

# INTT Physical Measurements

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# Goal

- Obtain the parameters for the affine transform that will put each sensor in its final position
  - Account for deviations from nominal introduced by manufacturing and assembly processes

# Procedure

The transform that puts the sensor to its final position is the same as the transformation matrix from the sensor's local coordinate system to the sPHENIX global coordinate system.

Compute the final transform as a sequence of transforms

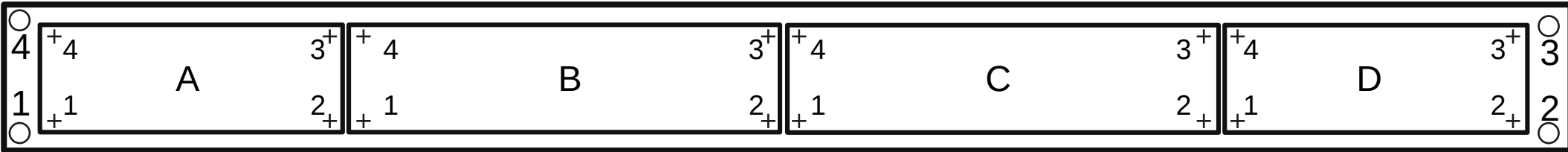
(sensor -> ladder) (ladder -> barrel) (barrel -> global)

- For each step, use survey data to find the actual values of these transforms
- Compare the actual transforms with nominal transforms for quality assurance

# Timeline

<b>Done</b> (sensor -> ladder)	<b>Next Week (Hopefully)</b> (ladder -> barrel)	<b>Final Assembly</b> (barrel -> global)
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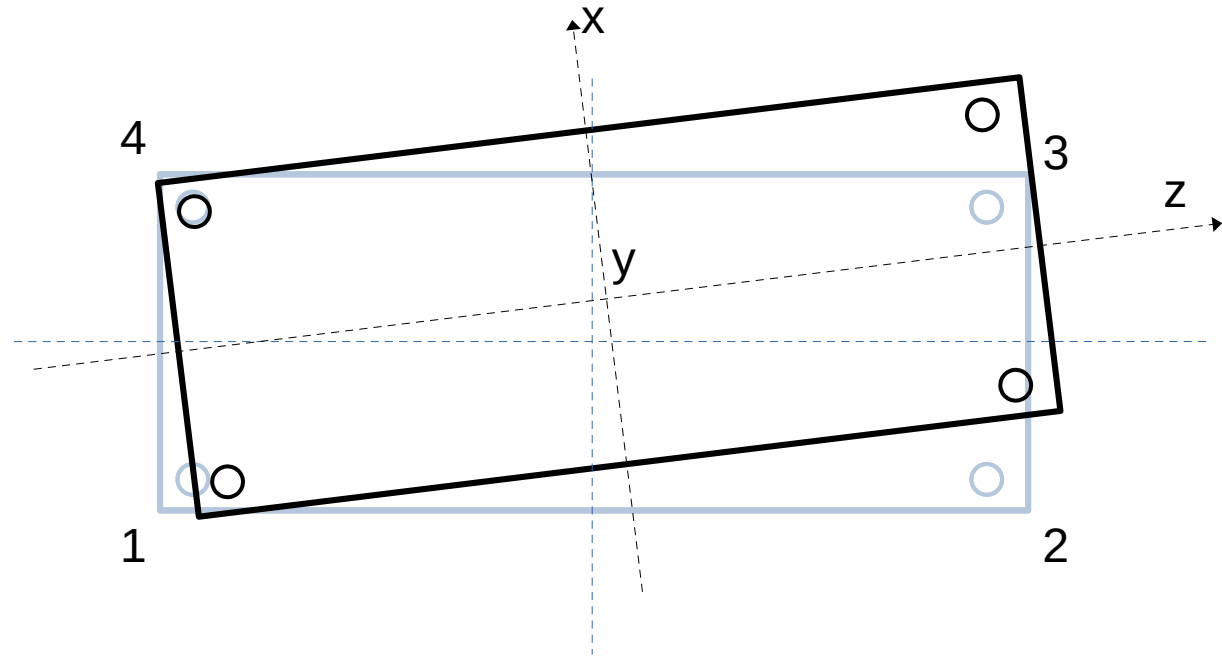
# Sensor-Ladder Transform



