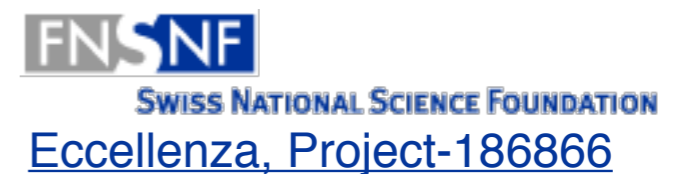


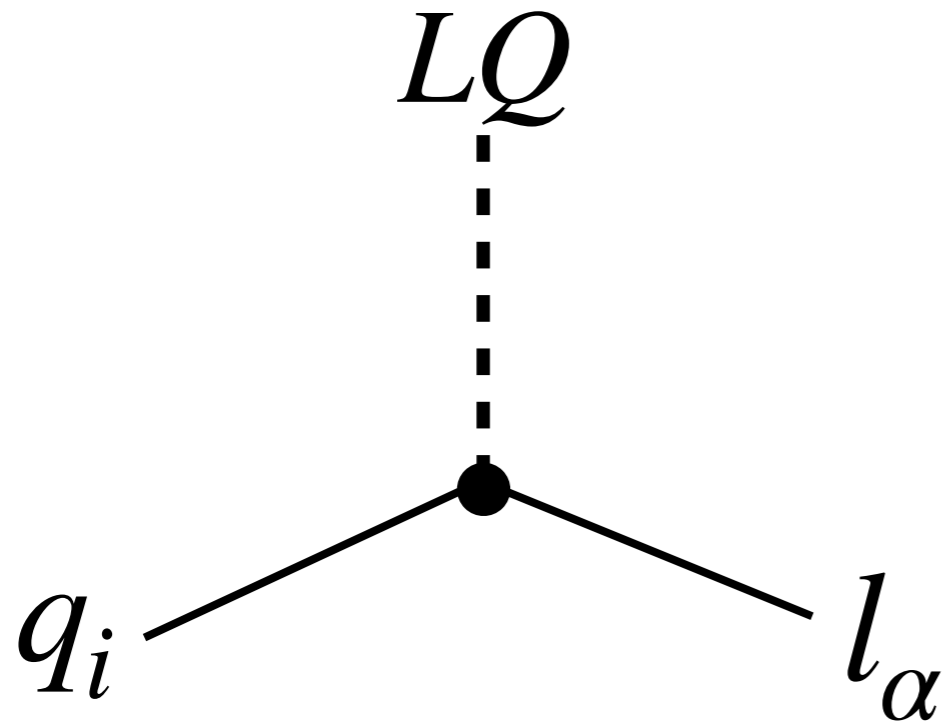
# Model building and phenomenology with leptoquarks

Admir Greljo



# Leptoquarks at the TeV scale?

Doršner, Fajfer, AG, Kamenik, Košnik; [1603.04993](#) (Physics Reports Review)

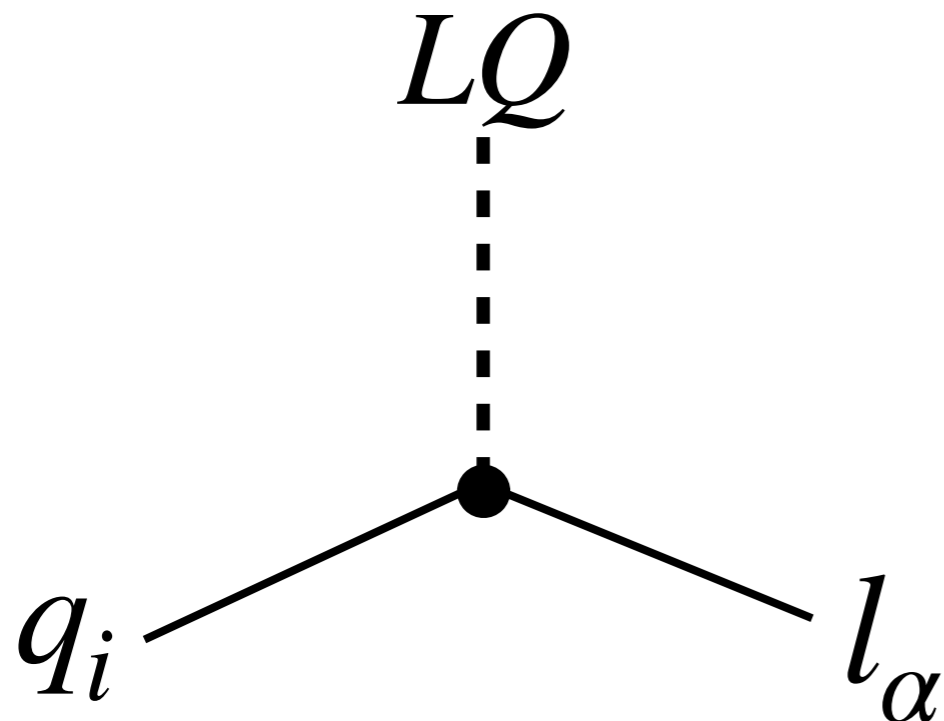


## Wanted:

- A LQ with a TeV-scale mass and (some)  $\mathcal{O}(1)$  couplings

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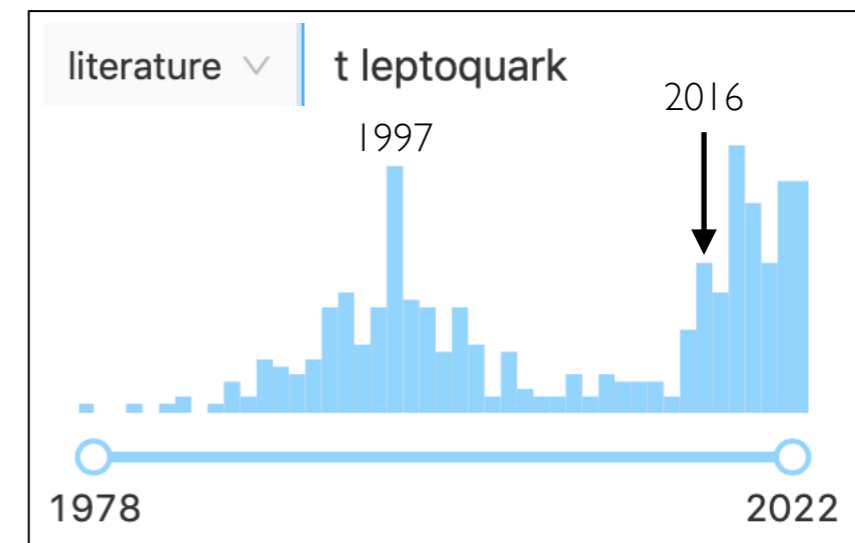
## Wanted:

- A LQ with a TeV-scale mass and (some)  $\mathcal{O}(1)$  couplings

## Why?

### Phenomenology

- Rich collider and flavor pheno?



### Theory

- Quark-lepton unification!  
Pati-Salam, SU(5), SO(10) GUT predict LQs but generically not in this mass-coupling range.  
New model building directions...

# Outline

## PART I

- Gauged lepton flavour: Selection rules for a TeV-scale leptoquark

Davighi, AG, Thomsen; [2202.05275](#)

AG, Stangl, Thomsen; [2103.13991](#)

## PART II

- A catalog of lepton flavour gauged  $U(1)_X$  models and applications

AG, Soreq, Stangl, Thomsen, Zupan; [2107.07518](#)

# Outline (Backup)

## PART I

- Phenomenology of a light lepton flavoured  $U(1)_X$  gauge boson  
AG, Stangl, Thomsen, Zupan; [2203.13731](#)

## PART II

- Interpretation of  $b \rightarrow s\ell\ell$  anomalies after the recent LHCb update  
AG, Salko, Smolkovic, Stangl; [2212.10497](#)

## PART III

- Future colliders: FCC-hh versus Muon Collider  
Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; [2205.13552](#)

# Accidental Symmetries in the SM

$$q_i, \ell_i, U_i, D_i, E_i \quad \text{flavour } i = 1, 2, 3$$

$$\mathcal{L}_{\text{SM}} \text{ sans Yukawa: } U(3)_q \times U(3)_\ell \times U(3)_U \times U(3)_D \times U(3)_E$$

$$-\mathcal{L}_{\text{Yuk}} = \bar{q} V^\dagger \hat{Y}_u \tilde{H} U + \bar{q} \hat{Y}_d H D + \bar{\ell} \hat{Y}_e H E$$

[ $U(3)^5$  transformation and a singular value decomposition theorem]



$$\mathcal{L}_{\text{SM}} : U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$$

- $B - L$  and  $L_i - L_j$  are exact
- $B + L$  is anomalous: non-perturbative dynamics implies a selection rule  $\Delta B = \Delta L = 0 \pmod{3}$

# TeV-scale BSM?

- A viable model at the TeV-scale should not (excessively) violate the accidental symmetries.
- Not a generic case!

## Example: Leptoquarks

$$\dim[\mathcal{O}] = 4$$

$$\mathcal{L}_4 = y_{ij} Q^i L^j S + z_{ij} Q^i Q^j S^\dagger$$

$B(S) = -\frac{1}{3}$                        $B(S) = \frac{2}{3}$

~~$U(1)_B$~~       Proton decay  $[z \cdot \gamma]$        $\tau_p \gtrsim 10^{34}$  years





~~$U(1)_e \times U(1)_\mu \times U(1)_\tau$~~        $\mu \rightarrow e \gamma$   $[i \neq j]$        $BR(\mu \rightarrow e \gamma) \lesssim 10^{-13}$

\* Dim-5  $qlS\phi$  can also be problematic.

\* Global symmetries are a low-energy property. Quantum gravity breaks them.

- Generic TeV-scale LQs are dead!

PART I

Gauged  $U(1)_X$    $e$   $\mu$   $\tau$   
+ leptoquarks   

The storyline

- Selection rules for a TeV-scale leptoquark
- Neutrino masses
- Proton stability
- Unification





# A $U(1)_X$ model

■ The initial model  $U(1)_{B-3L_\mu}$  AG, Stangl, Thomsen; [2103.13991](#)

■ The generalisation

$$X = 3m(B - L) - n(2L_\mu - L_e - L_\tau) , \quad \gcd(m, n) = 1$$

Davighi, AG, Thomsen; [2202.05275](#)

# A $U(1)_X$ model

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Davighi, AG, Thomsen; [2202.05275](#)

	Fields	$U(1)_X$
Quarks	$q_i, u_i, d_i$	$m$
Electrons and taus	$\ell_{1,3}, e_{1,3}, \nu_{1,3}$	$n - 3m$
Muons	$\ell_2, e_2, \nu_2$	$-2n - 3m$
Higgs	$H$	$0$
$(\bar{\mathbf{3}}, \mathbf{3}/\mathbf{1})_{1/3}$ — Leptoquarks	$S_3, S_1$	$2m + 2n$
Scalars (SM singlets)	$\phi_{e\tau}$	$6m - 2n$
	$\phi_\mu$	$6m + n$

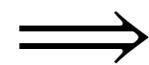
# Selection rules

Gauge symmetry selection rules:

✓  $q\mu S$

✗  $qqS^\dagger, qeS, q\tau S$

## “Muoquark”



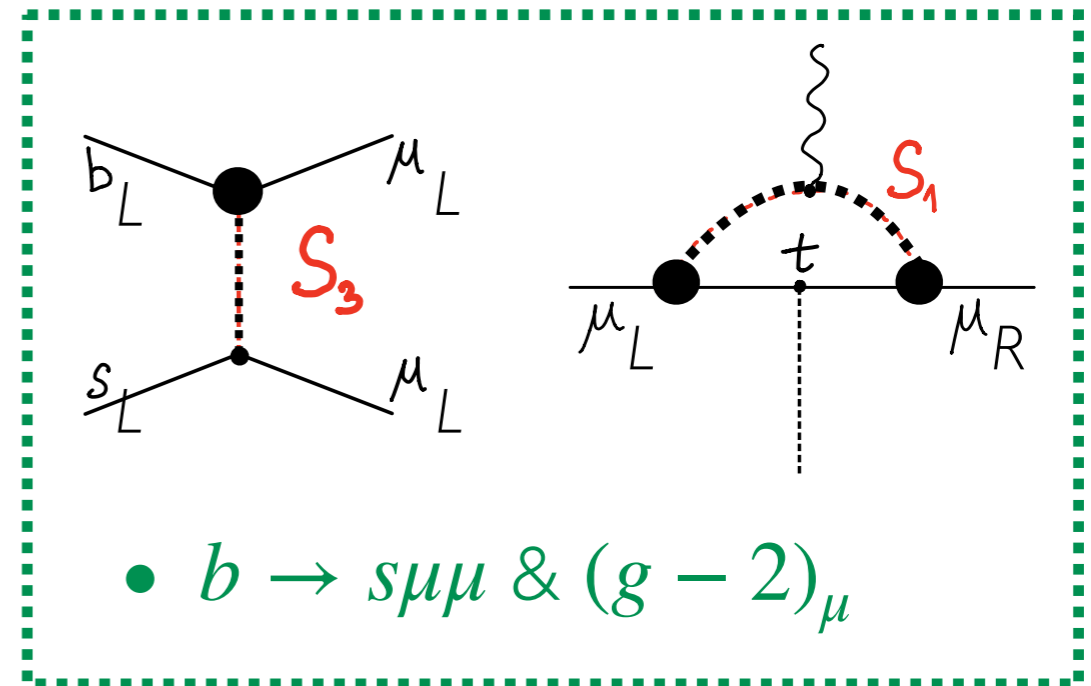
The accidental symmetry of  $\mathcal{L}_{LQ}$  is  $U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$  and the LQ charge is  $(-1/3, 0, -1, 0)$

# Selection rules

Gauge symmetry selection rules:

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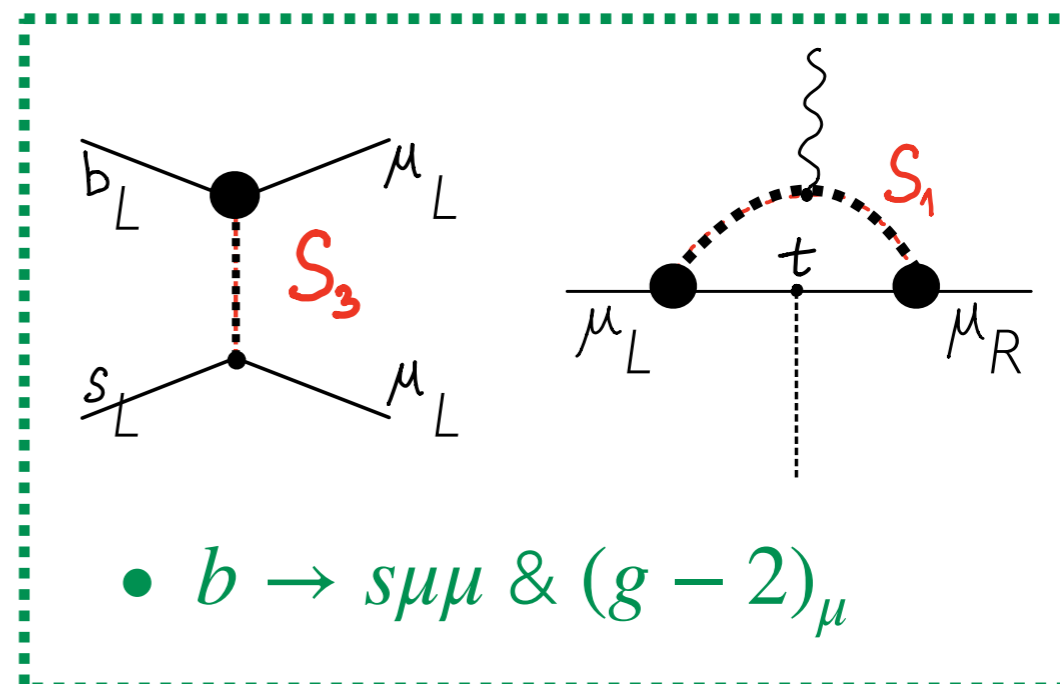


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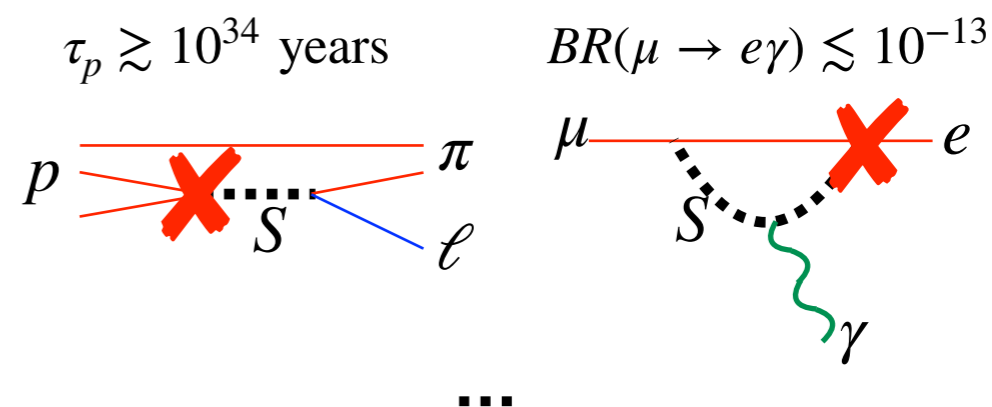
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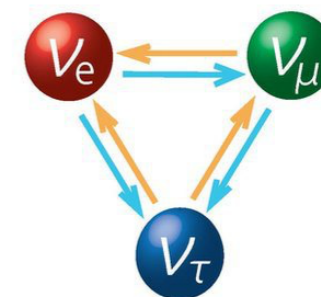


• No proton decay & cLFV



# Neutrino Masses

- The PMNS is full of  $\mathcal{O}(1)$  elements.
- The correct neutrino masses and mixings dictate the  $U(1)_X$  breaking.
- A dense Majorana mass matrix needs two SM-singlet scalar fields with charges  $6m - 2n$  and  $6m + n$  to get a VEV

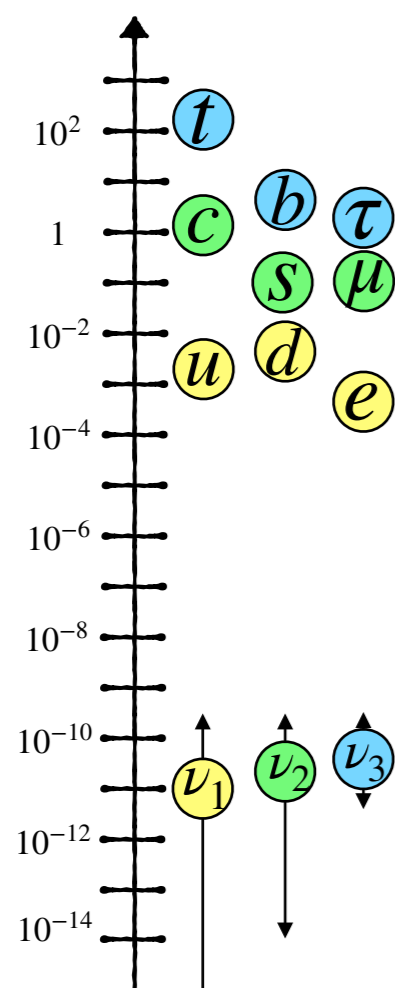


## Type-I seesaw mechanism

$$Y_\nu \sim \begin{pmatrix} \times & 0 & \times \\ 0 & \times & 0 \\ \times & 0 & \times \end{pmatrix} ; \quad \mathcal{L} \supset \bar{\nu}_R^{ic} \nu_R^j (\xi_{e\tau}^{ij} \phi_{e\tau} + \xi_{\mu}^{ij} \phi_\mu) \implies \frac{M_\nu}{v_X} \sim \begin{pmatrix} \times & \times & \times \\ \times & 0 & \times \\ \times & \times & \times \end{pmatrix}$$

- More general than two-zero minor structure type  $D_1^R$  [Asai; 1907.04042](#)
- This is enough to accommodate for:
  - Neutrino oscillations data,
  - The Planck limit on the sum of neutrino masses,
  - The absence of neutrinoless double beta decay.

# Neutrino Masses

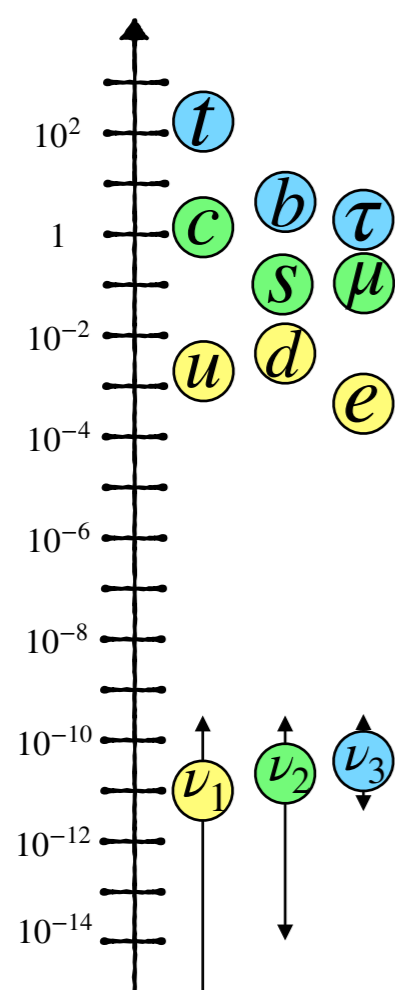


$U(1)_X$  breaking at the high scale?

The mass gap is explained if  $\langle \phi_{e\tau} \rangle, \langle \phi_\mu \rangle \gg \langle H \rangle$

Standard thermal leptogenesis at high scale

# Neutrino Masses



$U(1)_X$  breaking at the high scale?

The mass gap is explained if  $\langle \phi_{e\tau} \rangle, \langle \phi_\mu \rangle \gg \langle H \rangle$

Standard thermal leptogenesis at high scale

but

In the  $U(1)_X$  broken phase one can *naively* write “renormalisable” terms  $qqS^*$  and  $q_i \ell_j S$  that violate  $U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$

- What happens?
- Is there proton decay? cLFV?



# *The IR: discrete gauge subgroup*

$\phi_{e\tau}$	$6m - 2n$
$\phi_{\mu}$	$6m + n$

- Fixed by neutrinos

# The IR: discrete gauge subgroup

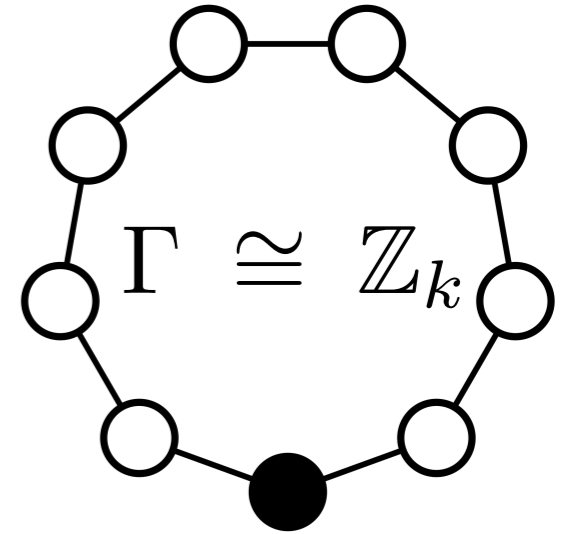
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- Fixed by neutrinos

$$k = \text{gcd}([\phi_{e\tau}]_X, [\phi_\mu]_X)$$

$$e^{i\frac{2\pi}{k}[\phi]_X}\phi = \phi$$

- The scalars  $\phi_{e\tau}$  and  $\phi_\mu$  are  $\Gamma$  singlets
- An unbroken discrete subgroup  $\Gamma \subset U(1)_X$  acting on matter in the IR



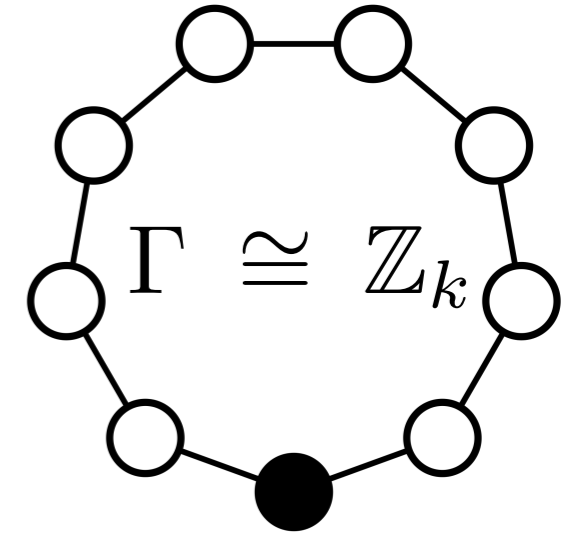
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- The diquark operators  $qqS^*$  are banned by  $\Gamma$  when:

$$(m, n) = (3a + r, 9b + 3r), \quad \text{for } r \in \{1, 2\},$$

$$(a, b) \in \mathbb{Z}^2, \text{ and } \text{gcd}(3a + r, b - a) = 1.$$

$$\Gamma \cong \begin{cases} \mathbb{Z}_9, & \text{for } b + r \in 2\mathbb{Z} + 1 \\ \mathbb{Z}_{18}, & \text{for } b + r \in 2\mathbb{Z} \end{cases}$$

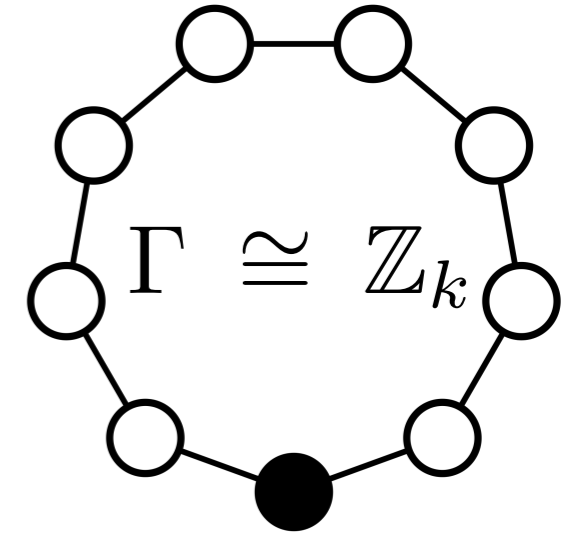
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- No proton decay!

- Both  $B - L$  and the lepton-flavoured factor required!  $X = 3m(B - L) - n(2L_\mu - L_e - L_\tau)$

# The IR: discrete gauge subgroup

$b + r \pmod{2}$	$\Gamma$	$\ell$	$q$	$S$	$qS\ell$	$qS^*q$
0	$\mathbb{Z}_{18}$	$9(b - a)$	$3a + r$	$6a + 8r$	0	$12r$
1	$\mathbb{Z}_9$	0	$3a + r$	$6a + 8r$	0	$3r$

Charges under the remnant discrete symmetry  $\Gamma$

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- The  $\Gamma$  protection goes beyond just banning the diquark operators. Integrate out  $S$ . Selection rule:

$$\Delta B = 0 \pmod{3}$$

**Exact proton stability to all orders in the SMEFT!**

~~$qqq\ell$~~  and so on

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**Exact proton stability to all orders in the SMEFT!**

~~$qqq\ell$~~  and so on

- Neutron—antineutron oscillations also forbidden
- $\Delta B = 3$  processes are allowed, in analogy to sphalerons.

