

Conceptual Design of FFA for Super Heavy Element Production using ERIT

2023.9.14 y.ishi KURNS

Outline

1. Introduction
2. Super heavy element
3. Possibility of ERIT for SHE production
 - Validity of the ERIT scheme for SHE ring
 - **Stability of the beams with different charge state**
4. Summary

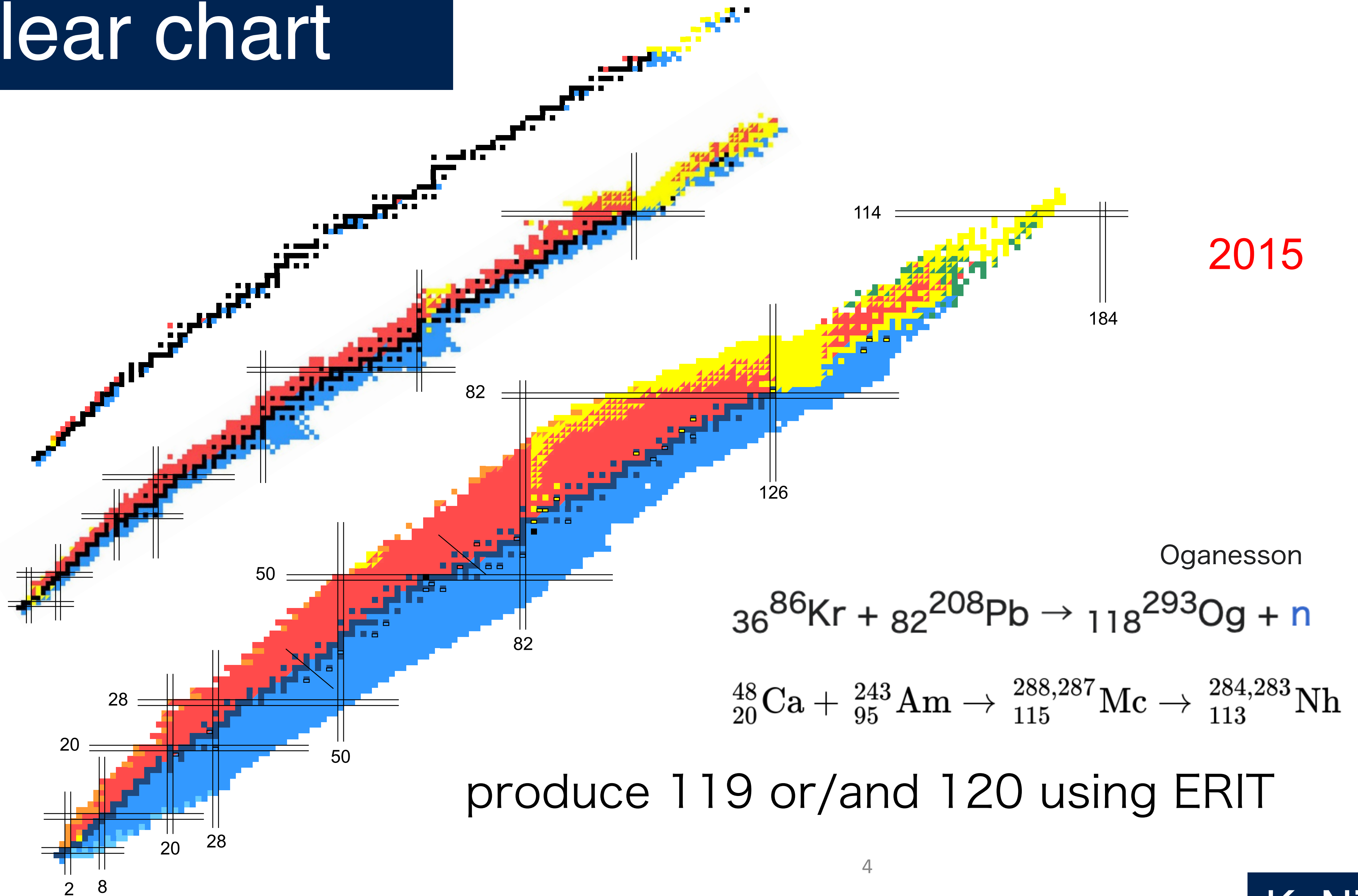
Introduction

1. It has been 14 years since the main ring started operation.
2. Machine operation has been stopped since March 2023.
3. Some users desire the beam from KURNS FFA, but No concrete plans for operation are in place.
4. The utilization plan of the entire facility and the future reuse of the FFAs are under consideration.
5. One of the main option is modification of the main ring to an ERIT ring for producing the super heavy element.

Nuclear chart

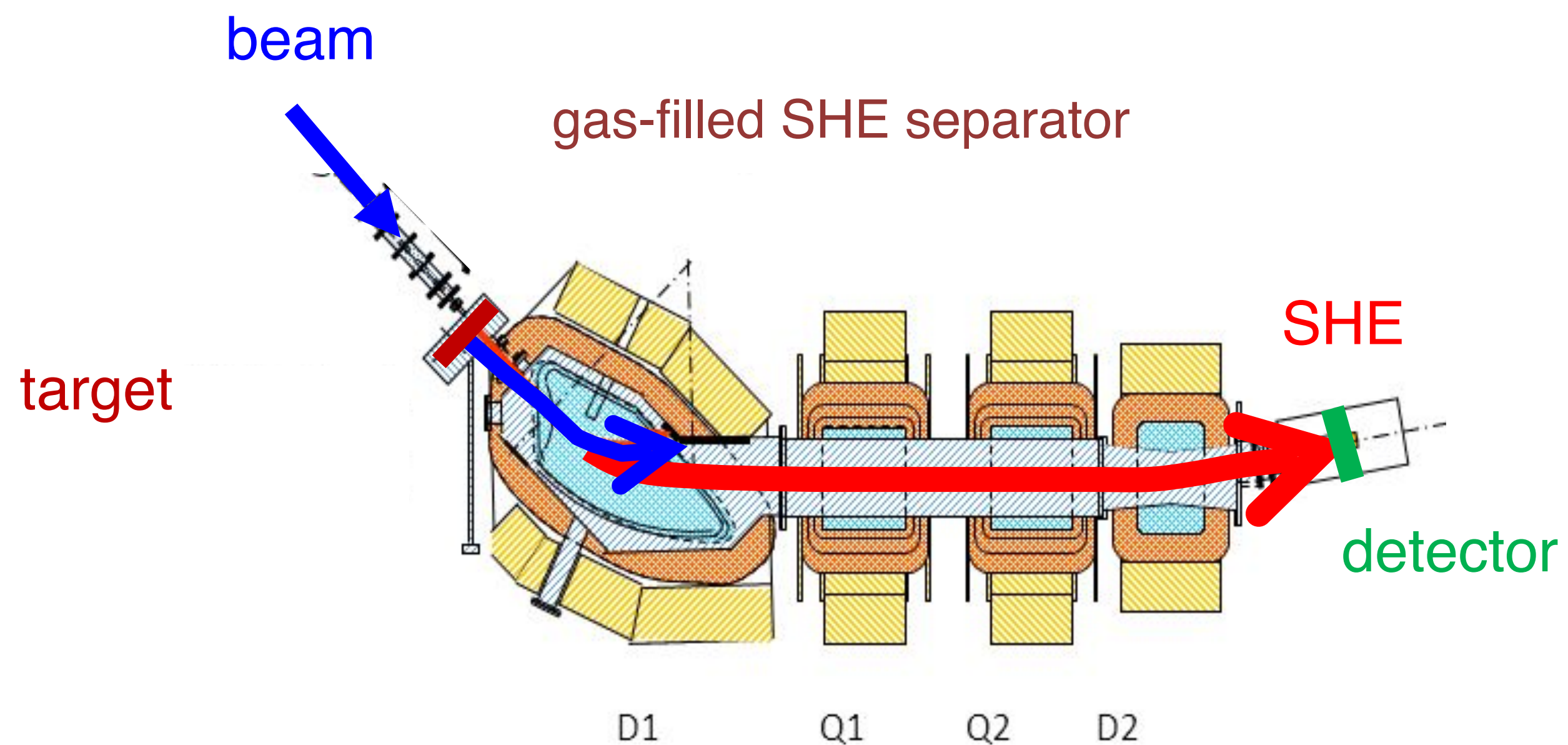
1935

1958



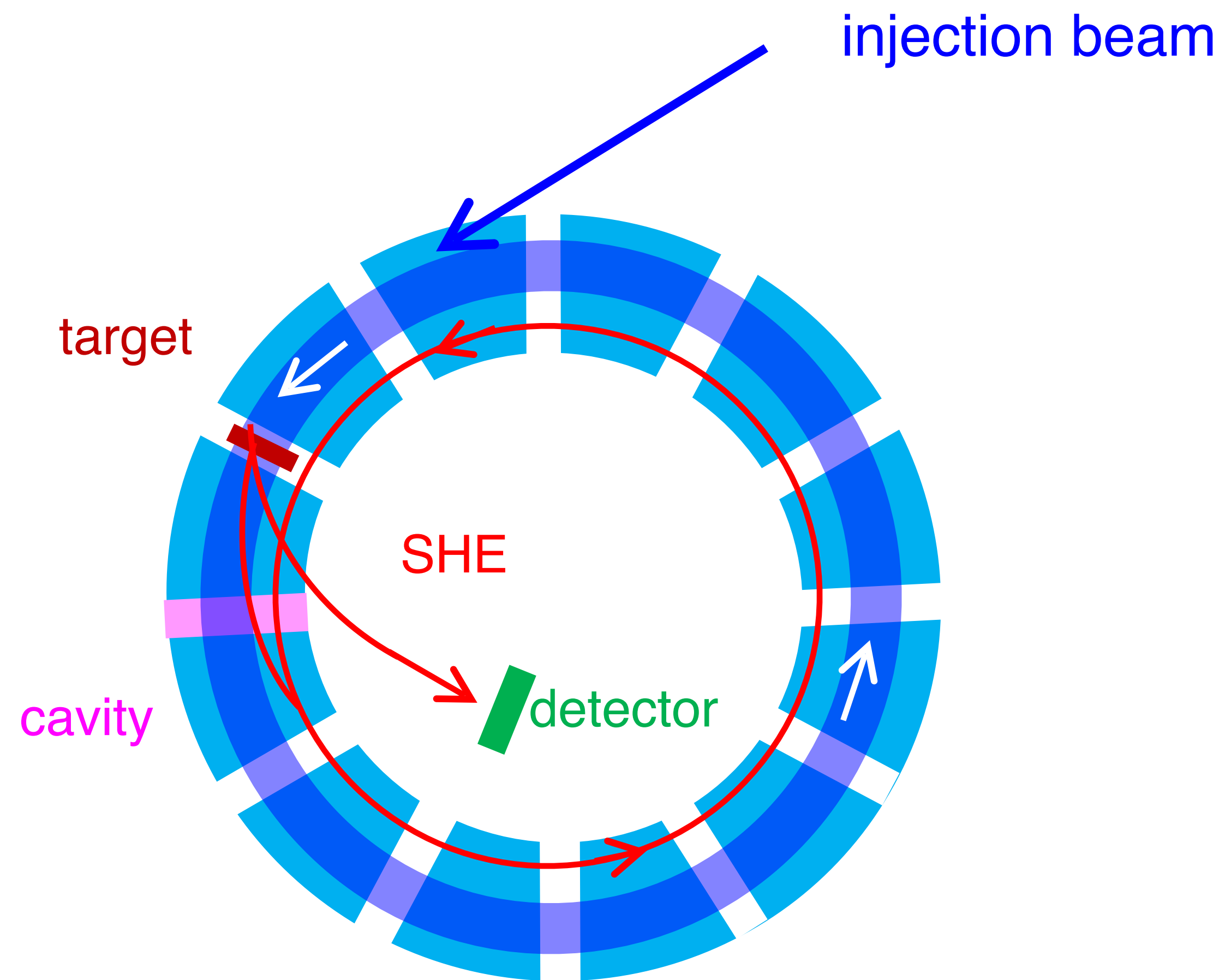
ERIT_SHE

conventional method



SHE: Super Heavy Element

new scheme



Beam species, target for SHE

test run



real run



ERIT_SHE

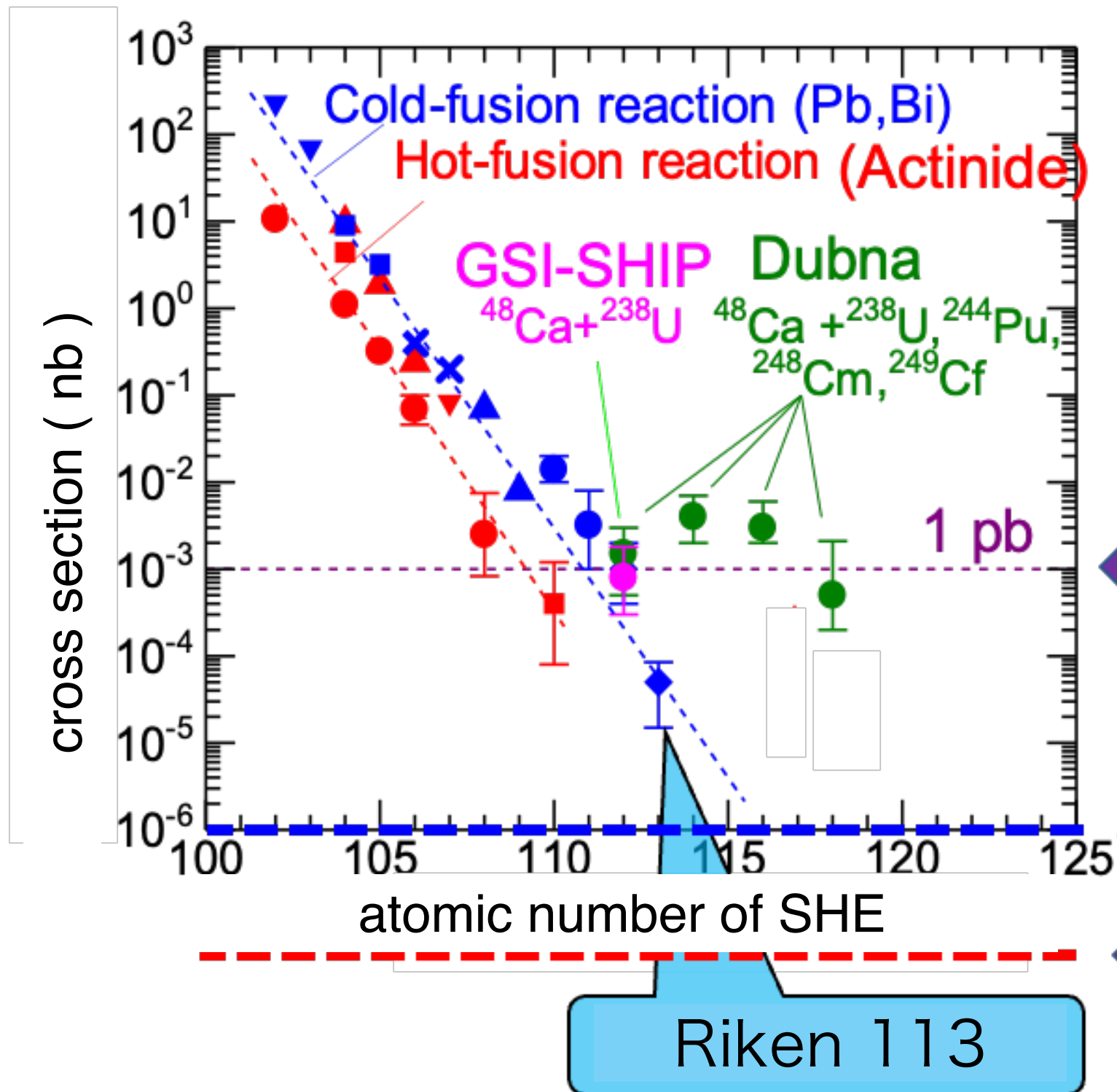
| target | beam | |
|----------------------------------------------|-----------------------|-----------------------|
| | Z=119 | Z=120 |
| ^{248}Cm (Z=96) 3.4×10^5 y | ^{51}V (23) | ^{54}Cr (24) |
| ^{249}Bk (Z=97) 327 d | ^{50}Ti (22) | ^{51}V (23) |
| ^{249}Cf (Z=98) 351 y | ^{45}Sc (21) | ^{50}Ti (22) |

assume ERIT can accumulate 1000 turns

1 pb one event per week using existing method

1 fb one event per 10 years using existing method

0.1 fb one event per month using ERIT

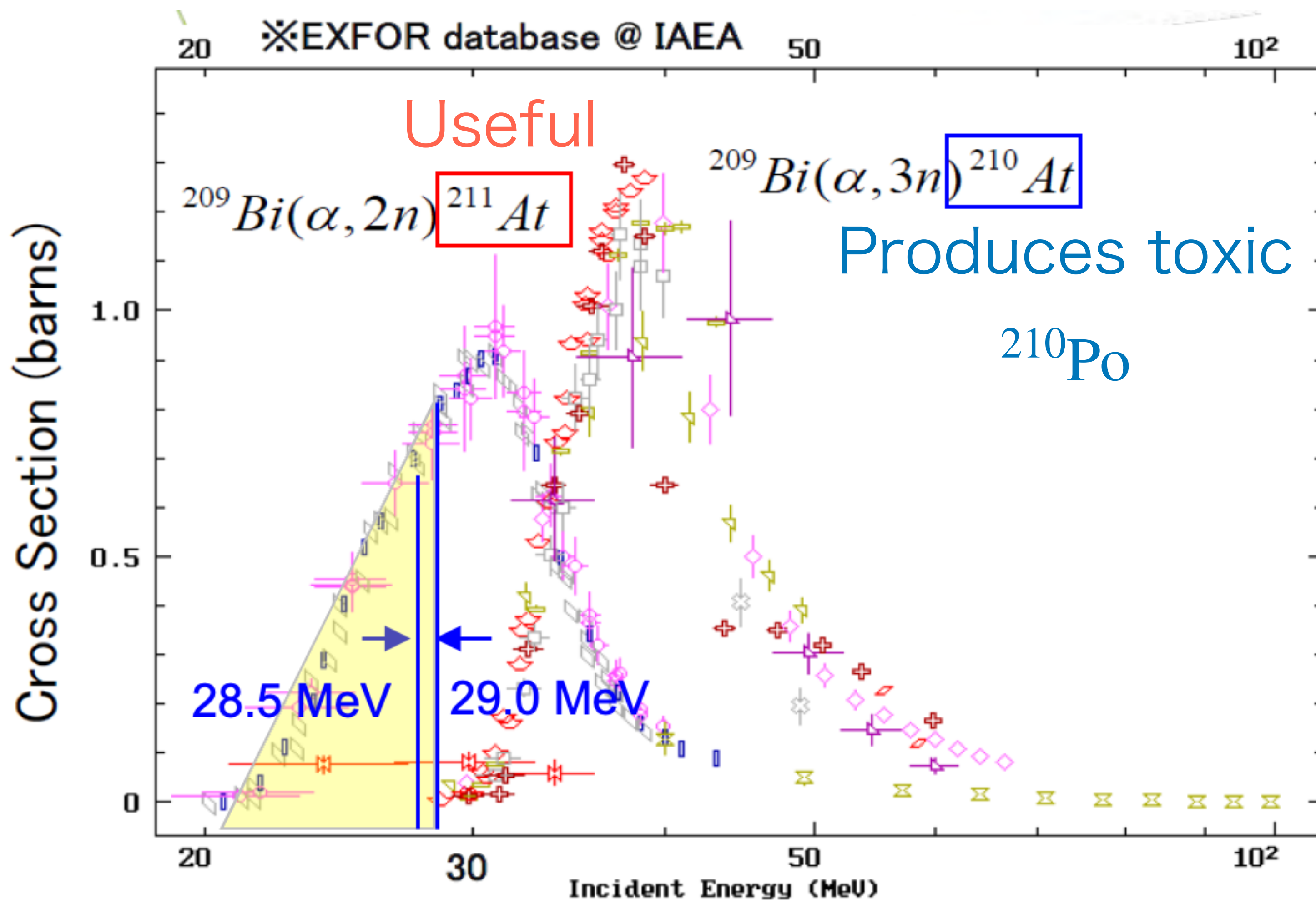




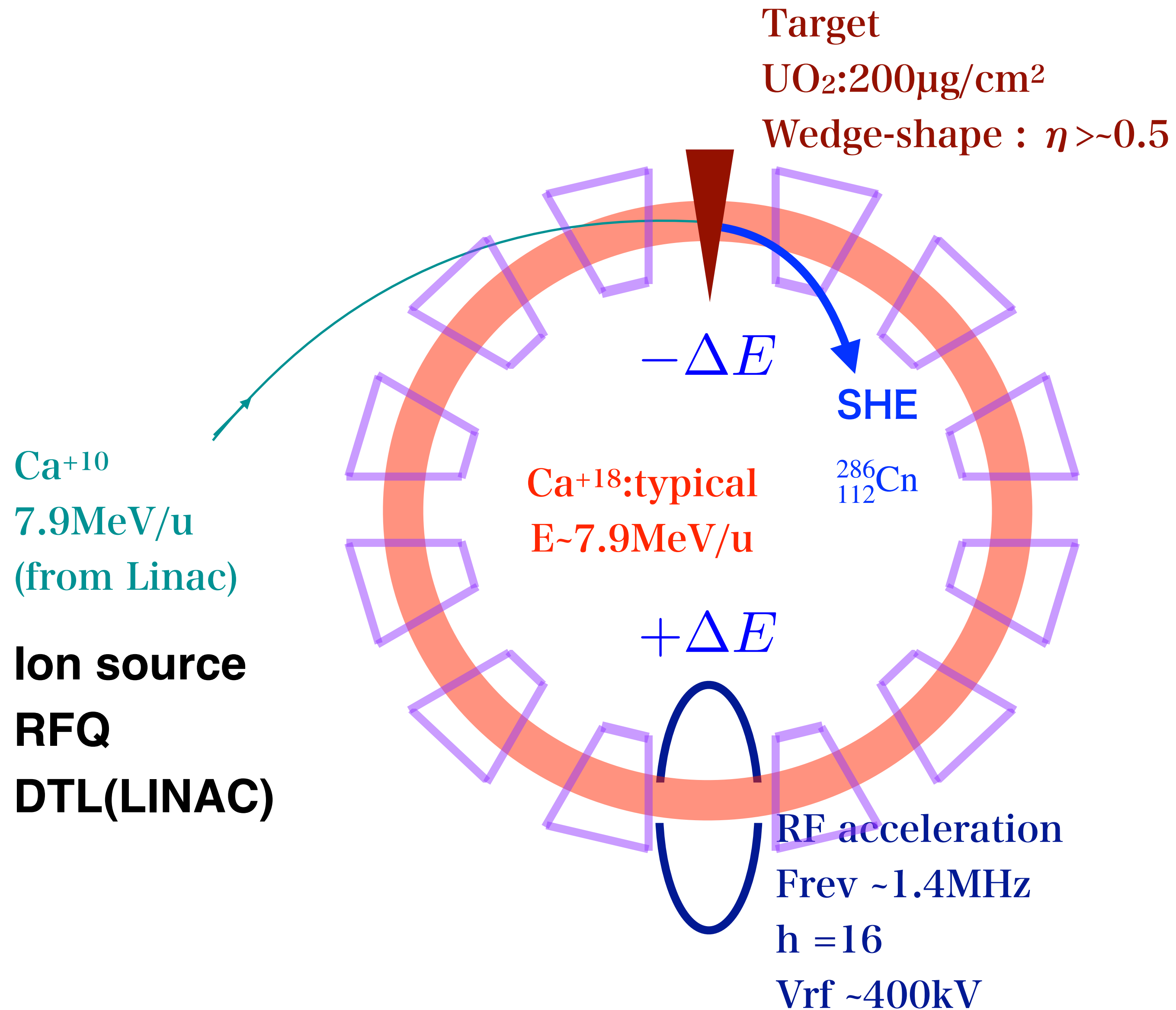
${}^{211}\text{At}$ can be produced using ${}^4\text{He}$ beam energies of 21 MeV to 29 MeV (${}^{209}\text{Bi}$ target 80 μm).

If the energy is higher than 29 MeV, the toxic ${}^{210}\text{Po}$ is produced and cannot be used.

The lifetime of ${}^{211}\text{At}$ is 7.2 hours and is produced after about 5 hours of irradiation.



ERIT_SHE scheme



Injection current : 1 pμA (6.25E12 pps)

assumption :

1000 turn survival

target thickness 200 μg/cm²

detection efficiency 10%

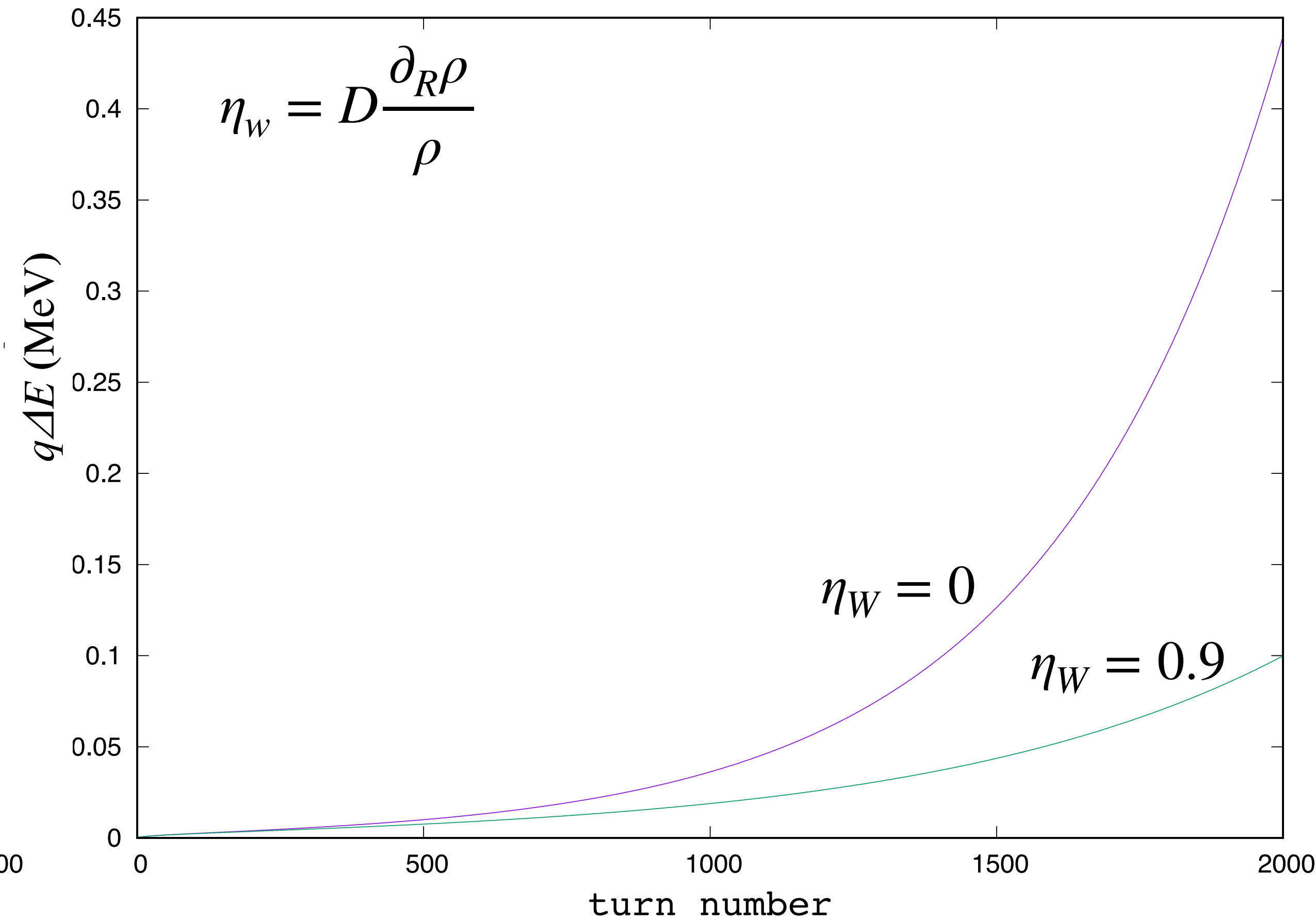
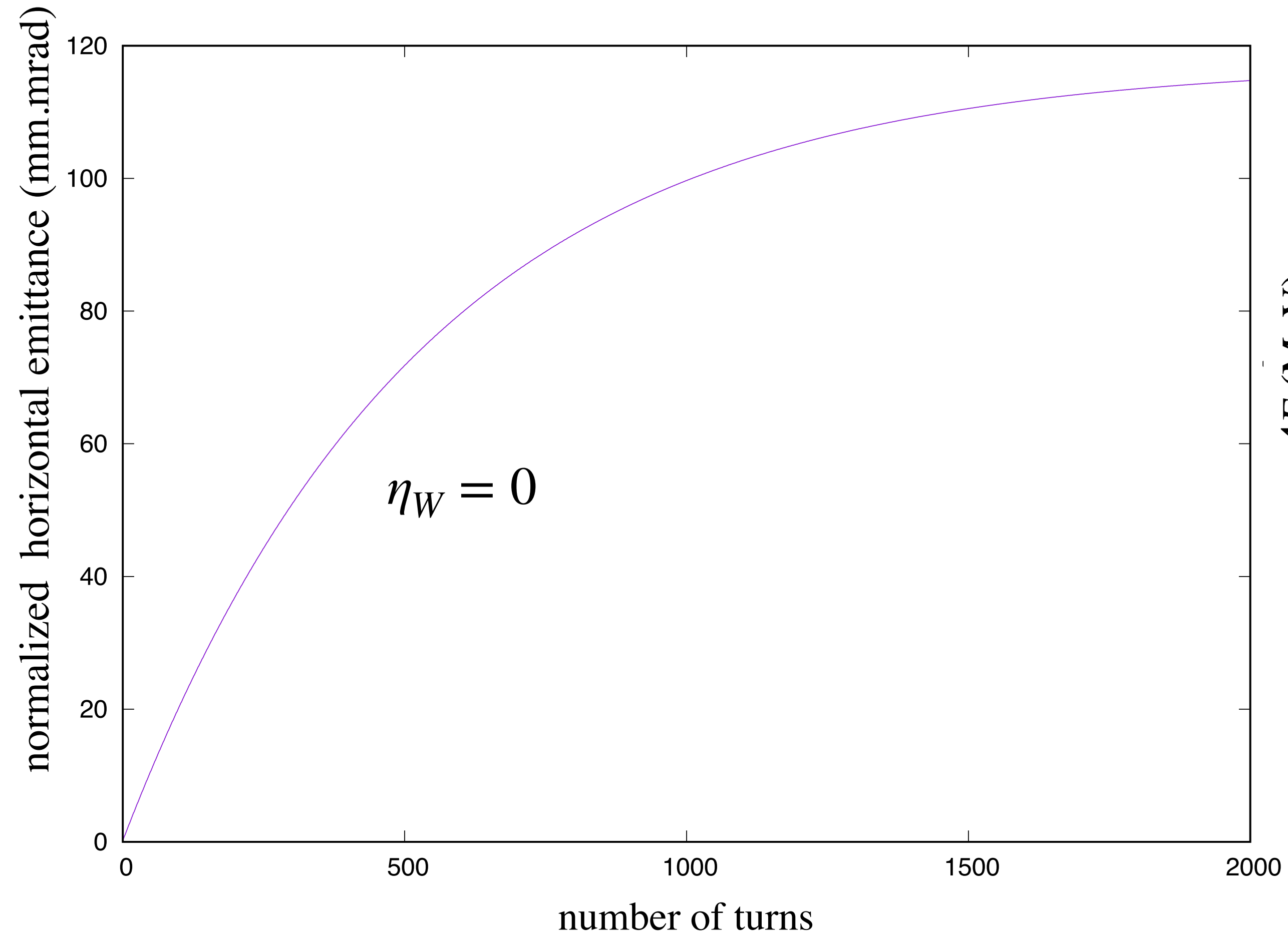
Can detect 1 SHE in every 38 days

Continuous injection

continuous production

continuous extraction

Growth of transverse emittance and energy spread



Summary of ERIT simulation

- Transverse emittance tends to constant value after 2000 turns due to the ionization beam cooling. $\rightarrow \epsilon_N = 115 \text{ mm.mrad}$
- As the beam cooling does not affect in longitudinal direction, energy spread increases. After 1000 turns $\rightarrow \langle \sigma_E \rangle \sim 50 * q \text{ keV}$
- Using wedge target, transverse-longitudinal coupling suppress the energy spread increase. $\eta = 0.9 \rightarrow \epsilon_N \sim 350 [\text{mm.mrad}]$, $\langle \sigma_E \rangle \sim 20 * q \text{ keV}$
 - Capable in terms of the ring acceptance.
- Cavity voltage
 - Assuming the target thickness is $200 \mu\text{g}/\text{cm}^2$, Energy loss $\sim 36 \text{ MeV/turn}$ ($h=16$).
 - cf. R.T. rf cavity ($\sim 10 \text{ MHz}$) $V_{\text{rf}} \sim 400 \text{ kV}$ (in ERIT case)

closed orbit of different charge state(static)