- 4 Holes at each corner of the ladder (1 – 4 starting low-left and going CCW)
- 4 Sensors (A – D going from -z to +z)
  - Each sensor has 4 marks (crosses) (1 – 4 starting low-left and going CCW)
- The measured positions of these points will provide the transforms of the ladder and sensors to a common, measurement frame
  - Then we know the sensor to ladder transform by knowing each one's transform to a common frame

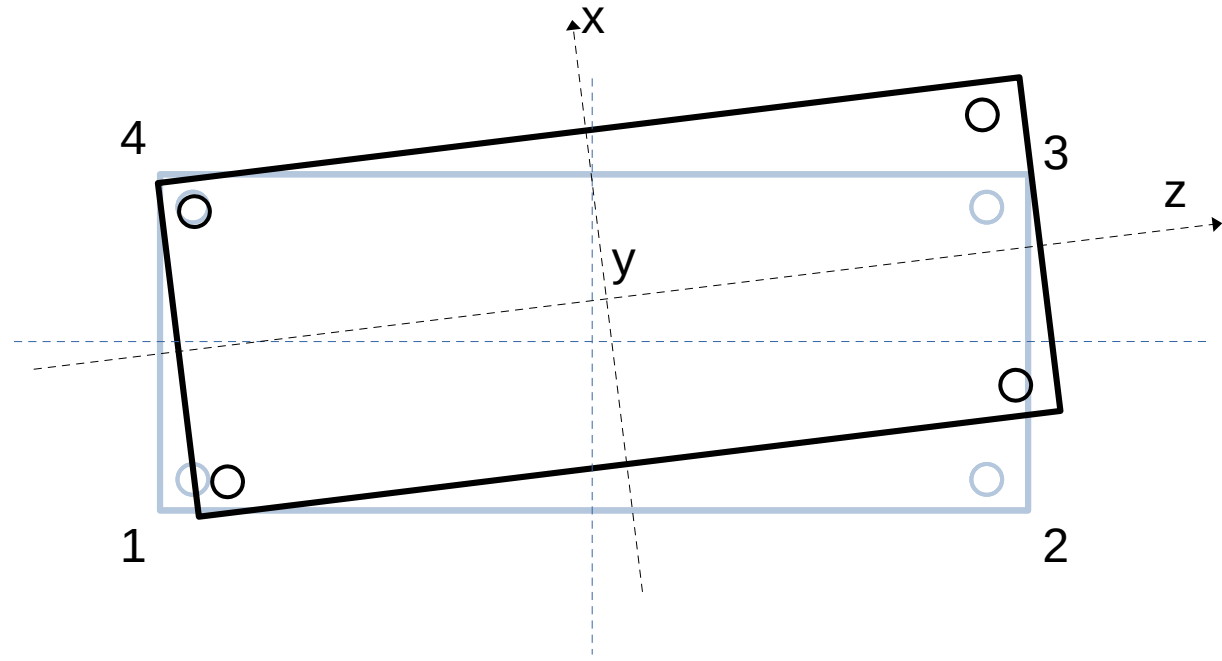
# Computing Measured Transforms

- Used diagonals to find measured coordinate system
  - $+z \parallel (u_{1 \rightarrow 3}) - (u_{2 \rightarrow 4})$
  - $+x \parallel (u_{1 \rightarrow 3}) + (u_{2 \rightarrow 4})$
  - $+y = (+z) \text{ cross } (+x)$ 
    - $(u_{i \rightarrow j})$  is a unit vector pointing from corner  $i$  to corner  $j$
- Therefore:
  - Measured coordinate axes are the columns of the 3D rotation matrix that rotates from local frame to measurement frame



# Computing Measured Transforms

- Used the average of measured corners as the measured center
- This is the translation (in the measurement frame) that should be applied after applying the rotation from previous slide
- The 4D affine transformation matrix is the rotation matrix augmented with this translation



# Transform Parameters

- The 4D affine transformation matrix has the following form:

$$\begin{bmatrix} [R] & \begin{matrix} dx \\ dy \\ dz \end{matrix} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- $dx, dy, dz$  are the Cartesian translation between coordinate system origins
- $[R]$  is the rotation matrix that transforms a vector in the child system to the parent system
- Equivalently,  $[R]$  is the rotation applied to the child system, if it started as aligned with the parent system, to achieve its final orientation



