

Resumption of PRISM-FFA for next generation muon decay experiments

Akira Sato, Osaka University

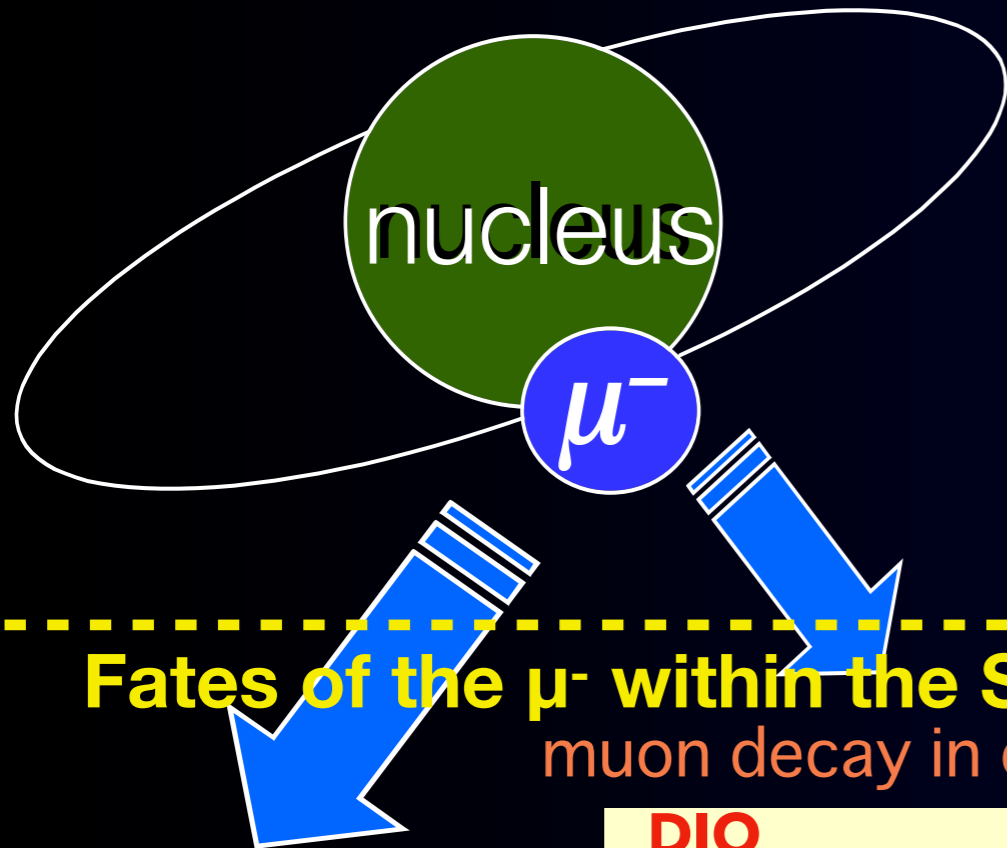
FFA`23, 2023/09/14, Jefferson Lab., US

Abstract

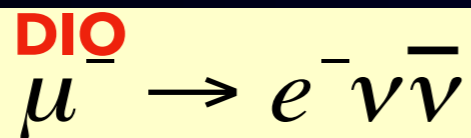
- PRISM-FFA was intensively studied from 2003 to 2009 for muon electron conversion process experiments with ultimate sensitivity.
- However, much of the manpower has since been focused on realizing COMET experiments without FFA, and the PRISM research has been taken over by the PRSIM Task Force.
- After more than 20 years of preparation, physical measurements of COMET and Mu2e will finally begin in the next few years.
- This is very exciting, but at the same time it is a time to start seriously considering future experiments.
- Recently, there has been renewed interest in the potential of PRSIM-FFA in connection with future muon programs planning at FNAL in Snowmass2021.
- We plan to use this opportunity to strengthen international cooperation among Japan, the U.S., and the U.K. etc, and to once again reexamine the PRISM-FFA.

What is a Muon to Electron Conversion?

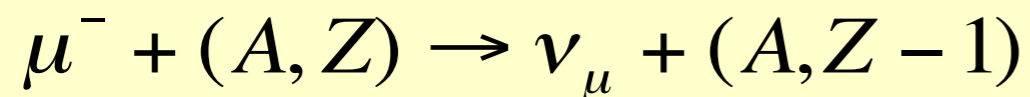
1s state in a muonic atom



Fates of the μ^- within the SM
muon decay in orbit

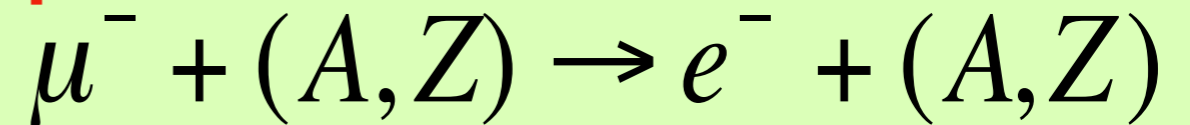


nuclear muon capture



Beyond the SM

μ -e conversion



Forbidden by the SM, because the lepton flavor is changed to μ -flavor to e-flavor.

Charged Lepton Flavor Violation (CLFV)

Event signature :

a single mono-energetic electron of 105MeV (for Al)

in the SM + ν masses

μ -e conversion can occur via ν -mixing, but expected rate is well below the experimentally accessible range. Rate $\sim O(10^{-54})$

Discovery of the μ -e conversion is a clear evidence of new physics beyond the SM.

in the SM + new physics

A wide variety of proposed extensions to the SM predict observable μ -e conversion rate.

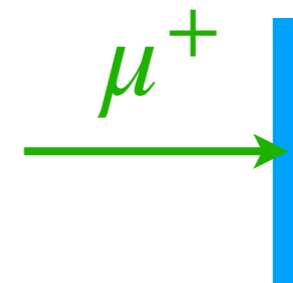
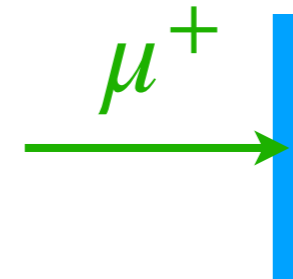
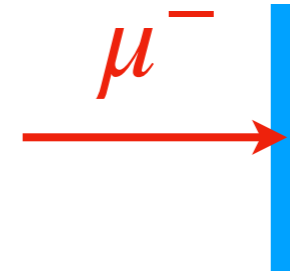
- μ -e conversion and CLFV searches can achieve $\sim 10^4$ TeV energy scale.

Muon CLFV searches

- $\mu^- N \rightarrow e^- N$
 - COMET@J-PARC, Mu2e@FNAL
 - Signal selection: one 105 MeV e^-
- $\mu^+ \rightarrow e^+ \gamma$
 - MEG-II@PSI
 - Signal selection: check E and p conservation
- $\mu^+ \rightarrow e^+ e^+ e^-$
 - Mu3e@PSI
 - Signal selection: check E and p conservation
- Muonium \rightarrow anti-Muonium

