<u>Chirality, Vorticity and Magnetic Field in Heavy Ion Collisions</u> UCLA Chirality Retreat

# Perspectives on the STAR isobar and gold-gold data

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## OUTLINE

- 1. Various methods to eliminate flow-induced backgrounds
- 2. Further background contamination from nonflow and genuine 3-particle correlations
- 3. Hint of CME in Au+Au, and upper limit in isobar
- 4. Summary & outlook

# THE $\Delta \gamma$ CORRELATOR

Voloshin, PRC 2004

Look for charge separation



$$\gamma_{\alpha\beta} = \left\langle \cos(\varphi_{\alpha} + \varphi_{\beta} - 2\varphi_{RP}) \right\rangle$$
  
$$\gamma_{+-,-+} > 0, \quad \gamma_{++,--} < 0$$
  
$$\Delta \gamma = \gamma_{\text{opposite-sign}} - \gamma_{\text{same-sign}} > 0$$

STAR, PRL 2009, PRC 2010



Significant signal  $\Delta \gamma \sim 5 \times 10^{-4}$ 

# BACKGROUND IN $\Delta \gamma$ CORRELATOR

Voloshin 2004; FW 2009; Bzdak, Koch, Liao 2010; Pratt, Schlichting 2010; ...



$$dN_{\pm} / d\varphi \propto 1 + 2v_{1} \cos \varphi^{\pm} + 2a_{\pm} \cdot \sin \varphi^{\pm} + 2v_{2} \cos 2\varphi^{\pm} + \dots$$
  

$$\gamma_{\alpha\beta} = \left[ \left\langle \cos(\varphi_{\alpha} - \psi_{RP}) \cos(\varphi_{\beta} - \psi_{RP}) \right\rangle - \left\langle \sin(\varphi_{\alpha} - \psi_{RP}) \sin(\varphi_{\beta} - \psi_{RP}) \right\rangle \right]$$
  

$$+ \left[ \frac{N_{cluster}}{N_{\alpha}N_{\beta}} \left\langle \cos(\varphi_{\alpha} + \varphi_{\beta} - 2\varphi_{cluster}) \cos(2\varphi_{cluster} - 2\varphi_{RP}) \right\rangle \right]$$
  

$$= \left[ \left\langle v_{1,\alpha}v_{1,\beta} \right\rangle - \left\langle a_{\alpha}a_{\beta} \right\rangle \right] + \frac{N_{cluster}}{N_{\alpha}N_{\beta}} \left\langle \cos(\varphi_{\alpha} + \varphi_{\beta} - 2\varphi_{cluster}) \right\rangle v_{2,cluster}$$

$$\Delta \gamma = 2 \left\langle a_1^2 \right\rangle + \frac{N_{\rho}}{N_{\alpha} N_{\beta}} \left\langle \cos(\varphi_{\alpha} + \varphi_{\beta} - 2\varphi_{\rho}) \right\rangle v_{2,\rho}$$

Flow-induced charge-dependent background: nonflow coupled with flow

 $\Delta \gamma_{
m Bkg} \propto v_2$  / N

SLIGHTLY MORE FORMALLY...  

$$\Delta \gamma = 2 \langle a_1^2 \rangle + \frac{N_{\rho}}{N_a N_{\beta}} \langle \cos(\varphi_a + \varphi_{\beta} - 2\varphi_{\rho}) \rangle v_{2,\rho}$$

$$\Delta C_3 = 2 \langle a_1^2 \rangle v_{2,c\perp B} + \frac{N_{2p}}{N_a N_{\beta}} \langle \cos(\varphi_a + \varphi_{\beta} - 2\varphi_{2p}) \rangle v_{2,2p} v_{2,c} + \frac{N_{3p}}{N_a N_{\beta} N_c} \langle \cos(\varphi_a + \varphi_{\beta} - 2\varphi_c) \rangle$$

$$= 2 \langle a_1^2 \rangle v_{2,c\perp B} + \frac{C_{2p} N_{2p}}{N^2} v_{2,2p} v_{2,c} + \frac{C_{3p} N_{3p}}{2N^3} \qquad N \approx N_+ \approx N_-$$