# Transform Parameters

- The 4D affine transformation matrix has the following form:

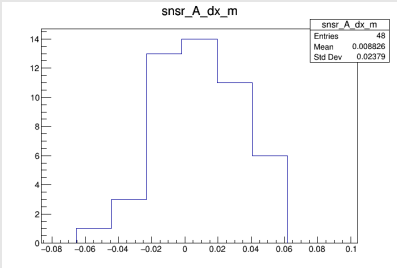
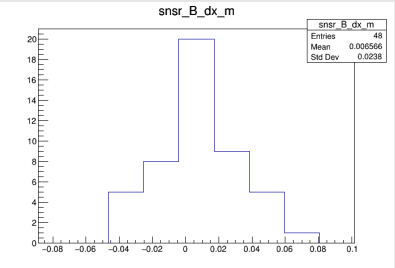
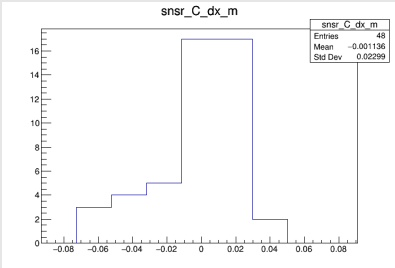
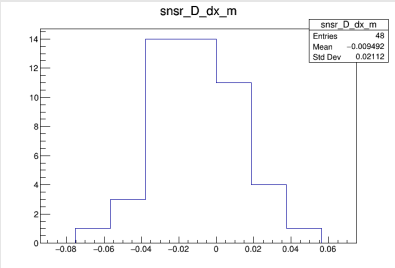
$$\begin{array}{cccc}
 & & & dx \\
 & & & dy \\
 [R] & & & dz \\
 0 & 0 & 0 & 1
 \end{array}$$

- [R] is parameterized by Tait-Bryan angles alpha, beta, gamma
- Rotate gamma about z axis
- Rotate beta about new y axis
- Rotate alpha about new x axis

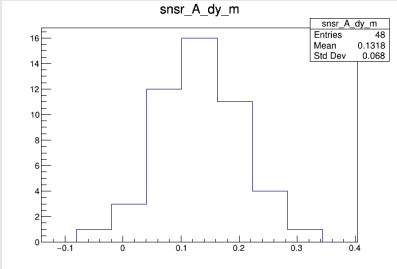
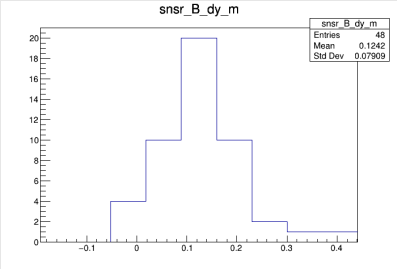
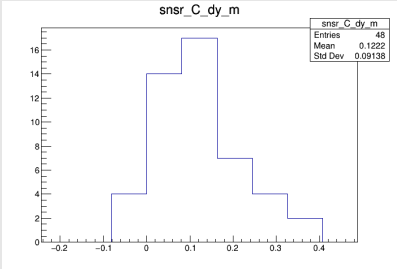
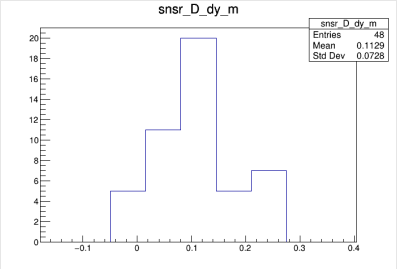
$X_1 Y_2 Z_3$	$\alpha = \arctan\left(\frac{-R_{23}}{R_{33}}\right)$ $\beta = \arctan\left(\frac{R_{13}}{\sqrt{1 - R_{13}^2}}\right)$ $\gamma = \arctan\left(\frac{-R_{12}}{R_{11}}\right)$
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[https://en.wikipedia.org/wiki/Euler\\_angles#Tait%E2%80%93Bryan\\_angles](https://en.wikipedia.org/wiki/Euler_angles#Tait%E2%80%93Bryan_angles)

