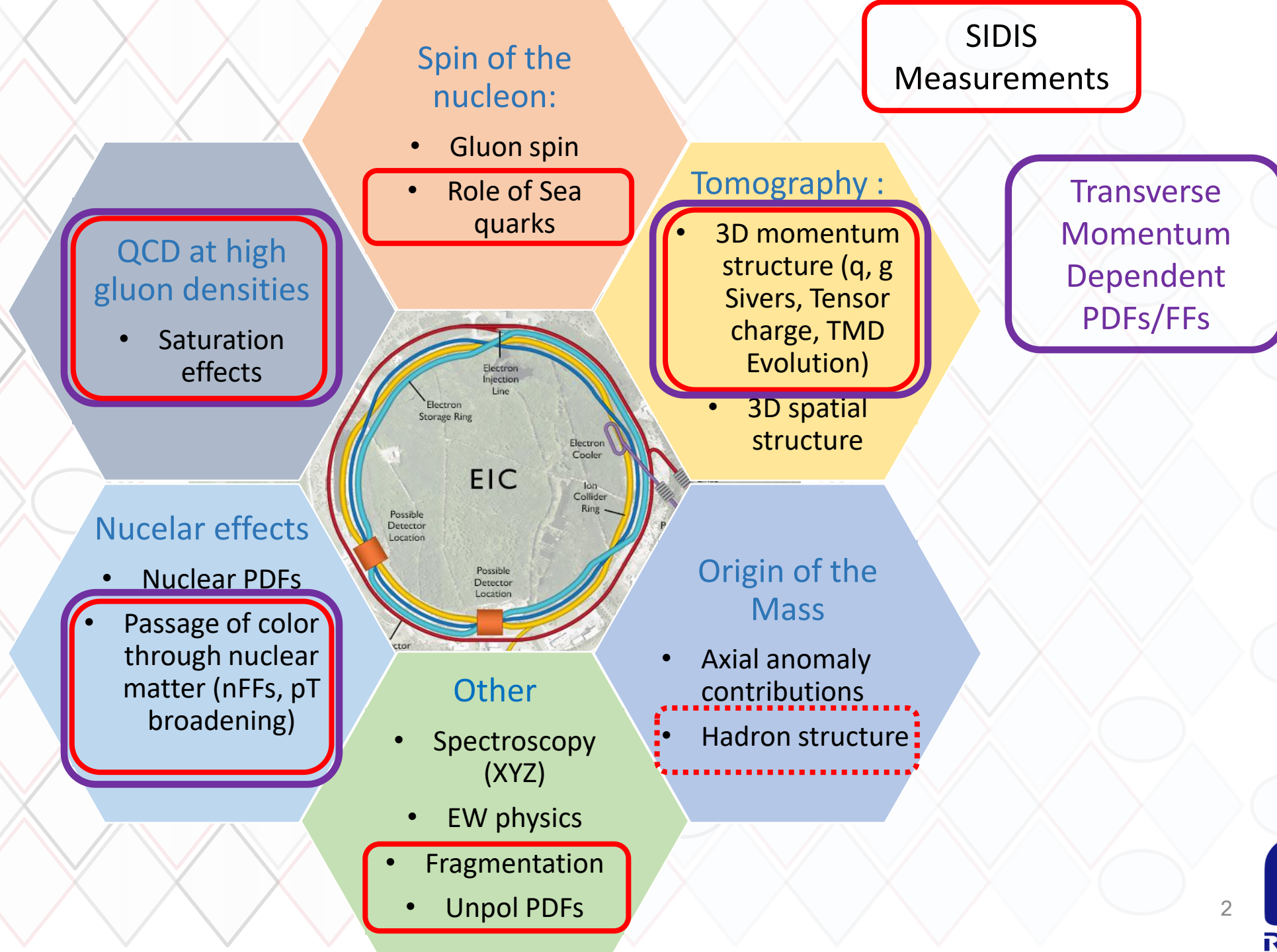


TMDs at the **Electron Ion Collider**

**2nd IR workshop,
December 8, 2022,
Ralf Seidl (RIKEN)**



What can the second IR help with?

- Cross checks – different systematics on
 - Spin orientation and Luminosity accounting?
 - Main DIS kinematics (different detector systems provide different uncertainties on scattered electron kinematics and full hadronic final state)
 - DIS kinematics also required for correct boosts to hadron frame
 - already the y dependent prefactors on various TMD terms
 - Similar for SIDIS kinematics, especially TMD related variables (transverse momentum, azimuthal angles, z)
 - Particle identification, esp. limited at low momentum (TOF range), but also at higher momenta relevant (different RICH options?)
- Secondary focusing can improve spectator proton detection in D and ^3He collisions → neutron PDFs/TMDs?

Transverse Spin

- Transversity

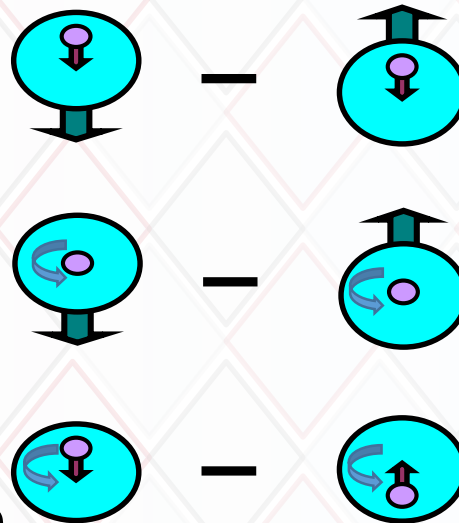
$$h_{1,q}(x)$$

- Sivers Function

$$f_{1T,q}^\perp(x, k_T)$$

- Boer Mulders function

$$h_{1T,q}^\perp(x, k_T)$$



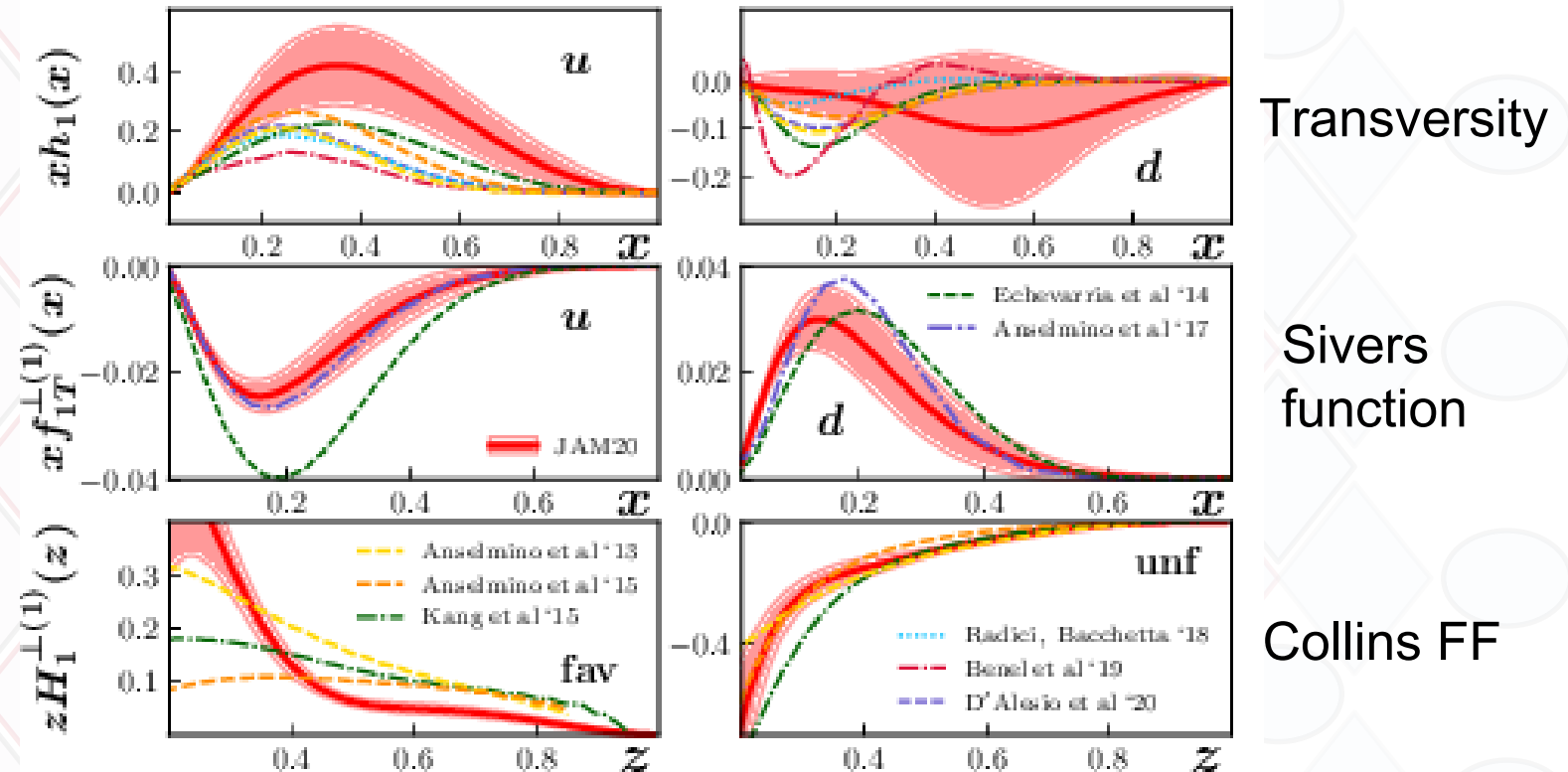
		Quark polarization		
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \odot$		$h_1^\perp = \uparrow - \downarrow$
	L		$g_1 = \rightarrow - \leftarrow$	$h_{1L}^\perp = \rightarrow - \leftarrow$
	T	$f_{1T}^\perp = \uparrow - \downarrow$	$g_{1T} = \rightarrow - \leftarrow$	$h_1 = \uparrow - \downarrow$ $h_{1T}^\perp = \rightarrow - \leftarrow$