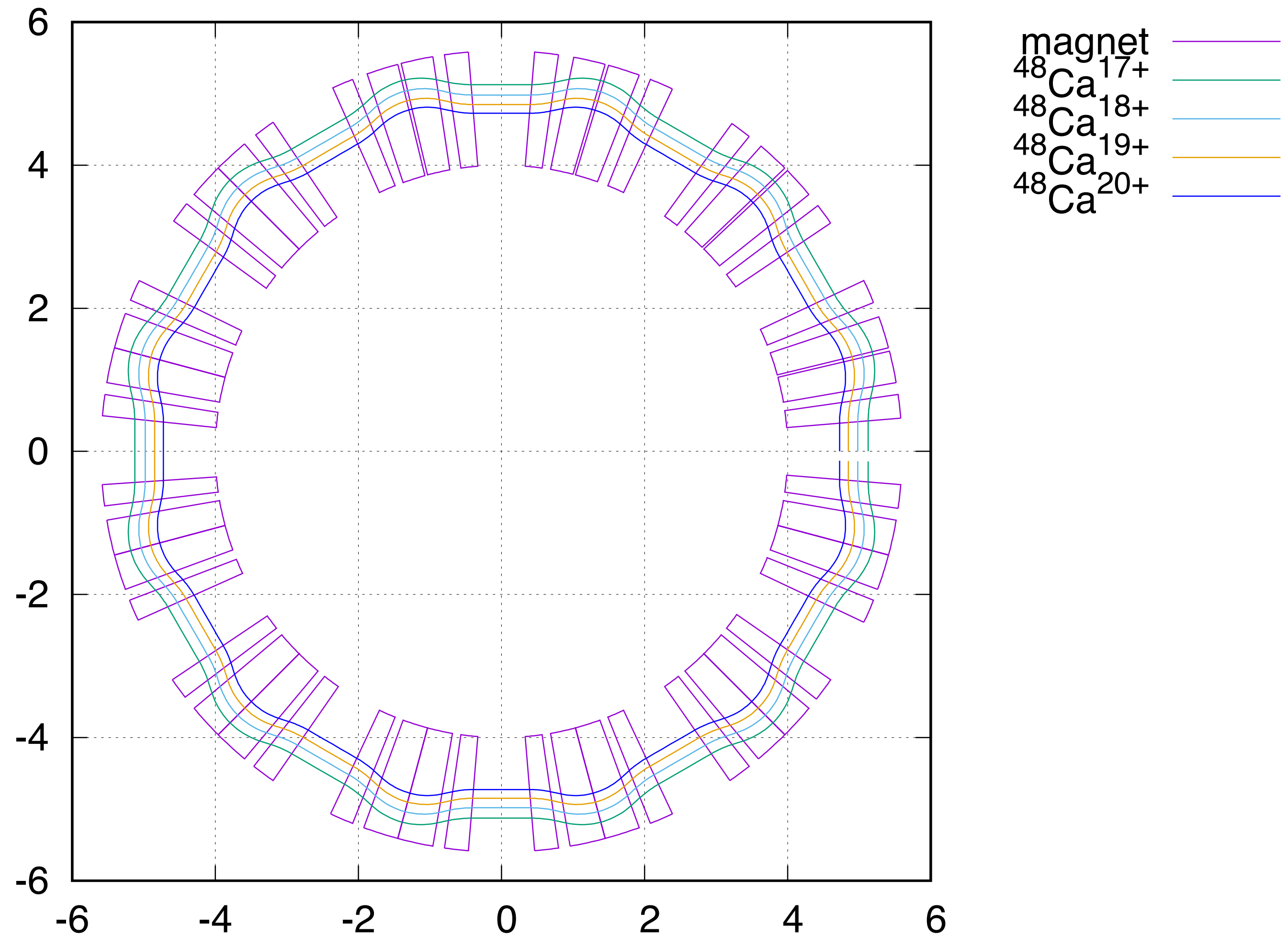
- Scaling FFA

$$\frac{r}{r_0} = \left(\frac{q_0}{q} \right)^{1/k}$$

- cf. $k=1$

- $q_0=+18, q=+19$

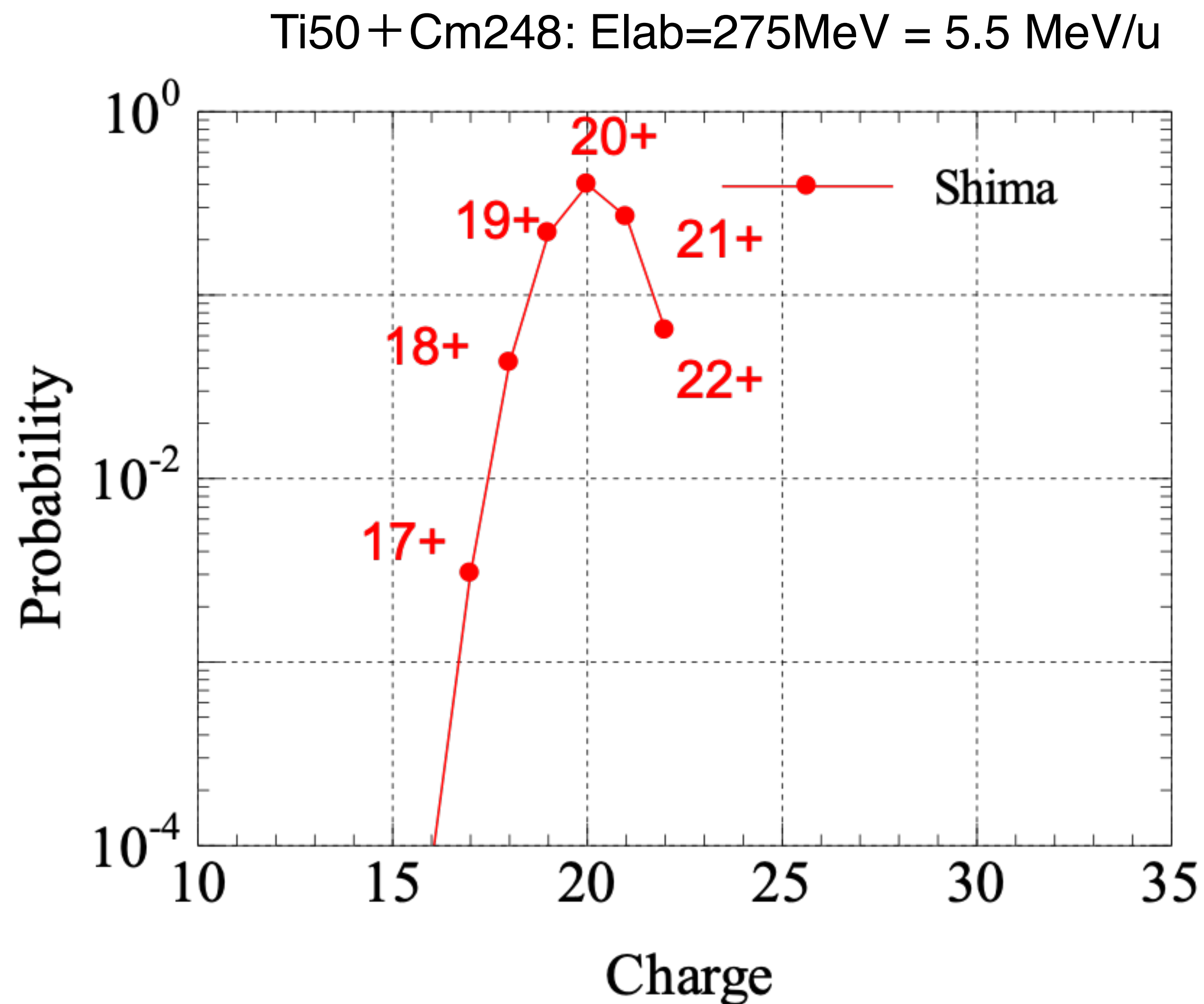
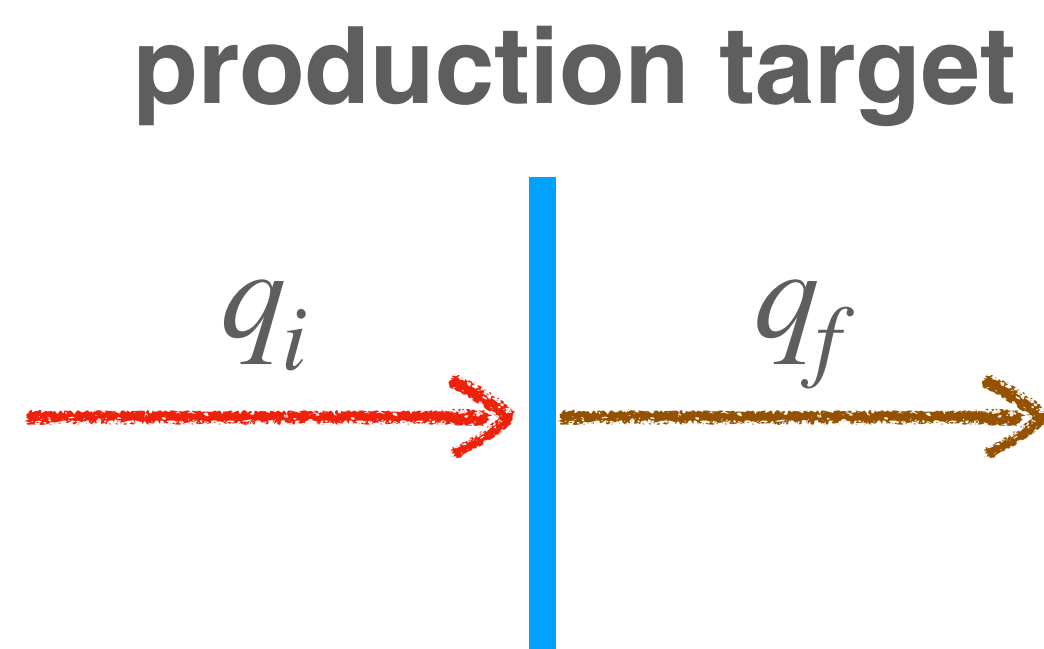
- $\rightarrow r/r_0=0.95$ $r_0=4\text{m} \rightarrow 3.8\text{m}$



From the ring, beams with different charges appear to have different momenta.

charge state distribution

- Initial charge state q_i will be changed into the state q_f passing thru the production target.
- Final charge state q_f is determined statistically by the probability distribution regardless the initial state q_i .

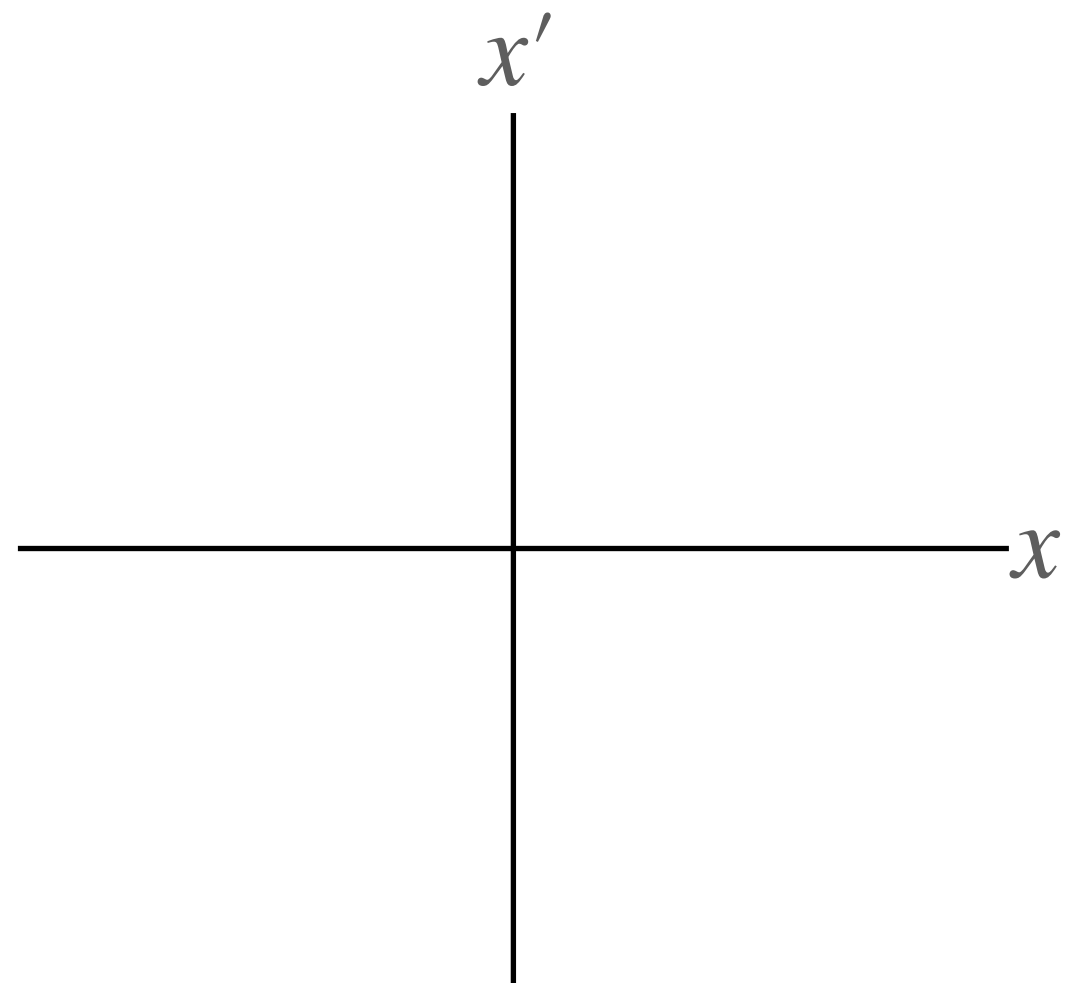


amplitude change due to charge state transition

- **Suppose the case of charge changing e.g. $+20 \rightarrow +22 \rightarrow +19$**

amplitude change due to charge state transition

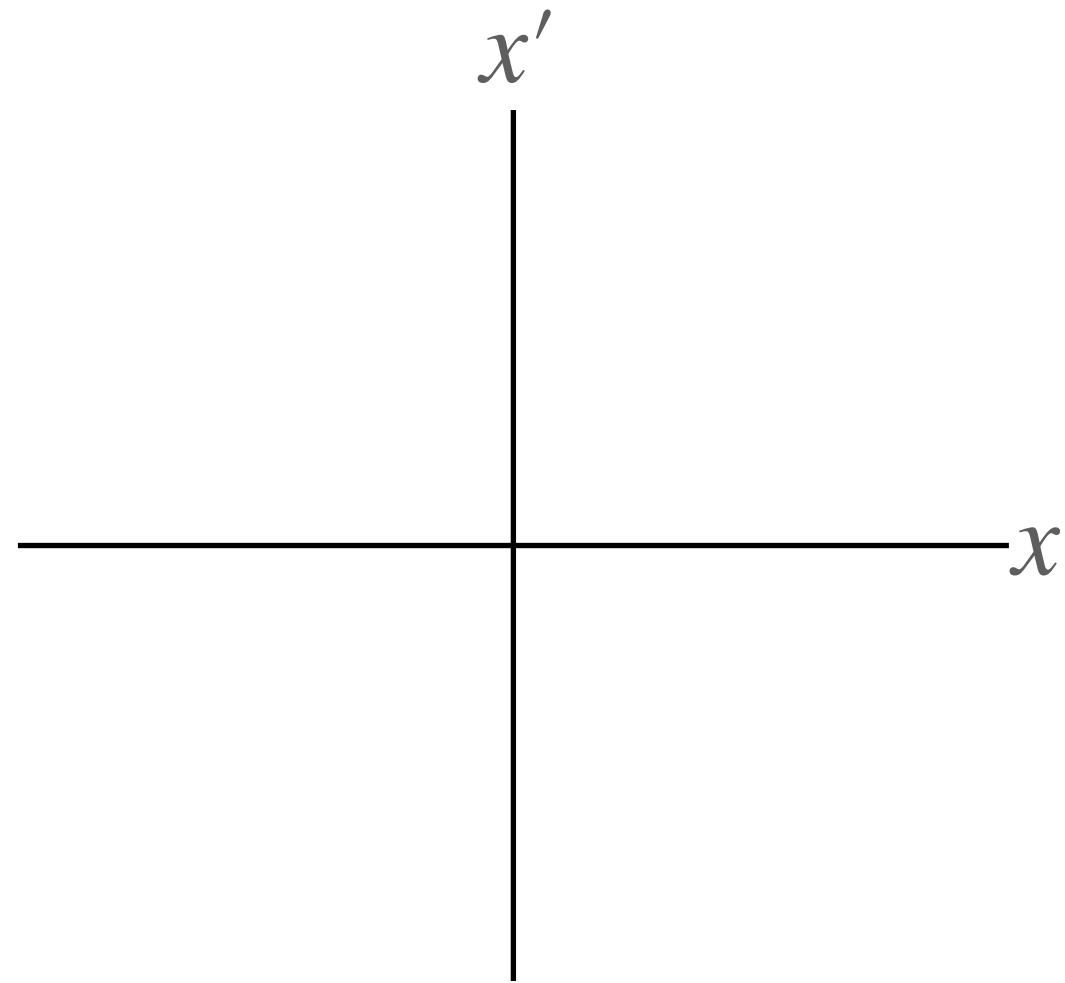
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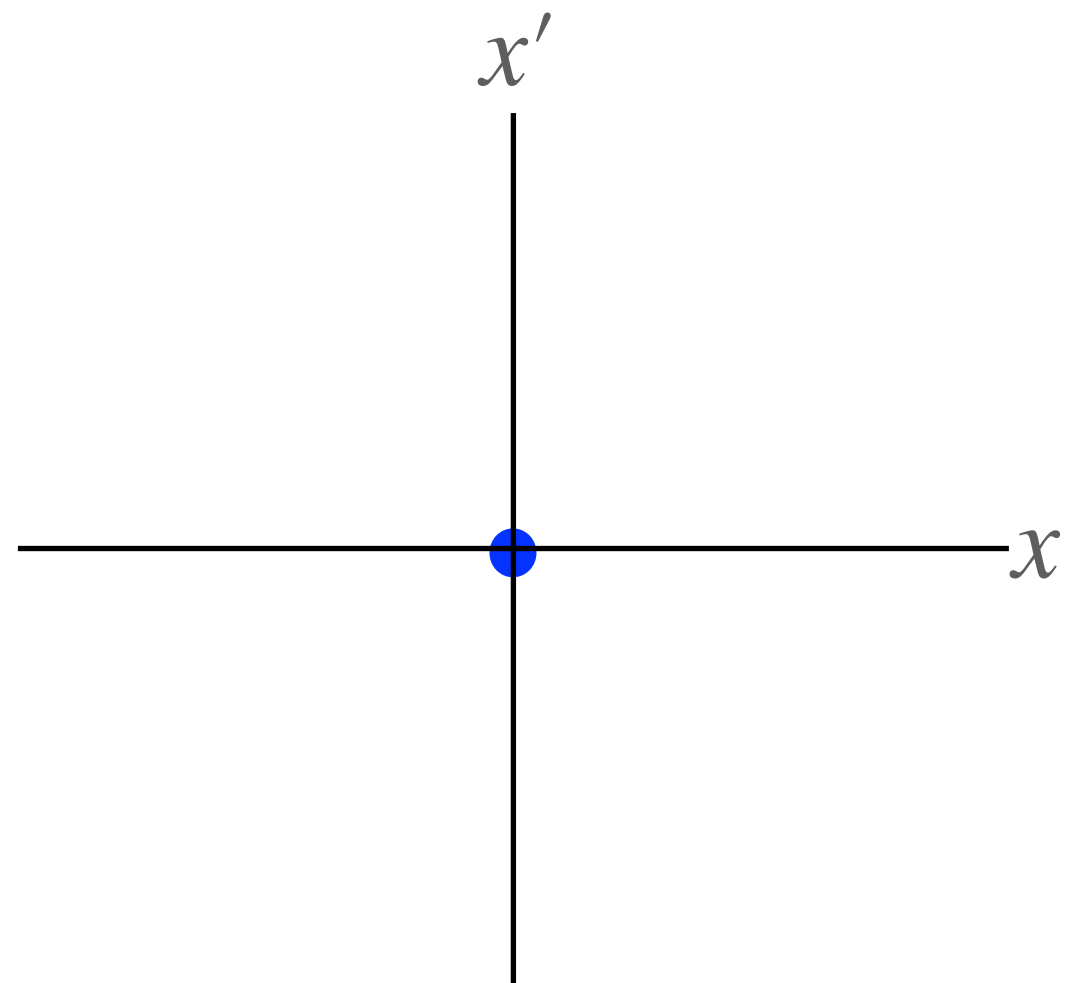
$$q = +20$$