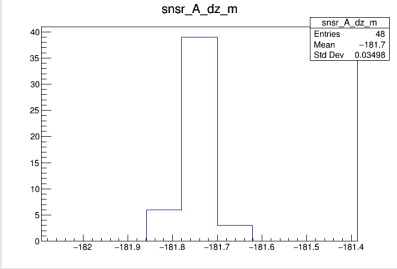
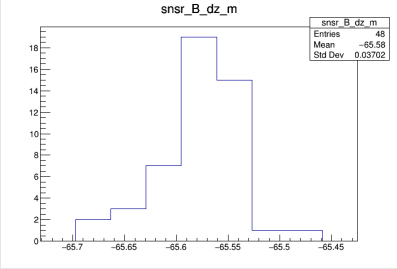
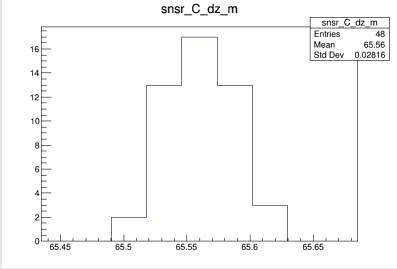
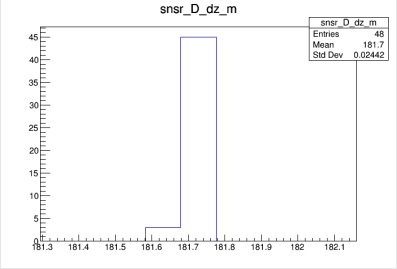
# dx Distribution

	Sensor A	Sensor B	Sensor C	Sensor D
mean (um)	8.8	6.6	-1.1	-9.5
std. dev. (um)	23.8	23.8	23.0	21.1
plot (mm)	 <p>snr_A_dx_m</p> <p>snr_A_dx_m Entries: 48 Mean: 0.00826 Std Dev: 0.02379</p>	 <p>snr_B_dx_m</p> <p>snr_B_dx_m Entries: 48 Mean: 0.00556 Std Dev: 0.0238</p>	 <p>snr_C_dx_m</p> <p>snr_C_dx_m Entries: 48 Mean: -0.00136 Std Dev: 0.02299</p>	 <p>snr_D_dx_m</p> <p>snr_D_dx_m Entries: 48 Mean: -0.00492 Std Dev: 0.02112</p>

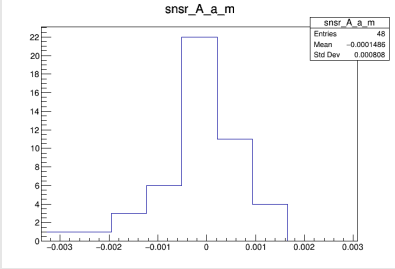
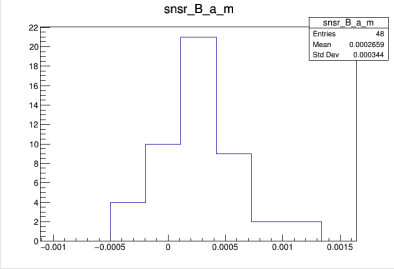
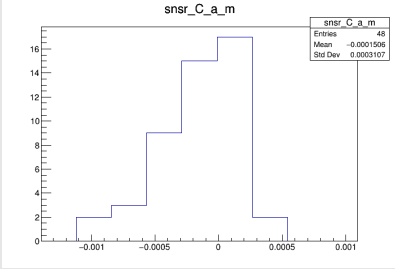
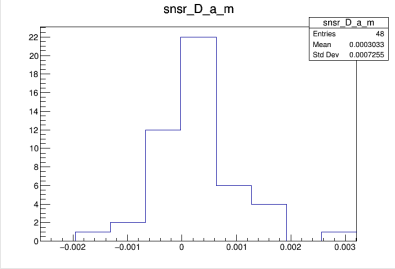
# dy Distribution

	Sensor A	Sensor B	Sensor C	Sensor D
mean (um)	131.8	124.2	122.2	112.9
std. dev. (um)	68.0	79.1	91.4	72.8
plot (mm)				

