n+²³⁵U Resonance Parameters and Neutrons Multiplicities in the Energy Region below 100 eV and Future Plans

M.T. Pigni¹, R. Capote², A. Trkov², V.G. Pronyaev³

- ¹ Oak Ridge National Laboratory, USA
- ² IAEA Nuclear Data Section, Austria
- ³ State Corporation Rosatom, Moscow, Russian Federation

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Outline

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 - Benchmark simulations (Trkov/Capote)
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Introduction

Motivation

- For nuclear critcality applications and many others, the existing evaluated data perform well in transport simulations partly owing to *compensating errors* in the nuclear data libraries
- CIELO collaboration provides a framework for nuclear data evaluation aimed to establish the highest fidelity general purpose nuclear database
- ²³⁵U among ¹H,¹⁶O,⁵⁶Fe,²³⁸U, ²³⁹Pu is one of the highest priority isotopes

Background

- Current status of ²³⁵U evaluation in ENDF/B-VII.1 library (2011)
 - Resonance parameters are the same as ENDF/B-VI.8 release (ORNL/TM-13516)¹
 - Description of the ²³⁵U resonance evaluation can be found in NEA/WPEC-18
- ²³⁵U ORNL resonance evaluation(=CIELOb18=**o23**) is part of the ENDF/B-VIII.0 β 2 and β 3 releases (2016)

¹See also L. C. Leal, H. Derrien, N. M. Larson, R. Q. Wright, Nucl. Sci. Eng., 131 230 (1999).

Nuclear Data ORNL Evaluation Overview

No.	Nucleus (I ^{<i>π</i>})	E _{max}	Method	$J_{3^{-}}$	J_{4^-}
1	²³⁵ U (7/2 ⁻)	2.25 keV	Reich-Moore	1433	1731

- The current ORNL resonance evaluation **o23** (ORNLv23) is an intermediate step of the evaluation process within CIELO
- The current **o23** resonance evaluation started from a set of resonance parameters (**o17**)
 - **o17** was documented in the ORNL presentation at the mini-CSEWG meeting (LANL, April 2016) and released in May 2016 as part of the ENDF/VIII.0 β 1 release.
- Particular emphasis in producing **o23** was devoted to
 - Sub-thermal and thermal : Thermal Constants (Pronyaev, micro. data)
 - Fission integrals (7.8-11 eV)
 - Neutron incident energies up to 20 eV for *measurements of* $\alpha = \sigma_{\gamma}/\sigma_f$ (or η)



Nuclear Data ORNL Evaluation Overview

- The current ORNL resonance evaluation **o23** is generated by the SAMMY code using the *Reich-Moore approximation*
 - All SAMMY inputs included in the current evaluation procedure are written using the most recent key-word for particle-pair definitions.
 - Isotopic impurities included
 - Parameters for the resolution functions (crunch data, γ-peak) of transmission experimental data (J. A. Harvey) retrieved from ORELA logbook (special thanks to K. Guber).
- Residuals and chi-squared of all experimental data



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SAMMY Algorithm

The various reaction cross sections $\sigma_{cc'}$ for an incoming channel c and outgoing channel c' can be written in terms of the matrix

$$X_{cc'} = \sqrt{P_c} L_c^{-1} \sum_{c''} \left[(L^{-1} - R)^{-1} \right]_{cc''} R_{c''c'} \sqrt{P_{c'}} \delta_{JJ'}, \tag{1}$$

where, in the eliminated-channel approximation, the matrix *R* (or *R*-matrix) for the channel spin group defined by the total spin J^{π} is

$$R_{cc'} = \left[\sum_{\lambda=1}^{n} \frac{\gamma_{\lambda c} \gamma_{\lambda c'}}{E_{\lambda} - E - \iota \bar{\Gamma}_{\lambda \gamma}/2} + R_{c}^{\text{ext}} \delta_{cc'}\right] \delta_{JJ'}$$
(2)

SAMMY derives from the best fit of experimental data the reducedwidth amplitude $\gamma_{\lambda c}$ related to the channel width using

$$\Gamma_{\lambda c} = 2\gamma_{\lambda c}^2 P_c(E) , \qquad (3)$$

where the penetrability factors depend on the Coulomb functions F_{ℓ} , G_{ℓ} as $P_c(E) = ka/[F_{\ell}^2(ka,\eta) + G_{\ell}^2(ka,\eta)]$.