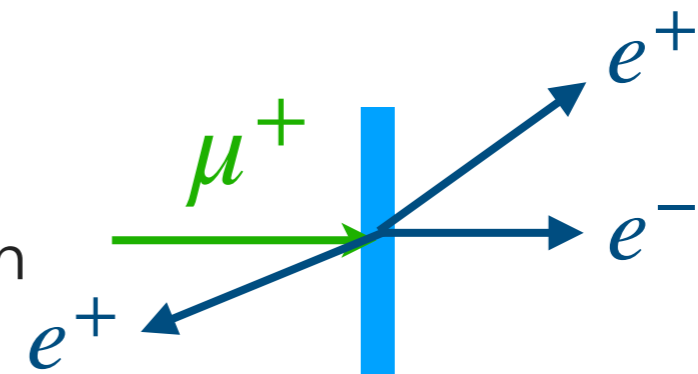
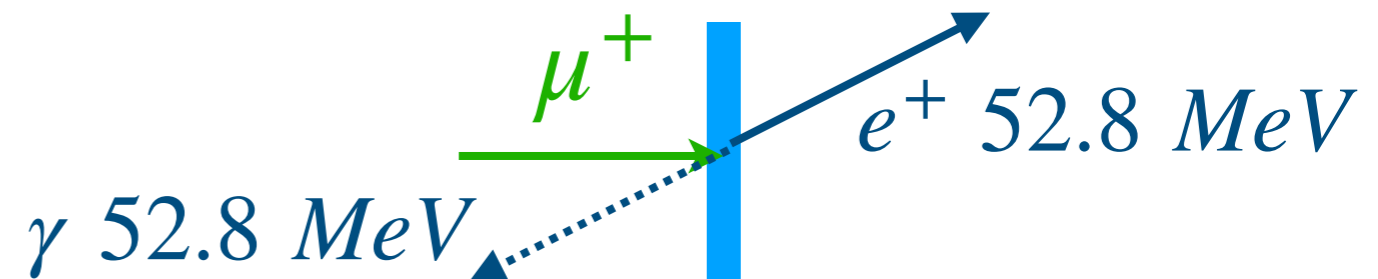
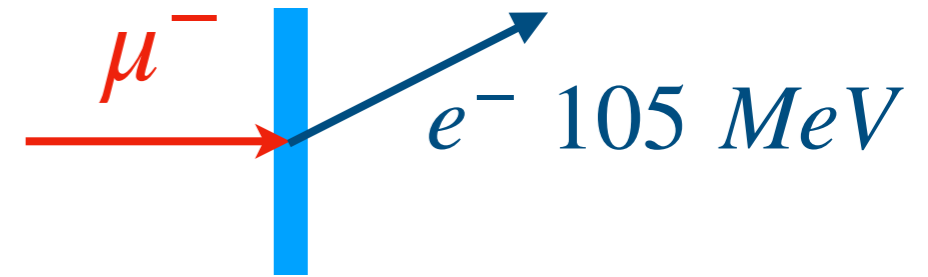
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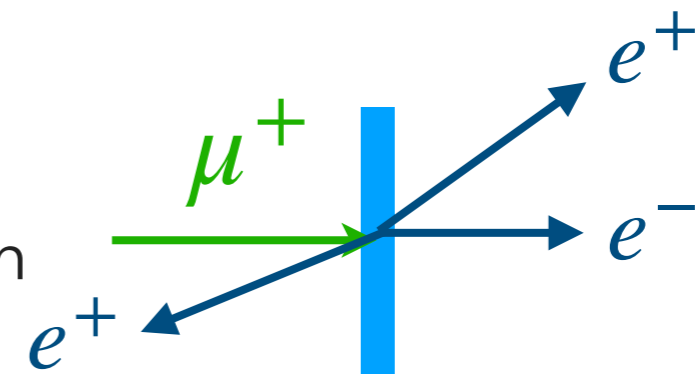
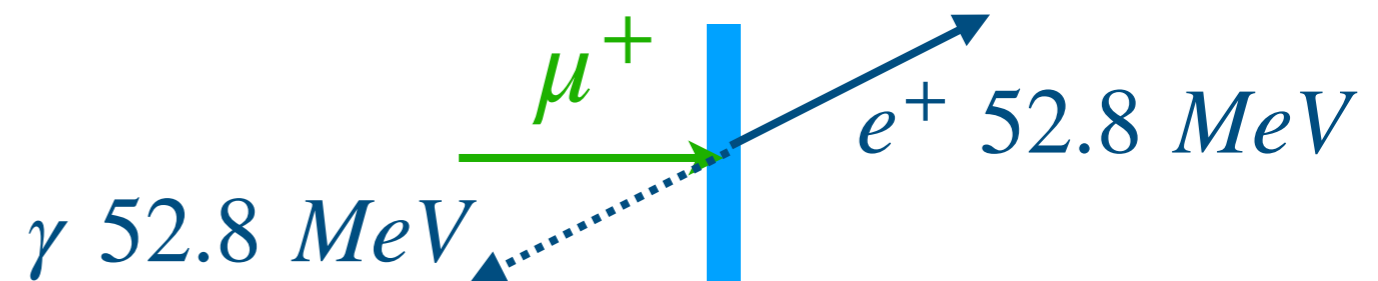
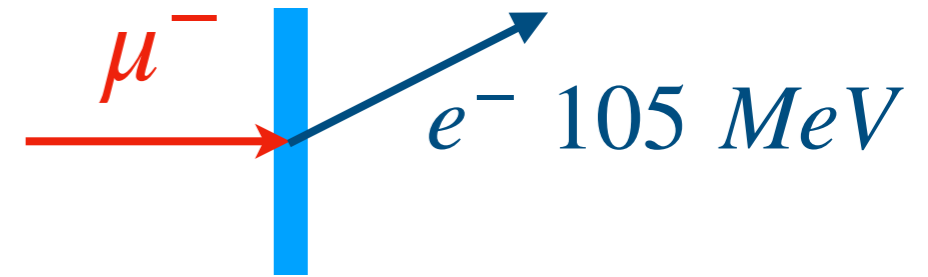
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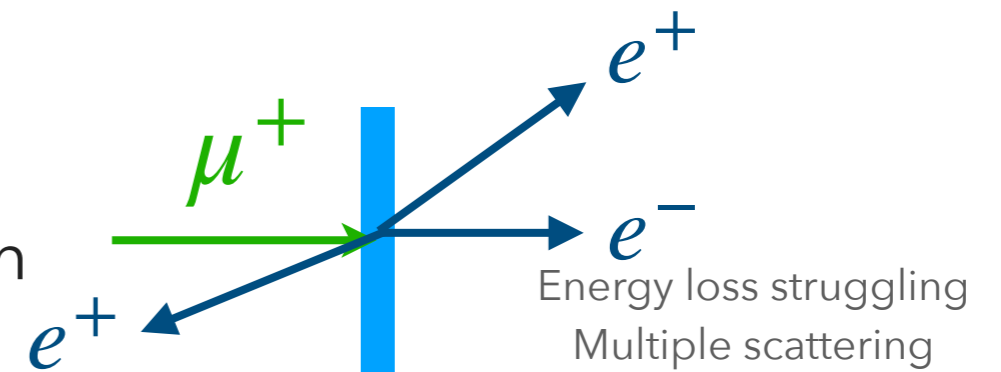
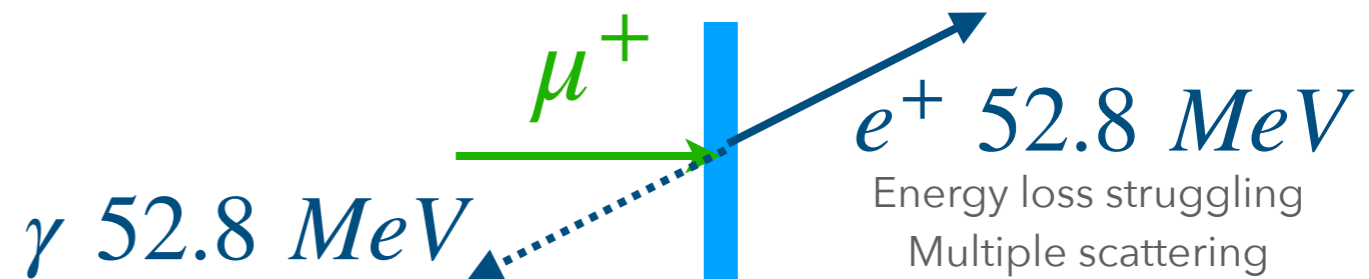
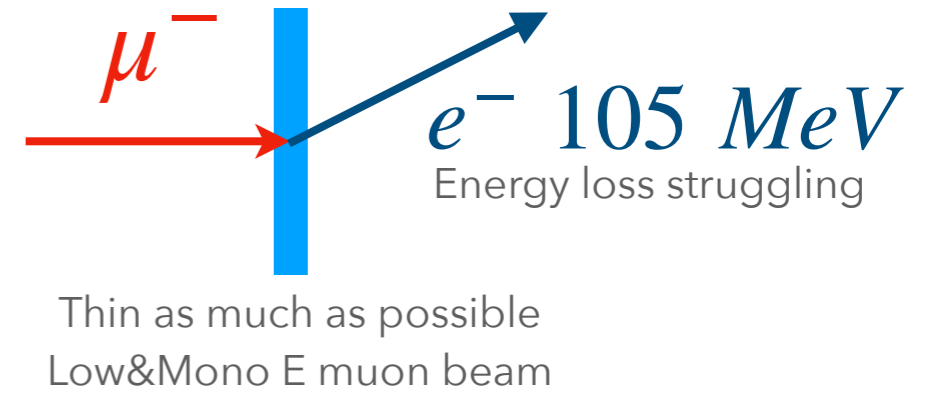
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Since these are ultra-rare decay processes, it is necessary to search for signal events among a huge number of background events. For all of these experiments, not only **muon beam intensity** but also **beam quality (mono energy, no unwanted particles)** is crucial.

Muon CLFV searches

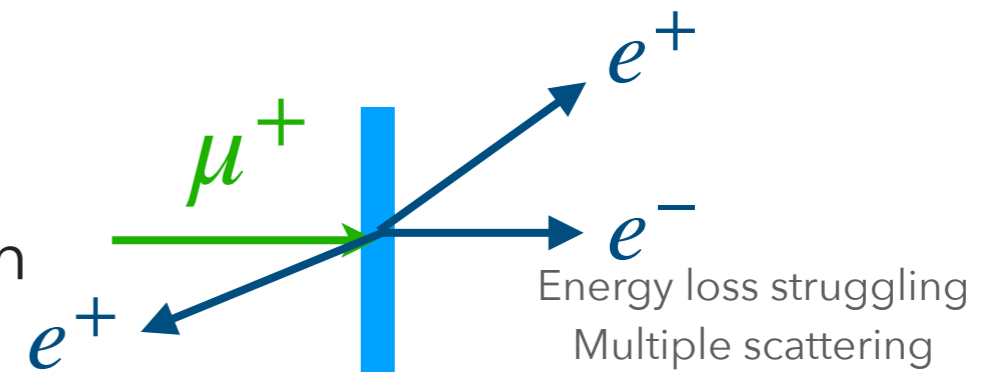
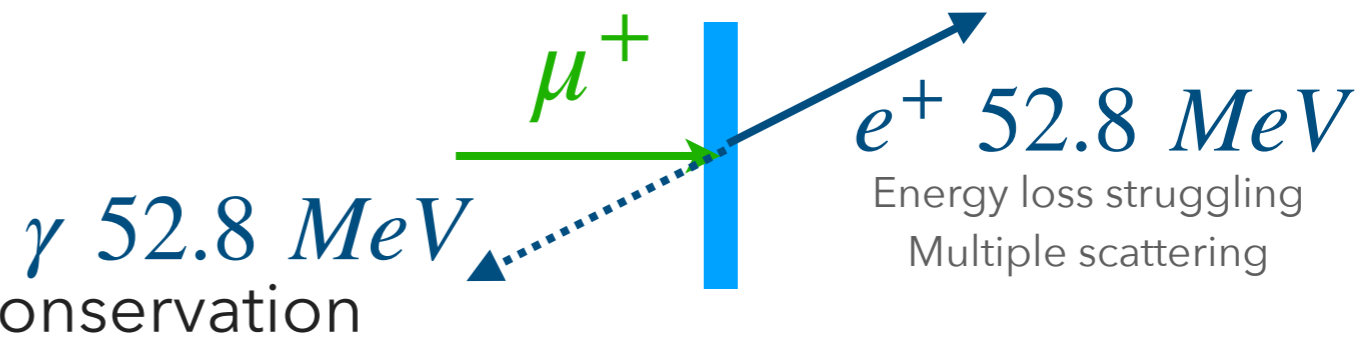
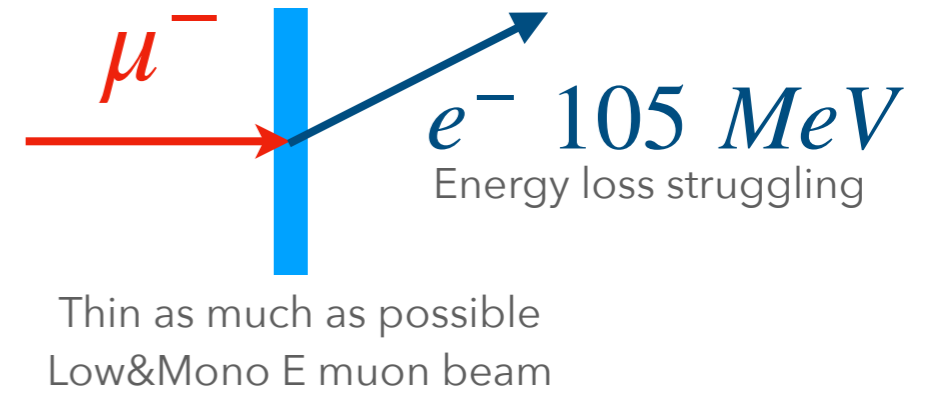
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FFA can offer solutions to make a good muon beam.

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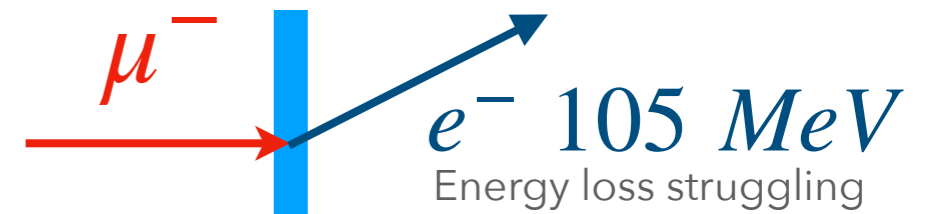
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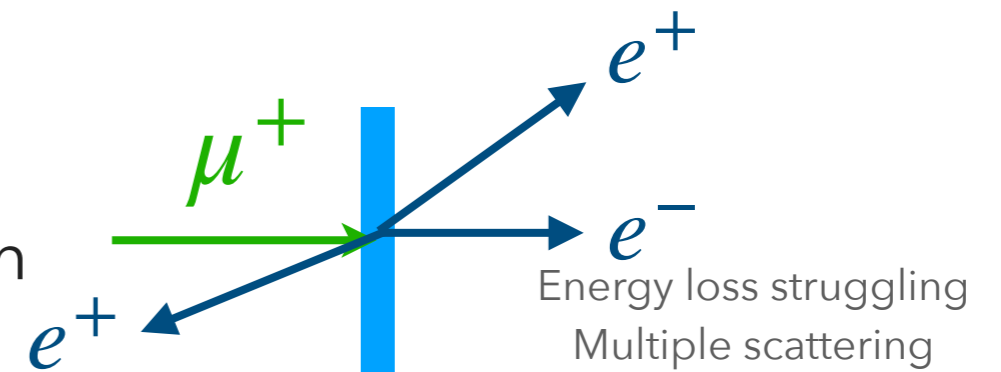
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Thin as much as possible
Low&Mono E muon beam