Closely related:

- Higher Twist correlations (TMD moments) $T_F(x, x)$
- TMD FFs (Collins, polarizing FFs, etc) $H_{1,q}^{\perp(1)}(z)$

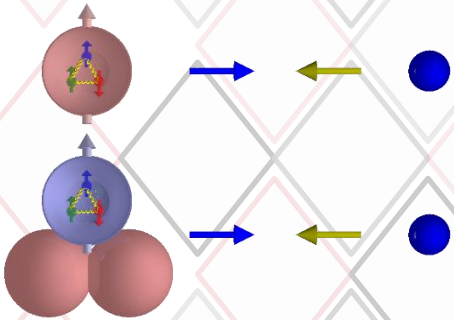
Current knowledge on these functions

- Only valence quark
Sivers and Transversity functions known at this time with substantial uncertainties
- Experimentally covered range $0.01 < x < 0.3$
- So far no sensitivity to sea quarks and gluons* and lower x

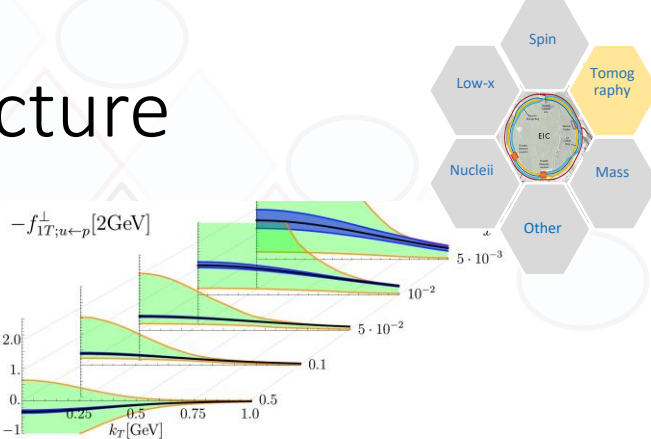


[Camarota et al, PRD 102 \(2020\) 054002](#)

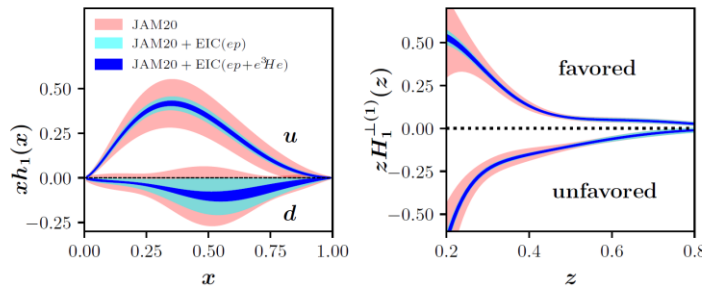
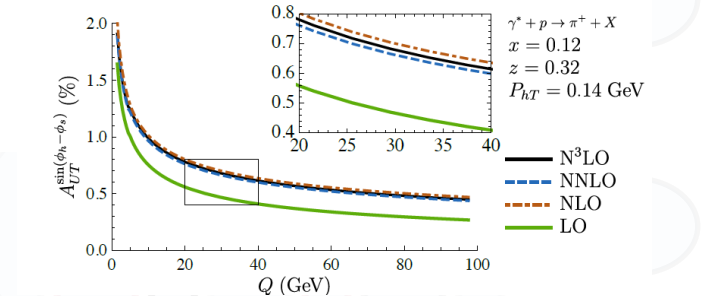
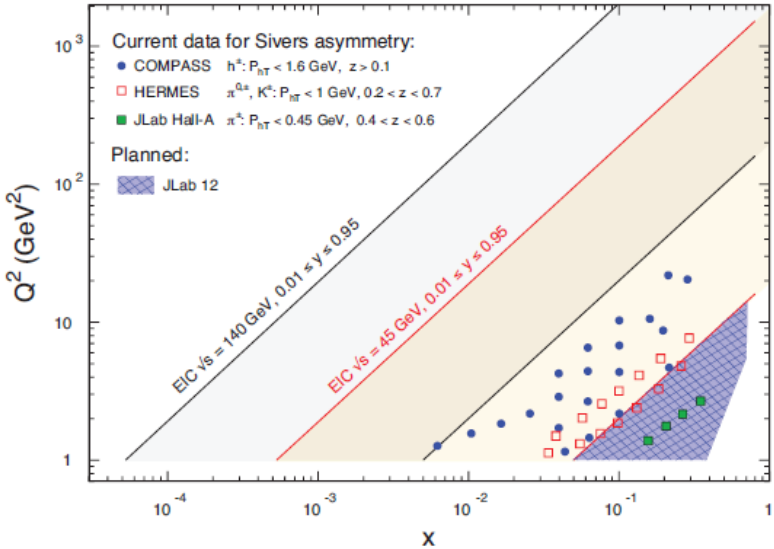
Motivation: 3D Transverse spin and momentum structure



Deliverables	Observables	What we learn	Stage I	Stage II
Sivers & unpolarized TMD quarks and gluon	SIDIS with Transverse polarization; di-hadron (di-jet)	Quantum Interference & Spin-Orbital correlations	3D Imaging of quarks valence+sea	3D Imaging of quarks & gluon; Q^2 (P_{hT}) range QCD dynamics
Chiral-odd functions: Transversity; Boer-Mulders	SIDIS with Transverse polarization	3 rd basic quark PDF; novel hadronization effects	valence+sea quarks	Q^2 (P_{hT}) range for detailed QCD dynamics



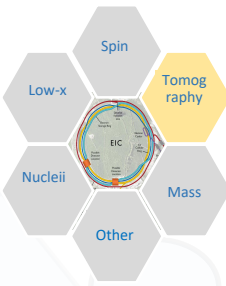
Tables from original EIC white paper



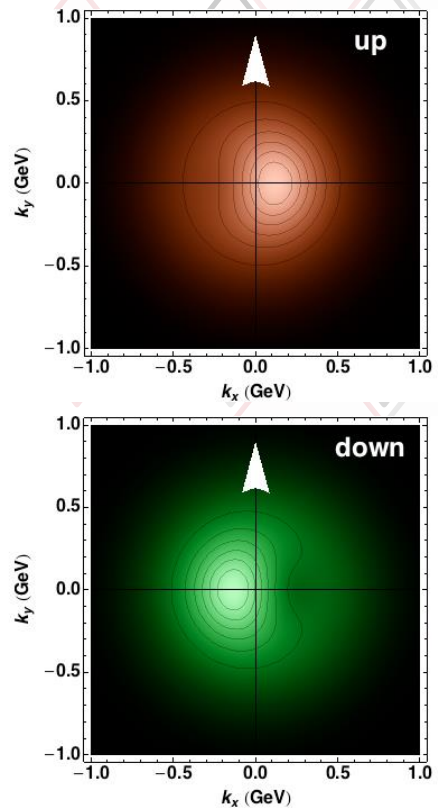
Current coverage for transverse spin related measurements

Seidl: EIC TMDs

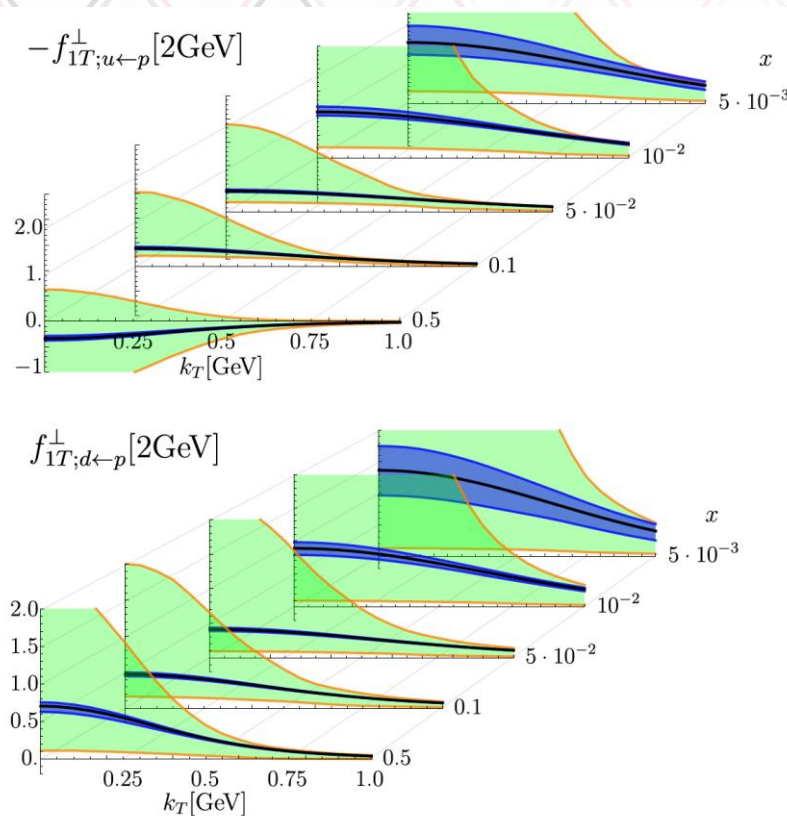
EIC impact for Sivers Functions



Transverse momentum imbalance of unpolarized partons in a transversely polarized nucleon \leftrightarrow model dependent relation to orbital angular momentum

