

Quark and Gluon Helicity Evolution at Small x

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Based on Florian Cougoulic, Yuri Kovchegov, Andrey Tarasov, Yossathorn Tawabutr, JHEP 07 (2022) 095



Proton helicity structure

The fundamental properties of hadrons, and in particular its spin, are defined by the complex dynamics of quarks and gluons which form a strongly bonded many-body parton system. This dynamics in the context of spin dependent observables is not well understood (spin puzzle, large uncertainties at small-x etc.)



There is a lot of interest to study quark and gluon helicity evolution at small x



D. De Florian, R. Sassot, M. Stra W. Vogelsang, PRL 113 (2014)

Helicity and sub-eikonal corrections at small-x

The analysis is non-trivial since it requires calculation of the sub-eikonal corrections at small-x. Indeed, in the leading (eikonal) approximation:



In the CGC EFT the shockwave background field has an infinitesimally small support and doesn't have the transverse component:

$$A_{\rm cl}^+(x) = -\frac{1}{\partial_{\perp}^2} \rho(x_{\perp}) \delta(x^-); \quad A_{\rm cl}^-(x) = A_{\rm cl}^i(x) = 0$$

To include spin effects one has to take into account sub-eikonal corrections, related both to the A_i component and non-zero width of the shock-wave

Impact factor

$$\int \frac{d^2 p_{\perp}}{4\pi^2} I(p_{\perp}, q_{\perp}) Tr\{U(p_{\perp})U^{\dagger}(q_{\perp} - p_{\perp})\}$$
Balitsky (

Light-cone Wilson lines contain no information on the proton helicity

McLerran, Venugopalan (1994)





² Subject of a for which both s Subjections and the role of the anomaly inable all. classical Ward identity (2.1) is corrected quantum mechanically, we the strate to be a strate of the second of t spections correlation function can be summarized in the photon has to be conserved The size of the design of the right had the classical Carrenton and the sign of the here and the second of the ch sublementat broderthat net for mont Frederichter as chassie alfinder ations ber chiral) hat is the the second of the state of the second with the residence of the second with the second of the second tancoire for the shift of the second feature distance we algo and the second second sector. "This res The property of the physical sector is the photon has to be conserved or claring the photon has to be photon has to be conserved or claring the photon has to be photon has as the diam function son of the light (hand bid to be bassical equatic ding expressions for the expectation value of 2the axial current diver-This means new and independent of the fermion mass. 1. (2.21). After a couple of integrations by parts, The only have to use Eq. (2.21). After a couple of integrations by parts, the correspondence of the set of grais grassically divergent and the correspondence of C_D be loafed using the Feynman rules of grain -(P, S) for (0) P, S) + O(-2)septilsating had a did bid this it weaks a context ad had integration of the axial current $\mu\nu\alpha\beta$ Shore, Veneziano (1992) $-\gamma_{\alpha}$ Shore, Veneziano (1992) $-\gamma_{\alpha}$ Janohlas (1990) Tarasov, Venugopajan (2020) quanting symmetry as an on out us hans, $l\epsilon$ Bhattacharya, Hatta; ¥ogelsang (2022)



Factorization scheme

To define the structure of the sub-eikonal correction one first needs to define the factorization scheme. Since we work in the small-x limit we use the rapidity factorization, where all fields are divided based on the value of the p^- component



Impact factor can be calculated by explicit integration over fast fields ($p^- > \sigma$), while slow fields ($p^- < \sigma$) are fixed and give rise to the operator









Background field method

The separation of fields into "slow" and "fast" can be formally done in the background field method. We start with a matrix element of an arbitrary operator:

$$\langle P_1 | \mathcal{O} | P_2 \rangle = \int \mathcal{D}A \int \mathcal{D}\psi \,\Psi_{P_1}^*(\vec{A}(t_f), \psi(t_f)) \,\mathcal{O}(A, \psi) \,\Psi_{P_2}(\vec{A}(t_i), \psi(t_i)) e^{iS_{QCD}(A, \psi)}$$

and separate fields into fast ("quantum") and slow ("background"):

