Measurement of Event Shape Observables with H1 at HERA

Henry Klest for the H1 Collaboration

CFNS NP-QCD Workshop, Sept. 21, 2022

H1prelim-21-032 – Triple-differential 1-Jettiness
H1prelim-22-033 – Groomed Event Shapes

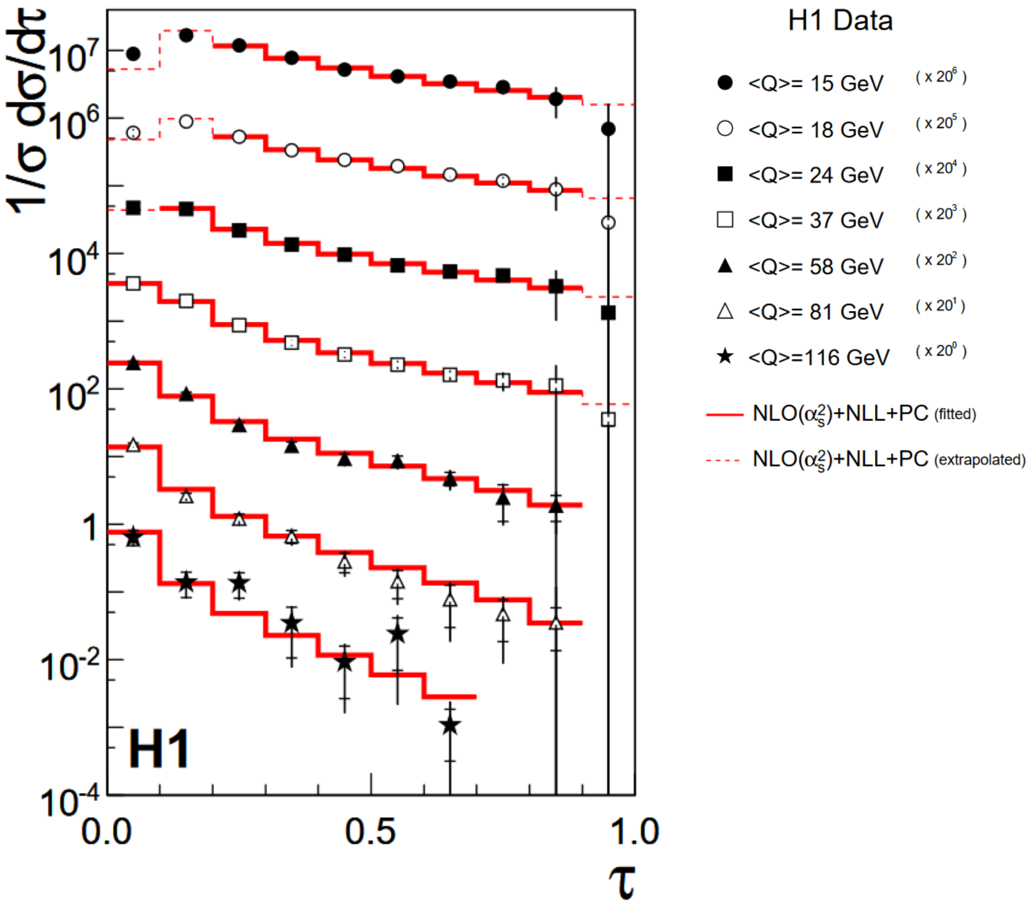
More results than I have time to discuss here, ask me about them!

FAR BEYOND

Event Shapes

$$\tau = 1 - T \quad \text{with} \quad T = \frac{\sum_h |\vec{p}_{z,h}|}{\sum_h |\vec{p}_h|}$$

- Inclusive observables where all particles contribute
  - E.g. Thrust – measures degree of collimation along an axis
- **Sensitive to QCD across scales**
- Calculable to high precision in perturbation theory
  - Fixed-order QCD → tail of thrust distribution
  - Soft-collinear effective theory (SCET) calculations → peak of thrust distribution
- Used extensively in e^+e^- and Breit frame e+p collisions



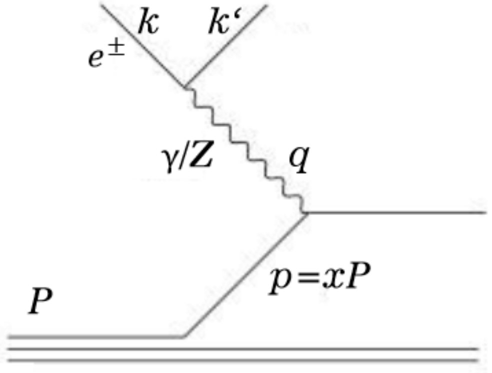
arXiv/0512014v1

Inclusive DIS & Breit Frame

$$Q^2 = -q^2 = -(k - k')^2$$

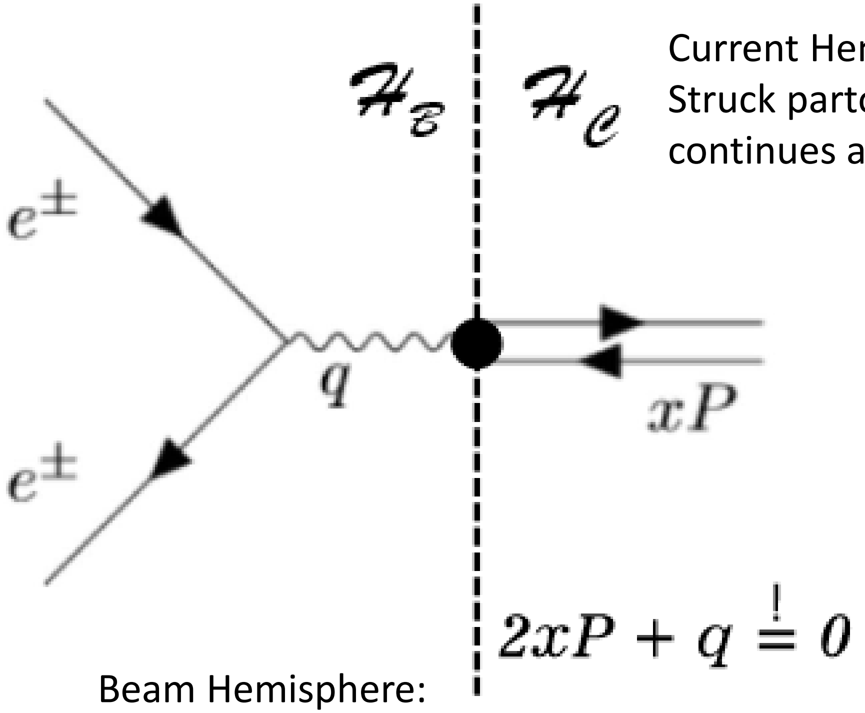
$$y = \frac{p \cdot q}{p \cdot k}$$

$$x = -\frac{q^2}{2P \cdot q} = \frac{Q^2}{2P \cdot q}$$



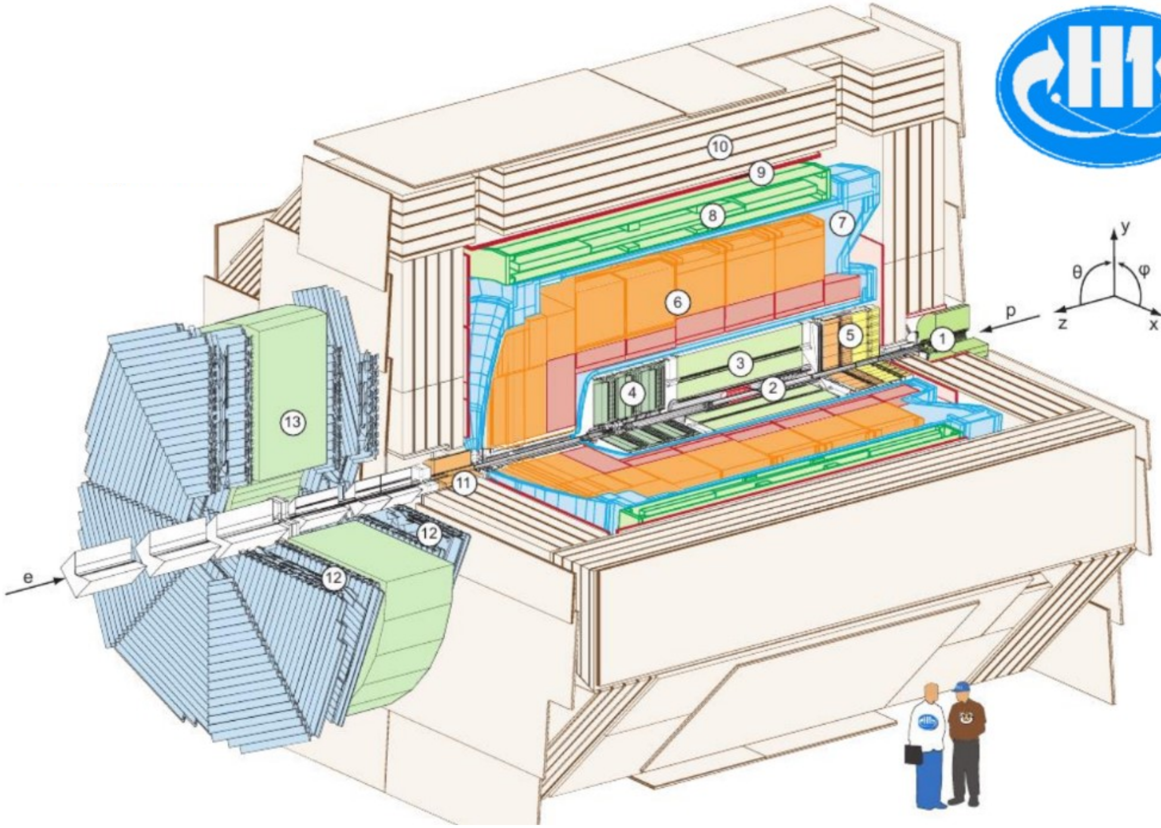
- HERA-II data
  - $Q^2 > 150$ GeV^2, $0.2 < y < 0.7$
  - No direct $x_{Bj.}$ cut applied
  - 352 pb^{-1} collected
- Breit Frame
  - Defined as the frame where $2x_{Bj.}P + q = 0$
    - Divides event into two hemispheres: "beam"/"remnant"/"target" hemisphere and "current"/"struck parton" hemisphere
  - Exchanged boson reverses struck parton's momentum
    - Parton has $\overrightarrow{xP}$ incoming, -$\overrightarrow{xP}$ outgoing

Current Hemisphere: Struck parton continues at η = -∞



Beam Hemisphere: Proton remnant continues at η = ∞

H1 Detector



- HERA
  - World's only high energy electron-proton collider

$E_e = 27.6\ \text{GeV}, E_p = 920\ \text{GeV}$
$\rightarrow \sqrt{s} = 319\ \text{GeV}$

  - 352 pb^{-1} collected in HERA-II run period from 2003-2007
- H1 Experiment
  - Hermetic detector with asymmetric design
    - Drift chamber + silicon tracking
    - High-resolution LAr calorimeter
  - Trigger on high-energy hadronic or EM LAr cluster
    - > 99% efficient for $y < 0.7$

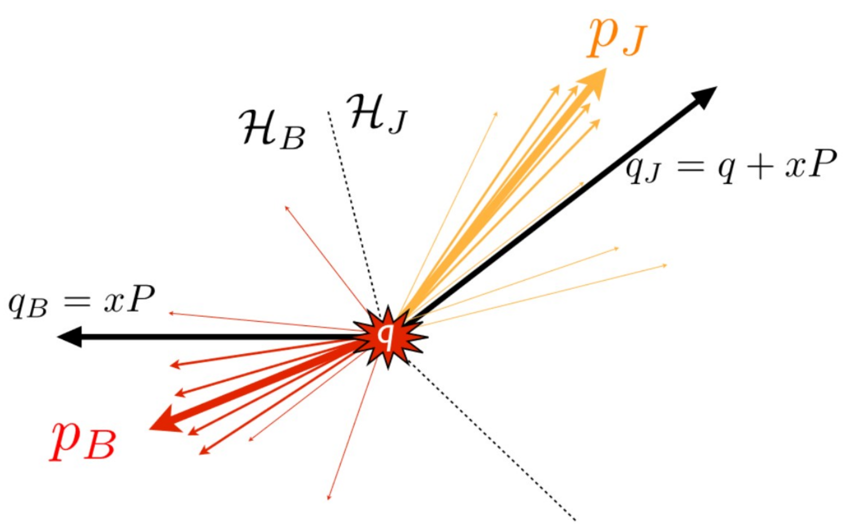
Electromagnetic part	Hadronic part
10 to 100 cm^2	50 to 2000 cm^2
20 to 30 X_0 (30784)	4.7 to 7 λ_{abs} (13568)
$\approx 11\%/\sqrt{E_e} \oplus 1\%$	$\approx 50\%/\sqrt{E_h} \oplus 2\%$

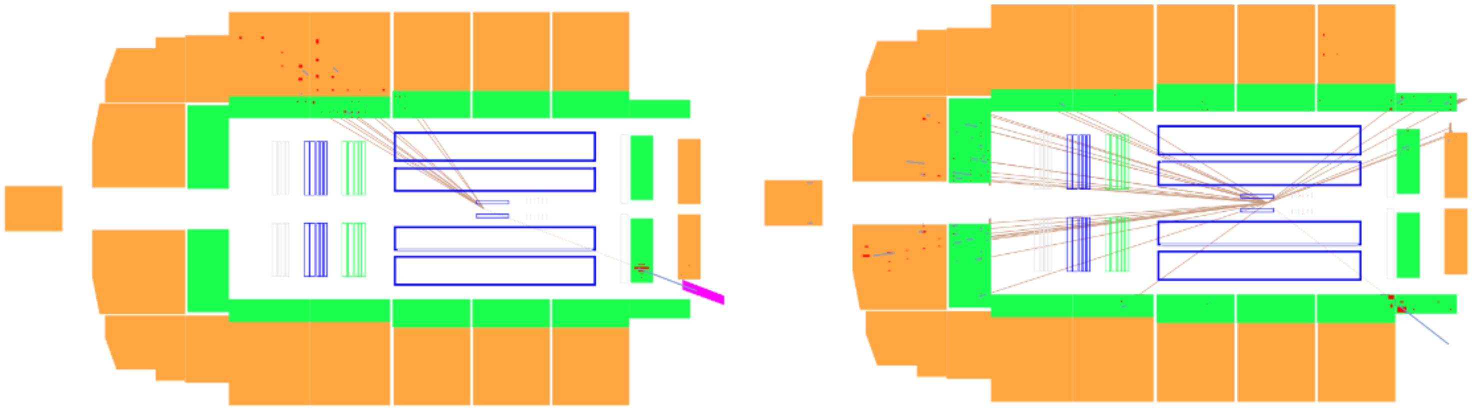
H1 LAr Calorimeter Specifications

1-Jettiness Event Shape

- Sum of four-vector dot product of final state particles with virtual boson axis or beam axis

$$\tau_1 \equiv \frac{2}{Q^2} \sum_{i \in X} \min\{q_B \cdot p_i, q_J \cdot p_i\}$$