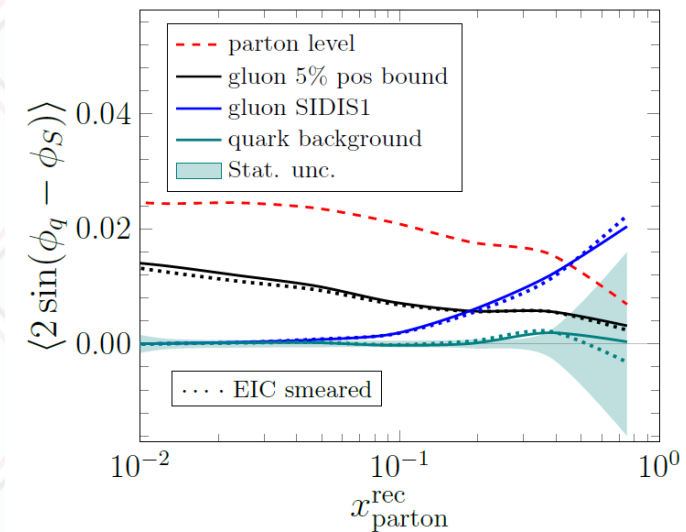


Bacchetta, Radici,
PRL 107 (2011) 212001



[YR](#): Fig 7.53
Vladimirov, et al

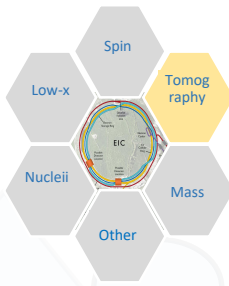
- Precise nucleon image in momentum space for quarks, sea-quarks and gluons



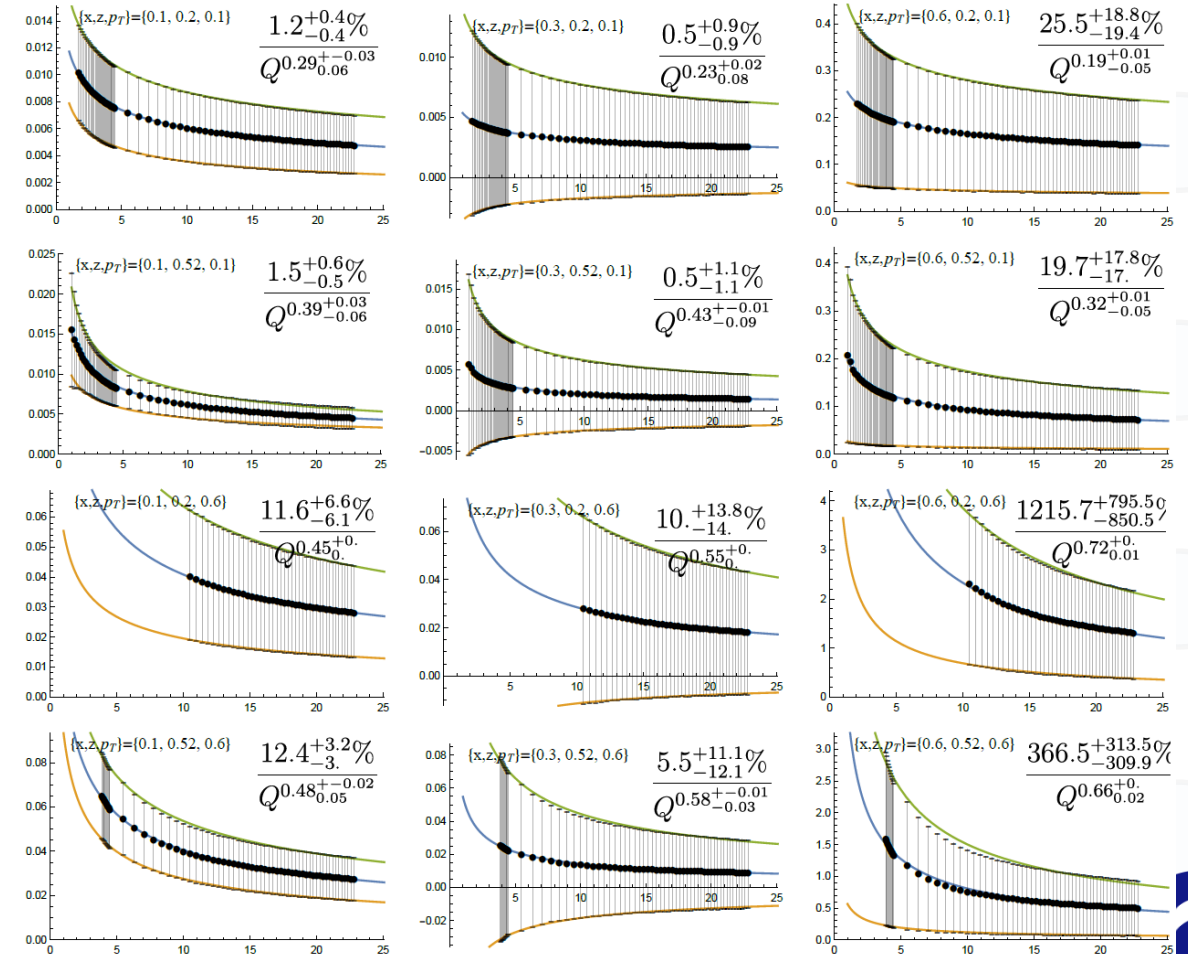
[YR](#) Fig 7.55
Xiao, et al

EIC access to TMD evolution

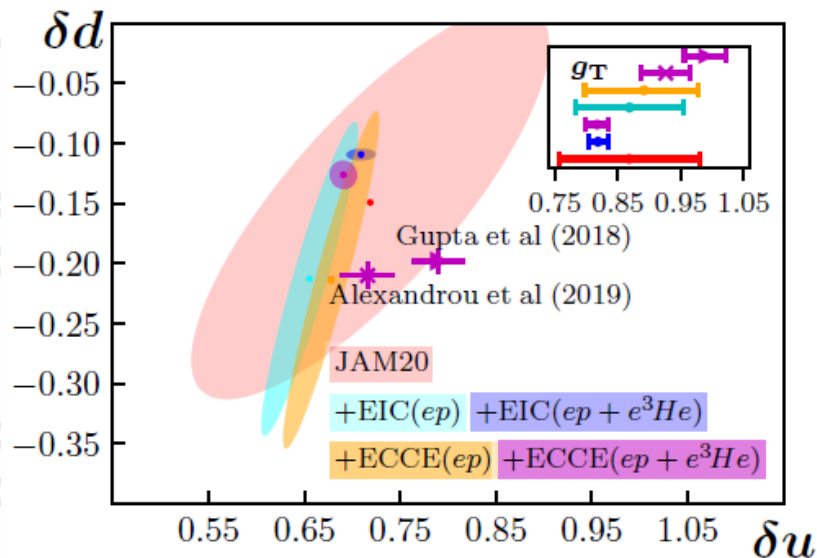
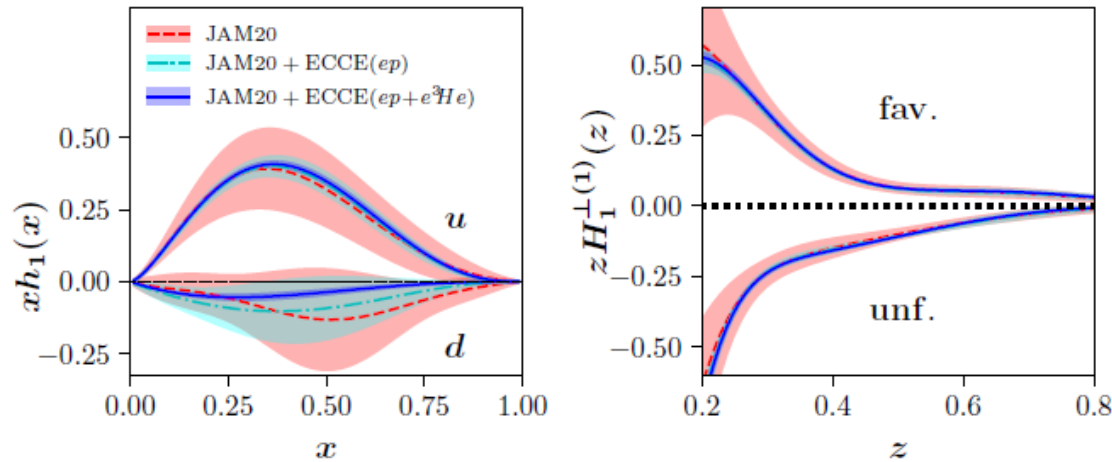
- Very important aspect is the study of TMD evolution
- Sivers asymmetries are expected to decrease at higher scales, but only logarithmically (ie they do NOT “disappear”)
- At higher x Asymmetries of several % expected
 - ➔ Well accessible with EIC over wide range in x and Q^2
 - ➔ Lower x to study sea and glue (both mostly unknown)



Vladimirov et al.



Tensor charges



hep-ex:2207.10890

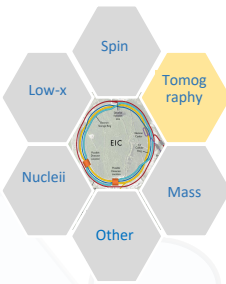
Neutron measurements

- Precise determination of tensor charges via Collins and di-hadron channels
- Better precision than lattice → potential access to BSM physics in case of discrepancies
- Preform full integrals, study role of sea quark transversity