$$A_{\mu} \to A^{\mathbf{q}}_{\mu} + A^{\mathbf{bg}}_{\mu}, \quad \psi \to \psi^{\mathbf{q}} + \psi^{\mathbf{bg}}$$

as a result the matrix element can be rewritten as

$$\langle P_1 | \mathcal{O} | P_2 \rangle = \int \mathcal{D}A^{\mathrm{bg}} \int \mathcal{D}\psi^{\mathrm{bg}} \Psi_{P_1}^* (\vec{A}^{\mathrm{bg}}(t_f), \psi^{\mathrm{bg}}(t_f)) \tilde{\mathcal{O}}(A^{\mathrm{bg}}, \psi^{\mathrm{bg}}, \sigma) \Psi_{P_2}(\vec{A}^{\mathrm{bg}}(t_i), \psi^{\mathrm{bg}}(t_i)) e^{iS_{QCD}(A^{\mathrm{bg}}, \psi^{\mathrm{bg}}, \sigma)} \psi^{\mathrm{bg}}(t_i) \psi^{\mathrm{bg}}(t_i)$$

$$\tilde{\mathcal{O}}(A^{\mathrm{bg}},\psi^{\mathrm{bg}},\sigma) = \int \mathcal{D}A^{\mathrm{q}} \int \mathcal{D}\psi^{\mathrm{q}} \mathcal{O}(A^{\mathrm{bg}},\psi^{\mathrm{bg}},\sigma)$$

and the QCD action in the background fields is

$$S_{bQCD}(A^{q},\psi^{q};A^{bg},\psi^{bg}) = S_{QCD}(A^{q}+A^{bg},\psi^{q}+\psi^{bg}) - S_{QCD}(A^{bg},\psi^{bg})$$

integrate over quantum fields $\mathcal{O}(A^{\mathbf{q}} + A^{\mathbf{bg}}, \psi^{\mathbf{q}} + \psi^{\mathbf{bg}})e^{iS_{bQCD}(A^{\mathbf{q}}, \psi^{\mathbf{q}}; A^{\mathbf{bg}}, \psi^{\mathbf{bg}})}$

Abbott (1981)

 $^{\mathrm{g}},\psi^{\mathrm{bg}})$

Propagators in the background field

Our goal is to perform integration over quantum fields which in general gives the following result

$$\tilde{\mathcal{O}}(A^{\mathrm{bg}},\psi^{\mathrm{bg}},\sigma) = \sum_{i}^{i}$$

Integration over quantum fields generates propagators in the background field. scalar propagator:

$$(x|\frac{1}{P^2 + i\epsilon}|y) = (x|\frac{1}{p^2 + g\{p^{\mu}, A_{\mu}(x)\} + g^2 A^{\mu}(x)A_{\mu}(x)}$$

quark propagator:

$$T\left[\psi(x)\bar{\psi}(y)\right]_A = \left(x\left|\frac{i}{\not P + i\epsilon}\right|y\right) = \left(x\left|\not P - \frac{i}{h}\right|\right)$$

Worldline representation of the propagator



Eikonal expansion of the gluon propagator (axial gauge)

The general form of the propagators has to be simplified. We construct an eikonal expansion in the shockwave approximation of the propagators which is suited to the rapidity factorization

$$T [C^{a}_{\mu}(x)C^{b}_{\nu}(y)] = -\frac{1}{2\pi} \int_{0}^{\infty} \frac{dp^{-}}{2p^{-}} e^{-ip^{-}(x-y)^{+}} \qquad \text{describes interaction with the background field} \\ \times (x_{\perp}|(g_{\mu i} - \frac{n_{\mu}}{p^{-}}p_{i})^{ac} e^{-i\frac{p_{\perp}^{2}}{2p^{-}}x^{-}} \mathcal{G}^{ij}(\infty, -\infty) e^{i\frac{p_{\perp}^{2}}{2p^{-}}y^{-}} (g_{j\nu} - p_{j}\frac{n_{\nu}}{p^{-}})^{db}|y_{\perp}) + \dots$$

eikonal contribution

$$\mathcal{G}^{ij}(\infty, -\infty) = g^{ij}U + \frac{g^{ij}s}{2P^+p^-}U^{q[2]} + \frac{i\epsilon^{ij}s}{2P^+p^-}U^{pol[1]}$$