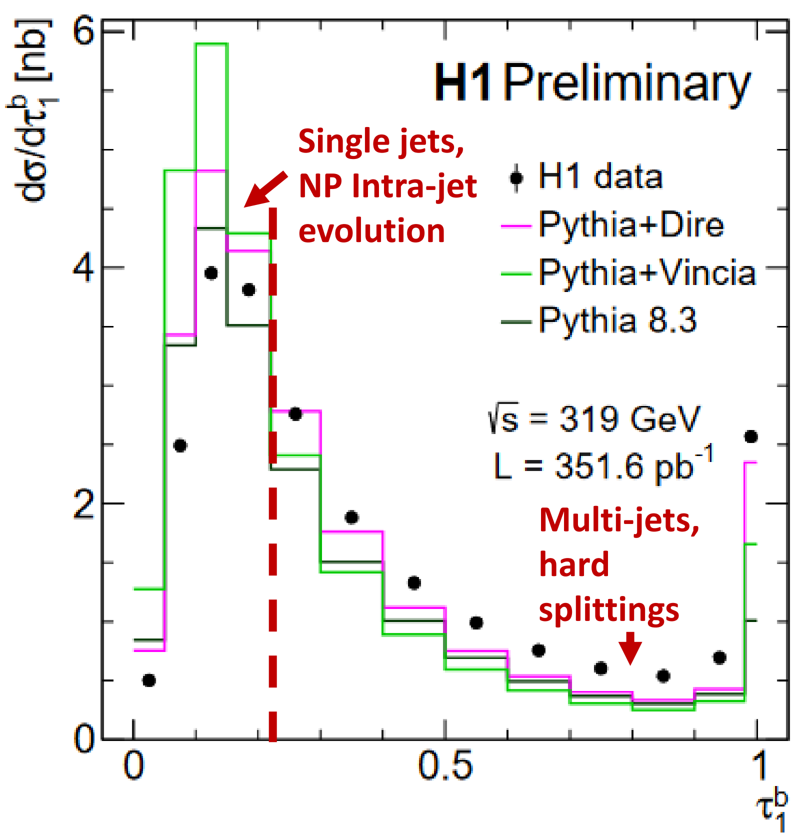




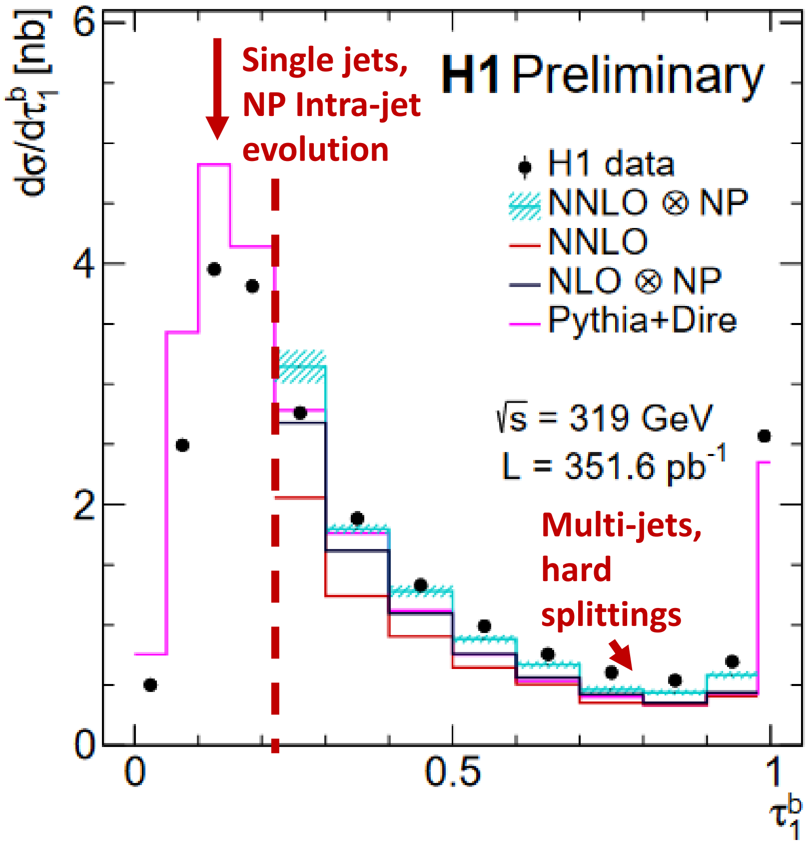
- DIS 1-jet configuration
- Most HFS particles collinear to scattered parton
  $\rightarrow$ Small τ_1^b

- Dijet event
- More and larger contributions to the sum over the HFS
  $\rightarrow$ Large τ_1^b

- Parton shower model comparison
  - Peak region highly sensitive to different showering
  - No fully satisfactory description

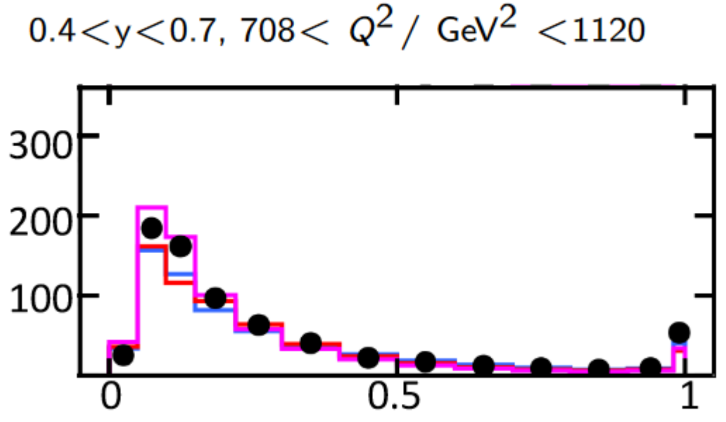


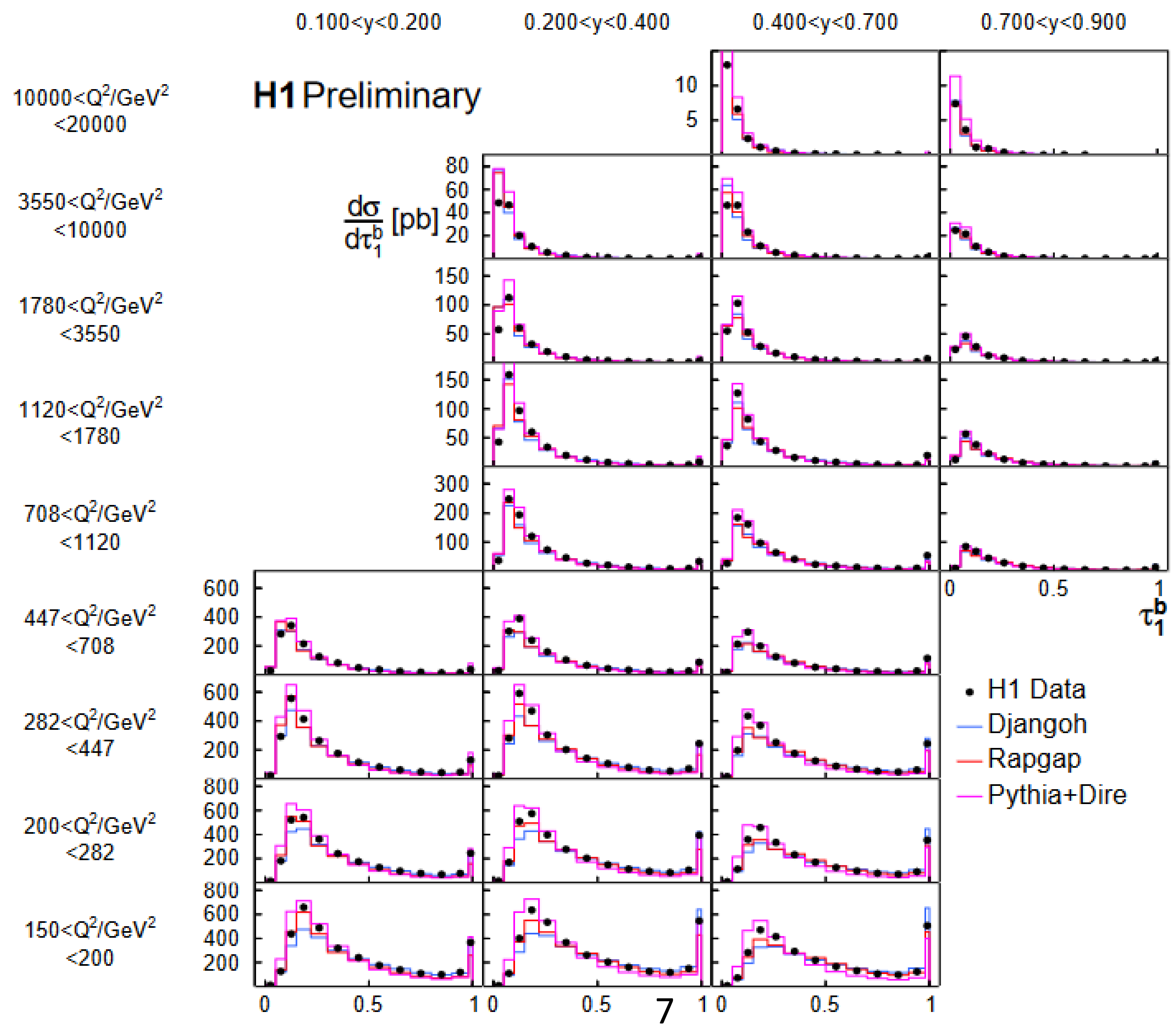
- $\gamma p \rightarrow 2\, Jets + X$ Prediction from NNLOJET
  - NP corrections from Pythia8.3
  - NNLO provides good description of tail region, improves over NLO



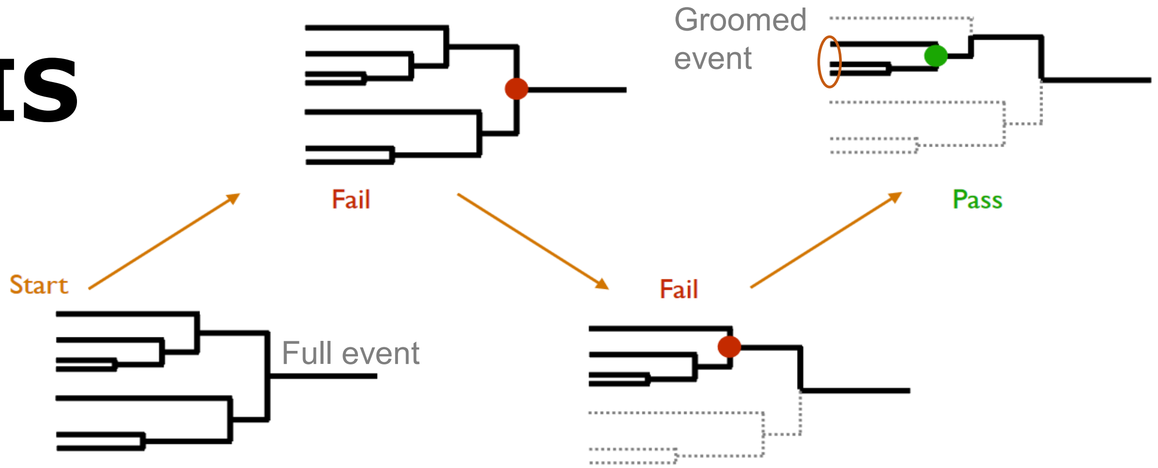
Triple-Differential Cross-Section

- With increasing Q:
  - Total cross-section decreases
  - Tail region decreases
  - Peak moves to lower τ
    - At higher momentum transfer, jets are more collimated
- With increasing y:
  - τ = 1 di-jet peak is enhanced





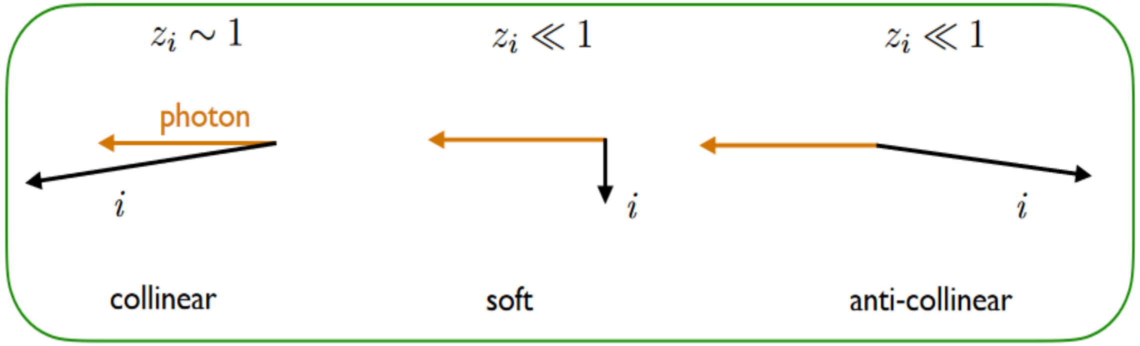
Event Grooming in DIS



- Whole event is clustered into one "jet"
- Iteratively de-cluster until grooming condition is passed
  - Analogous to Soft Drop in p+p
- Groomed events are similar to groomed jets!

$$z_i = \frac{P \cdot p_i}{P \cdot q} \xrightarrow[\text{frame}]{\text{Breit}} z_i = n \cdot p_i / Q = p_i^+ / Q \,.$$