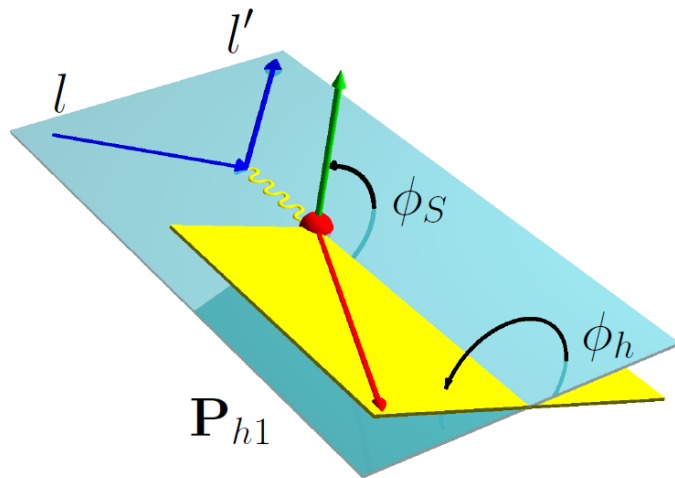
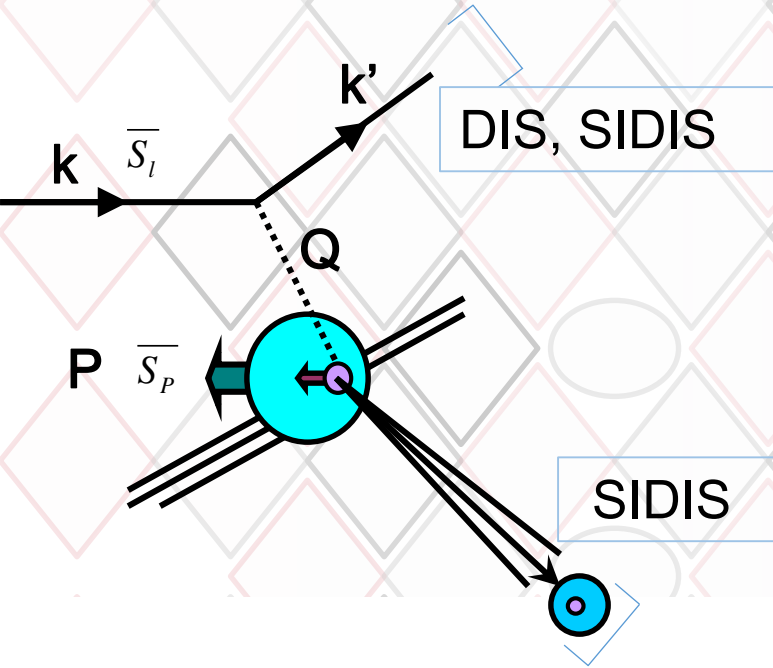
Similarly:

Single hadron channel ([YR](#) : Fig 7.54 [Gamberg et al Phys.Lett.B 816 \(2021\) 136255](#))

Di-hadron channel ([YR](#) : Fig 7.56, Radici)



SIDIS Kinematics



Detect also final-state hadron(s): Additional benefit of **flavor, spin and transverse momentum sensitivity** via Fragmentation functions

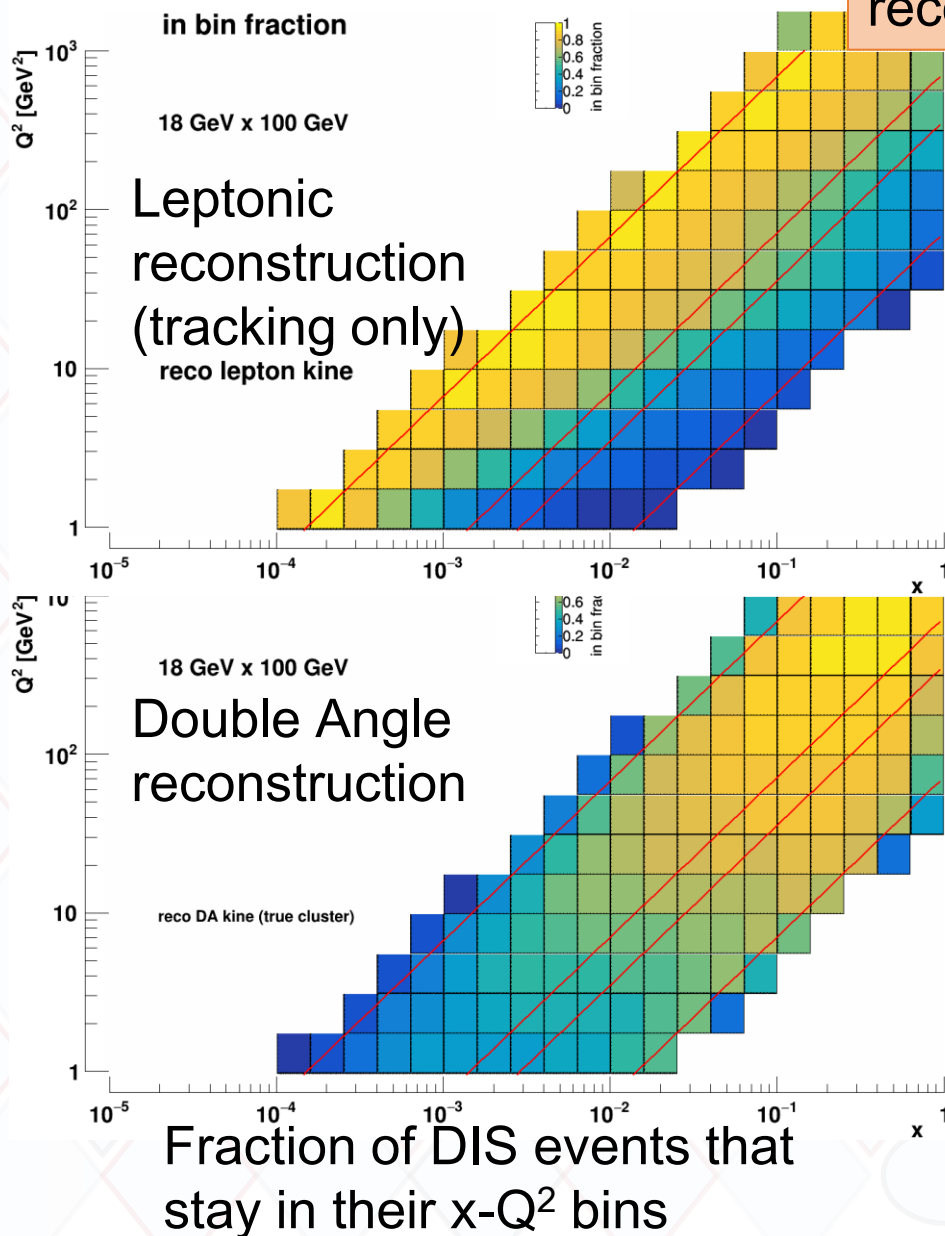
$$\frac{d^6\sigma}{dx dQ^2 dz dP_{hT} d\phi_S d\phi_h} \stackrel{LO}{\propto} \sum_{q, \bar{q}} e_q^2 q(x, Q^2, k_t) \otimes D_{1,q}^h(z, Q^2, p_t)$$

z :	Fractional hadron momentum wrt to parton momentum ($0 < z < 1$)
P_{hT} :	transverse hadron momentum wrt to virtual photon (convolution over intrinsic transverse momenta of PDFs and FFs)
ϕ_S :	Azimuthal angle of nucleon (transverse) spin wrt to scattering plane, along virtual photon axis
ϕ_h :	Azimuthal angle of hadron wrt to scattering plane, along virtual photon axis

- Current fragmentation: related to struck quark (favored fragmentation $u \rightarrow \pi^+$, $d \rightarrow \pi^-$, $s \rightarrow K^-$, etc)
- Transverse momentum and angles rely also on correct boost to hadron rest system

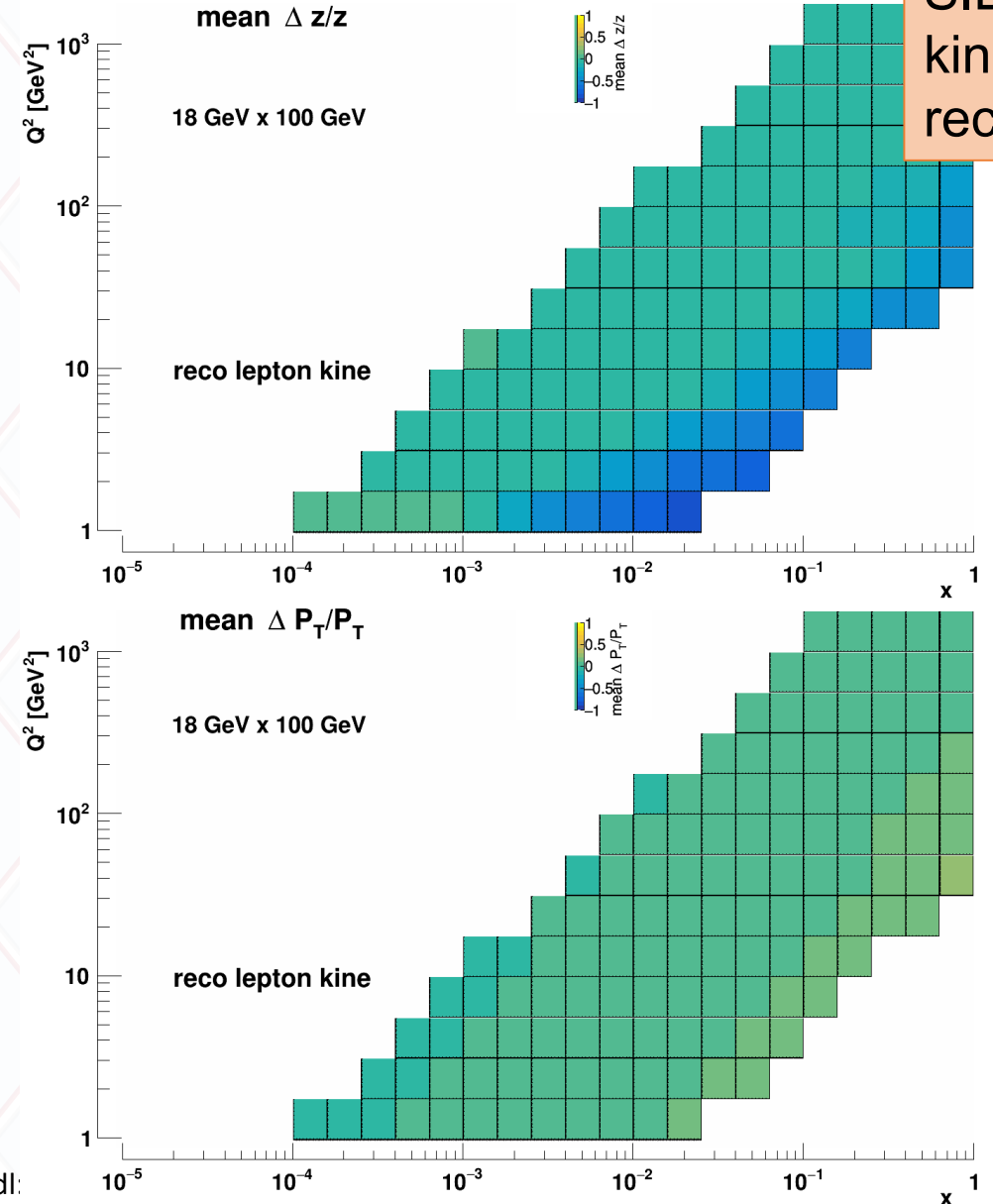
PID reconstruction

- Full Pythia6+GEANT simulations of the ECCE detector used for various (SI)DIS kinematic resolutions and for various reconstruction methods (lepton, Jaquet-Blondel, Double Angle, etc)
- x and y resolutions suffer from lepton method at lower y, partially recoverable in double angle method (hybrid of scattered lepton + hadronic final state)