$$C_{2p} = \langle \cos(\varphi_a + \varphi_{\beta} - 2\varphi_{2p}) \rangle$$

$$\Delta \gamma = 2 \langle a_1^2 \rangle \frac{v_{2,c\perp B}}{v_{2,c}^*} + \frac{C_{2p} N_{2p}}{N^2} \frac{v_{2,2p} v_{2,c}}{v_{2,c}^*} + \frac{C_{3p} N_{3p}}{2N^3 v_{2,c}^*} \qquad C_{3p} = \langle \cos(\varphi_a + \varphi_{\beta} - 2\varphi_c) \rangle_{3p}$$

$$\int \int \sum_{\substack{nonflow \\ nonflow \\ nonflow \\ flow-induced bkgd}} v_{2,c\perp B} + \frac{C_{2p} N_{2p}}{2N^3 v_{2,c}^*} + \frac{C_{3p} N_{3p}}{2N^3 v_{2,c}^*} \qquad C_{3p} = \langle \cos(\varphi_a + \varphi_{\beta} - 2\varphi_c) \rangle_{3p}$$

# STATISITICAL EVENT-SHAPE-ENGINEERING



# DYNAMICAL EVENT-SHAPE-ENGINEERING



on v<sub>2</sub> within a given centrality Upper limit 7%

Promising way to extract possible CME signal. Will need to assess nonflow effects

Upper limit 26%

# THE R OBSERVABLE

Ajitanand, Lacey, et al., PRC **83** (2011) 011901 Magdy, Lacey, et al., PRC **97** (2018) 061901(R)

$$\Delta S = \left\langle \sin\left(\varphi - \psi_{2}\right) \right\rangle_{+} - \left\langle \sin\left(\varphi - \psi_{2}\right) \right\rangle_{-}$$
$$R(\Delta S) = \frac{N(\Delta S_{\text{real}})}{N(\Delta S_{\text{shuffled}})} / \frac{N(\Delta S_{\text{real}}^{\perp})}{N(\Delta S_{\text{shuffled}}^{\perp})}$$

Width of R( $\Delta$ S) distribution reduces to variance sin\*sin, cos\*cos  $\rightarrow$ equivalently the  $\Delta\gamma$  variable

shuffled width: 
$$\sigma_R'^{-2} = N \Delta \gamma \propto v_2$$

Choudhury et al., CPC 46 (2022) 014101

Earlier claims of CME; many issues identified. ESE studies indicate "v2-independence." Latest claim by Lacey et al., arXiv:2203.10029: Scale by N, so isobar R compatible with CME. See *Comment* by FW, arXiv:2204.08450

Execution of R analysis: 
$$\Delta S = \left(\Delta S_{\text{West-POI}}^{\text{East-EP}} + \Delta S_{\text{East-POI}}^{\text{West-EP}}\right)/2$$



Issue identified: Reuse of data in average causes autocorrelation, yielding non-zero intercept. *Feng et al, PRC 103 (2021) 034912* 

Positive intercept not present in analysis with separate  $\Delta S$ 

# **SPECTATOR & PARTICIPANT PLANES**

H.-j. Xu, FW, et al., CPC 42 (2018) 084103, arXiv:1710.07265 S.A. Voloshin, PRC 98 (2018) 054911, arXiv:1805.05300





 $A = \Delta \gamma_{\text{\{SP\}}} / \Delta \gamma_{\text{\{PP\}}}, \ a = v_2_{\text{\{SP\}}} / v_2_{\text{\{PP\}}}$ 

# Au+Au Collisions at 200 GeV (2.4B MB)

STAR, PRL 128 (2022) 092301, arXiv:2106.09243



- Peripheral 50-80% collisions: consistent-with-zero signal with relatively large errors
- Mid-central 20-50% collisions: indication of finite CME signal with 1-3 $\sigma$  significance
- How much is there remaining nonflow contamination?