## What about cLFV?

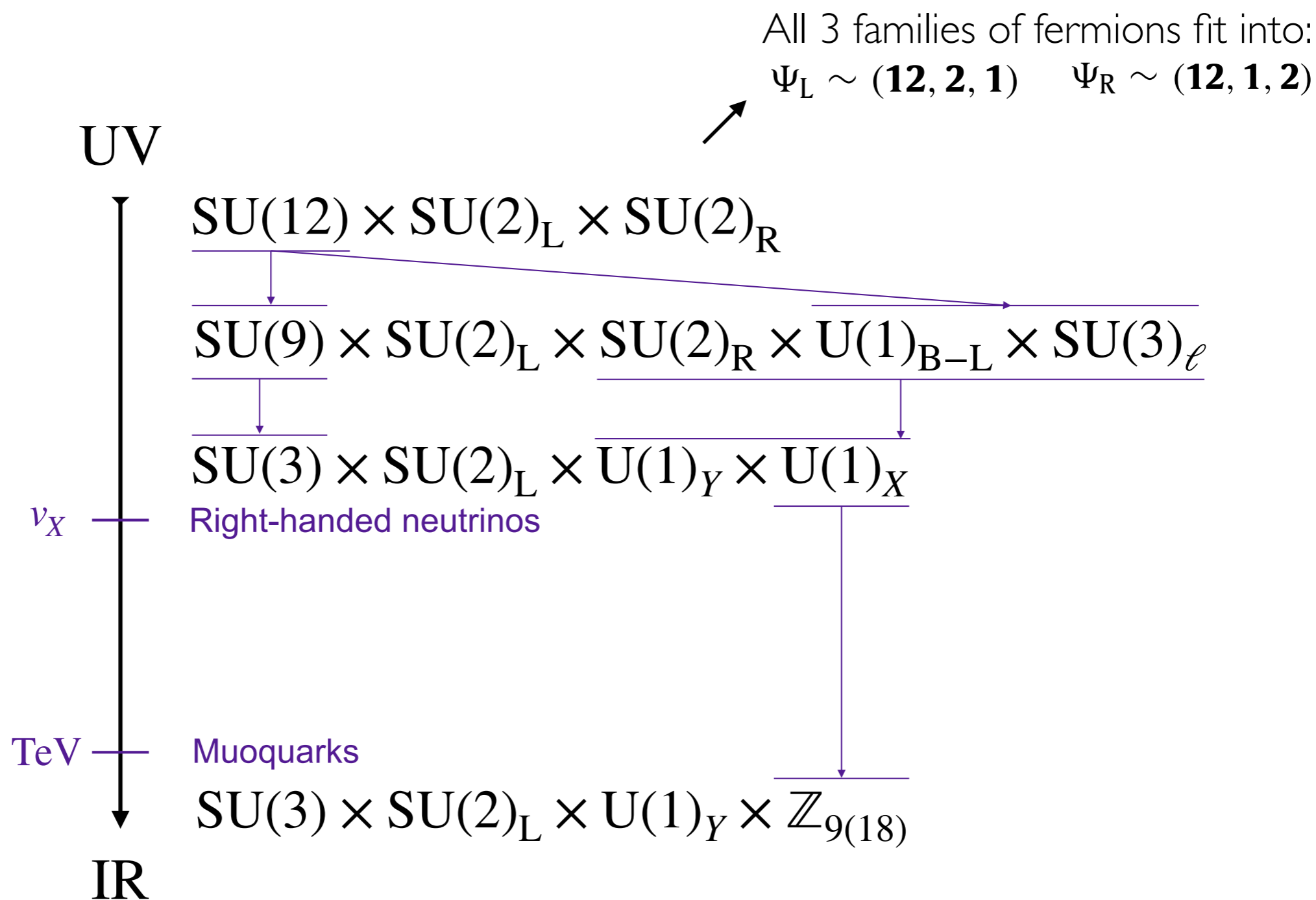
- $\Gamma$  is lepton flavour universal, otherwise no PMNS.
- cLFV through higher-dim. operators in the  $U(1)_X$ -invariant effective theory:

$$\frac{1}{\Lambda^2} \phi_{e\tau} \phi_{\mu}^* q \mathcal{S}_{1/3} \ell_{1,3} \qquad \frac{1}{\Lambda^2} \phi_{e\tau} \phi_{\mu}^* u \mathcal{S}_1 e_{1,3}$$

- A modest scale separation is sufficient to suppress cLFV processes to a level compatible with current bounds.



# Deeper into the UV: Unification



Tentative gauge–flavour unification scenario.

PART II

# Gauged $U(1)_X$

+ leptoquarks



## The storyline

- A catalog of models
- Radiative lepton masses and magnetic moments



# The $U(1)_X$ atlas

- 18 chiral fermions

$$\begin{aligned}
 Q_i &\sim (\mathbf{3}, \mathbf{2}, \frac{1}{6}, X_{Q_i}), & U_i &\sim (\mathbf{3}, \mathbf{1}, \frac{2}{3}, X_{U_i}), & D_i &\sim (\mathbf{3}, \mathbf{1}, -\frac{1}{3}, X_{D_i}), \\
 L_i &\sim (\mathbf{1}, \mathbf{2}, -\frac{1}{2}, X_{L_i}), & E_i &\sim (\mathbf{1}, \mathbf{1}, -1, X_{E_i}), & N_i &\sim (\mathbf{1}, \mathbf{1}, 0, X_{N_i}).
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 \end{aligned}$$

- Six anomaly cancelation conditions:

$$\begin{aligned}
 \text{SU}(3)_C^2 \times \text{U}(1)_X &: \sum_{i=1}^3 (2X_{Q_i} - X_{U_i} - X_{D_i}) = 0, \\
 \text{SU}(2)_L^2 \times \text{U}(1)_X &: \sum_{i=1}^3 (3X_{Q_i} + X_{L_i}) = 0, \\
 \text{U}(1)_Y^2 \times \text{U}(1)_X &: \sum_{i=1}^3 (X_{Q_i} + 3X_{L_i} - 8X_{U_i} - 2X_{D_i} - 6X_{E_i}) = 0, \\
 \text{Gravity}^2 \times \text{U}(1)_X &: \sum_{i=1}^3 (6X_{Q_i} + 2X_{L_i} - 3X_{U_i} - 3X_{D_i} - X_{E_i} - X_{N_i}) = 0, \\
 \text{U}(1)_Y \times \text{U}(1)_X^2 &: \sum_{i=1}^3 (X_{Q_i}^2 - X_{L_i}^2 - 2X_{U_i}^2 + X_{D_i}^2 + X_{E_i}^2) = 0, \\
 \text{U}(1)_X^3 &: \sum_{i=1}^3 (6X_{Q_i}^3 + 2X_{L_i}^3 - 3X_{U_i}^3 - 3X_{D_i}^3 - X_{E_i}^3 - X_{N_i}^3) = 0.
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- Integer charges:  $-10 \leq X_{F_i} \leq 10$  [Allanach, Davighi, Melville; 1812.04602](#)

21'546'920 inequivalent solutions (up to flavour permutation, etc)

# The $U(1)_X$ atlas

- The symmetry breaking scalar fields:

$$H = (\mathbf{1}, \mathbf{2}, \frac{1}{2}, X_H), \quad \phi = (\mathbf{1}, \mathbf{1}, 0, X_\phi)$$

$$X_H = 0$$

- Without loss of generality

\* By field redefinitions, shifting  $X_f \rightarrow X_f - aY_f$  for all fields, gives an equivalent theory.

$$\mathcal{L} \supset -\frac{1}{4} F_{i\mu\nu} h_{ij}^{-1} F_j^{\mu\nu},$$

$$U(1)^n = U(1)_1 \times \cdots \times U(1)_n$$

$$D_\mu^f = \partial_\mu - i q_i^f A_{i\mu}$$

Field redefinitions

$$A_i^\mu \rightarrow L_{ij} A_j^\mu$$



$$\mathcal{L} \supset -\frac{1}{4} F_{i\mu\nu} \tilde{h}_{ij}^{-1} F_j^{\mu\nu},$$

$$\tilde{h} = L^{-1} h (L^{-1})^\top$$

$$D_\mu^f = \partial_\mu - i \tilde{q}_i^f A_{i\mu},$$

$$\tilde{q}^f = L^\top q^f$$

$$\tilde{q}_f = L^\top q_f \quad \text{where} \quad L = \begin{pmatrix} 1 & -a \\ 0 & 1 \end{pmatrix}.$$



# Lepton-flavoured catalog

Quark flavour universal class

- $Y_{u,d}$  are allowed  $\Rightarrow X_{Q_i} = X_{U_j} = X_{D_k}$   
( $X_H = 0$ )

$$-10 \leq X_{F_i} \leq 10$$

[276 inequivalent solutions]

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 $(X_H = 0)$  [276 inequivalent solutions]
- Leptoquark selection rules  
 eg.  $S_3$  LQ:  $X_{L_2} \neq \{X_{L_{1,3}}, -3X_q\}$  [273 inequivalent solutions]  
 \* For all other LQs up to dim-5, see the paper.



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- Further classification:
  - $Y_e$  allowed  $\Rightarrow$  **vector category** :  $X_{L_i} = X_{E_i}$  [252 inequivalent solutions]
  - chiral category** : the rest. [21 inequivalent solutions]

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- Further classification:

$Y_e$  allowed  $\Rightarrow$  **vector category** :  $X_{L_i} = X_{E_i}$  [252 inequivalent solutions]

**chiral category** : the rest. [21 inequivalent solutions]

$$x_f = c_e L_e + c_\mu L_\mu + c_\tau L_\tau - \left( \frac{c_e + c_\mu + c_\tau}{3} \right) B + \sum_i c_{N_i} L_{N_i}$$

ACC:  $(c_e + c_\mu + c_\tau = \sum_i c_{N_i}$  and  $c_e^3 + c_\mu^3 + c_\tau^3 = \sum_i c_{N_i}^3)$

See backup

# Lepton-flavoured catalog

## Quark flavour universal class

$$-10 \leq X_{F_i} \leq 10$$

- $Y_{u,d}$  are allowed  $\Rightarrow X_{Q_i} = X_{U_j} = X_{D_k}$  [276 inequivalent solutions]  
( $X_H = 0$ )

- Leptoquark selection rules  
eg.  $S_3$  LQ:  $X_{L_2} \neq \{X_{L_{1,3}}, -3X_q\}$  [273 inequivalent solutions]

- Further classification:

$Y_e$  allowed  $\Rightarrow$  **vector category** :  $X_{L_i} = X_{E_i}$  [252 inequivalent solutions]

**chiral category** : the rest. [21 inequivalent solutions]

Next example

# Chiral models: Radiative $y_\mu$

- The dimension-4 muon Yukawa is forbidden by  $U(1)_X$

$$X_{L_2} \neq X_{E_2} \quad (X_H = 0)$$

Example:

$\tilde{L}_{\mu-\tau}$  model:

$$(X_{L_1}, X_{L_2}, X_{L_3}) = (0, 7, -7),$$

$$(X_{N_1}, X_{N_2}, X_{N_3}) = (5, 3, 8),$$

$$(X_{E_1}, X_{E_2}, X_{E_3}) = (-3, 8, -5),$$

$$X_{Q_i, D_i, U_i} = 0.$$

# Chiral models: Radiative $y_\mu$

- The dimension-4 muon Yukawa is forbidden by  $U(1)_X$

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- Introduce two scalar muoquarks  $S_\pm = (\mathbf{3}, \mathbf{2}, 7/6, X_{S_\pm})$

$$\mathcal{L} \supset \eta_L \bar{t}_R \ell_L^2 i\sigma_2 S_+ - \eta_R \bar{q}_L^3 \mu_R S_-$$

Charges:

$$X_{S_+} = -X_{L_2} + X_{U_i}$$

$$X_{S_-} = -X_{E_2} + X_{Q_i}$$

Example:

$\tilde{L}_{\mu-\tau}$  model:

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$$\mathcal{L} \supset -A\phi S_+^\dagger S_-$$

Charges:

$$X_{S_+} = -X_{L_2} + X_{U_i}$$

$$X_{S_-} = -X_{E_2} + X_{Q_i}$$

$$X_\phi = -X_{S_-} + X_{S_+}$$

Example:

$\tilde{L}_{\mu-\tau}$  model:

$$(X_{L_1}, X_{L_2}, X_{L_3}) = (0, 7, -7),$$

$$(X_{N_1}, X_{N_2}, X_{N_3}) = (5, 3, 8),$$

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# Chiral models: Radiative $y_\mu$

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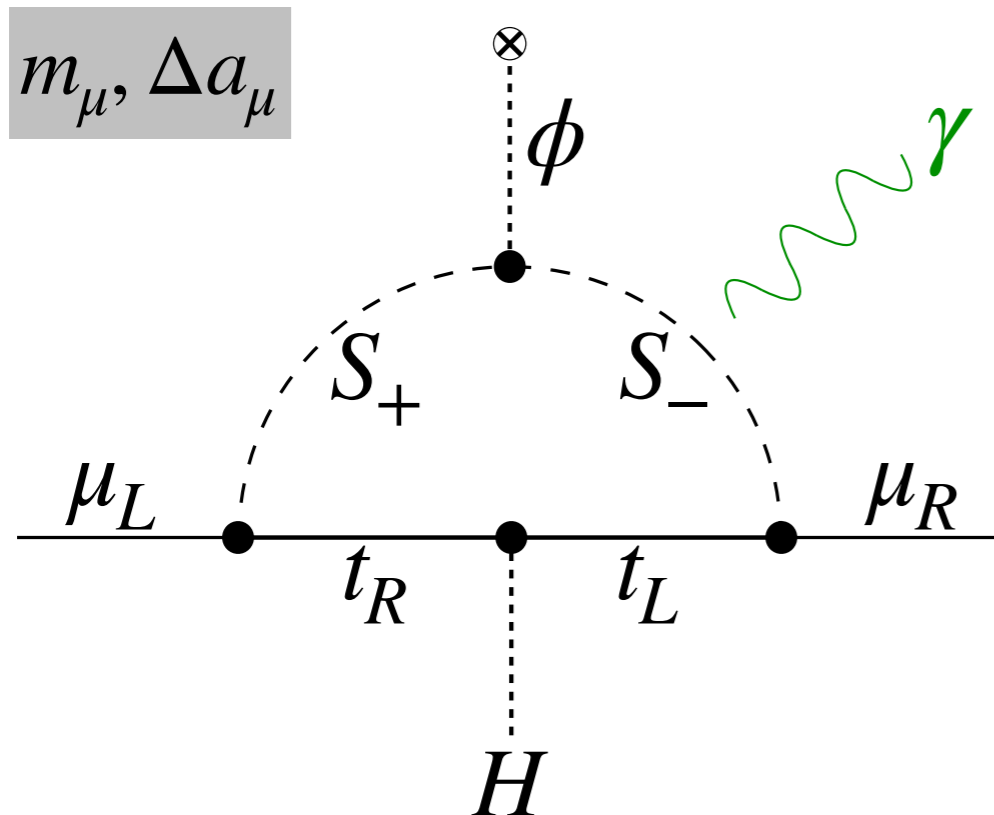
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$$\Delta a_\mu = \frac{m_\mu^2}{m_t^2} \tilde{F} \left( \frac{m_{S_1}^2}{m_t^2}, \frac{m_{S_2}^2}{m_t^2} \right)$$

$$\tilde{F}(x_1, x_2) = \left( \frac{x_1 \log x_1}{1-x_1} - \frac{x_2 \log x_2}{1-x_2} \right)^{-1} \left[ \frac{3x_1-1}{(1-x_1)^2} - \frac{3x_2-1}{(1-x_2)^2} + \frac{2x_1^2 \log x_1}{(1-x_1)^3} - \frac{2x_2^2 \log x_2}{(1-x_2)^3} + 2Q_S \left( \frac{1}{1-x_1} - \frac{1}{1-x_2} + \frac{x_1 \log x_1}{(1-x_1)^2} - \frac{x_2 \log x_2}{(1-x_2)^2} \right) \right]$$

# Chiral models: Radiative $y_\mu$

- The dimension-4 muon Yukawa is forbidden by  $U(1)_X$

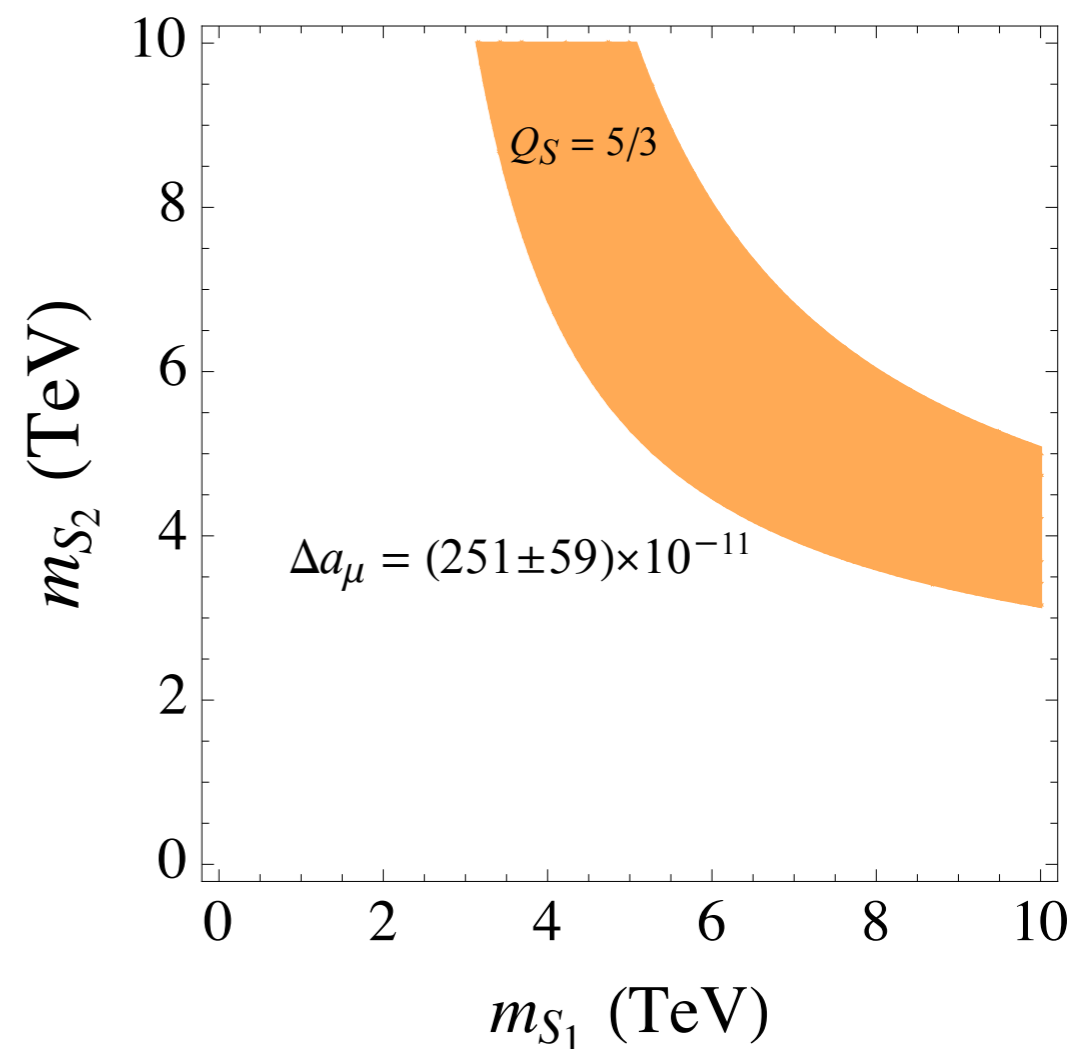
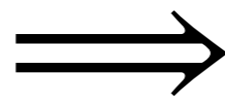
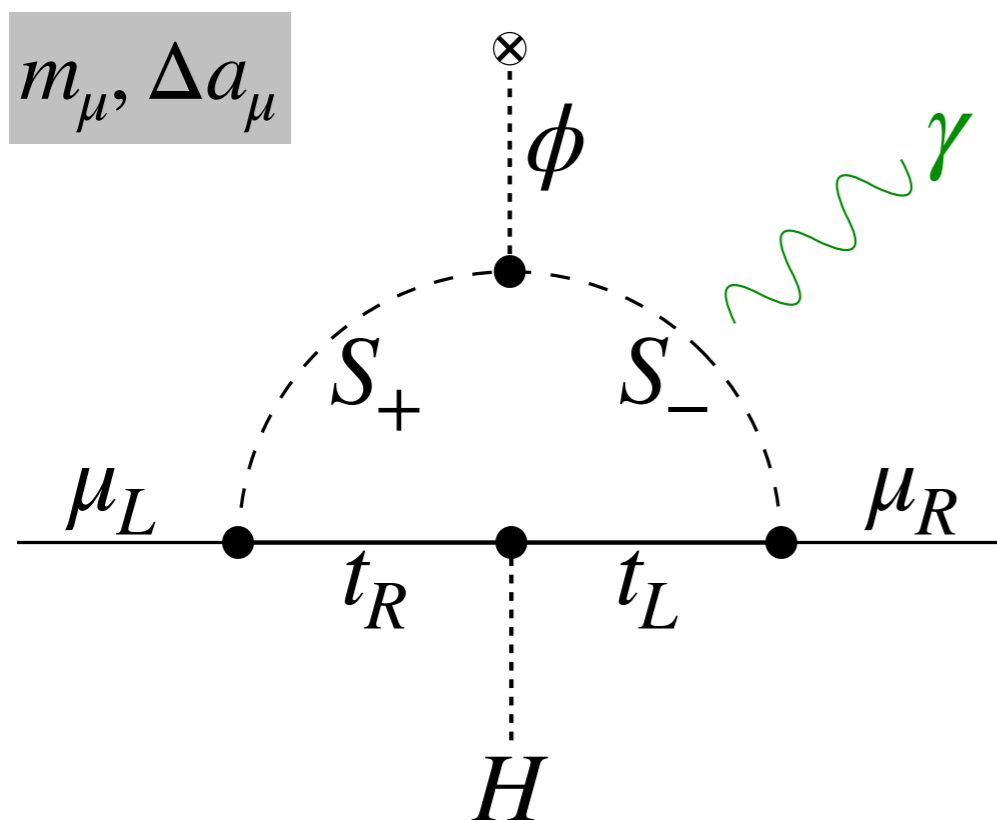
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- Mix them via  $U(1)_X$  breaking

$$\mathcal{L} \supset -A\phi S_+^\dagger S_-$$





# Conclusions

- Gauged lepton flavour  $\implies$  Selection rules for TeV-scale Leptoquarks
- A mechanism to render the proton **exactly** stable to all orders in EFT:  
*Spontaneously broken lepton-flavoured gauged  $U(1)$  in the UV to generate neutrino masses, leaving a discrete symmetry in the IR*
- A catalog of anomaly-free lepton flavour  $U(1)$  gauge models yet to fully be explored

***Backup***

PART I

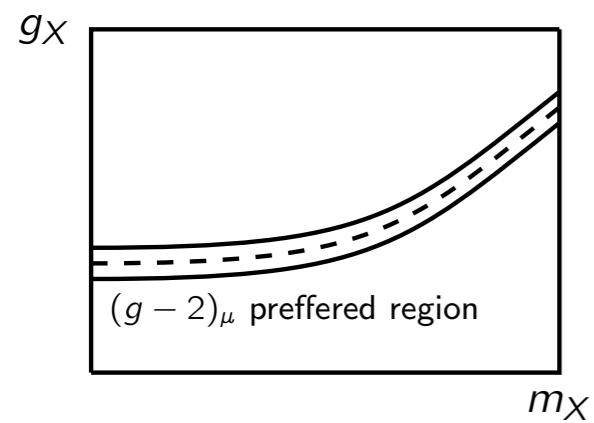
# Light $U(1)_X$ gauge boson

The storyline

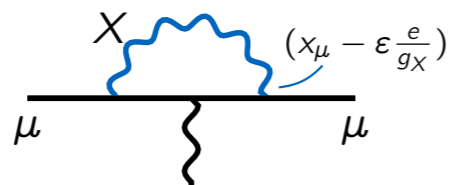
- In the context of  $(g-2)_\mu$

- Vector category:  $x_f = c_e L_e + c_\mu L_\mu + c_\tau L_\tau - \left( \frac{c_e + c_\mu + c_\tau}{3} \right) B + \sum_i c_{N_i} L_{N_i}$

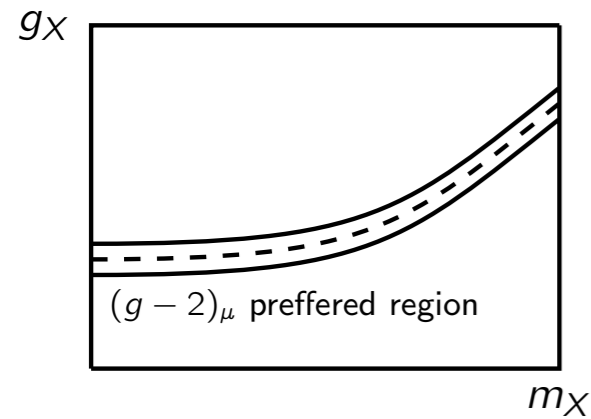
# Muon $(g - 2)_\mu$



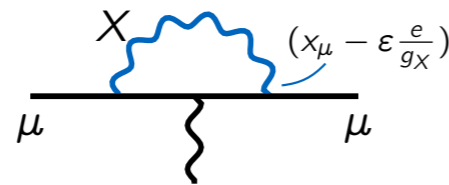
$x_f$ : charge of fermion  $f$   
 $\varepsilon$ : kinetic mixing of  $X$  and  $\gamma$



# Muon $(g - 2)_\mu$



$x_f$ : charge of fermion  $f$   
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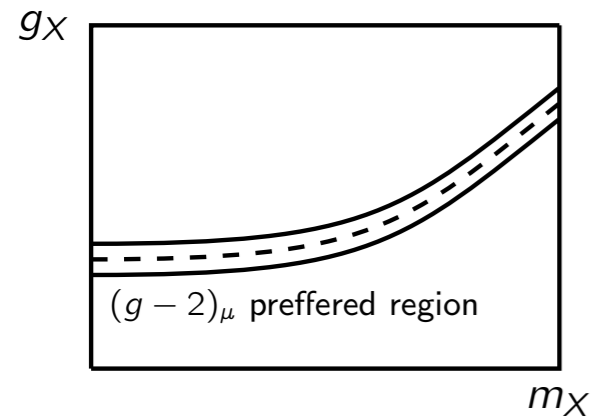
Targeted mass range 10 MeV — 1 TeV

