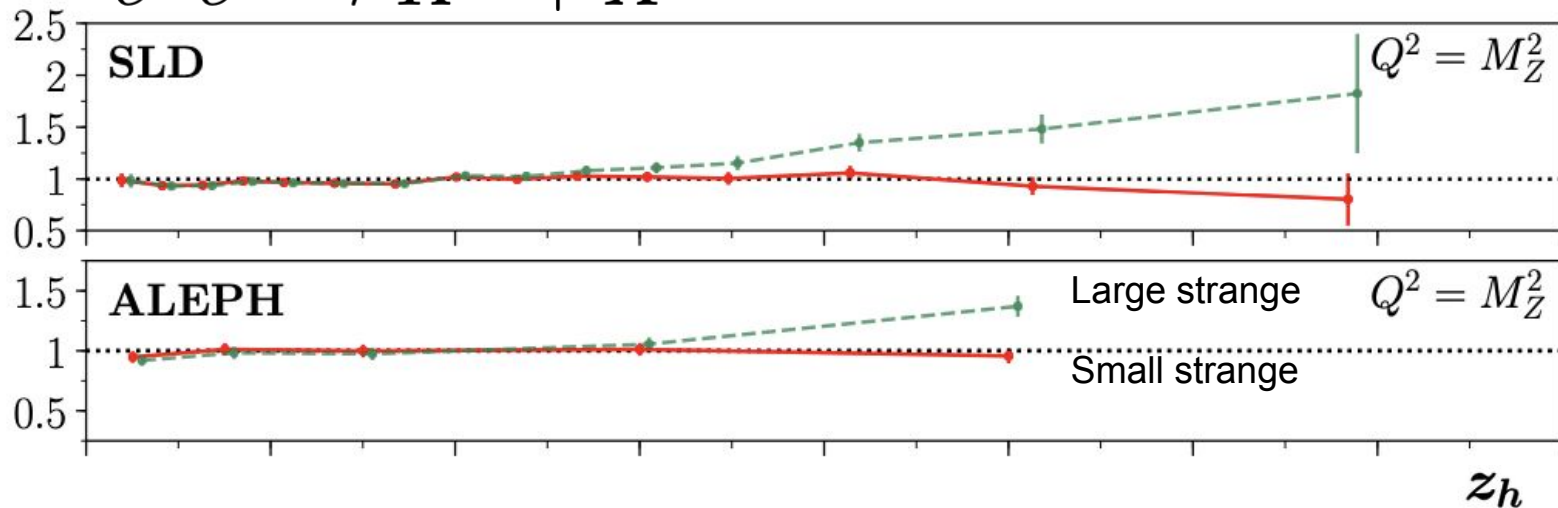
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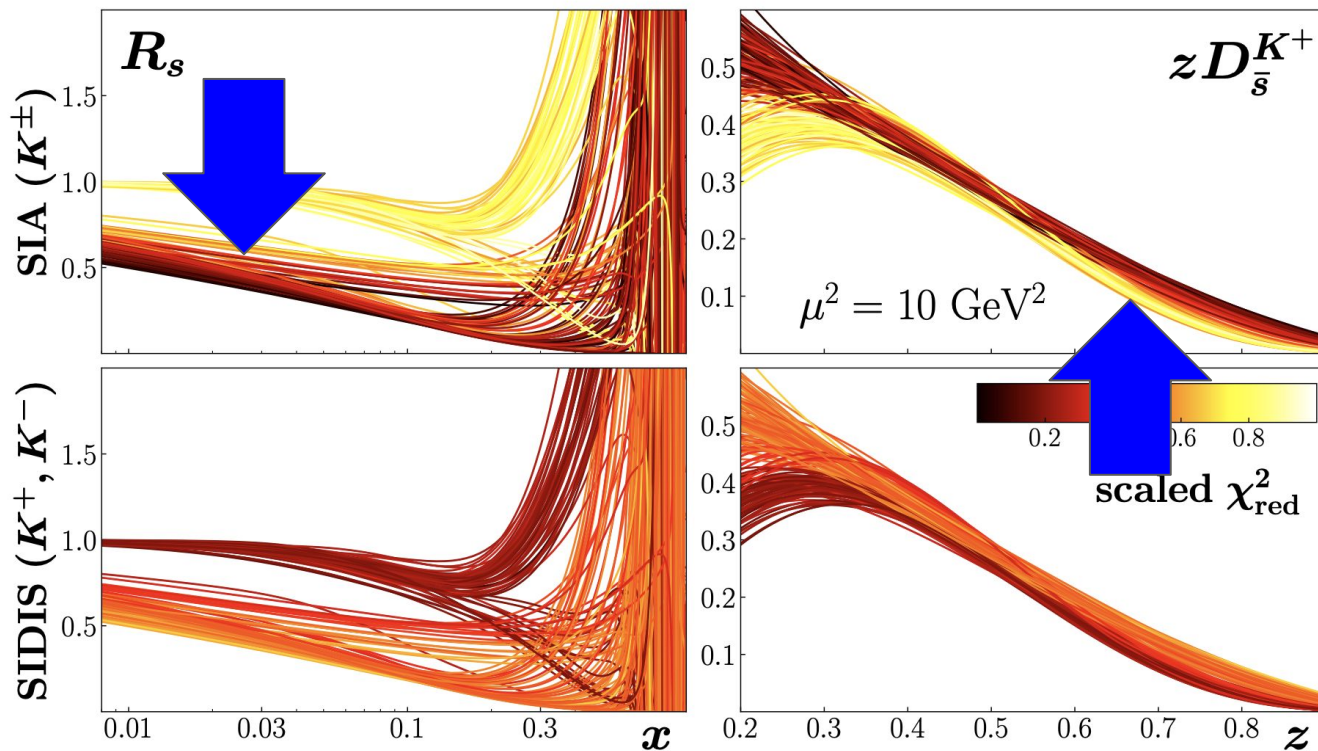
$$e^+e^- \rightarrow K^\pm + X$$

data/theory



- LEP kaon data disfavor small  $s \rightarrow K$  fragmentation
- SIDIS data compensate large strange FF by suppressing strange PDF