#### **REMAINING NONFLOW EFFECTS**

$$f_{\rm CME} = \frac{\Delta \gamma_{\rm CME}(\rm PP)}{\Delta \gamma(\rm PP)} = \frac{A/a^{-1}}{1/a^2 - 1} \qquad \frac{A}{a} = \frac{\Delta \gamma\{\rm SP\}/\Delta \gamma\{\rm PP\}}{v_2\{\rm SP\}/v_2^*\{\rm PP\}} = \frac{\Delta C_3\{\rm SP\}}{v_2^2\{\rm SP\}} \cdot \frac{v_2^{*2}\{\rm PP\}}{C_3\{\rm PP\}} = \frac{1 + \varepsilon_{\rm nf}}{1 + \frac{\varepsilon_3/\varepsilon_2}{Nv_2^2\{\rm PP\}}}$$

$$\Delta C_3 = 2\left\langle a_1^2 \right\rangle v_{2,c\perp B} + \frac{C_{2p}N_{2p}}{N^2} v_{2,2p}v_{2,c} + \frac{C_{3p}N_{3p}}{2N^3}$$
Nonflow in  $\Delta \gamma \rightarrow {\rm negative} f_{\rm CME}$ 

$$\Delta C_3^{\rm Bkg}\{\rm SP\} = \frac{C_{2p}N_{2p}}{N^2} v_{2,2p}\{\rm SP\}v_{2,c}\{\rm SP\}$$

$$\Delta C_3^{\rm Bkg}\{\rm EP\} = \frac{C_{2p}N_{2p}}{N^2} v_{2,2p}\{\rm SP\}v_{2,c}\{\rm EP\} + \frac{C_{3p}N_{3p}}{2N^3}$$

$$\varepsilon_3 = \frac{C_{3p}N_{3p}}{2N}$$
Nonflow in  $v_2 \rightarrow {\rm positive} f_{\rm CME}$ 

$$\varepsilon_3 = \frac{C_{3p}N_{3p}}{2N}$$

$$f_{\rm CME}^* \approx \left(\epsilon_{\rm nf} - \frac{\epsilon_3/\epsilon_2}{Nv_2^2 \{\rm EP\}}\right) \left/ \left(\frac{1+\epsilon_{\rm nf}}{a^2} - 1\right) \right. \qquad f_{\rm CME}^* = \left(\frac{1+\epsilon_{\rm nf}}{1+\frac{\epsilon_3/\epsilon_2}{Nv_2^2 \{\rm EP\}}} - 1\right) \left/ \left(\frac{1+\epsilon_{\rm nf}}{a^2} - 1\right) = \left(\frac{1+\epsilon_{\rm nf}}{1+\frac{(1+\epsilon_{\rm nf})\epsilon_3/\epsilon_2}{Nv_2^2 \{\rm EP\}}} - 1\right) \right/ \left(\frac{1+\epsilon_{\rm nf}}{a^2} - 1\right) = \left(\frac{1+\epsilon_{\rm nf}}{1+\frac{(1+\epsilon_{\rm nf})\epsilon_3/\epsilon_2}{Nv_2^2 \{\rm EP\}}} - 1\right) \right/ \left(\frac{1+\epsilon_{\rm nf}}{a^2} - 1\right) = \left(\frac{1+\epsilon_{\rm nf}}{1+\frac{(1+\epsilon_{\rm nf})\epsilon_3/\epsilon_2}{Nv_2^2 \{\rm EP\}}} - 1\right) \right/ \left(\frac{1+\epsilon_{\rm nf}}{a^2} - 1\right) = \left(\frac{1+\epsilon_{\rm nf}}{1+\frac{(1+\epsilon_{\rm nf})\epsilon_3/\epsilon_2}{Nv_2^2 \{\rm EP\}}} - 1\right) \right/ \left(\frac{1+\epsilon_{\rm nf}}{a^2} - 1\right) = \left(\frac{1+\epsilon_{\rm nf}}{1+\frac{(1+\epsilon_{\rm nf})\epsilon_3/\epsilon_2}{Nv_2^2 \{\rm EP\}}} - 1\right) \right) \right/ \left(\frac{1+\epsilon_{\rm nf}}{a^2} - 1\right) = \left(\frac{1+\epsilon_{\rm nf}}{1+\frac{(1+\epsilon_{\rm nf})\epsilon_3/\epsilon_2}{Nv_2^2 \{\rm EP\}}} - 1\right) \right) \right) \left(\frac{1+\epsilon_{\rm nf}}{a^2} - 1\right)$$