amplitude change due to charge state transition

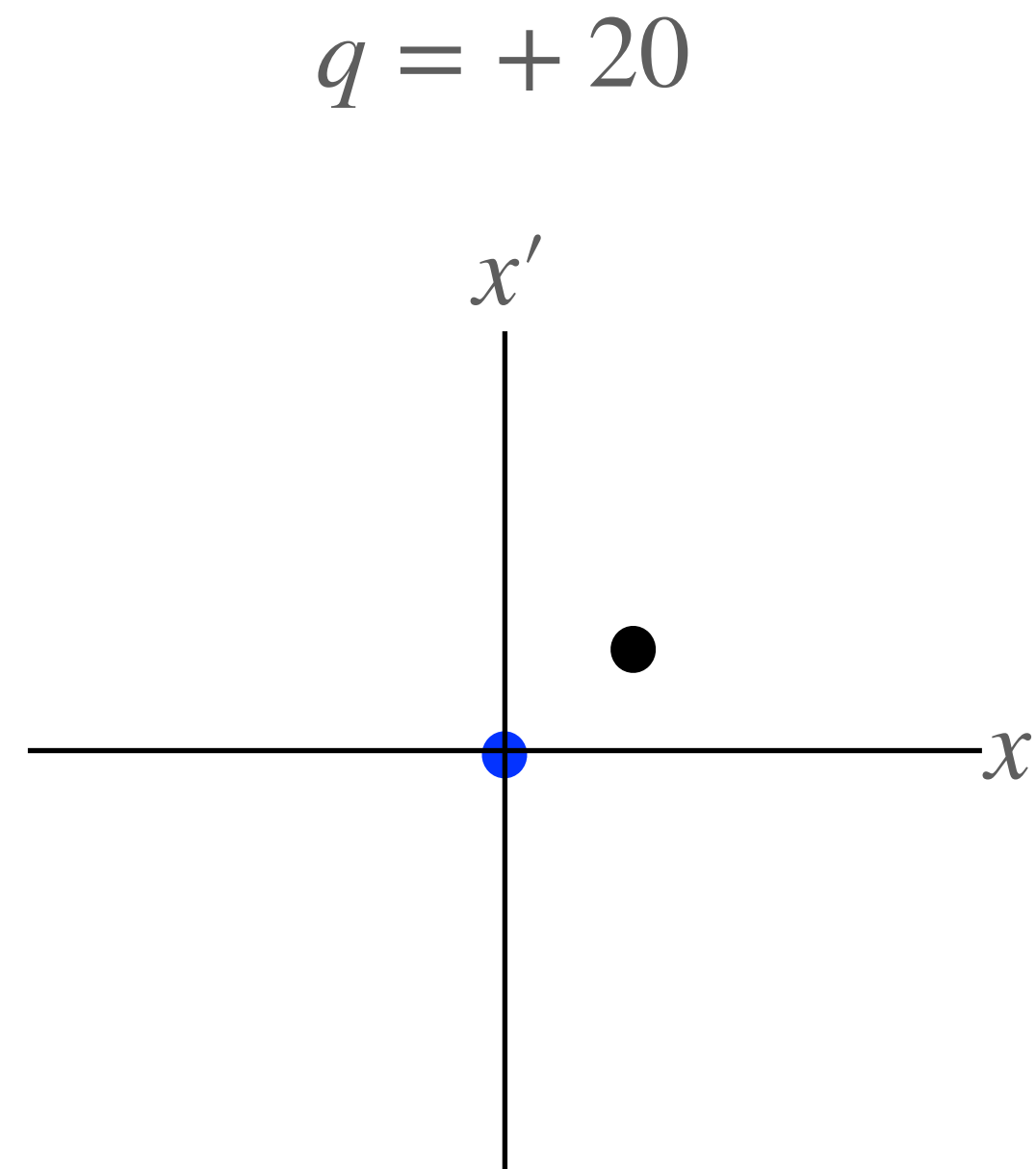
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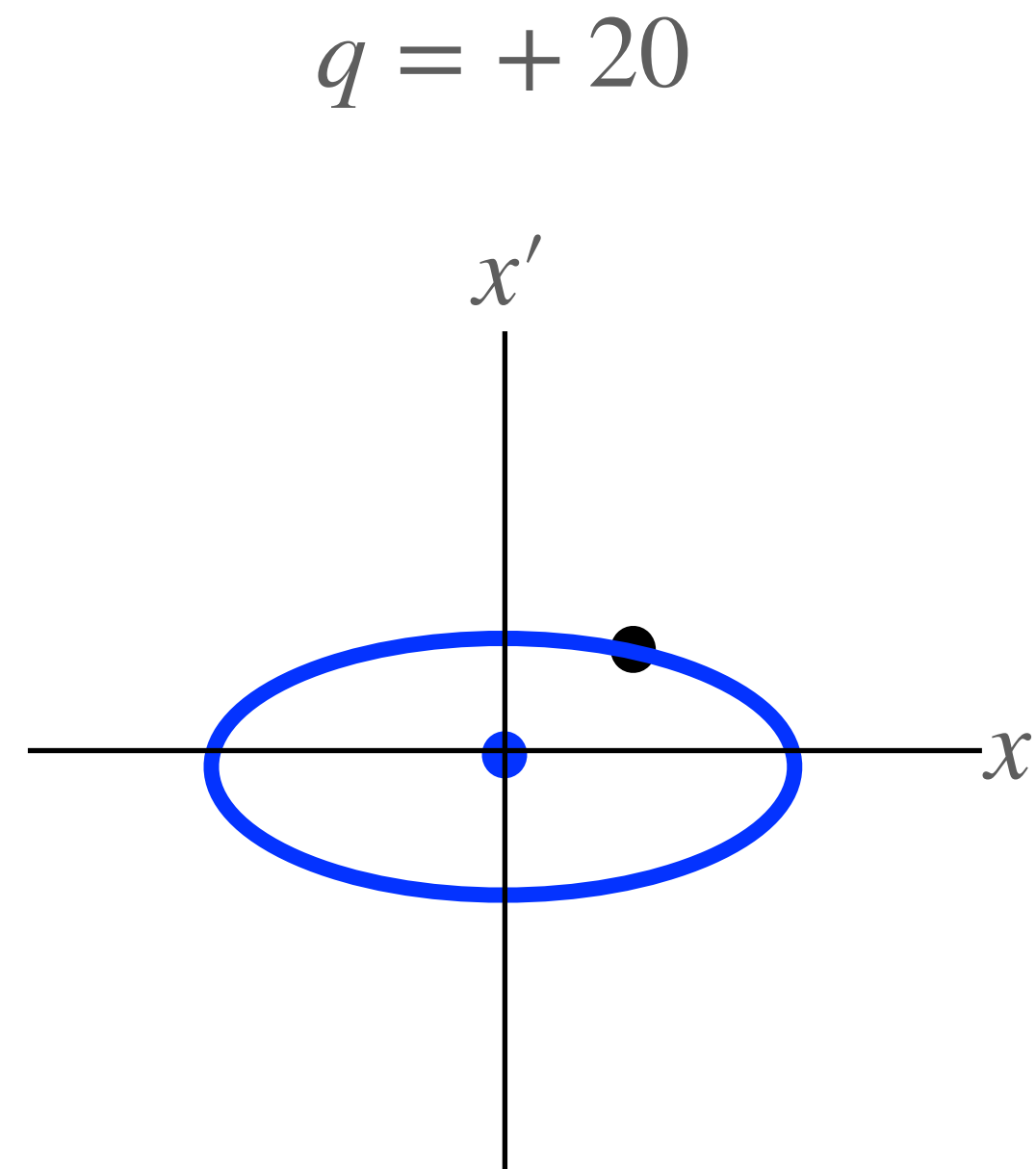
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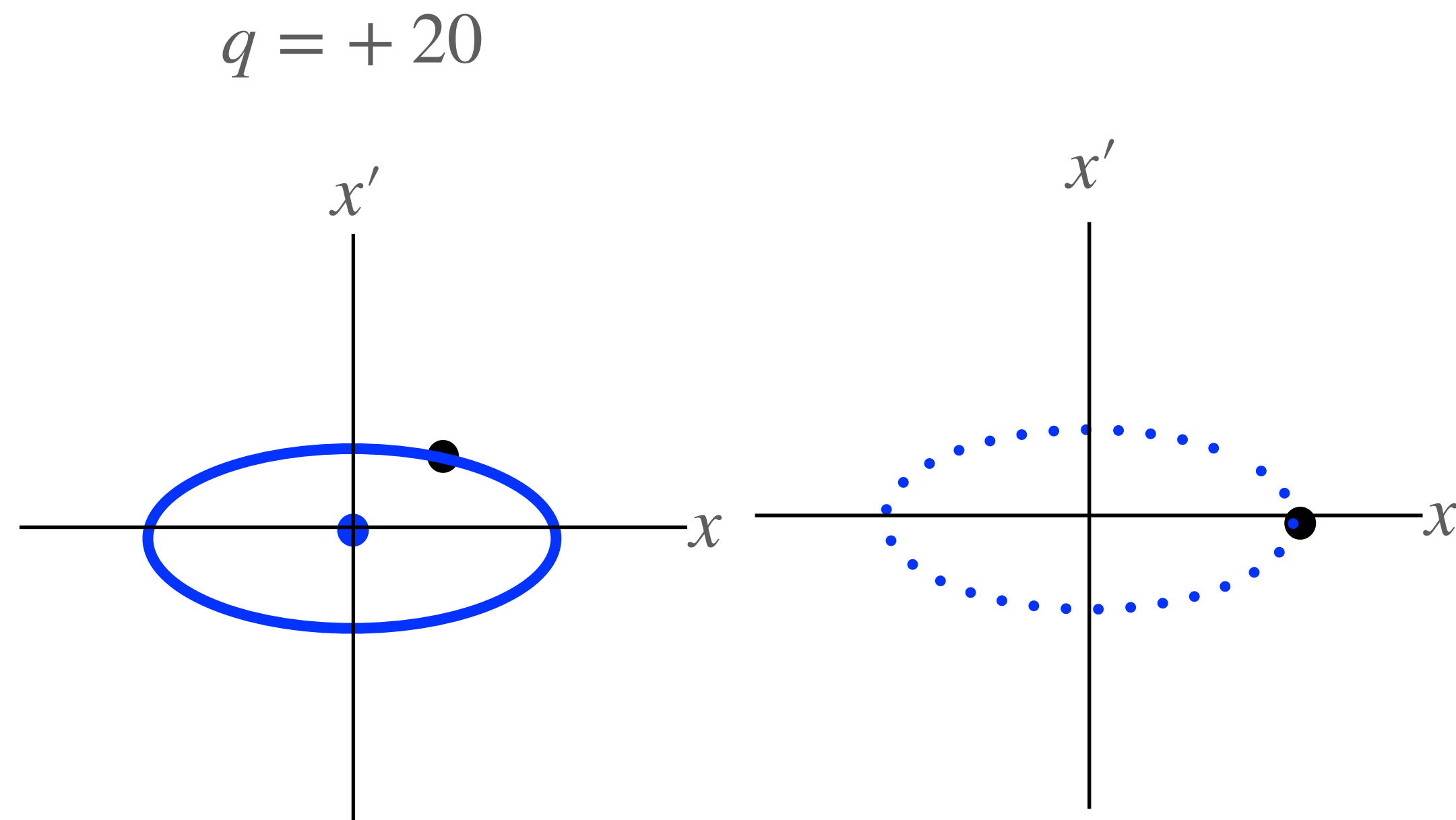
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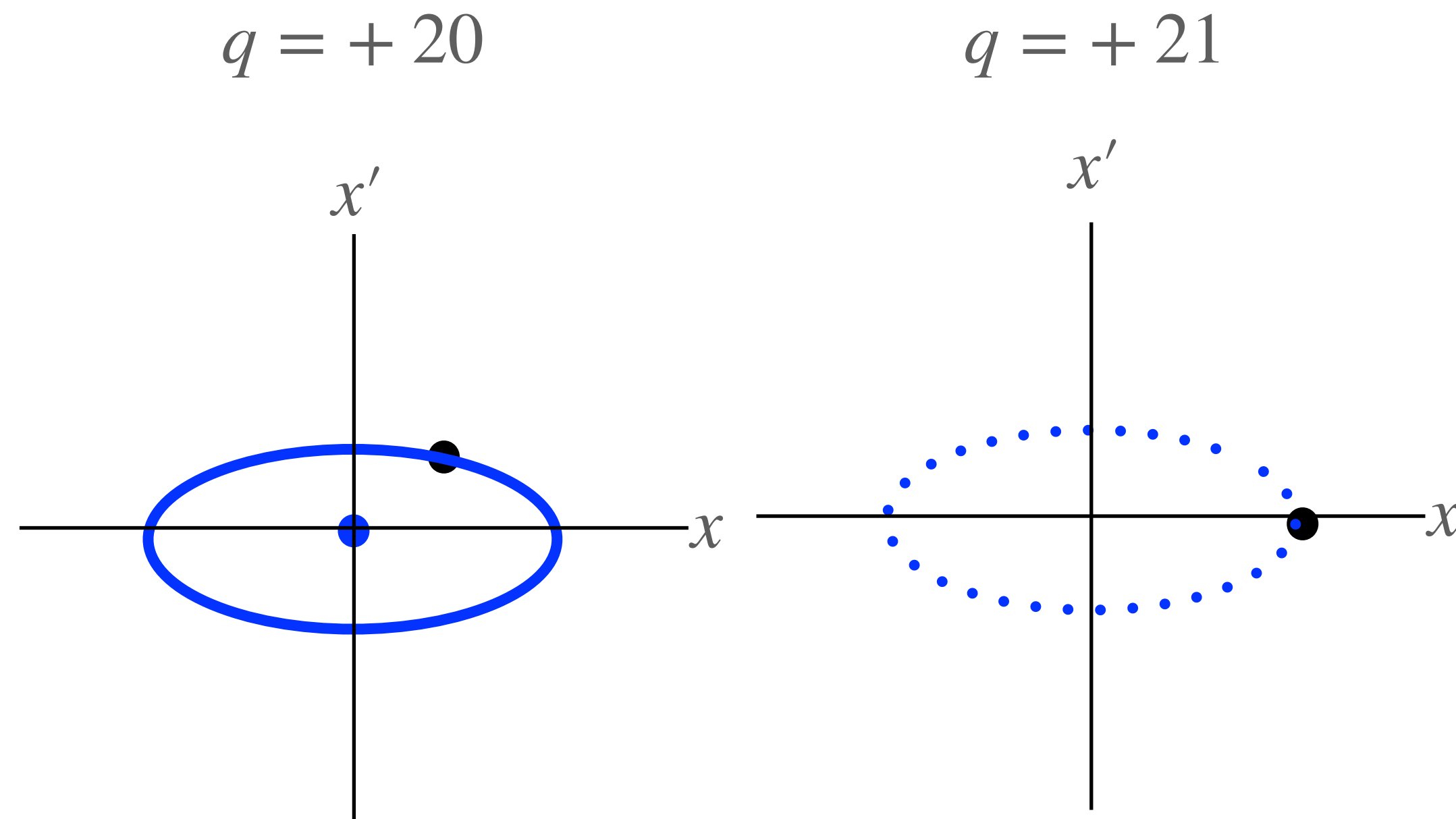
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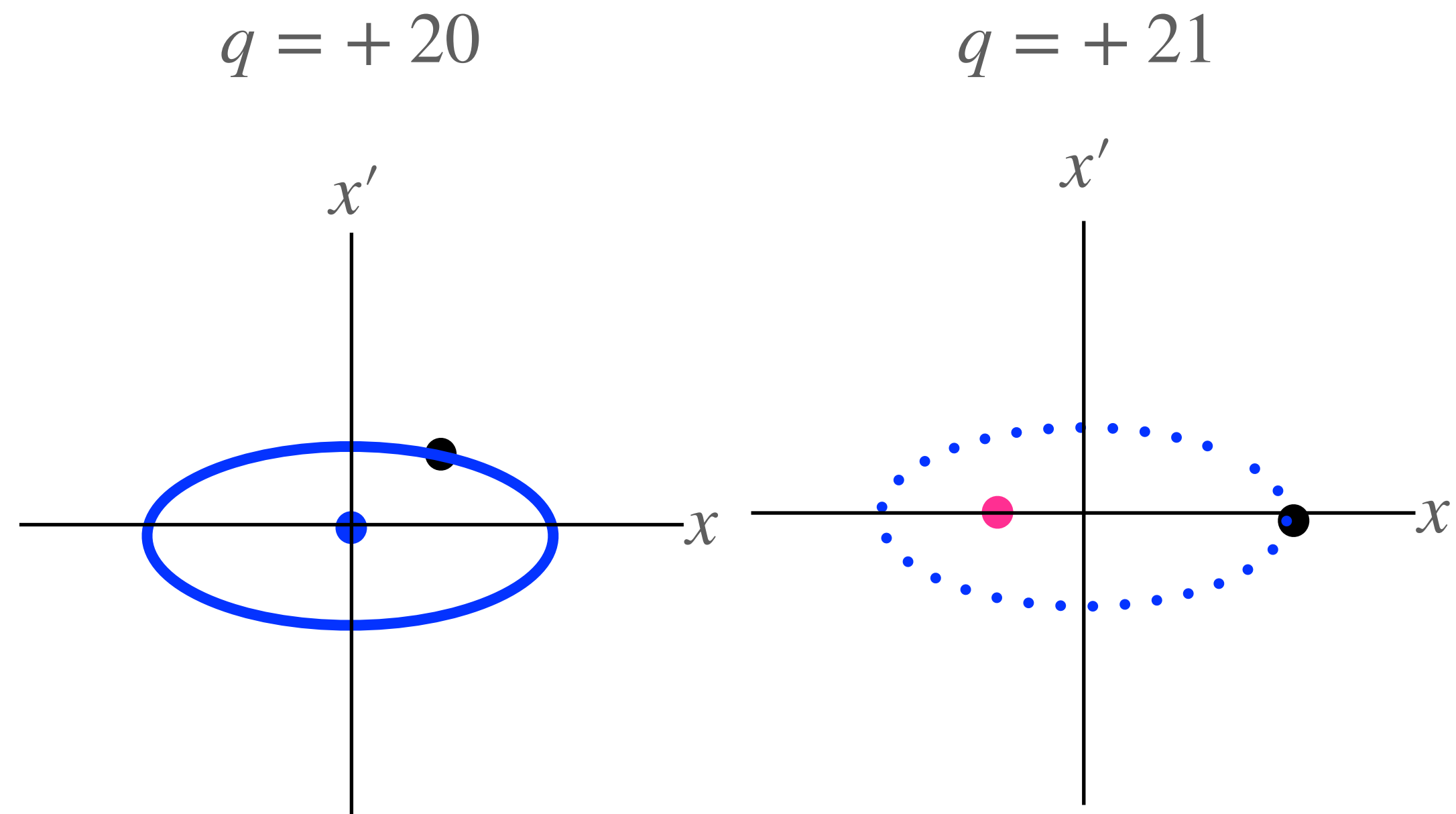
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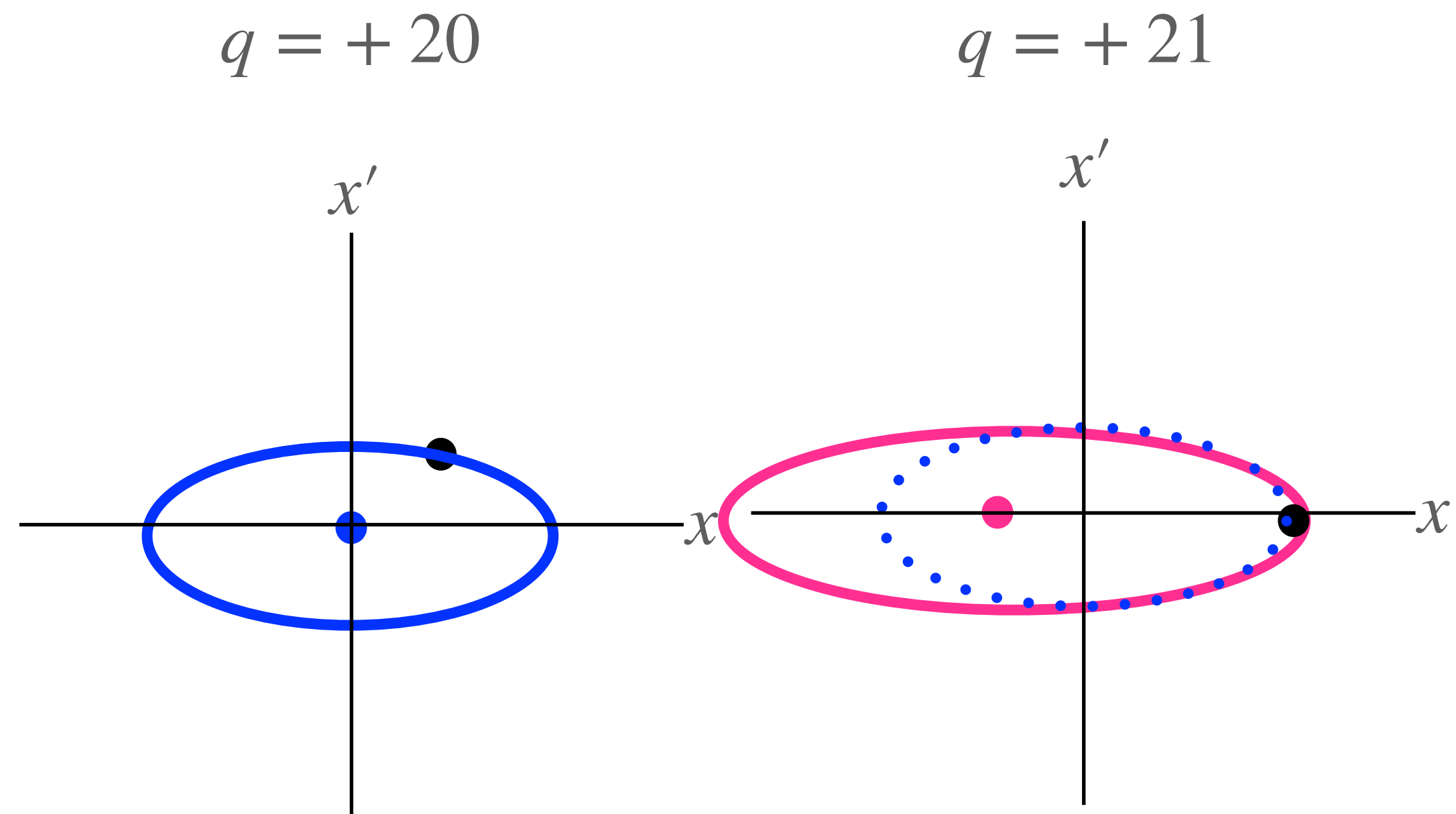
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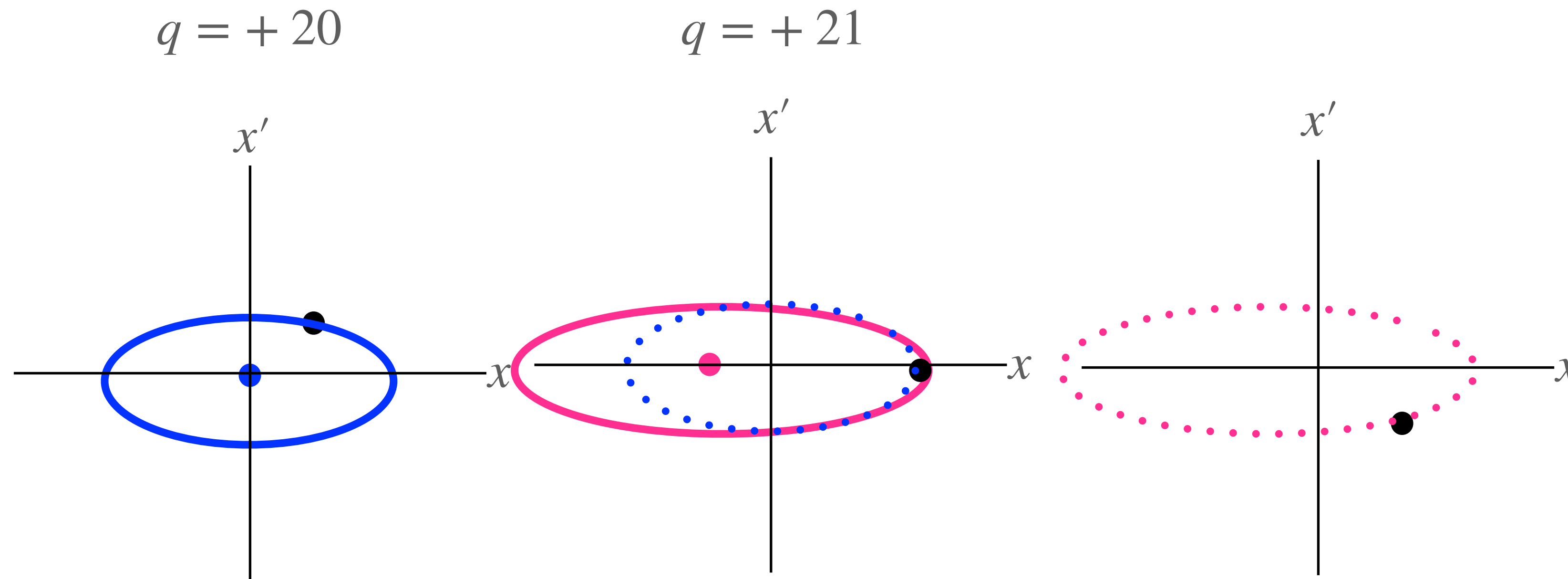
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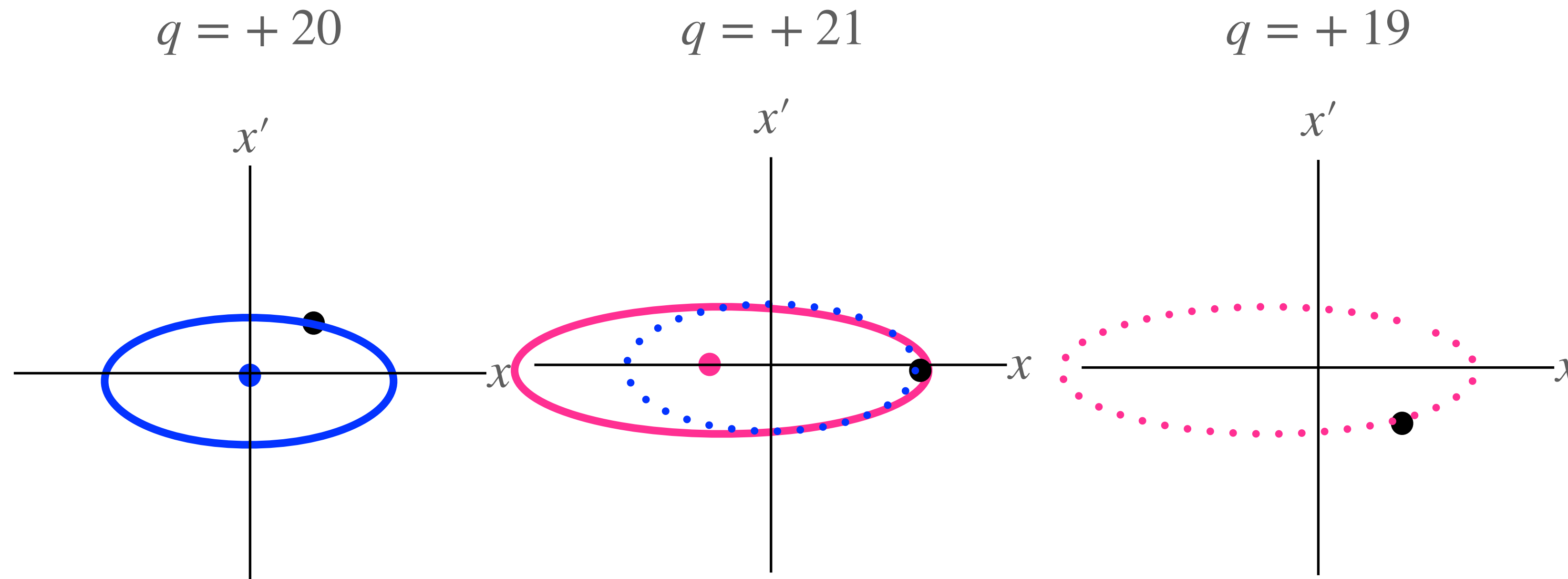
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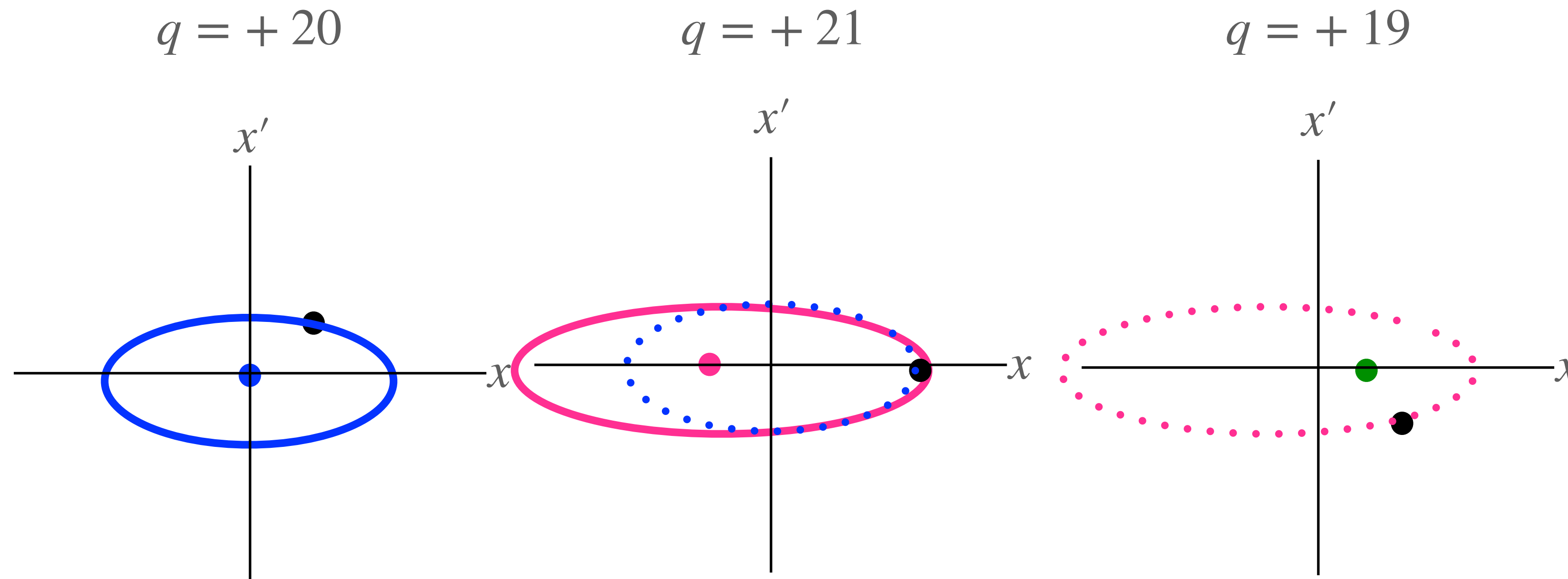
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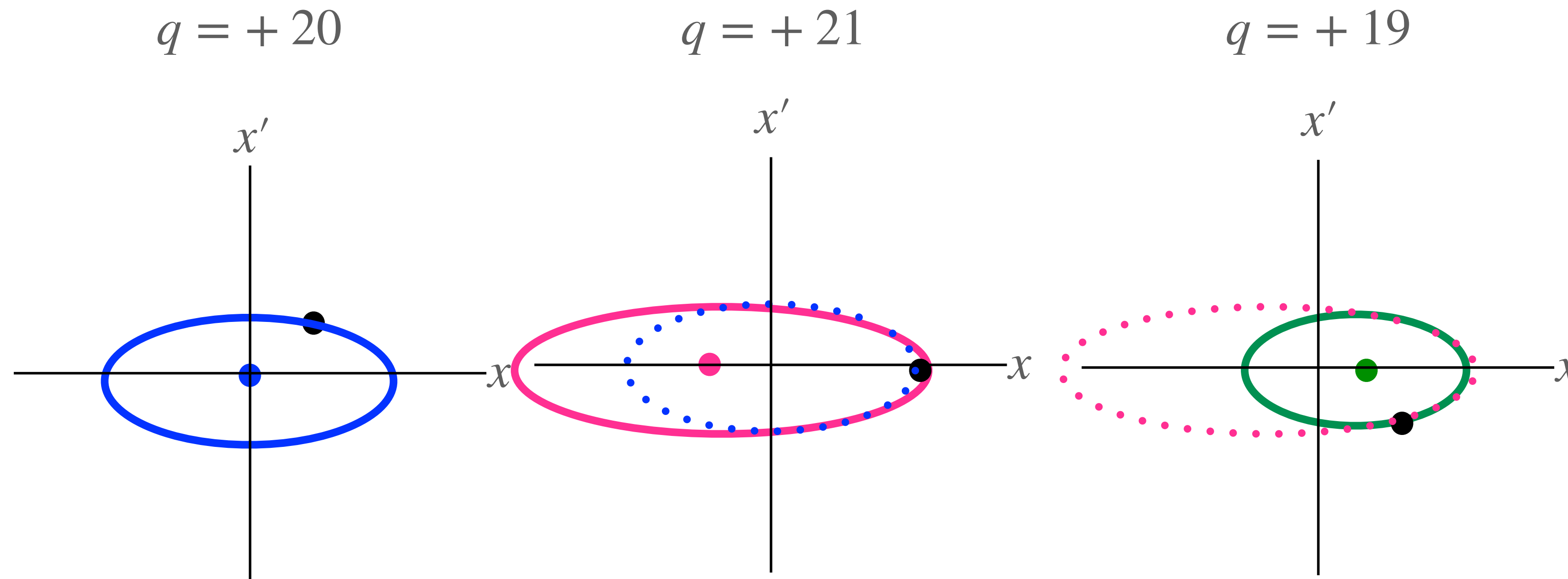
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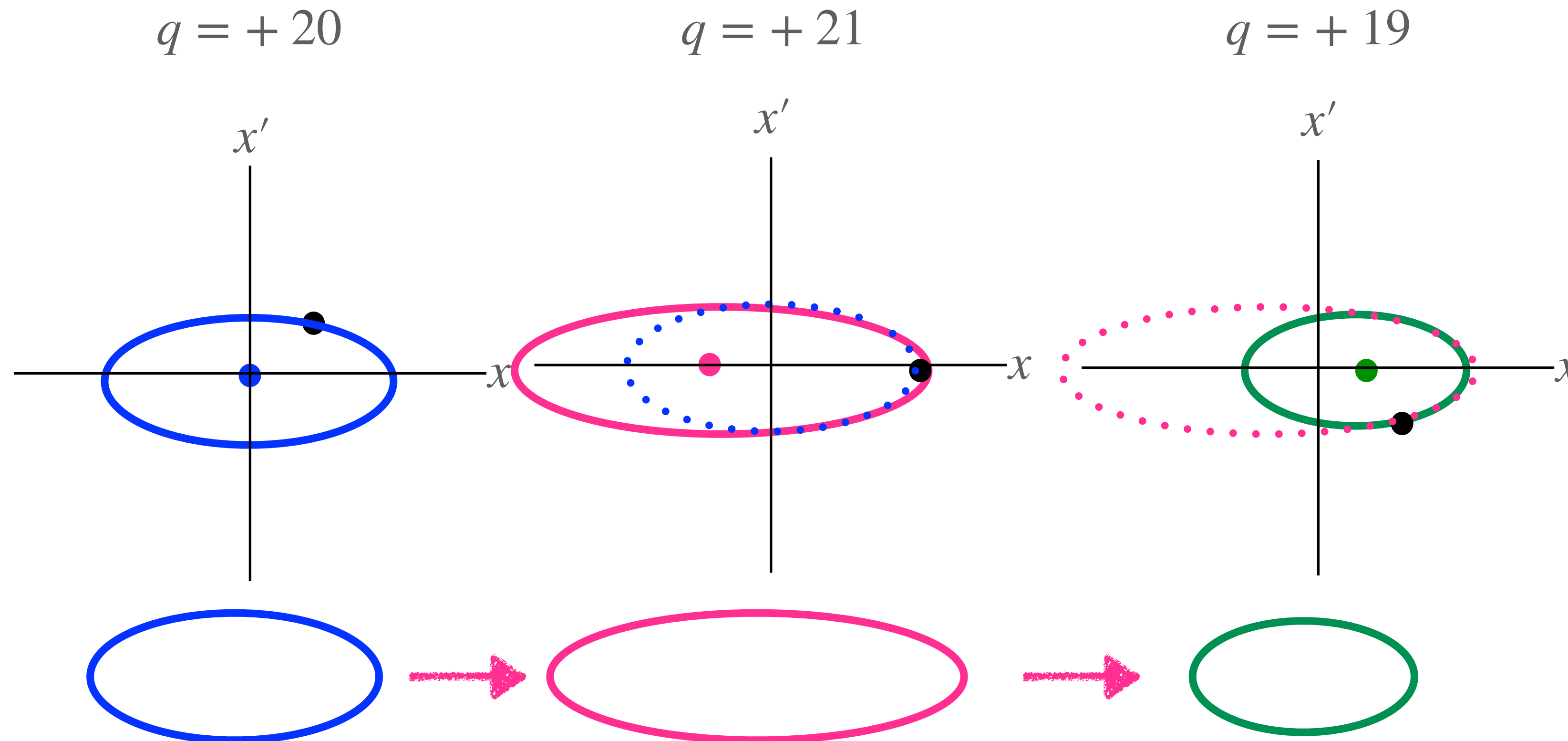
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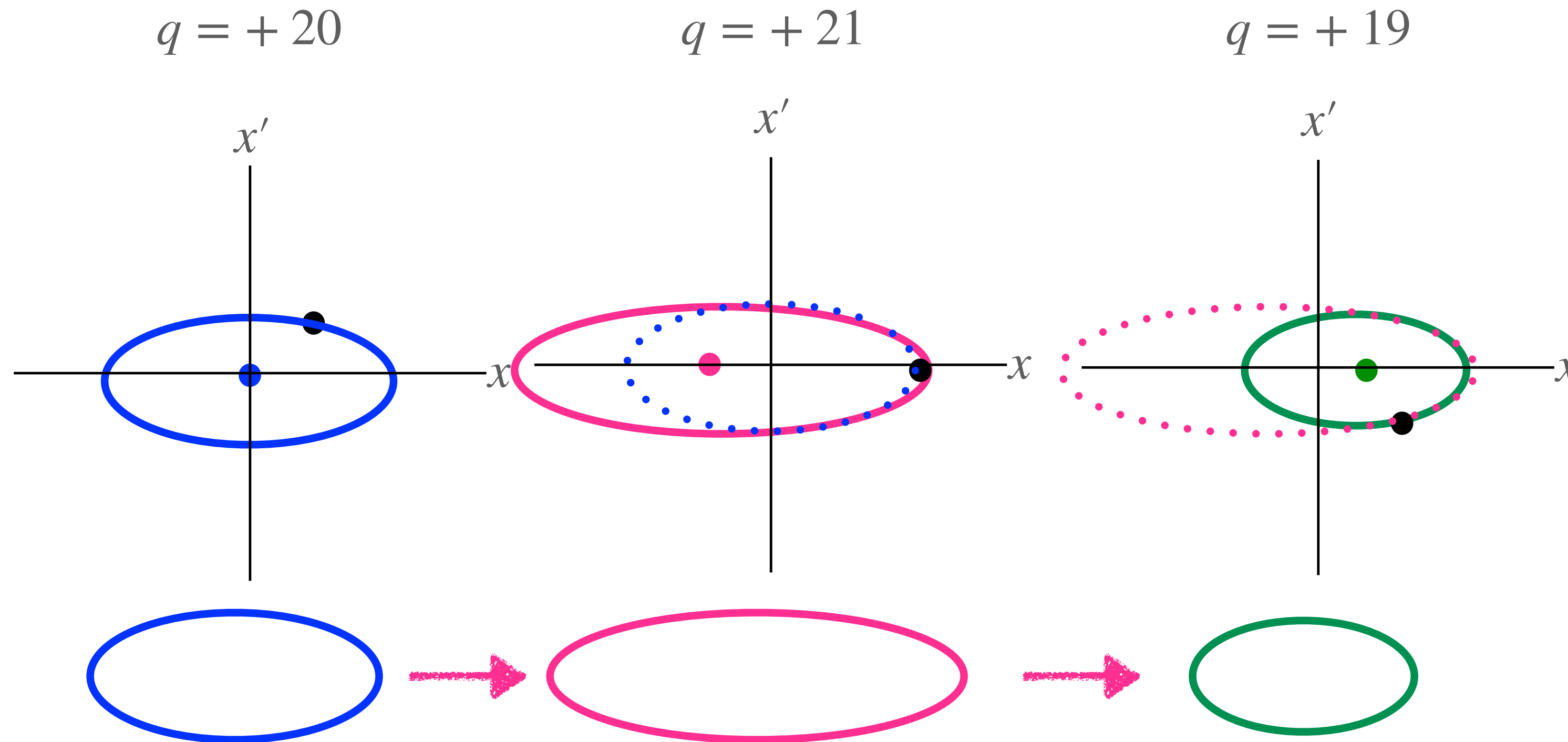
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amplitude change due to charge state transition