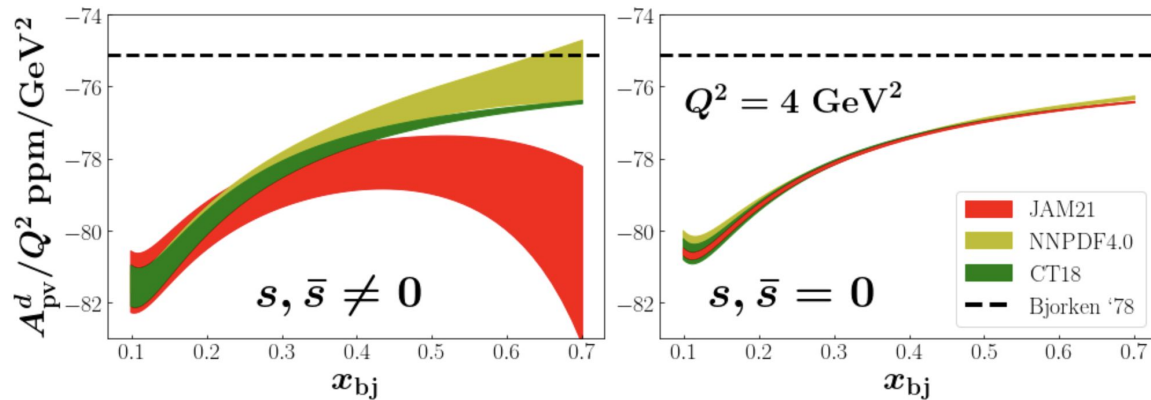
### Bottom line:

Simultaneous analysis suggests a strong strange suppression, and differs from other global analyses using LHC data alone

# Strangeness & Apv deuteron

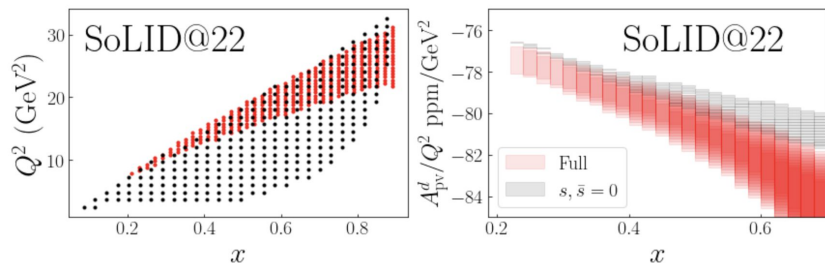
$$\left. \frac{A^{eD}}{Q^2} \right|_{y=0} = -\frac{3G}{10\pi\alpha\sqrt{2}} \left[ 2\epsilon_{AV}(e,u)(1 + \frac{3}{10}\delta) - \epsilon_{AV}(e,d)(1 - \frac{6}{5}\delta) \right].$$

Bjorken '78

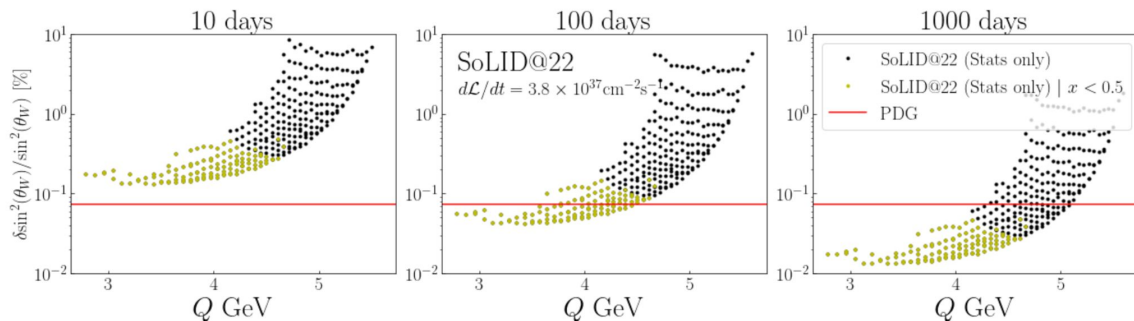
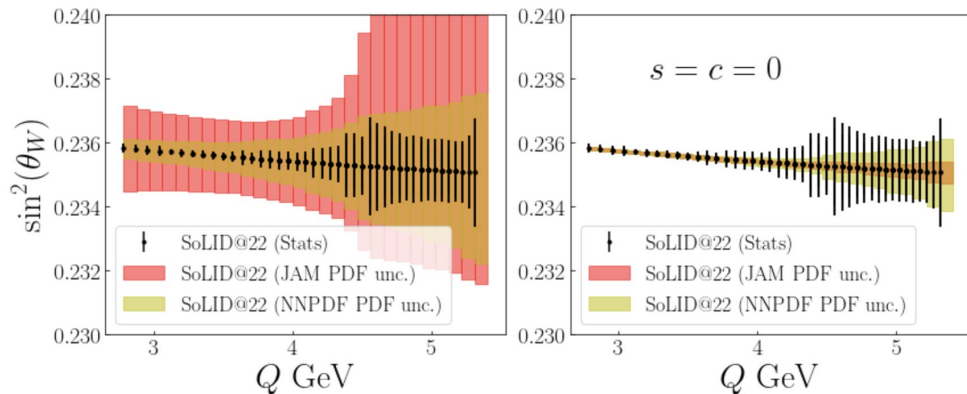


- Apv on deuteron has the opportunity to access directly Weinberg angle
- However, limited knowledge of strange quark PDF induces larger uncertainties for  $\sin^2\theta_w$  from Apv D
- On the other hand, under the SM hypothesis, Apv D can explore strangeness in the large- $x$  region

# Strangeness & Apv deuteron @ JLab++



- Apv D has significant constraining power on strange PDF → tested on two PDFs sets (JAM, NNPDF)
- Luminosity is critical to discover how strange the proton is!



- If strangeness is constrained elsewhere (LQCD, other HEP observables), high luminosity Apv D will deliver precision EW measurements