$$-\frac{igg^{ij}}{2p^-}p^k \int_{-\infty}^{\infty} dz^- z^- U[\infty, z^-]\mathcal{F}_{-k}U[z^-, -\infty] - \frac{igg^{ij}}{2p^-} \int_{-\infty}^{\infty} dz^- z^- U[\infty, z^-]\mathcal{F}_{-k}U[z^-, -\infty]p^k + \frac{ig^2g^{ij}}{2p^-} \int_{-\infty}^{\infty} dz^- z^- U[\infty, z^-]\mathcal{F}_{-k}U[z^-, -\infty] + O\left(\frac{1}{(p^-)^2}\right).$$

Sub-eikonal corrections are suppressed by $1/p^{-1}$

are different operators sub-eikonal level

see also Kovchegov, Pitonyak, Sievert (2017) Altinoluk, Armesto, Beuf, Martínez, Salgado (2014) **Chirilli (2019) Balitsky**, **Tarasov** (2015)







Helicity evolution and sub-eikonal operators

We find that only two operators contribute to the helicity evolution. There is a genuine helicity dependent operator (e.g. see term in the quark propagator) which gives an amplitude

$$Q_{10}(\sigma) \equiv \frac{1}{2N_c} \left\langle \! \left\langle \operatorname{Ttr} \left[V_0 \, V_1^{\operatorname{pol}[1]\dagger} \right] + \operatorname{Ttr} \left[V_1^{\operatorname{pol}[1]} \, V_1 \right] \right\rangle \right\rangle$$

$$\begin{aligned} V_x^{\rm G[1]} &= \frac{i\,g\,P^+}{s} \int\limits_{-\infty}^{\infty} dx^- V_x[\infty, x^-]\,F^{12}(x^-, x_\perp)\,\,V_x[x^-, x_\perp]\,V_x[x^-, x_\perp]\,V_x^{\rm G[1]} \\ &= \frac{g^2P^+}{2\,s} \int\limits_{-\infty}^{\infty} dx_1^- \int\limits_{x_1^-}^{\infty} dx_2^- V_x[\infty, x_2^-]\,t^b\,\psi_\beta(x_2^-, x_\perp)\,U_\alpha(x_2^-, x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x_\perp)\,U_\alpha(x$$

Helicity evolution which includes this operator has been studied before (Kovchegov, Pitonyak, Sievert 2016-2019), however the result didn't match the DGLAP evolution (Bartels, Ermolaev and Ryskin 1996).

 $V_0^{\dagger} \rangle \rangle (\sigma)$ $V_{r}^{\text{pol}[1]} = V_{r}^{\text{G}[1]} + V_{r}^{\text{q}[1]}$



Note that this operator doesn't contribute in the collinear limit

 $U_x^{ba}[x_2^-, x_1^-] \left[\gamma^+ \gamma^5\right]_{\alpha\beta} \bar{\psi}_{\alpha}(x_1^-, x_{\perp}) t^a V_x[x_1^-, -\infty]$

Helicity evolution and sub-eikonal operators

We find another operator at the sub-eikonal level which generates the DGLAP evolution. This operator comes from the scalar phase in the propagator when we expand it onto the light-cone direction. In particular at smallx this operator describes corrections due to non-zero width of the shock-wave.

$$G_{10}^{i}(\sigma) \equiv \frac{igP^{+}}{2sN_{c}} \left\langle \! \left\langle \mathbf{T} \operatorname{tr} \left[V_{0}^{\dagger} \int_{-\infty}^{\infty} dz^{-} z^{-} V_{1}[\infty, z^{-}] F^{+i} V_{1}[z^{-}, -\infty] \right] + \mathrm{c.c.} \right\rangle \! \right\rangle(\sigma)$$