Example of SIDIS resolutions studies

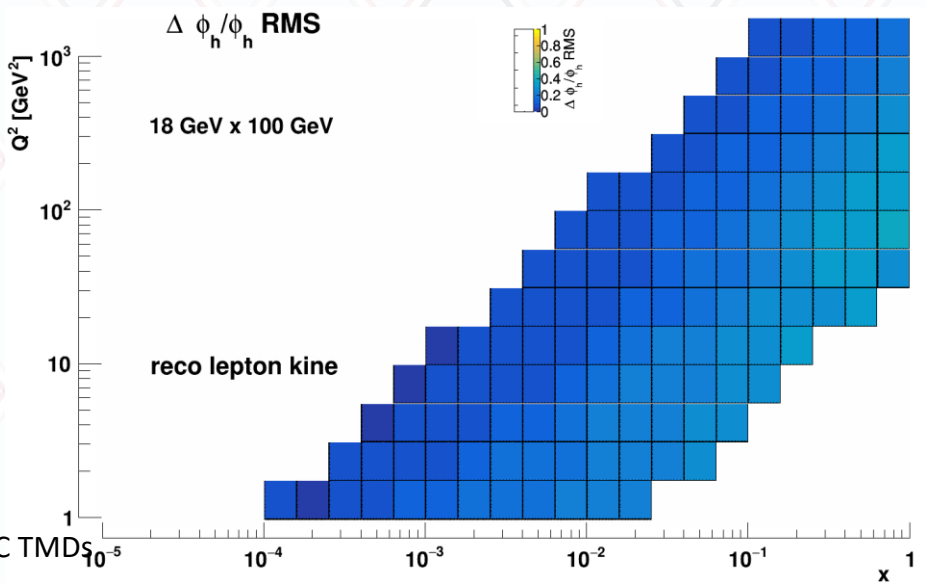
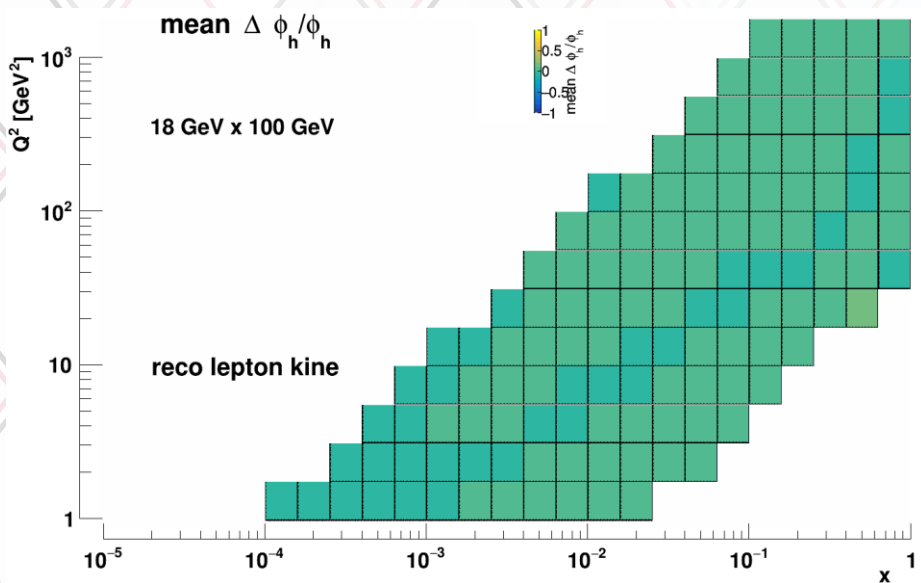
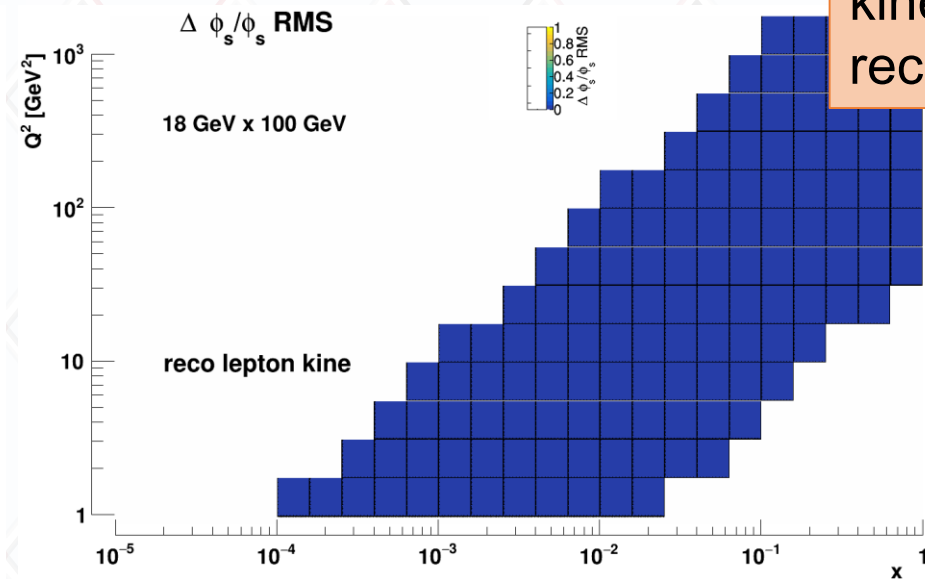
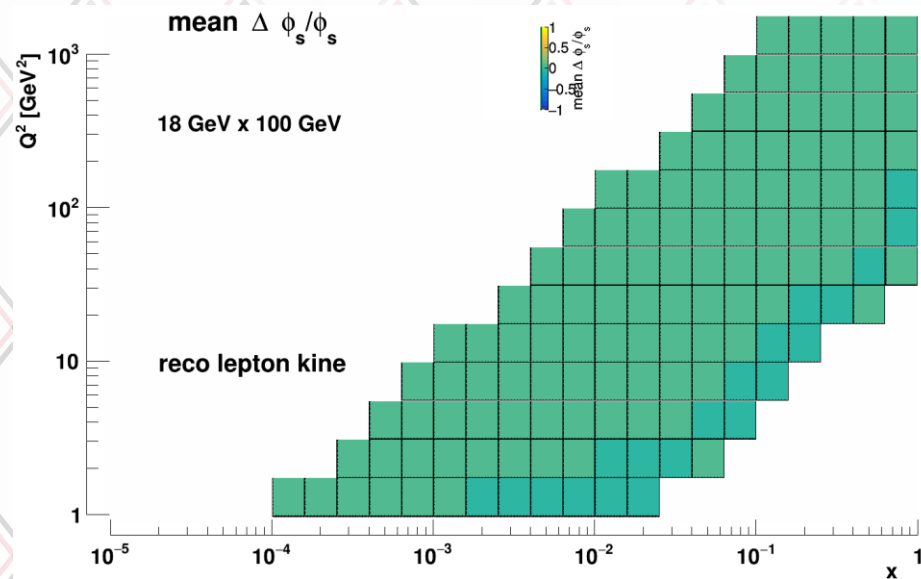
- Full Pythia6+GEANT simulations of the ECCE detector for various (SI)DIS kinematic resolution and reconstruction methods:
 - z resolution suffers in lepton method at lower y , partially recoverable in double angle method
 - p_T and azimuthal angles ϕ_h , ϕ_s very robust