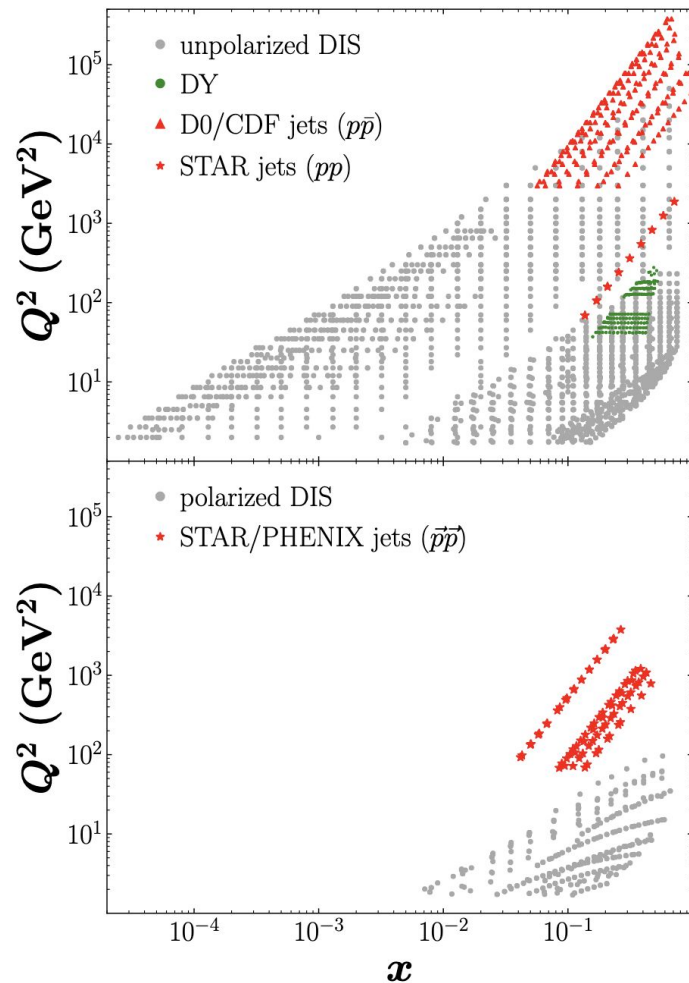
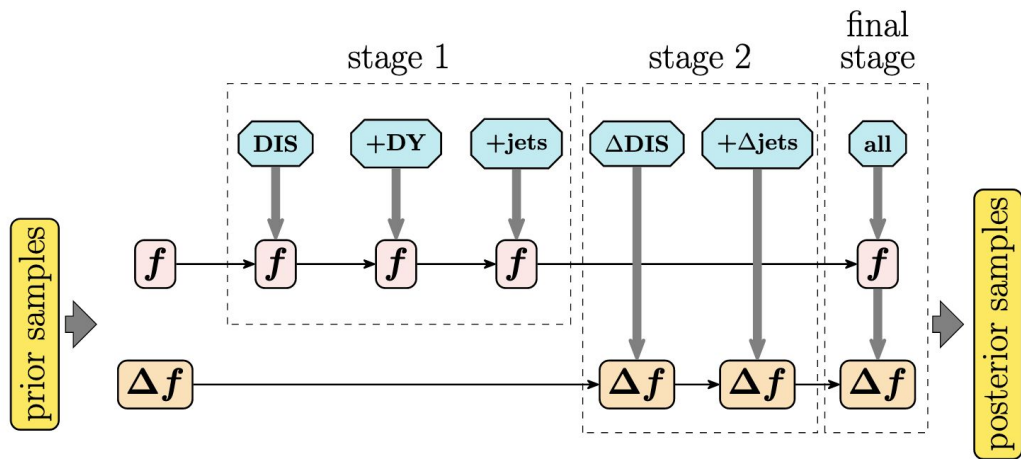
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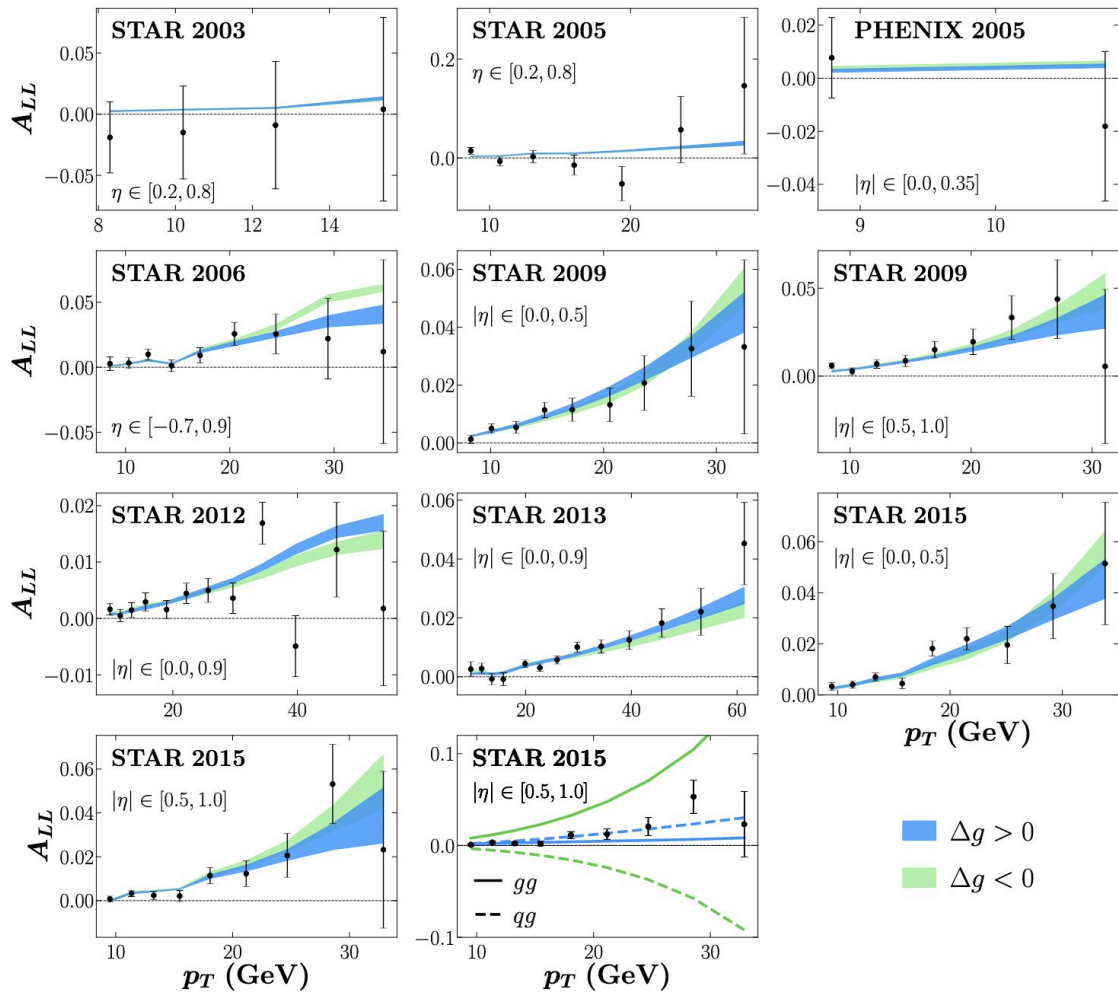
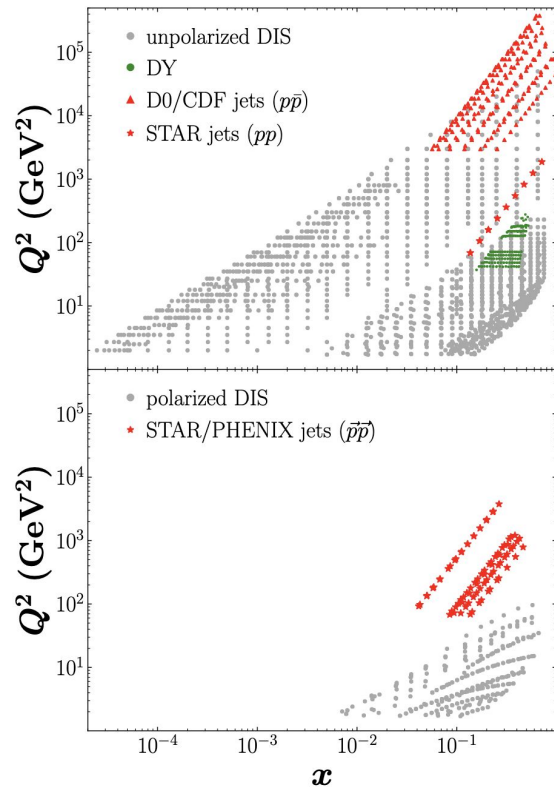
# How well do we know the gluon polarization in the proton?