This operator is related to the Jaffe-Manohar polarized gluon distribution. Can by obtained by expanding the exponential factor in the latter:

$$\int_{-\infty}^{\infty} dz^{-} e^{ixP^{+}z^{-}} V_{1}[\infty, z^{-}] F^{+i}(z^{-}, x_{1}) V_{1}[z^{-}, -\infty]$$
$$= -\int_{-\infty}^{\infty} dz^{-} V_{1}[\infty, z^{-}] \partial^{i} A^{+} V_{1}[z^{-}, -\infty] + ixP^{+} \int_{-\infty}^{\infty}$$

The operator can be also rewritten as $ig \int dz^{-} z^{-} V_{x}[c]$

$$\int dz^{-} z^{-} V_{1}[\infty, z^{-}] F^{+i} V_{1}[z^{-}, -\infty] + \dots$$

$$\infty, z^{-}] F_{-k} V_{x}[z^{-}, -\infty] = \frac{1}{2} \int_{-\infty}^{\infty} dz^{-} V_{x}[\infty, z^{-}] \left[D_{k} - \overleftarrow{D}_{k} \right] V_{x}[z^{-}]$$



Sub-eikonal corrections and helicity dependent observables

$$\sigma^{\gamma^* p} \propto -\sum_{f} \frac{N_c Z_f^2}{4\pi^4} \int d^2 x_{10} \int_{\Lambda^2/s}^{1} \frac{dz}{z} \left\{ 2 \left[z^2 + (1-z)^2 \right] a_f^2 \left[K_1(x_{10} a_f) \right]^2 G_2(x_{10}^2, zs) \right. \\ \left. + \left[(1-2z) a_f^2 \left[K_1(x_{10} a_f) \right]^2 - m_f^2 \left[K_0(x_{10} a_f) \right]^2 \right] Q(x_{10}^2, zs) \right\}$$

where dipole amplitudes are integrated over impact parameter:

$$\int d^2 \left(\frac{x_1 + x_0}{2}\right) G_{10}^i(zs) = (x_{10})^i_{\perp} G_1$$
$$\int d^2 \left(\frac{x_0 + x_1}{2}\right) Q_{10}(zs) = Q(x_{10}^2, zs)$$



Helicity dependent interaction via sub-eikonal operators

 $(x_{10}^2, zs) + \epsilon^{ij} (x_{10})^j G_2(x_{10}^2, zs)$

Evolution in the rapidity factorization approach

Introduce a new scale σ' and redefine the background fields as



 $\mathrm{T}\left[\mathcal{V}_{i}\left(A^{\mathrm{bg}}\right)\right]$

$$A^{\mathrm{bg}}_{\mu} \to \hat{A}^{\mathrm{q}}_{\mu} + \hat{A}^{\mathrm{bg}}_{\mu}, \quad \psi^{\mathrm{bg}} \to \hat{\psi}^{\mathrm{q}} + \hat{\psi}^{\mathrm{bg}}$$

Perform integration over new quantum fields in

$$[\int \mathcal{D}\hat{\psi}^{\mathrm{q}} \, \mathcal{V}_i(\hat{A}^{\mathrm{q}} + \hat{A}^{\mathrm{bg}}, \hat{\psi}^{\mathrm{q}} + \hat{\psi}^{\mathrm{bg}}, \sigma) e^{iS_{bQCD}(\hat{A}^{\mathrm{q}}, \hat{\psi}^{\mathrm{q}}; \hat{A}^{\mathrm{bg}})}$$

The result of integration yields an evolution equation of the

$$[g, \psi^{\mathrm{bg}}, \sigma)] = \int_{\sigma'}^{\sigma} \frac{dp^{-}}{p^{-}} \sum_{j} \mathcal{K}_{ij} \otimes \mathcal{V}_{j}(\hat{A}^{\mathrm{bg}}, \hat{\psi}^{\mathrm{bg}}, \sigma)$$