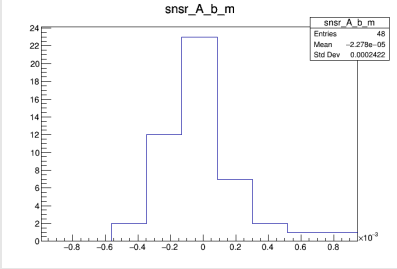
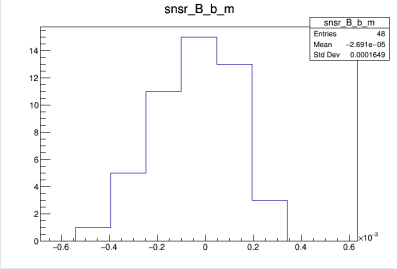
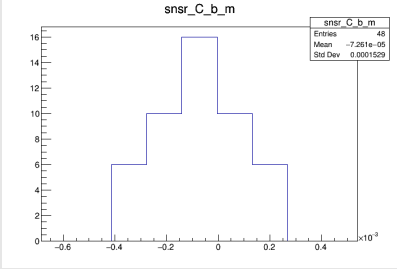
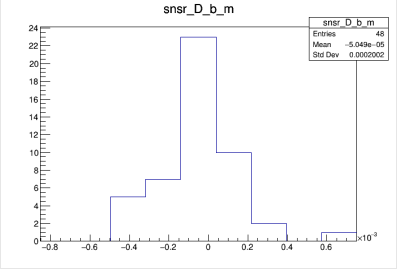
# dz Distribution

	Sensor A	Sensor B	Sensor C	Sensor D
mean (mm)	-181.7	-65.58	65.56	181.70
std. dev. (um)	35.0	37.0	28.2	24.4
plot (mm)				

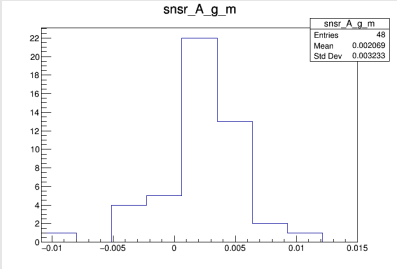
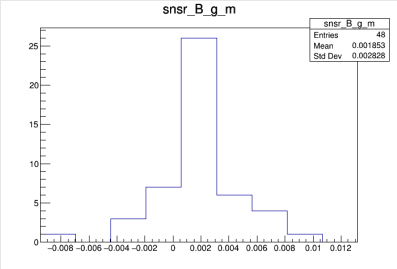
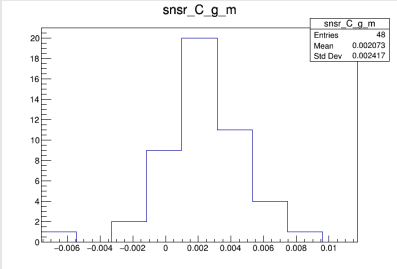
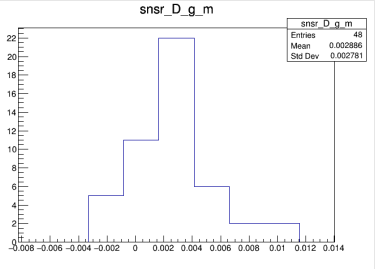
# alpha Distribution

	Sensor A	Sensor B	Sensor C	Sensor D
mean (mrad)	-0.15	-0.27	-0.15	0.30
std. dev. (mrad)	0.81	0.34	0.31	0.73
plot (rad)				

# beta Distribution

	Sensor A	Sensor B	Sensor C	Sensor D
mean (mrad)	-0.02	-0.03	-0.07	-0.05
std. dev. (mrad)	0.24	0.16	0.15	0.20
plot (rad)				

# gamma Distribution

	Sensor A	Sensor B	Sensor C	Sensor D
mean (mrad)	2.07	1.85	2.07	2.89
std. dev. (mrad)	3.23	2.82	2.42	2.78
plot (rad)				

# Notes on Results

- These are the parameters for the full transform from the sensor's frame to the ladder's frame
  - Therefore, each parameter should not necessarily have a mean of 0
  - However, all standard deviations should be small and indicate precision of assembly
- $dz$  is the actual translation of each sensor along the ladder; ideally
  - $dz = -181.75\text{mm}$  for sensor A
  - $dz = -65.55\text{mm}$  for sensor B
  - $dz = 65.55\text{mm}$  for sensor C
  - $dz = 181.75\text{mm}$  for sensor D
- Other parameters should have mean 0