SIDIS
kinematic
reconstruction

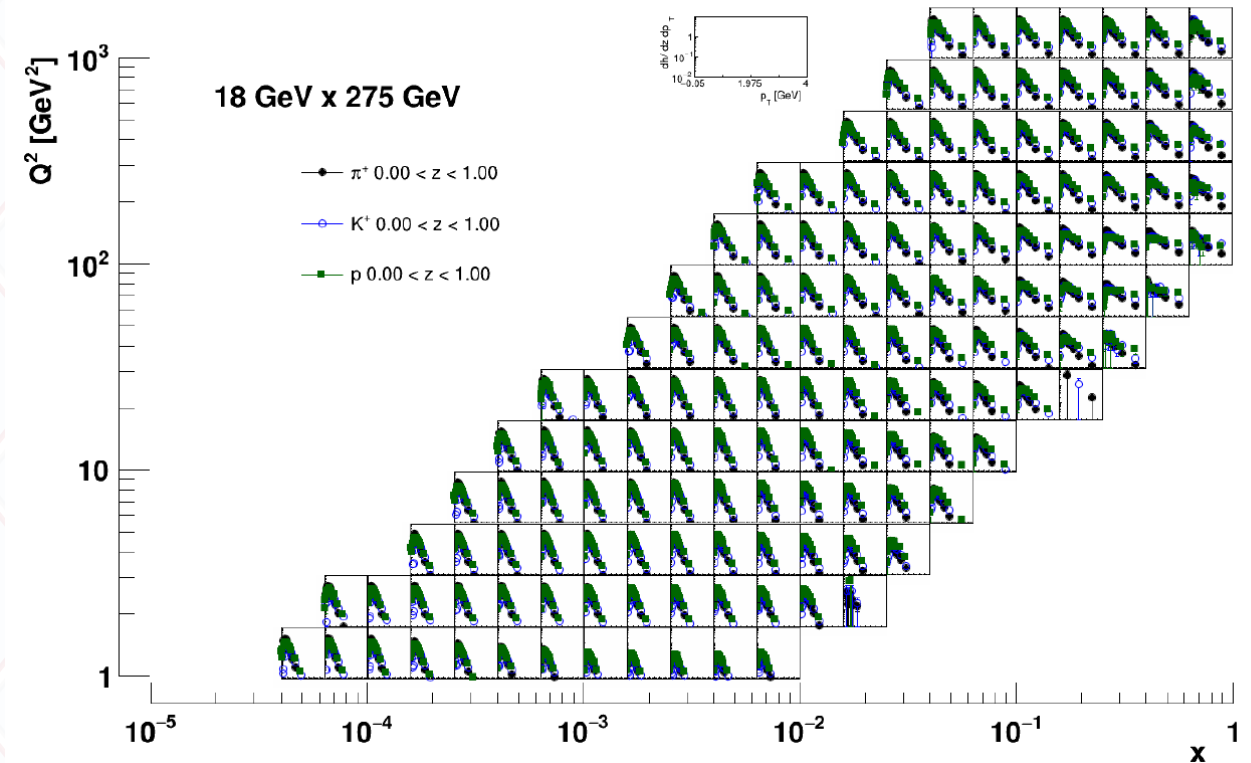
Azimuthal angles

SIDIS
kinematic
reconstruction



ECCE simulation setup, unpolarized TMD studies

- pythiaRHIC (Pythia 6) simulations for e+p collisions at 4 energies similar to YR
- Generator output simulated through GEANT4
- Scattered lepton ($|\eta| < 3.5$) DIS kinematic reconstruction using reco track momenta (assuming perfect eID)
- DIS cuts: $0.01 < y < 0.95$, $Q^2 > 1$, $W^2 > 10 \text{ GeV}^2$
- SIDIS cuts: pions and kaons ($|\eta| < 3.5$), using true PID (assuming successful unfolding)
- $25 \times 13 \times 12 \times 12$ kinematic bins (x, Q^2, z, P_T)
- Pion, kaon and proton multiplicities shown in all x - Q^2 bins as a function of P_T (integrated over z)

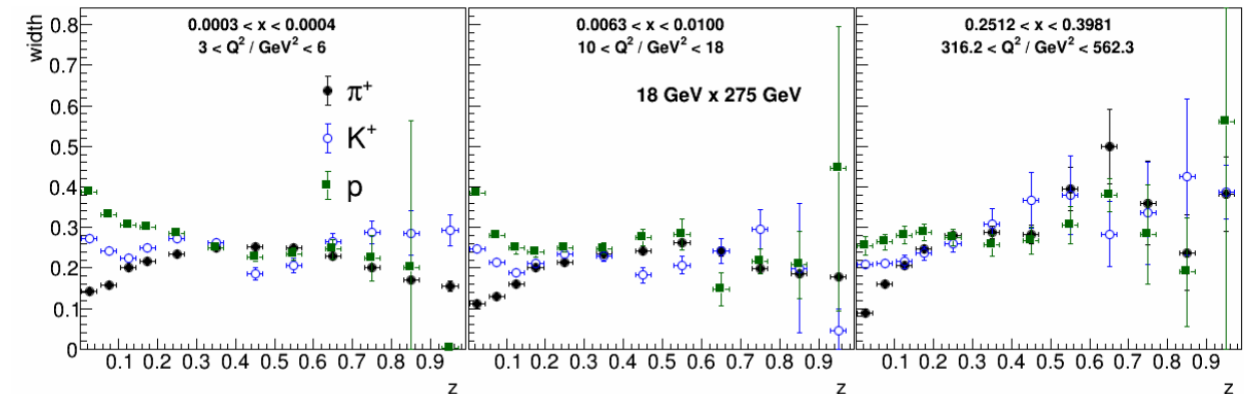
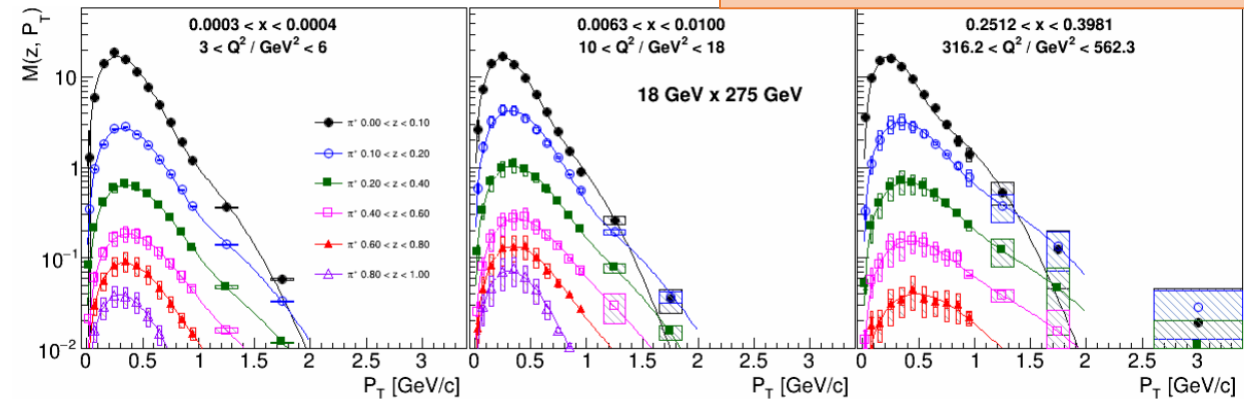


[hep-ex:2207.10893](https://arxiv.org/abs/hep-ex/2207.10893)

z-dependence of multiplicities and widths

z, Pt smearing →
unfolded uncertainties

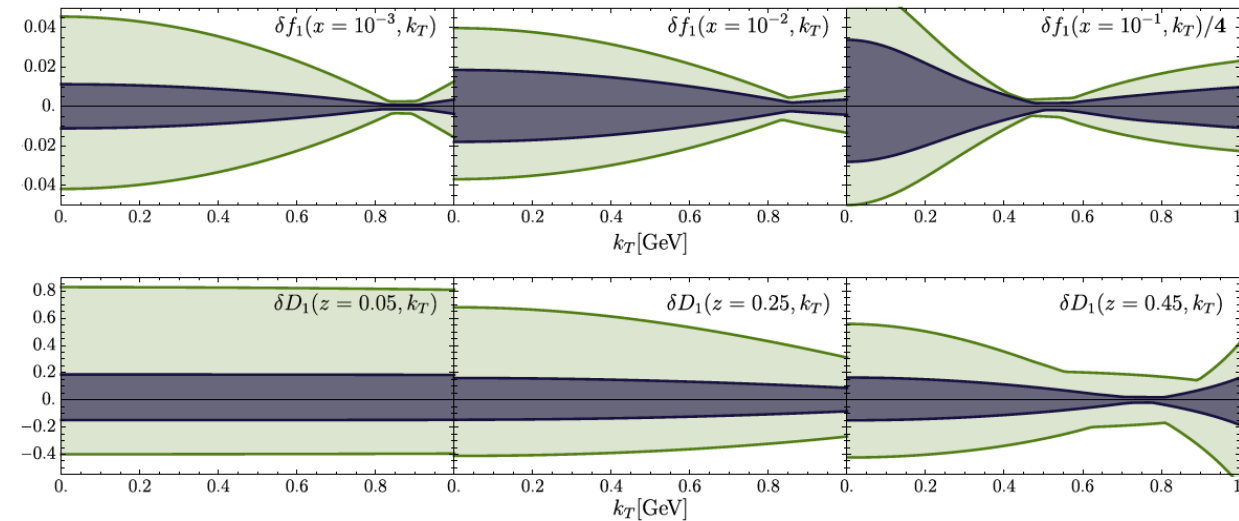
- Top: Explicit z dependence of select pion multiplicities in 3 x- Q^2 bins, including the double-Gaussian fits
- Bottom: behavior of the narrow Gaussian widths vs z for pions, kaons and protons
- Small z discrepancies likely due to target fragmentation



[hep-ex:2207.10893](https://arxiv.org/abs/hep-ex/2207.10893)

Impact for unpolarized TMD functions

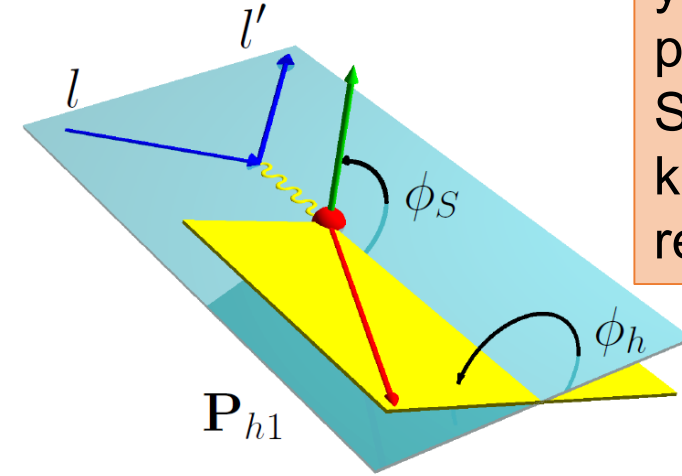
- Similar to YR impact studies following the latest SV global fit (<https://arxiv.org/abs/1912.06532>) for the unpolarized TMDs based on the existing SIDIS +DY data
- Consistent with Yellow Report expected impact



[hep-ex:2207.10893](https://arxiv.org/abs/hep-ex/2207.10893)

Experimental access to Transversity/tensor charge and Sivers function

- Both functions are accessible as different azimuthal modulations in transversely polarized SIDIS of single hadrons
- Reweight events according to true parton flavor q , hadron h , x , z , Q^2 , P_{hT} , azimuthal angles and random spin orientation
- Input structure functions (polarized and unpolarized) from Torino global fits (arXiv:0812.4366, arXiv:0805.2677) as in <https://github.com/prokudin/tmd-parametrizations/>
- Other TMD PDFs are similarly accessible via different modulations and spin orientations (though often higher twist effects present)
- Gluon Sivers via di-jet/di-HF TSSAs