Evolution diagrams



Evolution equations

 $-\infty$

$$\begin{split} &\frac{1}{2N_{c}}\left\langle\!\!\left\langle \mathrm{T}\operatorname{tr}\left[V_{0}V_{1}^{\mathrm{pol}[1]\dagger}\right] + \mathrm{c.c.}\right\rangle\!\!\left\langle(\sigma\right) = \frac{1}{2N_{c}}\left\langle\!\!\left\langle\mathrm{T}\operatorname{tr}\left[V_{0}V_{1}^{\mathrm{pol}[1]\dagger}\right] + \mathrm{c.c.}\right\rangle\!\!\right\rangle_{0}(\sigma) \\ &+ \frac{\alpha_{s}N_{c}}{2\pi^{2}}\int_{\sigma'}^{\sigma}\frac{dp^{-}}{p^{-}}\int d^{2}x_{2}\left\{\left[\frac{1}{x_{21}^{2}} - \frac{x_{21} \cdot x_{20}}{x_{21}^{2}x_{20}^{2}}\right]\frac{1}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[t^{b}V_{0}t^{a}V_{1}^{\dagger}\right]\left(U_{2}^{\mathrm{pol}[1]}\right)^{ba} + \mathrm{c.c.}\right\rangle\!\!\right\rangle(\sigma') \\ &+ \left[2\epsilon^{ij}\frac{x_{21}^{j}}{x_{21}^{4}} - \frac{\epsilon^{ij}(x_{21}^{j} + x_{20}^{j})}{x_{21}^{2}x_{20}^{2}} - \frac{2x_{20} \times x_{21}}{x_{21}^{2}x_{20}^{2}}\left(\frac{x_{21}^{j}}{x_{21}^{2}} - \frac{x_{20}^{j}}{x_{20}^{2}}\right)\right]\frac{1}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[t^{b}V_{0}t^{a}V_{1}^{\dagger}\right]\left(U_{2}^{\mathrm{iG}[2]}\right)^{ba} + \mathrm{c.c.}\right\rangle\!\!\right\rangle(\sigma')\right\} \\ &+ \frac{\alpha_{s}N_{c}}{4\pi^{2}}\int_{\sigma'}^{\sigma}\frac{dp^{-}}{p^{-}}\int\frac{d^{2}x_{2}}{x_{21}^{2}}\left\{\frac{1}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[V_{0}t^{a}V_{2}^{\mathrm{pol}[1]\dagger}t^{b}\right]U_{1}^{ba}\right\rangle\!\!\right\rangle(\sigma') + 2\frac{\epsilon^{ij}x_{21}^{j}}{x_{21}^{2}}\frac{1}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[t^{b}V_{0}t^{a}V_{2}^{\mathrm{iG}[2]\dagger}\right]U_{1}^{ba}\right\rangle\!\!\right\rangle(\sigma') + \mathrm{c.c.}\right\rangle\!\!\right\rangle(\sigma') + \epsilon c \\ &+ \frac{\alpha_{s}N_{c}}{2\pi^{2}}\int_{\sigma'}^{\sigma}\frac{dp^{-}}{p^{-}}\int d^{2}x_{2}\frac{x_{10}^{2}}{x_{21}^{2}}\left\{\frac{1}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[t^{b}V_{0}t^{a}V_{1}^{\mathrm{pol}[1]\dagger}\right]U_{1}^{ba}\right\rangle\!\!\right\rangle(\sigma') + 2\frac{\epsilon^{ij}x_{21}^{j}}{x_{21}^{2}}\frac{1}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[V_{0}V_{1}^{\mathrm{pol}[1]\dagger}\right]U_{1}^{ba}\right\rangle\!\!\right\rangle(\sigma') + \mathrm{c.c.}\right\rangle\!\!\right\} \\ &+ \frac{\alpha_{s}N_{c}}{2\pi^{2}}\int_{\sigma'}^{\sigma}\frac{dp^{-}}{p^{-}}\int d^{2}x_{2}\frac{x_{10}^{2}}{x_{21}^{2}}\left\{\frac{1}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[t^{b}V_{0}t^{a}V_{1}^{\mathrm{pol}[1]\dagger}\right]U_{1}^{ba}\right\rangle\!\!\right\rangle(\sigma') + 2\frac{\epsilon^{ij}x_{21}^{j}}{x_{21}^{2}}\frac{1}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[V_{0}V_{1}^{\mathrm{pol}[1]\dagger}\right]U_{1}^{ba}\right\rangle\!\!\right)(\sigma') + \mathrm{c.c.}\right\} \\ &+ \frac{\alpha_{s}N_{c}}\left\{\frac{1}{2\pi^{2}}\int_{\sigma'}^{\sigma}\frac{dp^{-}}{p^{-}}\int d^{2}x_{2}\frac{x_{10}^{2}}{x_{21}^{2}x_{20}^{2}\left\{\frac{1}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[t^{b}V_{0}t^{a}V_{1}^{\mathrm{pol}[1]\dagger}\right]U_{1}^{bb}\right\}\!\!\right)(\sigma') + 2\frac{\epsilon^{ij}x_{21}^{j}}{N_{c}^{2}}\left\langle\!\left\langle\mathrm{tr}\left[V_{0}V_{1}^{\mathrm{pol}[1]\dagger}\right]V_{1}^{j}\right\rangle(\sigma') + \mathrm{c.c.}\right\} \\ &+ \frac{\alpha_{s}N_{c}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}\left\{\frac{1}{2\pi^{2}}$$