Y. Zhou, N. Sato, and W. Melnitchouk (Jefferson Lab Angular Momentum (JAM) Collaboration)

Phys. Rev. D **105**, 074022 – Published 25 April 2022



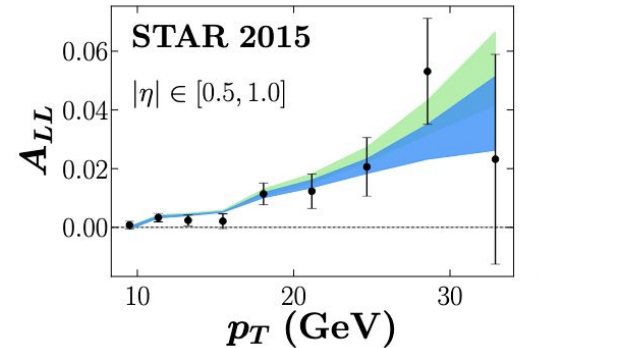
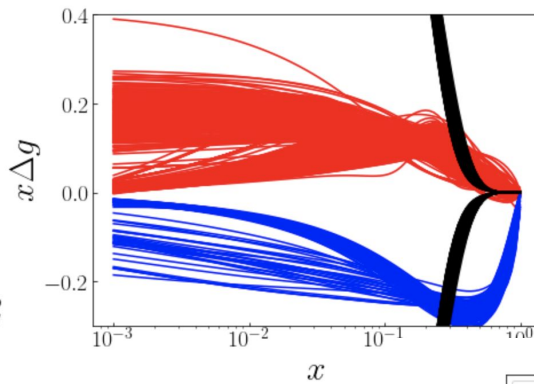
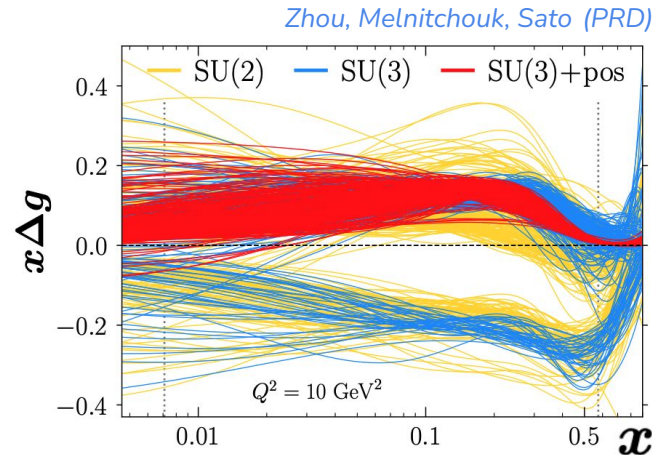
# Polarized jets



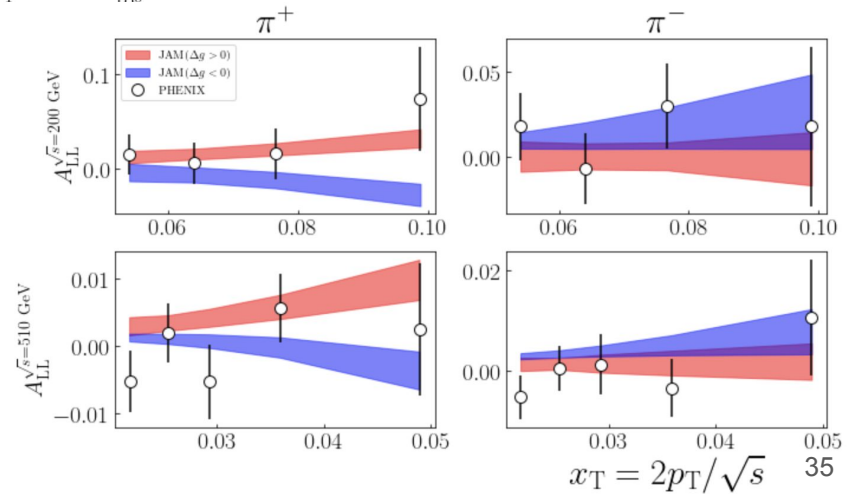
Negative gluon polarization?

$$\int_{0.05}^1 dx \Delta g(x) = \begin{array}{ll} 0.23 \pm 0.03 & \text{pos} \\ -0.62 \pm 0.03 & \text{neg} \end{array}$$

$\Delta g > 0$   
 $\Delta g < 0$



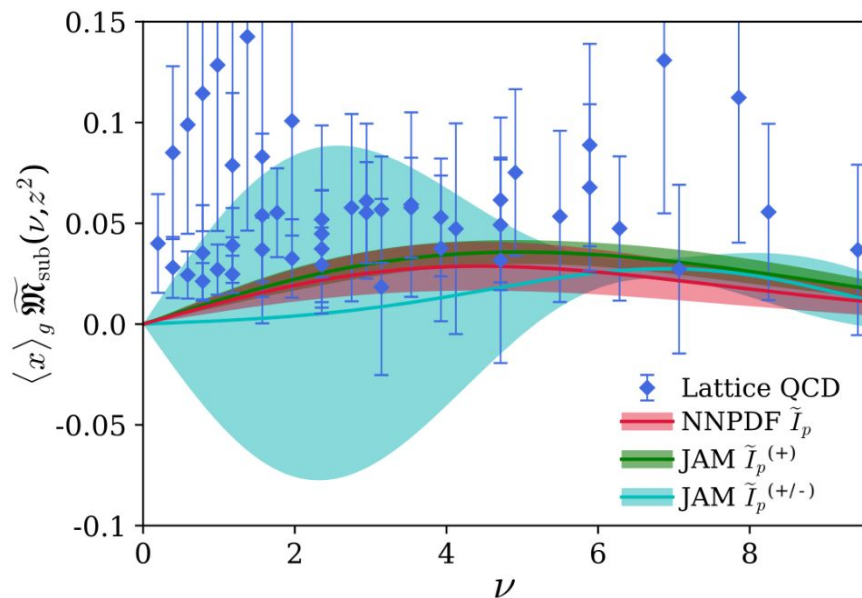
- Inclusion of RHIC polarized jet data allows both positive and negative gluon helicity solutions (in absence of positivity constraints on unpolarized gluon PDF)
- PHENIX has attempted to have empirical confirmation of gluon helicity sign (PRD102.032001, PRD91.032001)
- *Gluon helicity currently not as well constrained as was believed (independent of theory bias)*