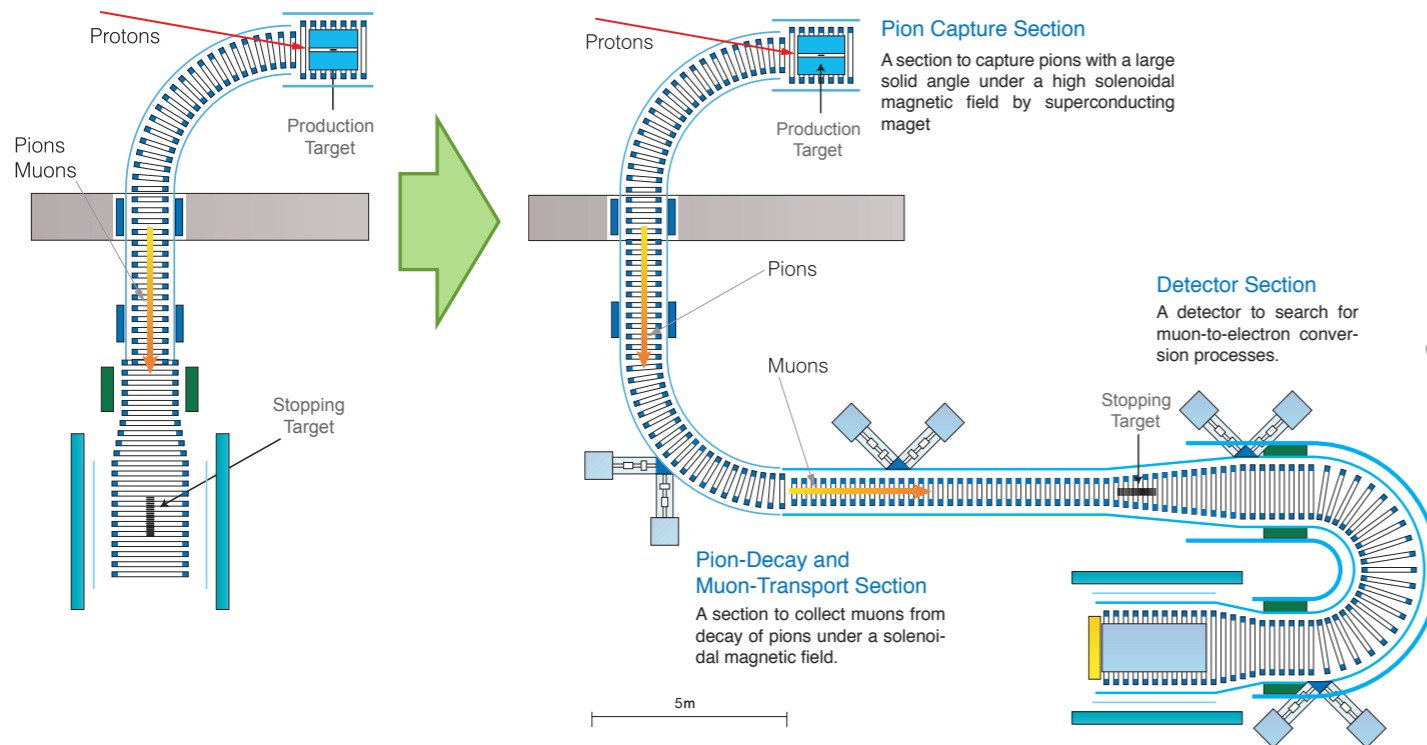


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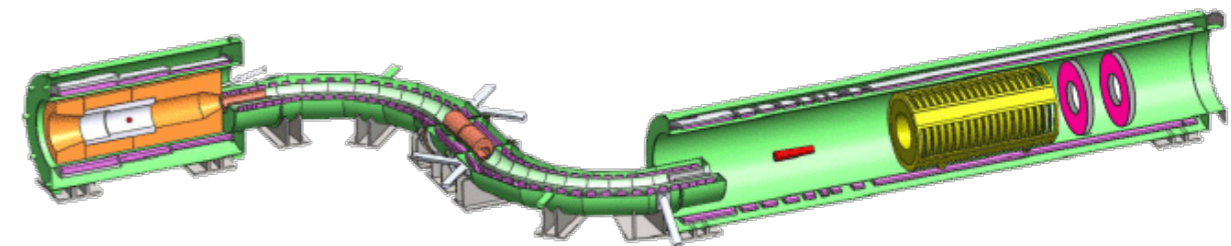
FFA can offer solutions to make a good muon beam.

COMET and Mu2e

COMET @J-PARC



Mu2e @FNAL



COMET Phase-I : S.E.S. $\sim 3 \times 10^{-15}$ on Al **Under construction**

COMET Phase-II : S.E.S. $\sim 3 \times 10^{-17}$ on Al **Planned**

Mu2e: S.E.S. $\sim 3 \times 10^{-17}$ on Al **Under construction**

Mu2e-II: S.E.S. $\sim 3 \times 10^{-18}$ on Al **Under discussion**

Features of the Setup

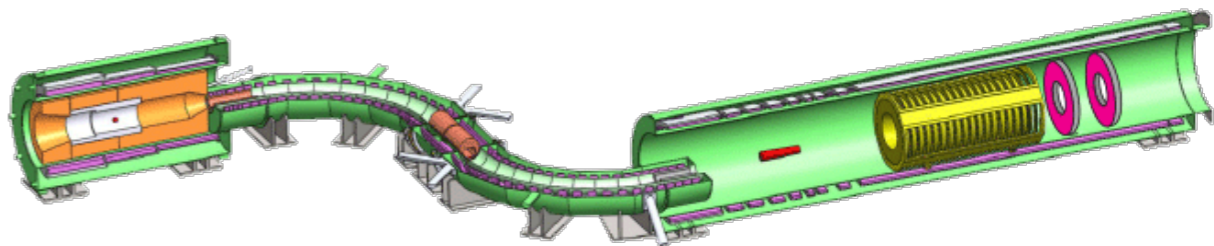
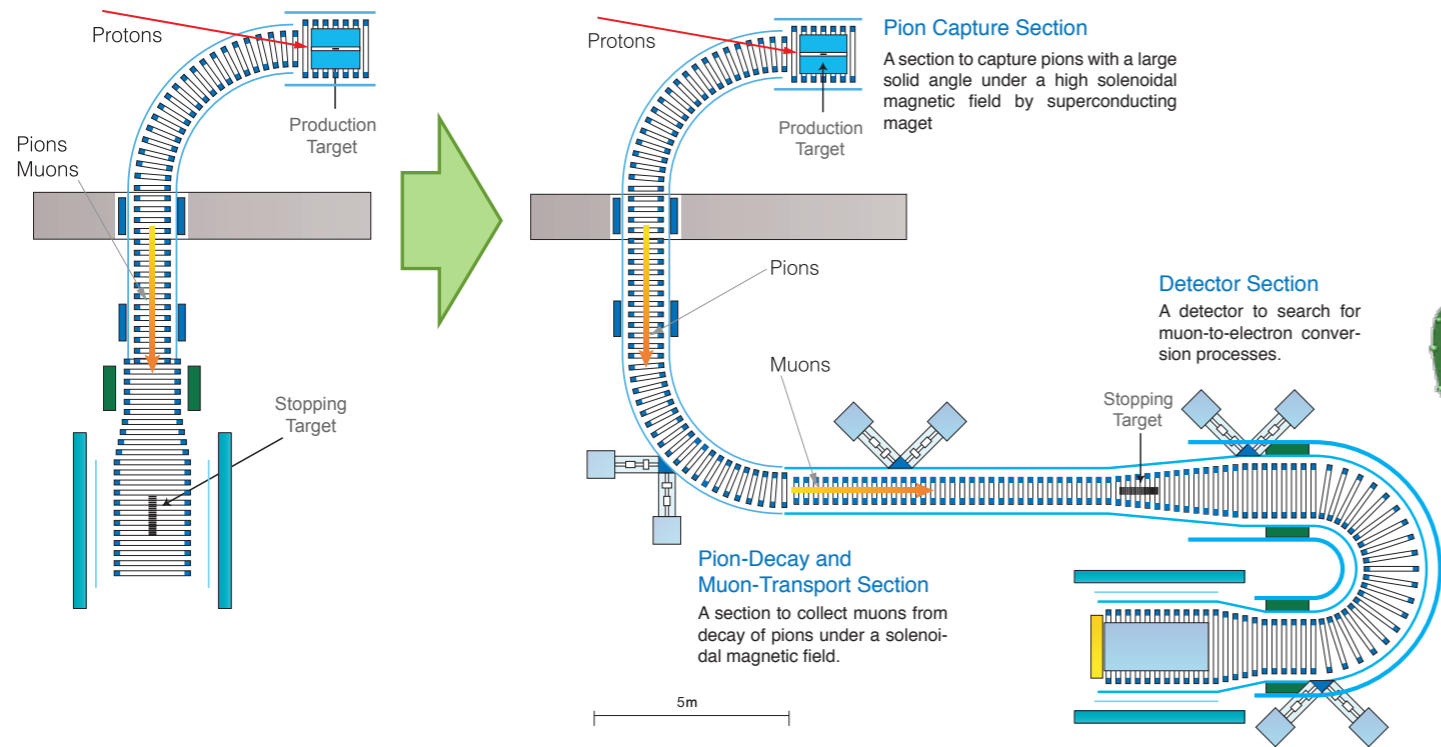
- * Solenoid channel
- * Stop μ^- at the stopping targets.
- * ID single electron from the target and measure its energy precisely.

- A very large number of researchers are working energetically to get these experiments started.