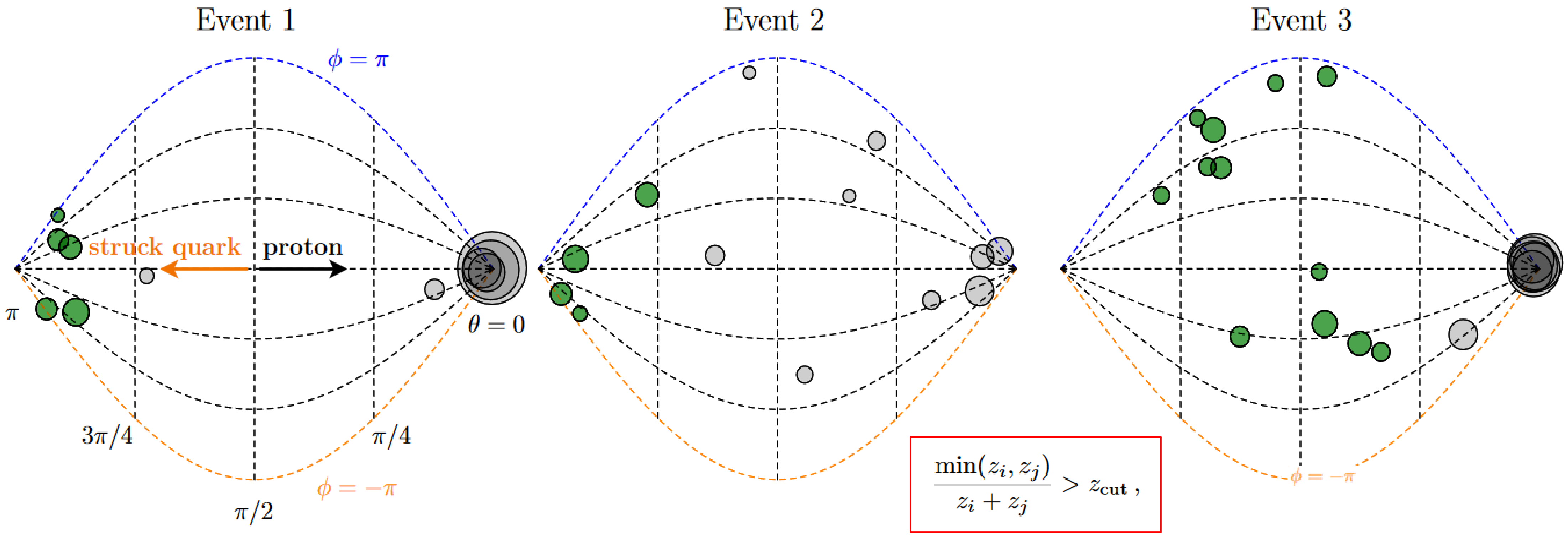
Limits (geometric interpretation in the Breit frame)



$$\frac{\min(p_{t1}, p_{t2})}{p_{t1} + p_{t2}} > z_{\text{cut}} \longrightarrow \frac{\min(z_i, z_j)}{z_i + z_j} > z_{\text{cut}}$$

p+p Soft Drop condition — DIS grooming condition

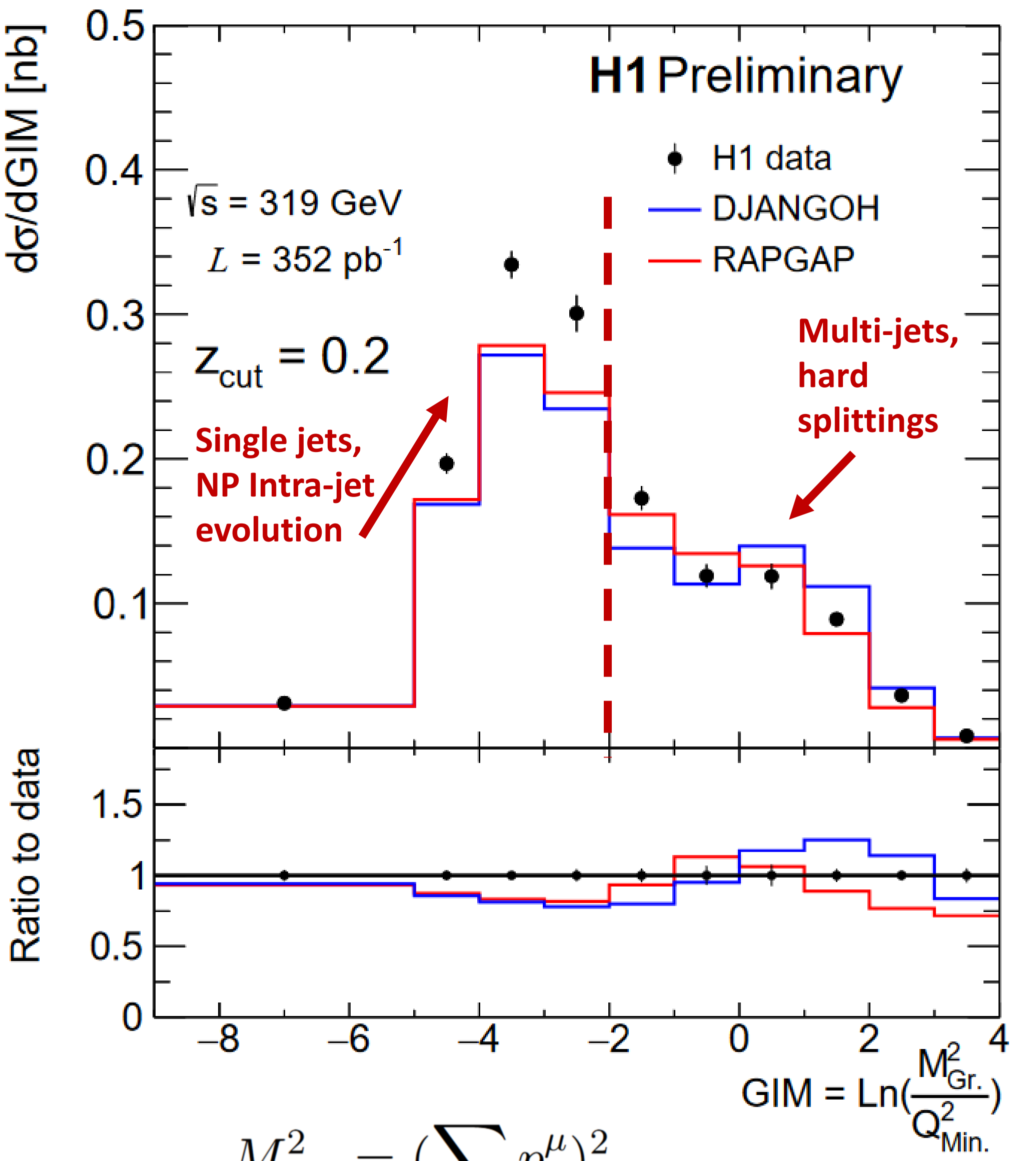
Breit Frame Event Displays

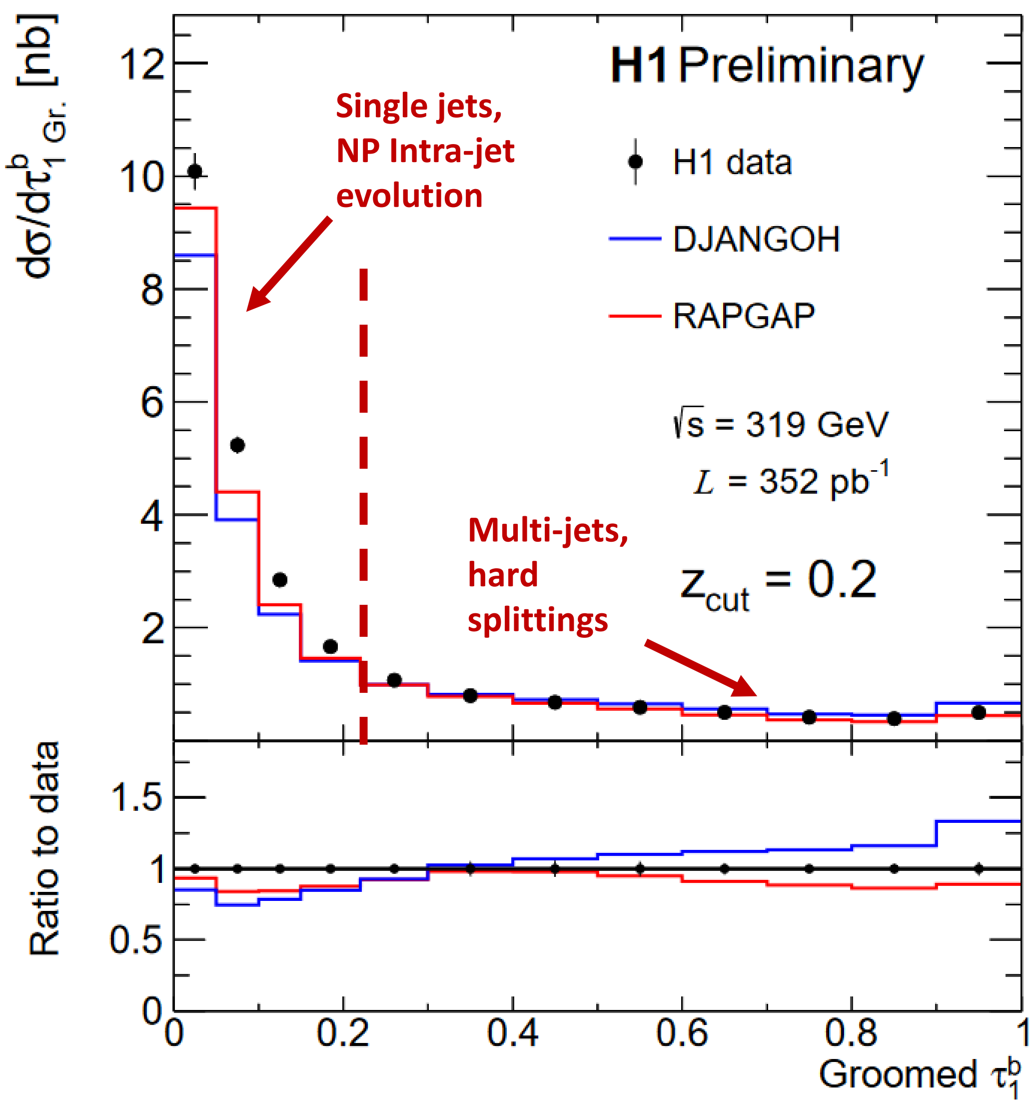


$$\frac{\min(z_i, z_j)}{z_i + z_j} > z_{\text{cut}} ,$$

Figure 2. Visualization of three PYTHIA 8 events at $\sqrt{s} = 63$ GeV and $Q \sim 10$ GeV before and after grooming. The particles in this events are represented by disks on the unfolded sphere. Green disks represent particles that pass grooming where grayed-out particles are removed from the event by the grooming procedure. For the grooming parameter we use here $z_{\text{cut}} = 0.1$

Observables

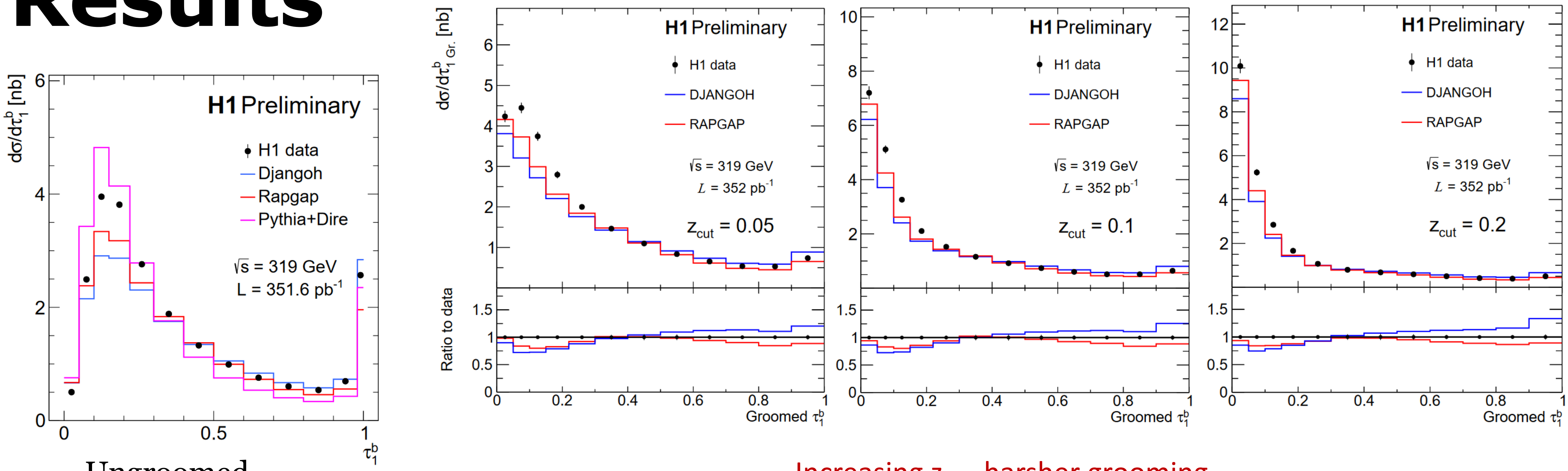




$$M^2_{Gr.} = (\sum_i p_i^\mu)^2$$

$$\tau_1 = \frac{2}{Q^2} \sum_{i \in \text{gr. ent.}} \min(q_B \cdot p_i,\, q_J \cdot p_i)$$