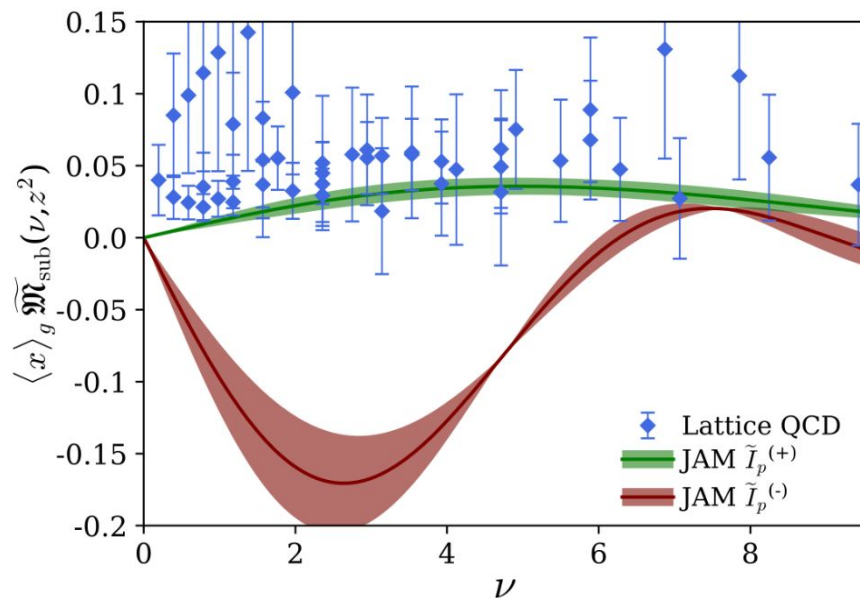


# Insights from LQCD

Egerer et al ('22)

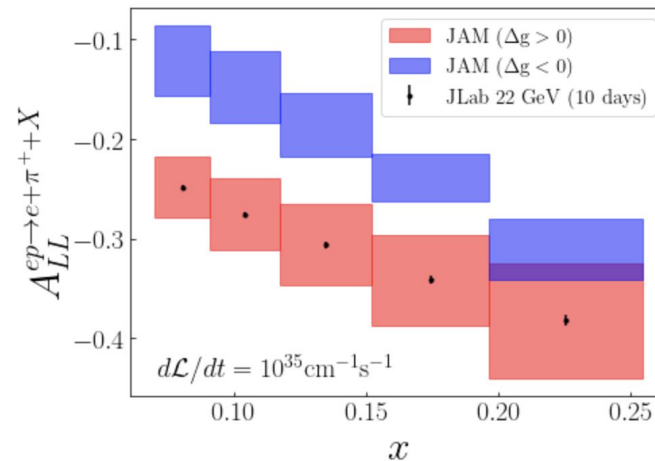
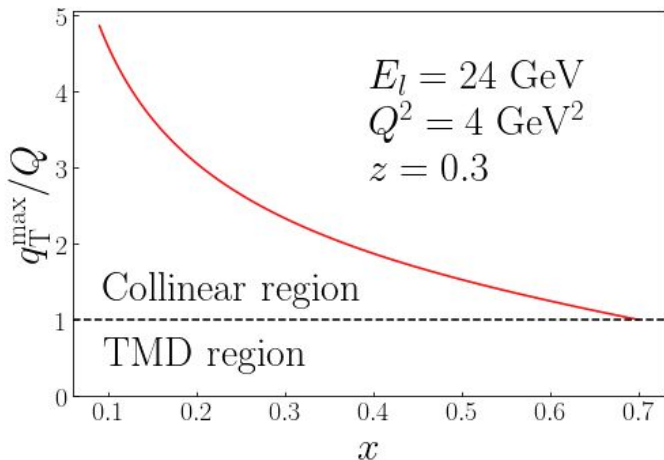
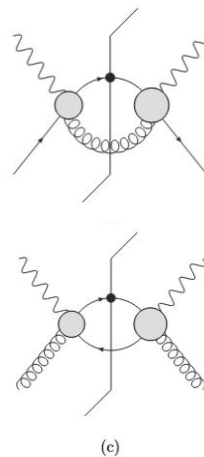
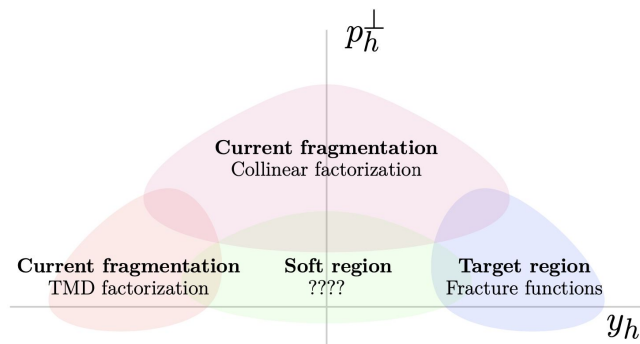


*HadStruc Collaboration*



Negative gluon helicity is ruled out by LQCD?