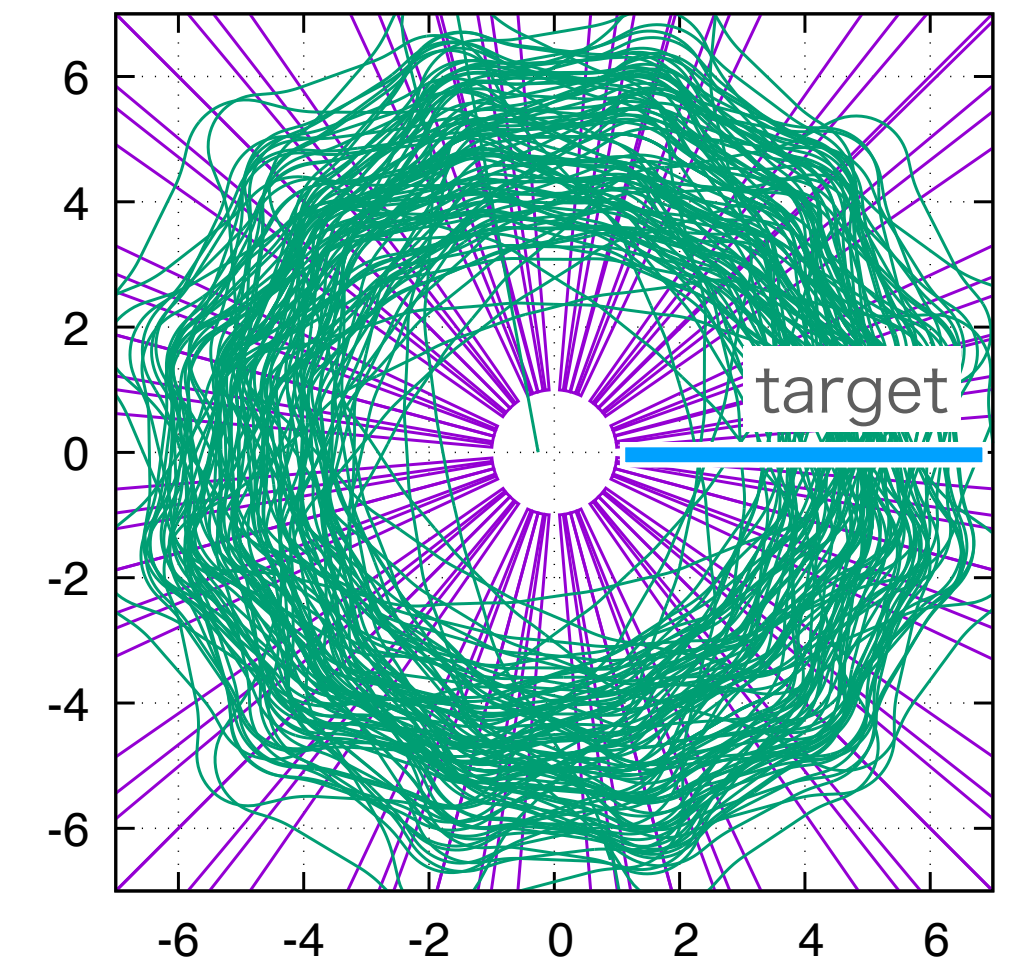
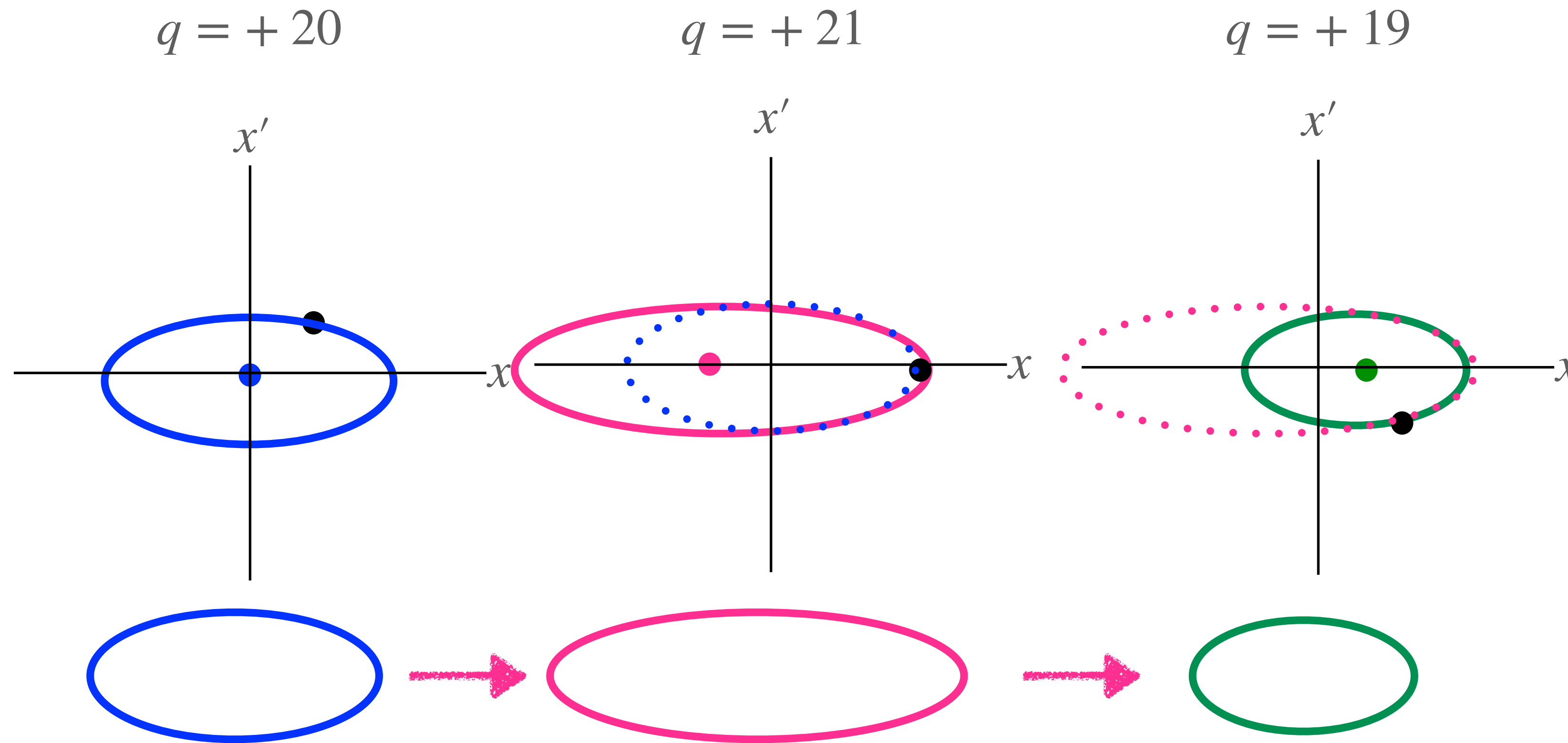
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- betatron amplitudes change turn by turn

amplitude change due to charge state transition

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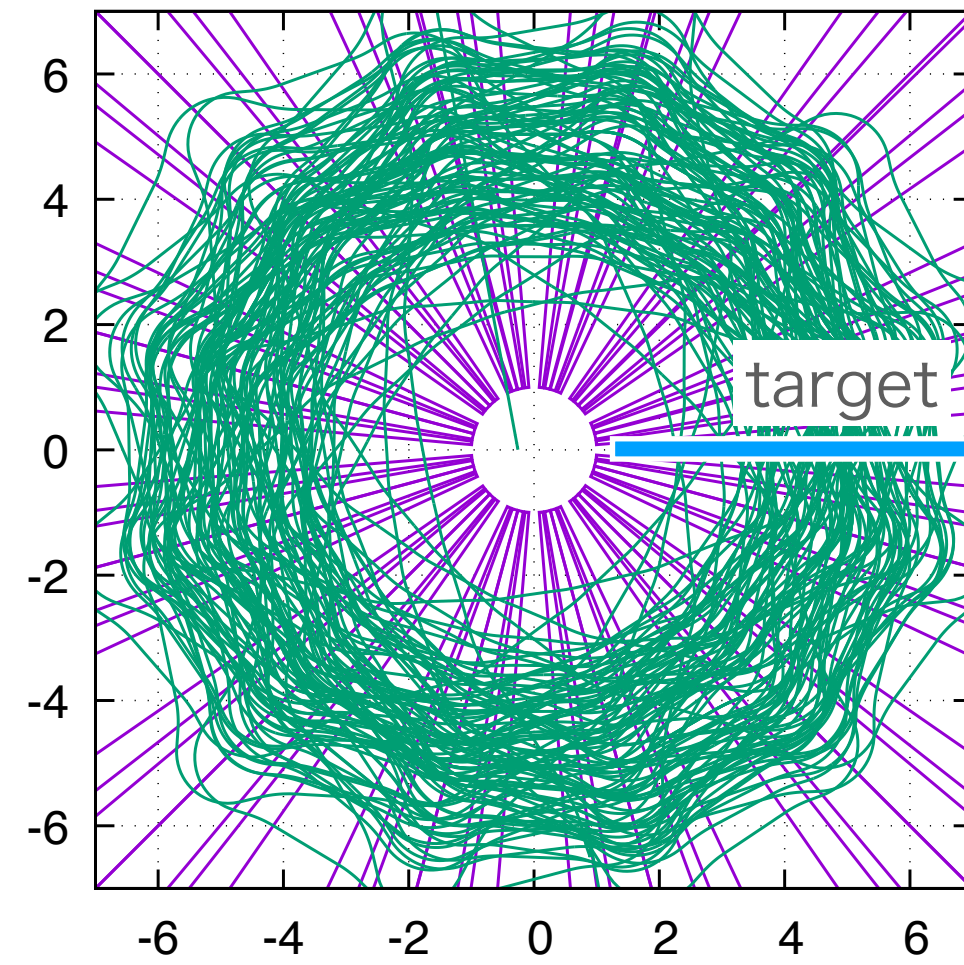


- **betatron amplitudes change turn by turn**

increase the k value

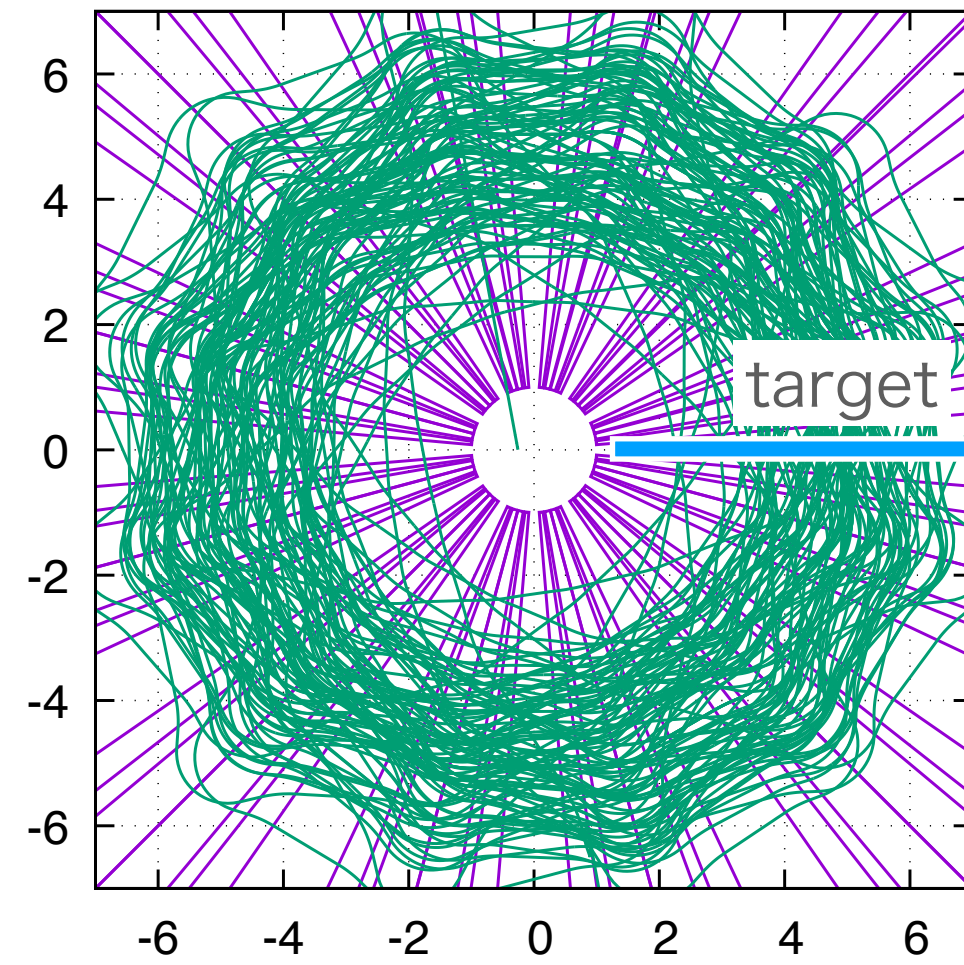
increase the k value

$$k = 1.1, \nu_x = 1.53, \nu_y = 2.27$$

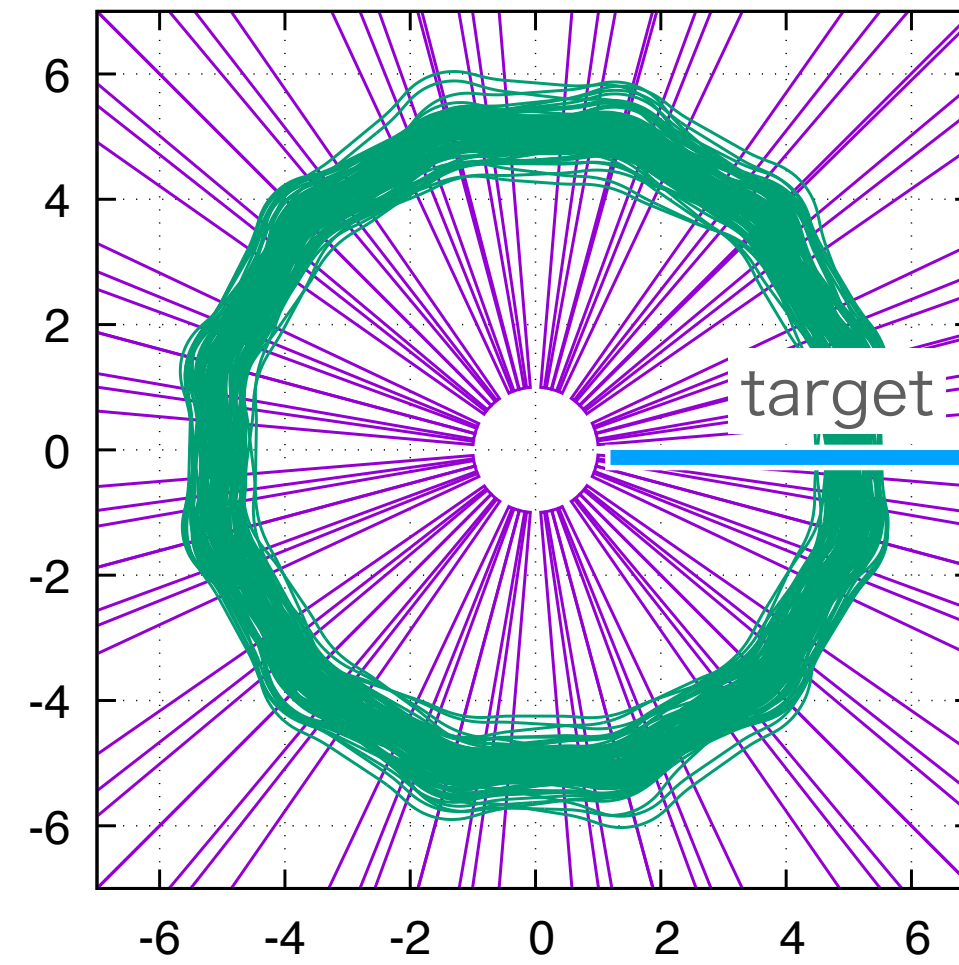


increase the k value

$$k = 1.1, \nu_x = 1.53, \nu_y = 2.27$$

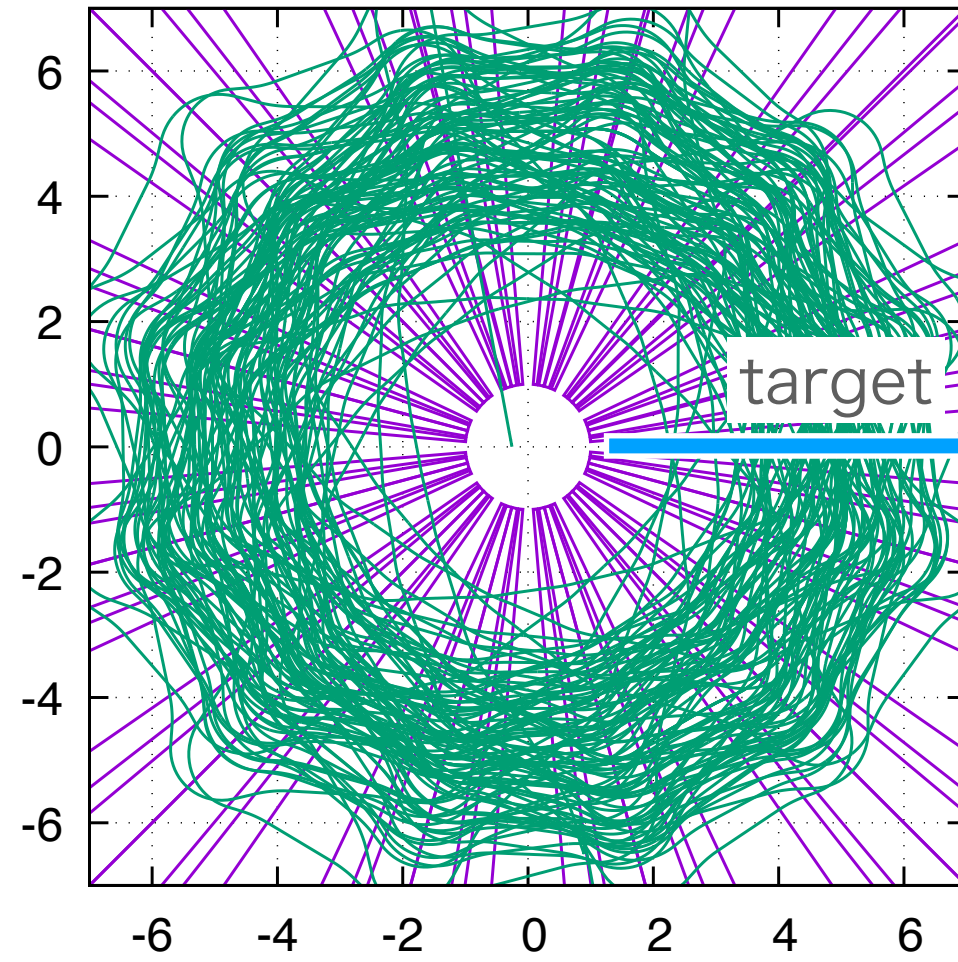


$$k = 2.1, \nu_x = 1.89, \nu_y = 2.07$$

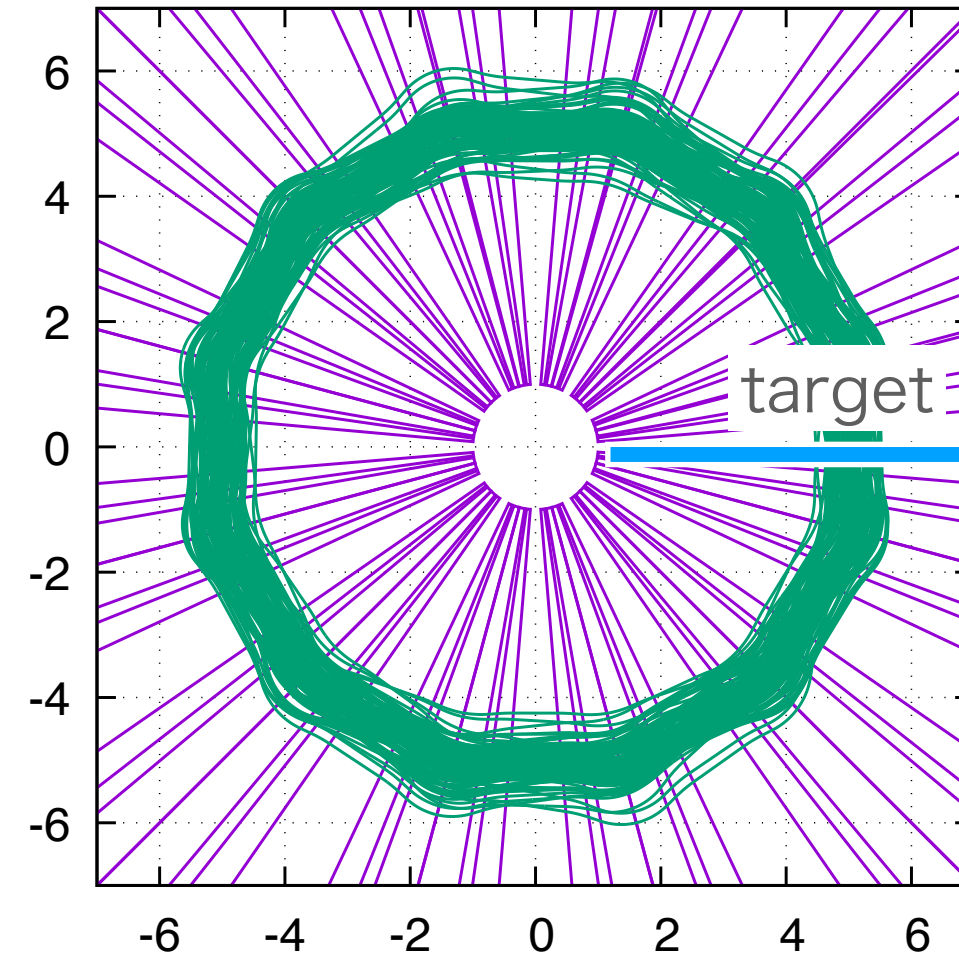


increase the k value

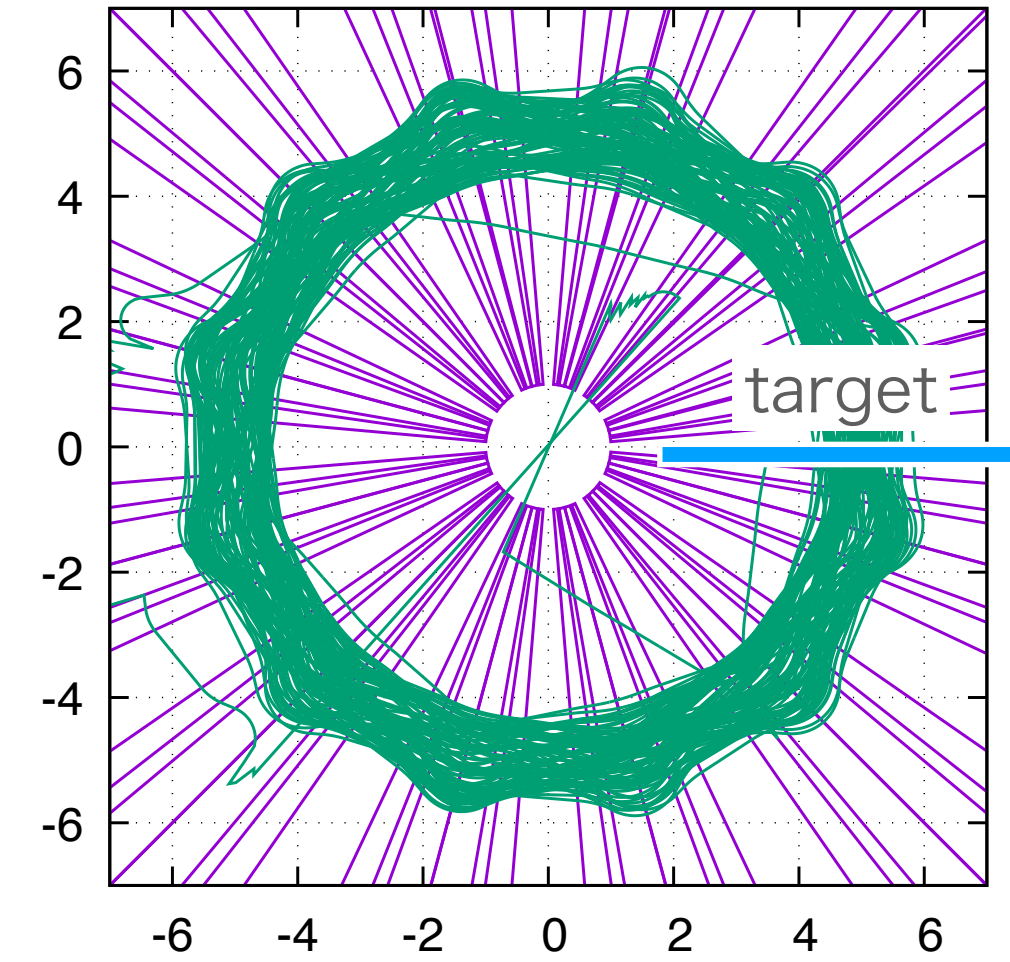
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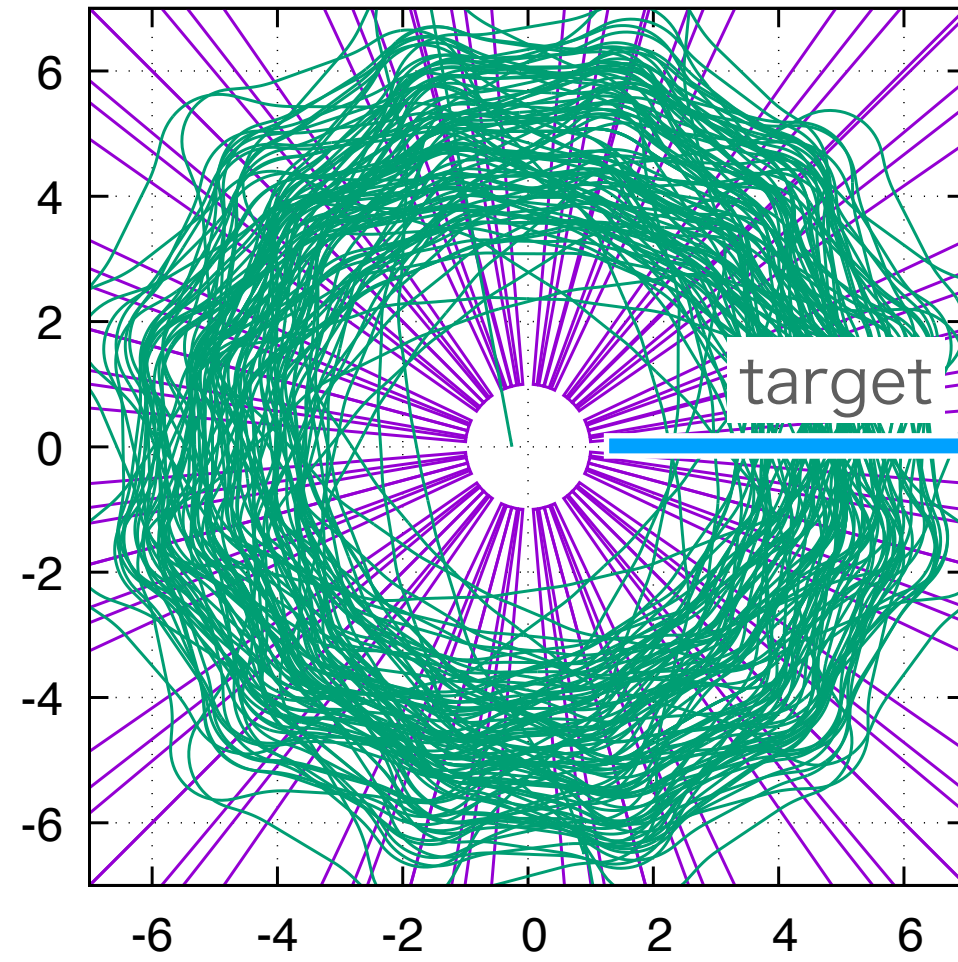


$$k = 4.1, \nu_x = 2.52, \nu_y = 1.62$$

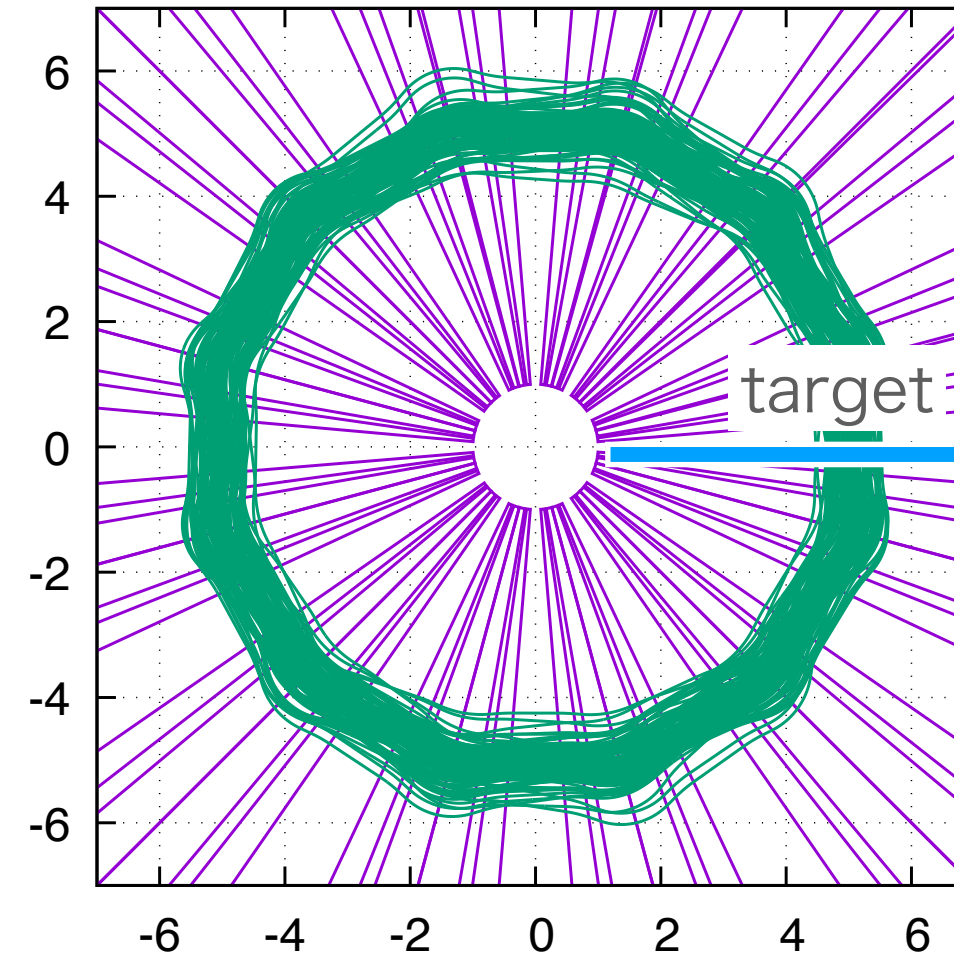


increase the k value

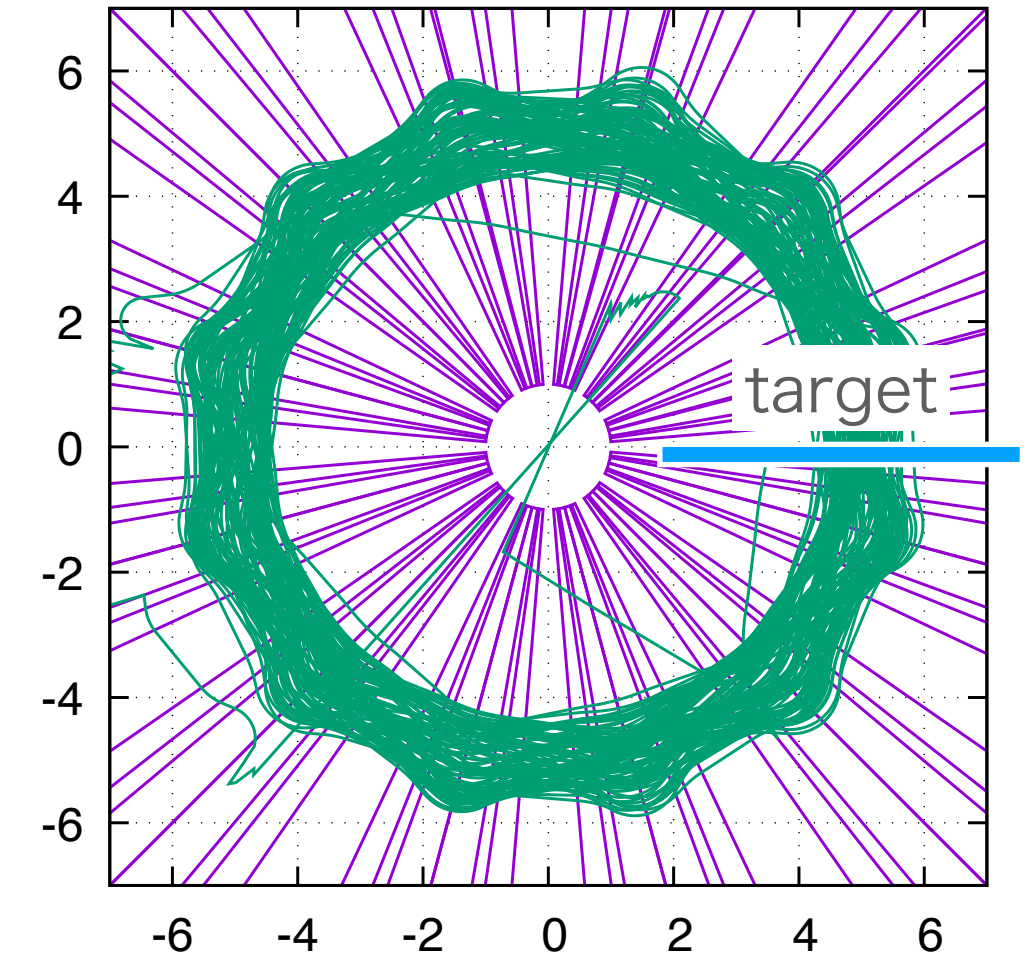
$k = 1.1, \nu_x = 1.53, \nu_y = 2.27$



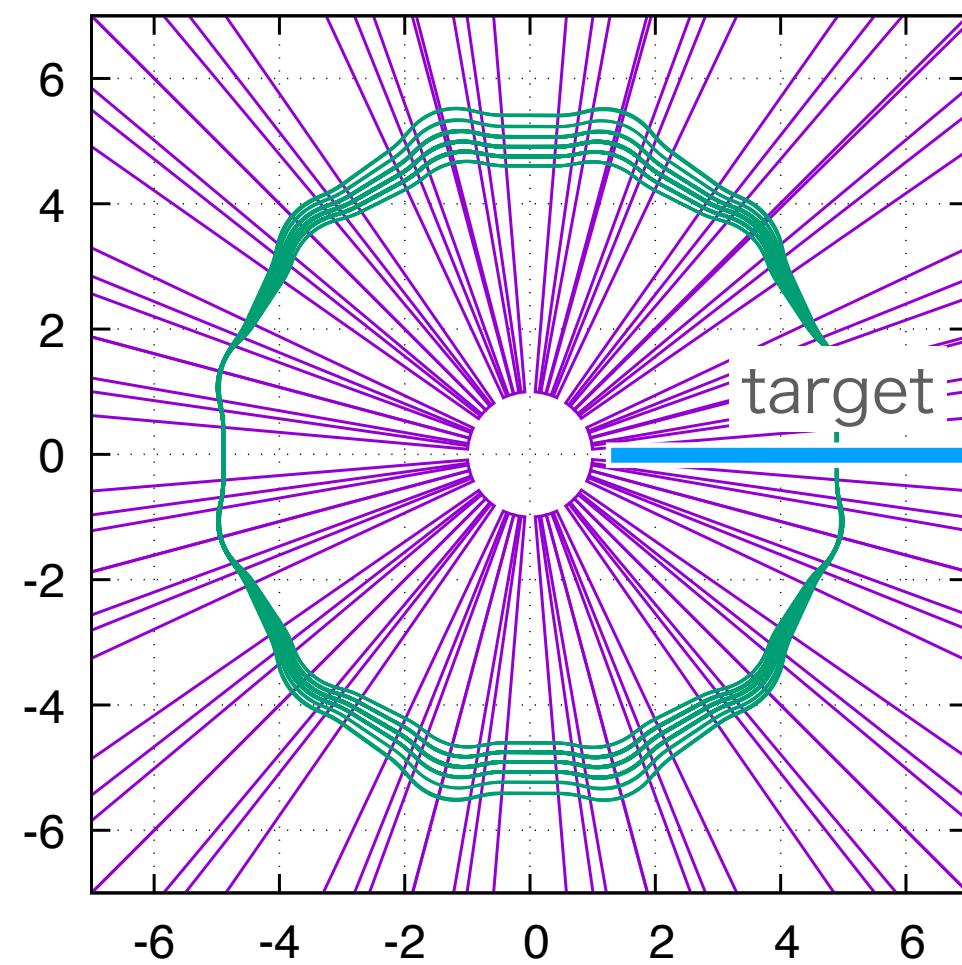
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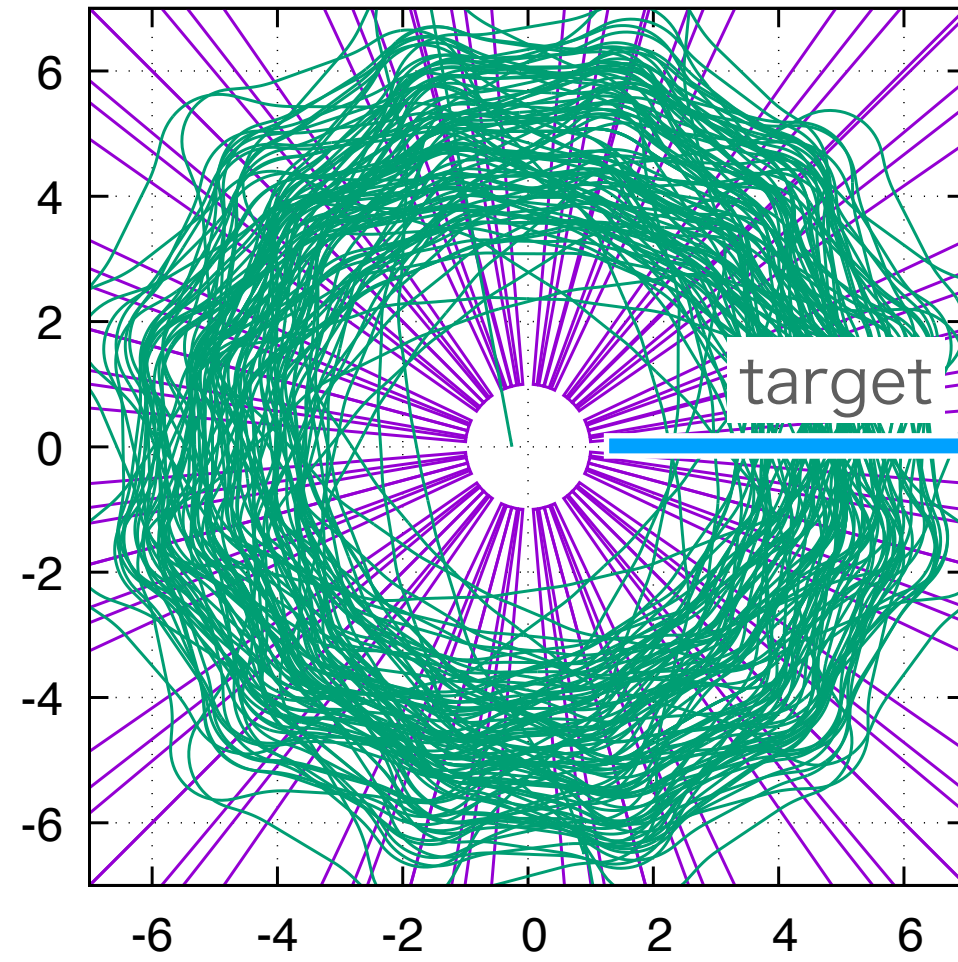