- Renormalisable models

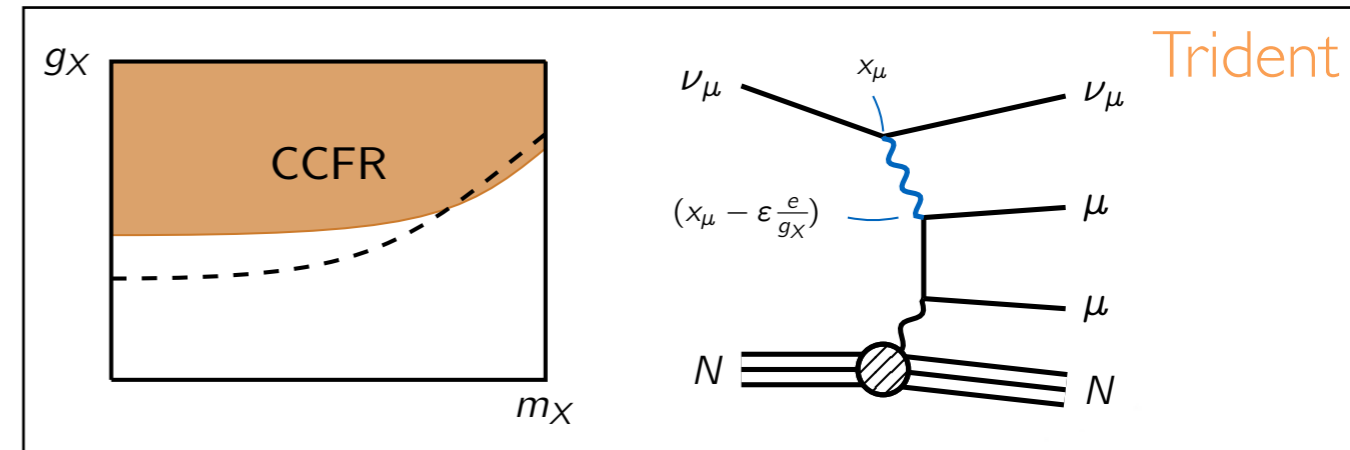
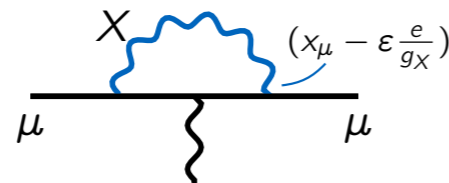
$$m_X \lesssim 4 \text{ GeV} \quad (\text{trident} + T)$$

AG, Stangl, Thomsen, Zupan; 2203.13731

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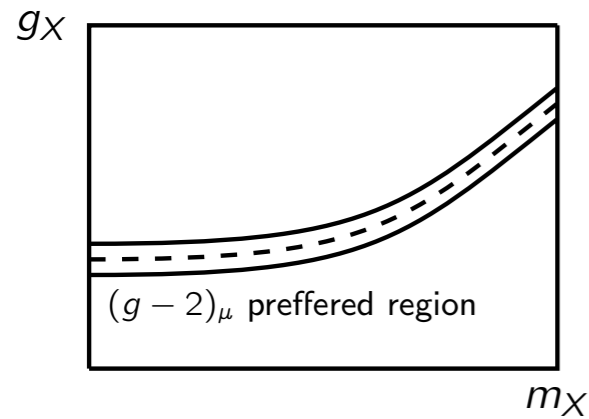
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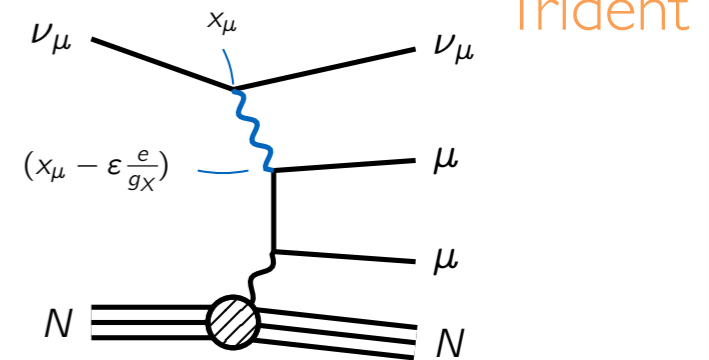
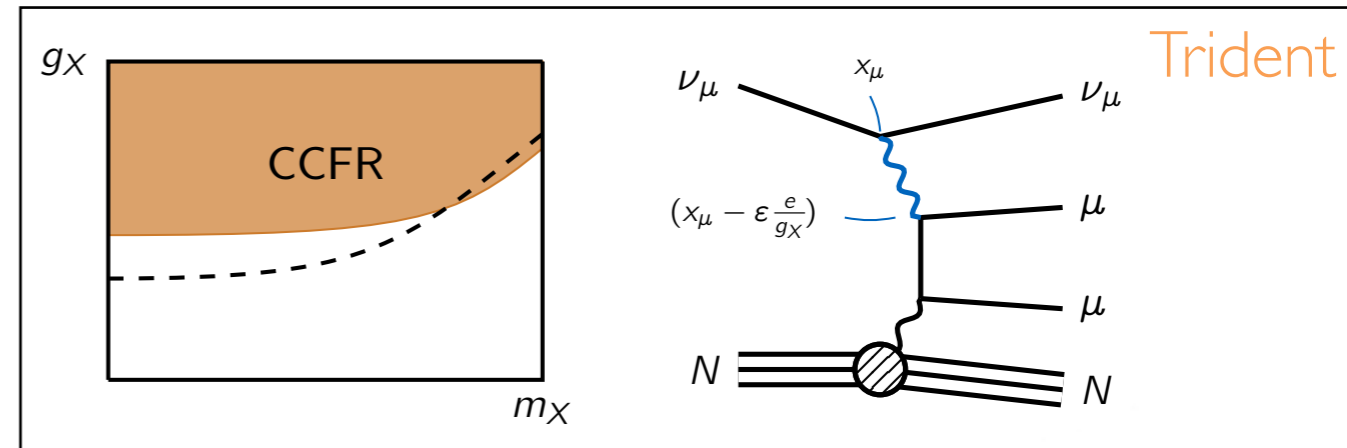
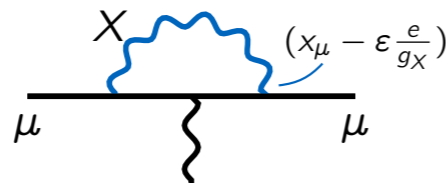
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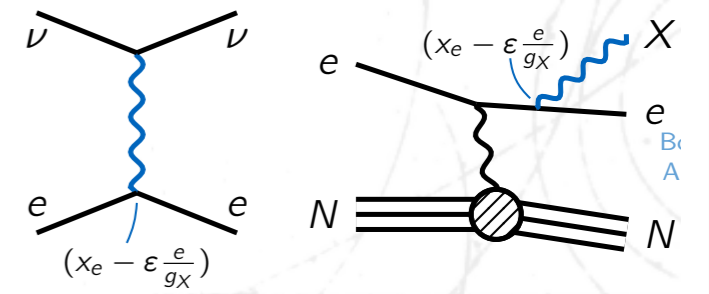
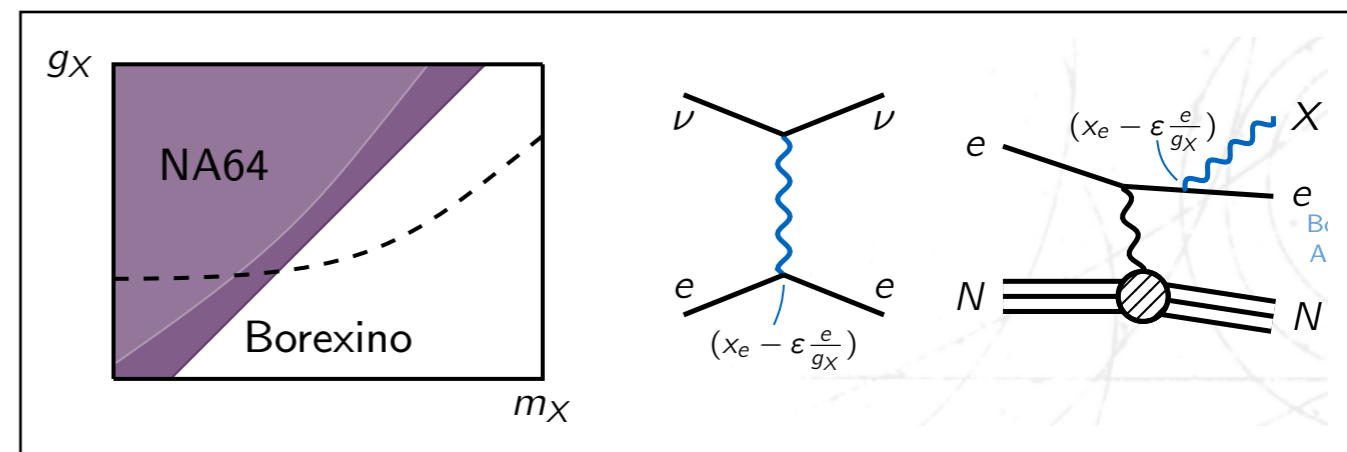


Targeted mass range 10 MeV — 1 TeV

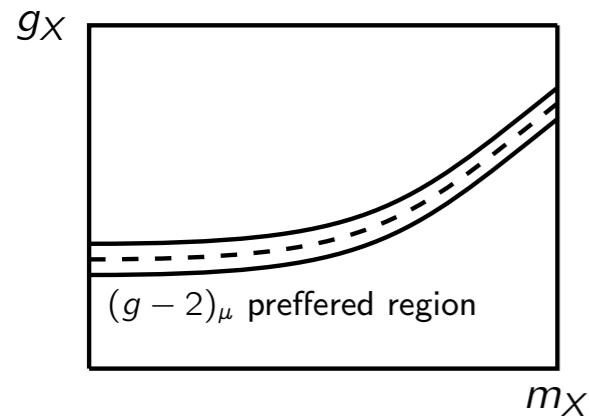
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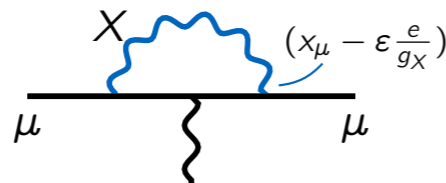
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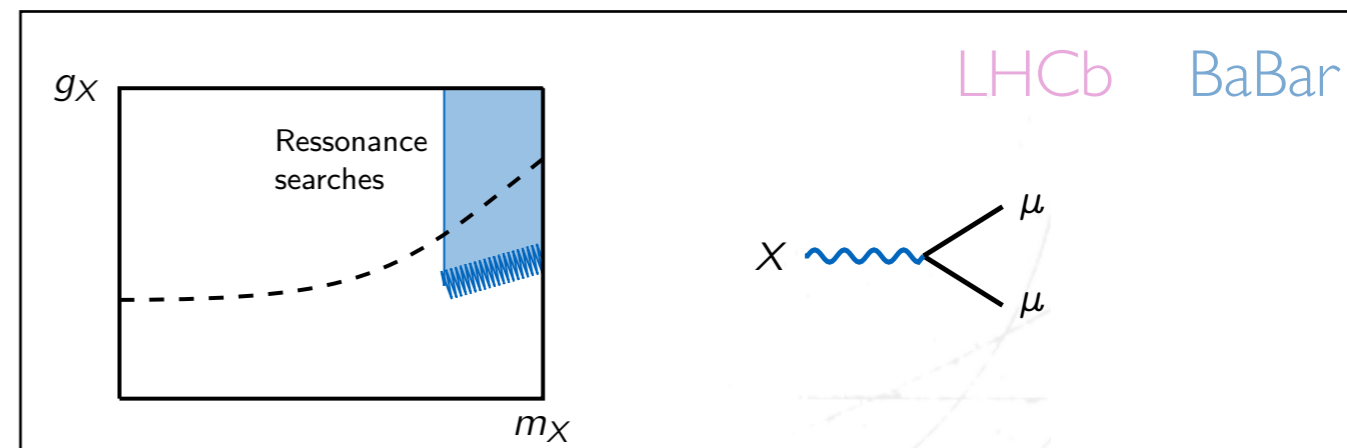
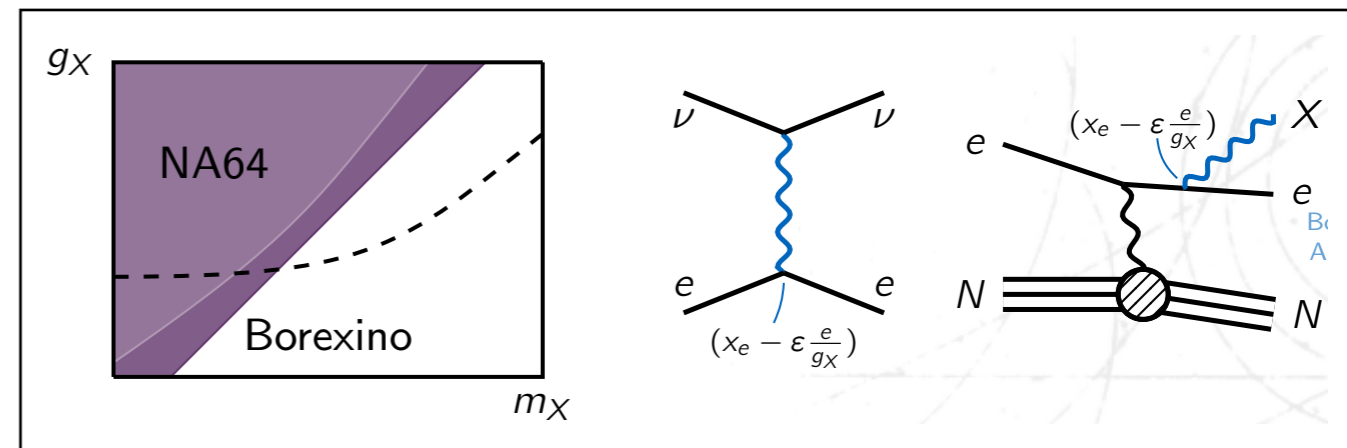
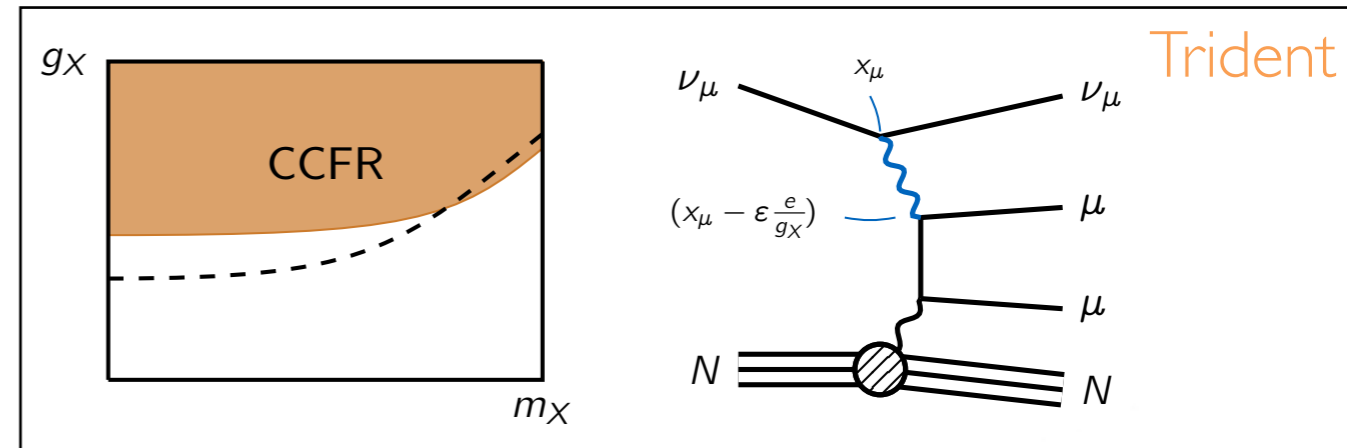


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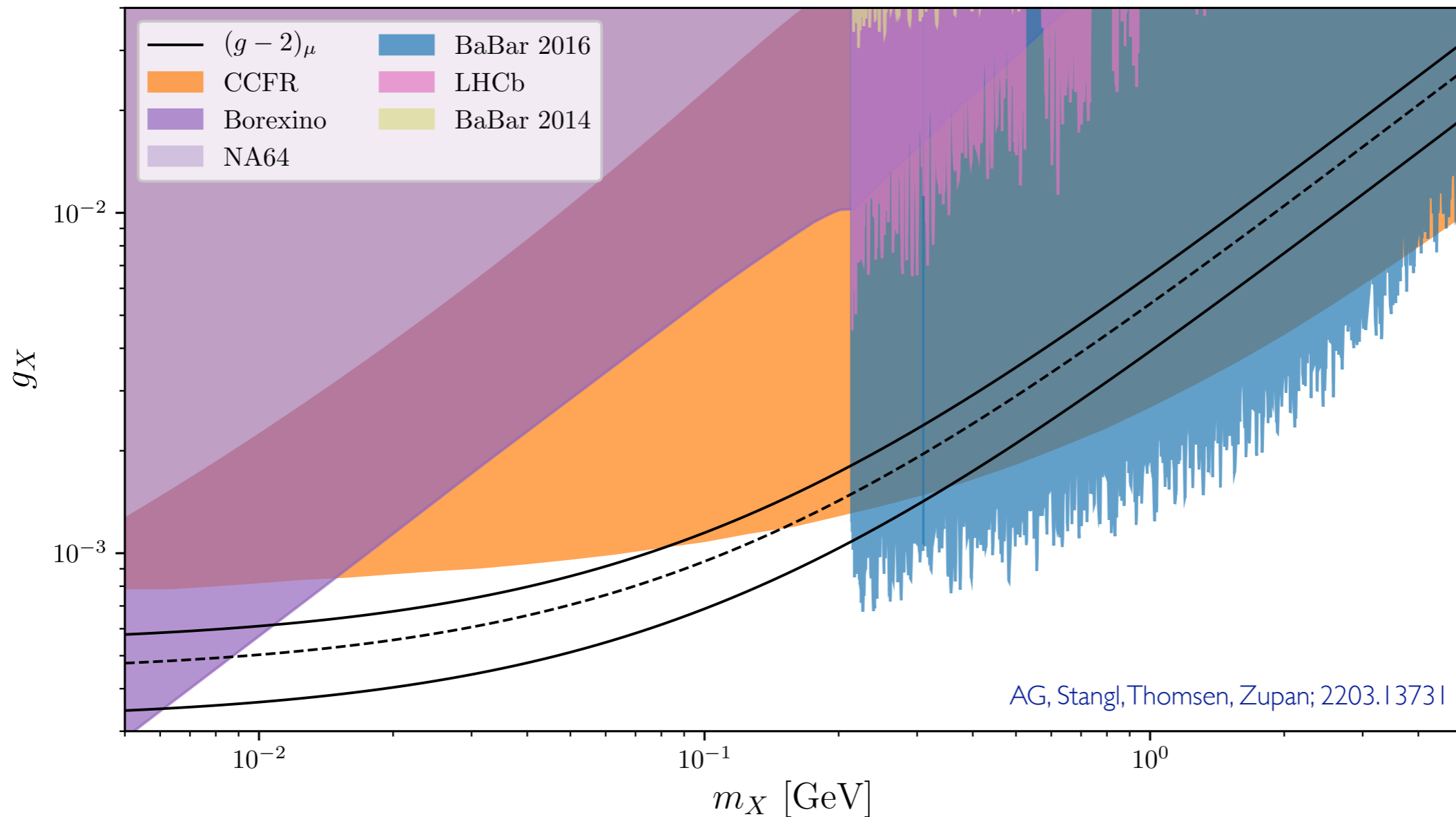
AG, Stangl, Thomsen, Zupan; 2203.13731





# Muon $(g - 2)_\mu$

$L_\mu - L_\tau$ ,  $\mu/\tau$ -loop effective kinetic mixing



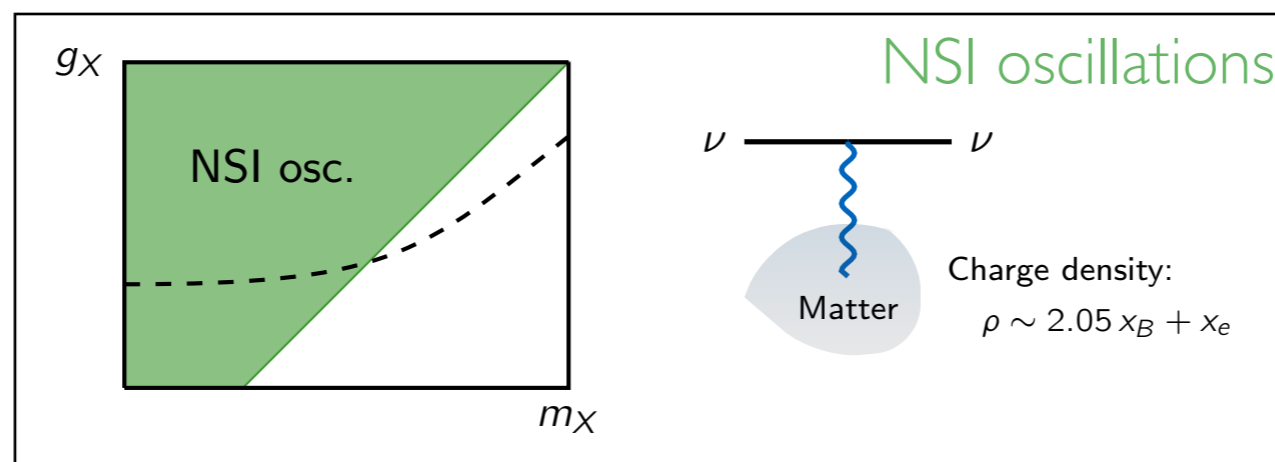
- A well-known example

$$L_\mu - L_\tau$$

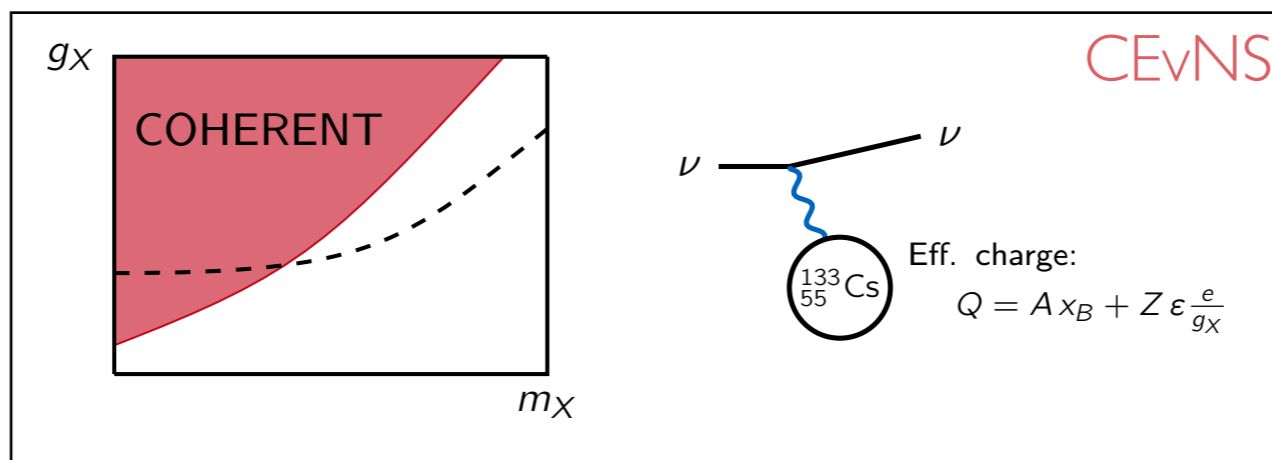
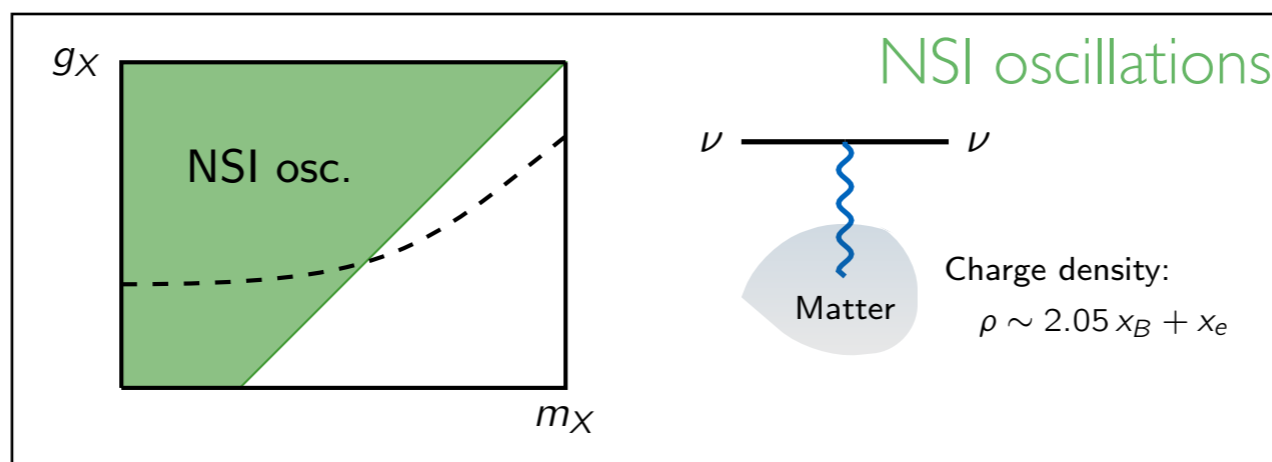
Baek *et al.* [hep-ph/0104141];  
Ma, Roy, Roy [hep-ph/0110146];  
many, many more...

- Other  $U(1)_X$ ?