Results



Ungroomed

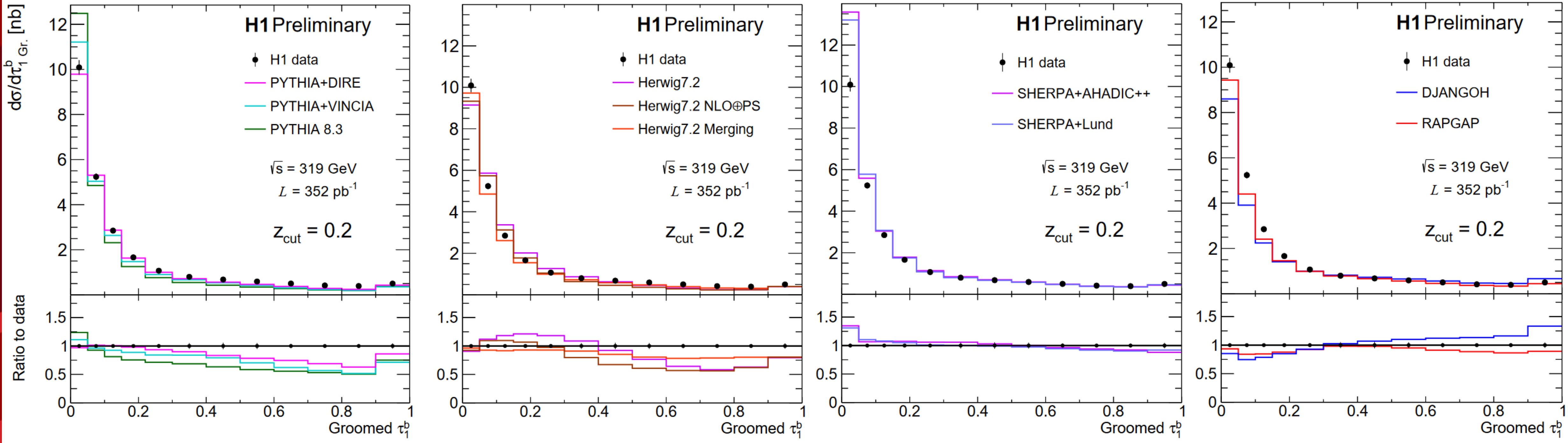
Increasing z_{cut}, harsher grooming

- RAPGAP and DJANGOH
  - Standard H1 MCs, tuned for HERA, LO CTEQ PDFs
  - Both use LEPTO for matrix elements $O(\alpha_S)$
- DJANGOH:
  - Color dipole model PS + string fragmentation
- RAPGAP:
  - DGLAP PS + string fragmentation

- Data is corrected for real QED ISR and FSR
- Uncertainty on data is statistical ⊕ systematic
  - Dominated by model uncertainty from bin-by-bin correction

Results – Groomed 1 Jettiness

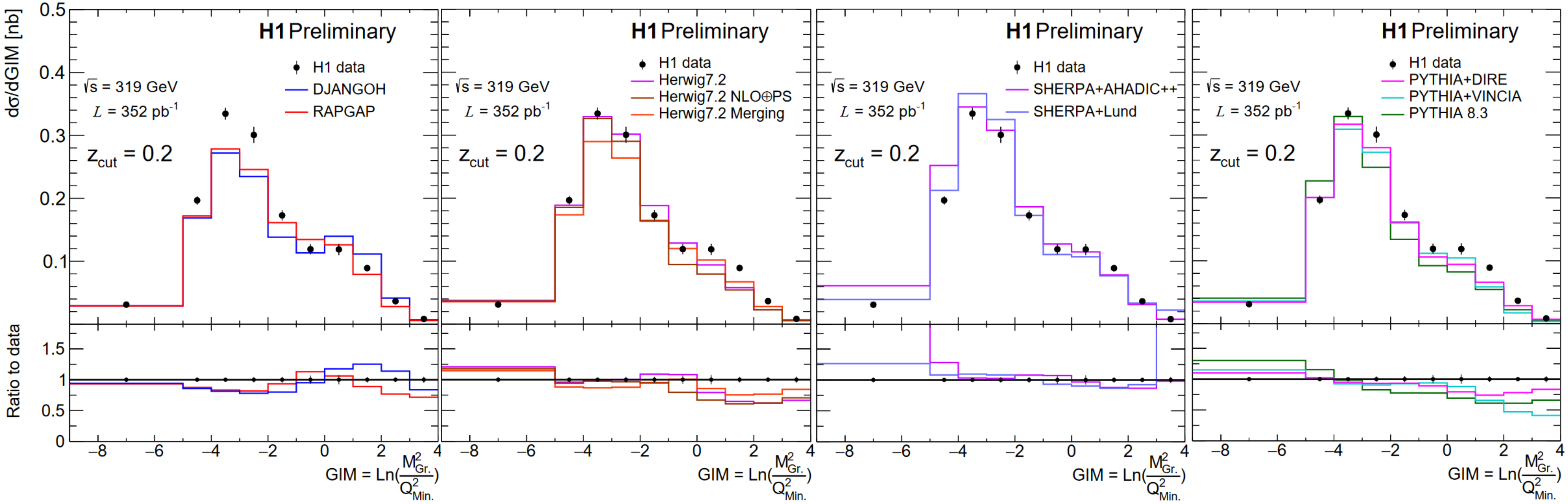
$$\tau_1 = \frac{2}{Q^2} \sum_{i \in \text{gr. ent.}} \min(q_B \cdot p_i, q_J \cdot p_i)$$



- PYTHIA – Version 8.3
  - VINCIA – Antenna Shower
  - DIRE - Dipole shower + multijet merging
- Herwig – Version 7.2 (Angular-ordered)
  - NLO ⊕PS – AO Shower, subtractive matching
  - Merging - Dipole shower + multijet merging
- SHERPA – Version 2.2.12 (MEPS@NLO)
  - AHADIC++ - Cluster Fragmentation
  - Lund – String Fragmentation

- Best tail region from SHERPA, RAPGAP
  - Fixed-order, multijets, hard splittings
- Best peak region from DIRE, Herwig Merging
  - Resummation, parton shower, hadronization

Results – Groomed Invariant Mass $M^2_{Gr.} = (\sum_i p_i^\mu)^2$



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  - AHADIC++ - Cluster Fragmentation
  - Lund – String Fragmentation

- $Q^2_{Min.}$ = 150 GeV²
- Best high mass region from SHERPA
  - Fixed-order, multijets, hard splittings
- Best low mass region from Herwig, DIRE
  - Resummation, parton shower, hadronization

Conclusion

- Groomed and ungroomed event shapes provide a strong handle on non-perturbative physics
  - Hadronization, parton showers, and the interplay between them

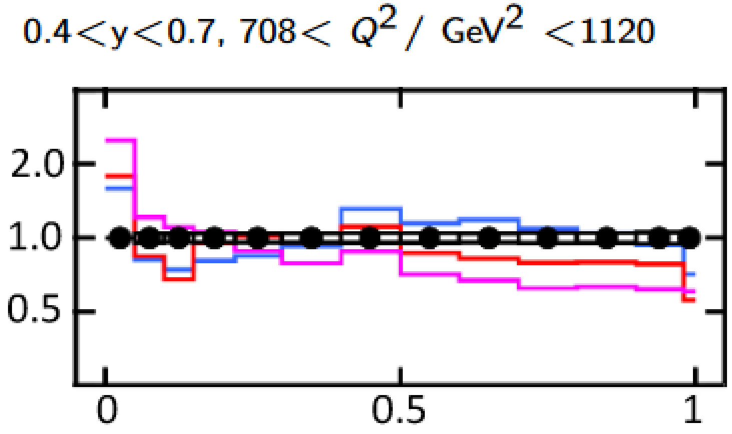
- H1 archived data provides an ideal environment for testing new theoretical tools (MC generators, analytic calculations) before the EIC turns on
  - Excellent playground for tuning MC generators
  - Clean collision system allows for higher sensitivity to NP jet dynamics
  - Room for non-perturbative universality studies (e^+e^-,p+p)

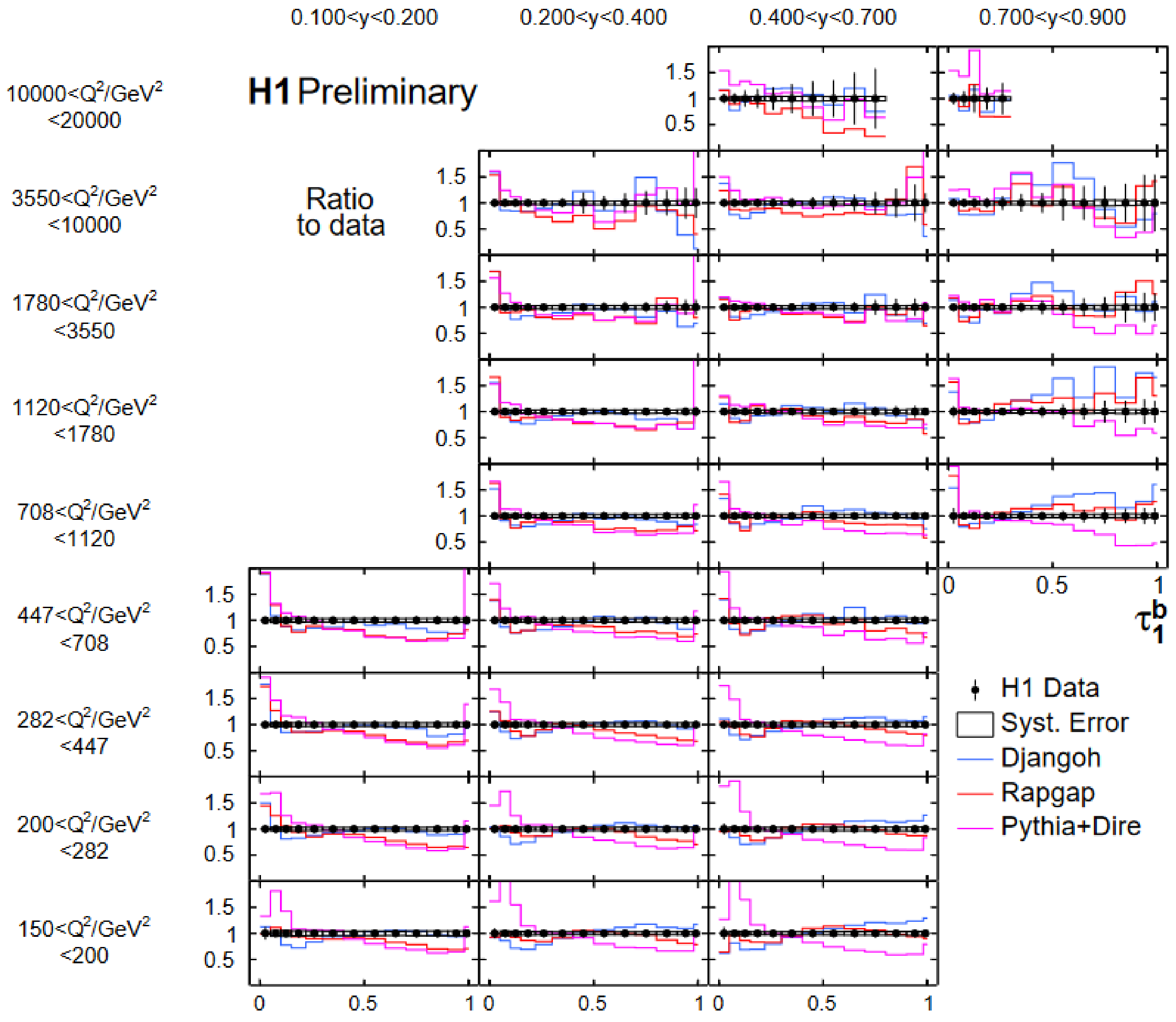
Thank you!

Backup

Triple-Differential Cross-Section

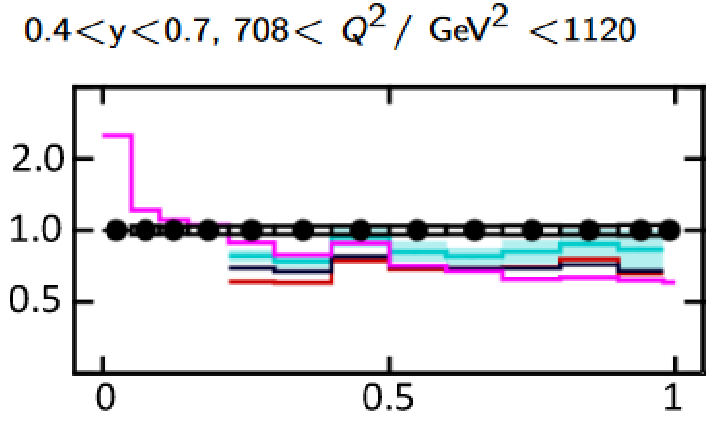
- Ratios to data
- Stat. uncertainties range from a few % to a few 10s of %
- Sys. uncertainties around 5%
- Djangoh and Rapgap perform reasonably well over full phase space
- Pythia+Dire too large in peak region