$k = 2.14, \nu_x = 1.998, \nu_y = 3.090$

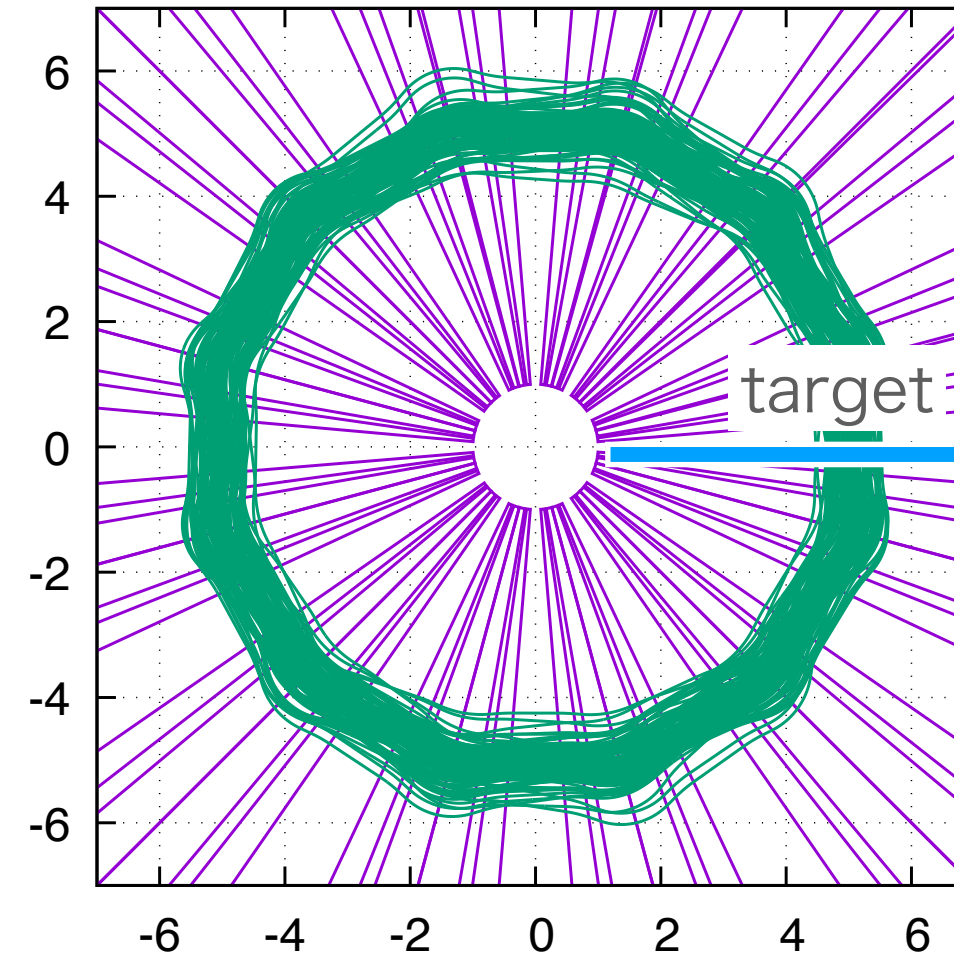


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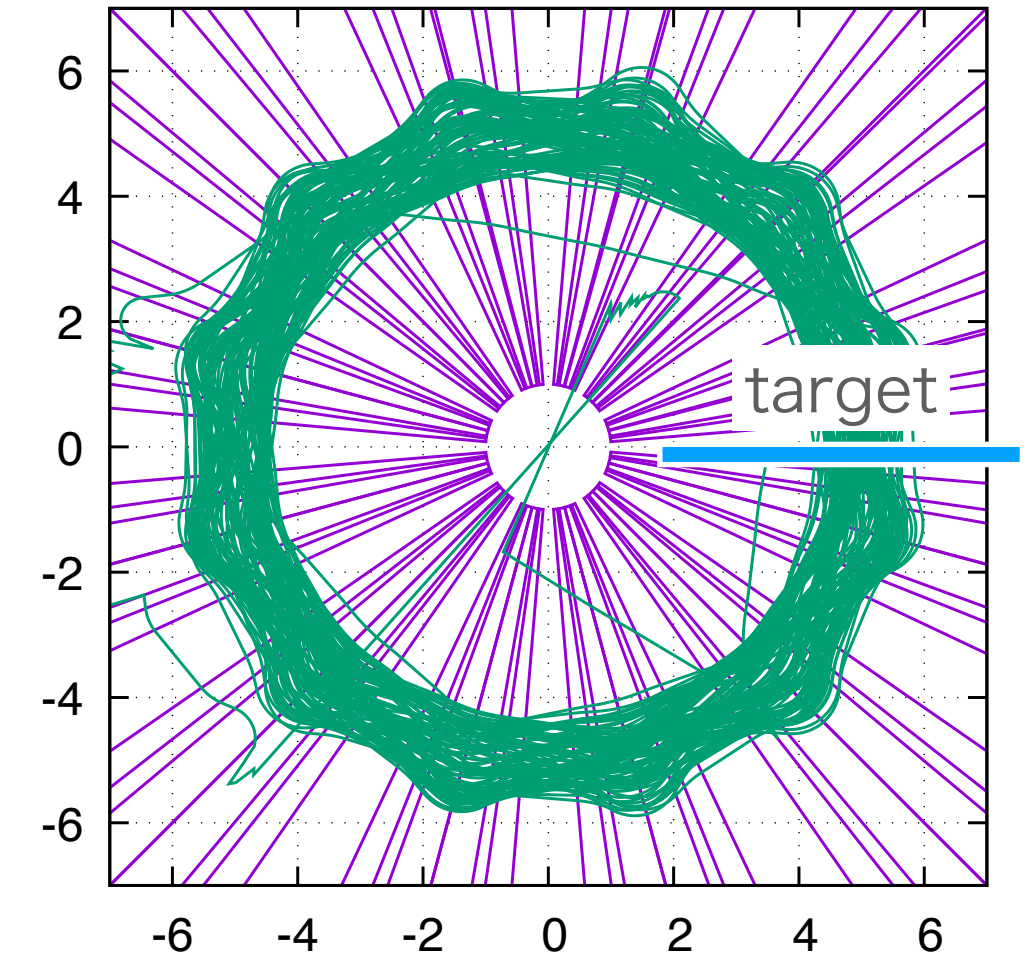
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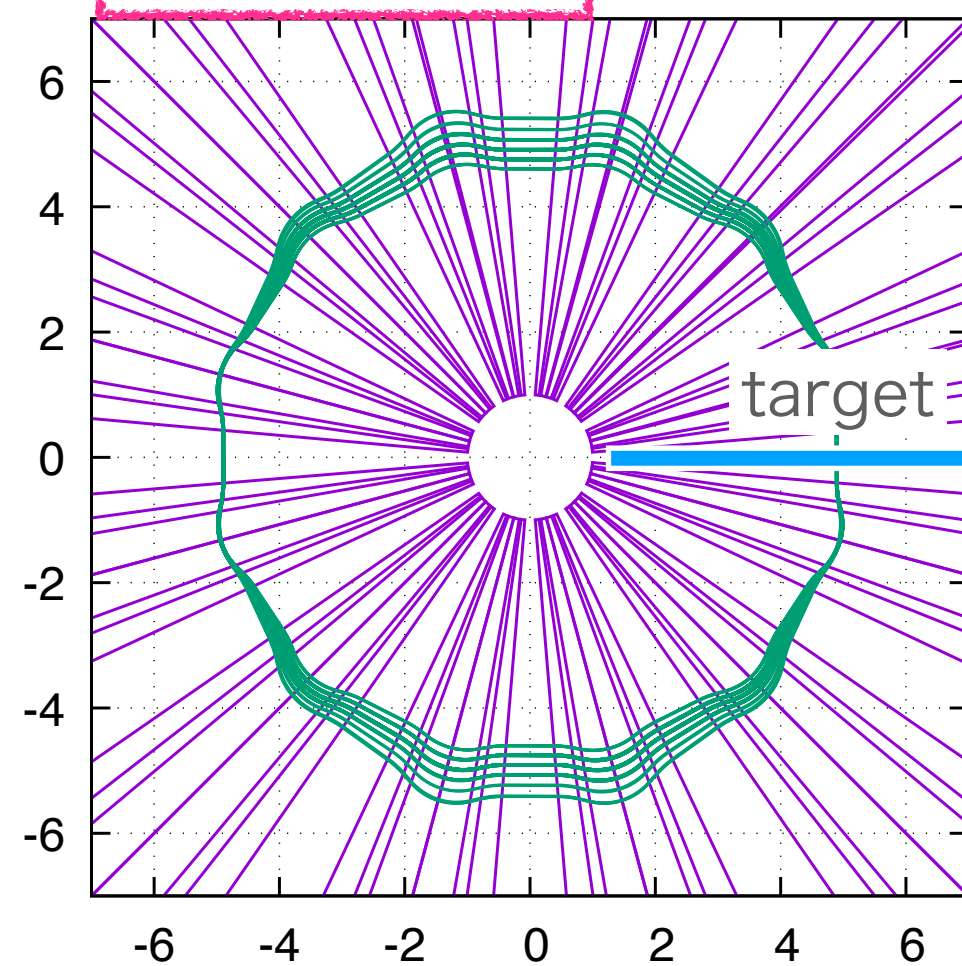
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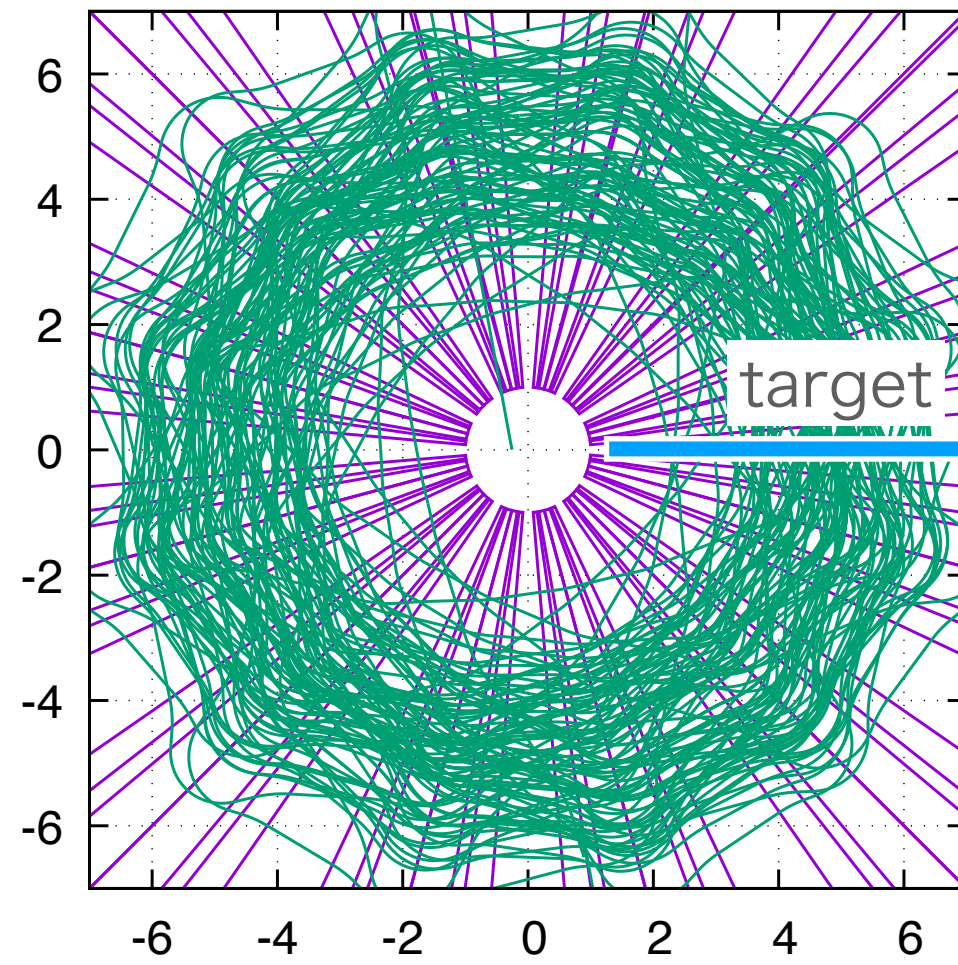


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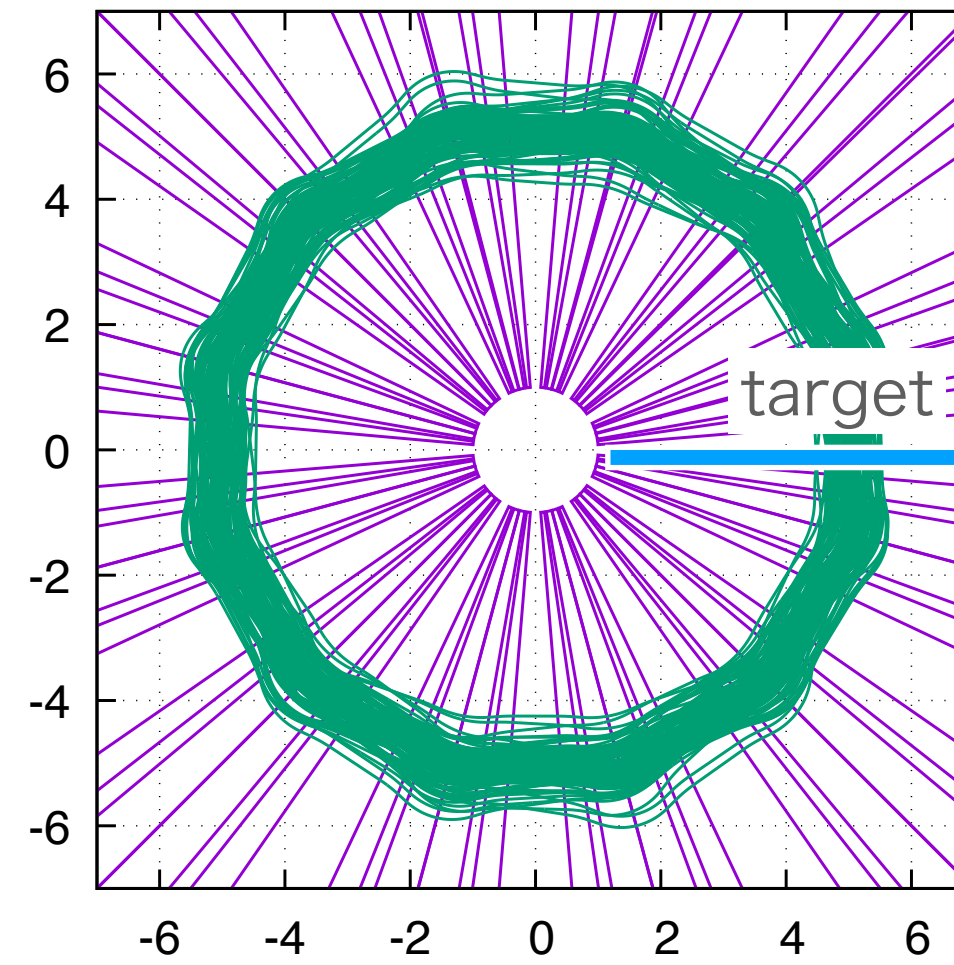


increase the k value

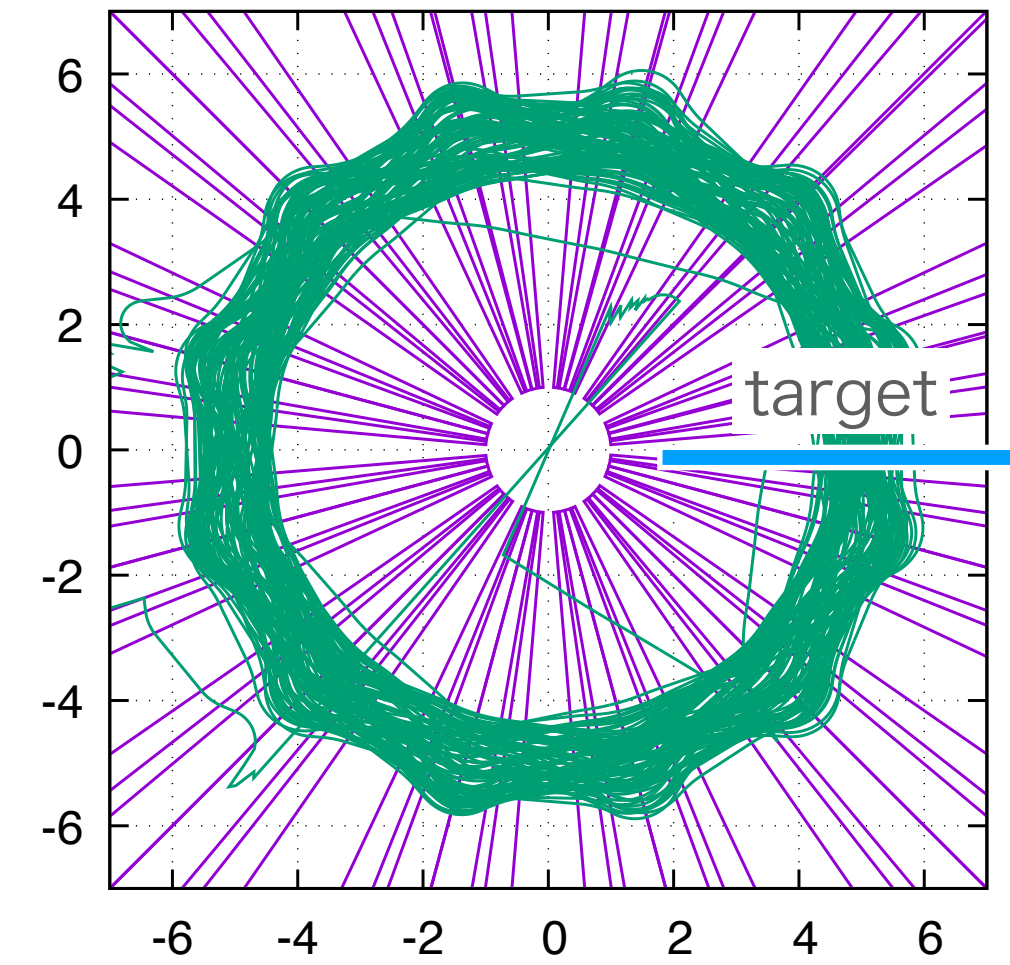
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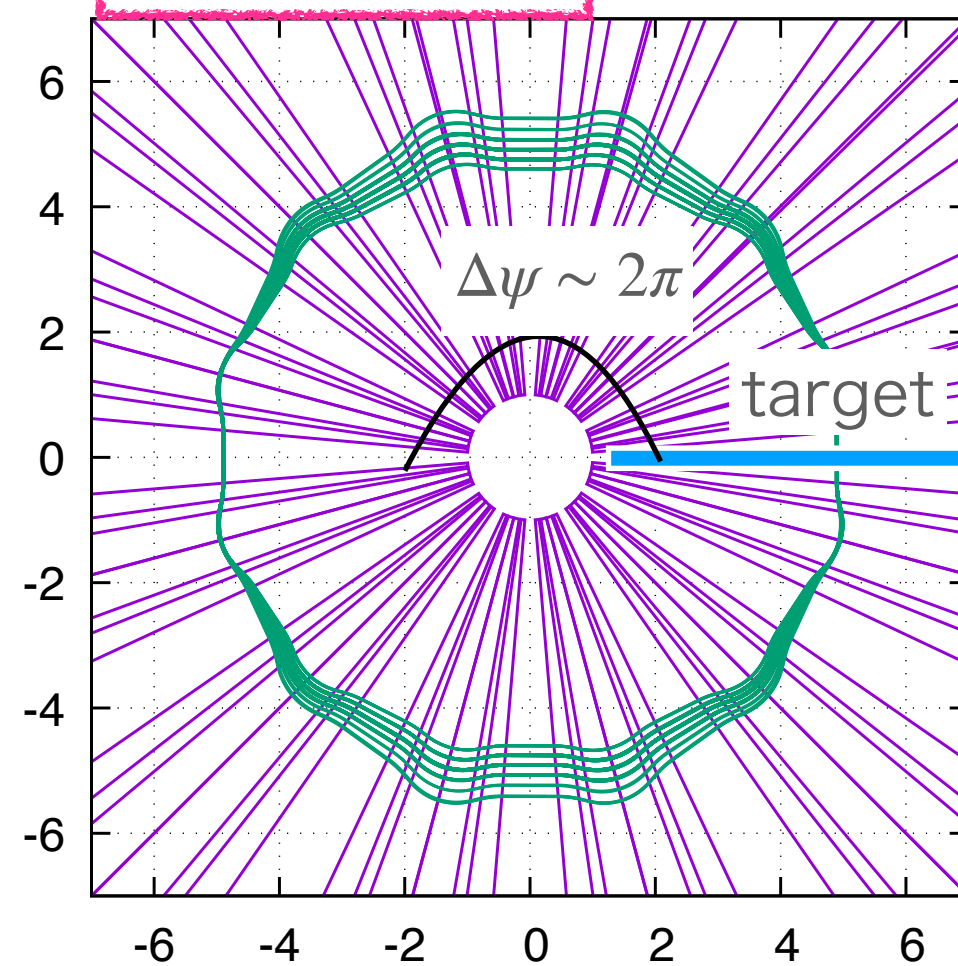
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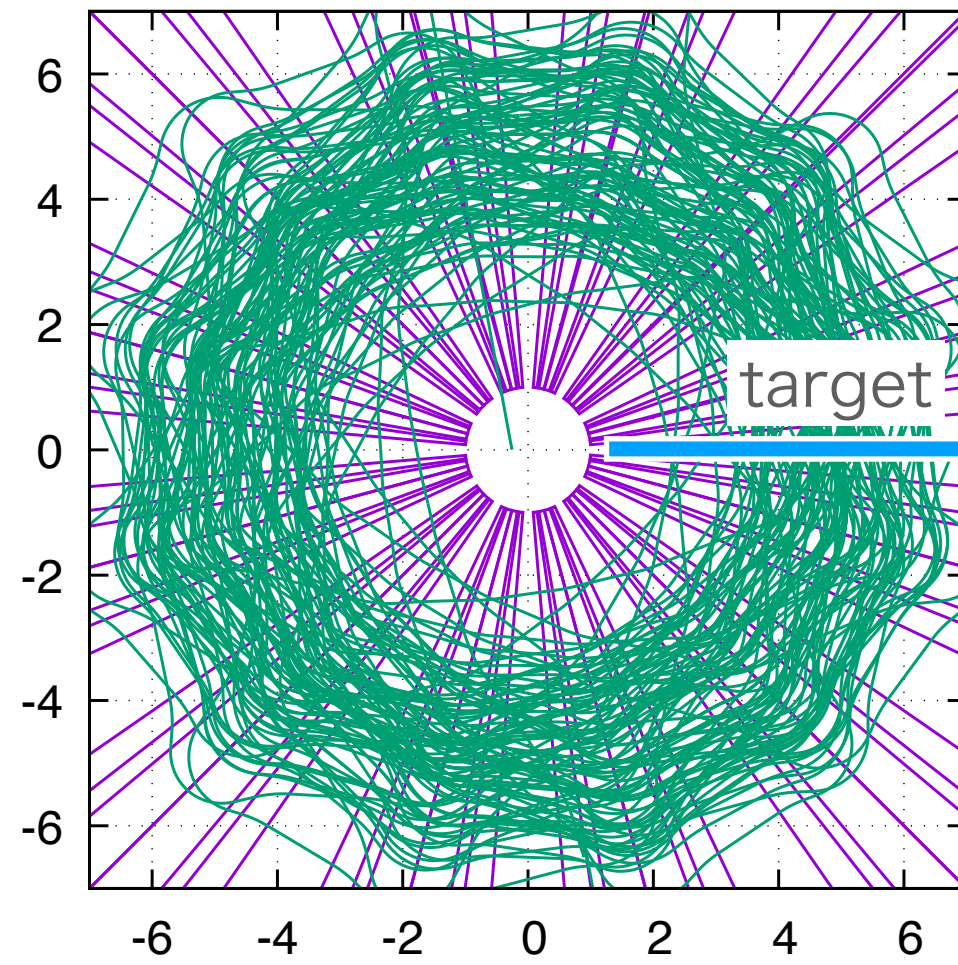


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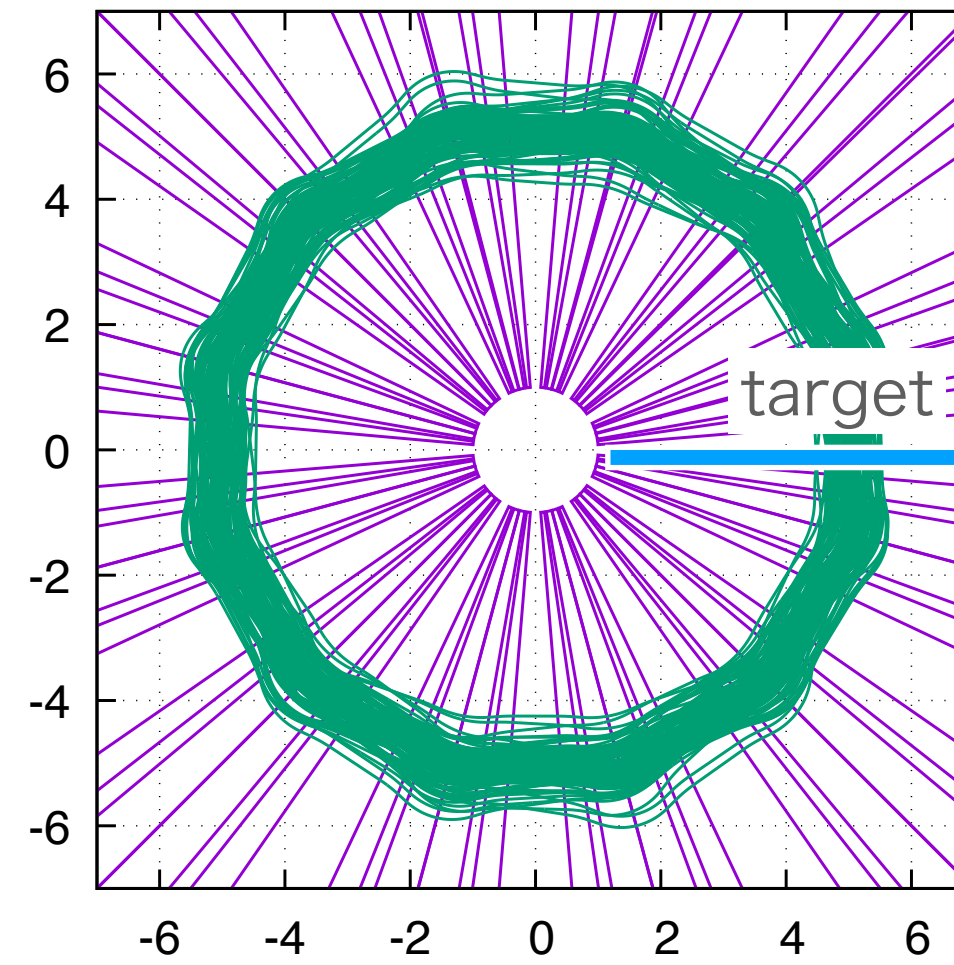