# Other constraints



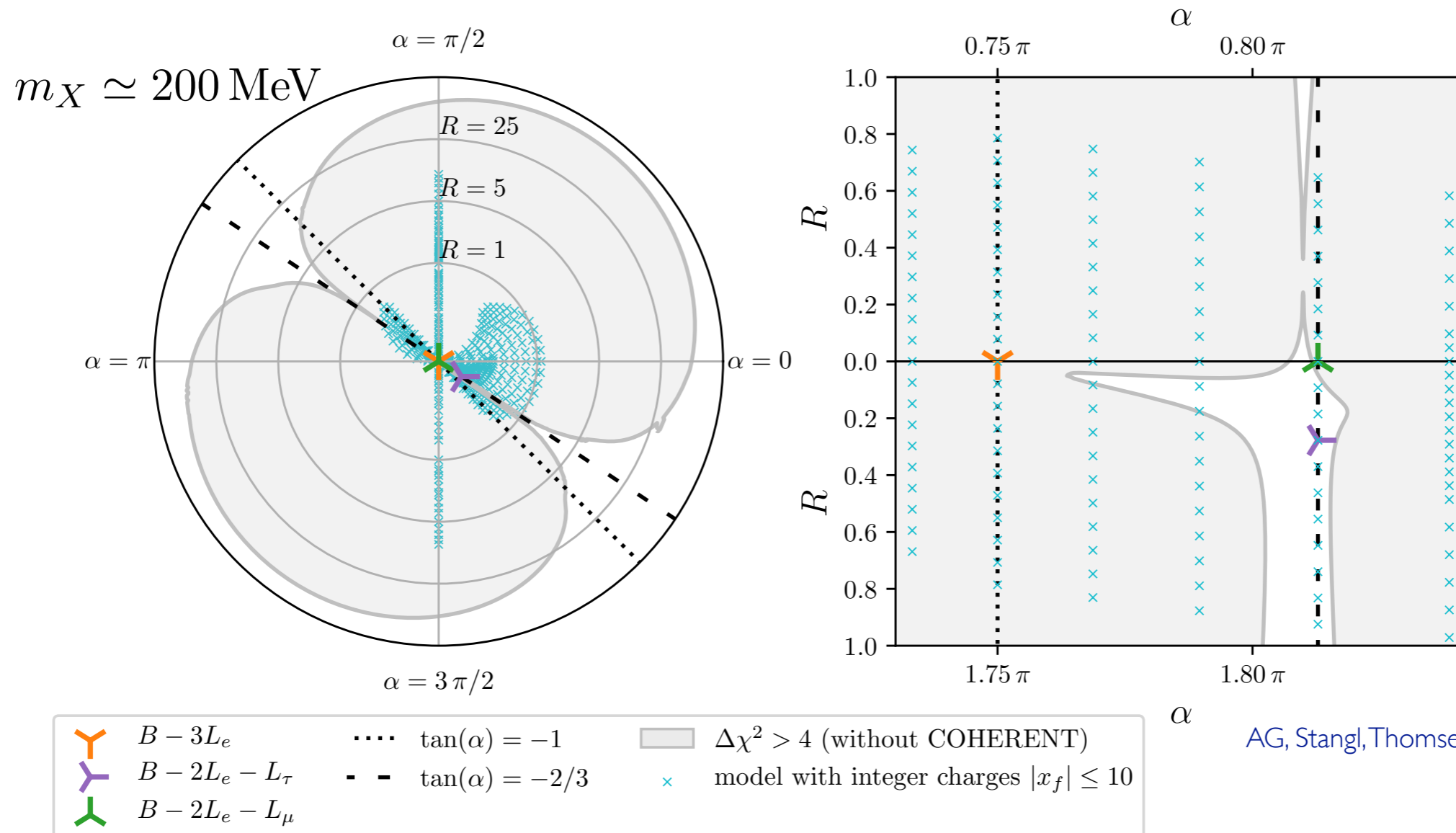
# Other constraints



# The impact of NSI

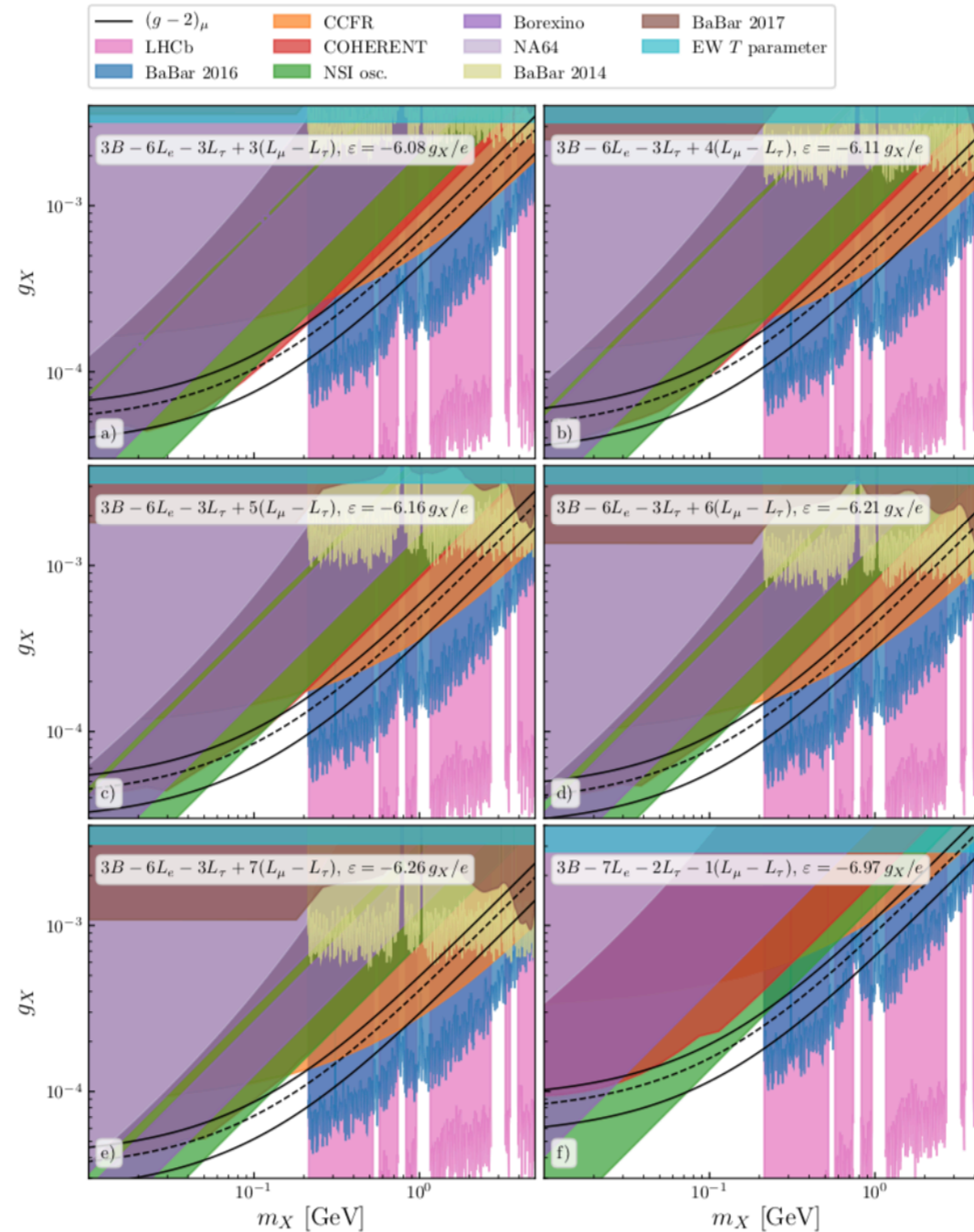
- Vector category

$$x_f \propto \sin(\alpha)(L_e - L_\mu) + \cos(\alpha)(B/3 - L_\mu) + R(L_\mu - L_\tau)$$



- Finally, including also COHERENT:  
Out of 419 models with  $|x_f| \leq 10$ , only 7 survive  $(g - 2)_\mu$  (in the narrow mass region).

# The impact of NSI



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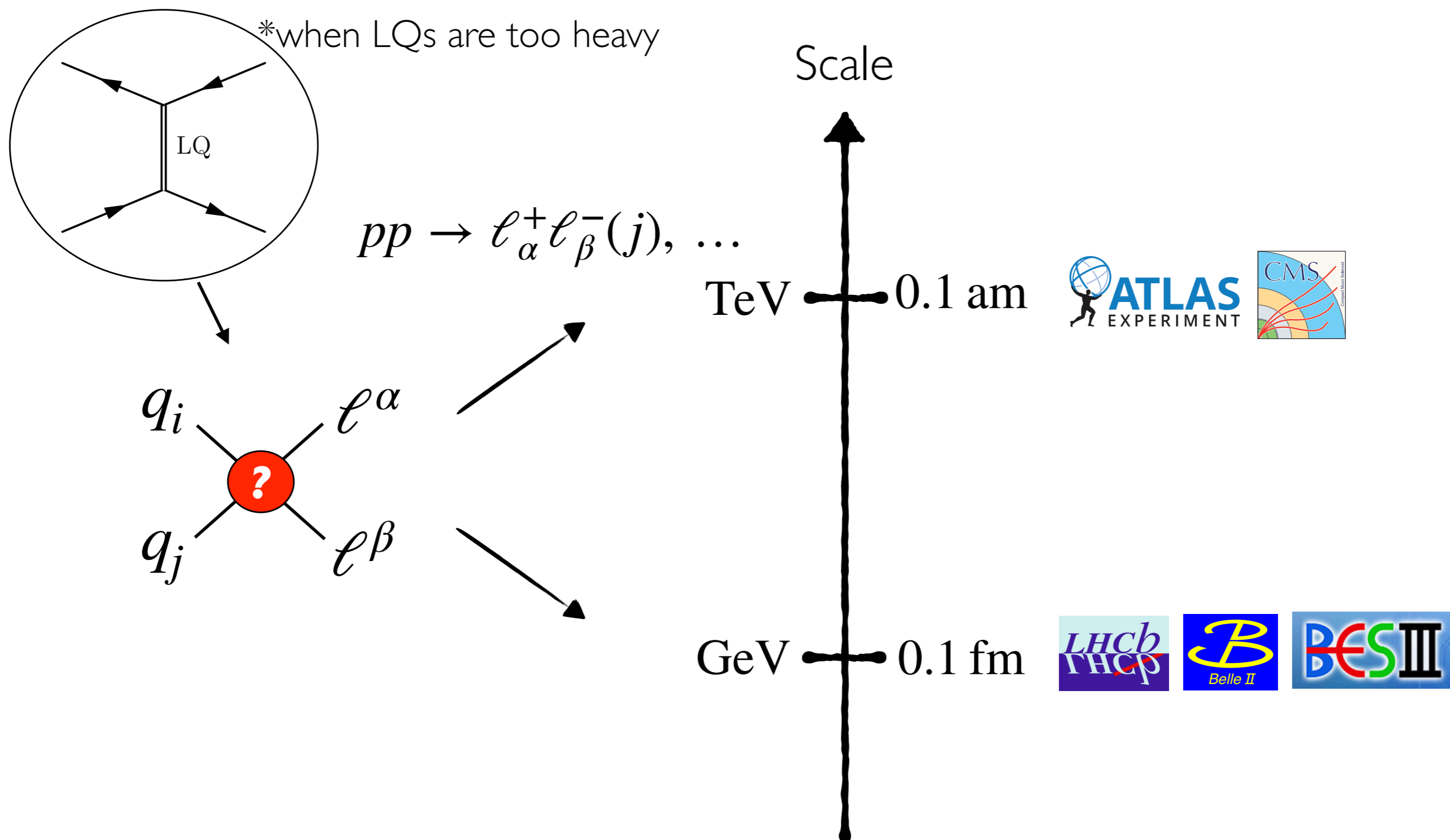
PART II

# Comments on $R_{K^{(*)}}$

The storyline

- Interpretation of  $b \rightarrow s\ell\ell$  anomalies after the recent LHCb update

# Drell-Yan versus B-decays



Example:  $b \rightarrow s\mu\mu$  vs Drell-Yan  
 AG, Marzocca; [1704.09015](#)

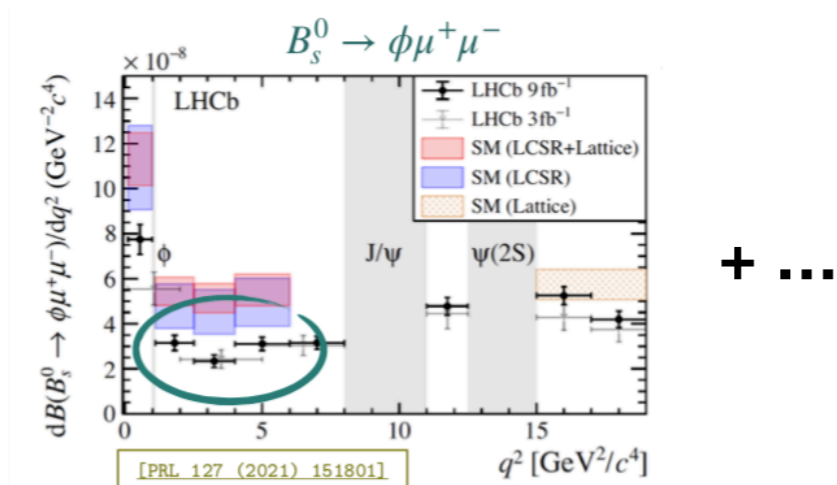
Systematic SMEFT study using **flavio**  
 AG, Salko, Smolkovic, Stangl; [2212.10497](#)

# The status of $b \rightarrow s\ell\ell$ anomalies

- Anomalies in  $b \rightarrow s\mu\mu$

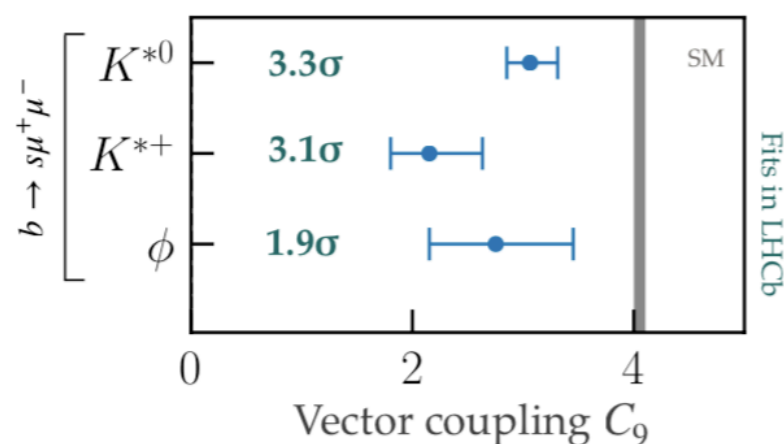
cf. Renato Quagliani, CERN seminar 20.12.2022.

$b \rightarrow s\mu^+\mu^-$  differential decay rates

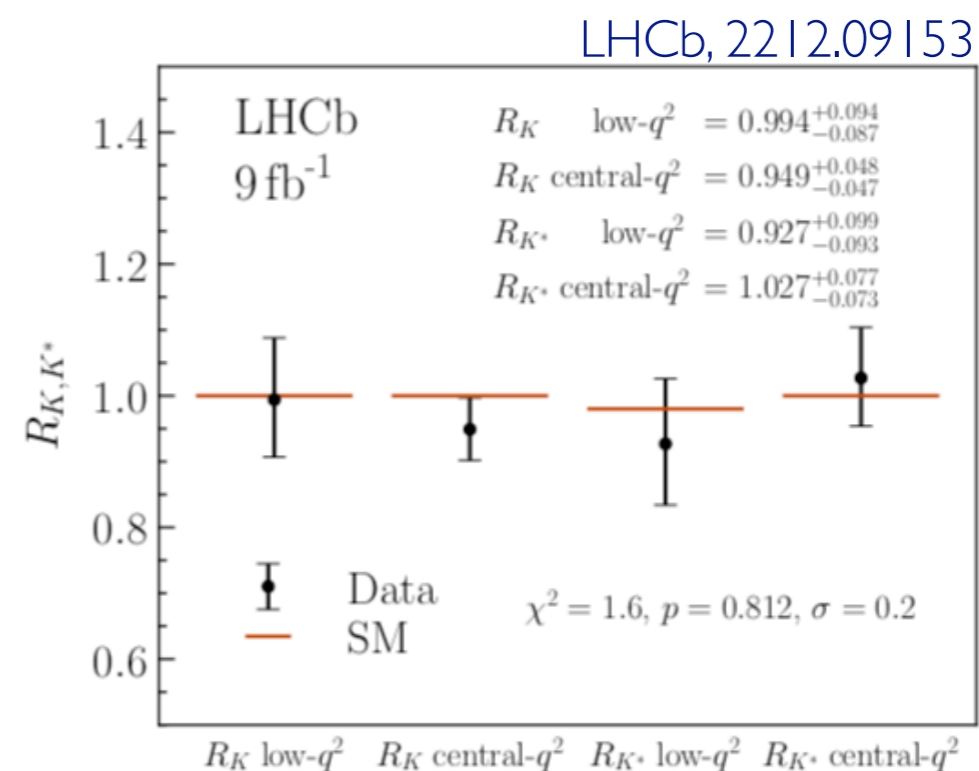


- But **L**epton **F**lavor **U**niversality ratios are SM-like

$b \rightarrow s\mu^+\mu^-$  angular analyses

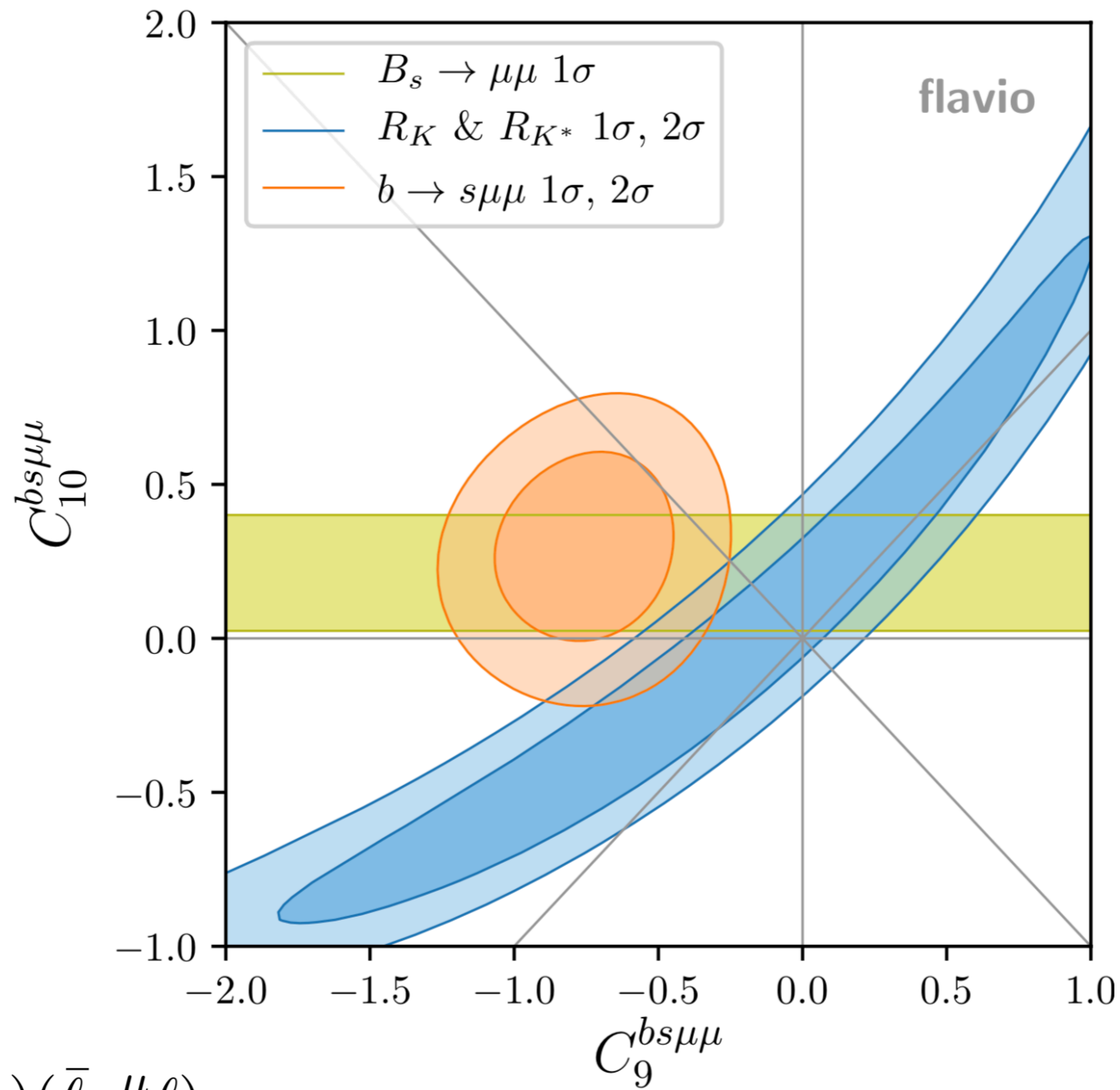


- Intriguing coherent and consistent pattern
  - However, *charm-loops* can mimic shift in  $C_9$





# The EFT fit

AG, Salko, Smolkovic, Stangl; [2212.10497](#)

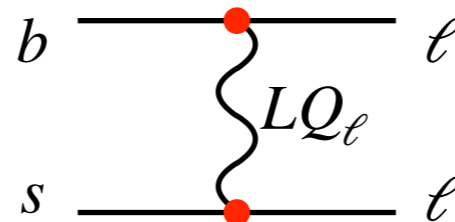
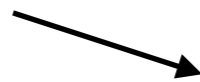
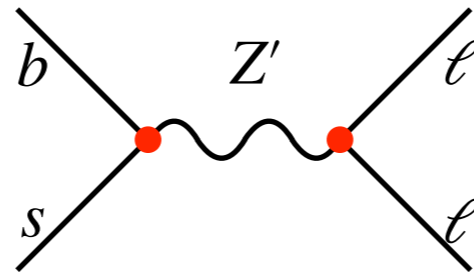
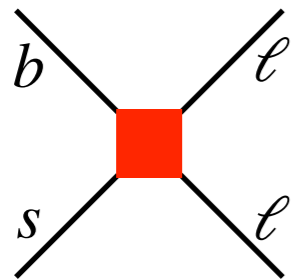
Tension!

$$O_9^{bqll} = (\bar{q}\gamma_\mu P_L b)(\bar{l}\gamma^\mu l),$$

$$O_{10}^{bqll} = (\bar{q}\gamma_\mu P_L b)(\bar{l}\gamma^\mu \gamma_5 l)$$

# LFU models for $b \rightarrow s\ell\ell$

## Tree-level models



- LFU  $Z'$

$$U(1)_{B-L}$$

$$U(1)_{3B_3-L}$$

...

- LFU  $LQ$  <sup>\*Single LQ  $\implies$  cLFV</sup>

$$(\bar{\mathbf{3}}, \mathbf{3}, 1/3) \times \mathbf{2} = LQ_e + LQ_\mu$$

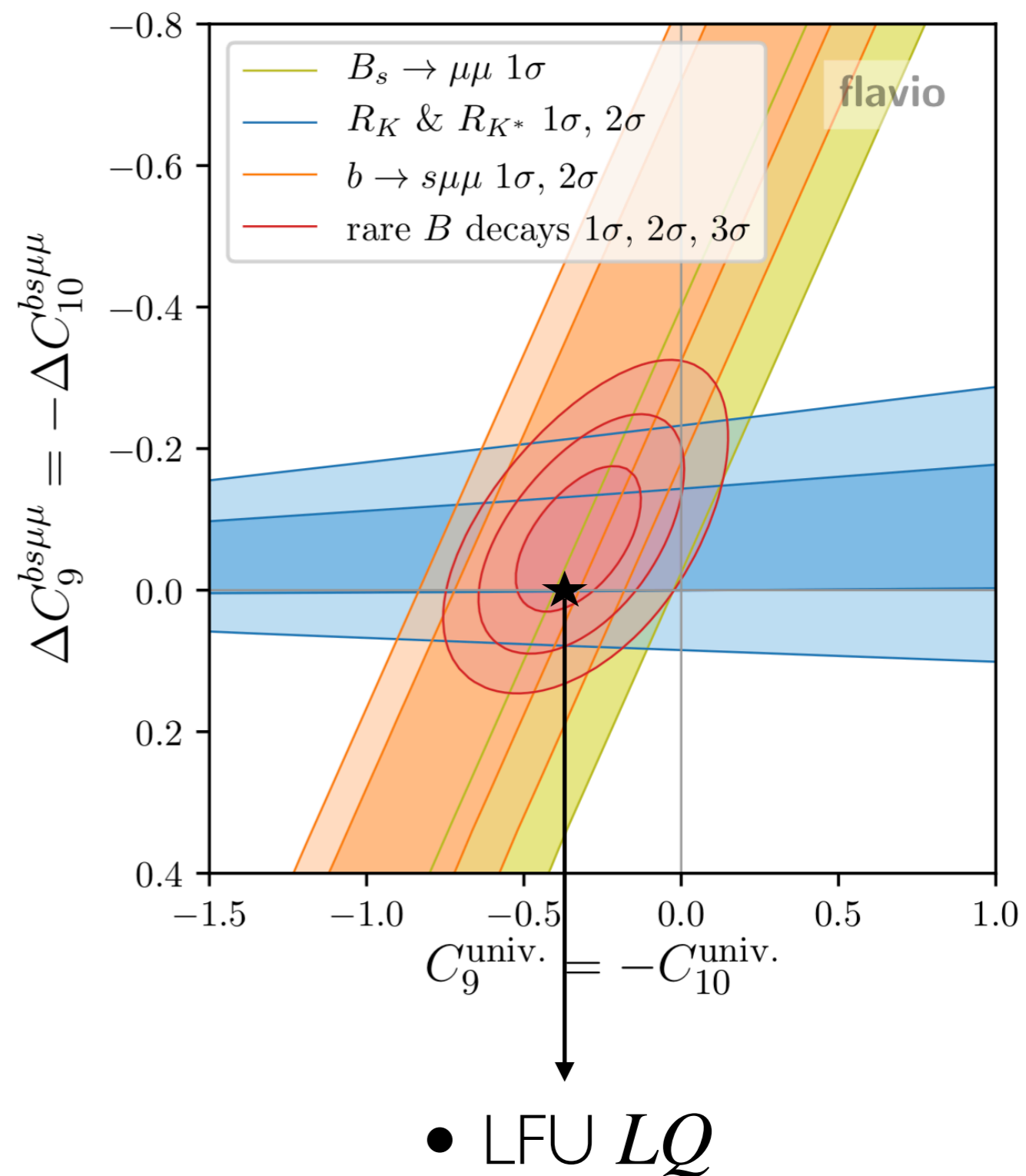
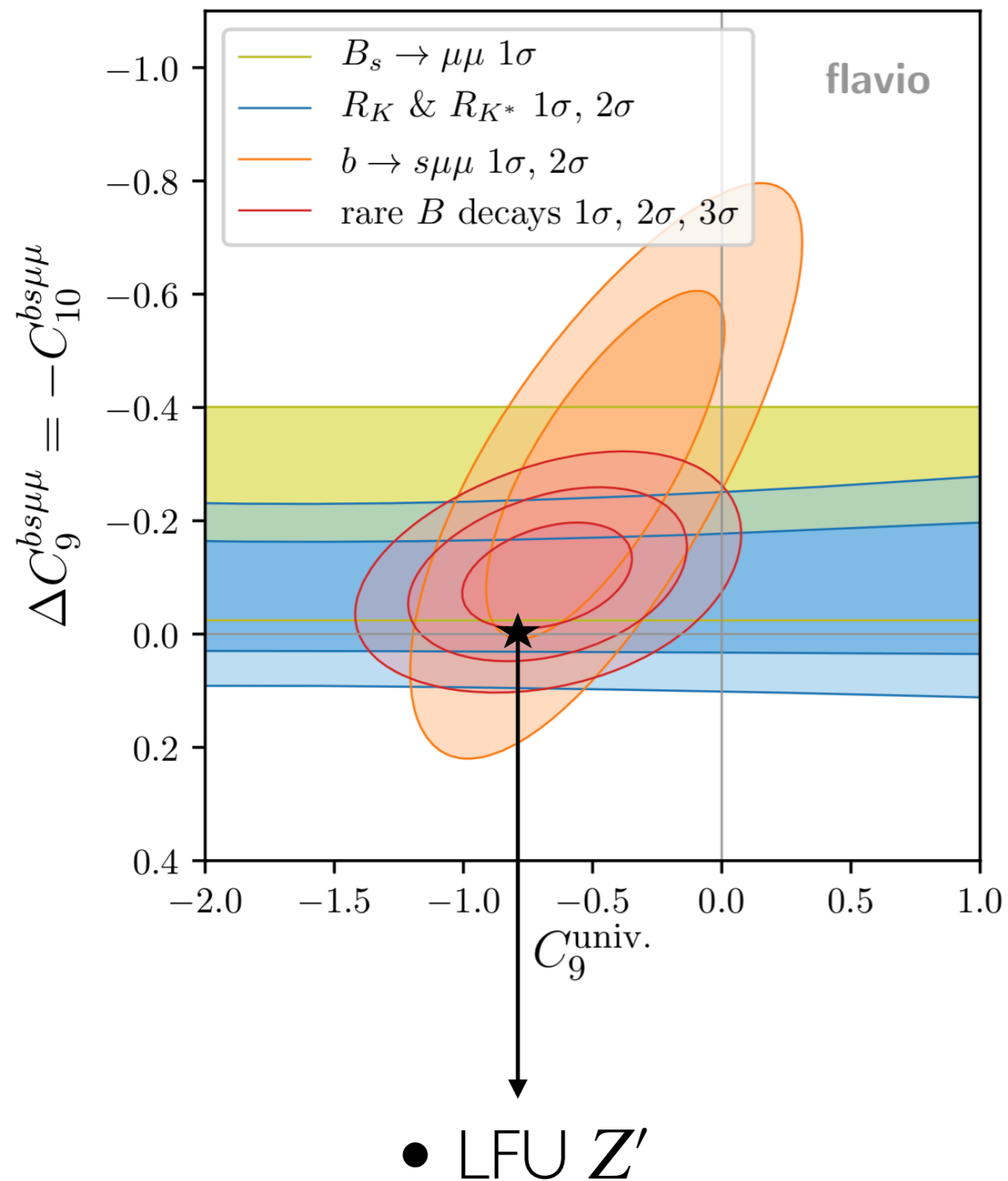
$$U(1)_e \times U(1)_\mu \times Z_2^{\text{LFU}}$$

$$\begin{array}{ccc} LQ_e & \longleftrightarrow & LQ_\mu \\ e & \longleftrightarrow & \mu \end{array}$$

Mass/Coupling degeneracy  
Gauged flavour (Part I) ?