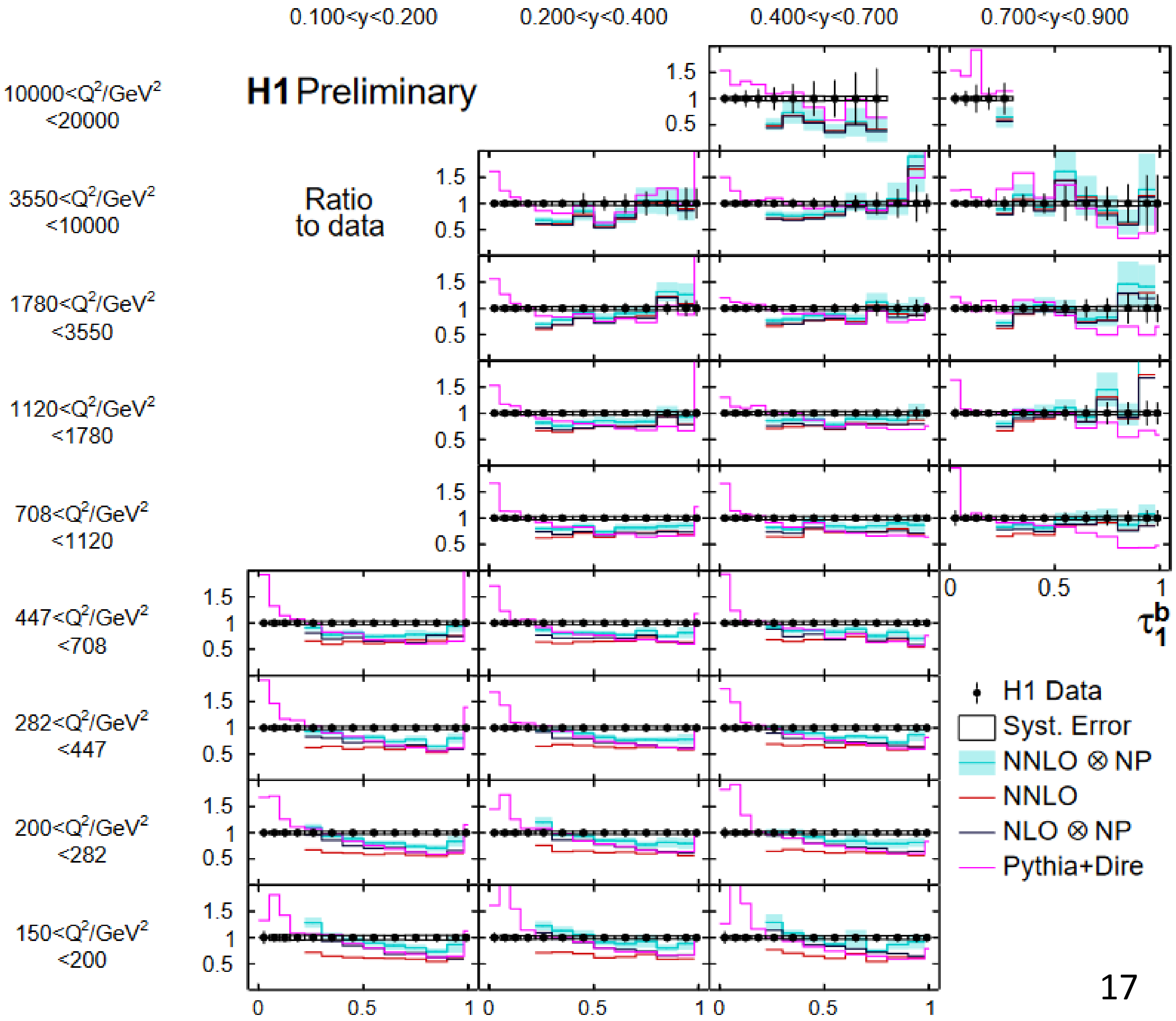




Triple-Differential Cross-Section

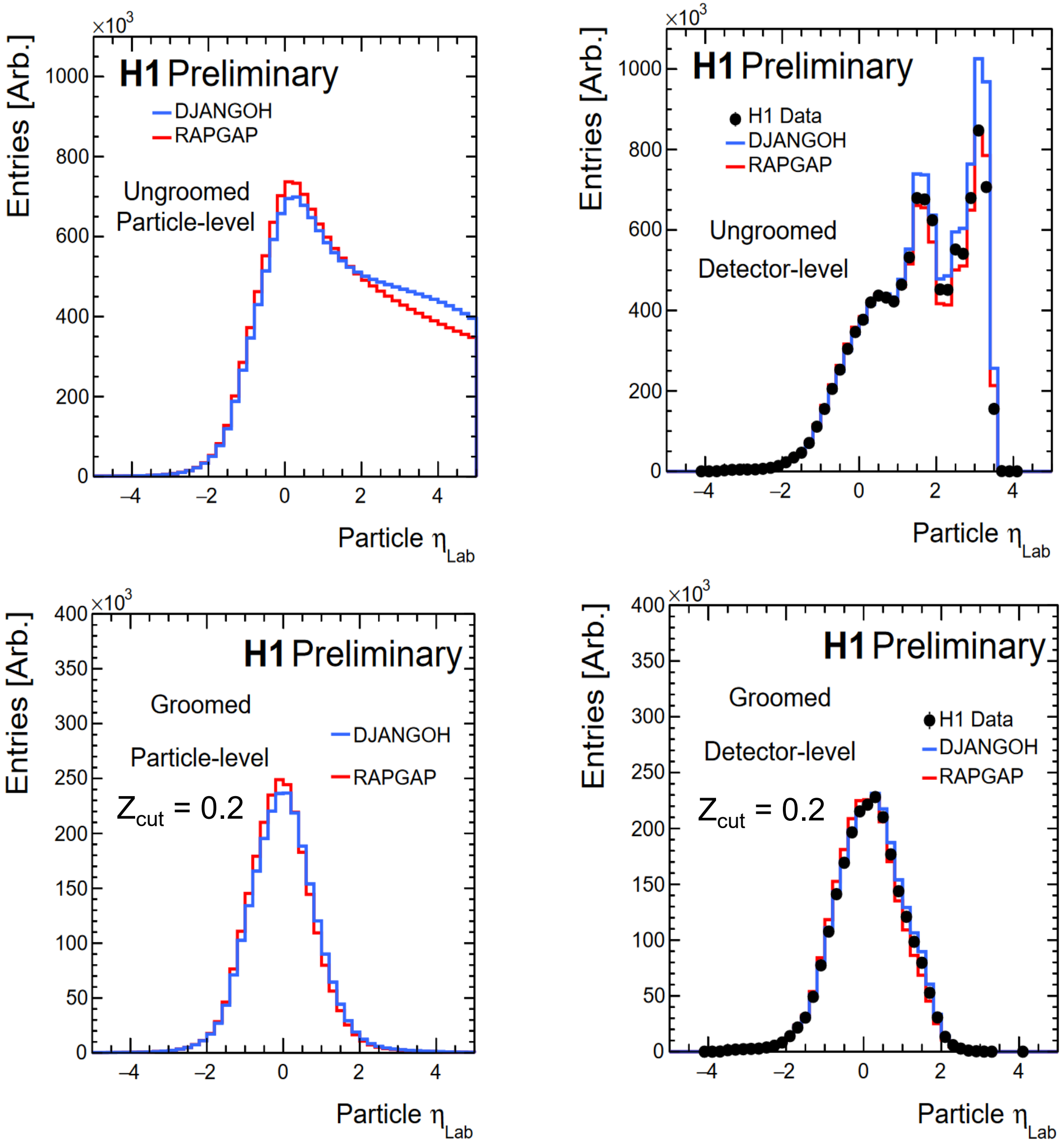
- NNLO QCD prediction for $ep \rightarrow 2\,Jets + X$
  - Reasonable description over full phase space
  - Scale uncertainties relatively small
  - NNLO improves over NLO
- NP corrections are sizable





Grooming Benefits

- No underlying event, why groom?
  - Less affected by lab-frame detector acceptance
  - Mitigate QCD remnant, ISR
  - No theoretically challenging non-global logarithms
- Ungroomed detector-level shows significant difference from particle-level
  - Detector acceptance, efficiencies
- Grooming events brings particle-level and detector-level distributions into much better agreement!

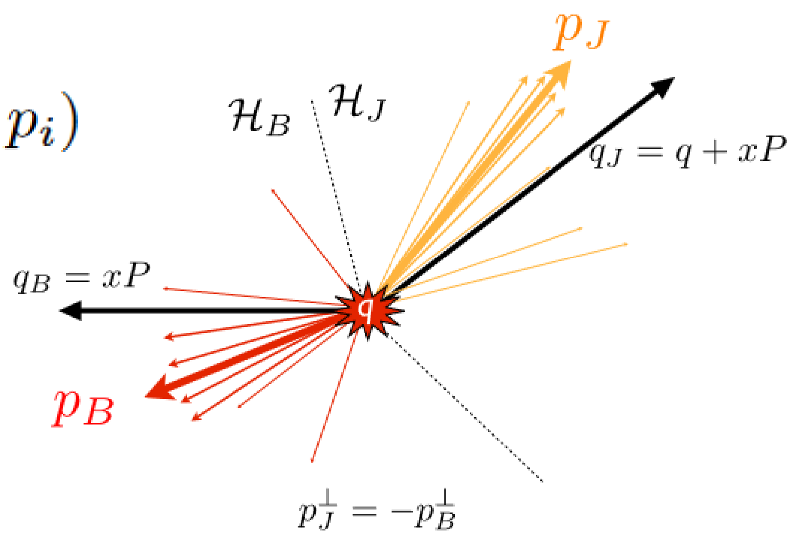


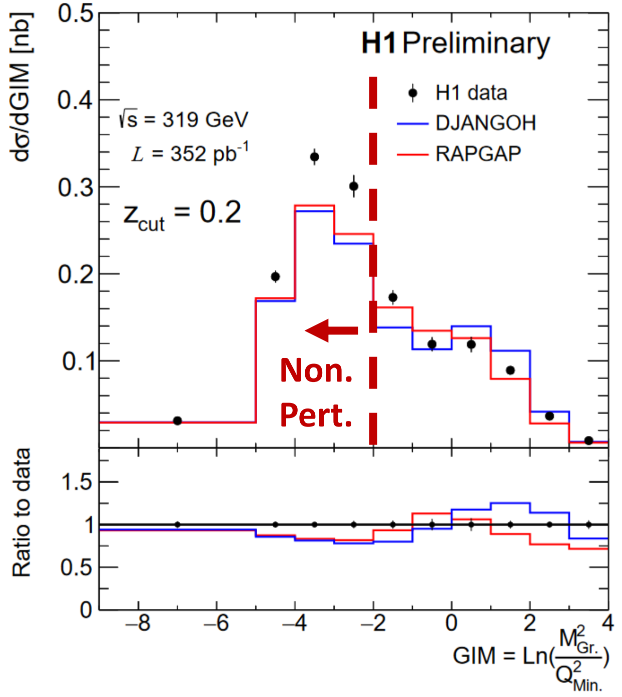
Observables

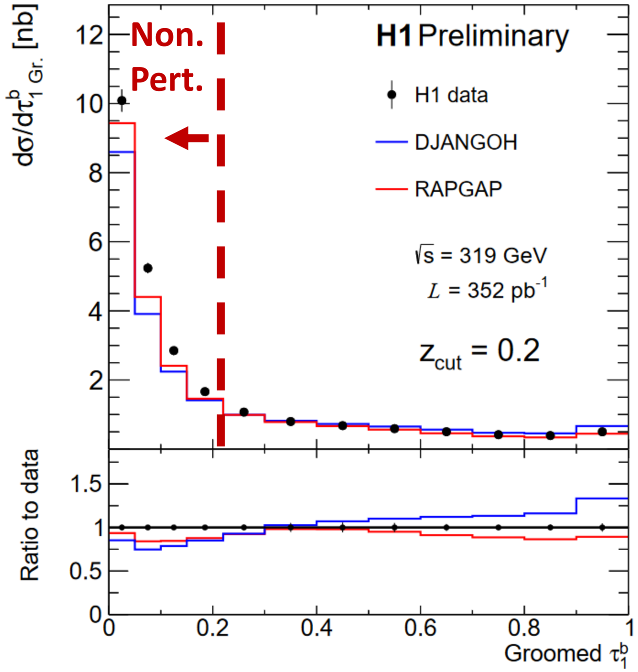
- After grooming procedure, a subset of particles survives
  - Event shape is calculated with these particles
  - Two event shapes studied here
- Groomed Invariant Mass (GIM) $M^2_{Gr.} = (\sum_i p_i^\mu)^2$
- Groomed 1-Jettiness

$$\tau_1 = \frac{2}{Q^2} \sum_{i \in \text{gr. ent.}} \min(q_B \cdot p_i,\, q_J \cdot p_i)$$