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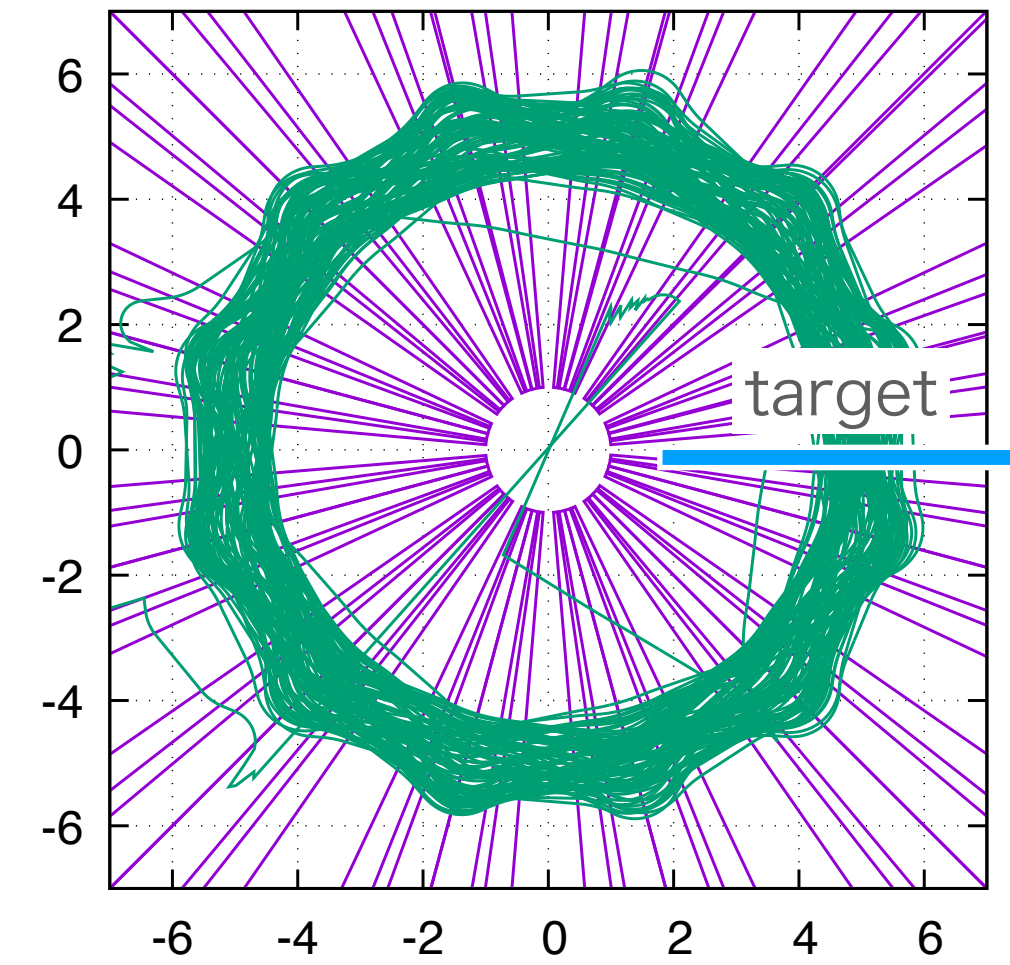
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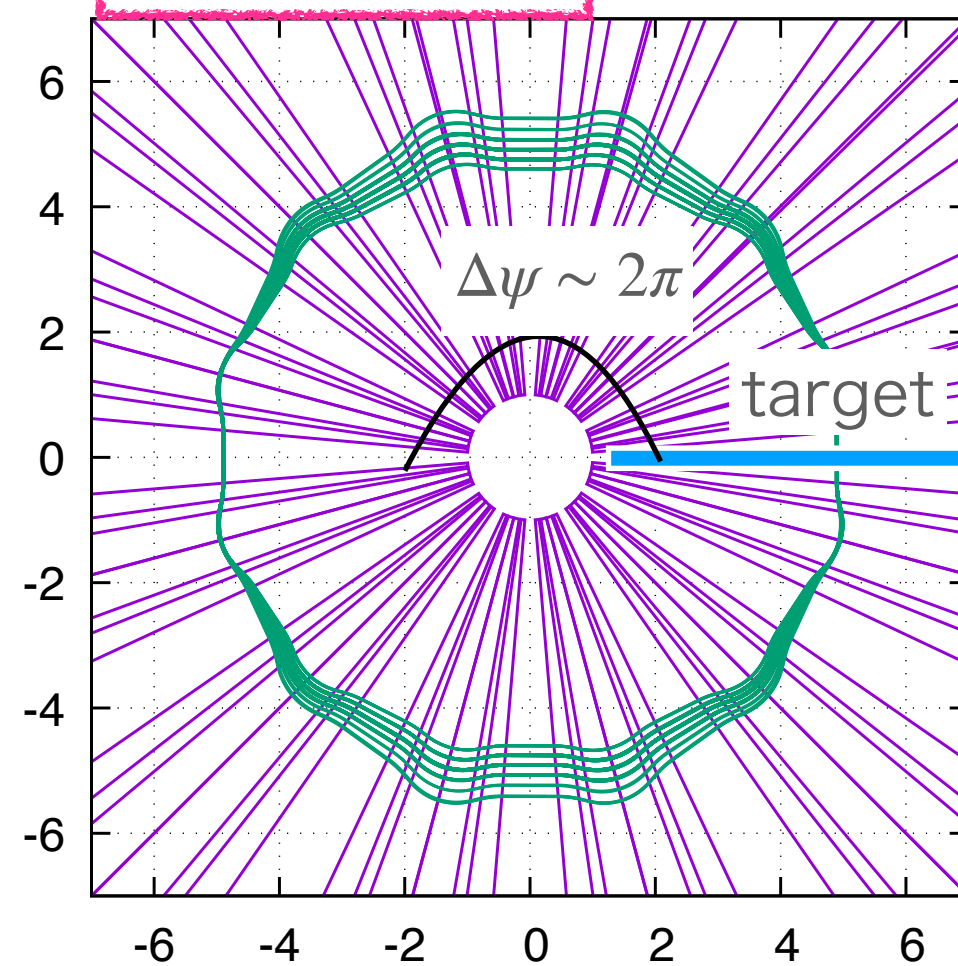
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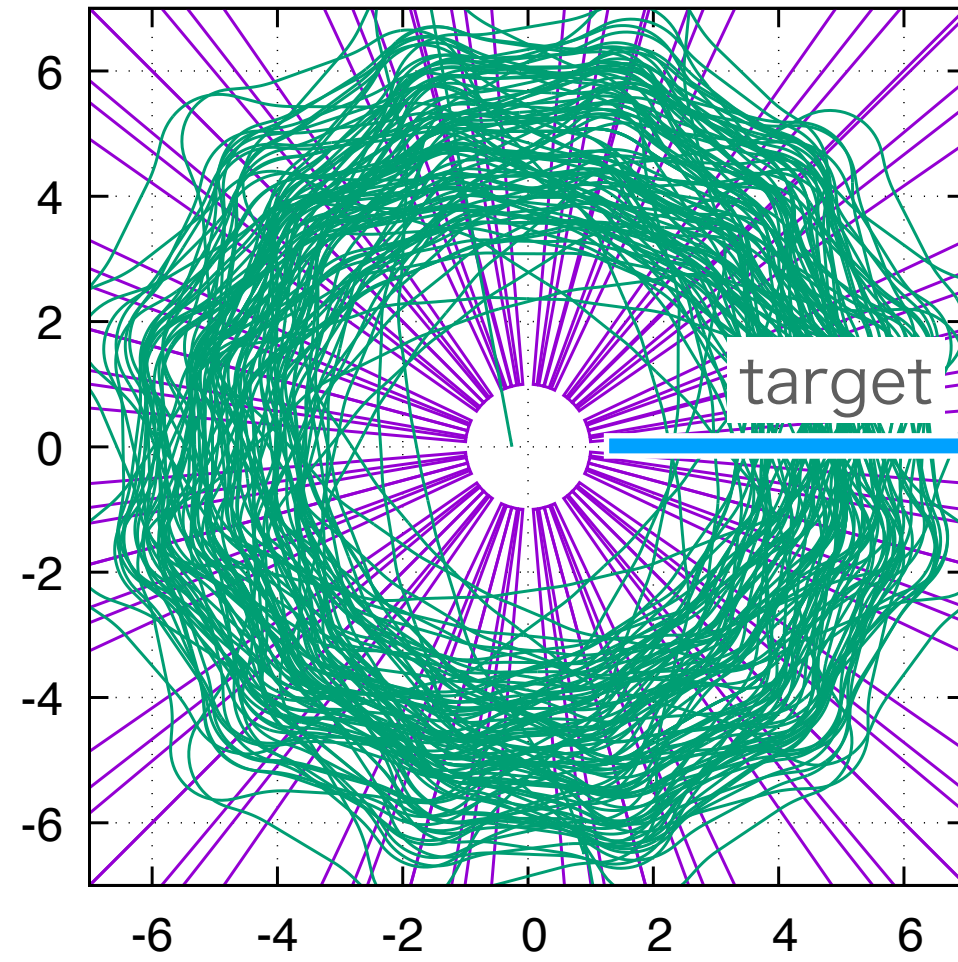
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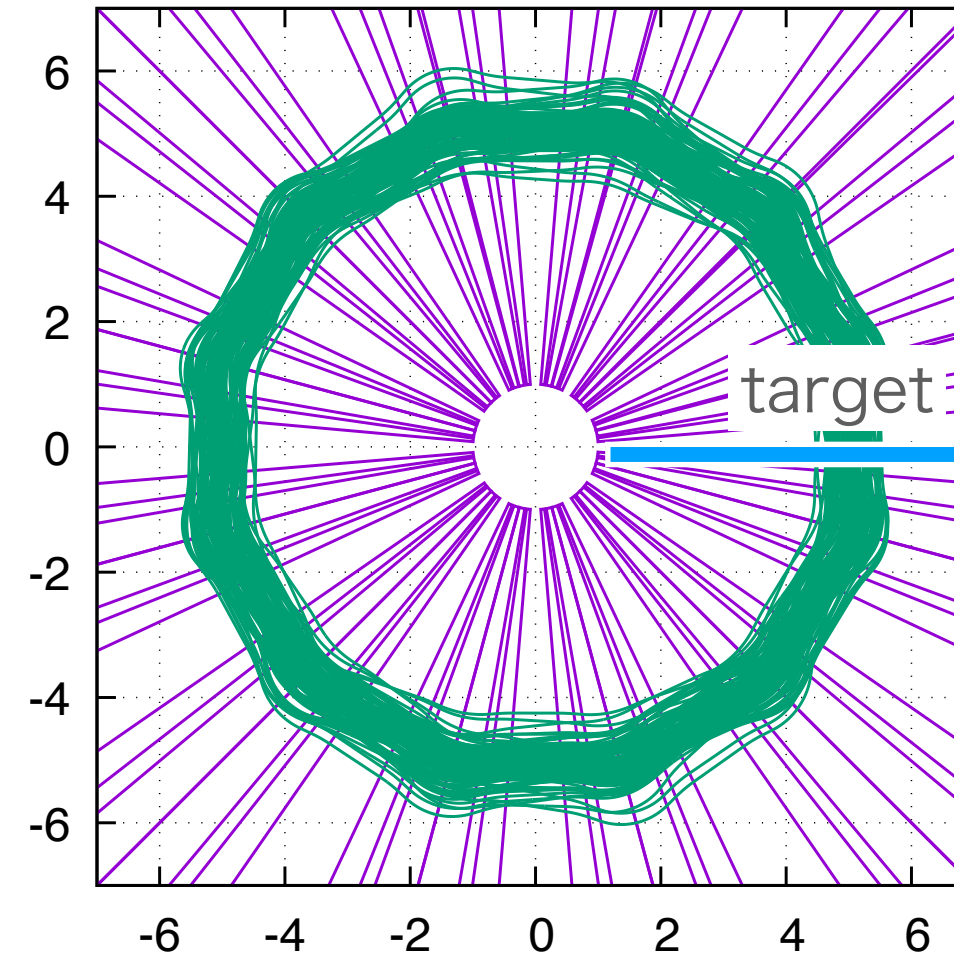
$$D_x \sim 0$$

increase the k value

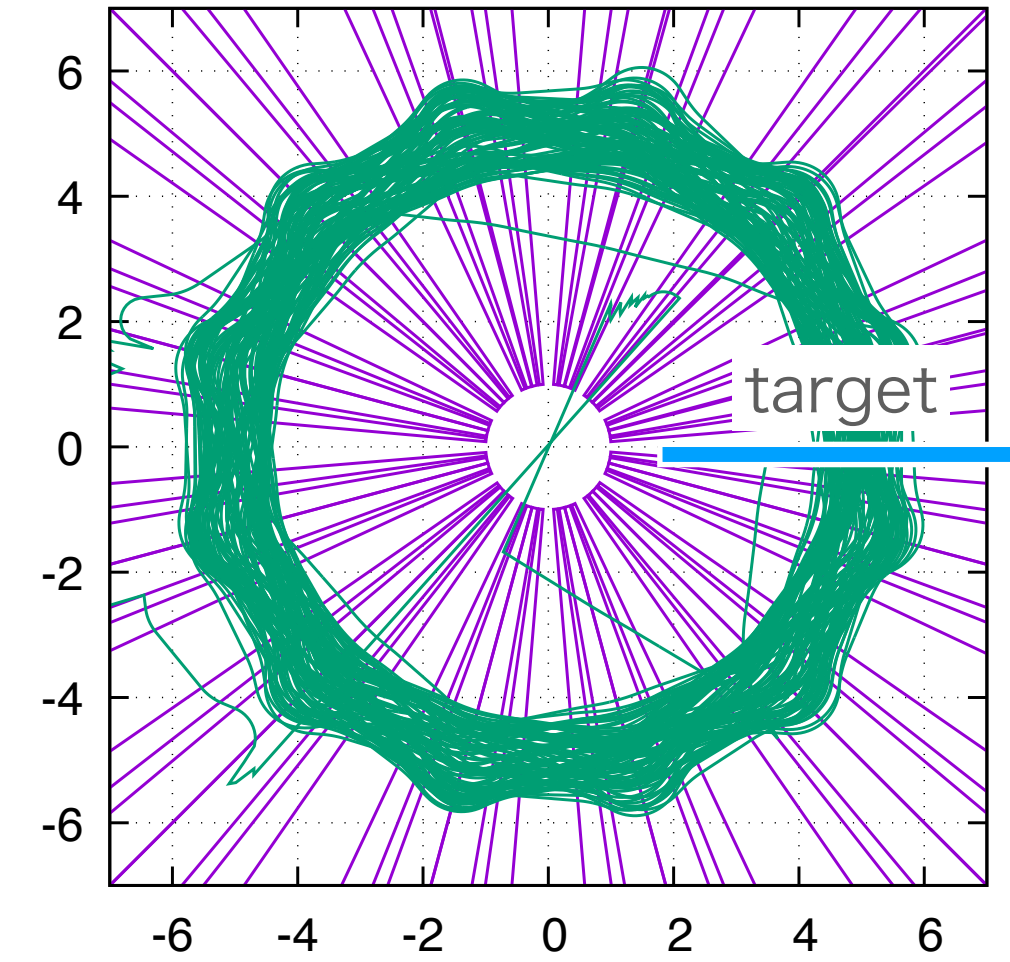
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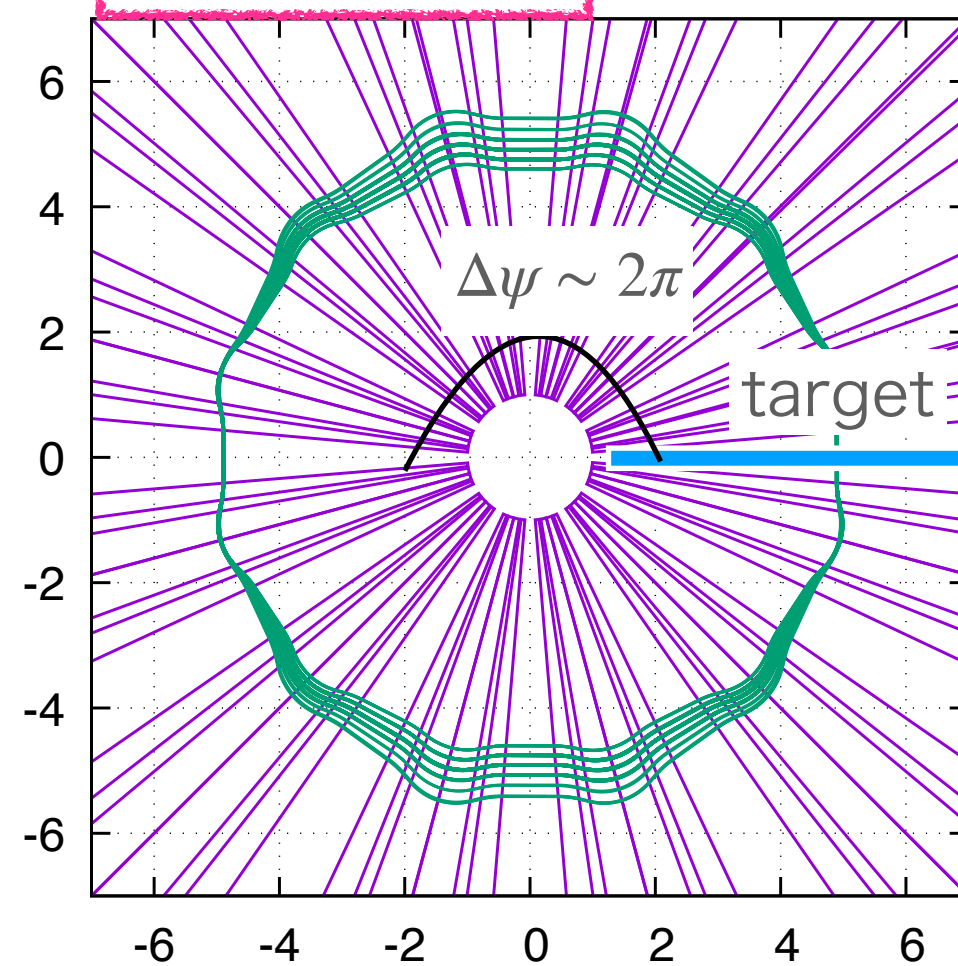
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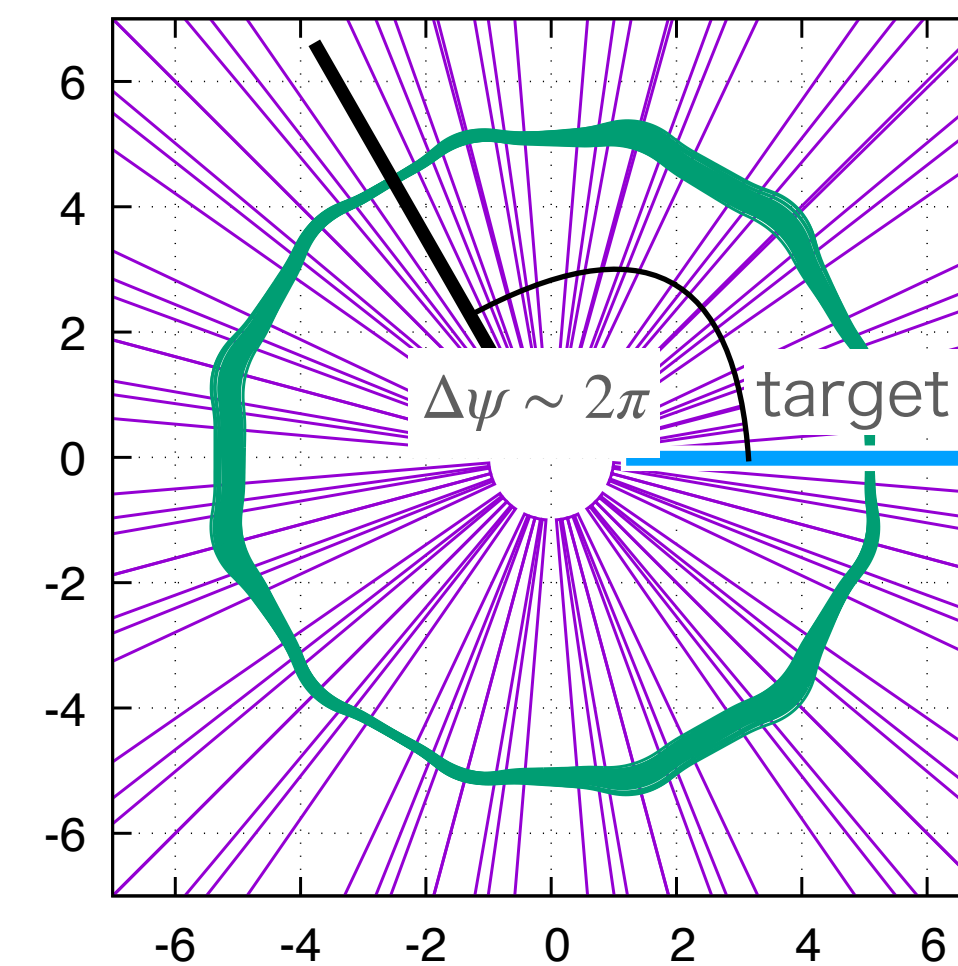


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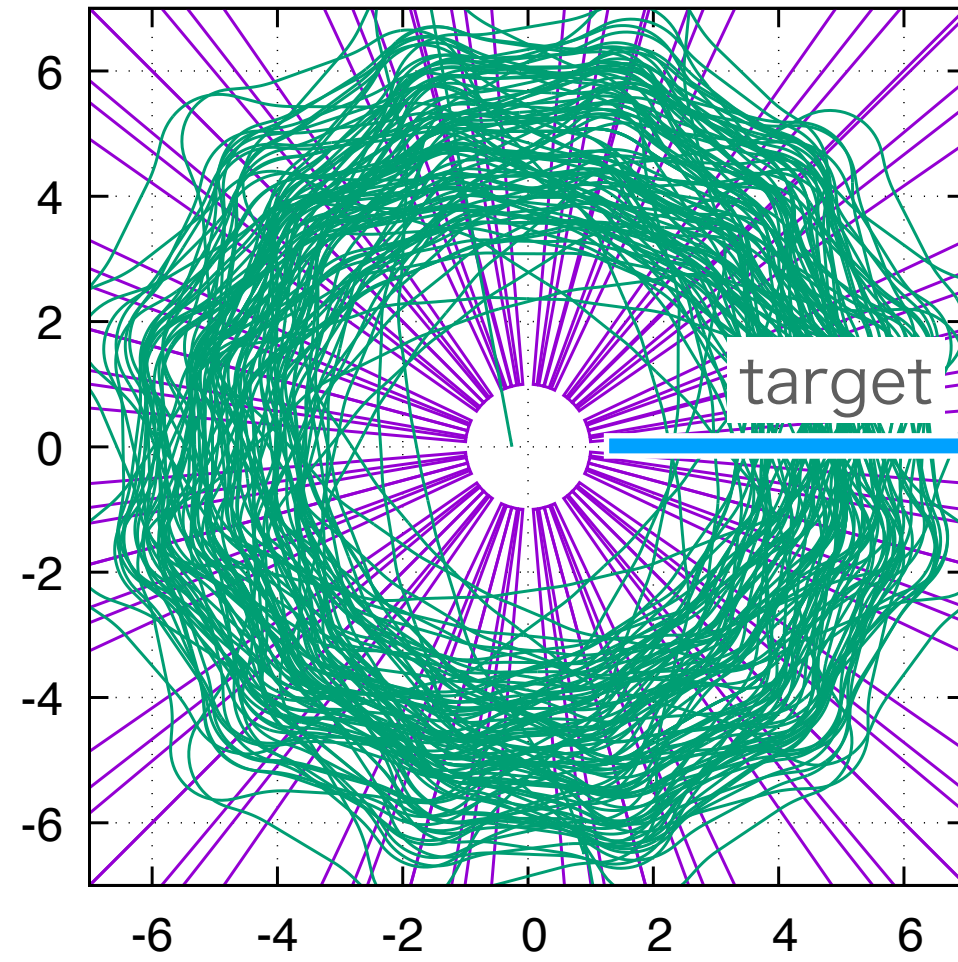
$D_x \sim 0$

$k = 5.57, \nu_x = 2.956, \nu_y = 1.245$

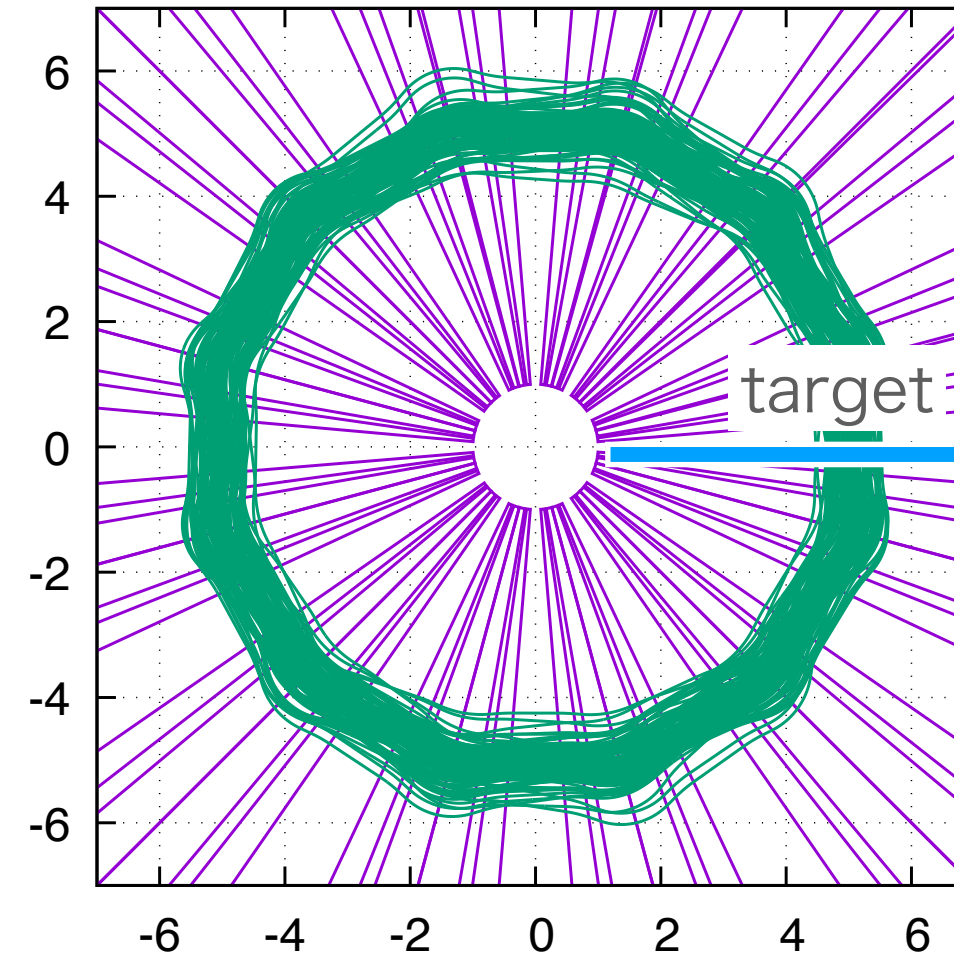


increase the k value

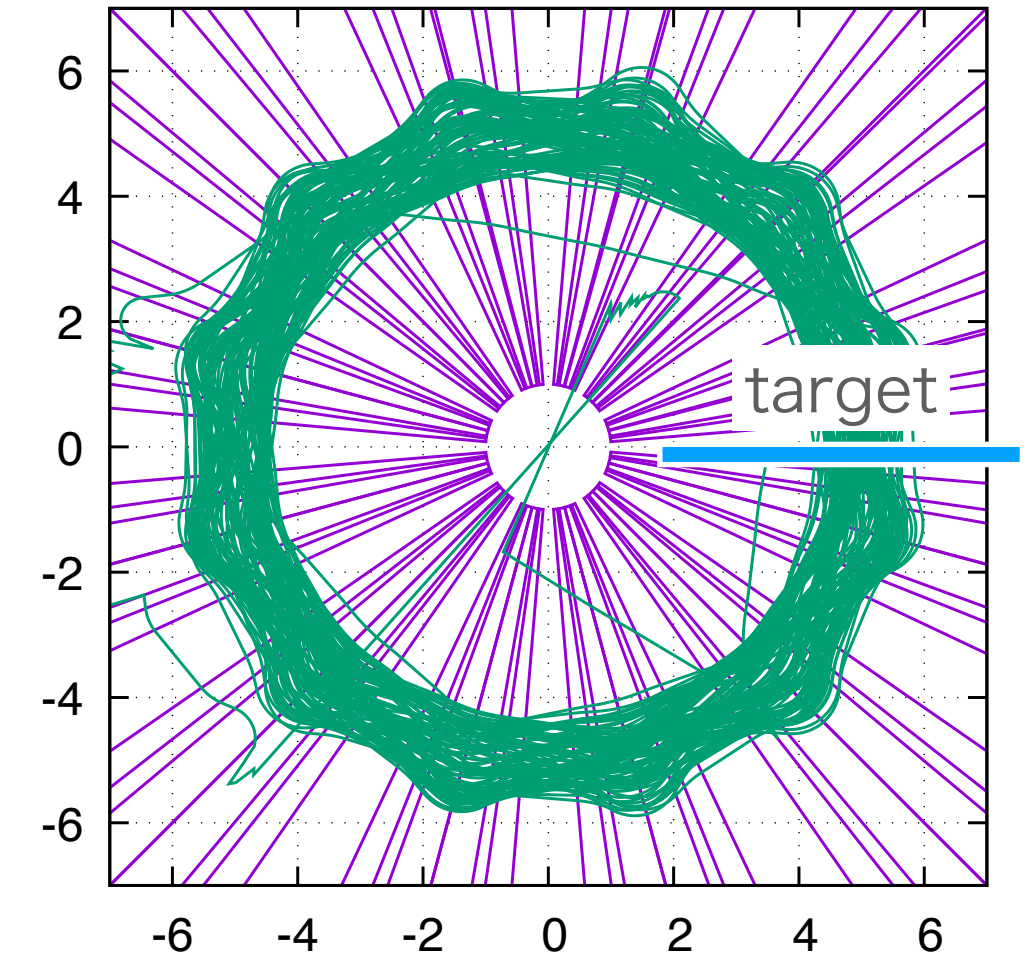
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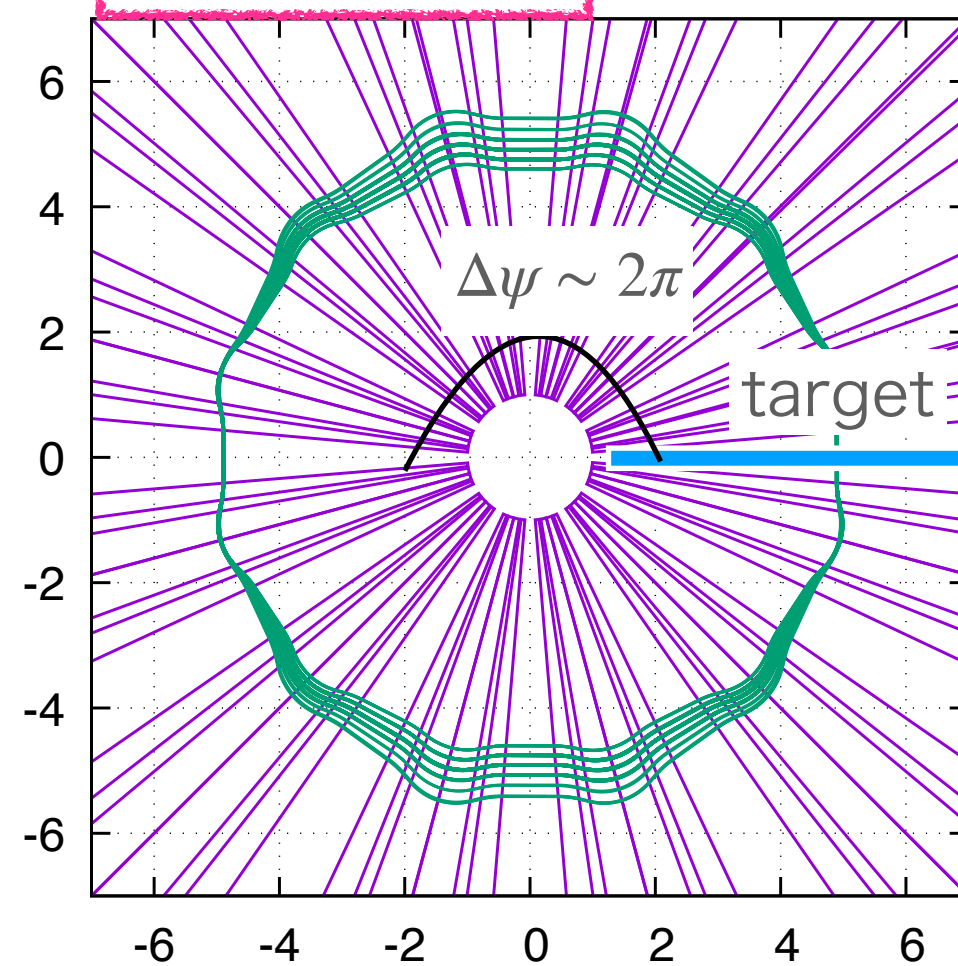
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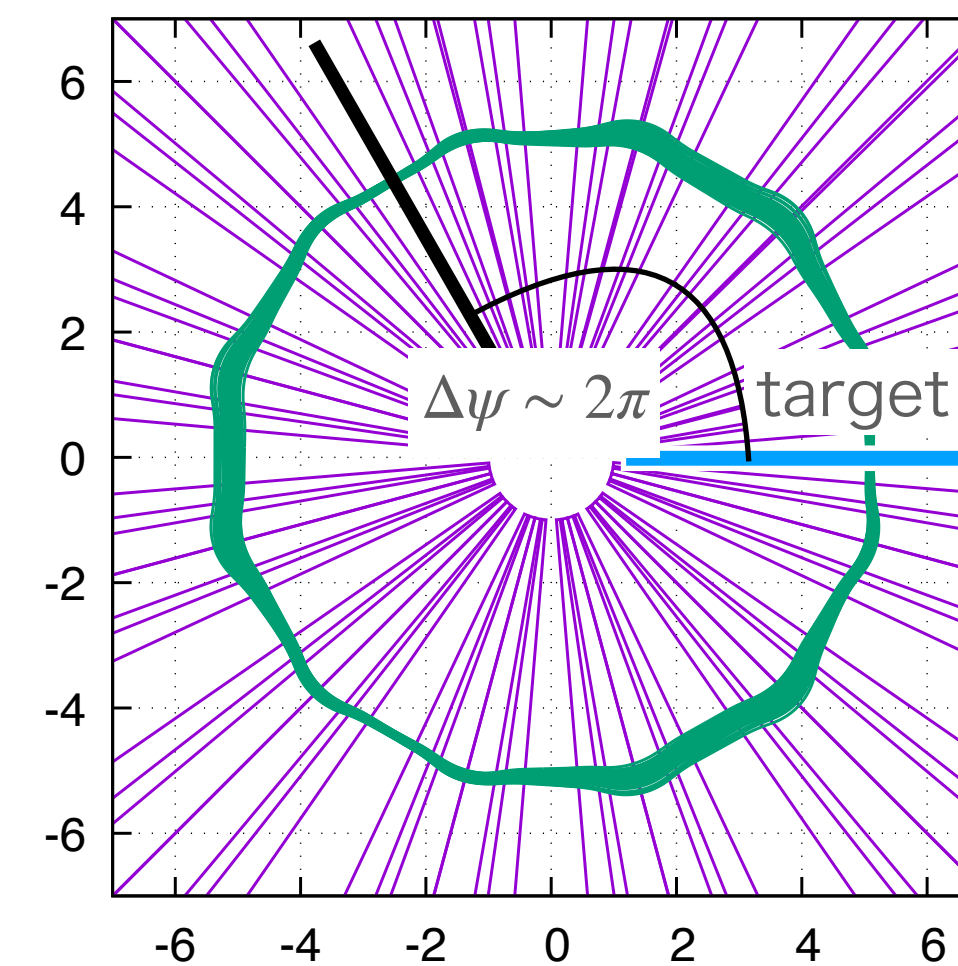
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$D_x \sim 0$