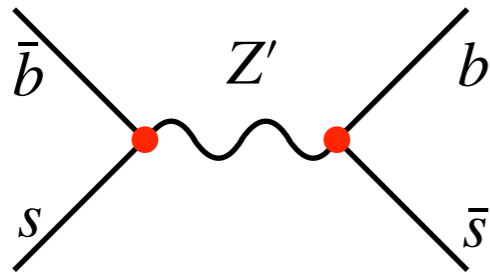
# The EFT fit

AG. Salko, Smolkovic, Stangl: 2212.10497



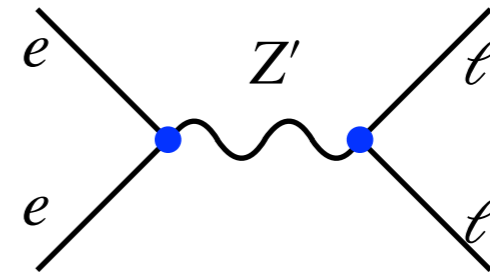
# LFU models: $Z'$

- The bounds from



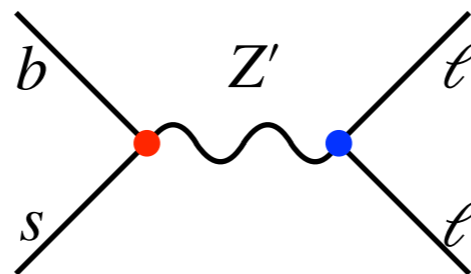
**Meson mixing**

+

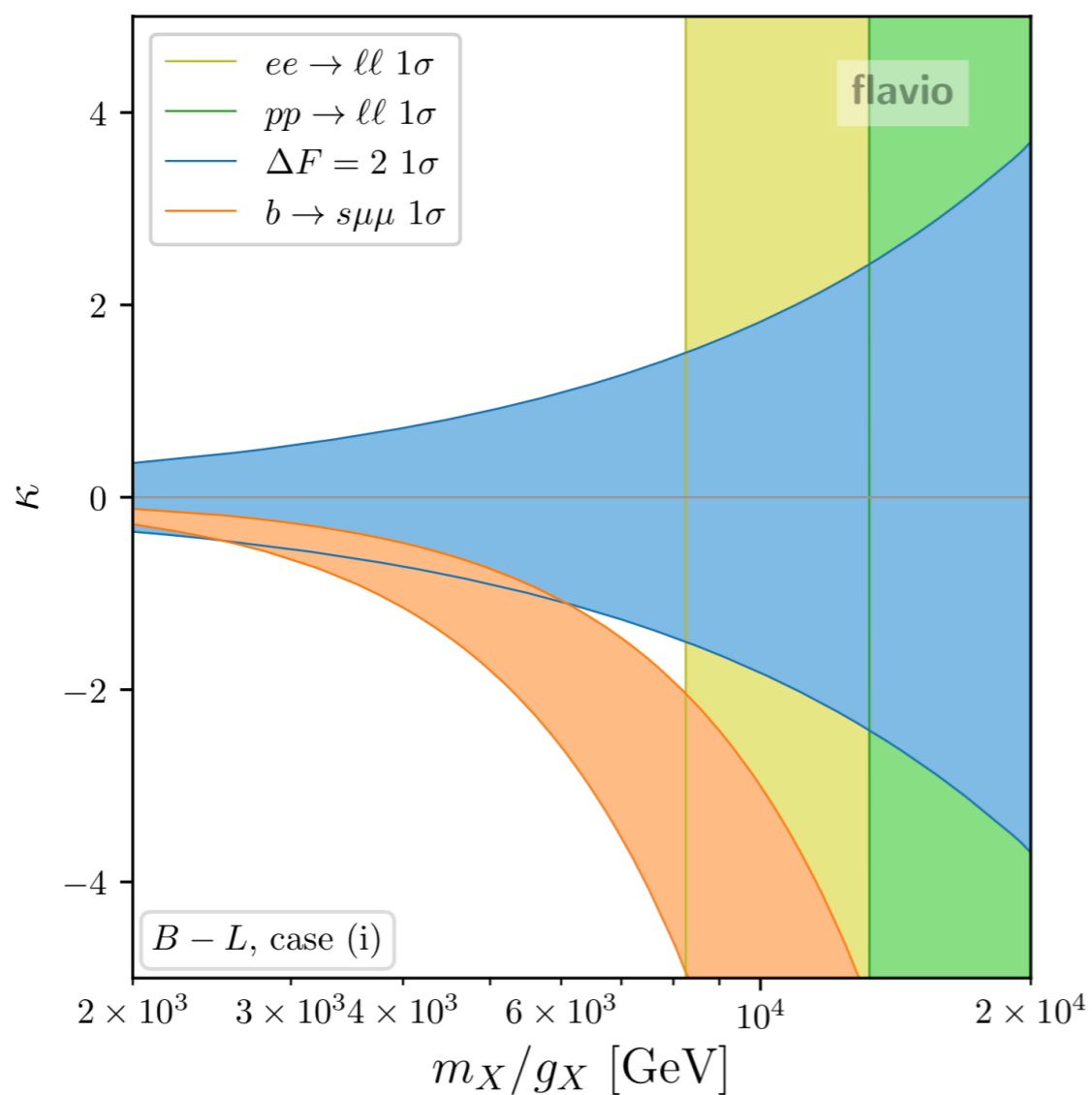


**LEP II**

are constraining

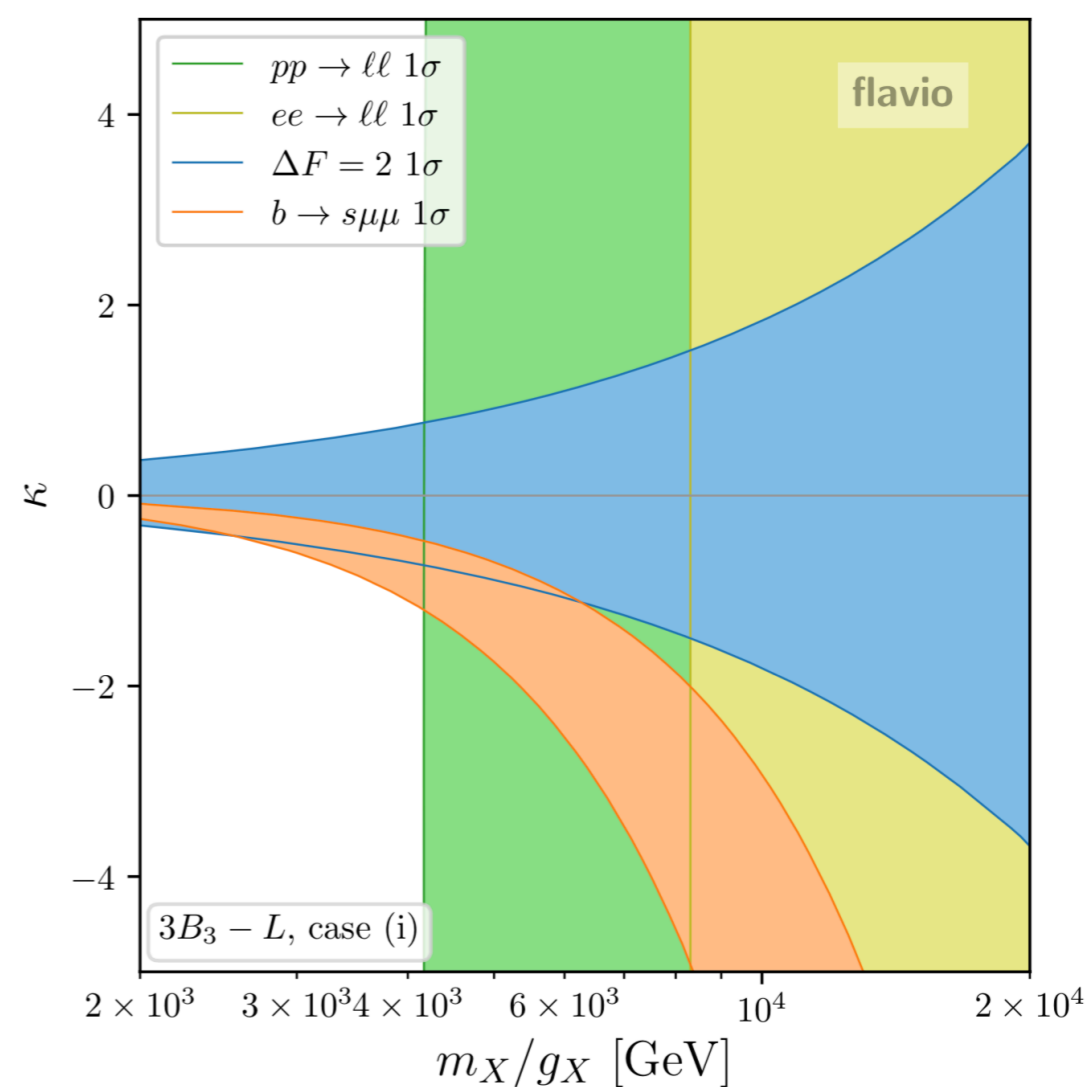


!

**LFU** models:  $Z'$  $B - L$ 

$$J_X^\mu = J_{B-L}^\mu + \frac{1}{3}\epsilon_{ij}\bar{q}_i\gamma^\mu q_j$$

$$\epsilon_{ij} = -\kappa |V_{ts}|(\delta_{i2}\delta_{j3} + \delta_{i3}\delta_{j2})$$

 $3B_3 - L$ 

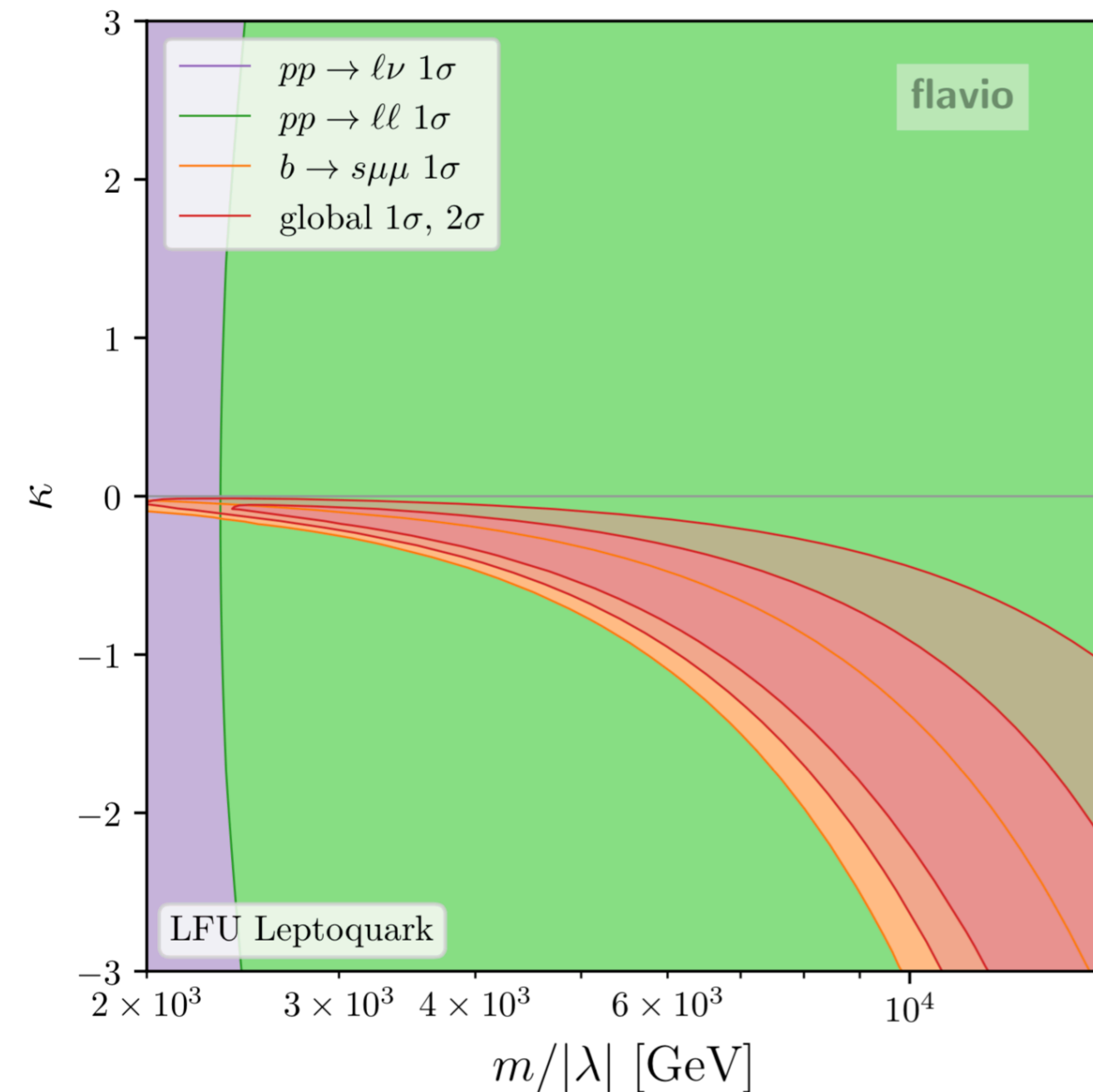
$$J_X^\mu = J_{3B_3-L}^\mu + \frac{1}{3}\epsilon_{ij}\bar{q}_i\gamma^\mu q_j$$

Tension!

# LFU leptoquark

$$\mathcal{L} \supset (D_\mu S^\alpha)^\dagger (D^\mu S^\alpha) - m^2 S^{\alpha\dagger} S^\alpha - (\lambda_i \bar{q}_i^c l_\alpha S^\alpha + \text{h.c.})$$

$$\lambda_i = \lambda (\kappa V_{td}, \kappa V_{ts}, 1)$$



- Tree-level  $2q2\ell$ ,
- Loop-suppressed  $4q$  and  $4\ell$



PART III

# Future Colliders

The storyline

- New physics in  $b \rightarrow s\mu\mu$ : FCC-hh versus a Muon Collider

# Motivation

- Short-distance  $bs\mu\mu$  contact interaction at the level of  $\mathcal{O}(10^{-5})G_F$ 
  - $\implies$  the violation of perturbative unitarity  $\lesssim 100 \text{ TeV}$
  - $\implies$  **Future Colliders**

## Competitors

Collider	C.o.m. Energy	Luminosity	Label
LHC Run-2	13 TeV	140 fb <sup>-1</sup>	LHC
HL-LHC	14 TeV	6 ab <sup>-1</sup>	HL-LHC
FCC-hh	100 TeV	30 ab <sup>-1</sup>	FCC-hh
Muon Collider	3 TeV	1 ab <sup>-1</sup>	MuC3
Muon Collider	10 TeV	10 ab <sup>-1</sup>	MuC10
Muon Collider	14 TeV	20 ab <sup>-1</sup>	MuC14



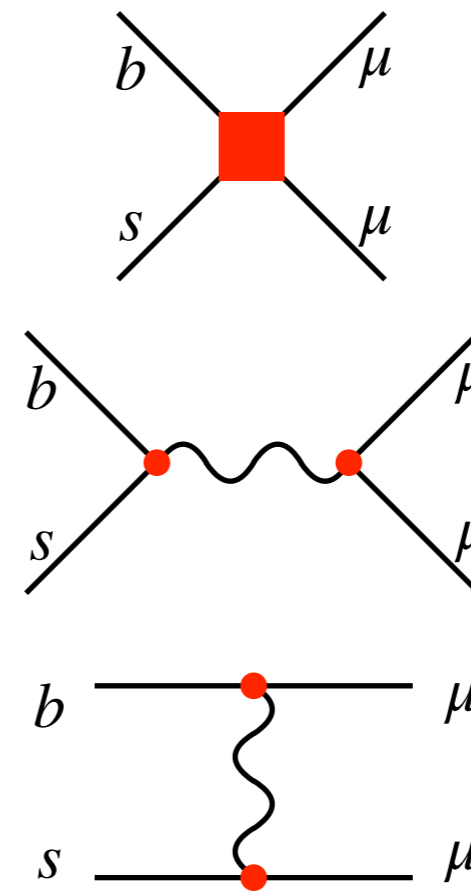
# The scope

■ New Physics benchmarks:

1. Semileptonic 4F interactions

2.  $Z'$

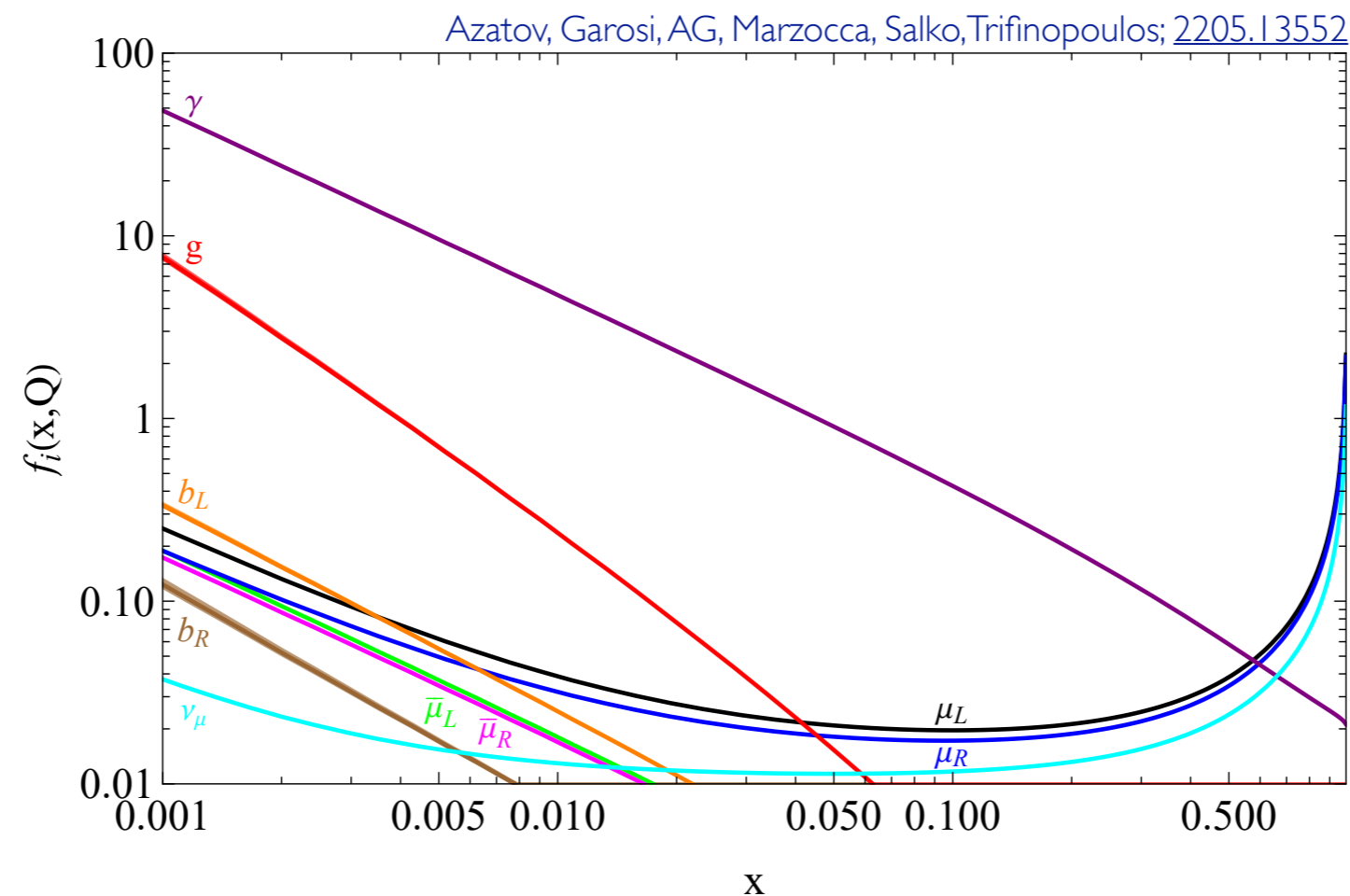
3. LQ



[See backup slides]

# The Muon Beam

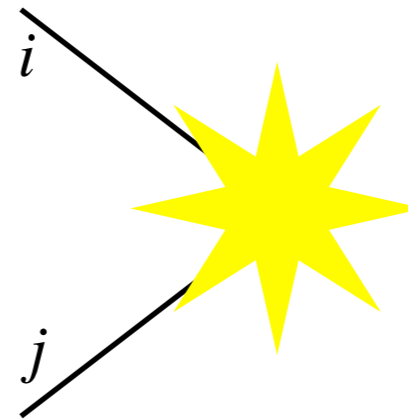
- Collinear radiation: Spreads the muon energy to lower values and generates different initial states  $\implies$  Parton Distribution Functions
- We cross-check and numerically solve the DGLAP equations from (Han et al, 2007.14300, 2103.09844) with appropriate initial conditions at the LL accuracy
- Selected PDFs at  $Q = 3 \text{ TeV}$ :



# The Muon Beam

- Parton luminosities

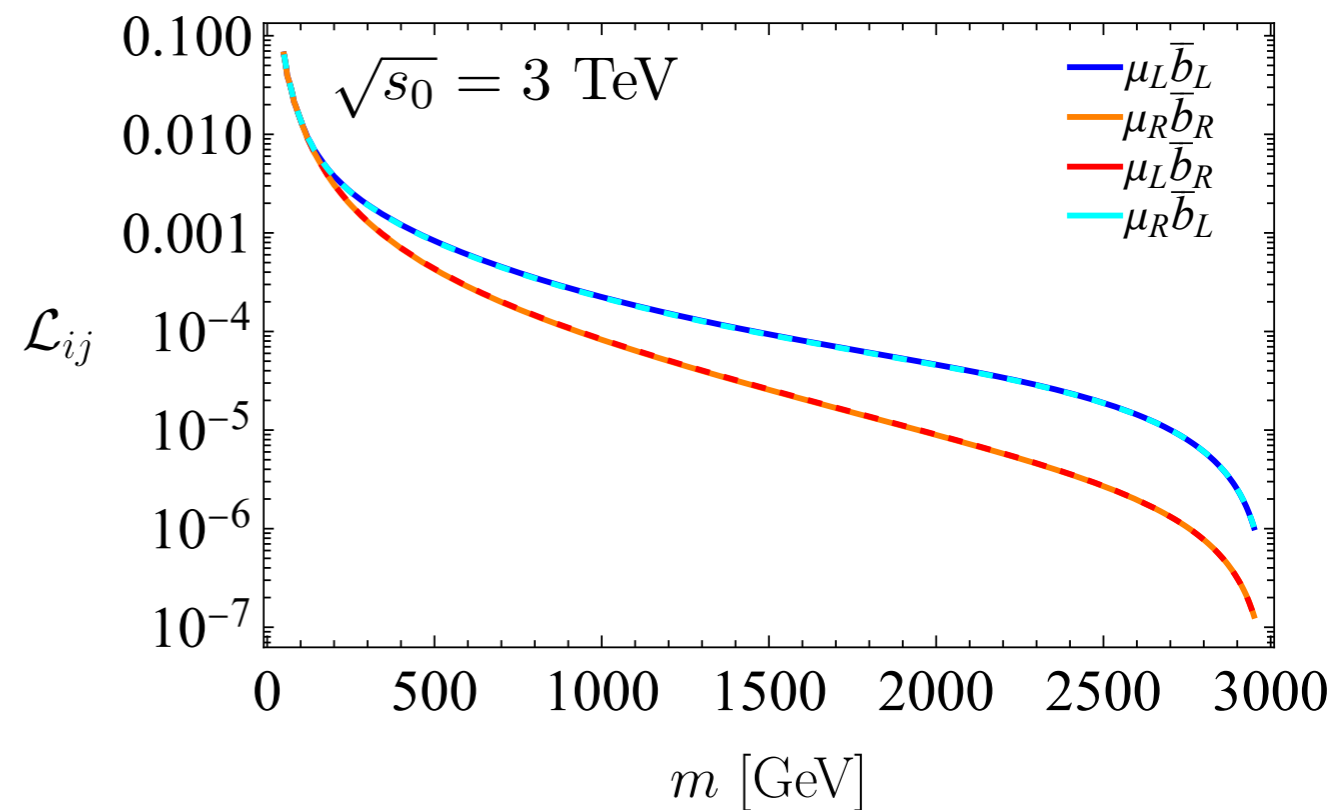
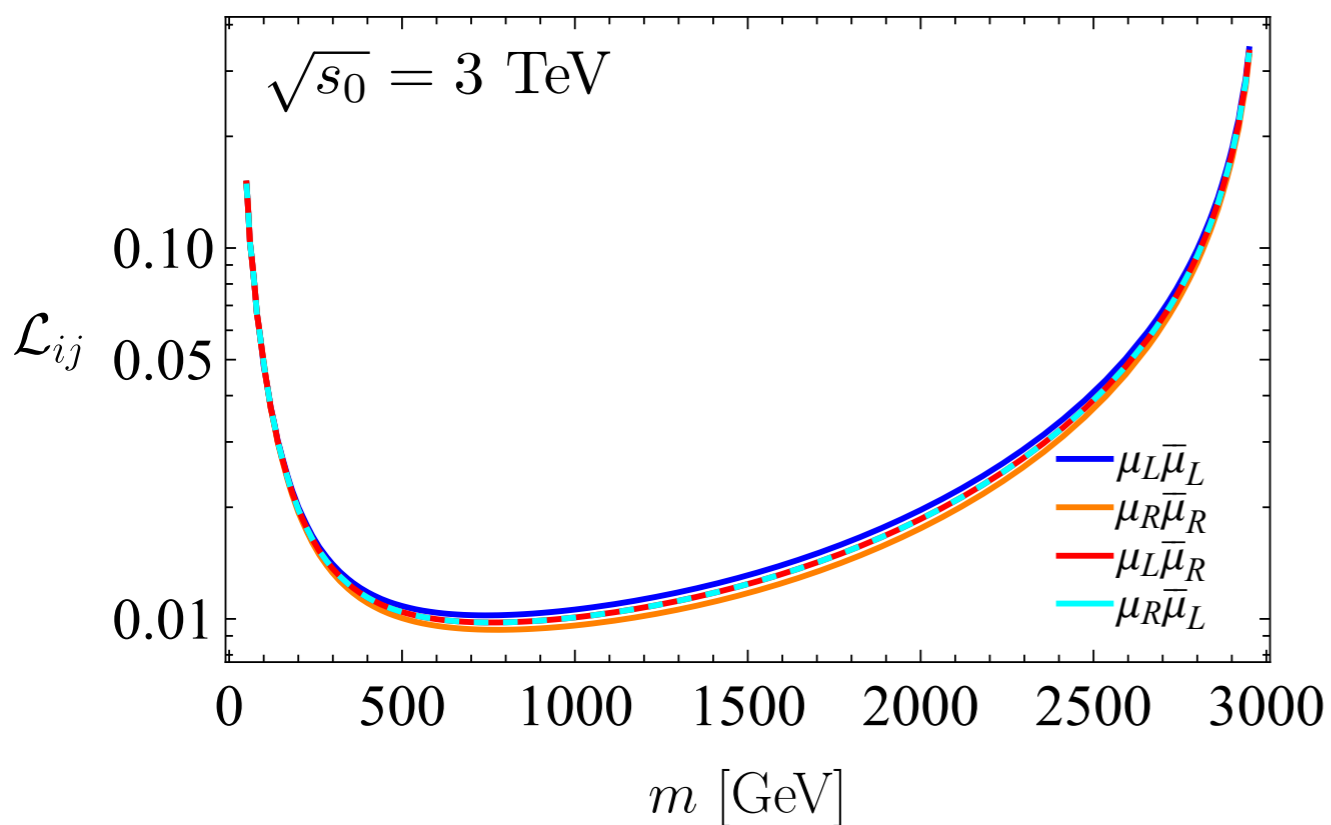
$$\mathcal{L}_{ij}(\tau) = \int_{\tau}^1 \frac{dx}{x} f_i(x, m) f_j\left(\frac{\tau}{x}, m\right)$$