# MODEL ESTIMATES OF NONFLOW



## **IMPLICATIONS TO Au+Au DATA**

STAR, PRL 128 (2022) 092301, arXiv:2106.09243 Feng, FW, et al., PRC 105 (2022) 024913, arXiv:2106.15595



There may indeed be hint of CME in the Au+Au data

#### **BACK TO ISOBAR DATA**

$$\Delta C_3 = 2 \left\langle a_1^2 \right\rangle v_{2,c\perp B} + \frac{C_{2p} N_{2p}}{N^2} v_{2,2p} v_{2,c} + \frac{C_{3p} N_{3p}}{2N^3}$$

$$\Delta C_3^{\text{Ru}} \{\text{EP}\} = \left(\frac{C_{2p}N_{2p}}{N^2}v_{2,2p}\{\text{EP}\}v_{2,c}\{\text{EP}\}\right)^{\text{Ru}} + \left(\frac{C_{3p}N_{3p}}{2N^3}\right)^{\text{Ru}}$$
$$\Delta C_3^{\text{Zr}} \{\text{EP}\} = \left(\frac{C_{2p}N_{2p}}{N^2}v_{2,2p}\{\text{EP}\}v_{2,c}\{\text{EP}\}\right)^{\text{Zr}} + \left(\frac{C_{3p}N_{3p}}{2N^3}\right)^{\text{Zr}}$$

Au+Au  

$$\Delta C_{3}^{\text{Bkg}}\{\text{SP}\} = \frac{C_{2p}N_{2p}}{N^{2}}v_{2,2p}\{\text{SP}\}v_{2,c}\{\text{SP}\}$$

$$\Delta C_{3}^{\text{Bkg}}\{\text{EP}\} = \frac{C_{2p}N_{2p}}{N^{2}}v_{2,2p}\{\text{EP}\}v_{2,c}\{\text{EP}\} + \frac{C_{3p}N_{3p}}{2N^{3}}$$



- Depending on the relative Ru+Ru/Zr+Zr difference of various nonflow effects, the baseline can be above, equal, or below unity
- Final isobar conclusion requires detailed nonflow studies

## **REMAINING NONFLOW EFFECTS**

FENG, Yicheng (STAR): QM'2022, SQM'2022



## **REMAINING NONFLOW EFFECTS**

FENG, Yicheng (STAR): QM'2022, SQM'2022

$$\boxed{C_3 = \frac{C_{2p}N_{2p}}{N^2}v_{2,2p}v_2 + \frac{C_{3p}N_{3p}}{2N^3}; \quad C_{2p} \equiv \left\langle \cos(\alpha + \beta - 2\phi_{2p}) \right\rangle}_{C_{3p}} \equiv \left\langle \cos(\alpha + \beta - 2c) \right\rangle_{3p}}$$

$$\begin{bmatrix} \varepsilon_{2} \equiv \frac{C_{2p}N_{2p}}{N} \cdot \frac{v_{2,2p}}{v_{2}} \\ \varepsilon_{3} \equiv \frac{C_{3p}N_{3p}}{2N} \end{bmatrix} \begin{bmatrix} v_{2}^{*2} \equiv v_{2}^{2} + v_{2,nf}^{2} \\ \varepsilon_{nf} \equiv v_{2,nf}^{2} / v_{2}^{2} \end{bmatrix} \quad N \approx N_{+} \approx N_{-} \\ \Delta X \equiv X^{\text{Ru}} - X^{\text{Zr}}$$