COMET and Mu2e

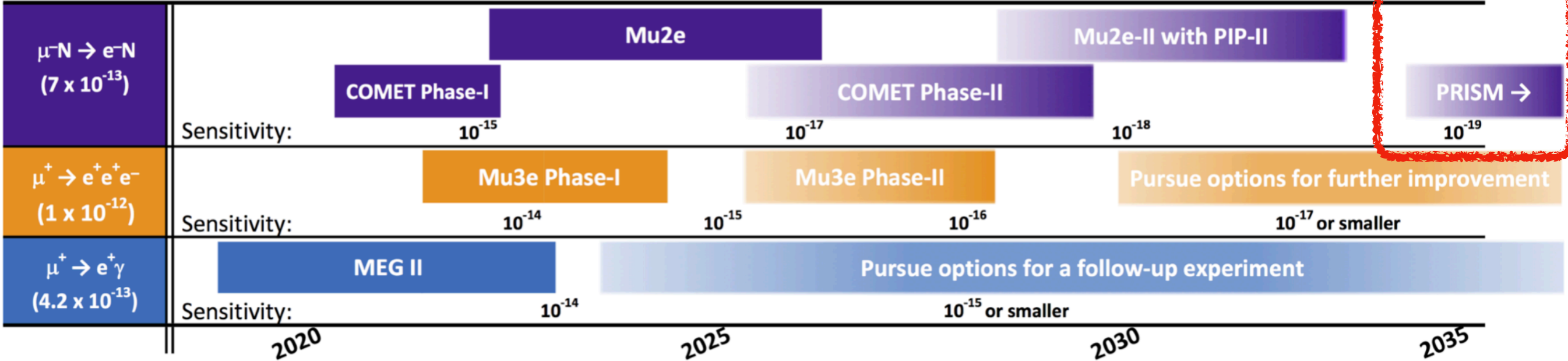
COMET @J-PARC

Mu2e @FNAL



This talk

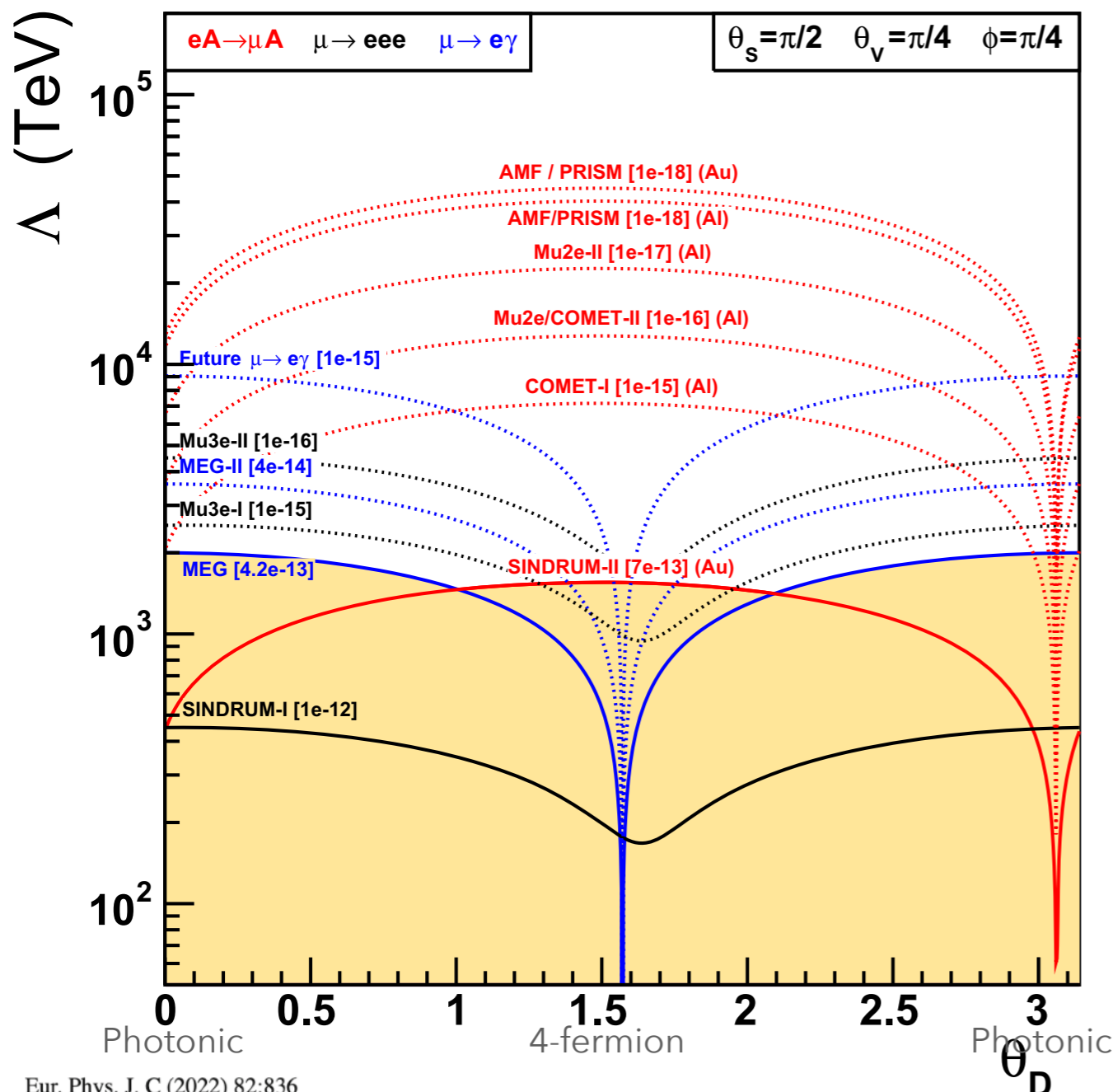
Searches for Charged-Lepton Flavor Violation in Experiments using Intense Muon Beams



Data Taking (Approved Experiments)
 Proposed Future Running

What to aim for in the next experiment

- **Case 1:** No signal discovered in COMET and Mu2e
 - BR < 6.3×10^{-17} (90% CL) will be achieved
 - **Next: Further sensitivity improvement** (Mu2e-II: < 5.8×10^{-18})



$$\delta\mathcal{L} = \frac{1}{\Lambda_{LFV}^2} \left[C_D(m_\mu \bar{e}\sigma^{\alpha\beta} P_R\mu) F_{\alpha\beta} + C_S(\bar{e}P_R\mu)(\bar{e}P_R e) \right. \\ \left. + C_{VR}(\bar{e}\gamma^\alpha P_L\mu)(\bar{e}\gamma_\alpha P_R e) \right. \\ \left. + C_{VL}(\bar{e}\gamma^\alpha P_L\mu)(\bar{e}\gamma_\alpha P_L e) + C_{A\text{light}}\mathcal{O}_{A\text{light}} \right. \\ \left. + C_{A\text{heavy}\perp}\mathcal{O}_{A\text{heavy}\perp} \right] \quad (2.1)$$

Table 2 Dimensionless operator coefficients expressed in the angular coordinates. The radial coordinate is $1/\Lambda_{LFV}^2$, $\theta_I : 0.. \pi$ and $\phi : 0..2\pi$. As discussed in Appendix 1, the $\vec{e}_{VL} \times \vec{e}_{VR}$ plane was projected to a line, deviations from which are measured by θ_V . In general, the basis vectors $\{e_A\}$ are not unit vectors, and their normalisation is given in Table 5 and after Eq. (C.3) for the primed vectors

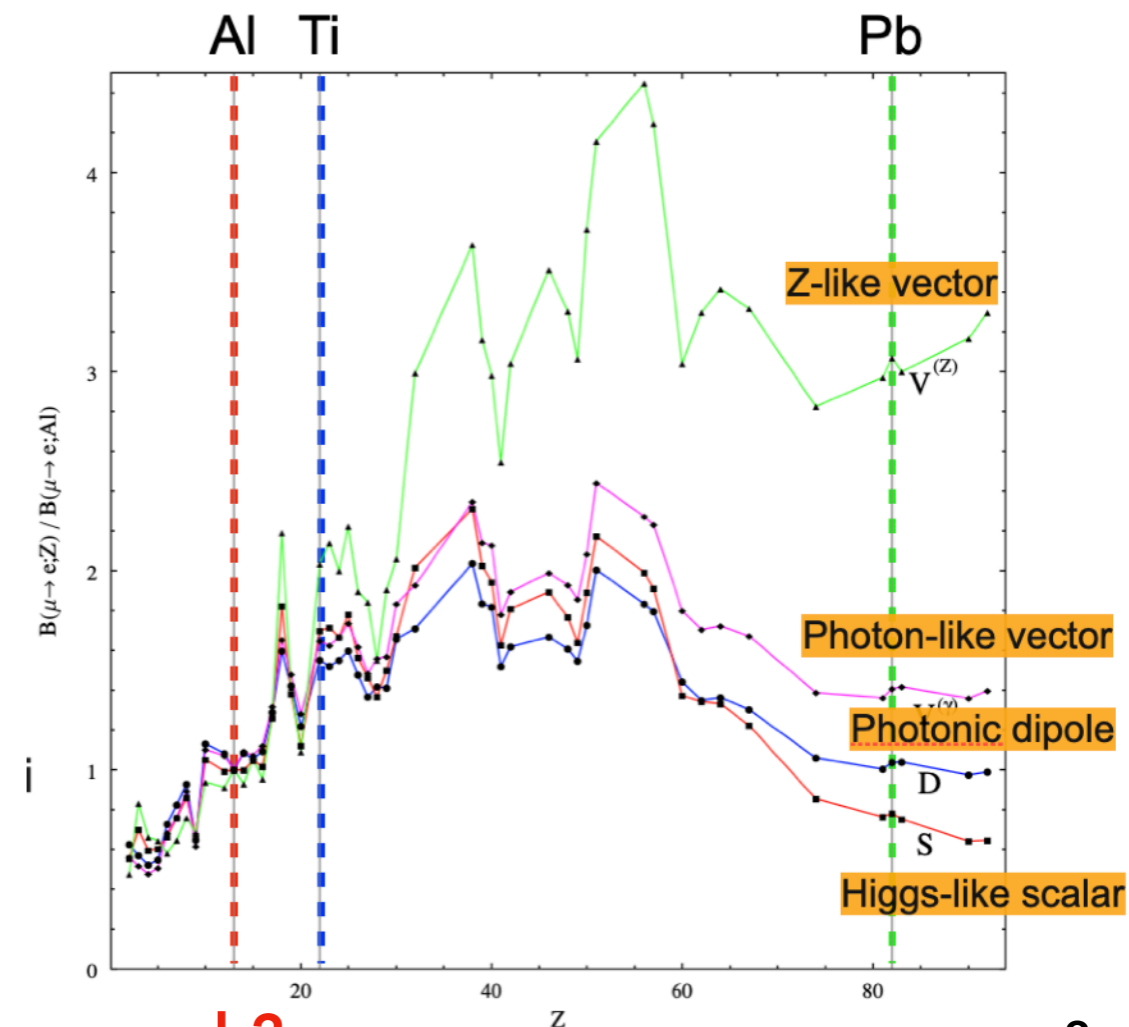
$\vec{C} \cdot \vec{e}_D$	$ \vec{e}_D \cos \theta_D$
$\vec{C} \cdot \vec{e}_S$	$ \vec{e}_S \sin \theta_D \cos \theta_S$
$\vec{C} \cdot \vec{e}_{VL}$	$ \vec{e}'_{VL} \sin \theta_D \sin \theta_S \cos \theta_V$
$\vec{C} \cdot \vec{e}_{VR}$	$ \vec{e}'_{VR} \sin \theta_D \sin \theta_S \cos \theta_V$
$\vec{C} \cdot \vec{e}_{A\text{light}}$	$ \vec{e}_{A\text{light}} \sin \theta_D \sin \theta_S \sin \theta_V \sin \phi$
$\vec{C} \cdot \vec{e}_{A\text{heavy}\perp}$	$ \vec{e}_{A\text{heavy}\perp} \sin \theta_D \sin \theta_S \sin \theta_V \cos \phi$

What to aim for in the next experiment

- **Case 1:** No signal discovered in COMET and Mu2e
 - $BR < 6.3 \times 10^{-17}$ (90% CL) will be achieved.
 - **Next: Further sensitivity improvement** (Mu2e-II: $< 5.8 \times 10^{-18}$)
- **Case 2:** Signal events discovered in COMET and/or Mu2e
 - BR(Al) will be determined.

- **Next: Change the stopping target material**

- To study physics mechanism
 - (A,Z) dependence
 - Spin dependence
- Candidate target material
 - Al ($\tau \sim 880$ ns), SI, SD (COMET/Mu2e)
 - Ti ($\tau \sim 330$ ns)
 - (Nuclear spin=0; SI),
 - Pb,Au ($\tau \sim 80$ ns)



How? Higher intensity muon beam is needed. It is enough?

Potential Backgrounds for μ -e Conversion

- Because μ -e conversion is an ultra rare decay process, in the future experiments, we need to improve both **muon intensity**, and the **background reduction** power.

Table 14. Summary of the estimated background events for a single-event sensitivity of 3×10^{-15} in COMET Phase-I with a proton extinction factor of 3×10^{-11} .

Type	Background	Estimated events	
Physics	Muon decay in orbit	0.01	DIO
	Radiative muon capture	0.0019	
	Neutron emission after muon capture	< 0.001	
	Charged particle emission after muon capture	< 0.001	
Prompt beam	* Beam electrons		RPC
	* Muon decay in flight		
	* Pion decay in flight		
	* Other beam particles		
	All (*) combined	≤ 0.0038	
	Radiative pion capture	0.0028	
	Neutrons	$\sim 10^{-9}$	
Delayed beam	Beam electrons	~ 0	DB
	Muon decay in flight	~ 0	
	Pion decay in flight	~ 0	
	Radiative pion capture	~ 0	
	Antiproton-induced backgrounds	0.0012	
Others	Cosmic rays [†]	< 0.01	
Total		0.032	

[†] This estimate is currently limited by computing resources.