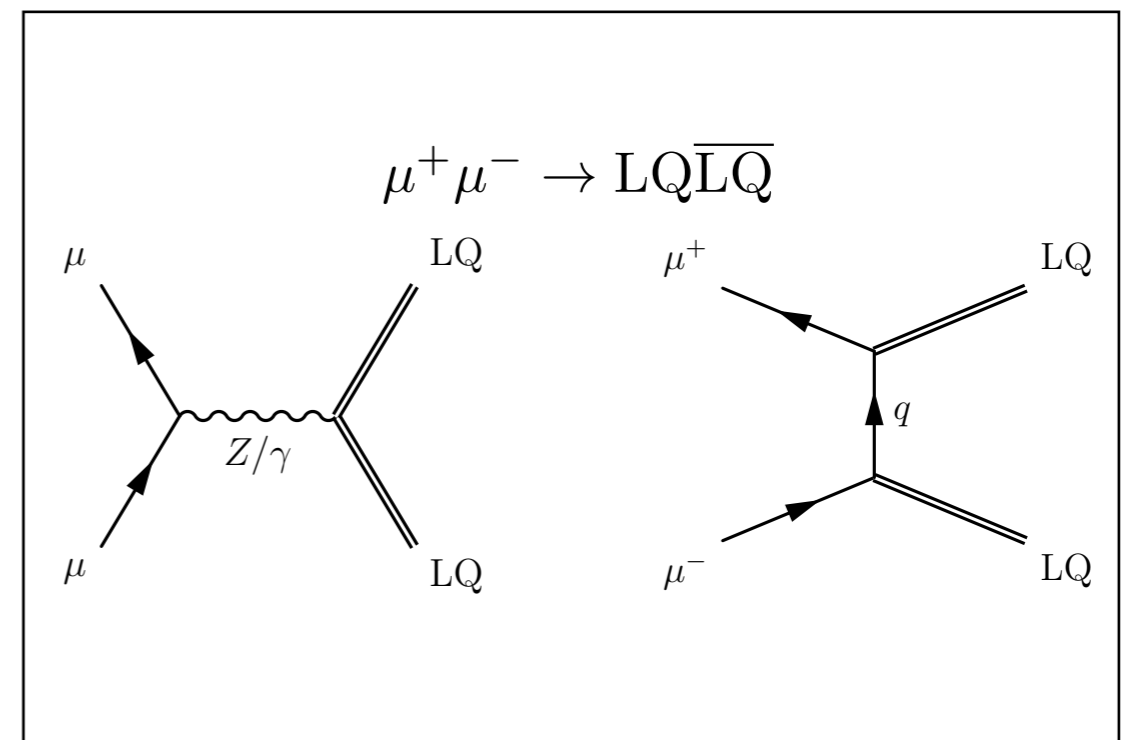
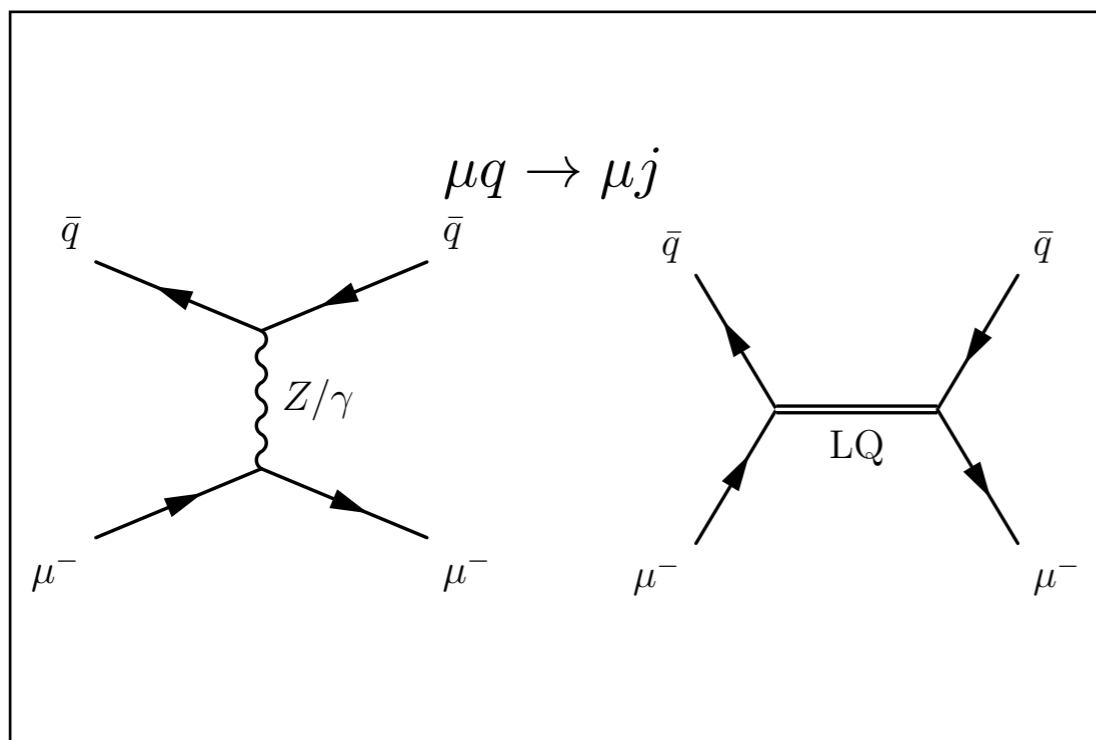
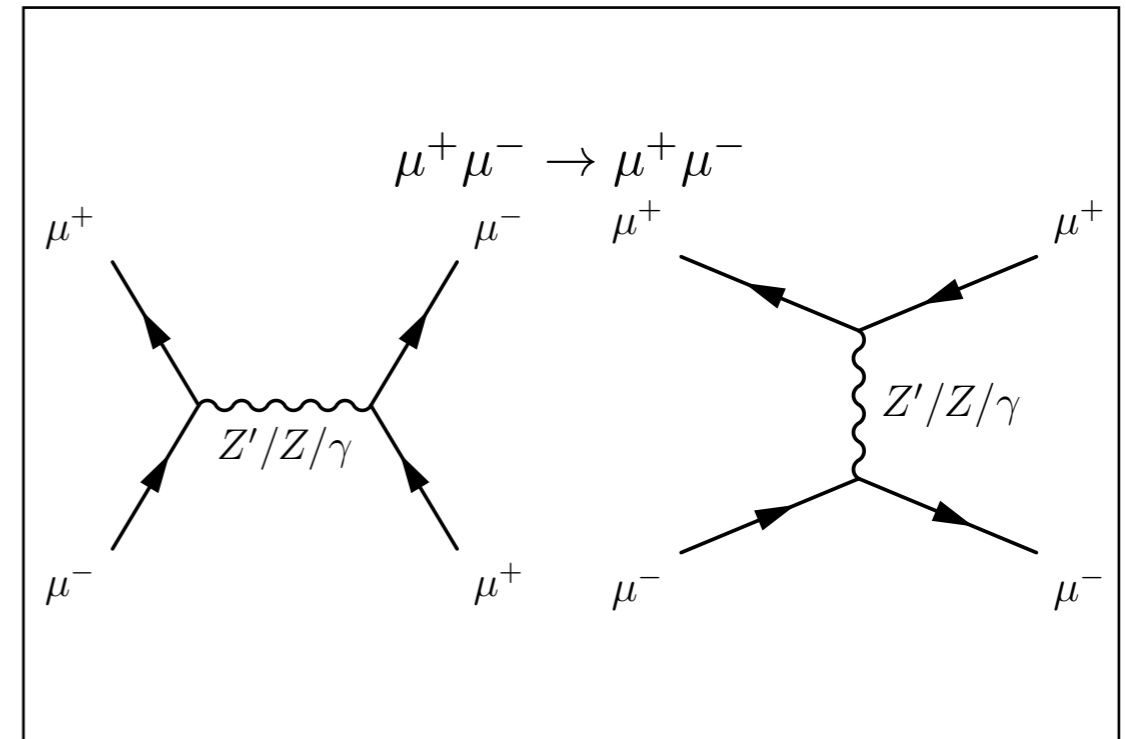
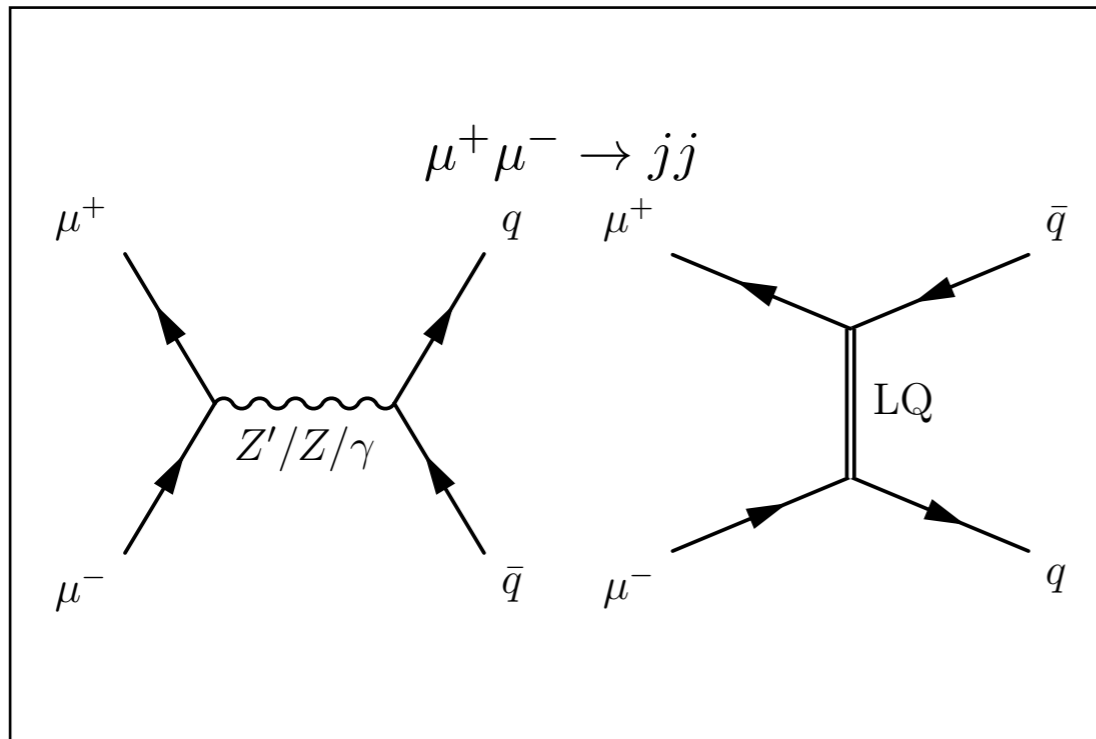
$$m^2 = (p_i + p_j)^2$$

$$\tau = m^2/s_0$$

Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; [2205.13552](#)



# The signatures at MuC



# The signatures at MuC

$$m_X < \sqrt{s_0}$$

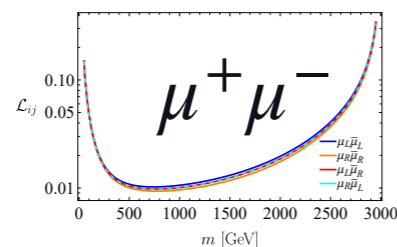
$$m_X > \sqrt{s_0}$$

- Kinematical features at  $m_{\mu\mu} \sim m_X$   
e.g. a resonance peak
- Corrections to the bins  $m_{\mu\mu} \approx \sqrt{s_0}$   
“fifth force searches”

- Corrections to the bins  $m_{\mu\mu} \approx \sqrt{s_0}$   
“EFT searches”

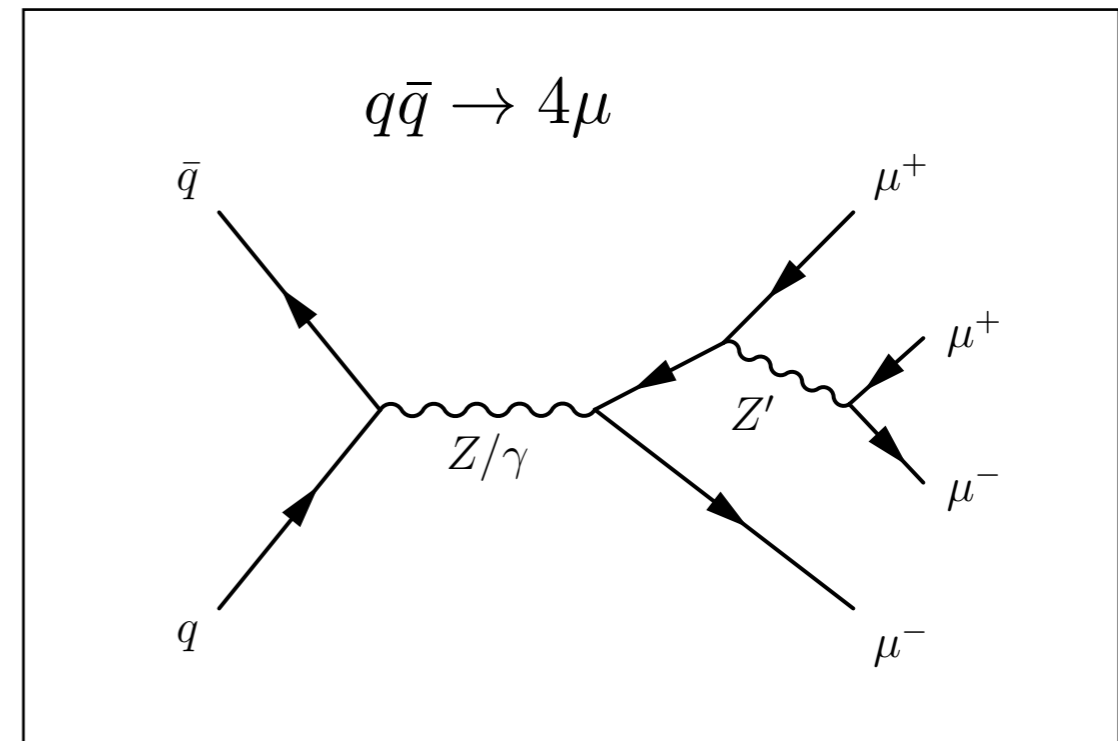
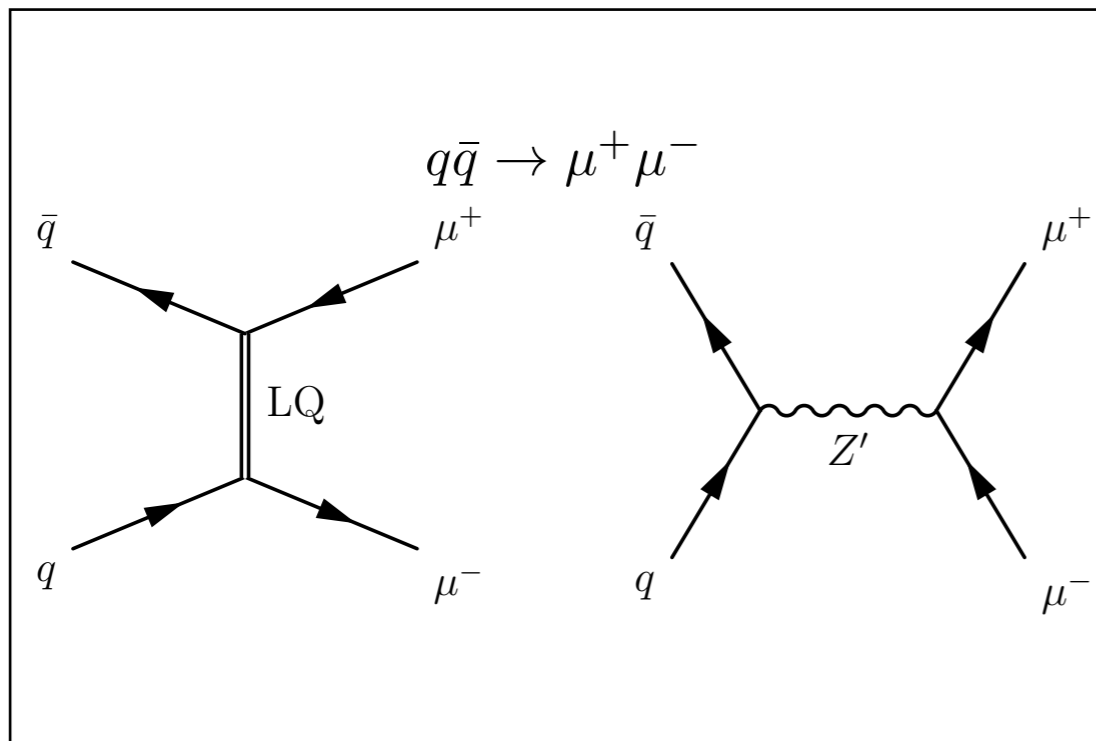


- Only effective  
at MuC due to



- Monotonously decreasing  
luminosities in proton colliders

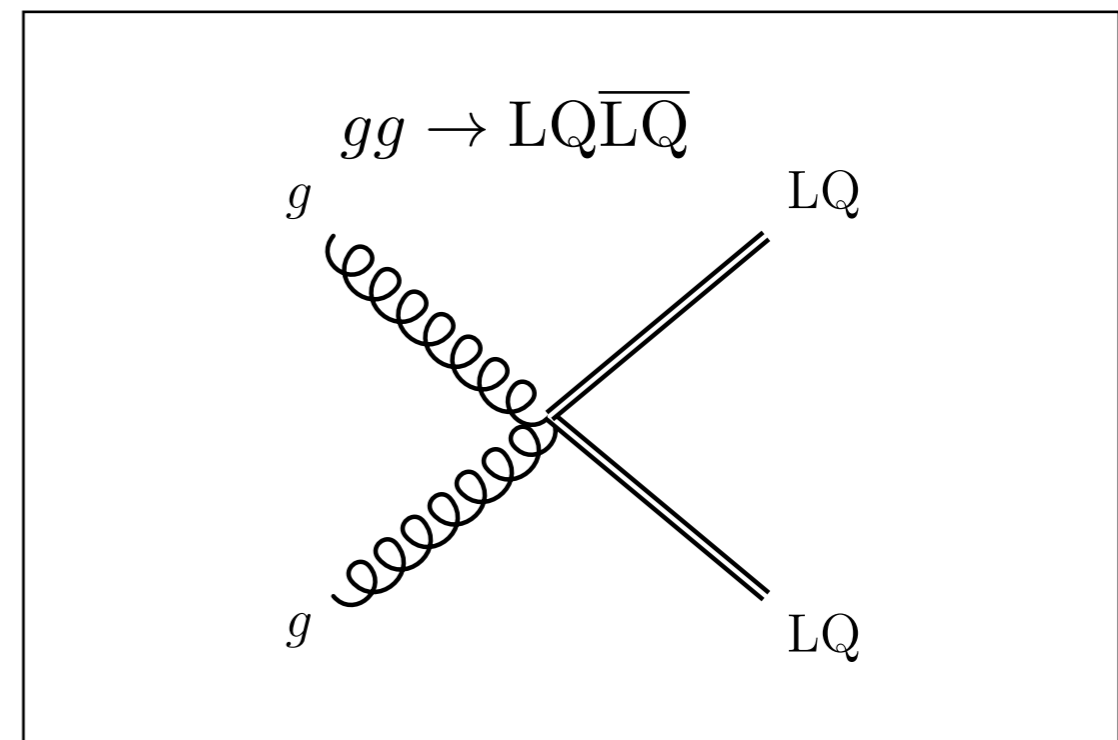
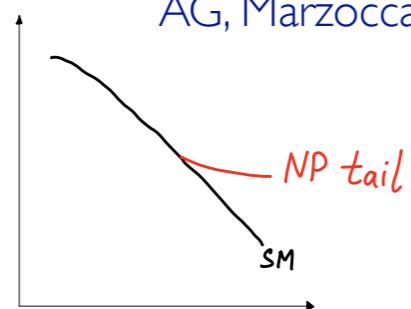
# The signatures at hadron colliders



- Corrections to the high-mass Drell-Yan
- LHC data already useful to constrain models for  $b \rightarrow s\mu\mu$

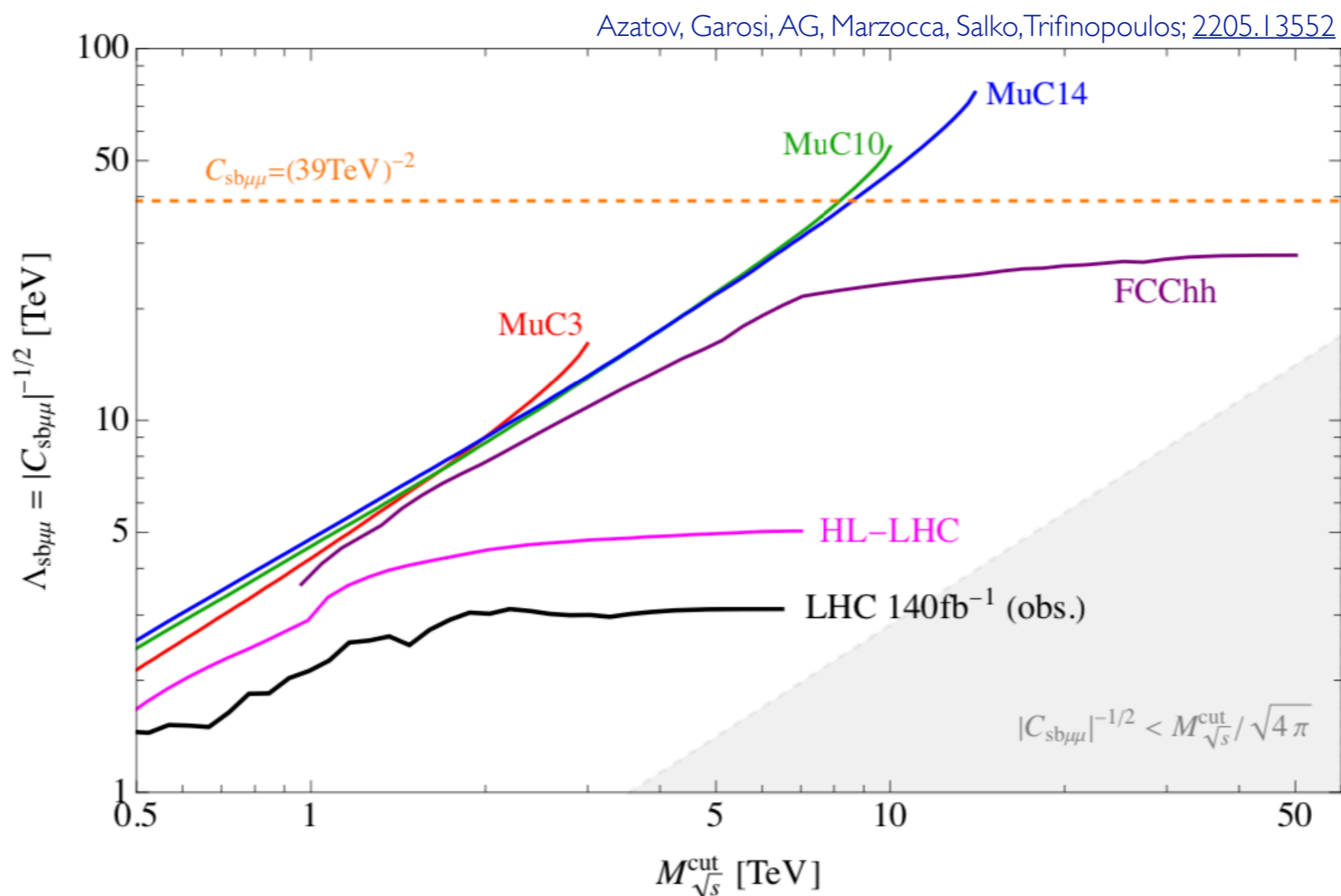
AG, Marzocca; 1704.09015

EFT limit



# Contact interactions

The pessimistic case

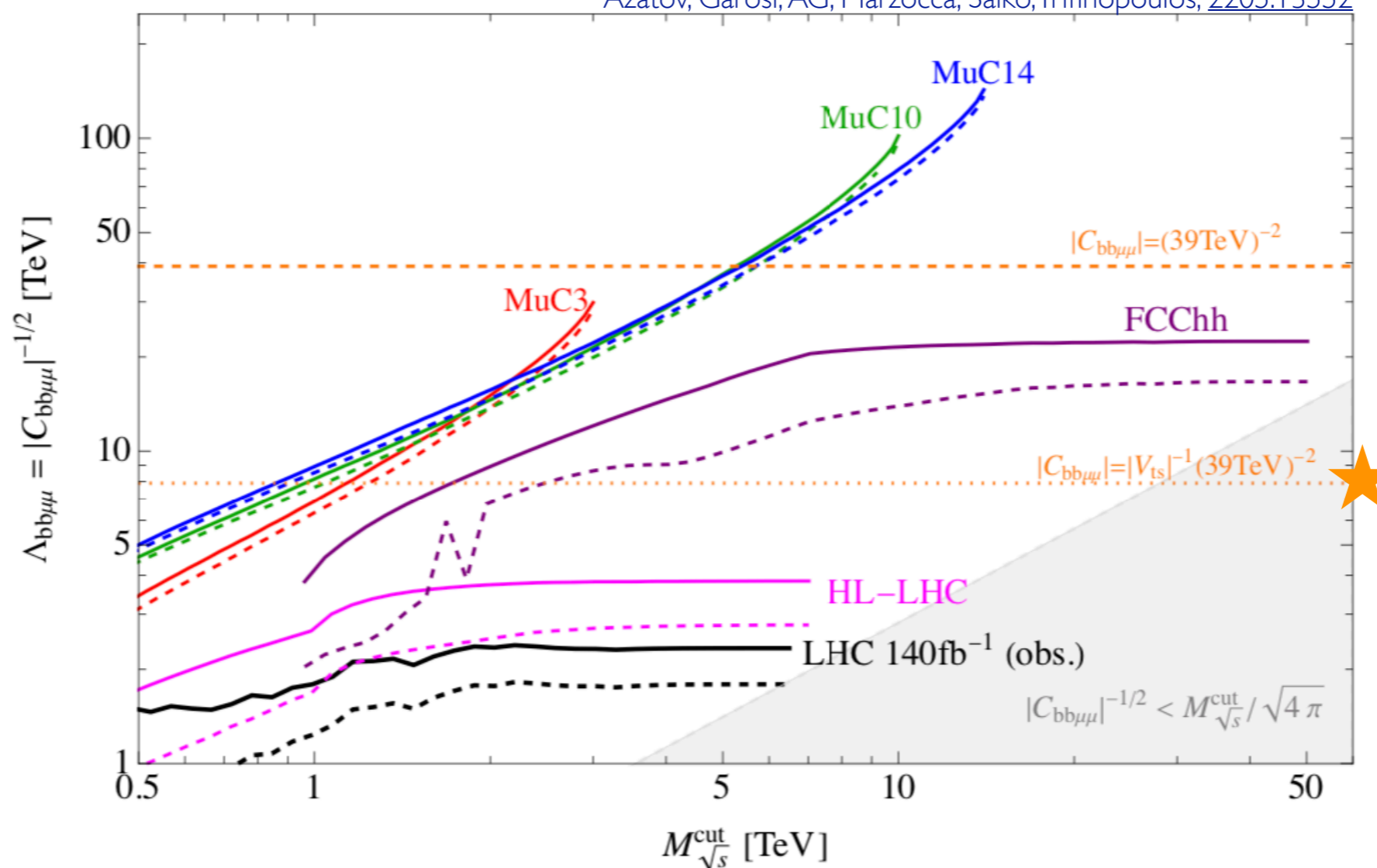


**Figure 7.** Sensitivity reach (95%CL) for the  $(\bar{s}_L \gamma_\alpha b_L)(\bar{\mu}_L \gamma^\alpha \mu_L)$  contact interaction as function of the upper cut on the final-state invariant mass, compared to the value required to fit  $bs\mu\mu$  anomalies (dashed orange line).