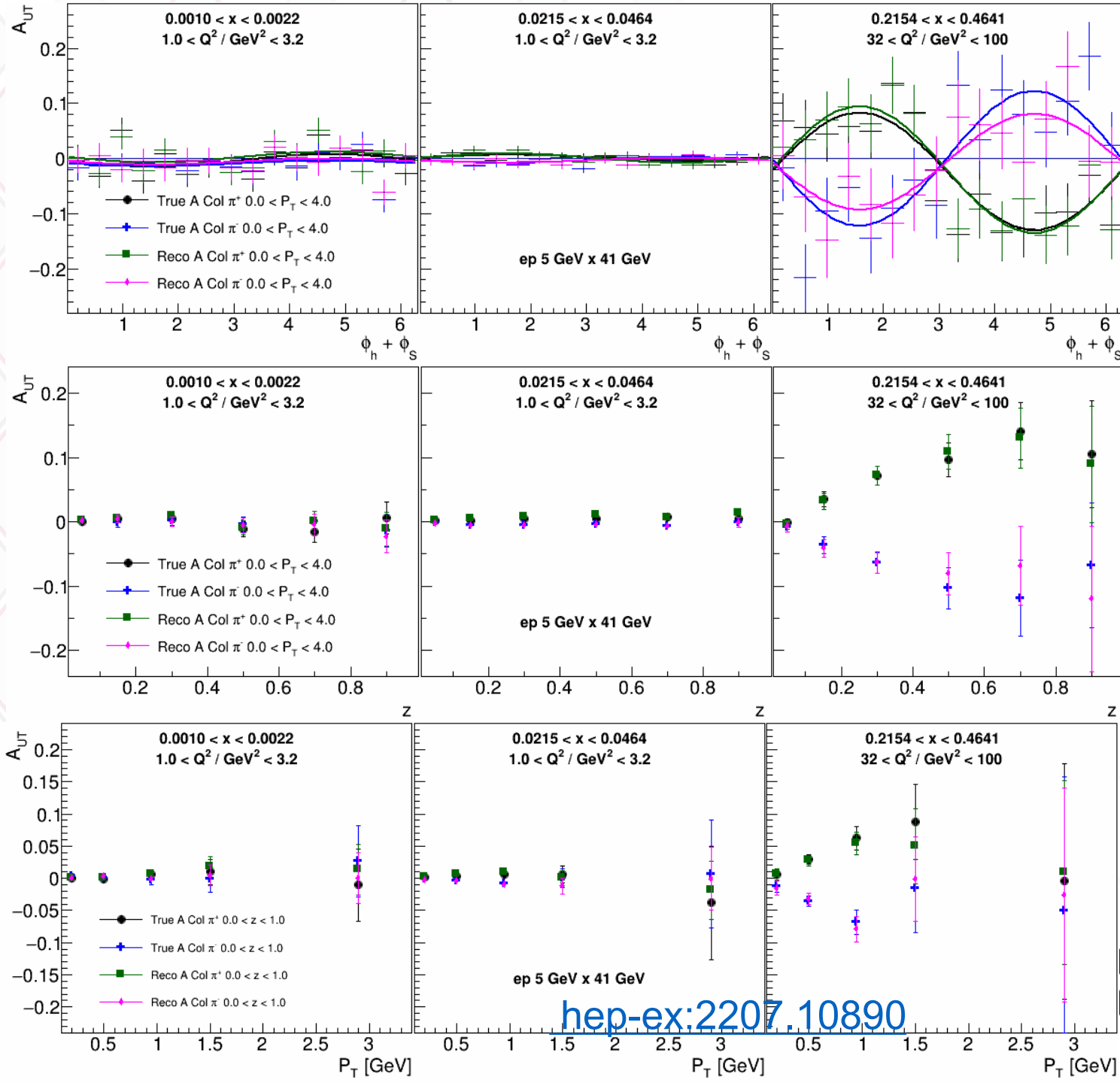
y dependent
prefactors,
SIDIS
kinematic
reconstruction

$$A_{UT}^{\sin(\phi_h + \phi_S)}(x, z, P_T) \propto \mathbf{S}_T \frac{\sum_{q, \bar{q}} e_q^2 \delta q(x, k_t) \otimes H_1^\perp(z, p_t)}{\sum_{q, \bar{q}} e_q^2 q(x, k_t) \otimes D_1(z, p_t)}$$

$$A_{UT}^{\sin(\phi_h - \phi_S)}(x, z, P_T) \propto \mathbf{S}_T \frac{\sum_{q, \bar{q}} e_q^2 f_{1T}^{\perp, q}(x, k_t) \otimes D_1(z, p_t)}{\sum_{q, \bar{q}} e_q^2 q(x, k_t) \otimes D_1(z, p_t)}$$

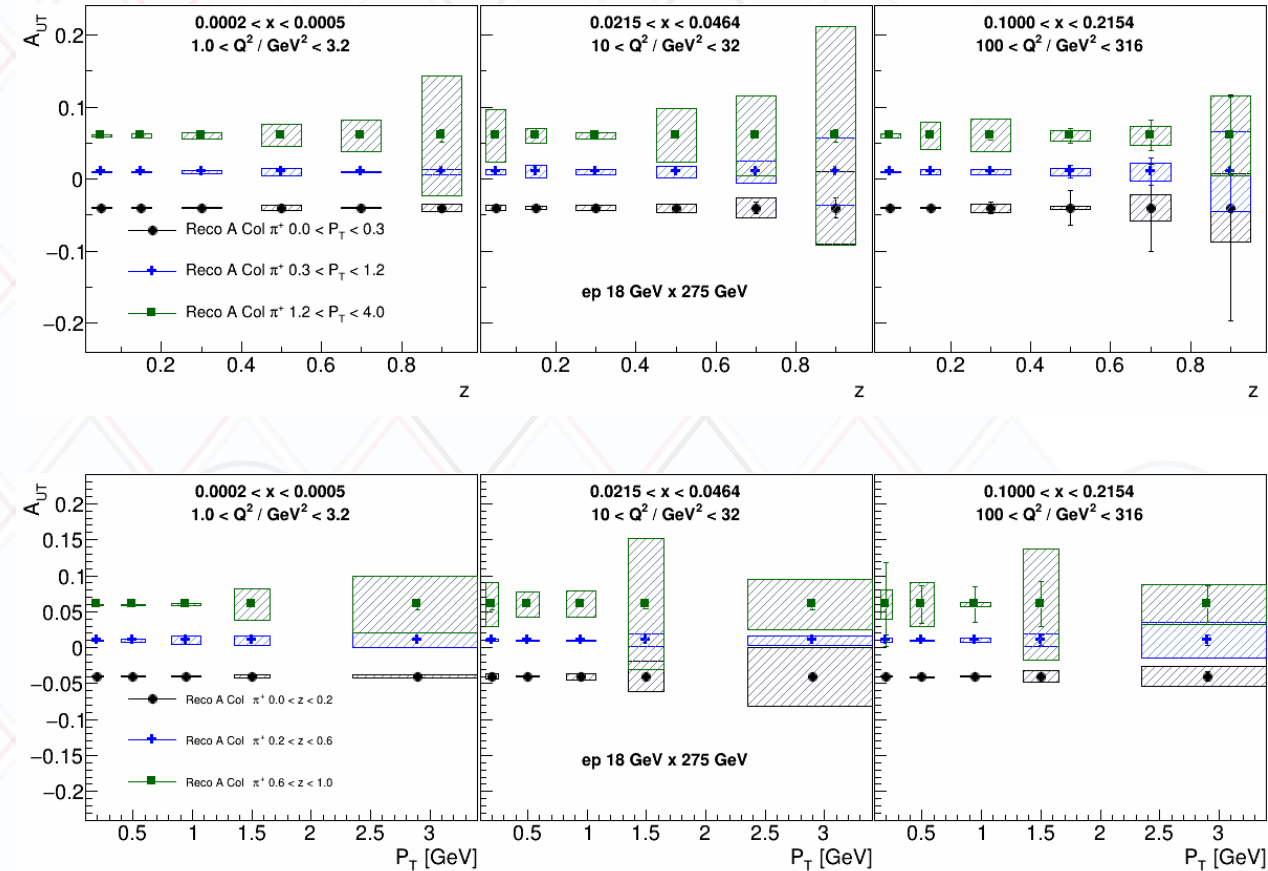
Example Asymmetries

- Examples in 3 x and Q^2 bins: on top for the Collins angular combination for charged pions true and reconstructed in an intermediate z bin
- Lower figures: same, either projected vs z or vs P_T