$$\tau_1^b \rightarrow \quad q_J = q + xP, \quad q_B = xP$$







Results

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- Uncertainty on data is statistical ⊕ systematic
- RAPGAP and DJANGOH
  - Standard H1 MCs
  - Both use LEPTO for matrix elements $O(\alpha_S)$
- DJANGOH:
  - Color dipole model for parton shower + string fragmentation
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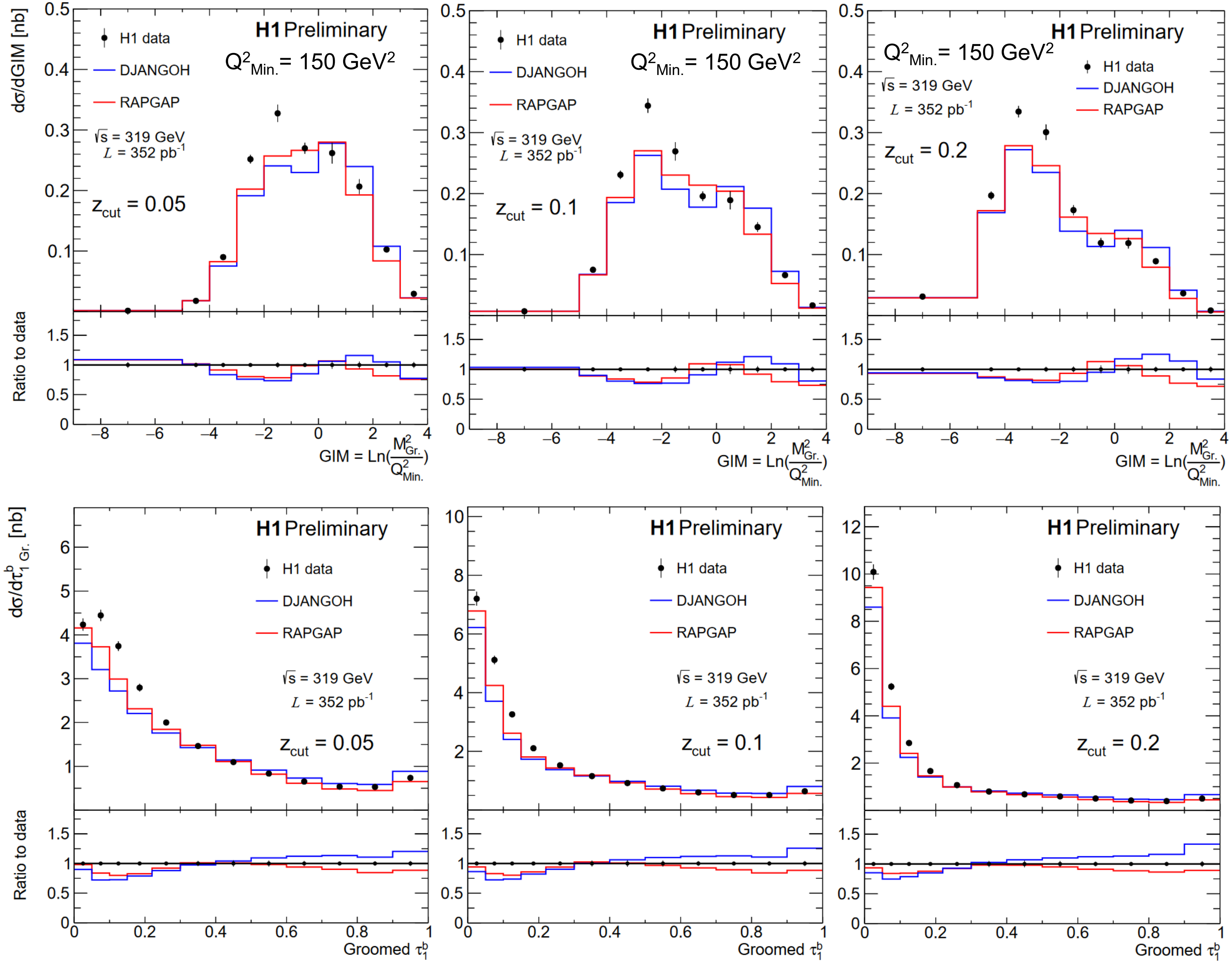
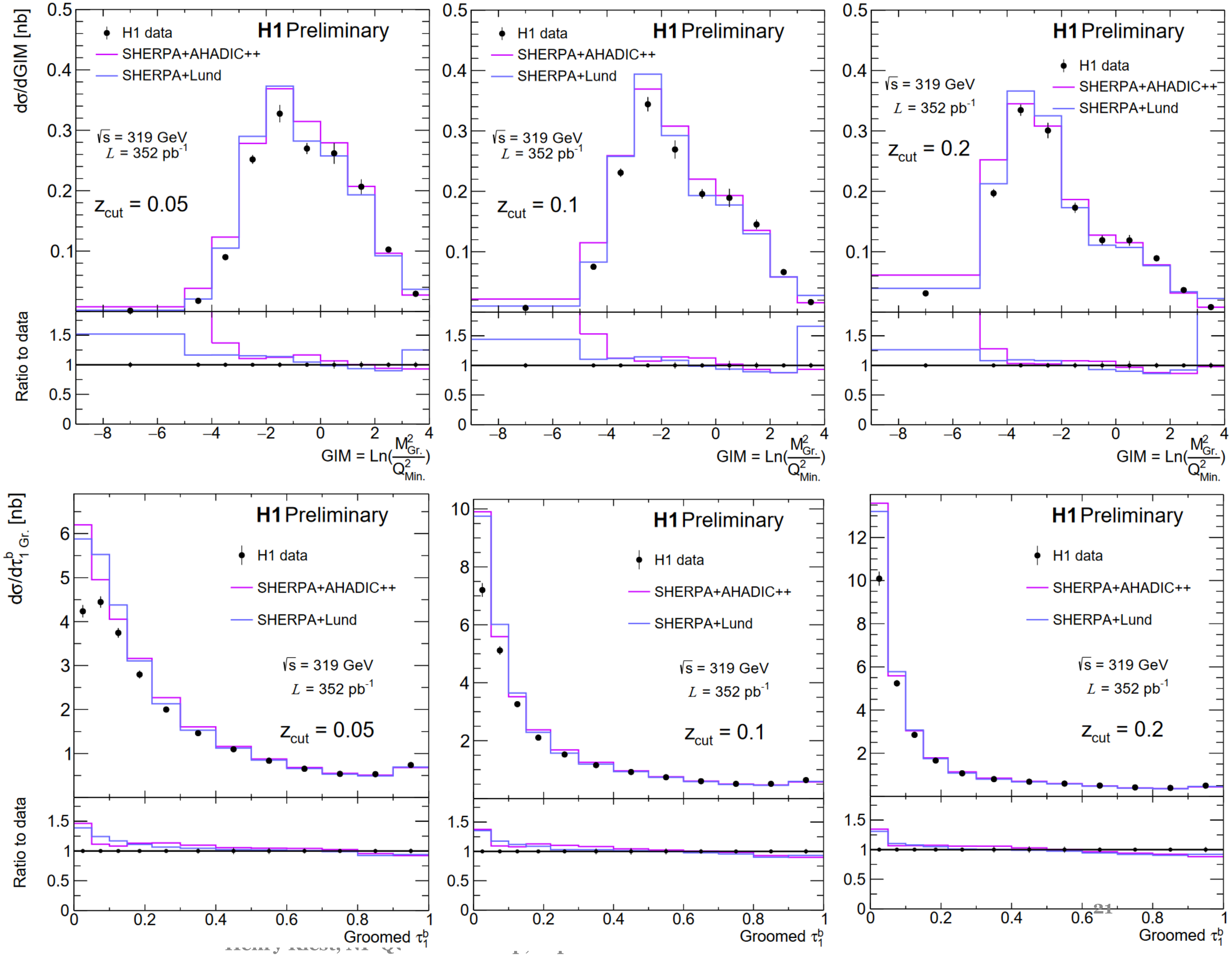


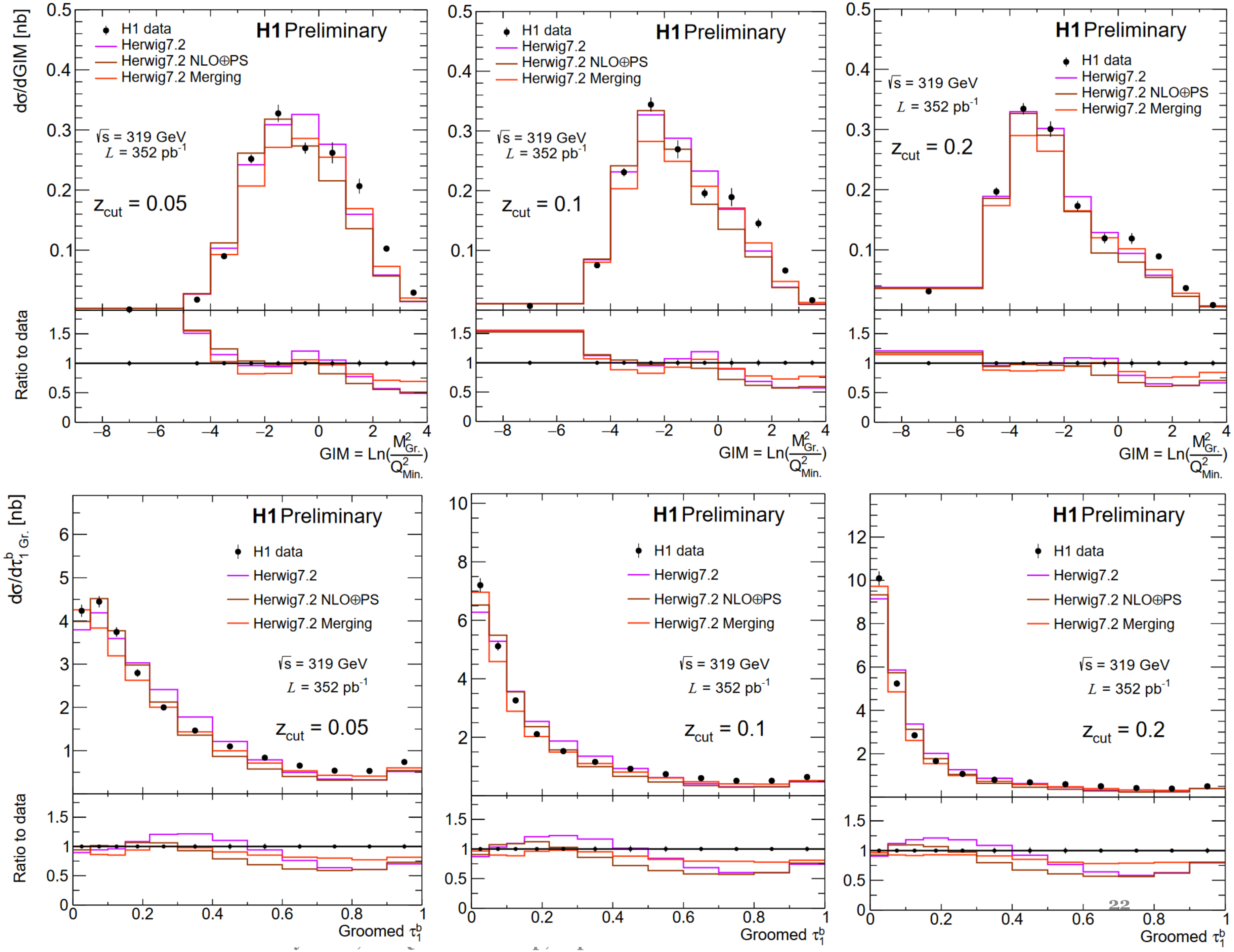
Results

- SHERPA
  - Version 2.2.12
  - MEPS@NLO
- AHADIC++:
  - SHERPA native cluster hadronization model
- Lund:
  - Lund string model from PYTHIA
- Both models provide good description of fixed-order region



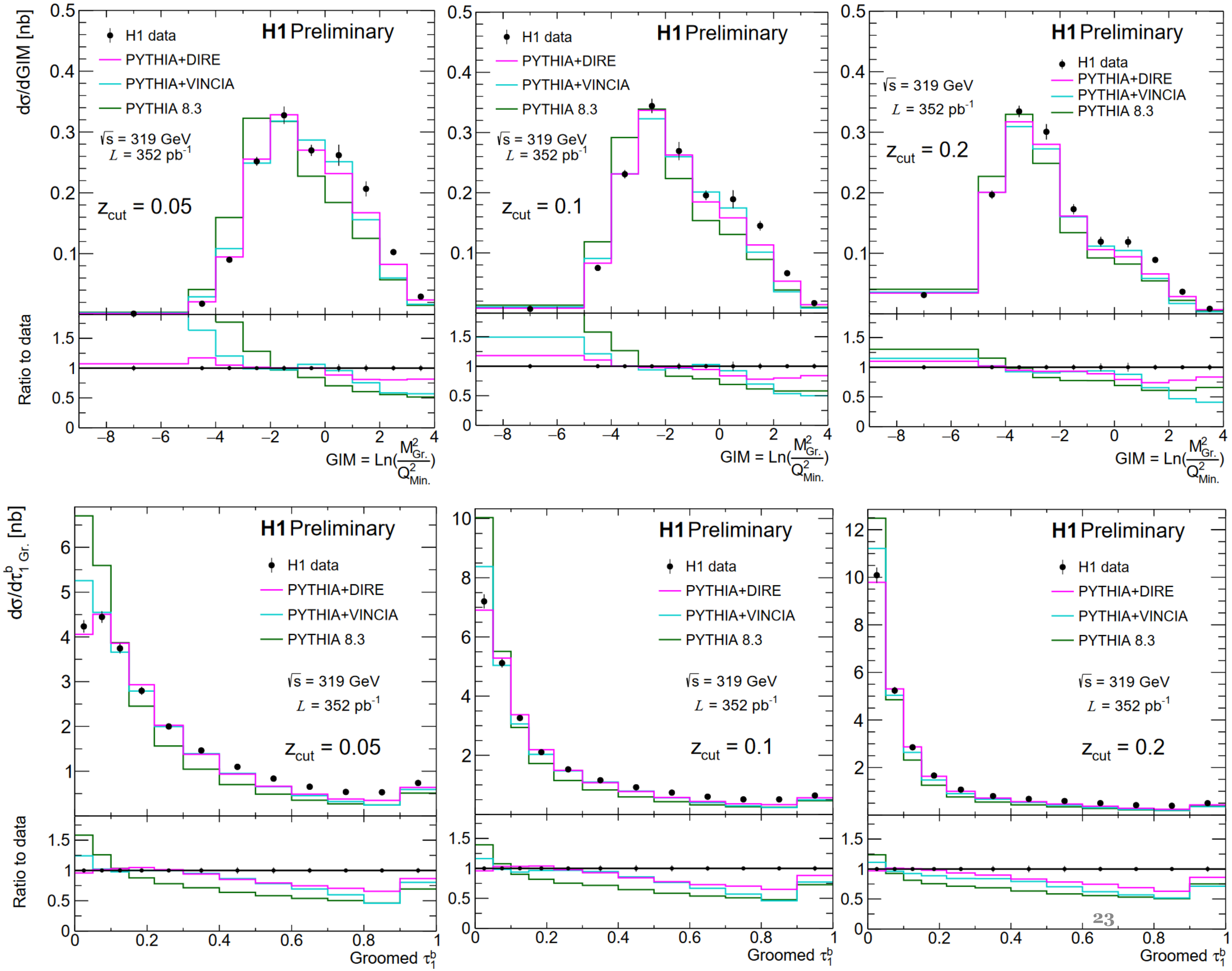
Results

- Herwig
  - Version 7.2.2
- NLO⊕PS:
  - Herwig internal implementation of MC@NLO via Matchbox
- Merging:
  - Dipole shower with multijet merging



Results

- PYTHIA
  - Version 8.3
  - No external matrix elements
- DIRE:
  - Dipole resummation
  - Excellent description in resummation region
- VINCIA:
  - Antenna shower