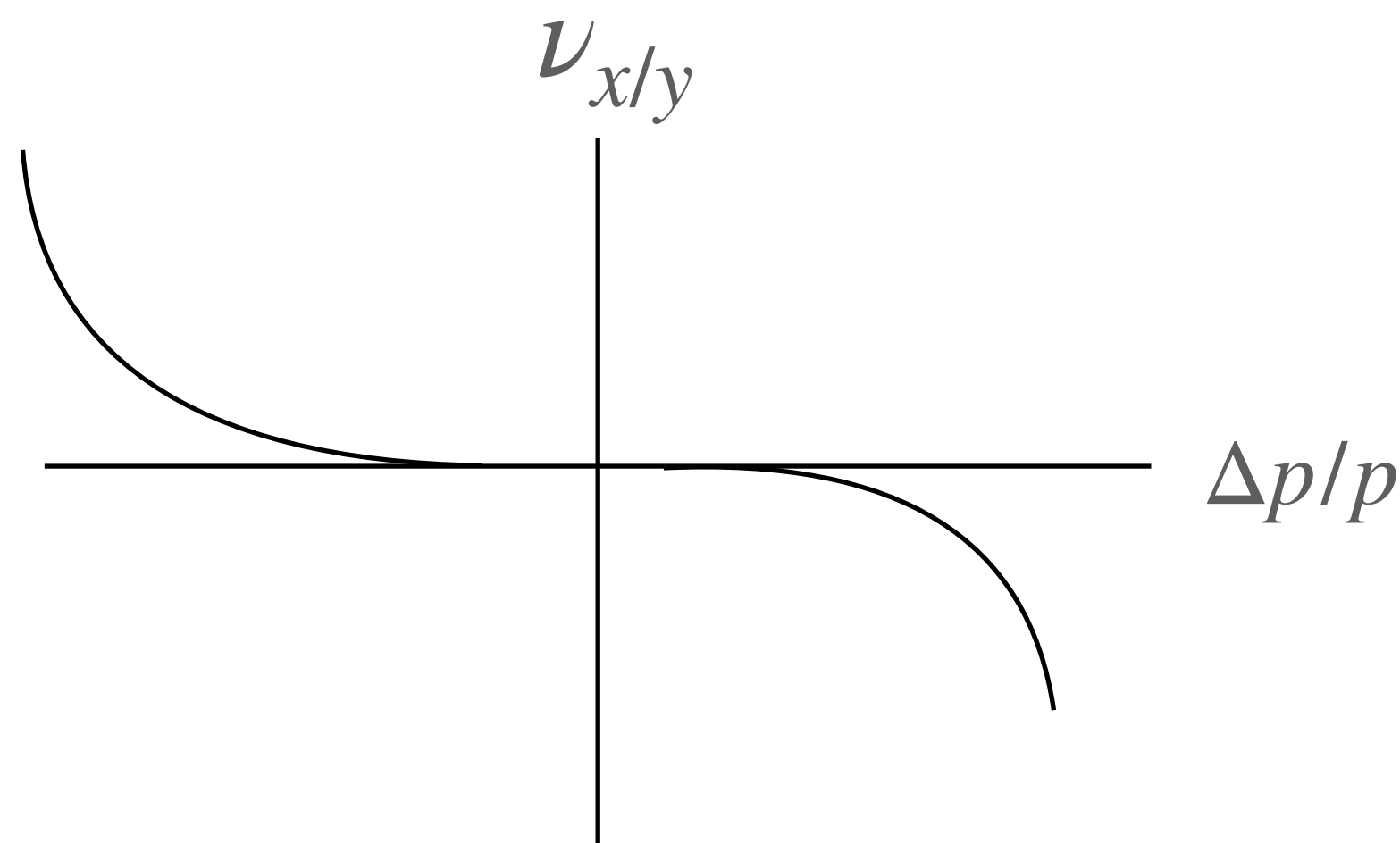
$D'_x \sim 0$ at the target

in ordinary synchrotron lattice

- Betatron amplitude variations caused by COD fluctuation due to the charge state variation can be suppressed by making dispersion suppressed sections and locating the target in that section as well as FFA lattice with an integer horizontal tune.
- Betatron amplitude change caused by ellipse fluctuation i.e. tune fluctuation coming from the higher order chromaticity, which doesn't exist in "scaling" FFA rings.

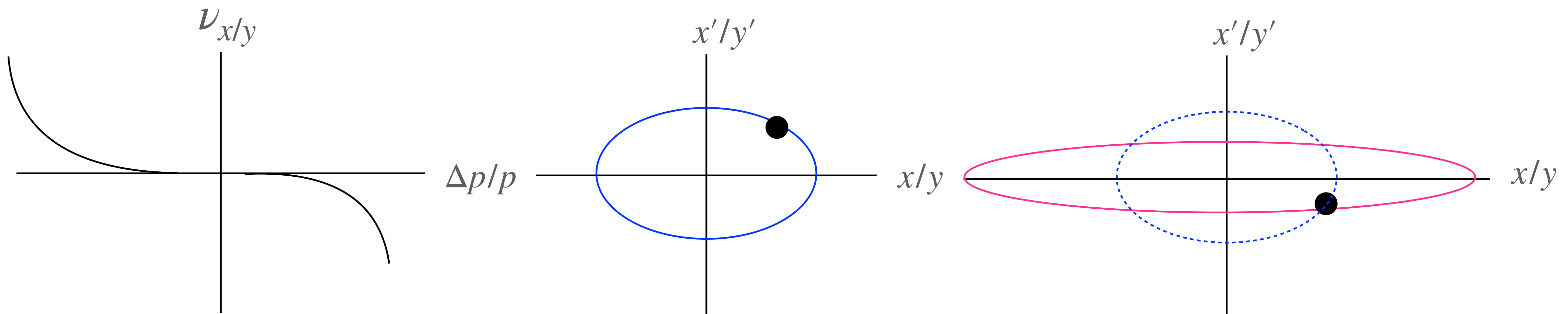
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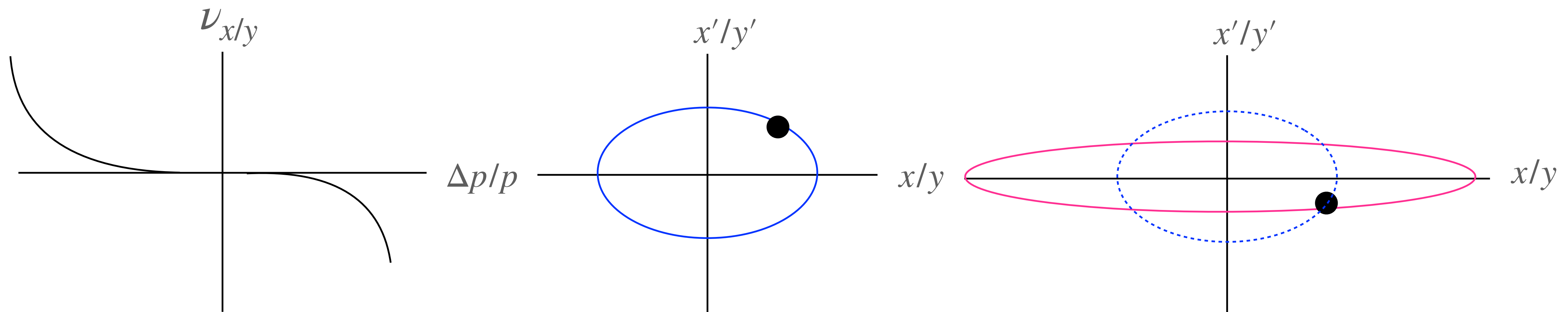
in ordinary synchrotron lattice

- Betatron amplitude variations caused by COD fluctuation due to the charge state variation can be suppressed by making dispersion suppressed sections and locating the target in that section as well as FFA lattice with an integer horizontal tune.
- Betatron amplitude change caused by ellipse fluctuation i.e. tune fluctuation coming from the higher order chromaticity, which doesn't exist in “scaling” FFA rings.



in ordinary synchrotron lattice

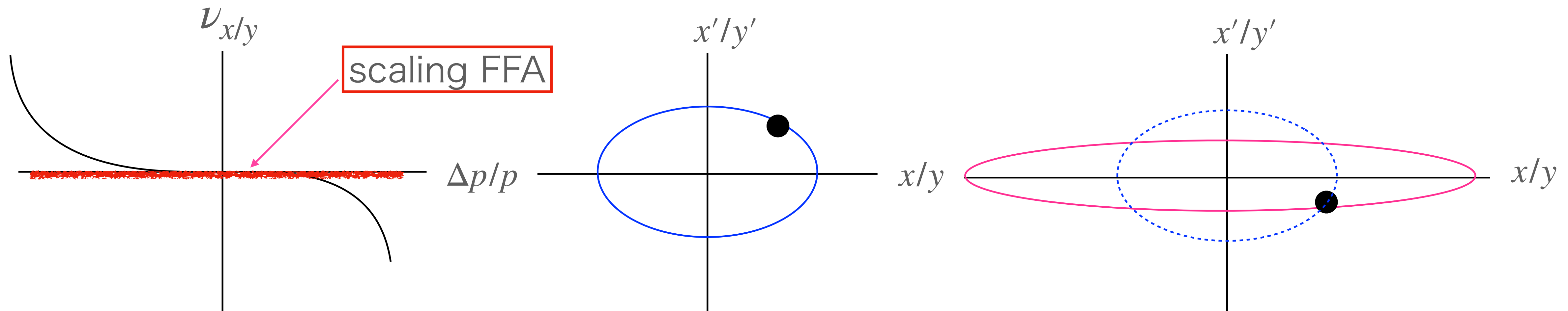
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- Because of this, it was considered difficult to realize a multi-charge state beam storage ring

in ordinary synchrotron lattice

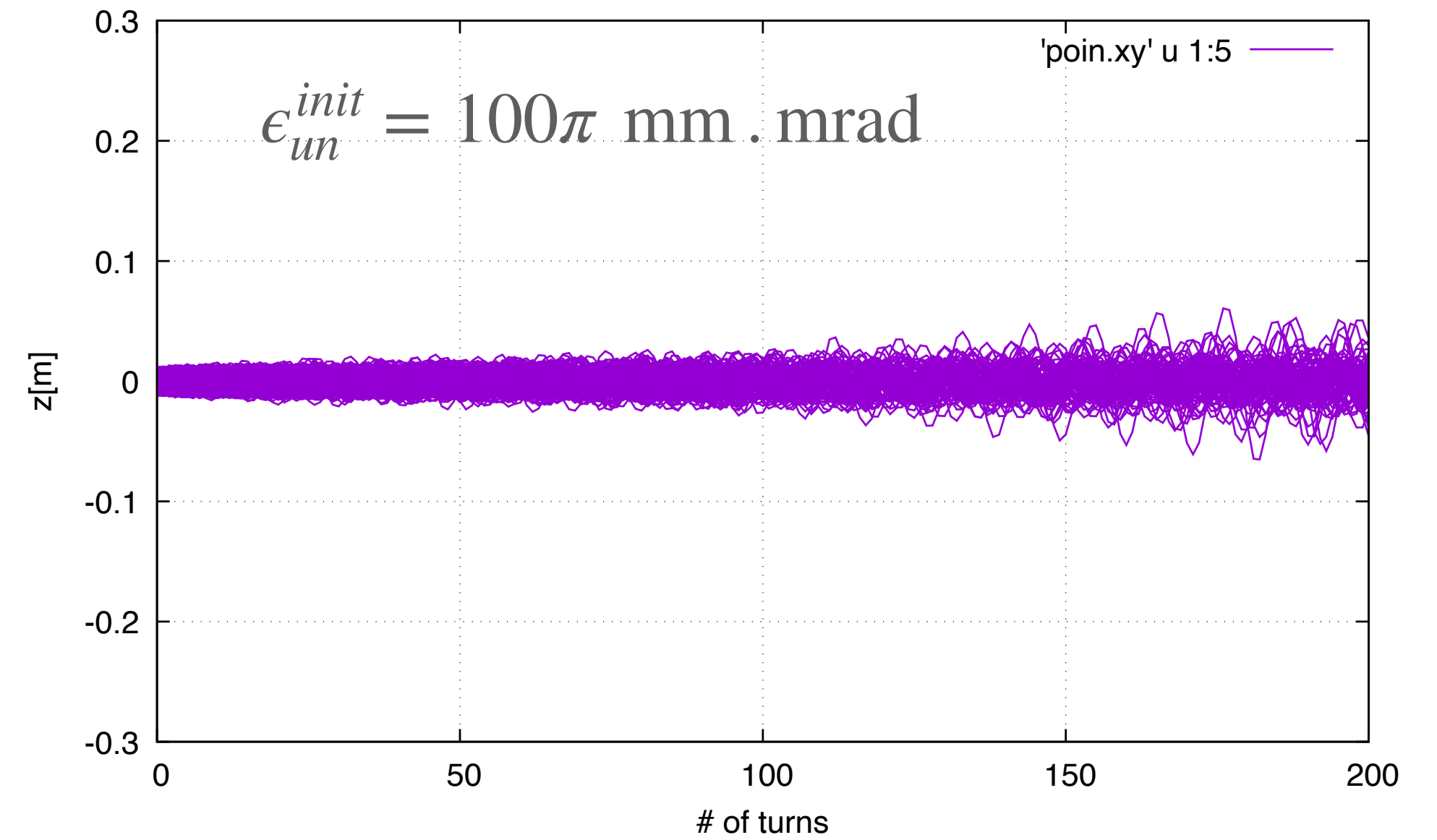
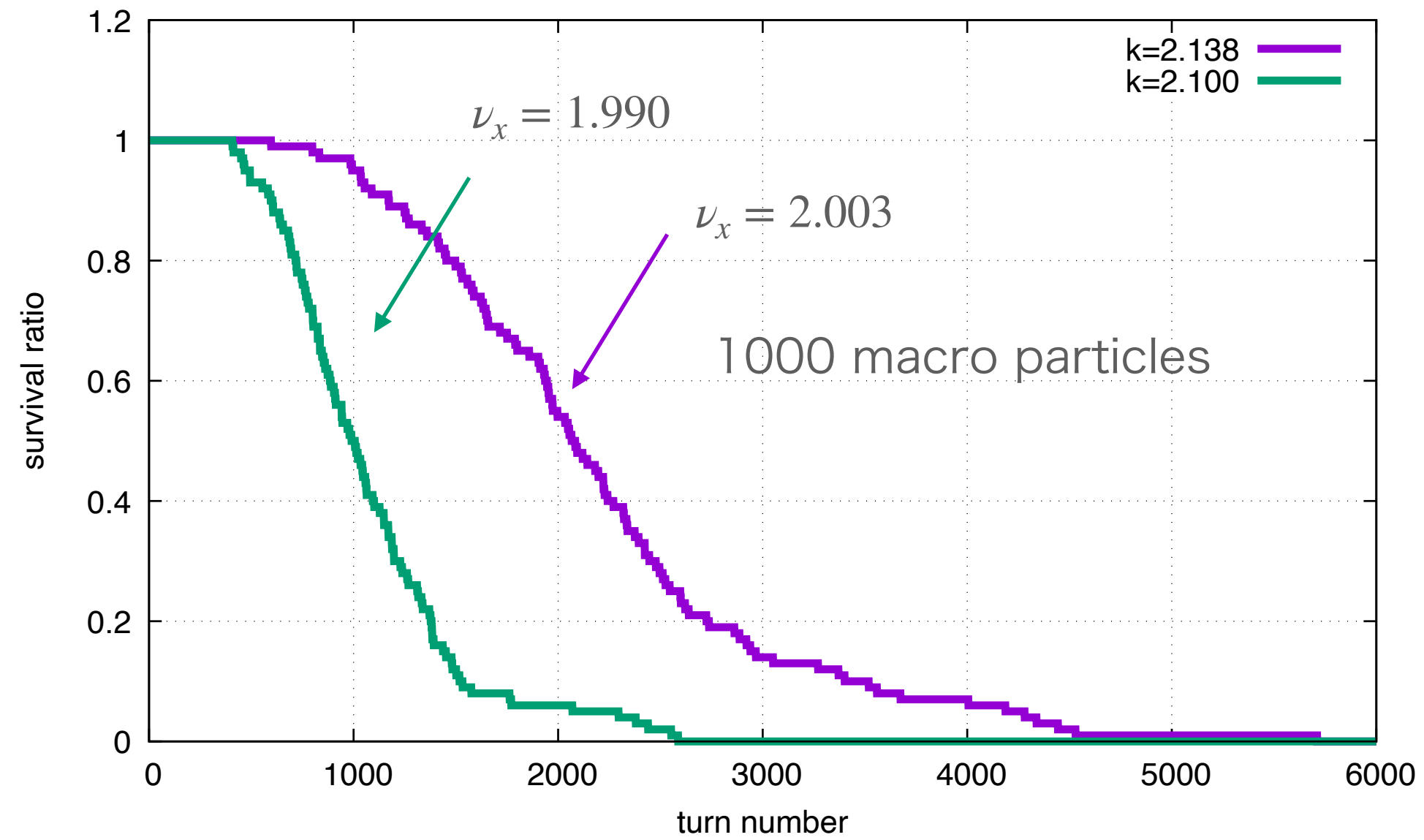
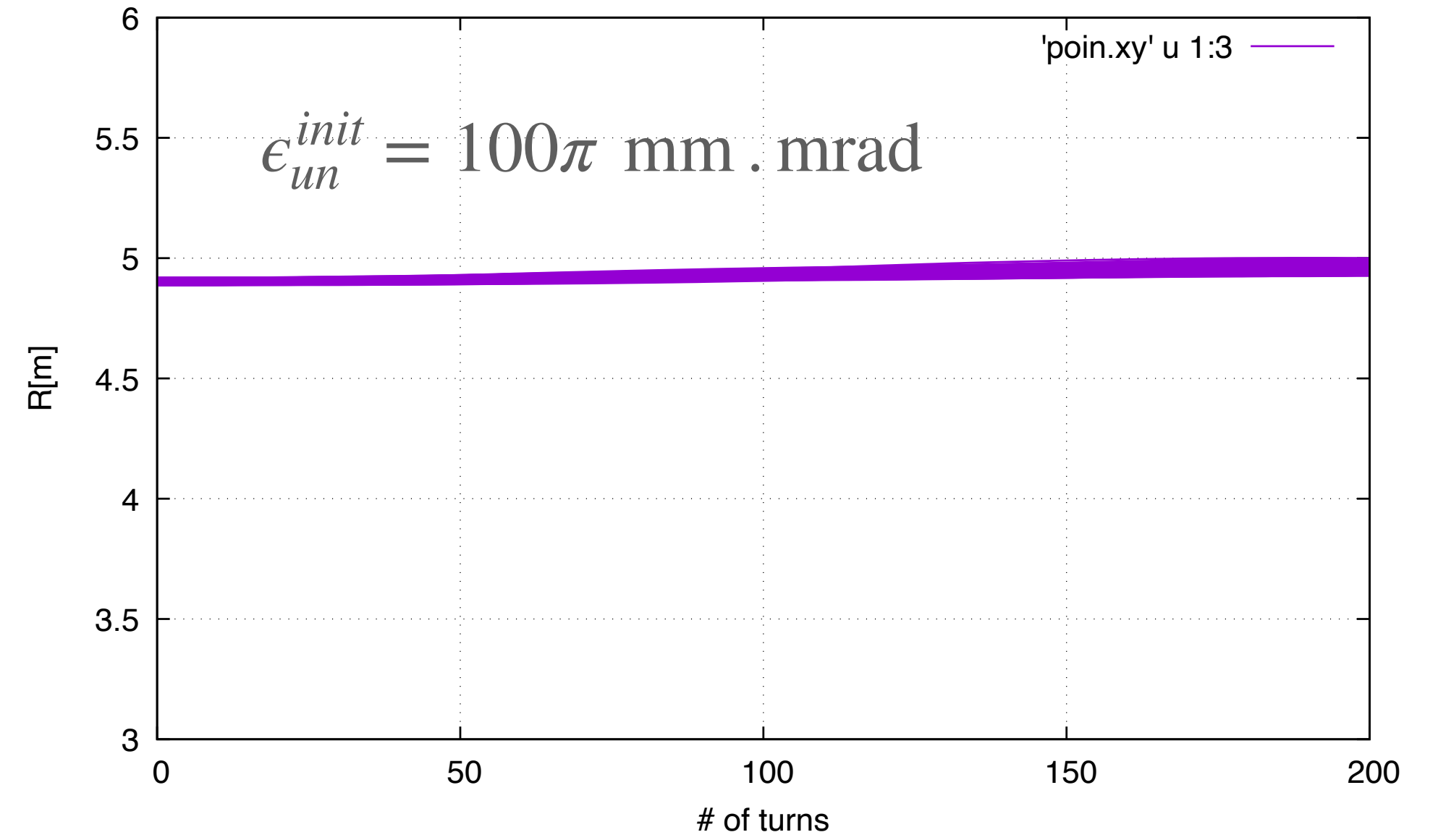
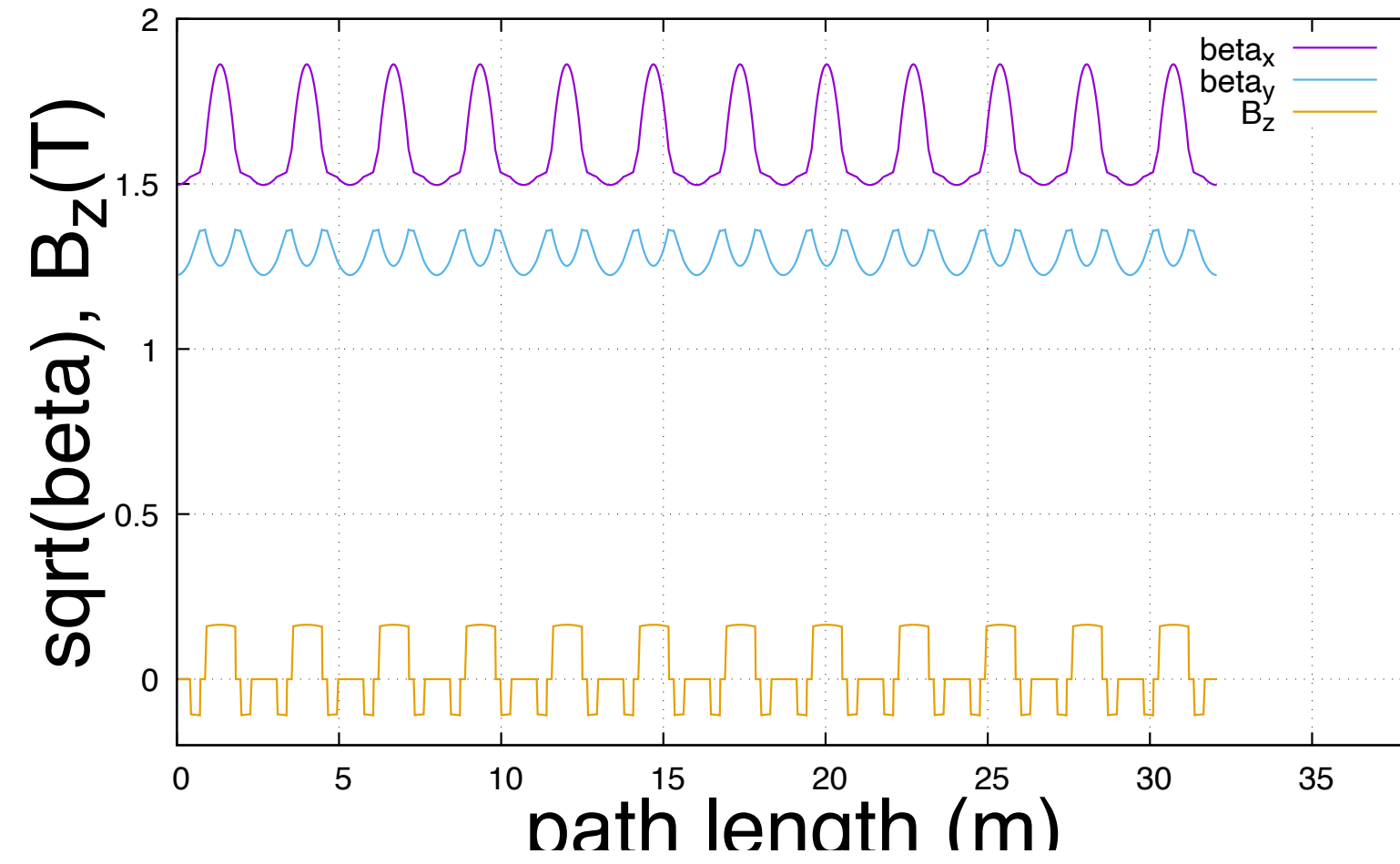
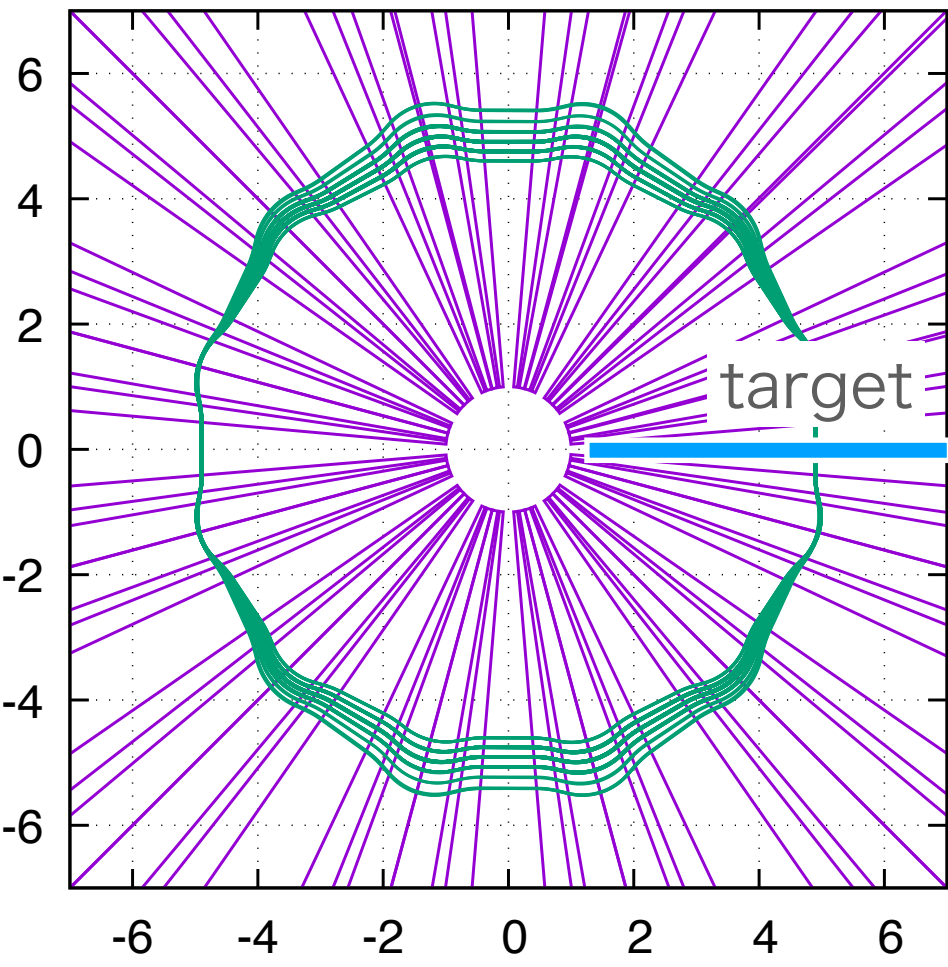
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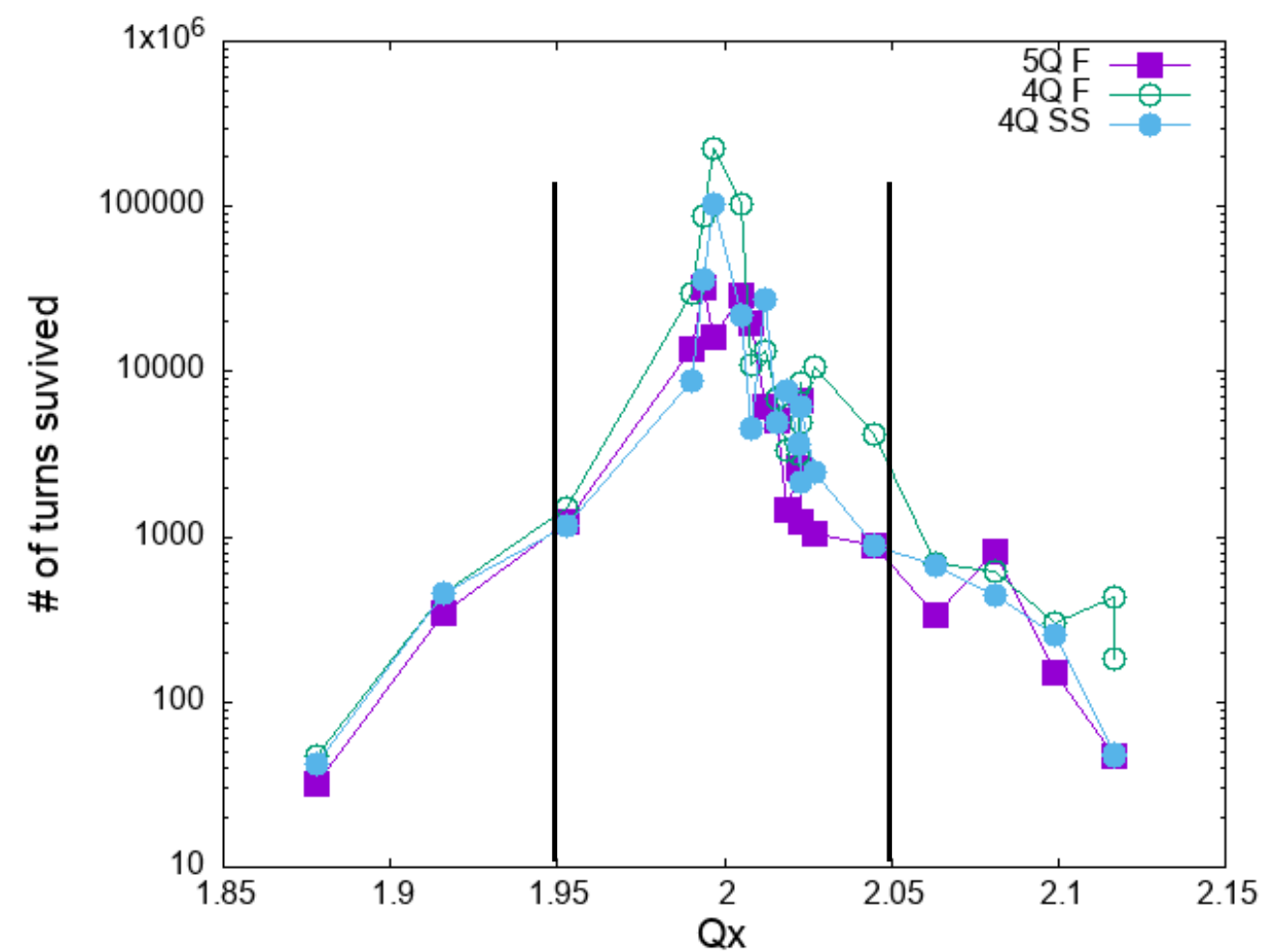
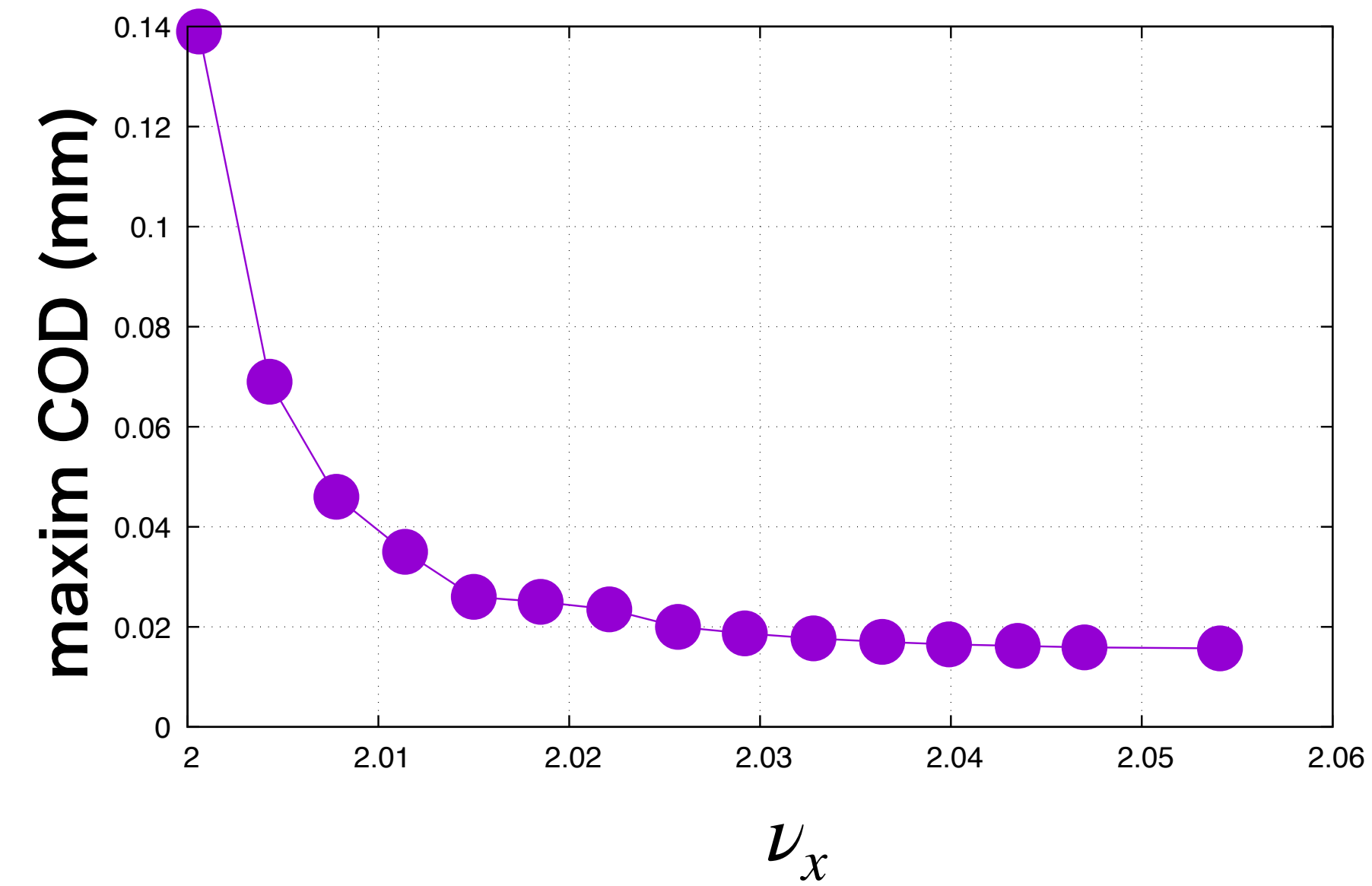
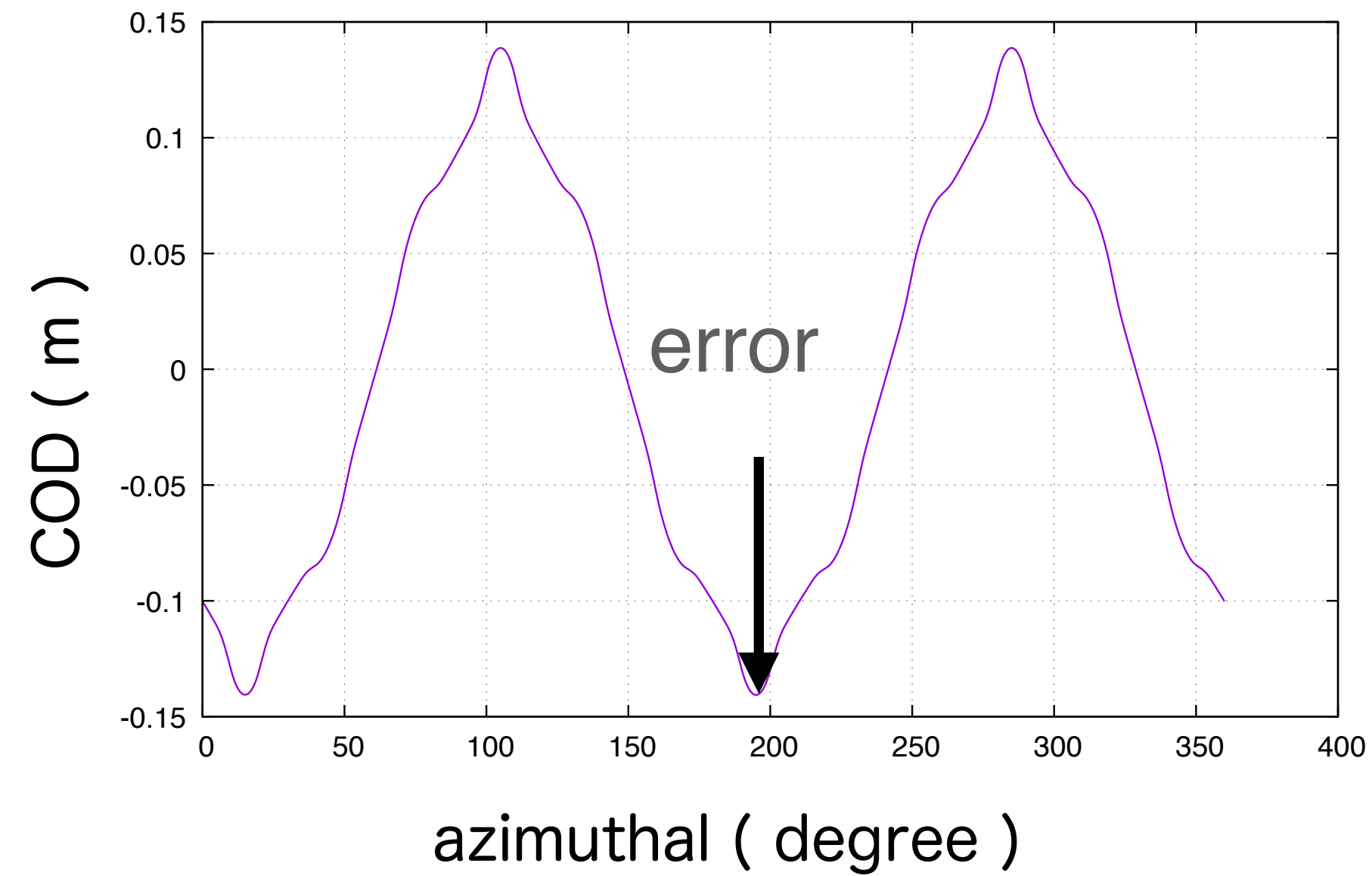
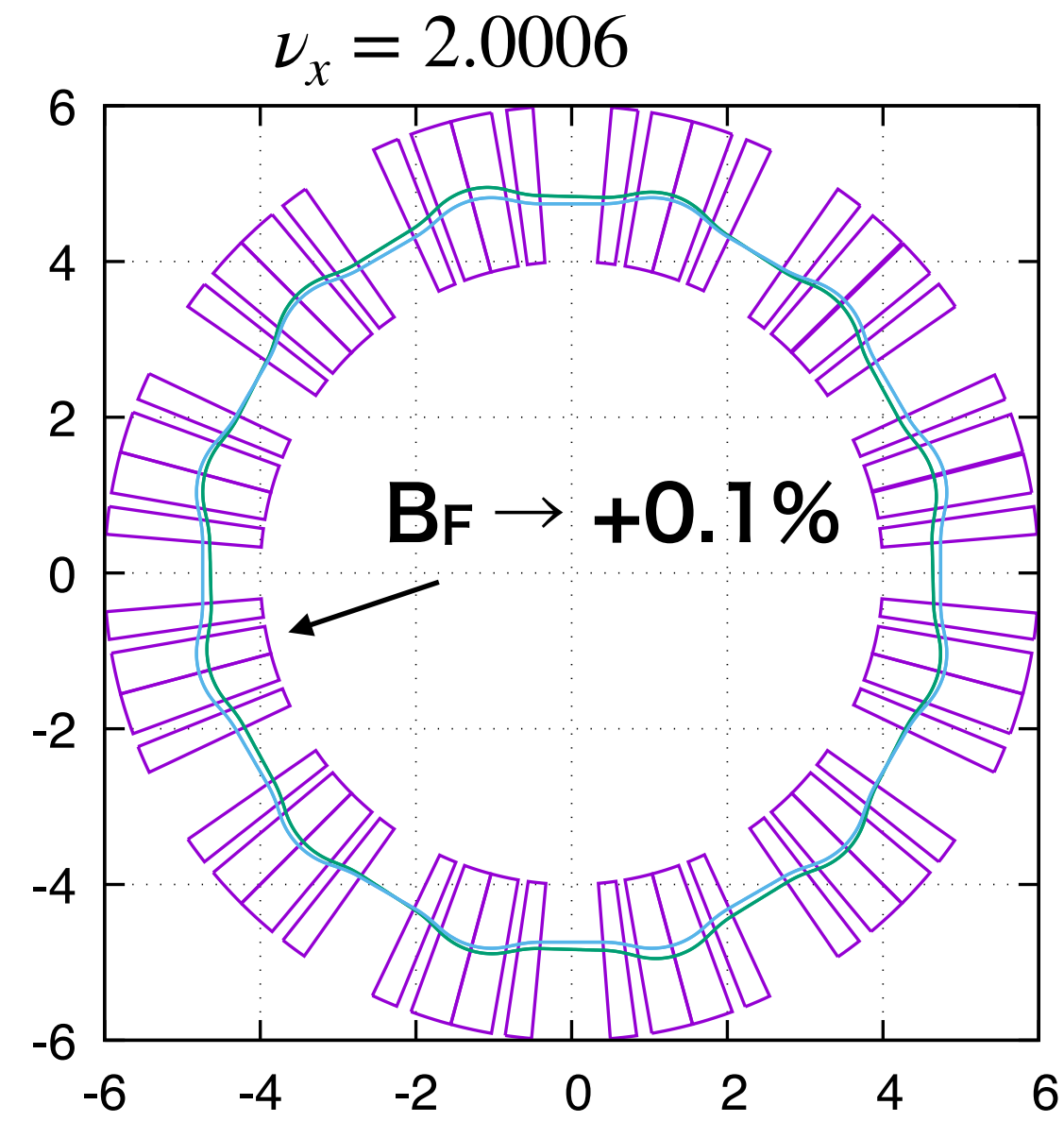
multi particle tracking