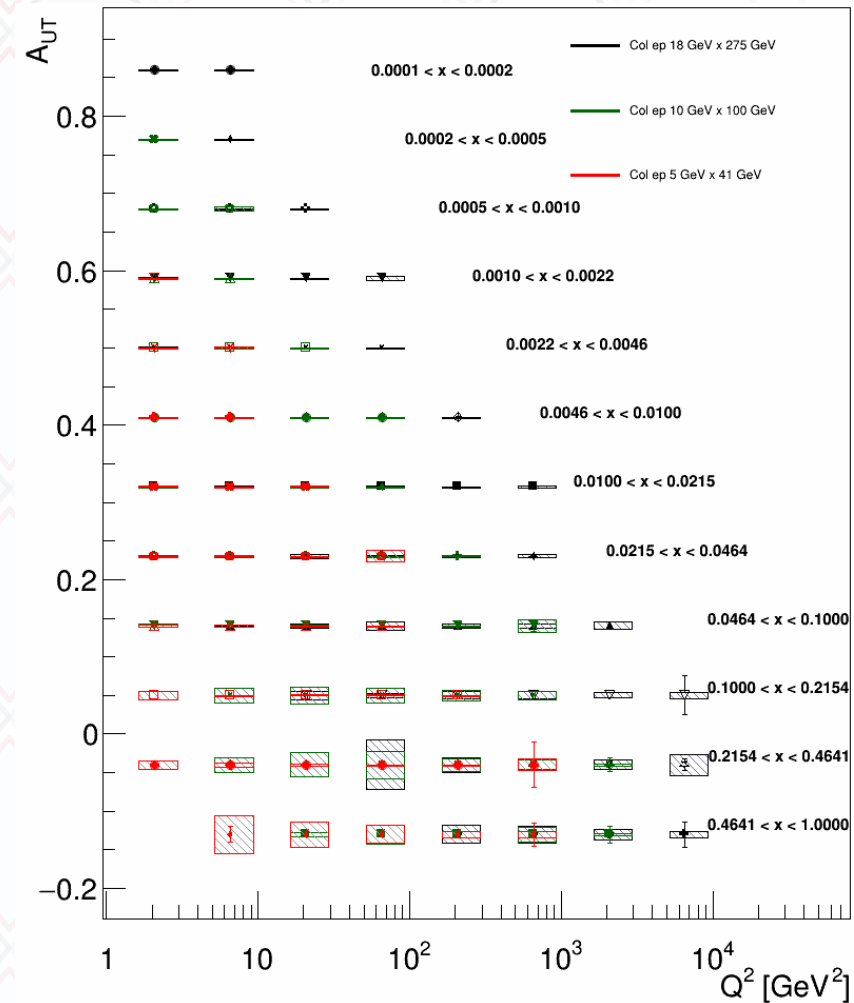
Projections to 10fb^{-1}

- Systematic uncertainties estimated from differences between true and reconstructed asymmetries \rightarrow they are likely largely overestimated since most of the kinematic smearing would be unfolded, but give a sense of where uncertainties still might be larger due to that unfolding



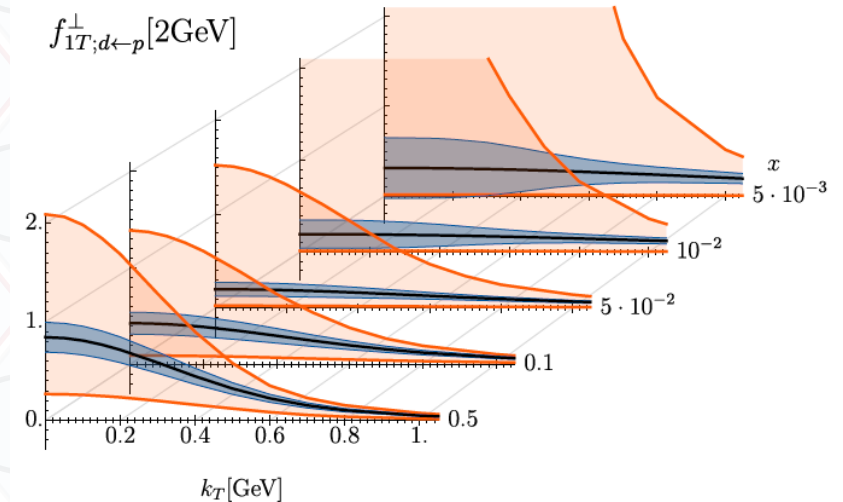
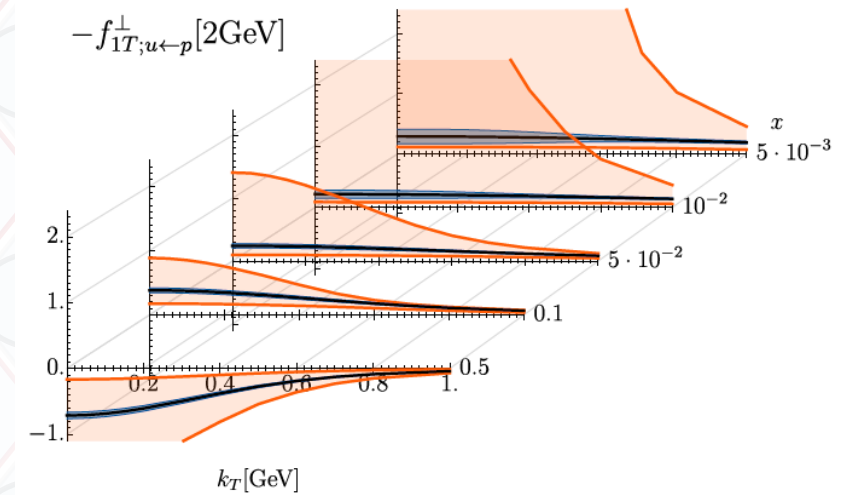
Scale dependence (and interplay of collision energies)

- An example of the expected uncertainties in x and Q^2 to study the scale dependence of the Sivers/Collins asymmetries (as TMD evolution is not very well known/contains other nonperturbative pieces)
- Overlap of the different energies shows how they increase the lever arm
- Note: in future evolution analysis likely more Q^2 bins and maybe not as fine x binning



Impact for Sivers functions

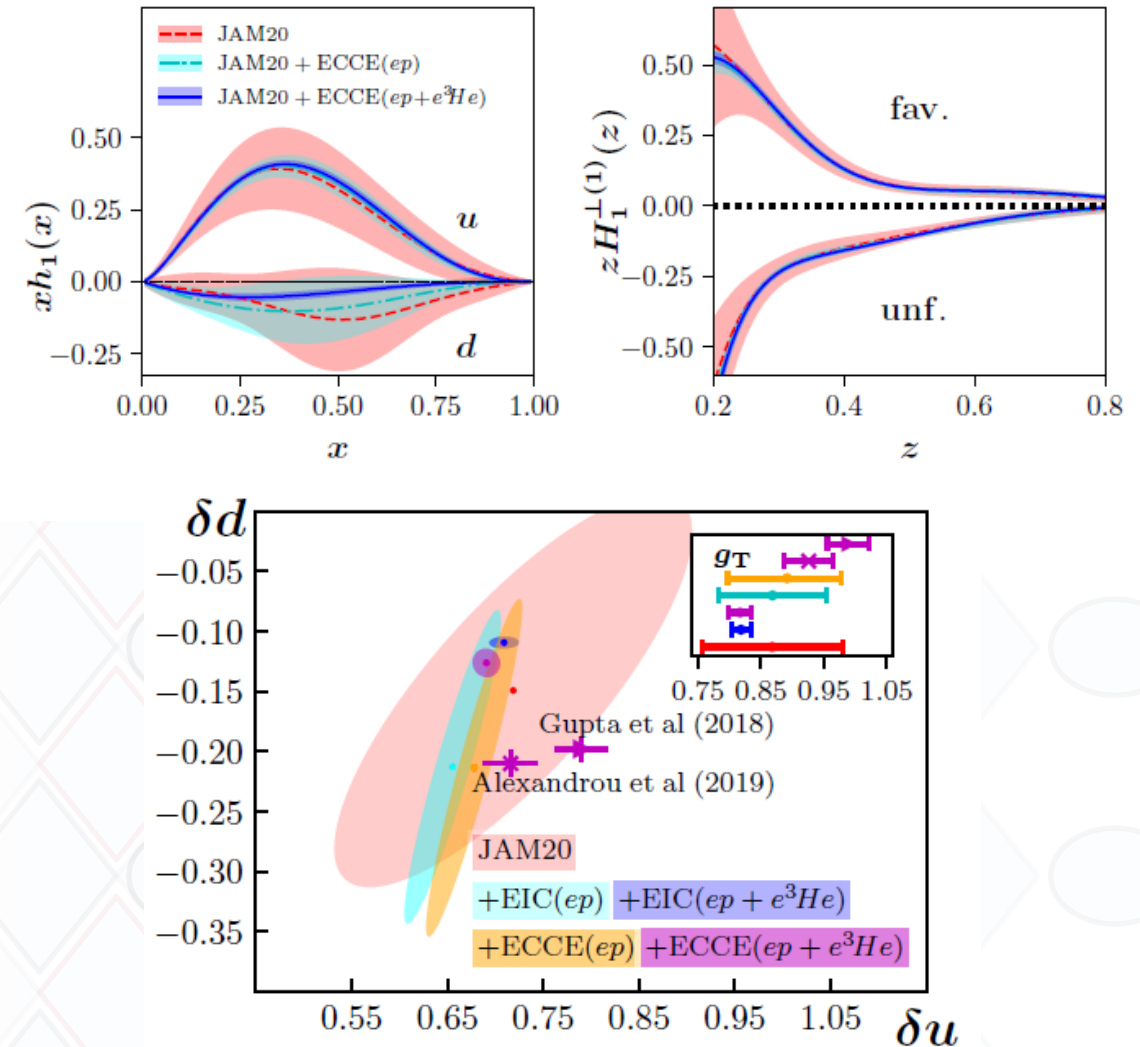
- Similar to YR impact studies following the latest BPV global fit (arXiv:2103.03270) for the Sivers function based on the existing SIDIS +DY data
- Uncertainties are shown for current level of knowledge on up/down Sivers functions at various x vs k_T and expected impact from ECCE



[hep-ex:2207.10890](https://arxiv.org/abs/hep-ex/2207.10890)

Tensor charge impact

- Similar to [Gamberg et al Phys.Lett.B 816 \(2021\) 136255](#) (for YR) use fitting code from latest global fit Cammarota et al arXiv:2002.08384 to extract impact on Transversity, Collins functions and tensor charges
- Together with projected JLAB12 data precision to compare with Lattice results (and check for possible discrepancies)



Summary

- TMDs provide valuable input on the 3D momentum picture of the nucleon
- Closely related spin-spin (Transversity) and spin-orbit (Sivers function, Boer-Mulders function) effects
- Tensor charge as potential probe for BSM effects
- Full Geant studies show that ECCE/ePIC successfully addresses the TMD/SIDIS measurements of the EIC Yellow Report
- Continuation of evaluation as ePIC detector evolves, impact of kinematic reconstruction methods, prepare for unfolding (PID, tracking), understand radiative corrections, etc
- A second IR detector will likely contribute much in terms of reducing the total uncertainties on all TMD measurements, similar to joint H1 and ZEUS analysis on unpolarized PDFs