# Gluon helicity @ JLab++



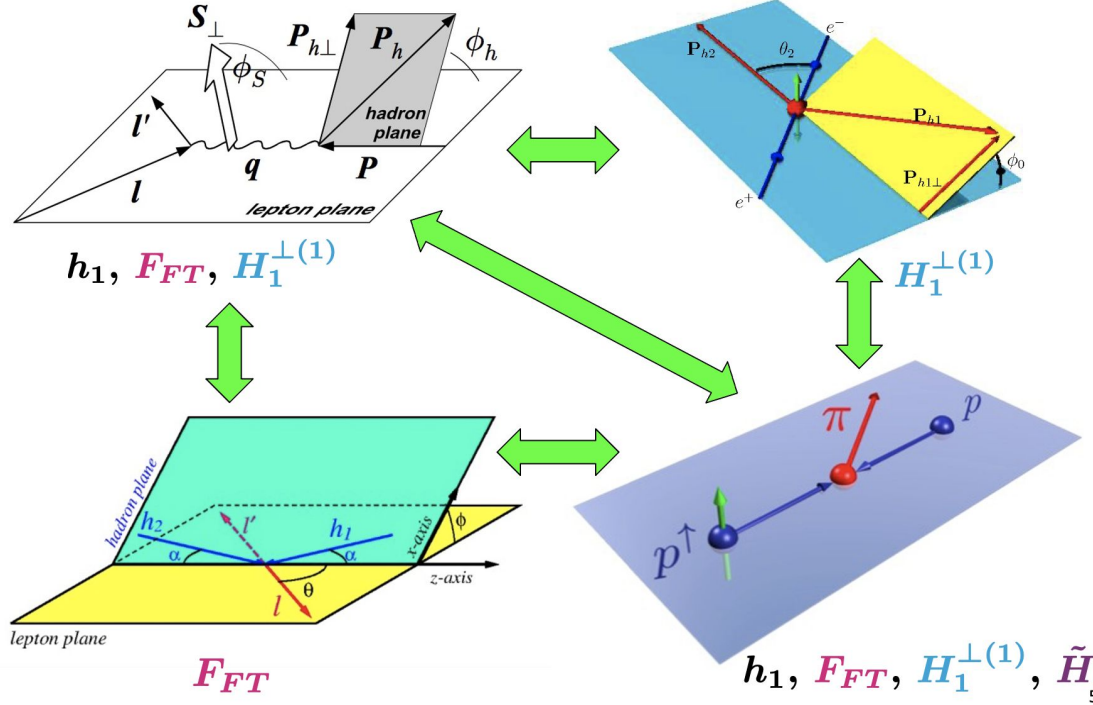
- Hadron production with large transverse momentum has an opportunity to discriminate the sign of gluon polarization
- For JLab 22 as well as EIC, there would be plenty of phase space to use collinear factorization
- More dedicated studies are on the way

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# Global analysis of SSA (TMD + CT3)

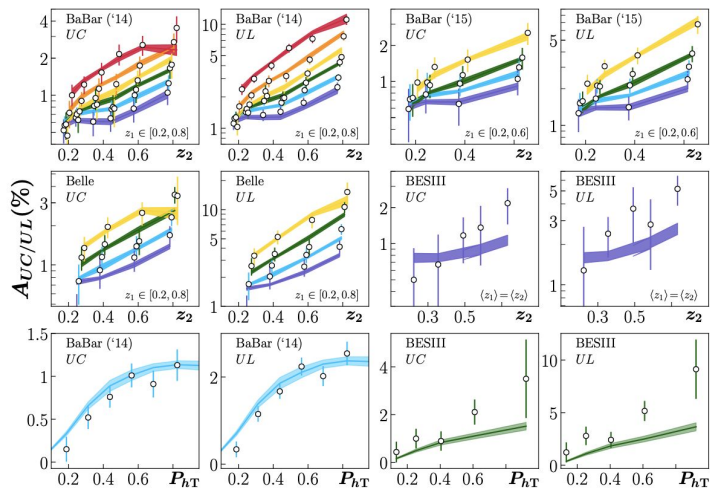
Cammarota et al ('20)



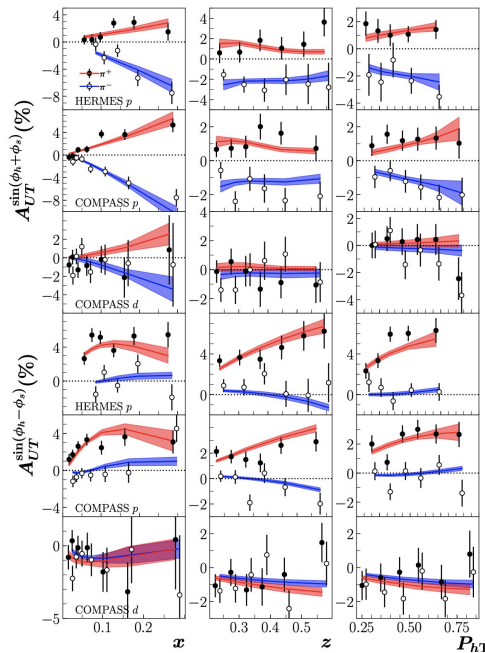
- Framework based on parton model approach to TMDs
- First steps to test universality of the combined TMD and CT3 framework
- Future analysis can build upon this work by implementing proper TMD evolution