The COMET Collaboration, "COMET Phase-I technical design report", Progress of Theoretical and Experimental Physics, Volume 2020, Issue 3, March 2020, 033C01, <https://doi.org/10.1093/ptep/ptz125>

Ways for BG reduction in COMET/Mu2e for SES $\sim 10^{-17}$

Low mass tracker

Improve e- energy resolution

Beam pulsing with separation of $\sim 1 \mu\text{s}$

Measure between the beam pulses

High proton beam extinction: $\sim 10^{-10}$

Curved solenoids for momentum selection

Eliminate energetic muon ($>75\text{MeV}/c$)

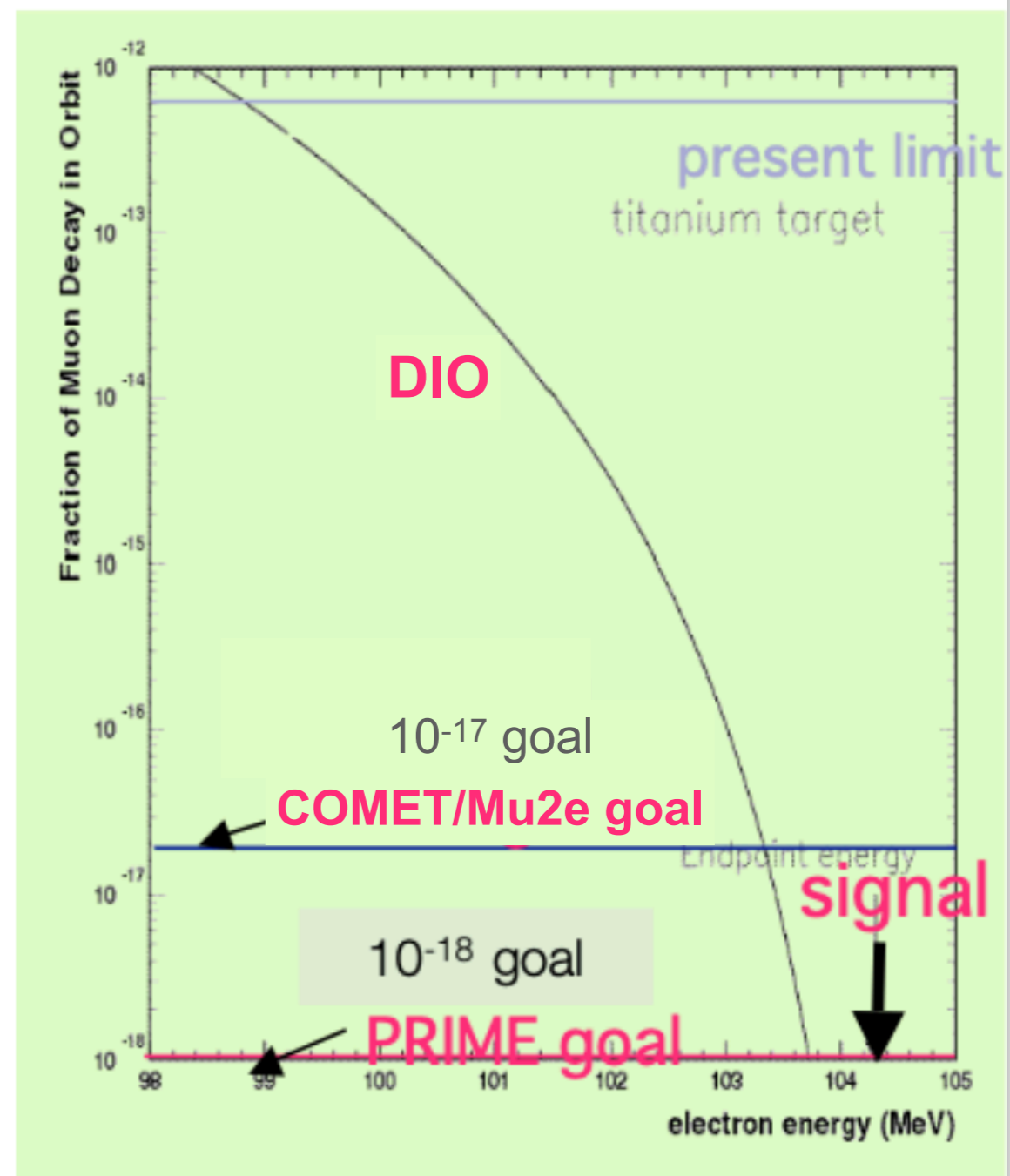
Long muon transport

Reduce pion contamination

COMET/Mu2e is not enough for future experiments. Need new ideas.

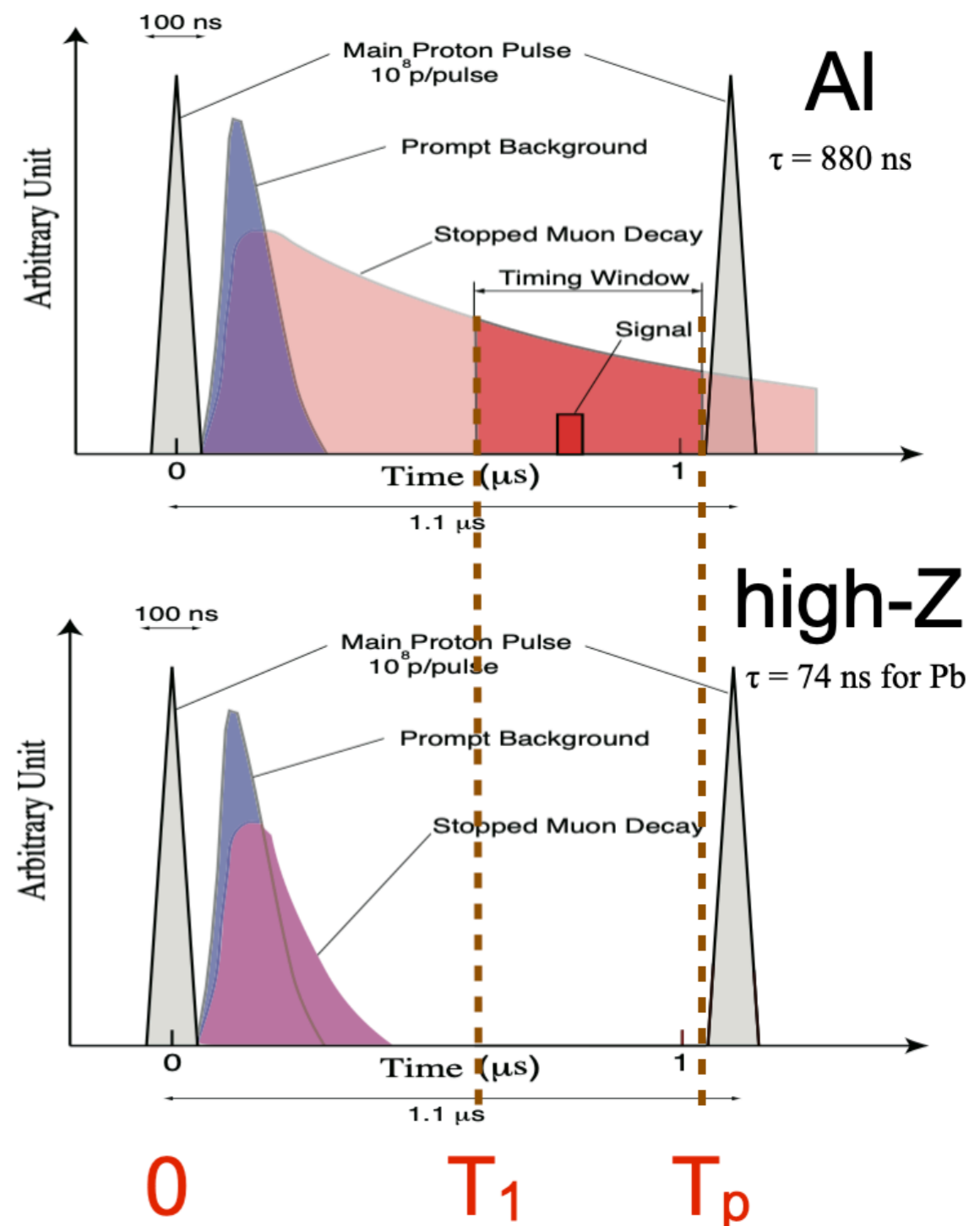
Problems to go beyond the 10^{-18} sensitivity

- COMET/Mu2e scheme has some critical problems in further improving experimental sensitivity for 10^{-18} level and the detailed physics study changing the stopping target.
- **DIO reduction is not enough**
 - Reconstructed momentum resolution is not enough to reject DIO electrons.
 - σ_p : mainly from tracker performance and energy struggling in the target.
 - Energy struggling in the stopping targets is not negligible.
- **Cannot use the heavy target material**
 - The measurement starts after 700 nsec after the prompt. Material of a muon stopping target is limited to low Z.
 - For high Z target, muon life is short (~ 80 ns). We have to open the measurement window as early as possible, but there are a lot of prompt BG.
 - The solenoid beam line is not long enough, so that late pions might come in a beam. Radiative Pion Capture can be a crucial BG.
- **Beam background rejection is not enough**
 - It is heavily relied on proton beam extinction of 10^{-10} , which is uncertain.



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We need a big quality μ^- beam to improve BG rejection.

μ^- beam w/ small E spread

No unwanted particles

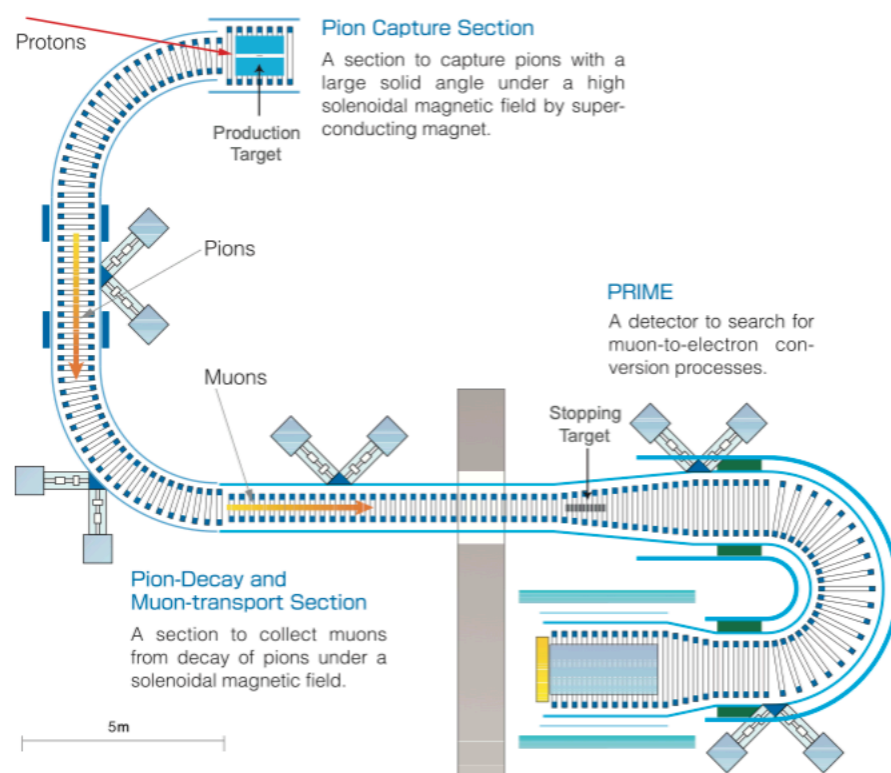
- * Pions
- * anti-protons
- * $e^- > 105$ MeV/c
- * $\mu^- > 75$ MeV/c