# Conclusions

- Distributions of transform parameters are roughly bell-shaped
  - Nothing multi-modal or anomalous to suggest a systematic defect
- Standard deviations of the spatial translations were on the order of  $\sim 30\mu\text{m}$ 
  - $dy$  is slightly larger (expected)
- Indicate very precise placement of sensors on the ladder
- Standard deviations of the angular rotations were at worst on the order of  $\sim 2\text{mrad}$
- Overall precision of spatial parameters is very good

# Backup Slides

# Nominal Ladder Marks

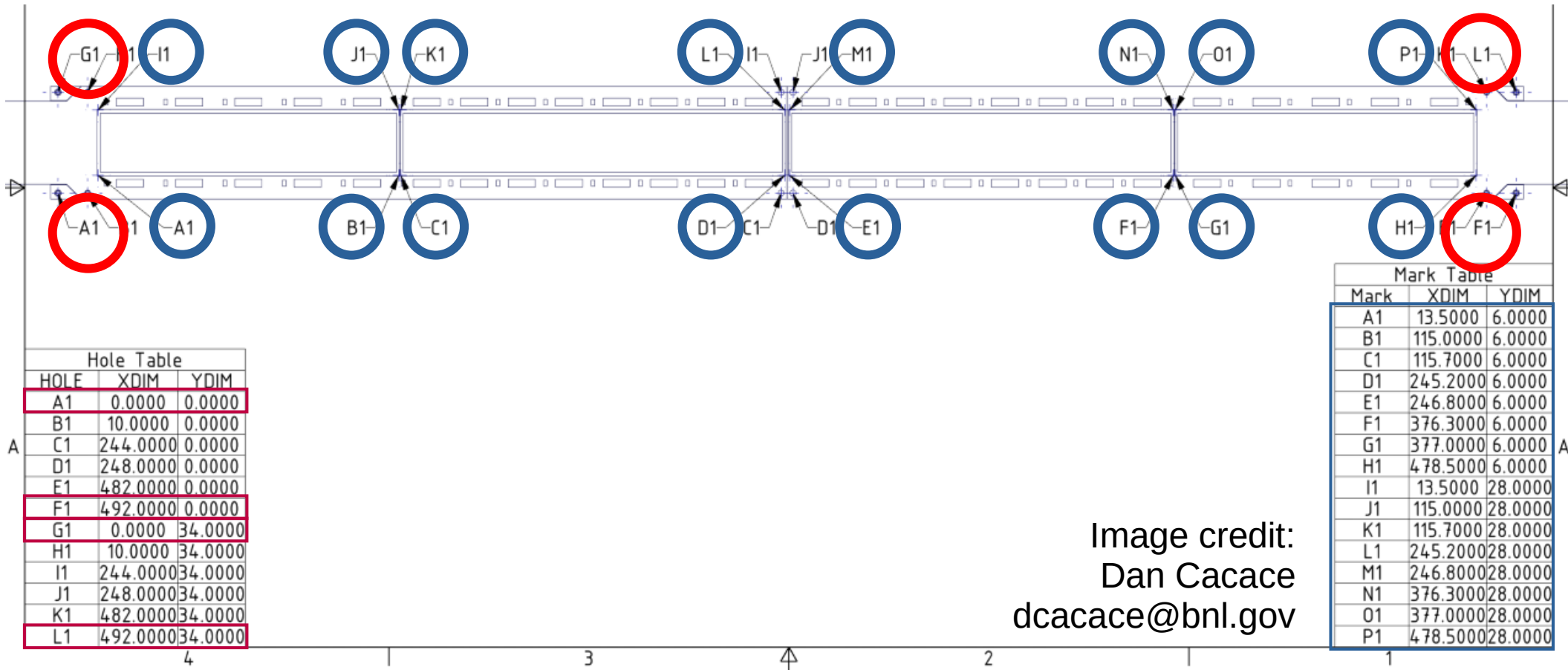


Image credit:  
Dan Cacace  
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