# Data vs theory...

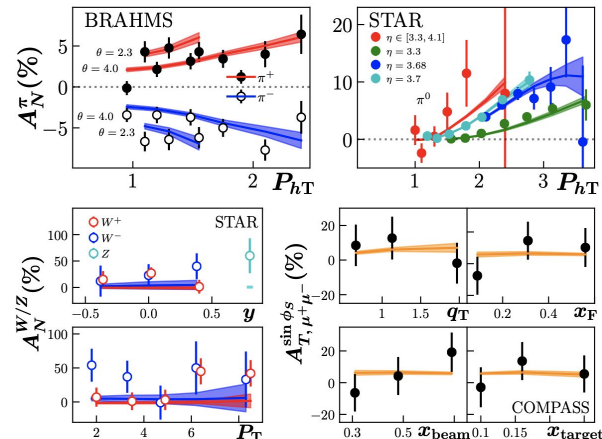
SIA



SIDIS



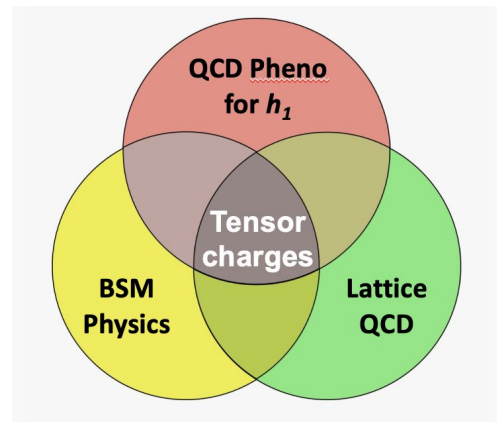
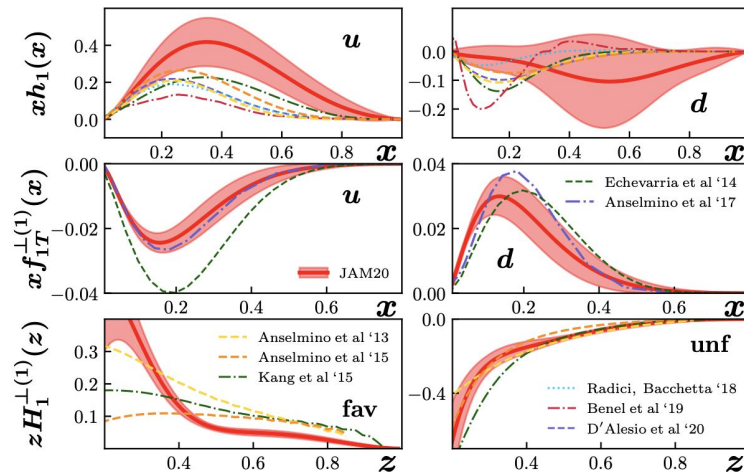
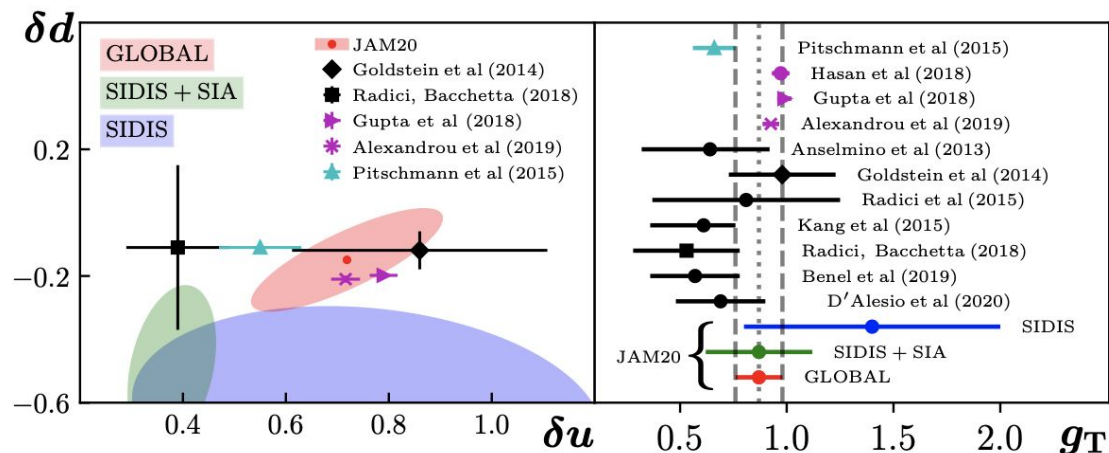
A\_N in p+p / pi + p



Observable	Reactions	Non-Perturbative Function(s)	$\chi^2/N_{\text{pts.}}$	Refs.
$A_{\text{SIDIS}}^{\text{Siv}}$	$e + (p, d)^\uparrow \rightarrow e + (\pi^+, \pi^-, \pi^0) + X$	$f_{1T}^\perp(x, k_T^2)$	$150.0/126 = 1.19$	[65, 66, 68]
$A_{\text{SIDIS}}^{\text{Col}}$	$e + (p, d)^\uparrow \rightarrow e + (\pi^+, \pi^-, \pi^0) + X$	$h_1(x, k_T^2), H_1^\perp(z, z^2 p_\perp^2)$	$111.3/126 = 0.88$	[66, 68, 71]
$A_{\text{SIA}}^{\text{Col}}$	$e^+ + e^- \rightarrow \pi^+ \pi^- (\text{UC}, \text{UL}) + X$	$H_1^\perp(z, z^2 p_\perp^2)$	$154.5/176 = 0.88$	[74–77]
$A_{\text{DY}}^{\text{Siv}}$	$\pi^- + p^\uparrow \rightarrow \mu^+ \mu^- + X$	$f_{1T}^\perp(x, k_T^2)$	$5.96/12 = 0.50$	[73]
$A_{\text{DY}}^{\text{Siv}}$	$p^\uparrow + p \rightarrow (W^+, W^-, Z) + X$	$f_{1T}^\perp(x, k_T^2)$	$31.8/17 = 1.87$	[72]
$A_N^h$	$p^\uparrow + p \rightarrow (\pi^+, \pi^-, \pi^0) + X$	$h_1(x), F_{FT}(x, x) = \frac{1}{\pi} f_{1T}^{\perp(1)}(x), H_1^{\perp(1)}(z)$	$66.5/60 = 1.11$	[7, 9, 10, 13]

# Extraction of tensor charges

- Empirical confirmation that tensor charges inferred from data agree with LQCD within uncertainties
- In this work, Soffer bounds were not imposed

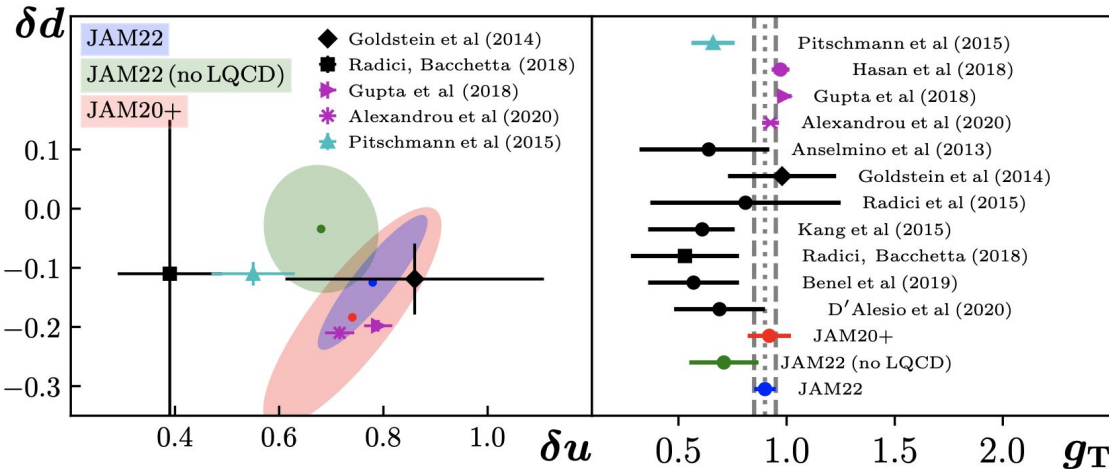
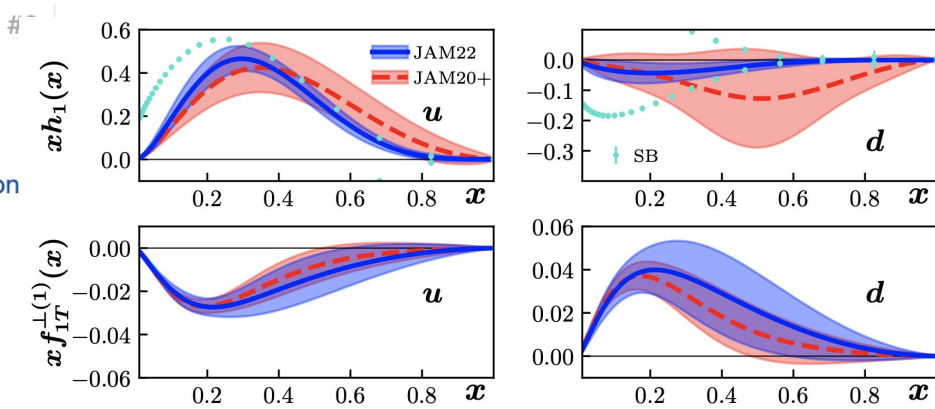




