Radiative Corrections for Impact Studies

Kemal Tezgin

Brookhaven National Laboratory

kemaltezgin@gmail.com

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Radiative corrections - collinear approximation

- Radiative corrections can have a significant impact on the interpretation of experimental data
- Collinear approximation: Neglect the transverse component of the 4-momenta of the emitted photon



Radiative corrections in DIS

Initial and final state radiative corrections [Kripfganz, Möhring, Spiesberger, Z.Phys.C 49 (1991)]

$$\frac{d^2\sigma}{dxdy} = \int_0^1 \frac{dz_1}{z_1} D_{e/e}(z_1) \int_0^1 \frac{dz_3}{z_3^2} \bar{D}_{e/e}(z_3) \frac{y}{\hat{y}} \frac{d\hat{\sigma}_{\text{Born}}}{d\hat{x}d\hat{y}}$$
$$\frac{d^2\sigma}{dxdQ^2} = \int_0^1 dz_1 z_1 D_{e/e}(z_1) \int_0^1 \frac{dz_3}{z_3^2} \bar{D}_{e/e}(z_3) \frac{y}{\hat{y}} \frac{d\hat{\sigma}_{\text{Born}}}{d\hat{x}d\hat{Q}^2}$$

$$D_{e/e}(z) = \bar{D}_{e/e}(z) = \left[\delta(1-z)\left[1 + \frac{\alpha}{2\pi}L\left(2\ln\epsilon + \frac{3}{2}\right)\right] + \theta(1-\epsilon-z)\frac{\alpha}{2\pi}L\frac{1+z^2}{1-z}\right]$$

where $L = ln \frac{Q^2}{m_e^2}$

$$\hat{x} = \frac{z_1 x y}{z_1 z_3 + y - 1}, \qquad \hat{y} = \frac{z_1 z_3 + y - 1}{z_1 z_3}, \qquad \hat{Q}^2 = \frac{z_1}{z_3} Q^2$$

$$z_1^{\min} = \frac{1-y}{1-xy}, \qquad z_3^{\min} = 1-y(1-x)$$

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Radiative corrections in DIS

$$\int_0^1 dz \left[\delta(1-z) \left[1 + \frac{\alpha}{2\pi} L \left(2\ln \epsilon + \frac{3}{2} \right) \right] + \theta(1-\epsilon-z) \frac{\alpha}{2\pi} L \frac{1+z^2}{1-z} \right]$$





Radiative corrections in DVCS

Initial and final state radiative corrections

$$\frac{d^5\sigma}{dxdQ^2dtd\phi d\phi_S} = \int_0^1 dz_1 z_1 D_{e/e}(z_1) \int_0^1 \frac{dz_3}{z_3^2} \bar{D}_{e/e}(z_3) \frac{y}{\hat{y}} \frac{d^5\hat{\sigma}_{\mathsf{Born}}}{d\hat{x}d\hat{Q}^2dtd\phi d\phi_S}$$

Define new variables: $z_1 = 1 - 10^{z_1'}, \quad z_3 = 1 - 10^{z_3'}, \quad z_1', z_3' \in [-8, 0]$

$$\frac{d^{5}\sigma}{dxdQ^{2}dtd\phi d\phi_{S}} = \int_{-8}^{0} dz'_{1} (1 - z_{1}) z_{1} \ln(10) D_{e/e}(z_{1})$$
$$\int_{-8}^{0} dz'_{3} \frac{1 - z_{3}}{z_{3}^{2}} \ln(10) \overline{D}_{e/e}(z_{3}) \frac{y}{\hat{y}} \frac{d^{5}\hat{\sigma}_{\text{Born}}}{d\hat{x}d\hat{Q}^{2}dtd\phi d\phi_{S}}$$
$$\hat{x} = \frac{z_{1}xy}{z_{1}z_{3} + y - 1}, \qquad \hat{y} = \frac{z_{1}z_{3} + y - 1}{z_{1}z_{3}}, \qquad \hat{Q}^{2} = \frac{z_{1}}{z_{3}}Q^{2}$$
$$z_{1}^{\min} = \frac{1 - y}{1 - xy}, \qquad z_{3}^{\min} = 1 - y(1 - x)$$

Kinematics used in the samples:

- pure DVCS, 10 \times 100 GeV, $\epsilon = 10^{-2}$
- 0.0001 < *x*_{Bj} < 0.630957
- $0.04 < |t| < 1.3 GeV^2$
- 1.0 < Q² < 10.0*GeV*²
- $0.0 < \phi < 2\pi$
- 0.0 < ϕ_S < 2 π
- 0.01 < *y* < 0.85

Radiative corrections - first set

• Contributions from the following graphs:



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Radiative corrections - first set of kinematics



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• Contributions from the following graphs:



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Radiative corrections – second-order corrections

• Expression for 2 × *ISR* [Kripfganz, Möhring, Spiesberger, Z.Phys.C 49 (1991)]

$$\begin{split} \frac{d^{2}\sigma}{dxdy}\Big|_{i}^{(2)} &= \frac{1}{2} \left(\frac{\alpha}{2\pi}\right)^{2} L_{e}^{2} \\ &\cdot \left\{ \sum_{z_{min}}^{1} dz_{1} \left[2\frac{1+z_{1}^{2}}{1-z_{1}} \left(2\ln\left(1-z_{1}\right)-\ln\left(z_{1}\right)+\frac{3}{2} \right) \right. \\ &\cdot \left(\sigma_{0}(z_{1},1)-\sigma_{0}(1,1)\right) \\ &+ \left(\left(1+z_{1}\right)\ln z_{1}-2(1-z_{1})\right)\sigma_{0}(z_{1},1) \right] \\ &+ \left\{ \left[S(z_{1}^{\min}) \right]^{2} + 4\text{Li}_{2}(1-z_{1}^{\min}) \\ &+ z_{1}^{\min}(z_{1}^{\min}-2)\ln z_{1}^{\min} - \frac{1}{4}(z_{1}^{\min})^{4} - (z_{1}^{\min})^{3} \\ &- (z_{1}^{\min})^{2} - z_{1}^{\min} + \frac{13}{4} \right\} \sigma_{0}(1,1) \right\}. \end{split}$$
(31)

• The corresponding radiator function:

$$D_{\theta/\theta}^{(2)}(z) = \delta(1-z) \left(\frac{\alpha}{2\pi}\right)^2 \frac{L_{\theta}^2}{2} \left[\frac{13}{4} + 6\ln\epsilon + 4\ln^2\epsilon + 2z_{\min}^2 \ln(z_{\min}) - z_{\min}^2\right] \\ + \Theta(1-\epsilon-z) \left(\frac{\alpha}{2\pi}\right)^2 \frac{L_{\theta}^2}{2} \left[2\frac{1+z^2}{1-z} \left(2\ln(1-z) - \ln(z) + \frac{3}{2}\right) + (1+z)\ln(z) - 2(1-z)\right]$$

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Radiative corrections - second set kinematics



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Radiative corrections - energy of radiated photons

Energy of radiated photons in the first set:



Energy of radiated photons in the second set:



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- The effects of RCs on the kinematic variables have been assessed
- First-order contributions as well as three of the second-order diagrams have been implemented