Pulsed beam w/ a high extinction factor
: no particle b/w pulses

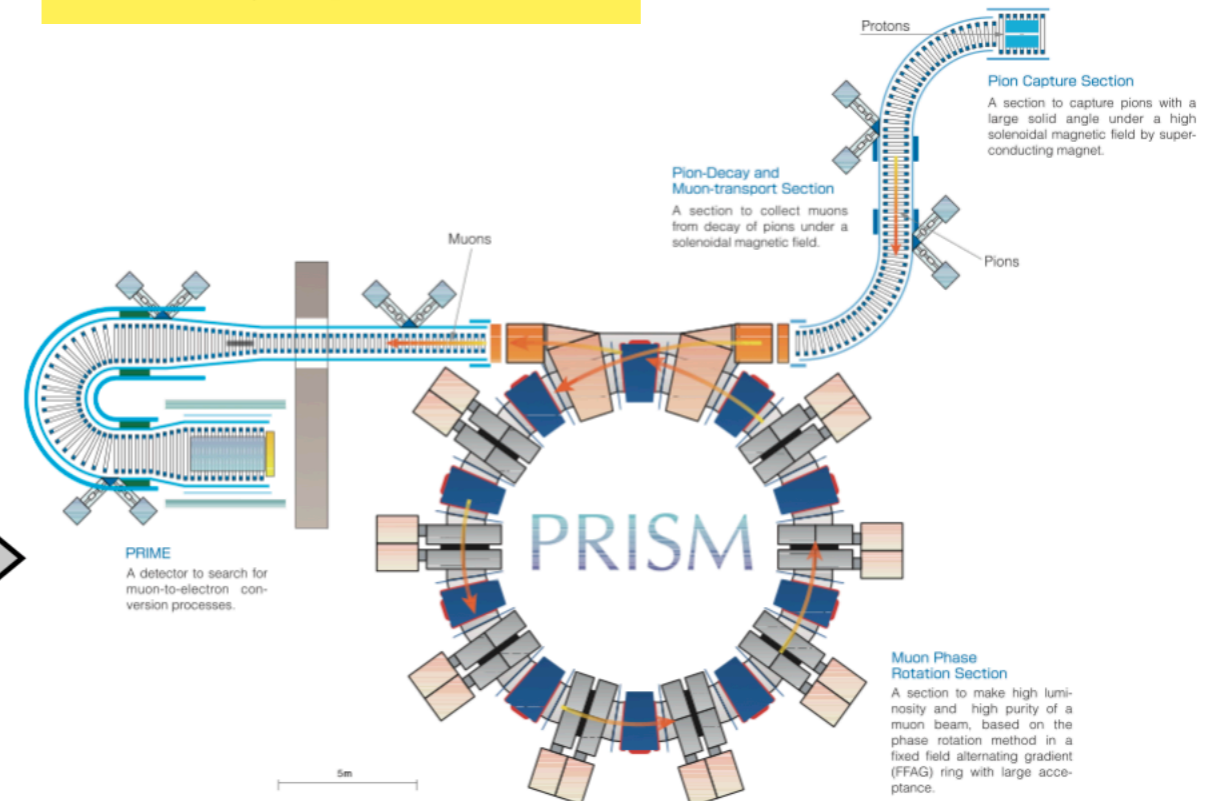
PRISM/PRIME as the next μ -e experiment

- We proposed the PRISM/PRIME idea as a solution of these problems for below the 10^{-18} level μ -e conversion experiment.

COMET



PRISM/PRIME



$$B(\mu^- + Al \rightarrow e^- + Al) < 10^{-16}$$

- without a muon storage ring.
- with a slowly-extracted pulsed proton beam.
- doable at the J-PARC NP Hall.
- regarded as the first phase / MECO type
- Early realization

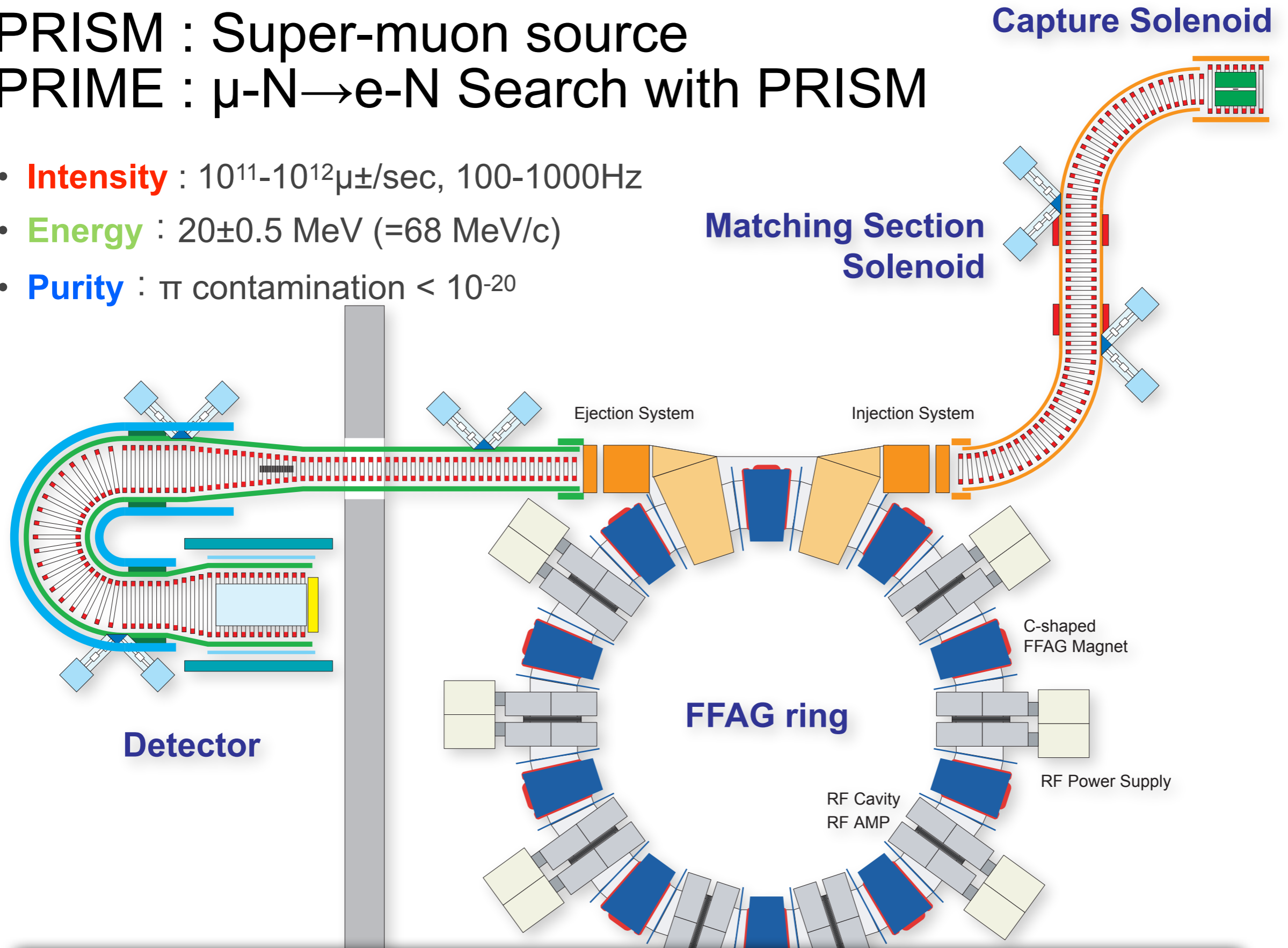
$$B(\mu^- + Ti \rightarrow e^- + Ti) < 10^{-18}$$

- with a muon storage ring.
- with a fast-extracted pulsed proton beam.
- need a new beamline and experimental hall.
- regarded as the second phase.
- Ultimate search

PRISM : Super-muon source

PRIME : $\mu\text{-N} \rightarrow e\text{-N}$ Search with PRISM

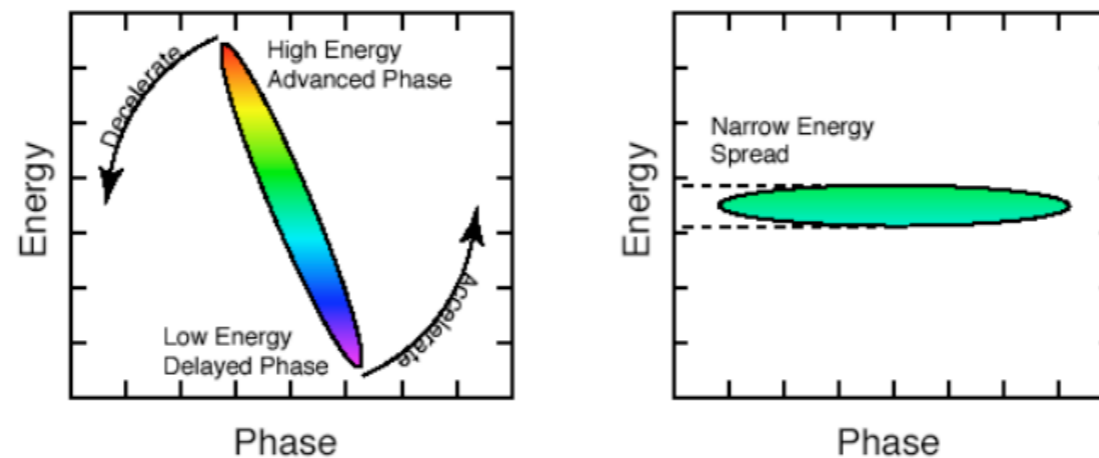
- **Intensity** : $10^{11}\text{-}10^{12}\mu\pm/\text{sec}$, 100-1000Hz
- **Energy** : 20 ± 0.5 MeV (=68 MeV/c)
- **Purity** : π contamination $< 10^{-20}$



PRISM-FFAG is a key device to achieve the mono-energetic and pure muon beam. Phase rotation is applied in the ring.

High brightness beam by PRISM

- To make a narrow energy spread muon beam, a technique of **phase rotation** is adapted.
- The phase rotation is to decelerate fast beam particles and accelerate slow beam particles.



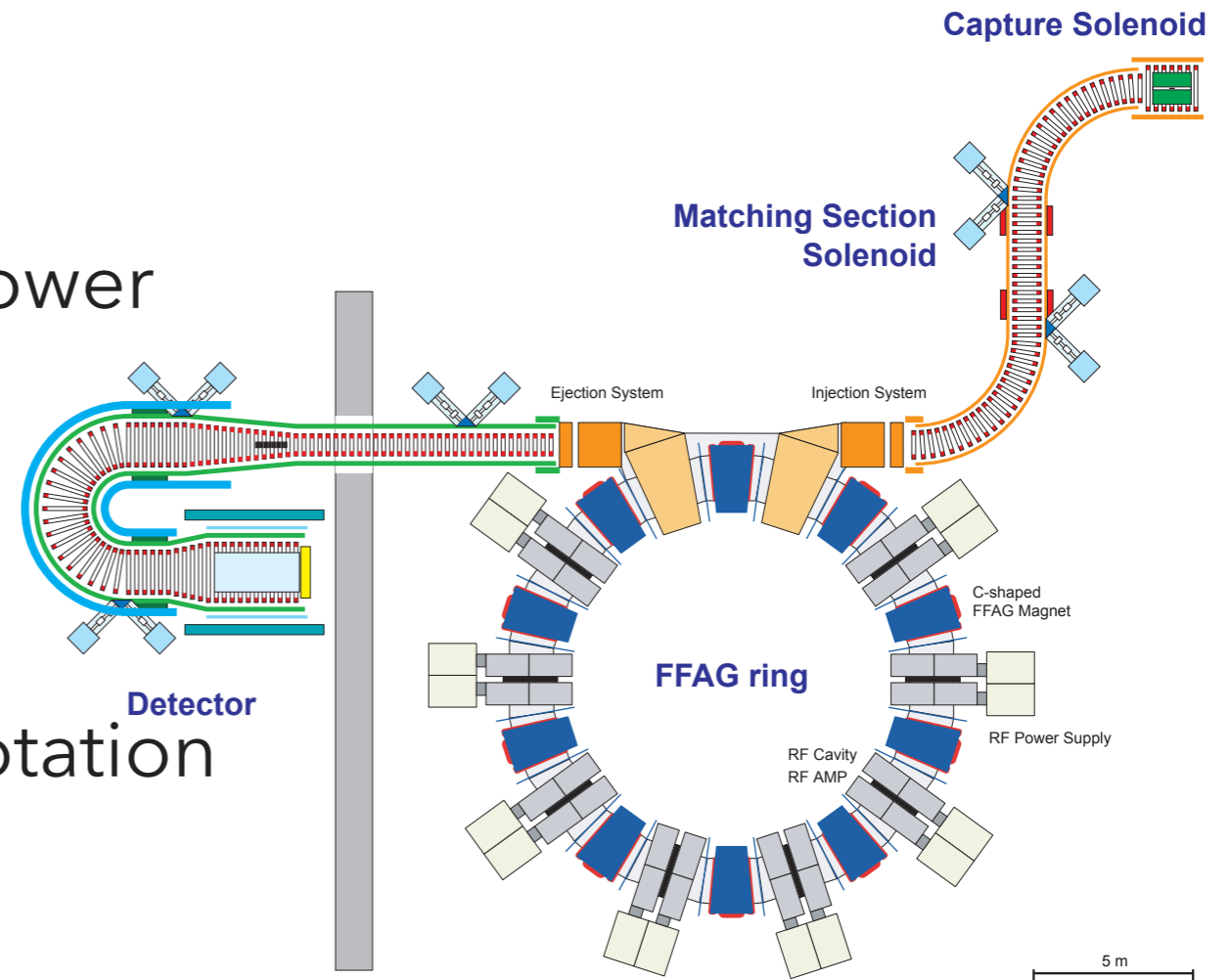
- To identify energy of beam particles, a time of flight (TOF) from the proton bunch is used.
 - Fast particle comes earlier and slow particle comes late.
- Proton beam pulse should be narrow (< 10 ns).
- Phase rotation is a well established technique. To adapt it to muon beam (large emittance), FFA ring provides a good solution.