# Updated QCD global analysis of single transverse-spin asymmetries I: Extracting $\tilde{H}$ , and the role of the Soffer bound and lattice QCD

Leonard Gamberg (Penn State U., Berks-Lehigh Valley), Michel Malda (Lebanon Valley Coll.), Joshua A. Miller (Lebanon Valley Coll. and Temple U.), Daniel Pitonyak (Lebanon Valley Coll.), Alexei Prokudin (Penn State U., Berks-Lehigh Valley and Jefferson Lab) et al. (May 2, 2022)

e-Print: 2205.00999 [hep-ph]



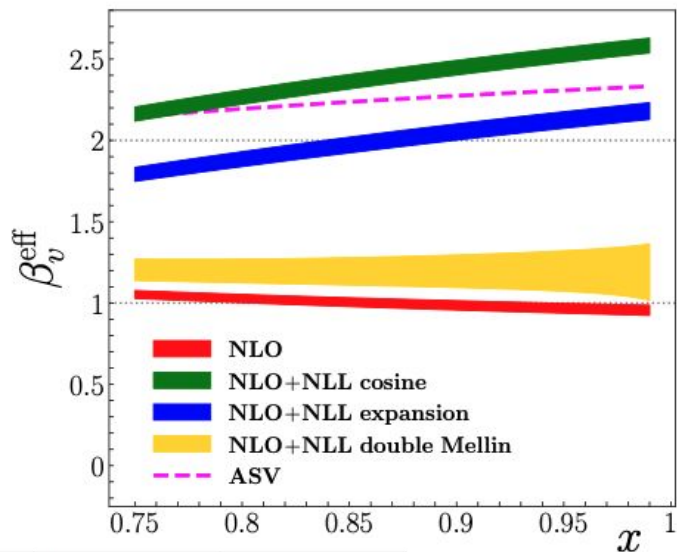
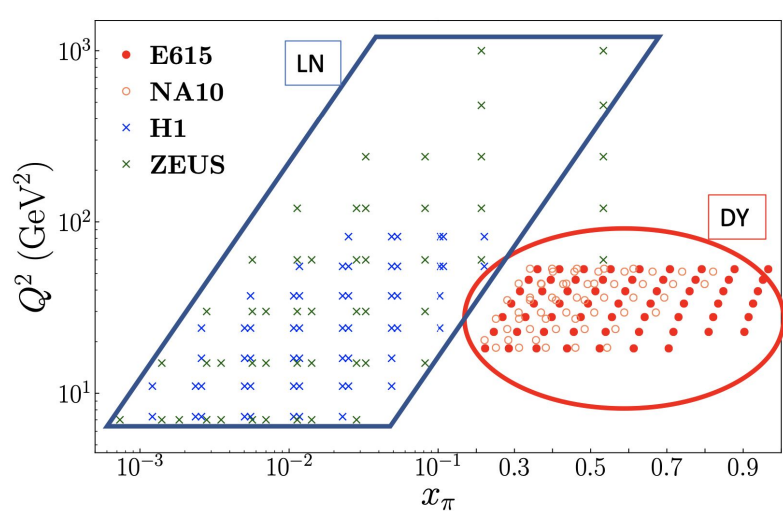
- Updated HERMES data with the recent multi-dimensional bins
- Inclusion of Soffer bounds and lattice tensor charges does not spoil universal agreement



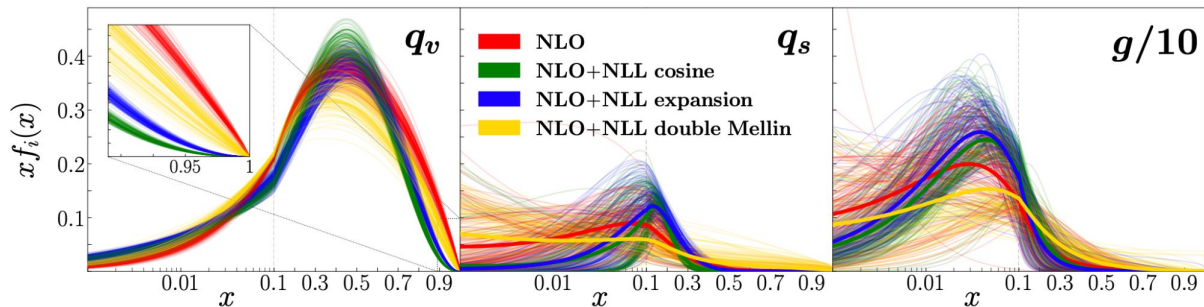
# Outline

1. Isovector EMC effect with MARATHON data
2. Sea asymmetry with SeaQuest and STAR data
3. Strange suppression from simultaneous analysis of PDFs and FFs
4. Gluon polarization in the proton
5. Origin of single transverse-spin asymmetries in high-energy collisions
6. Meson structure

# Pion pdfs with DY threshold resummation



Barry, Ji, Melnitchouk,  
Sato ('21)



The large- $x$  asymptote of pion PDFs are more consistent with 1, despite expectation from QCD models

# Summary/Outlook

New era of global analysis of hadron structure → new tools, new tricks  
(theory + experiment + data analysis)

Simultaneous extraction paradigm is important for proper UQ

Need for new observables to be included global analysis



## JAM collaboration

### **Staff / Faculty**

W. Melnitchouk (JLab), T. Rogers (ODU/JLab),  
A. Prokudin (PSU), D. Pitonyak (LVC), L. Gamberg (PSU), Z. Kang (UCLA) J. Qiu (JLab), A. Accardi (Hampton/JLab), A. Metz (Temple), C.-R. Ji (NCSU),  
M. Constantinou (Temple), F. Steffens (Bonn),  
Y. Kovchegov (OSU), M. Sievert (NMSU), I. Cloet (ANL),

### **Students / Postdocs**

R. Abdul Khalek (JLab), C. Cocuzza (Temple), Y. Zhou (South China Normal University),  
P. Barry (JLab), E. Moffat (ANL), D. Adamiak (OSU), A. Freese (WU).

$$\mathcal{L}_{\text{QCD}} = \sum_q \bar{\psi}_q (i\gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{2} \text{Tr}[G_{\mu\nu} G^{\mu\nu}]$$