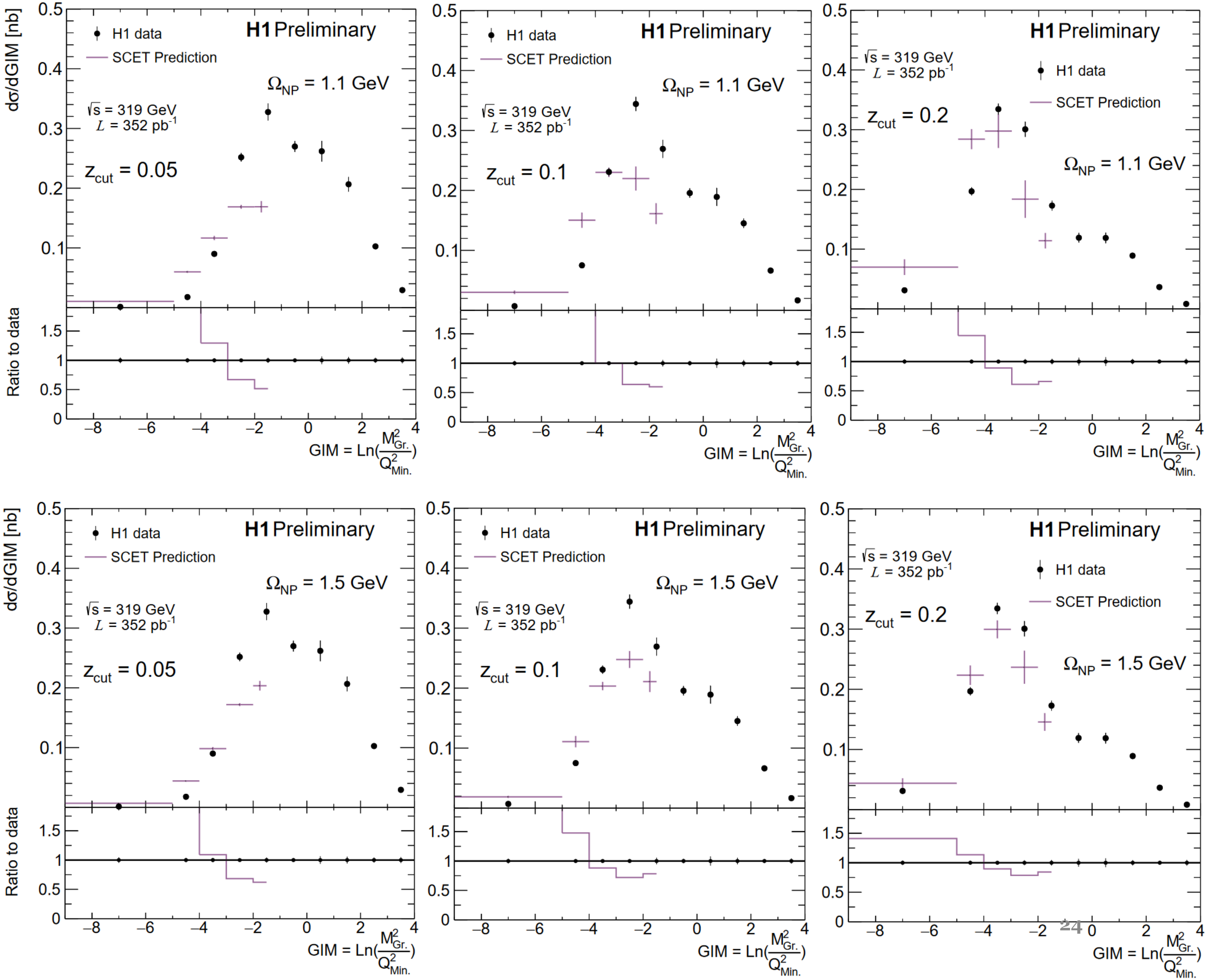


Results

- Analytic - SCET
  - From Y. Makris [1]
  - Evaluated at two values of Ω_{NP}
    - Shape function mean
  - No fixed-order calculation yet incorporated
- Agreement improves with increasing z_{cut}, Ω_{NP}
  - Non-perturbative effects are significant!
  - Factorization validity improves to higher z_{cut}

$$\frac{d\sigma_{\text{had.}}}{dx dQ^2 dm^2_{\text{gr.}}} = \int d\epsilon \frac{d\sigma}{dx dQ^2 dm^2_{\text{gr.}}}\left(m^2_{\text{gr.}} - \frac{\epsilon^2}{z_{\text{cut}}}\right) f_{\text{mod.}}(\epsilon) ,$$

$$f_{\text{mod.}}(\epsilon) = N_{\text{mod.}} \frac{4\epsilon}{\Omega^2} \exp\left(\frac{2\epsilon}{\Omega}\right)$$



region 1: $1 \gg z_{\text{cut}} \gg m_{\text{gr.}}^2/Q^2$

$$\lambda = \frac{m_{\text{gr.}}^2}{Q^2} \,,$$

$$p = (p^+, p^-, p^\perp)$$

$$n\text{-collinear:} \quad p_n \sim Q(z_{\text{cut}}, 1, \sqrt{z_{\text{cut}}}) \,,$$

$$\text{soft:} \quad p_s \sim Q z_{\text{cut}}(1,1,1) \,,$$

$$\text{collinear-soft:} \quad p_{cs} \sim Q(\lambda, z_{\text{cut}}, \sqrt{z_{\text{cut}}\lambda}) \,,$$

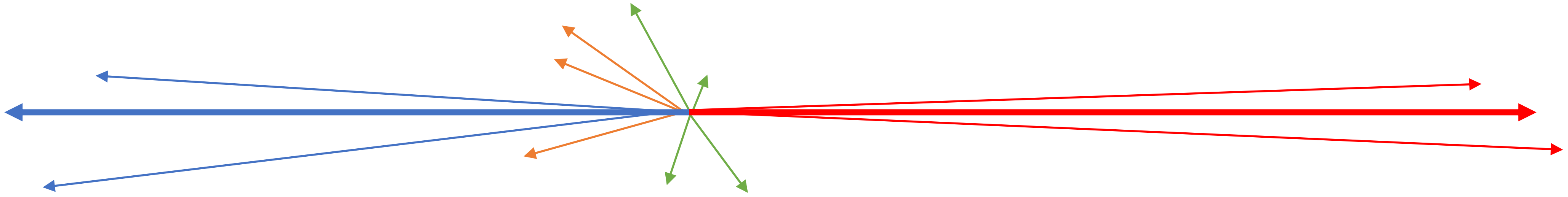
$$\bar{n}\text{-collinear:} \quad p_{\bar{n}} \sim Q(1, \lambda, \sqrt{\lambda}) \,,$$

Jet Direction (Breit η=-∞) = $\bar{n}$-collinear direction

Beam Direction (Breit η=-∞) = n-collinear direction

Soft Radiation (Isotropic)

Collinear-soft radiation, wide-angle soft radiation mostly along jet direction



$$\frac{d\sigma}{dx dQ^2 dm_{\text{gr.}}^2} = H(Q,y,\mu) S(Q z_{\text{cut}}, \mu) \sum_f \mathcal{B}_{f/P}(x, Q^2 z_{\text{cut}}, \mu) \int de_{\bar{n}} de_{cs}\, \delta(m_{\text{gr.}}^2 - e_{\bar{n}} - e_{cs}) J(e_{\bar{n}}, \mu^2) \mathcal{C}(e_{cs} z_{\text{cut}}, \mu^2) \times \left[1 + \mathcal{O}\left(z_{\text{cut}}, \frac{m_{\text{gr.}}^2}{z_{\text{cut}} Q^2}\right)\right] , \quad (15)$$

In Region 1, shape of distribution depends only on jet and collinear-soft functions, which are independent of Q region 1: $1 \gg z_{\rm cut} \gg m^2_{\rm gr.}/Q^2$

$$\lambda = \frac{m^2_{\rm gr.}}{Q^2}\,,$$

$$p = (p^+, p^-, p^\perp)$$

$$\begin{aligned}
n\text{-collinear:} &\quad p_n \sim Q(z_{\rm cut}, 1, \sqrt{z_{\rm cut}})\,,\\
\text{soft:} &\quad p_s \sim Q z_{\rm cut}(1,1,1)\,,\\
\text{collinear-soft:} &\quad p_{cs} \sim Q(\lambda, z_{\rm cut}, \sqrt{z_{\rm cut}\lambda})\,,\\
\bar{n}\text{-collinear:} &\quad p_{\bar{n}} \sim Q(1, \lambda, \sqrt{\lambda})\,,
\end{aligned}$$

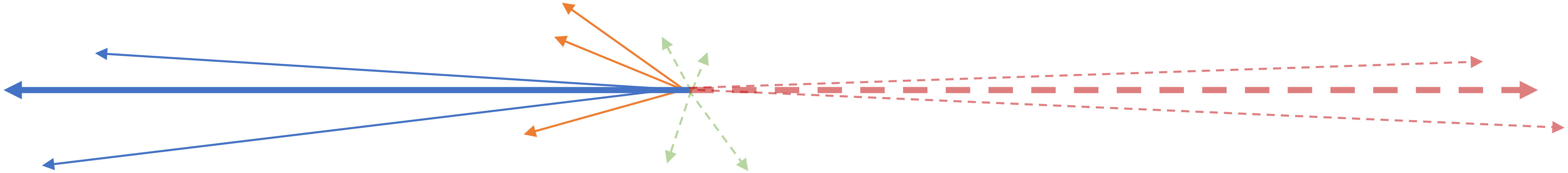
Jet Direction (Breit η=-∞) = $\bar{n}$-collinear direction

Beam Direction (Breit η=-∞) = n-collinear direction

Soft Radiation (Isotropic)

Collinear-soft radiation, wide-angle soft radiation mostly along jet direction

Grooming causes only Jet and Collinear-soft radiation to contribute to shape of distribution in the single-jet (low invariant mass) limit



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In Region 1, shape of distribution depends only on jet and collinear-soft functions, which are independent of Q

Centauro

$$d_{ij} = \min(p_{Ti}^{2p}, p_{Tj}^{2p})\Delta R_{ij}^2/R^2\ , \qquad d_{iB} = p_{Ti}^{2p}$$

vs.

$$d_{ij} = (\Delta\bar{\eta}_{ij})^2 + 2\bar{\eta}_i\bar{\eta}_j(1-\cos\Delta\phi_{ij})\ ,$$

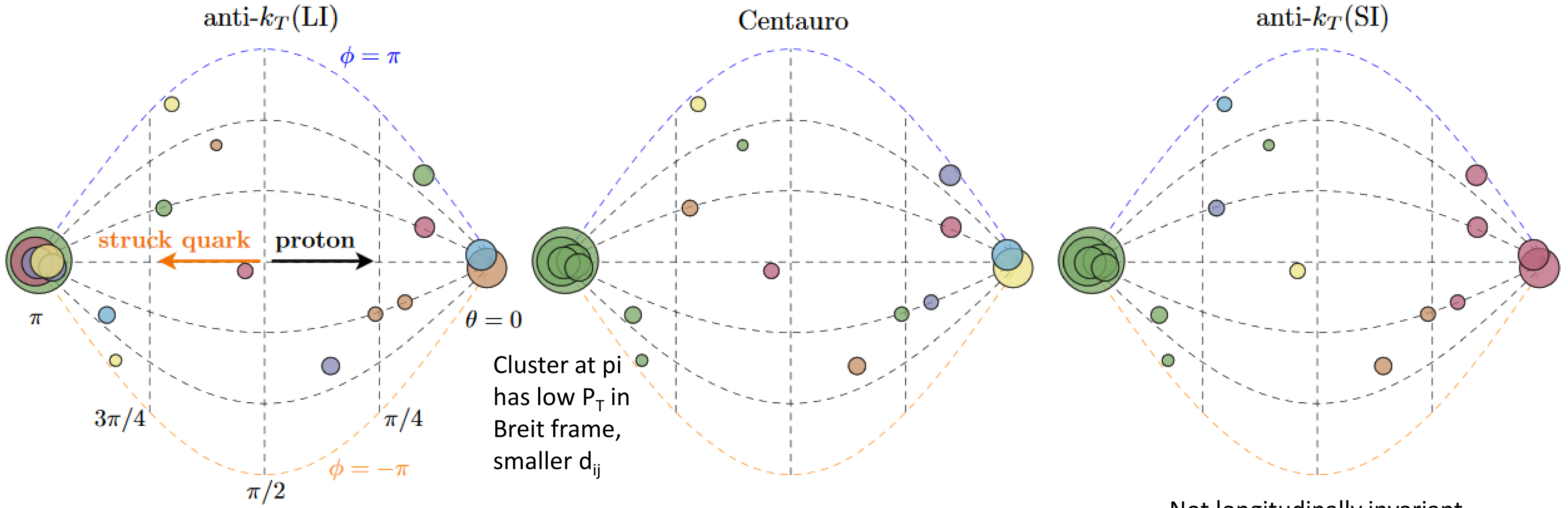
where

$$\bar{\eta}_i \equiv 2\sqrt{1+\frac{q\cdot p_i}{x_B P\cdot p_i}} \xrightarrow[\text{frame}]{\text{Breit}} \frac{2p_i^\perp}{p_i^+}\ ,$$

vs.

$$d_{ij} = \min(E_i^{2p}, E_j^{2p})\frac{1-c_{ij}}{1-c_R}\ , \qquad d_{iB} = E_i^{2p}$$

where $c_{ij} = \cos\theta_{ij}$ and $c_R = \cos R$.



Cluster at pi has low P_T in Breit frame, smaller d_{ij}

Doesn't preferentially capture struck quark

Not longitudinally invariant

Figure 2. Jet clustering in the Breit frame using the longitudinally-invariant anti-k_T(LI), Centauro, and spherically-invariant anti-k_T(SI) algorithms in a DIS event simulated with PYTHIA 8. Each particle is illustrated as a disk with area proportional to its energy and the position corresponds to the direction of its momentum projected onto the unfolded sphere about the hard-scattering vertex. The vertical dashed lines correspond to constant θ and curved lines to constant ϕ. All the particles clustered into a given jet are colored the same.

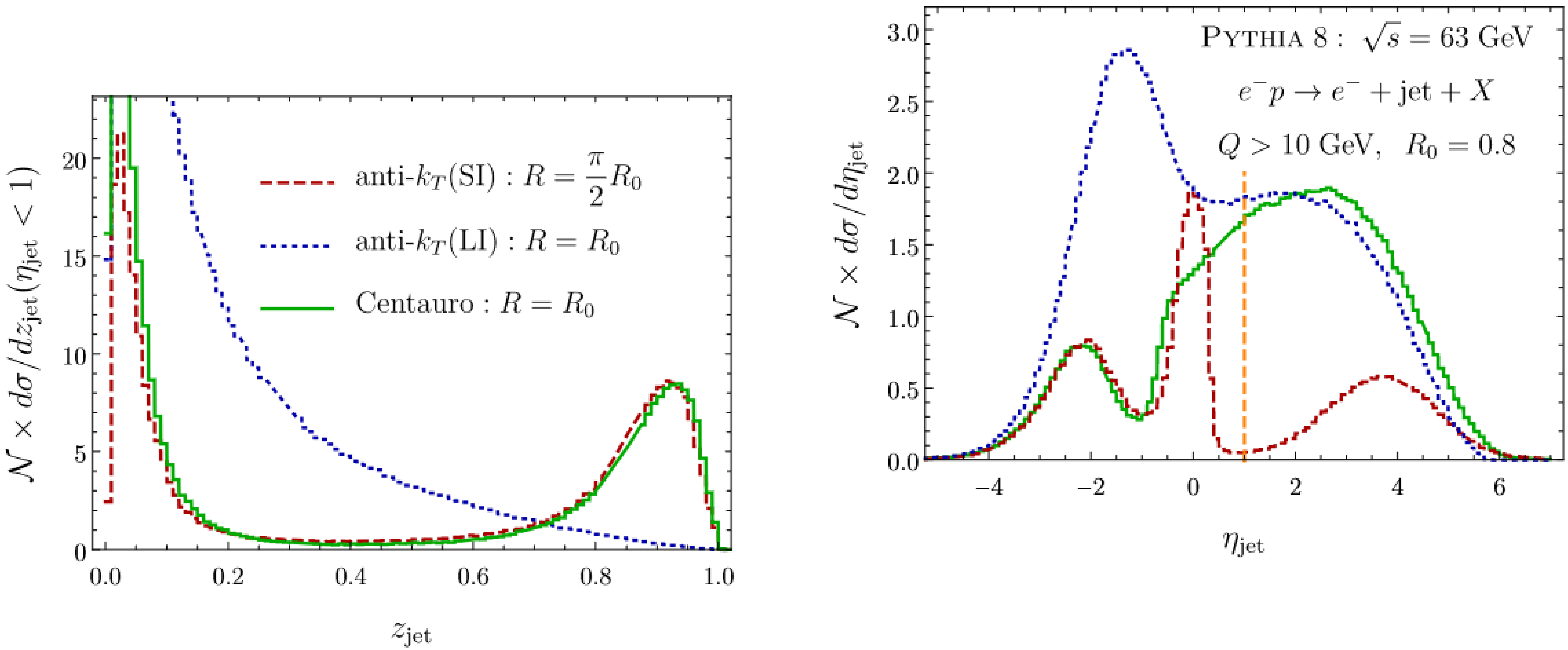


Figure 4. Pseudorapidity (top panel) and momentum fraction z_{jet} (bottom panel) of jets clustered with anti-k_T(LI), anti-k_T(LI) and Centauro algorithms in the Breit frame. Here $\mathcal{N}$ is an overall normalization constant chosen to improve readability and is the same for all curves in a graph.