$k = 2.14, \nu_x = 1.998, \nu_y = 3.090$



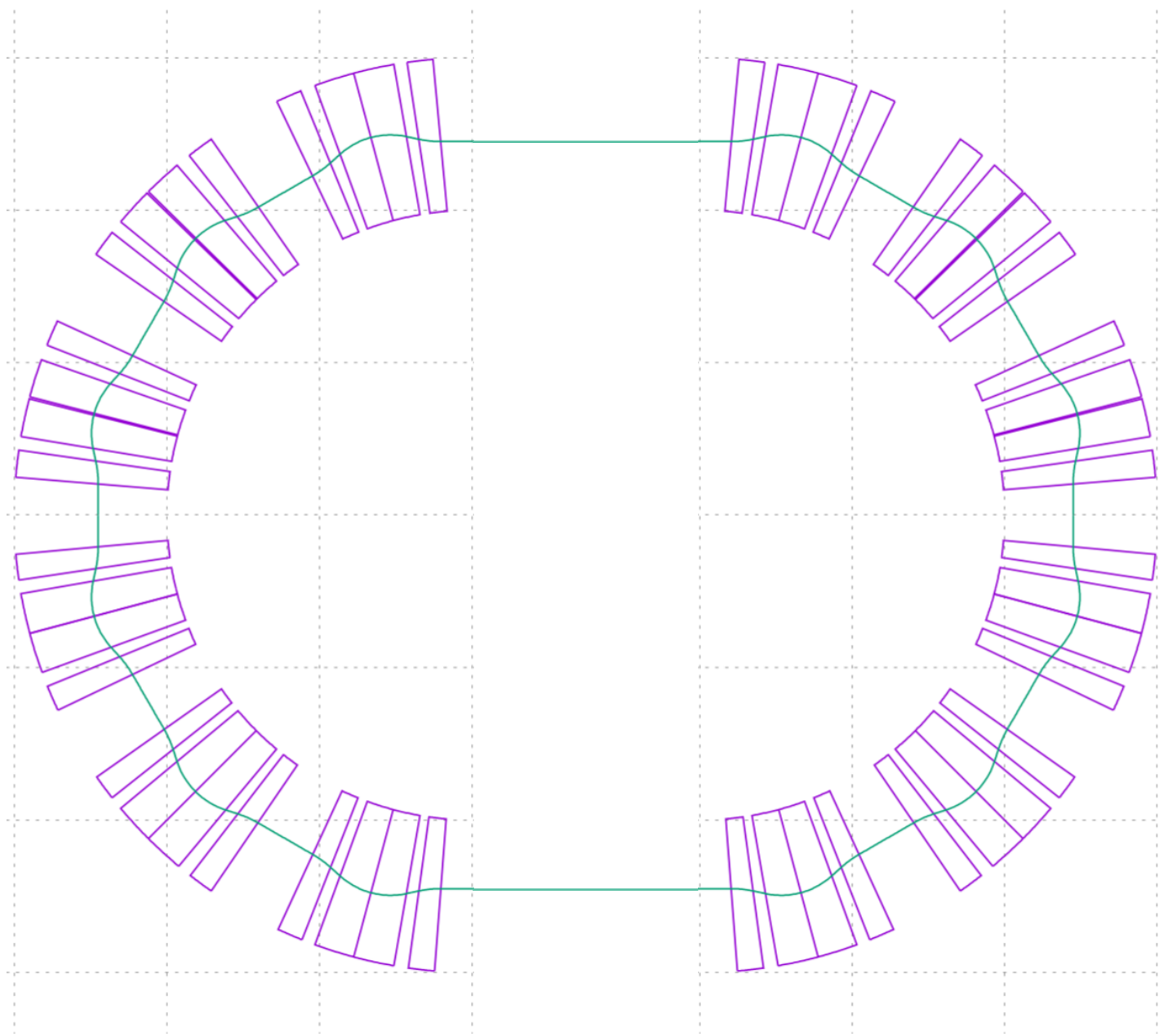
error sensitivity near $\nu_x = 2$

$k=2.140$



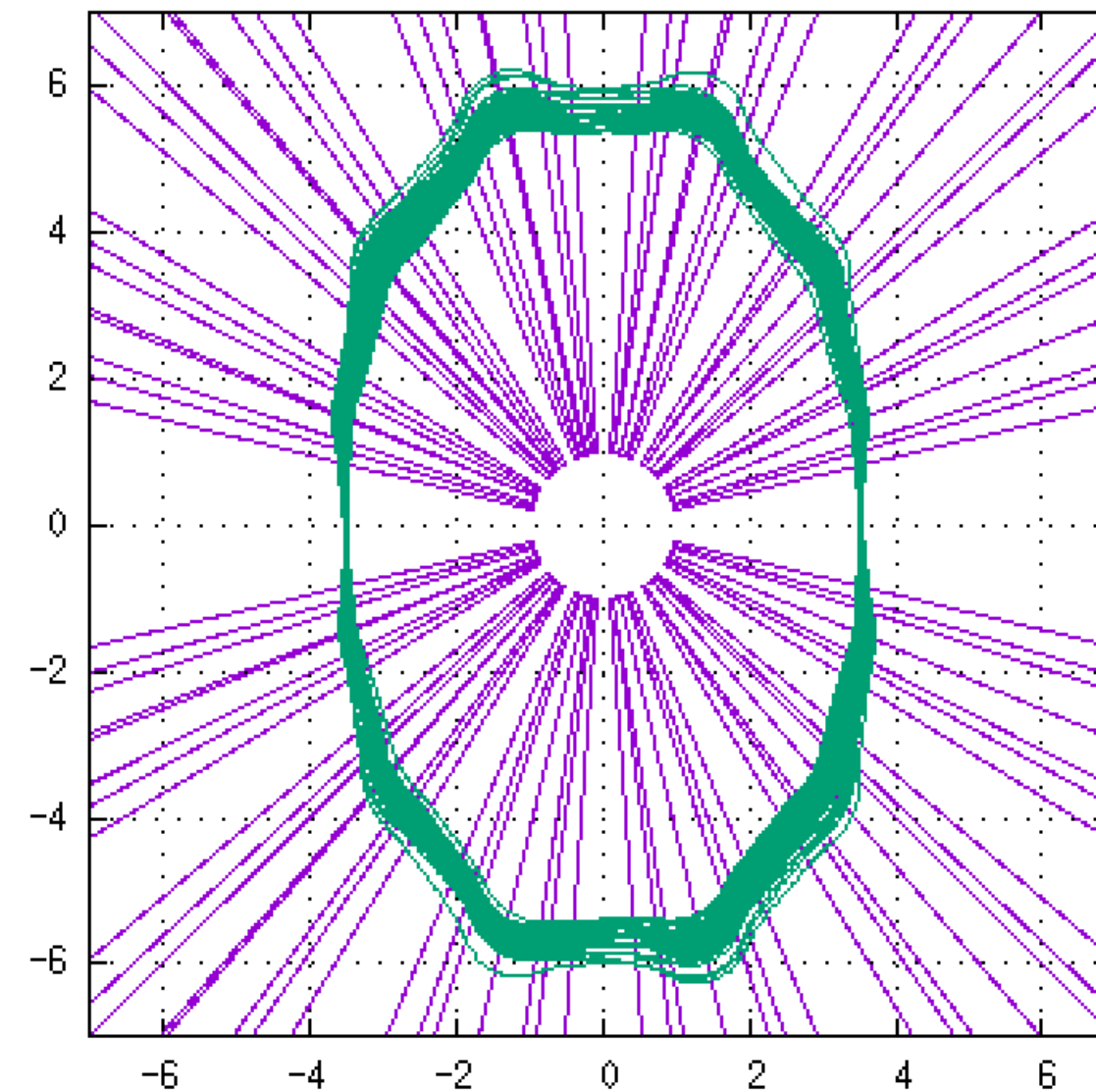
setting the ν_x at least 0.05 away from the $\nu_x = 2$, beam survives ~ 1000 turns.

ERIT with long straight



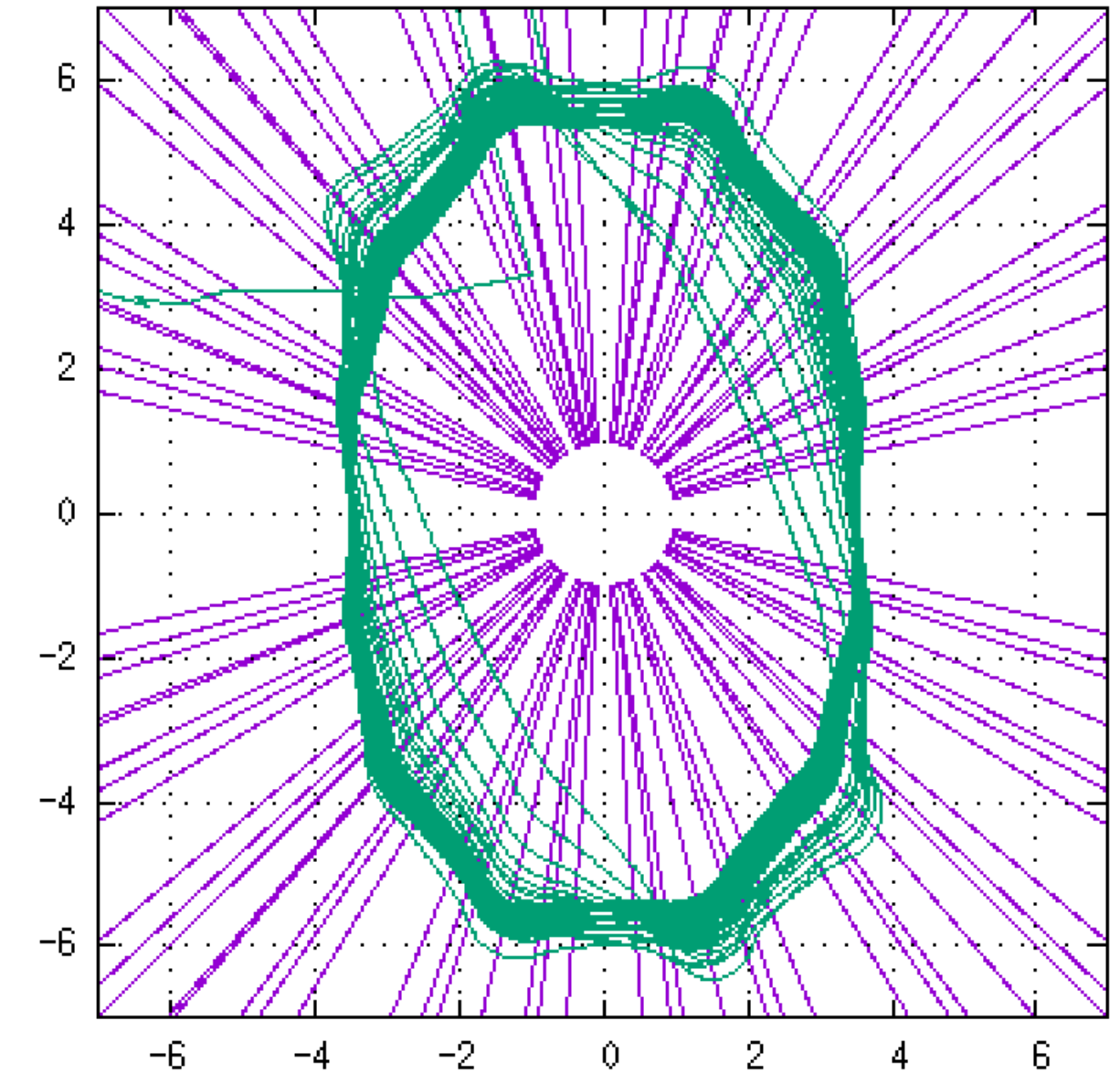
race track configuration
violates the scaling law
which is essential for multi-
charge ERIT

$$\nu_x = 1.95$$



insertion of the wedge drift
section fulfills the scaling
law

$$\nu_x = 1.96$$



the approach to the resonance
 $1\nu_x = 2$
makes closed orbit unstable

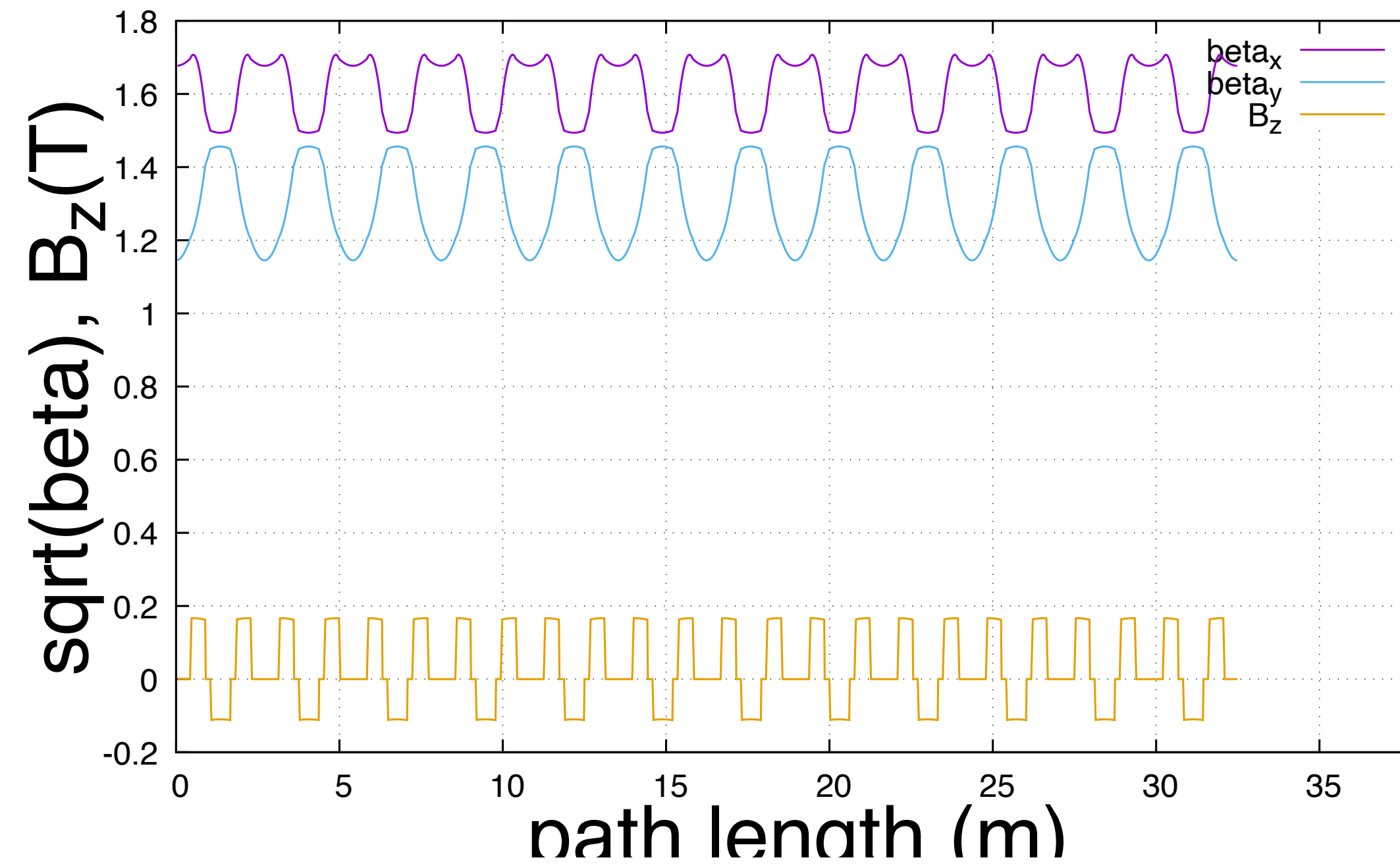
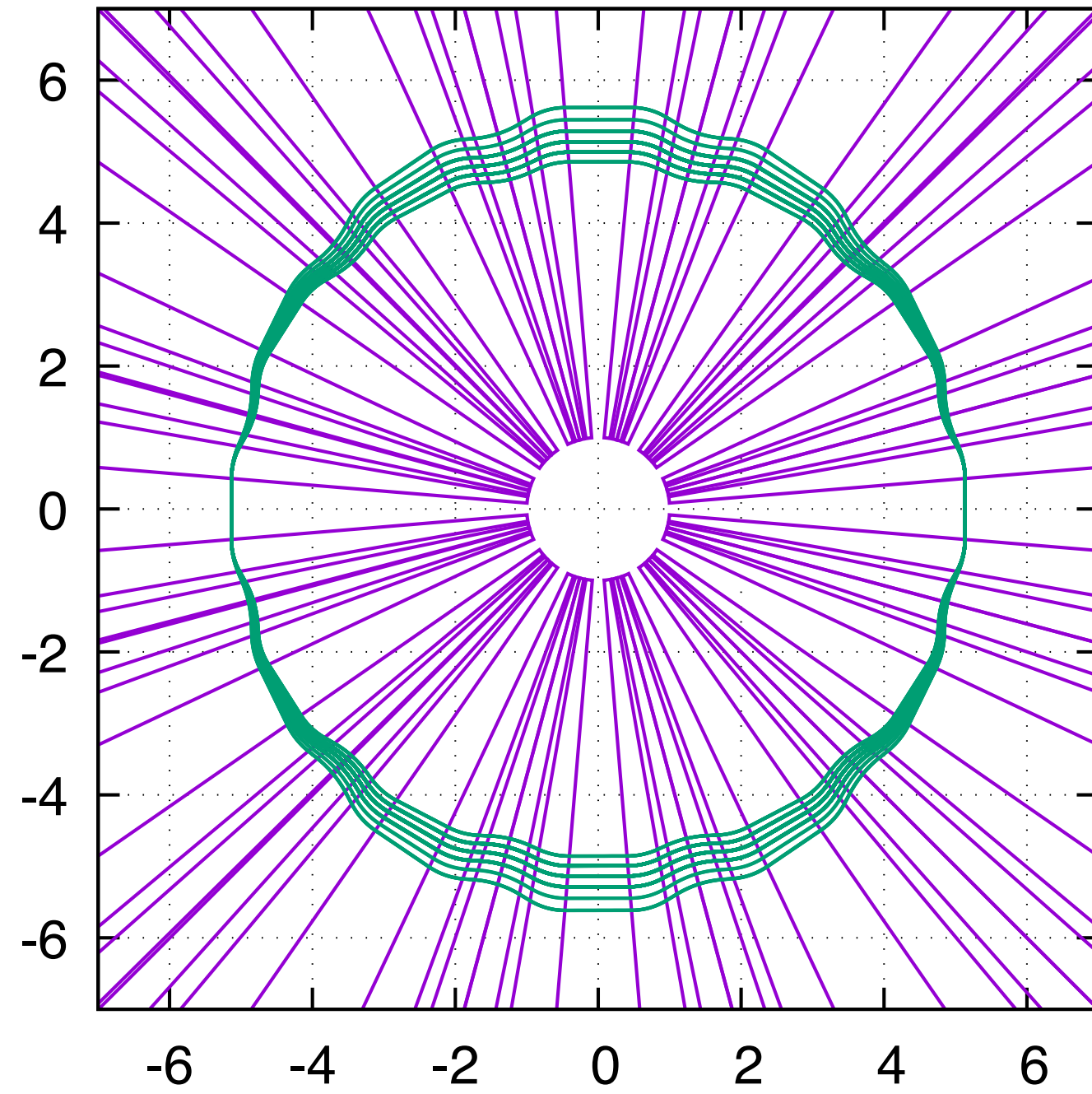
Summary

1. ERIT for producing superheavy element as one of the plans for reuse of the main ring is under consideration.
2. Multi charge state beams can circulate in the ring with the target located at the pseudo dispersion free section.
3. Operating ERIT near $\nu_x = 2.05$ (1.95) can accumulate multi-charged beams.
4. Zero chromaticity is essential for multi-charge state ERIT.
5. Use the Lagrangian insertion?

backup 1

qx_lin qy_lin 1.9951819469793564 3.1304266121053614

FDF



```

#####
# S1 #####
ls      drift    4.75d0    0.000000  1.0      0.0      10      0.      0.
fmag    fmag     5.12d0    -1.7000   5.2000   2.500    10      1.      1.
ss      drift    1.7d0     0.000000  1.0      0.0      10      0.      0.
dmag    dmag     3.43d0    1.200000  5.2000   2.500    10      1.      0.
dmag    dmag     3.43d0    1.200000  5.2000   2.500    10      0.      1.
ss      drift    1.7d0     0.000000  1.0      0.0      10      0.      0.
fmag    fmag     5.12d0    -1.7000   5.2000   2.500    10      1.      1.
ls      drift    4.75d0    0.000000  1.0      0.0      10      0.      0.
//
    
```