# Contact interactions

The realistic case ★

Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; [2205.13552](#)

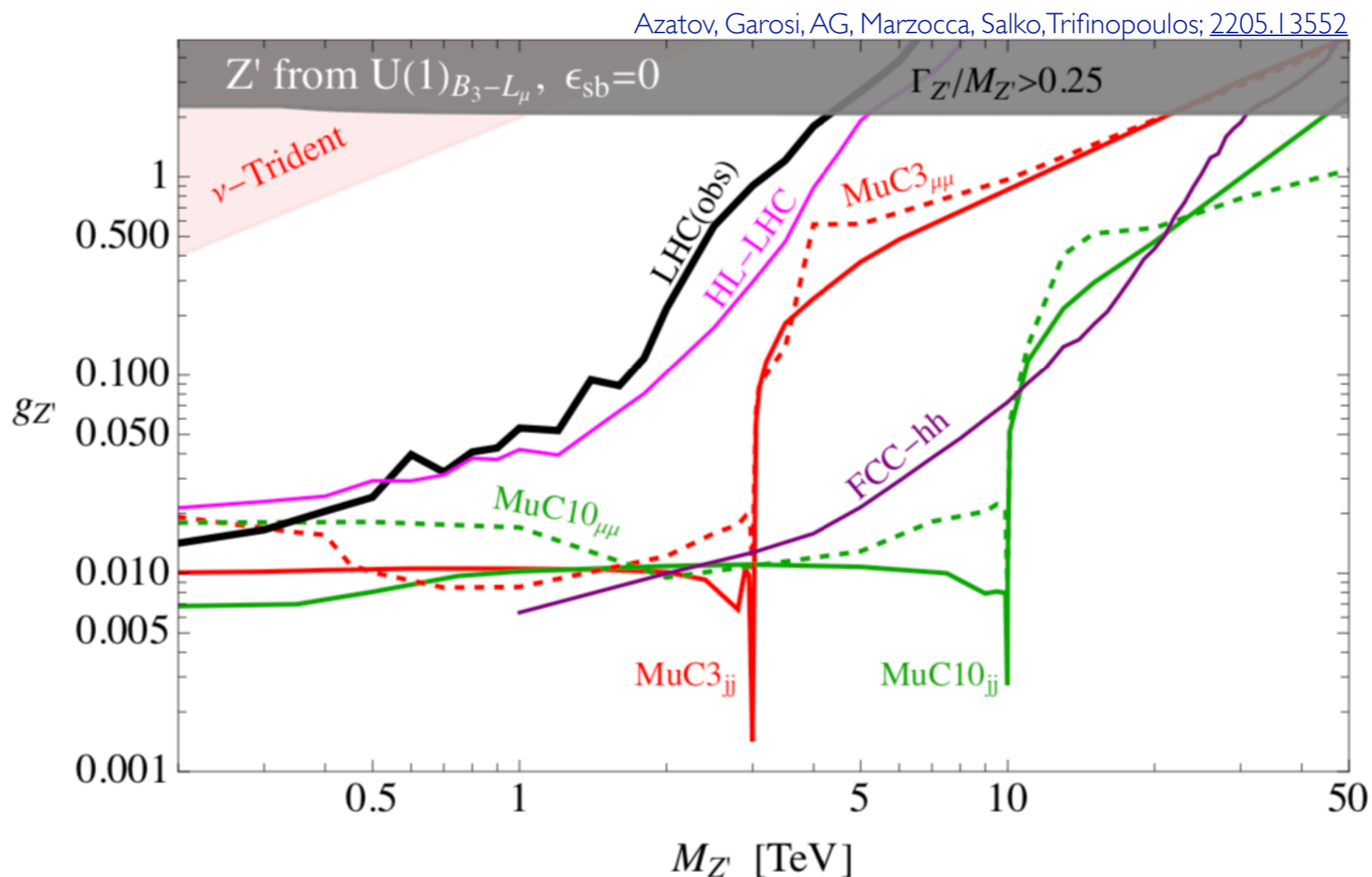


**Figure 8.** Sensitivity reach (95%CL) for the  $(\bar{b}_L \gamma_\alpha b_L)(\bar{\mu}_L \gamma^\alpha \mu_L)$  contact interaction as function of the upper cut on the final-state invariant mass. Solid (dashed) lines represent the limit for positive (negative) values of  $C_{bb\mu\mu}$ . The orange dotted and dashed lines shows reference values in relation to the  $bs\mu\mu$  anomalies fit, with or without a  $1/V_{ts}$  enhancement of the  $bb$  operator compared to the  $bs$  one, respectively.



# $Z'$ models: $B_3 - L_\mu$

$$\mathcal{L}_{Z'_{B_3-L_\mu}}^{\text{int}} = -g_{Z'} Z'_\alpha \left[ \frac{1}{3} \bar{Q}_L^3 \gamma^\alpha Q_L^3 + \frac{1}{3} \bar{b}_R \gamma^\alpha b_R + \frac{1}{3} \bar{t}_R \gamma^\alpha t_R - \bar{L}_L^2 \gamma^\alpha L_L^2 - \bar{\mu}_R \gamma^\alpha \mu_R + \left( \frac{1}{3} \epsilon_{sb} \bar{Q}_L^2 \gamma^\alpha Q_L^3 + \text{h.c.} \right) + \mathcal{O}(\epsilon_{sb}^2) \right]$$

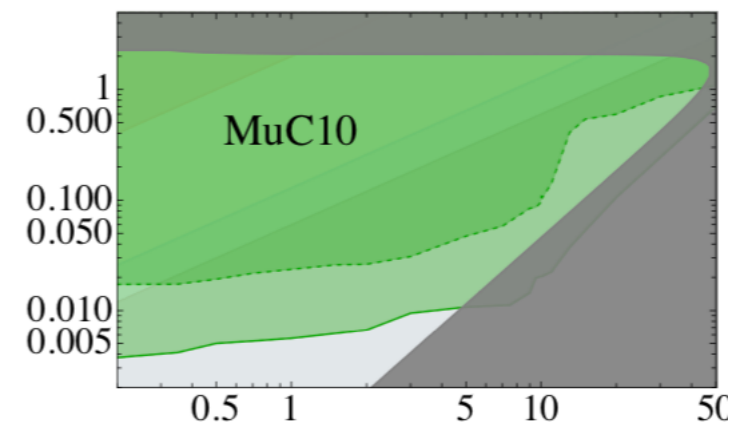
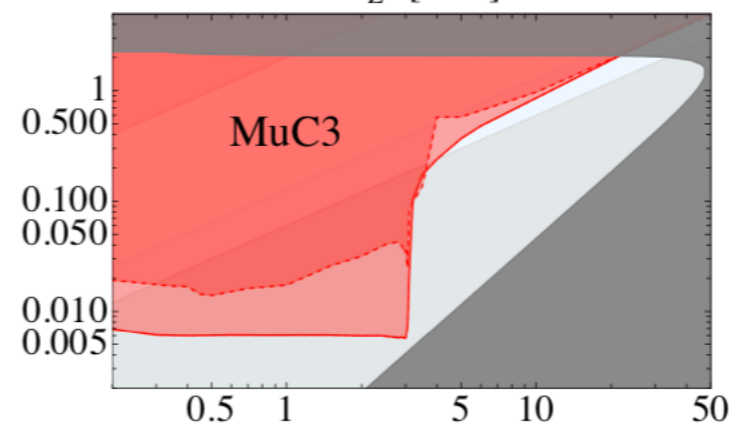
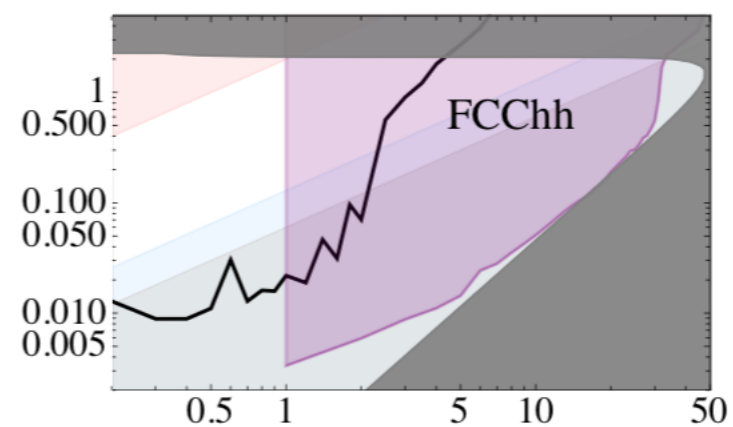
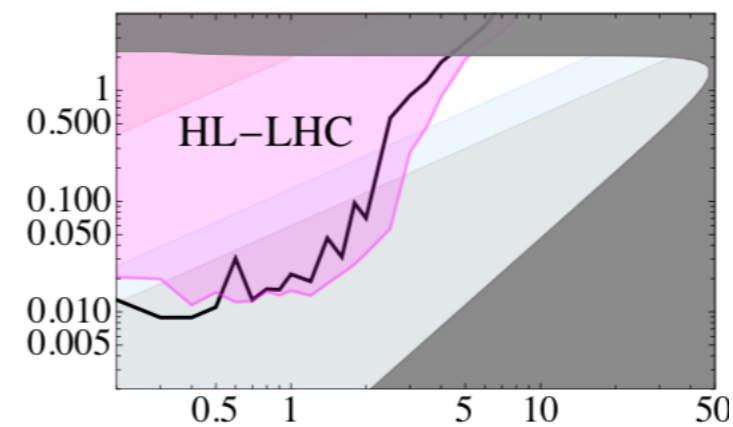
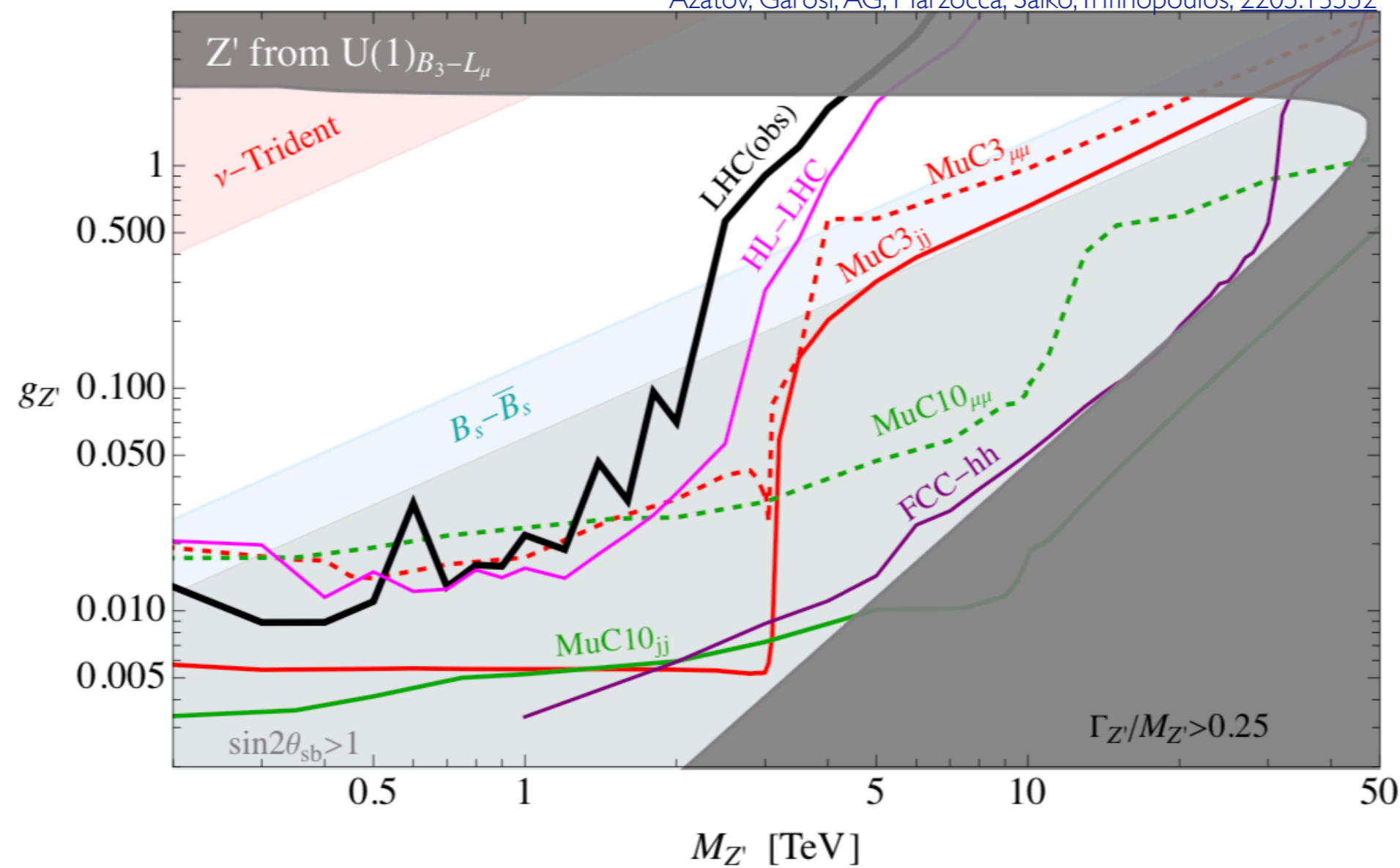


**Figure 9.** Discovery reach at  $5\sigma$  for the  $B_3 - L_\mu$  model with  $\epsilon_{sb} = 0$ , for different final states at each collider (as indicated by the labels). The region excluded at 95% CL by LHC [111] is above the black line while in the dark gray region the  $Z'$  has a large width, signaling a loss of perturbativity.

# $Z'$ models: $B_3 - L_\mu$

$$bs\mu\mu : \epsilon_{sb} = -1.7 \times 10^{-3} \left( \frac{M_{Z'}}{g_{Z'} \text{TeV}} \right)^2$$

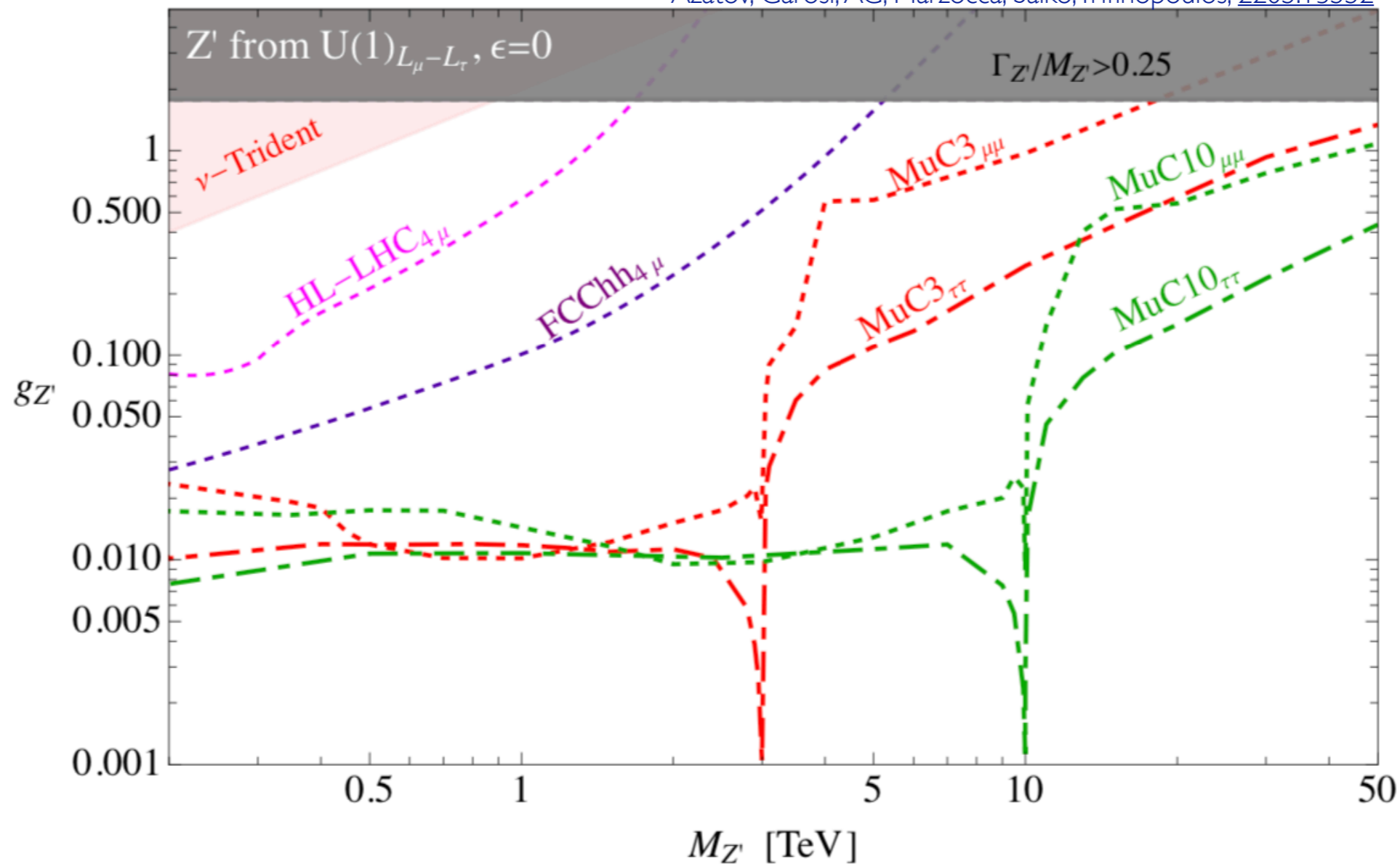
Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; 2205.13552



# $Z'$ models: $L_\mu - L_\tau$

$$\mathcal{L}_{Z' L_\mu - L_\tau}^{\text{int}} = -g_{Z'} Z'_\alpha \left[ \bar{L}_L^2 \gamma^\alpha L_L^2 + \bar{\mu}_R \gamma^\alpha \mu_R - \bar{L}_L^3 \gamma^\alpha L_L^3 - \bar{\tau}_R \gamma^\alpha \tau_R + \right. \\ \left. + |\epsilon_b|^2 \bar{Q}_L^3 \gamma^\alpha Q_L^3 + |\epsilon_s|^2 \bar{Q}_L^2 \gamma^\alpha Q_L^2 + (\epsilon_b \epsilon_s^* \bar{Q}_L^2 \gamma^\alpha Q_L^3 + \text{h.c.}) + \dots \right]$$

Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; [2205.13552](#)



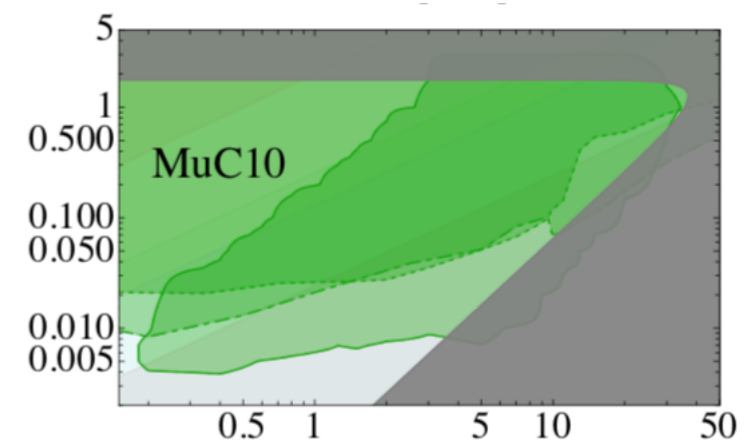
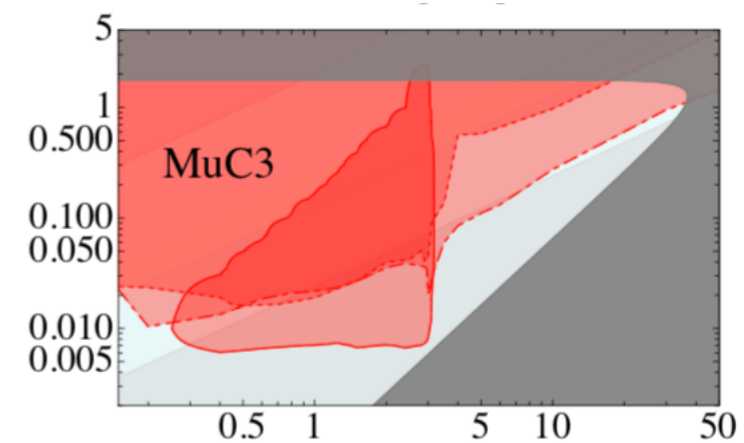
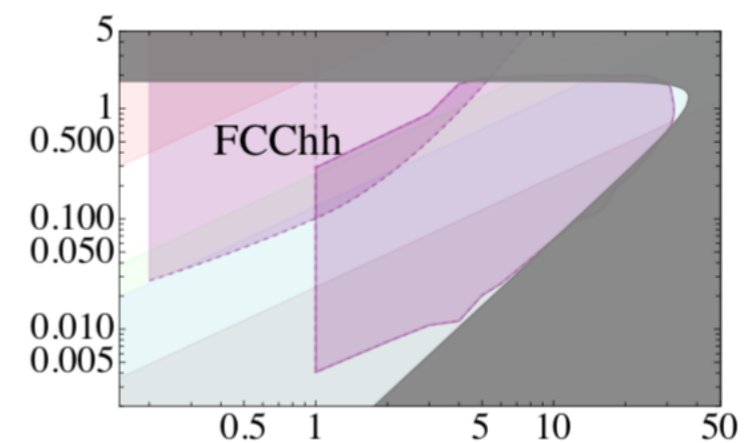
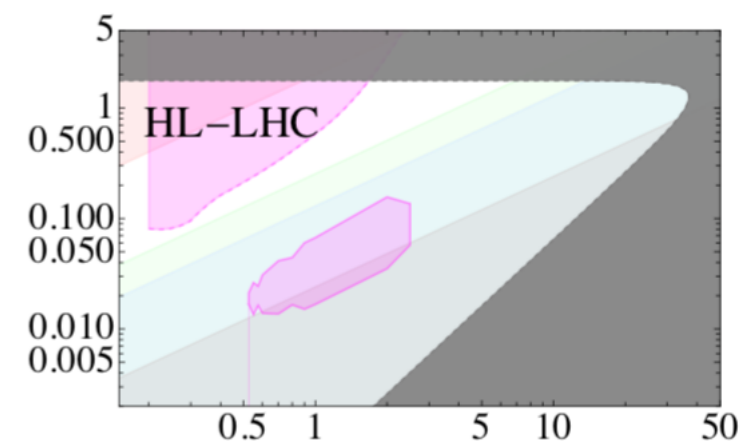
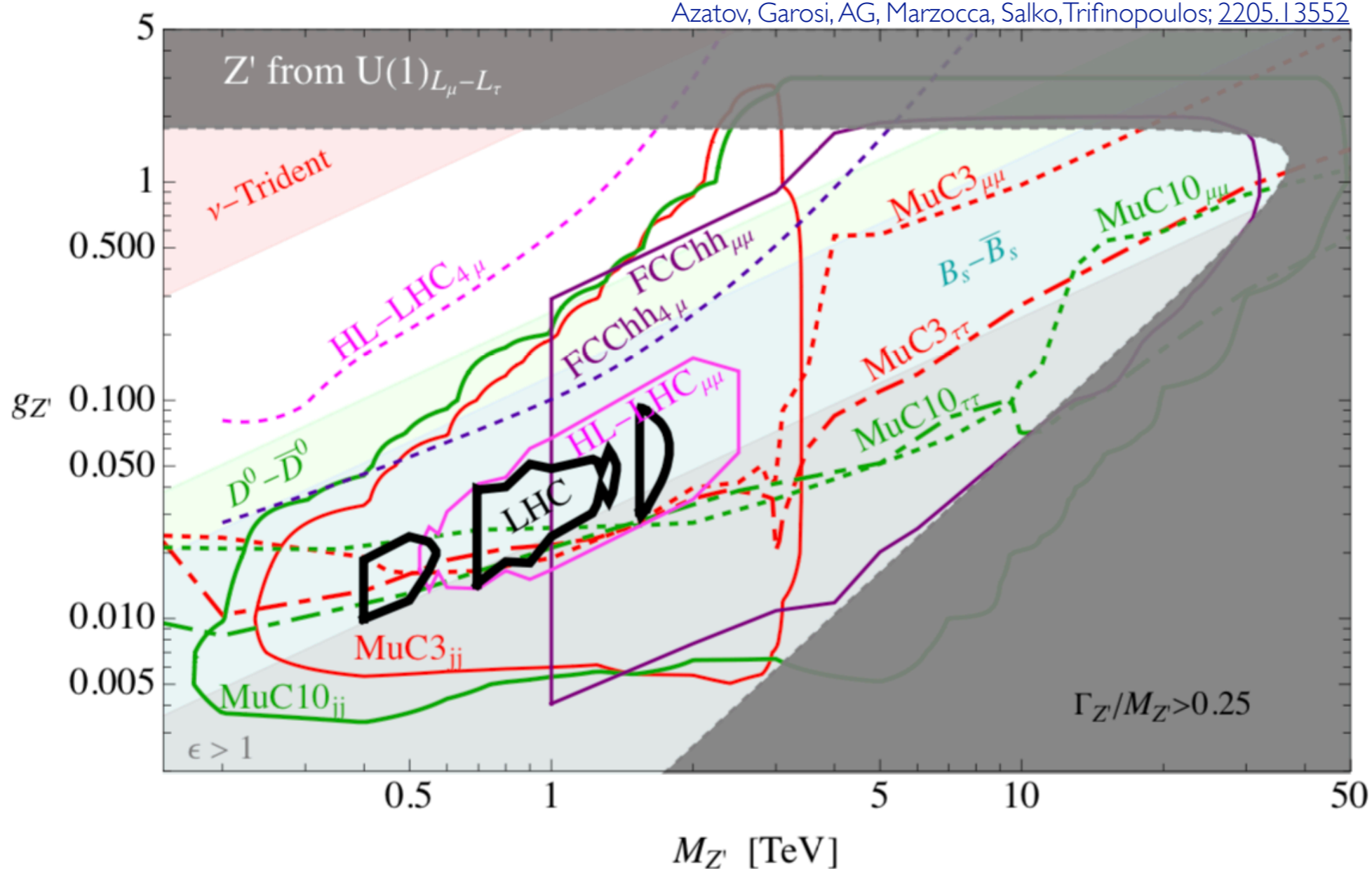
**Figure 11.** Discovery reach at  $5\sigma$  for the  $L_\mu - L_\tau$  model with  $\epsilon_s = \epsilon_b = 0$  in Eq. (5.6). In the dark gray region the  $Z'$  has a large width, signaling a loss of perturbativity.