Differential and Integral Data

Differential data

- Application of the *R*-matrix SAMMY method (Reich-Moore) to determine a consistent set of neutron resonance parameters (RP) based on the fit of available experimental data (transmission, capture, angular distribution, ...)
- Statistical properties of RP such as average spacing $\langle D_\ell \rangle$ and strength function S_ℓ



Integral data

- Resonance parameter and covariance are converted into the ENDF/B format - file 2 (parameter) and 32 (covariance matrix)
- Process ENDF/B file with processing codes as NJOY or AMPX in order to generate cross section in point-wise and/or group representation
- Test evaluations against integral benchmarks (e.g. reaction rate) sensitive to a specific energy range (RRR)

$$R = \int_{RR} \sigma(E) \phi(E) dE \qquad (4)$$



Thermal Cross Sections and Integrals

- o23 values for fission and capture thermal cross sections are based on ²³⁵U(n,f) thermal constants obtained on the basis of microscopic data (i.e., only considering Wallner thermal capture measurements)
- Fission integral (I₄=247.0 b⋅eV in the Figure below) between 7.8 and 11 eV based on recommendation of Neutron Standards (246.4 b⋅eV)



Results



- n+²³⁵U η measurements of Brooks, Wartena, and Weigmann (left) and Gwin's fission measured cross sections (right) compared to ENDF/B-VII.1 and ENDF/B-VIII.0 β 2 values.
- the CIELO η (decreased) values are, on average, in better agreement with the experimental data
 - achieved by increasing the capture cross sections, mostly in the valley of the resonances while keeping their peak values unchanged. The resonance at $E_n=2$ eV is clearly an example.
- The sensitivity of the resonance parameters to fission cross sections seems to be more relevant than to capture cross sections at neutron energies \geq 4 eV (see fission cross sections shown in blue continuous line).



Other Results



Neutron multiplicities $\bar{v}(E)^2$

• In the observed $\bar{v}(E)$ there are clear fluctuations roughly correlated with the energy of compound nucleus resonances, but also partially explained by the influence of the $(n, \gamma f)$ process, where a γ is emitted prior to the fission event



Figure 1: $\bar{v}(E)$ relative to $\bar{v}(E_{\text{th}})$ calculated at thermal energy (0.0253 eV) for n+²³⁵U reactions. Several experimental data sets are compared to three evaluated data.



²Pronyaev/Capote

ATLF benchmark simulations³

- Results of the suite of integral benchmarks for thermal solutions of highly enriched uranium (HEU-SOL-THERM)
- Results displayed as a function of the above-thermal-leakage fraction (ATLF)



Figure 2: Differences (in pcm) between predicted and measured k_{eff} of ATLF benchmarks using ENDF/B-VII.0 (in red) and the ENDF/B-VIII.0 β_2 evaluation (in black).



³Trkov/Capote

Future plans

- To improve the evaluation work by including newly measured data for fission and capture cross sections, namely from the RPI and nTOF collaborations
- To include an improved set of resonance parameters for incident neutron energies above 500 eV. The present evaluation is based on the ENDF/B-VII.1, in which the set of resonances are pseudo-resonances with different statistical properties than the true resonances in the energy range up 100 eV



• To include improved distribution of the fission widths. Analyses of the ²³⁵U fission widths showed that the number of degrees of freedom does not obey the chi-squared distribution



Summary and Conclusions

- We applied the *R*-matrix SAMMY method using the Reich-Moore approximation to determine a consistent set of neutron resonance parameters for ²³⁵U
- The **o23**=CIELOb18 is currently part of the ENDF/B-VIII.0 β 3 (October 2016)
- Constraints applied on the **o23** resonance parameter evaluation are
 - Brooks' η experimental data
 - Standard thermal cross sections and the fission integral between 7.8-11 eV
 - New thermal Prompt Fission Neutron Spectra (PFNS)
- The present set of resonance parameters yields cross sections still in reasonable agreement with the suite of experimental data
- The validation analysis on the thermal benchmarks showed good agreement with the experimental response and that the **o23** resonance parameters are compatible with the current values of \bar{v} (from thermal constants) and thermal PFNS (average energy 2.00±0.01)
- Paper submitted to ND2016 conference proceedings

Conclusion : new resonance analysis allowed to combine new evaluation of Thermal Neutron Constants, the recommended value of the fission resonance integral from 7.8-11 eV, new PFNS evaluation, and to describe Brooks data while keeping an excellent agreement with existing fission, capture and transmission measurements.

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Thank you!