Centauro

$$d_{ij} = \min(p_{Ti}^{2p}, p_{Tj}^{2p})\Delta R_{ij}^2/R^2 , \qquad d_{iB} = p_{Ti}^{2p}$$

vs.

$$d_{ij} = (\Delta\bar{\eta}_{ij})^2 + 2\bar{\eta}_i\bar{\eta}_j(1 - \cos\Delta\phi_{ij}) ,$$

where

$$\bar{\eta}_i \equiv 2\sqrt{1 + \frac{q \cdot p_i}{x_B P \cdot p_i}} \xrightarrow[\text{frame}]{\text{Breit}} \frac{2p_i^{\perp}}{p_i^{+}} ,$$

vs.

$$d_{ij} = \min(E_i^{2p}, E_j^{2p})\frac{1 - c_{ij}}{1 - c_R} , \qquad d_{iB} = E_i^{2p}$$

where $c_{ij} = \cos\theta_{ij}$ and $c_R = \cos R$.

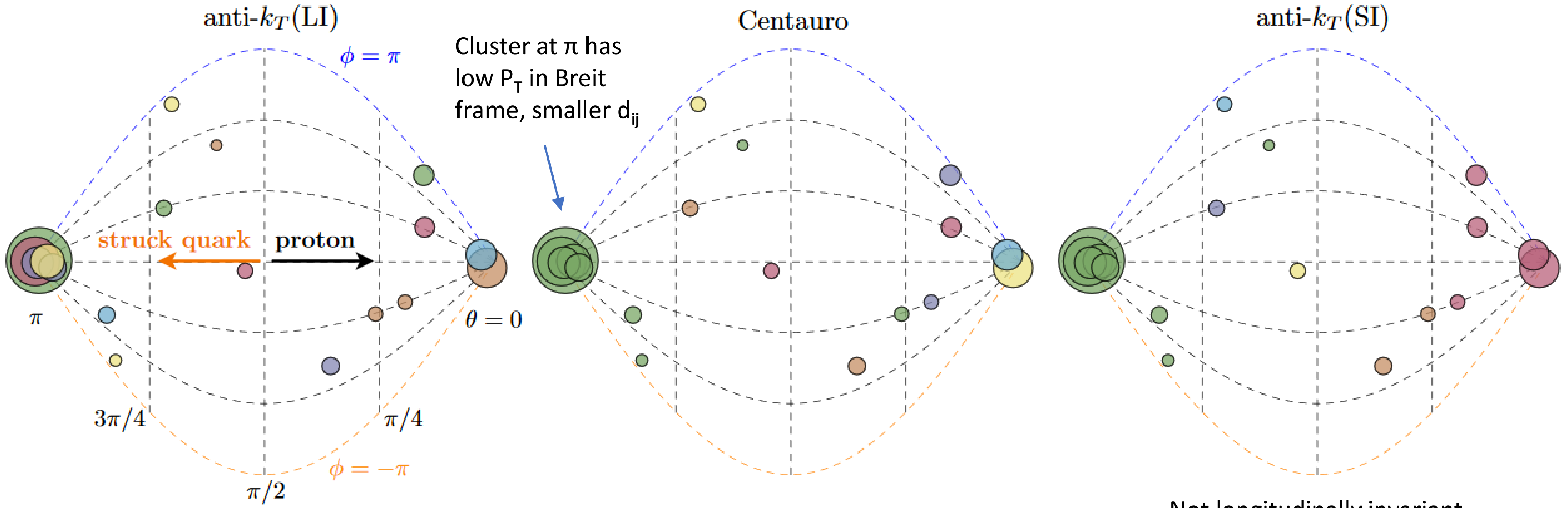


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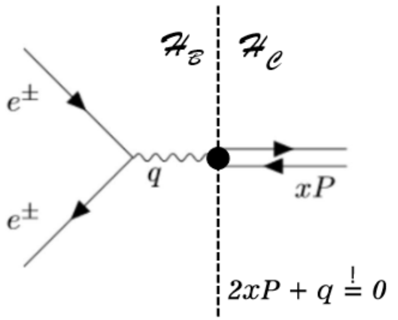
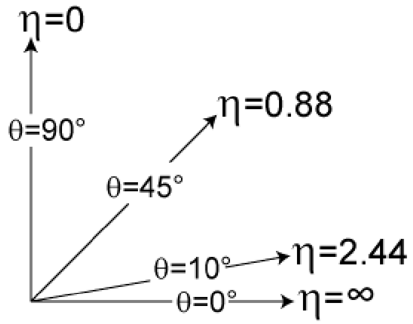
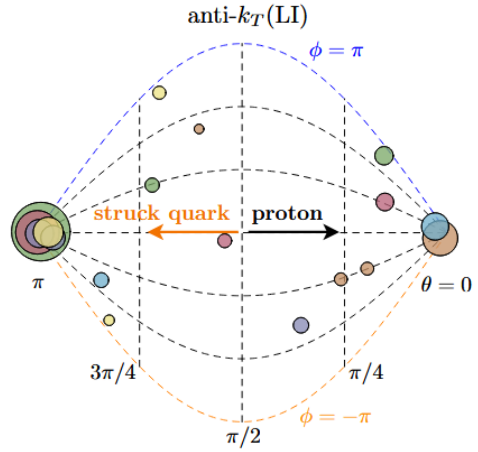
Figure 2. Jet clustering in the Breit frame using the longitudinally-invariant anti-k_T(LI), Centauro, and spherically-invariant anti-k_T(SI) algorithms in a DIS event simulated with PYTHIA 8. Each particle is illustrated as a disk with area proportional to its energy and the position corresponds to the direction of its momentum projected onto the unfolded sphere about the hard-scattering vertex. The vertical dashed lines correspond to constant θ and curved lines to constant ϕ. All the particles clustered into a given jet are colored the same.

Stony Brook University

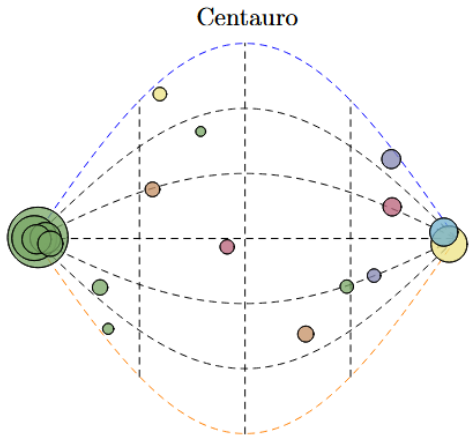
Centauro

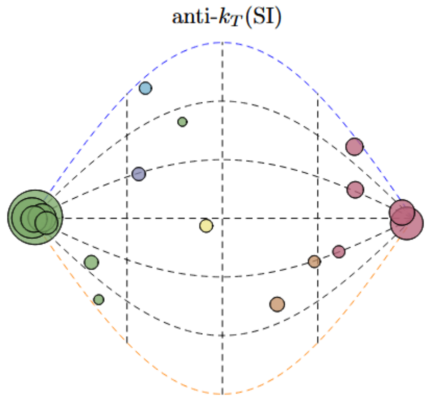






- Jet algorithm with asymmetric clustering measure
  - Treat current hemisphere and beam hemisphere differently
- Typical longitudinally-invariant jet algorithms cluster in (rapidity, azimuthal angle) space and fail to capture the born-level configuration in the Breit frame
  - Particles close to struck-parton direction have divergent rapidity, and therefore divergent distance between each other!
    - Makes study of single-jet Born level configuration impossible!
- Use spherically invariant clustering (polar angle, azimuthal angle) in the struck-parton direction and longitudinally invariant in beam direction
- Tends to create one hard jet in struck-parton direction and many weak single particle jets in beam direction, which can easily be filtered away

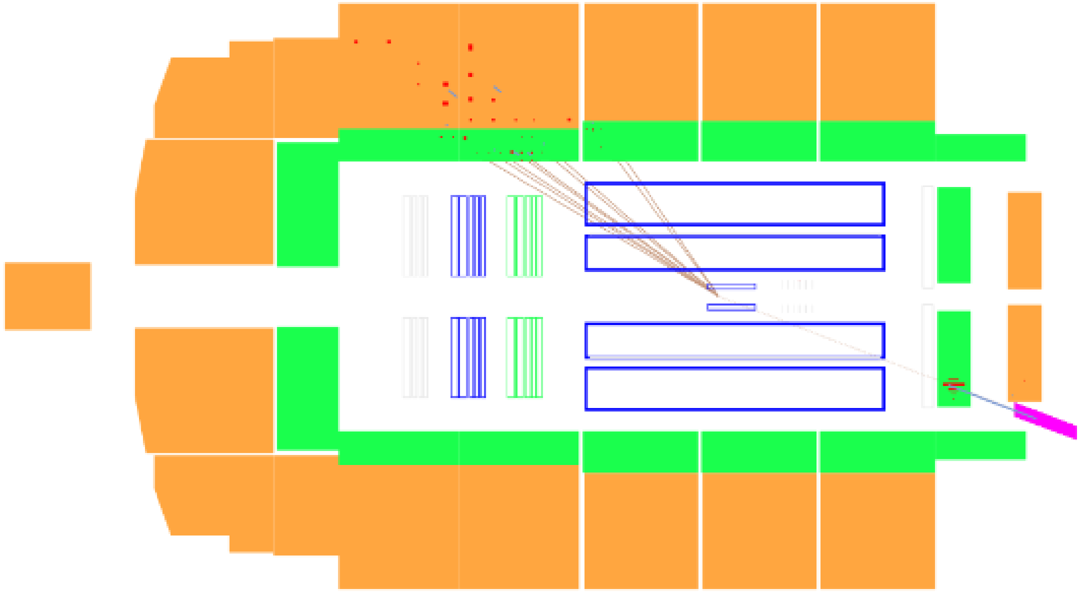


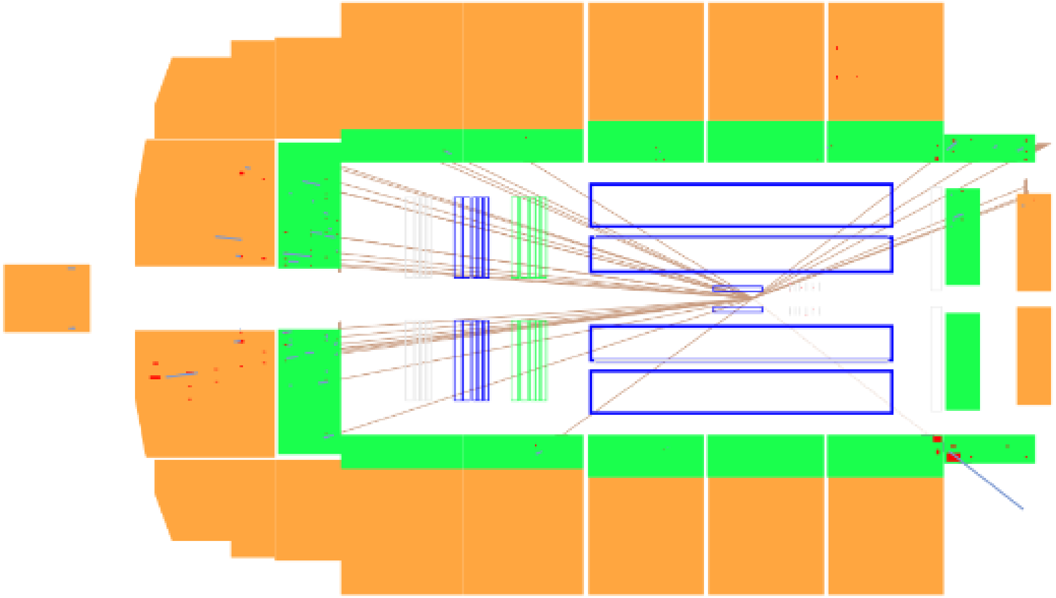


1-jettiness

$$\tau_1^b = \frac{2}{Q^2} \sum_{i \in X} \min\{xP \cdot p_i, (q + xP) \cdot p_i\}$$

Visualisation of the 1-jettiness with event displays





- DIS 1-jet configuration
- Most HFS particles collinear to scattered parton
  $\rightarrow$ Small τ_1^b

- Dijet event
- More and larger contributions to the sum over the HFS
  $\rightarrow$ Large τ_1^b

z_{cut}	0.05	0.1	0.2
Pythia8.3	0.31%	1.3%	6.3%
Pythia+Vincia	0.52%	1.7%	6.9%
Pythia+DIRE	0.47%	1.2%	5.6%
SHERPA+AHADIC++	0.03%	0.31%	3.6%
SHERPA+LUND	0.09%	0.59%	4.9%
HERWIG	0.038%	0.36%	3.6%
HERWIG+Merging	0.04%	0.39%	3.6%
HERWIG+MC@NLO	0.04%	0.39%	3.8%
DJANGO (Gen.)	0.09%	0.5%	4.0%
RAPGAP (Gen.)	0.07%	0.4%	3.7%
DJANGO (Det.)	1.0%	2.3%	7.8%
RAPGAP (Det.)	0.9%	2.2%	7.6%
H1 Data	1.0%	2.3%	7.7%

Table 1: Percentage of events that fail grooming. Rapgap and Djangoh are listed for both detector and generator level.