Background rejection by PRISM

- **(1) Narrow muon beam energy spread**
 - goal : +- 3 %; **High brightness beam**
 - **by phase rotation** at the PRISM-FFA ring
 - Muons can easily stop in a very thin stopping target (1/10 of COMET/Mu2e). Reduce energy straggling in the target. **Improve the resolution of the reconstructed momentum.**
- **(2) Long muon flight length**
 - about 40 m circumference x 5-6 turns at PRISM-FFA ring
 - pion survival rate of $<10^{-20}$; **No pion contamination**
 - **Pion Radiative Capture BG is negligible**
- **(3) Muon beam energy selection before the detector**
 - momentum slit after the PRISM-FFAG ring
 - 68 MeV/c +- 3% (not 104 MeV)
 - **Muon decay in flight BG is negligible. No signal like e- in the beam. Pure low- μ - beam**
- **(4) Beam extinction at muons**
 - Kicker magnets of the PRISM-FFA ring
 - **no proton extinction needed**
- **(5) Small duty factor of detection**
 - $\sim 10^{-4}$ for a detection of 1 μ s with 100 Hz repetition
 - The rep. rate depends on the kicker specification.
 - **Better suppression of Cosmic-ray BG**
 - **Ideal time structure**

PRISM specifications (Akira's baseline lattice)

- Intensity :
 - 2×10^{12} muons/sec.
 - for multi-MW proton beam power
- Central Momentum :
 - 68 MeV/c
- Momentum Spread :
 - $\pm 2\%$ (from $\pm 20\%$) by phase rotation
- Beam Repetition :
 - 100 - 1000 Hz
 - due to repetition of kicker magnets of the muon storage ring.
- Beam Energy Selection :
 - 68 MeV/c $\pm 2\%$
 - at extraction of the muon storage ring.



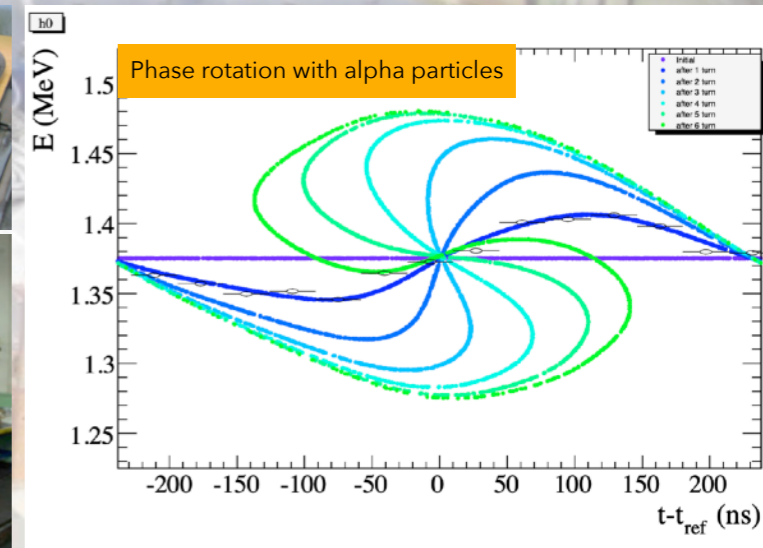
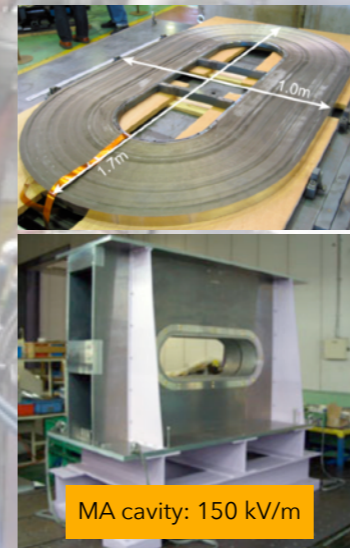
6-sector PRISM-FFAG at RCNP, Osaka Univ.



6-sector PRISM-FFAG at RCNP, Osaka Univ.

We had R&D program on the muon storage ring from 2003 to 2009. Many successful outcomes were achieved.

large aperture FFAG magnets,
high field gardened RF system
6-cell FFAG and
phase rotation test with α particles.



However, to improve the feasibility of the PRISM μ -e conversion experiment, we still need to solve issues