# REMAINING NONFLOW EFFECTS FENG, Yicheng (STAR): QM'2022, SQM'2022

$$\frac{\left[C_{3} = \frac{C_{2p}N_{2p}}{N^{2}}v_{2,2p}v_{2} + \frac{C_{3p}N_{3p}}{2N^{3}}; C_{2p} = \left(\cos(\alpha + \beta - 2\phi_{3})\right)\right]}{\left[C_{3p} = \left(\cos(\alpha + \beta - 2c\right)\right]_{v_{p}}}$$

$$\frac{\left(N\Delta\gamma/v_{2}^{*}\right)^{Ru}}{\left(N\Delta\gamma/v_{2}^{*}\right)^{2r}} = \frac{\left(NC_{3}/v_{2}^{*2}\right)^{Ru}}{\left(NC_{3}/v_{2}^{*2}\right)^{2r}} \approx \frac{\mathcal{E}_{2}^{Ru}}{\mathcal{E}_{2}^{2r}} \cdot \frac{\left(1 + \mathcal{E}_{nf}\right)^{2r}}{\left(1 + \mathcal{E}_{nf}\right)^{Ru}} \cdot \frac{\left(1 + \frac{\mathcal{E}_{3}/\mathcal{E}_{2}}{Nv_{2}^{2}}\right)^{Ru}}{\left(1 + \mathcal{E}_{nf}\right)^{2r}} \approx \frac{\mathcal{E}_{2}^{Ru}}{\mathcal{E}_{2}^{2r}} \cdot \frac{\left(1 + \mathcal{E}_{nf}\right)^{2r}}{\left(1 + \mathcal{E}_{nf}\right)^{Ru}} \cdot \frac{\left(1 + \frac{\mathcal{E}_{3}/\mathcal{E}_{2}}{Nv_{2}^{2}}\right)^{2r}}{\left(1 + \mathcal{E}_{nf}\right)^{2r}} \approx \frac{\mathcal{E}_{2}^{Ru}}{\mathcal{E}_{2}^{2r}} - \frac{\Delta\mathcal{E}_{nf}}{1 + \mathcal{E}_{nf}} + \frac{\frac{\mathcal{E}_{3}/\mathcal{E}_{2}}{Nv_{2}^{2}}}{\left(\frac{\Delta\mathcal{E}_{3}}{Nv_{2}^{2}} - \frac{\Delta N}{N} - \frac{\Delta v_{2}^{2}}{\mathcal{E}_{2}}\right)^{2r}}{\left(\frac{\Delta \gamma}{Nv_{2}^{2}}\right)^{2r}} \approx \frac{\mathcal{E}_{2}^{Ru}}{\mathcal{E}_{2}^{2r}} - \frac{\Delta\mathcal{E}_{nf}}{1 + \mathcal{E}_{nf}} + \frac{\mathcal{E}_{3}/\mathcal{E}_{2}}{\frac{Nv_{2}^{2}}{Nv_{2}^{2}}} \left(\frac{\Delta\mathcal{E}_{3}}{\mathcal{E}_{3}} - \frac{\Delta\mathcal{E}_{2}}{\mathcal{E}_{2}} - \frac{\Delta N}{N} - \frac{\Delta v_{2}^{2}}{\mathcal{E}_{2}^{2}}\right)^{2r}}{\left(\frac{\Delta \gamma}{Nv_{2}^{2}}\right)^{2r}} = \frac{100}{(1 + \mathcal{E}_{nf})^{2r}} = \frac{100}{(1 + \mathcal{E}_{nf})^{2}} = \frac{100}{(1 + \mathcal{E}_{$$

# **ISOBAR SIGNAL MAY BE SMALL**

Feng, Lin, Zhao & FW, PLB 820 (2021) 136549, arXiv:2103.10378

AVFD simulations in preparation for isobar blind analysis



Caveats: Axial charge densities and sphaleron transition probabilities could be different between Au+Au and isobar, e.g. AVFD-glasma  $\mu_5$ /s: isobar/AuAu ~ 1.5

# SUMMARY, NEAR FUTURE, OUTLOOK

- CME is a very important physics. Large efforts to eliminate backgrounds.
  - Flow-induced background
  - $\circ$  Nonflow contamination in v<sub>2</sub> measurements
  - Genuine 3-particle correlation background

- Invariant mass depndence
- Event-shape engineering
- Isobar collisions
- Spectator/participant plane comparison
- Isobar signal consistent with zero (not contradictory to Au+Au);
   Stringent upper limit on the way.
- Au+Au data (2.4 B MB events) hint at finite CME signal with small significance;
   Rigorous nonflow data analysis on the way. Expect 20B Au+Au from 2023+25 runs.