# $Z'$ models: $L_\mu - L_\tau$

$$bs\mu\mu : \epsilon_b \epsilon_s^* = -5.7 \times 10^{-4} \left( \frac{M_{Z'}}{g_{Z'} \text{TeV}} \right)^2$$

e.g.  $\epsilon_b = -\epsilon_s$

Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; [2205.13552](#)

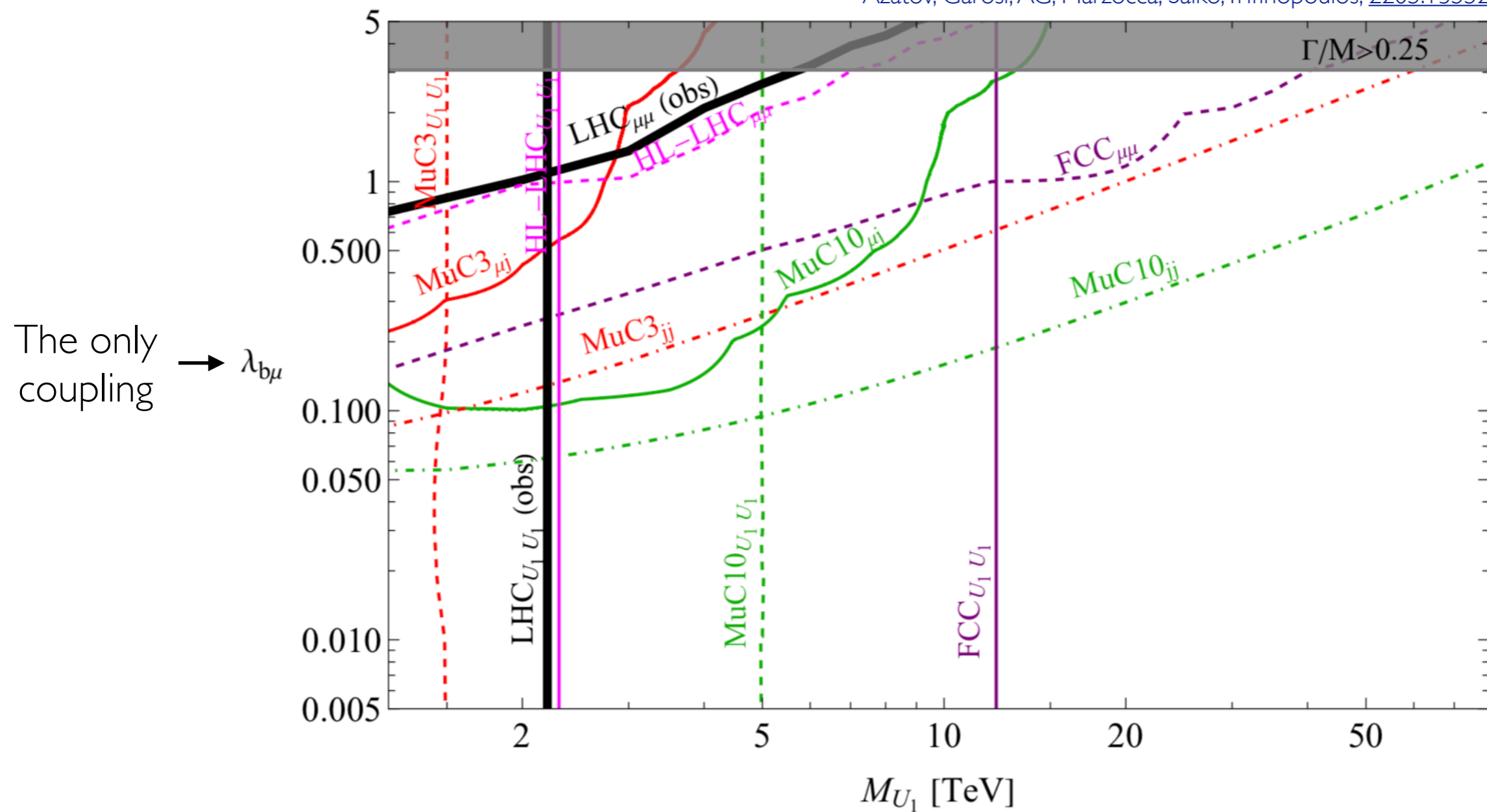


# Vector Leptoquark

$$U_1 \sim (\mathbf{3}, \mathbf{1}, 2/3)$$

$$\mathcal{L}_{U_1}^{\text{int}} = \lambda_{i\mu} \overline{Q}_L^i \gamma_\alpha L_L^2 U_1^\alpha + \text{h.c.} = \lambda_{i\mu} U_1^\alpha \left( V_{ji} \bar{u}_L^j \gamma_\alpha \nu_\mu + \bar{d}_L^i \gamma_\alpha \mu_L \right) + \text{h.c.}$$

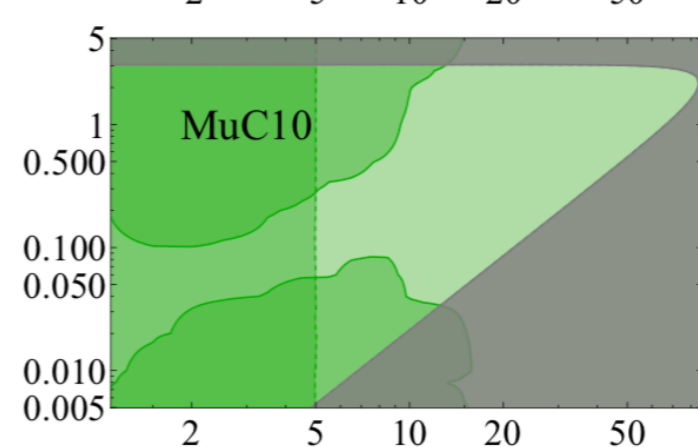
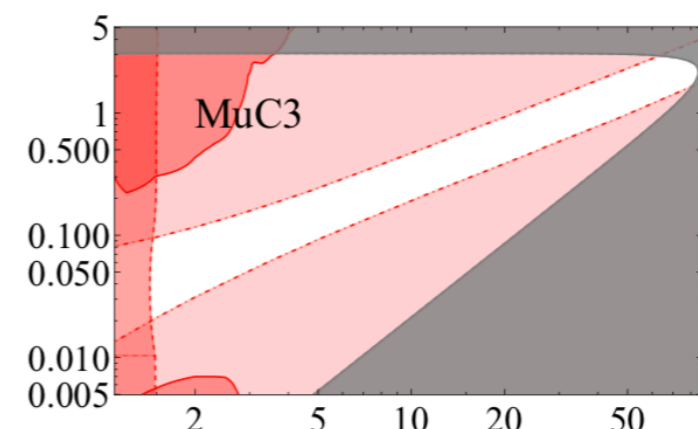
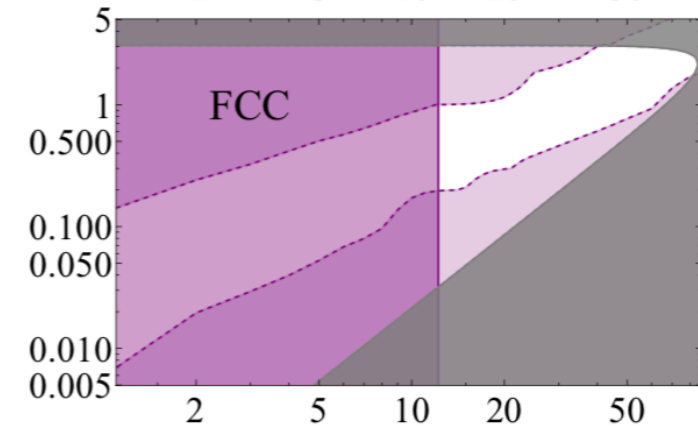
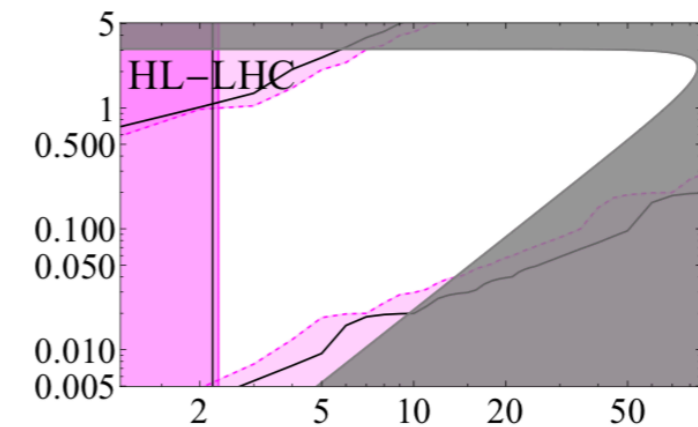
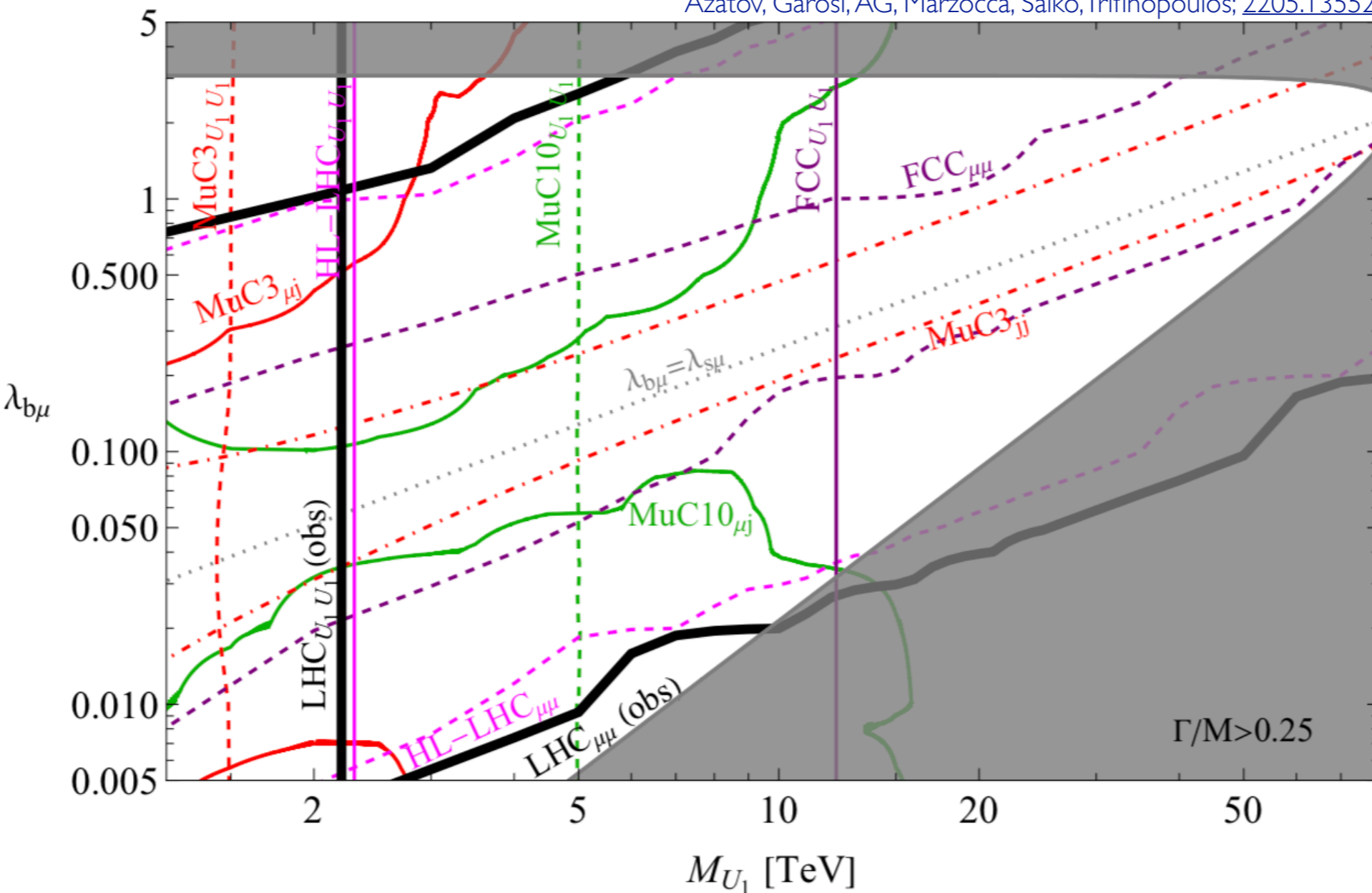
Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; 2205.13552



# Vector Leptoquark

$$\lambda_{b\mu} \lambda_{s\mu} = -8.4 \times 10^{-4} \left( \frac{M_{U_1}}{\text{TeV}} \right)^2$$

Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; [2205.13552](#)



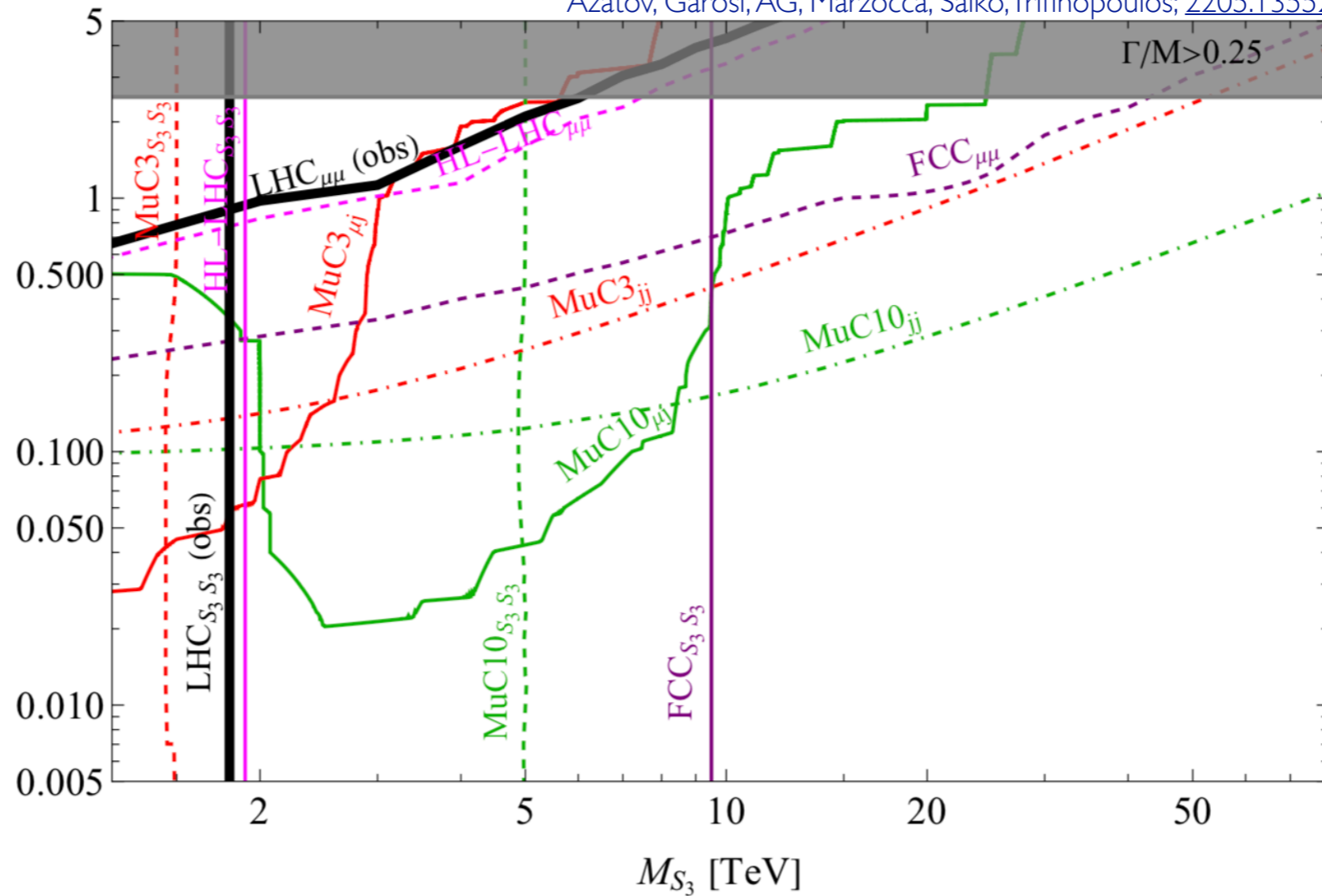
# Scalar Leptoquark

$$S_3 \sim (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$$

$$\begin{aligned} \mathcal{L}_{S_3}^{\text{int}} &= \lambda_{i\mu} \overline{Q}_L^{ic} \epsilon \sigma^I L_L^2 S_3^I + \text{h.c.} , \\ &= -\lambda_{i\mu} S_3^{(1/3)} (V_{ji}^* \overline{u}_L^{jc} \mu_L + \overline{d}_L^{ic} \nu_\mu) + \sqrt{2} \lambda_{i\mu} \left( V_{ji}^* S_3^{(-2/3)} \overline{u}_L^{jc} \nu_\mu - S_3^{(4/3)} \overline{d}_L^{ic} \mu_L \right) + \text{h.c.} \end{aligned}$$

Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; [2205.13552](#)

The only coupling  $\rightarrow \lambda_{b\mu}$

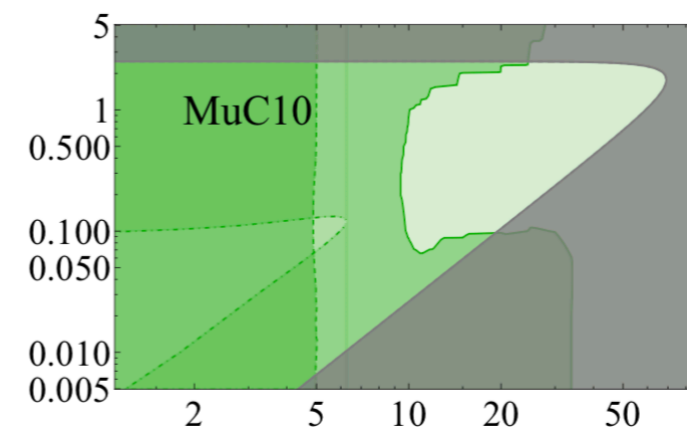
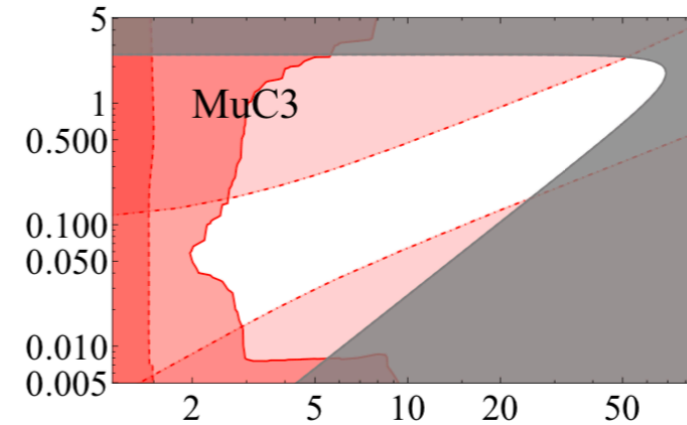
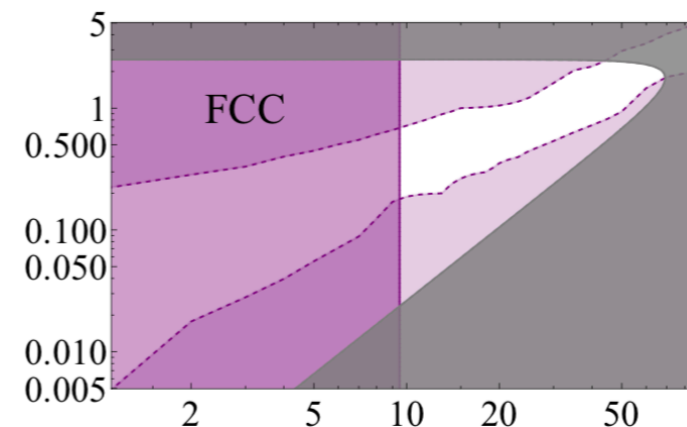
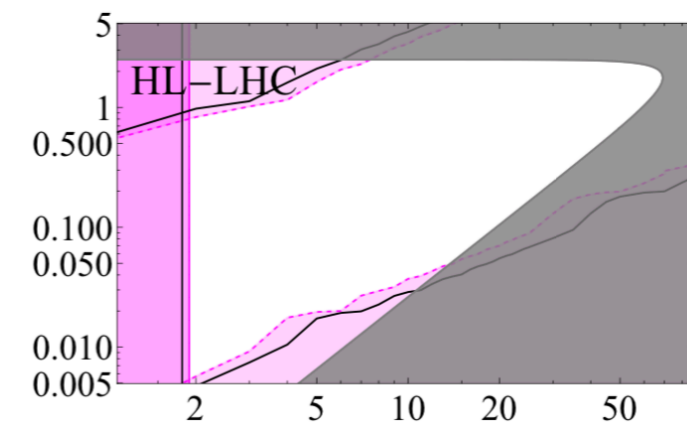
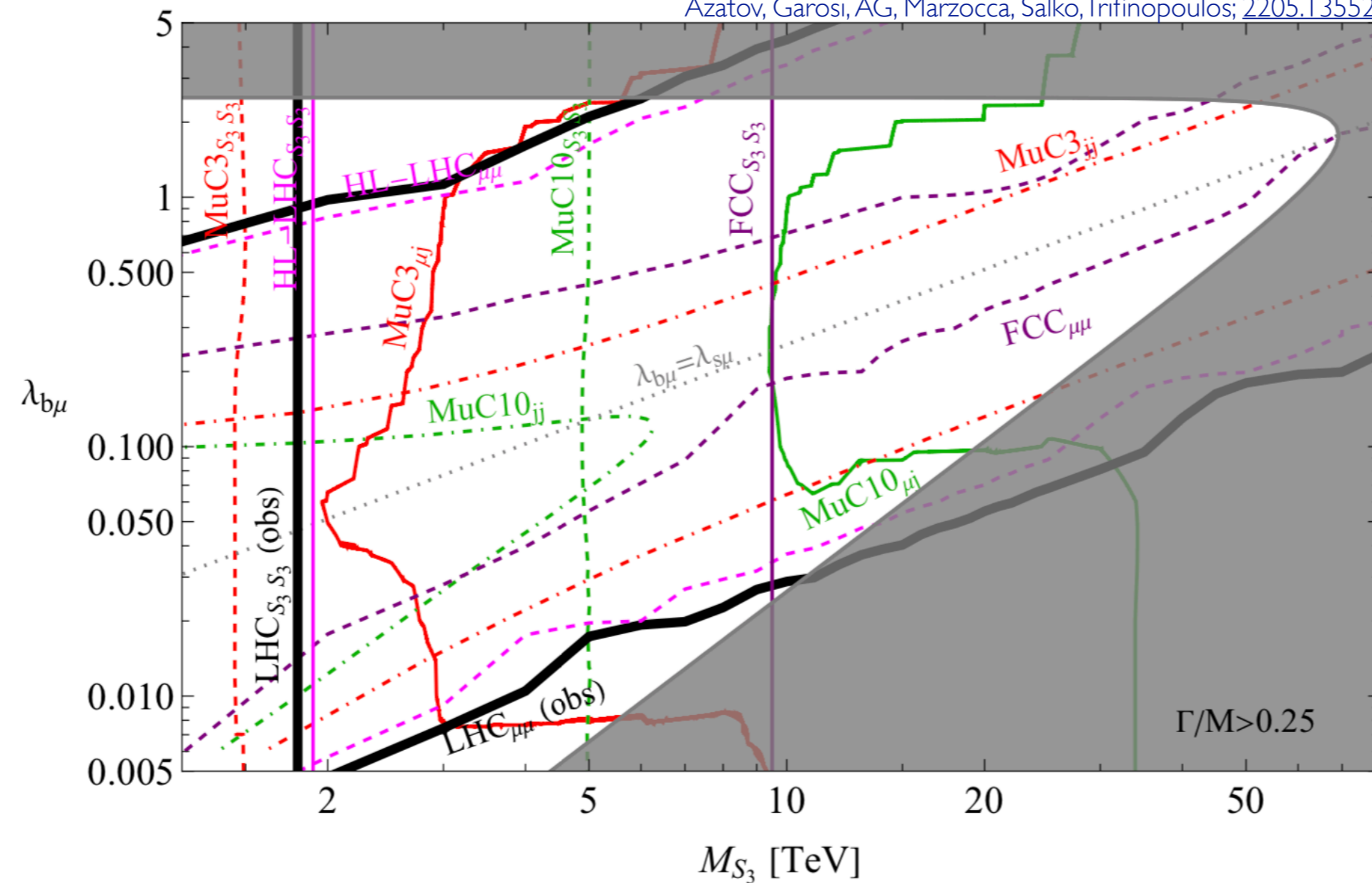


**Figure 13.** The  $5\sigma$  discovery prospects at future colliders for the  $S_3$  leptoquark assuming the  $U(2)^3$  quark flavour symmetry and the exclusive leptoquark coupling to muons (see Section 6.1).

# Scalar Leptoquark

$$\lambda_{b\mu} \lambda_{s\mu} = -8.4 \times 10^{-4} \left( \frac{M_{S_3}}{\text{TeV}} \right)^2$$

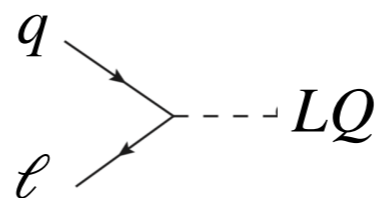
Azatov, Garosi, AG, Marzocca, Salko, Trifinopoulos; [2205.13552](#)





# Resonant Leptoquark production

- From the lepton PDF inside the proton



Buonocore, Haisch, Nason, Tramontano, Zanderighi; [2005.06475](#)  
 AG, Selimovic; [2012.02092](#)  
 Haisch, Polesello; [2012.11474](#)

- NLO QCD + QED matched to parton shower: POWHEG + HERWIG implementation

Buonocore, AG, Krack, Nason, Selimovic, Tramontano, Zanderighi; [2209.02599](#)