Matching between solenoid and FFAG

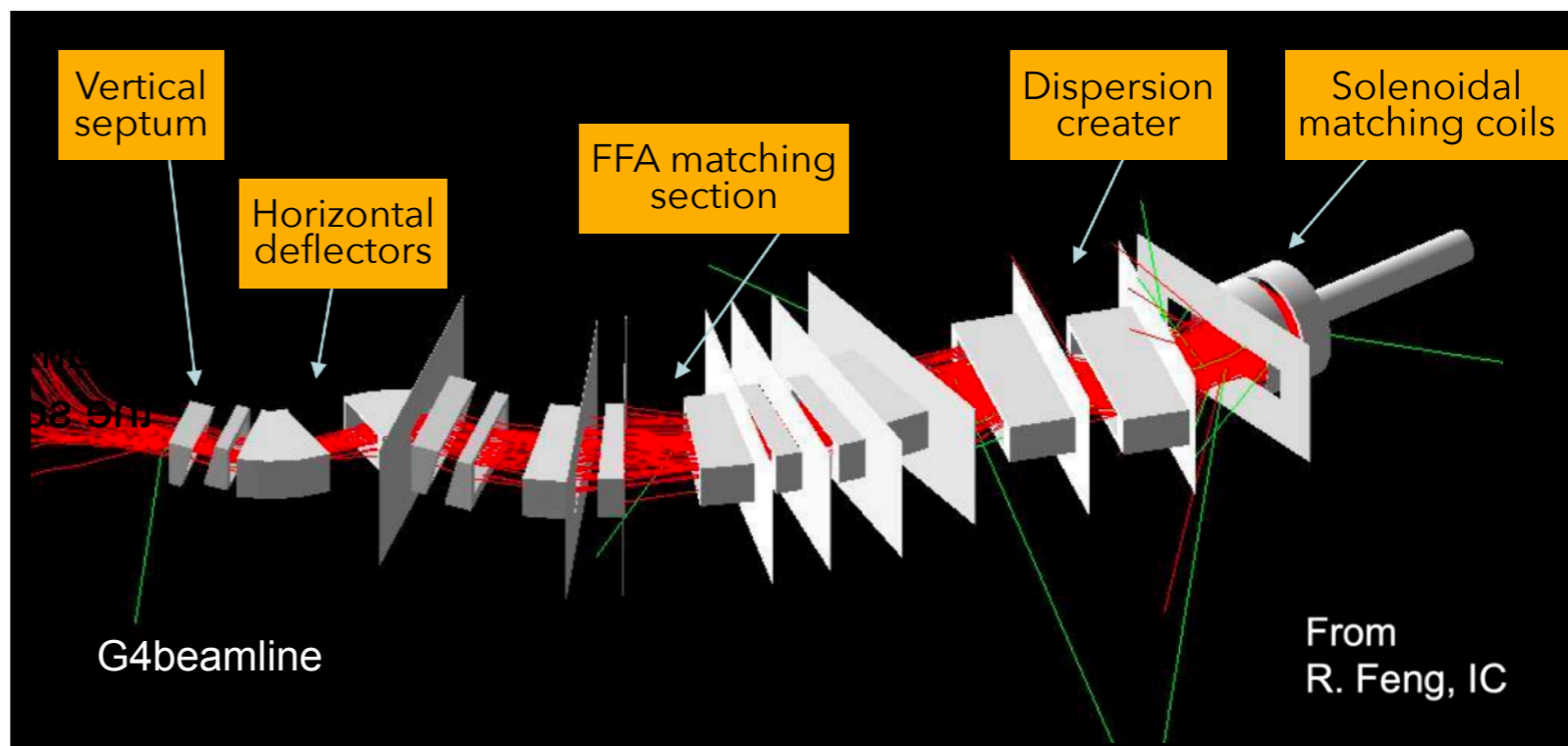
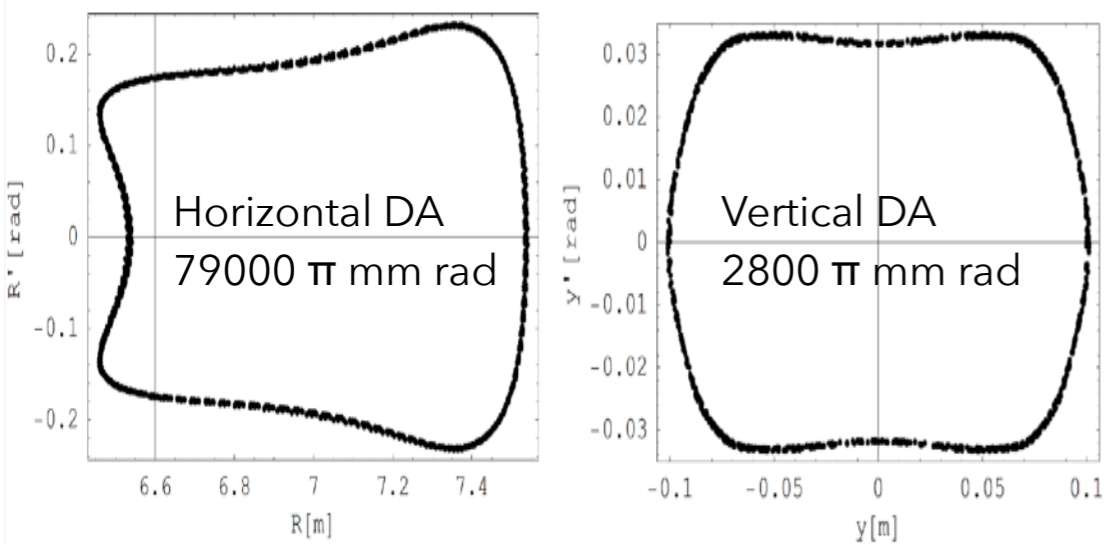
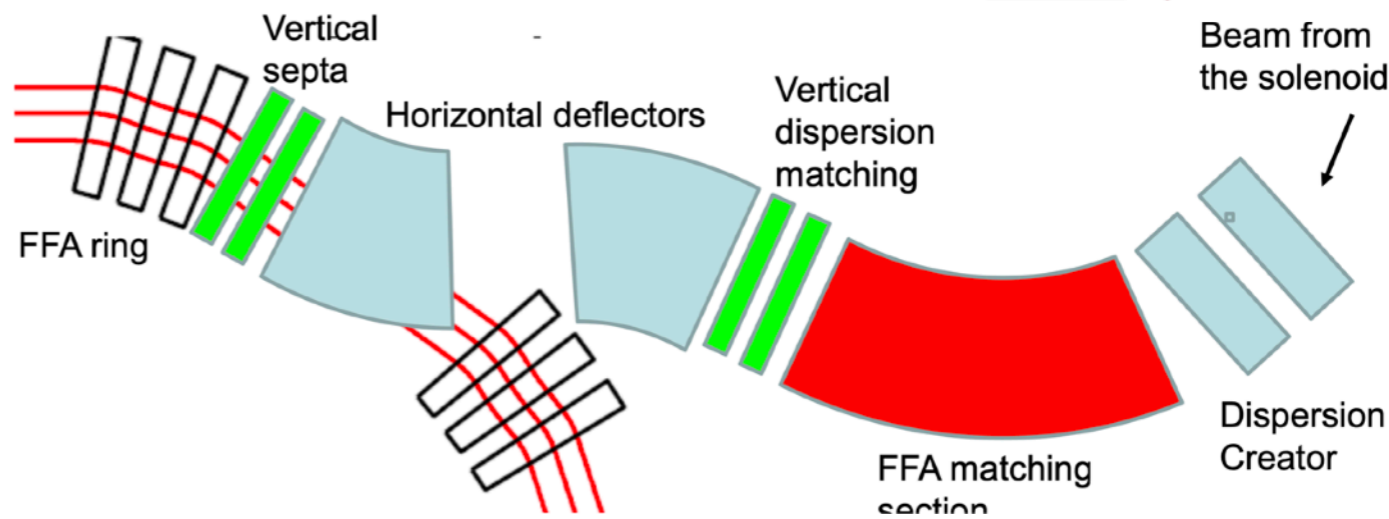
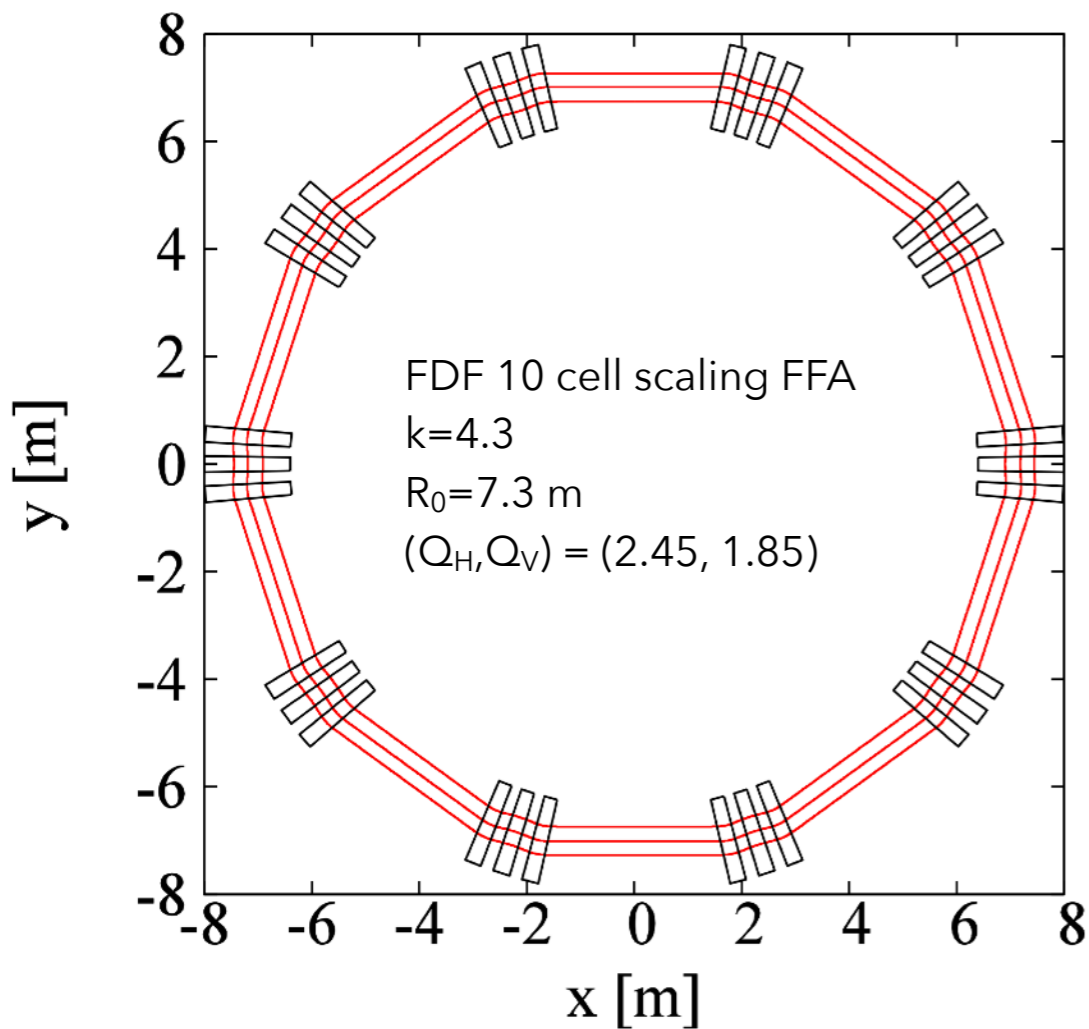
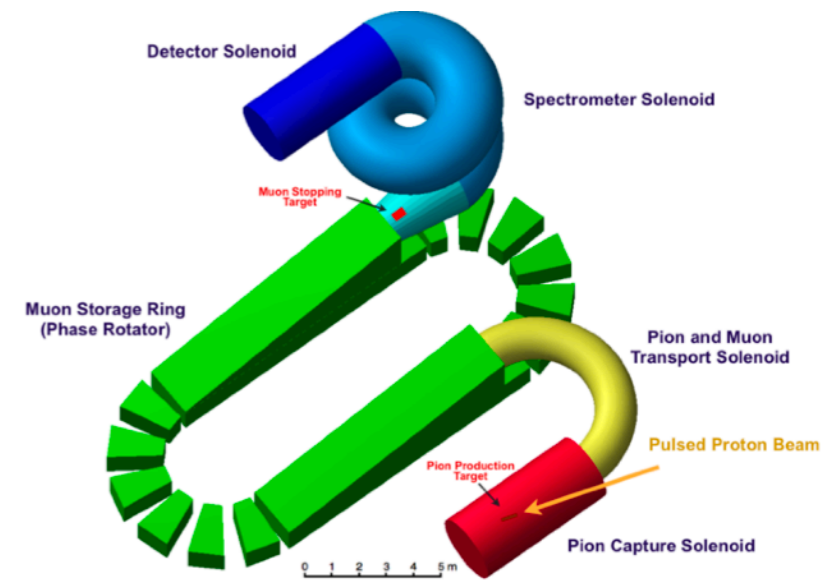
Injection and extraction and kickers for the FFAG ring

Cost for the RF system

After this, R&D is continued by PRISM Task Force.

In PRISM Task Force led by Jaroslaw

- New FDF lattice, Injection/Extraction studied



FNAL-AMF plan

- The discussion in Snowmass2021 has brought renewed attention to the potential of the PRISM idea in future muon research.

New Facility: AMF

hep-ex 2203.08278

- The “Advanced Muon Facility” would use PIP-II to enable
 - **CLFV in all three muon modes: world-leading facility**
 - two new small rings for $\mu N \rightarrow eN$ at high Z and additional x100 in rate
 - with a possible DM experiment
 - x100-1000 more beam for $\mu \rightarrow e\gamma$ and $\mu \rightarrow 3e$ than are possible at PSI
 - Possible muonium-antimuonium and muon EDM

R. Bernstein, FNAL

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Snowmass RPF5

Use PRISM for these experiments to use bright and pure mu⁺/mu⁻ beams

- I and Bob Bernstein (FNAL) are making a plan to revisit the PRISM idea and initiate a collaborative effort for its realistic design for use in future muon research programs in Japan and the US.
 - You are welcome to join us.

Workshop on a Future Muon Program at Fermilab

- It was held at FNAL, 27-29 Mar 2023.
 - <https://indico.fnal.gov/event/57834/>
 - We had two sessions to discuss FFA possibilities for AMF.
- The proceeding was opened last night for the summary.
 - <https://arxiv.org/abs/2309.05933>

FERMILAB-CONF-23-464-PPD
CALT-TH-2023-036

Workshop on a Future Muon Program At Fermilab

27-29 Mar 2023
US/Pacific timezone

- Overview
- Timetable
- Venue and maps
- Parking at Caltech
- Accommodation
- Transportation information
- Wireless information
- Zoom connection
- Dining and Entertainment
- Registration
- Registration payment
- Participant List
- Contribution List

Future muon program at Fermilab

The Snowmass report on rare processes and precision measurements recommended Mu2e-II and a next generation muon facility at Fermilab (Advanced Muon Facility) as priorities for the frontier. This workshop is devoted to pursuing design studies for Mu2e-II, to organizing efforts for the next generation muon facility, and to identifying synergies with other R&D efforts (e.g. muon collider). Topics will include high-power targetry, status of R&D for Mu2e-II, development of compressor rings, FFA and concepts for muon experiments (conversion, decays, muonium and other opportunities) at AMF.

The workshop will be held in a hybrid format, but participants are strongly encouraged to attend in person.

Check the "zoom connection" tab for clickable links to zoom rooms

Starts 27 Mar 2023, 06:00
Ends 29 Mar 2023, 22:30
US/Pacific

Registration
Registration for this event is currently open.

[Register now](#)

Workshop organizers

- echenard@caltech.edu
- fcp@caltech.edu

arXiv:2309.05933v1 [hep-ex] 12 Sep 2023

Workshop on a future muon program at FNAL

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Things to consider for FFA

- Redesign the FFA ring to match the specifications of future proton accelerators (PIP-II/J-PARC ...).
- Change the final muon momentum as low as possible.
 - $68\text{MeV}/c \rightarrow < 40\text{ MeV}/c$
- Establish a realistic design for injection into and extraction from the FFA ring, ready to proceed with hardware development.
- Simultaneous phase rotation of negative and positive muons in one ring.
- Shows the muon beam performance that FFA can achieve.
- ...

The design of the FFA is highly dependent on many factors; Physics goals, proton driver, pion production and transport... Cooperation with experts from various fields is necessary.

Summary

- μ -e conversion experiments are very important because it is sensitive to physics at high energy scales and allows us to explore the mechanism of the new physics even after the discovery of the event.
- In Japan and the U.S., though, the COMET and Mu2e experiment are just about to begin, we are starting to consider the design of the next experiments to be carried out after COMET Phase-II and Mu2e-II.
- The PRISM concept with a FFA muon storage ring has the potential to solve various difficulties in future experiments.
- We plan to obtain a joint project budget from Japan and the U.S. and begin revisiting the PRISM idea. We also plan to consider the use of PRISM for positive muon experiments.
 - Any advices and cooperation from FFA/accelerator experts is very important.
 - If you are interested, please join us.