which gives rise to the dipole amplitude G_{10}^i . We construct an evolution equation for this amplitude as well. The evolution equations contain mixing between two types of operators.





Evolution equations in the large $N_{\!\mathcal{C}}$ limit

We obtain a closed system of DLA evolution equations for helicity at large N_c (four equations in total) Cougoulic, Kovchegov, Tarasov, Tawabutr (2022)

$$G(x_{10}^2, zs) = G^{(0)}(x_{10}^2, zs) + \frac{\alpha_s N_c}{2\pi} \int_{\frac{1}{sx_{10}^2}}^z \frac{dz'}{z'} \int_{\frac{1}{z's}}^{x_{10}^2} \frac{dx_{21}^2}{x_{21}^2} \left[\Gamma(x_{10}^2, x_{21}^2, z's) + 3G(x_{21}^2, z's) + 2G_2(x_{21}^2, z's) + 2\Gamma_2(x_{10}^2, x_{21}^2, z's) \right]$$

$$\Gamma(x_{10}^2, x_{21}^2, z's) = G^{(0)}(x_{10}^2, z's) + \frac{\alpha_s N_c}{2\pi} \int_{\frac{1}{sx_{10}^2}}^{z'} \int_{\frac{1}{sx_{10}^2}}^{\min\left[x_{10}^2, x_{21}^2 \frac{z'}{z''}\right]} \int_{\frac{1}{z''s}}^{\min\left[x_{10}^2, x_{21}^2 \frac{z'}{z''}\right]} \frac{dx_{32}^2}{x_{32}^2} \left[\Gamma(x_{10}^2, x_{32}^2, z''s) + 3G(x_{32}^2, z''s) + 2G_2(x_{32}^2, z''s) + 2\Gamma_2(x_{10}^2, x_{32}^2, z''s) + 2G_2(x_{32}^2, z''s) + 2G_2(x_$$

where amplitudes G, Γ , G_2 and Γ_2 parametrize operators with dipole amplitudes G_{10}^i and Q_{10} .

One can construct a numerical solution of these equations, which leads to a result which is consistent with the small-x DGLAP evolution and is in complete agreement with the result obtained in the infrared evolution equations (IREE) approach (see Bartels, Ermolaev and Ryskin 1996)

+ two similar equations for G_2 and Γ_2

$$\Delta \Sigma(x, Q^2) \sim \Delta G(x, Q^2) \sim \left(\frac{1}{x}\right)^{3.66\sqrt{3}}$$



Summary

- We consider the problem of small Bjorken-x evolution of the gluon and flavor-singlet quark helicity distributions in the shock-wave formalism
- We obtain a complete set of the sub-eikonal corrections relevant to the small-x helicity evolution
- We find that the evolution contains not only fields strength operator F_{12} and quark axial current $\bar{\psi}\gamma^+\gamma_5\psi$, but also a sub-eikonal operator $D^i - \overleftarrow{D}^i$
- The operator $D^i \overleftarrow{D}^i$ is related to the Jaffe-Manohar polarized gluon distribution and has a meaning of the sub-eikonal (covariant) phase
- We construct novel evolution equations mixing all three operators
- We also construct closed double-logarithmic evolution equations in the large- N_c and large- N_c & N_f limits





Thank you for your attention!