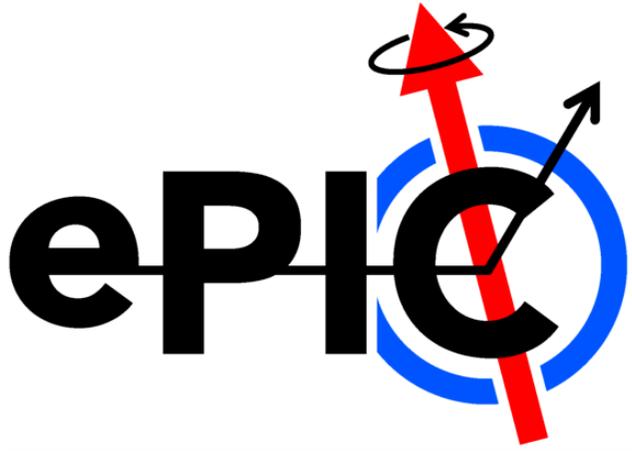




Comments / Thoughts about low Q^2 physics program with ePIC

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DOE NP contract: DE-SC0013405

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Outline

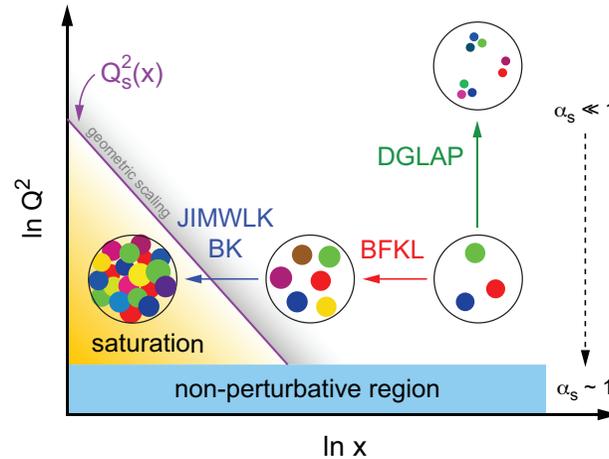
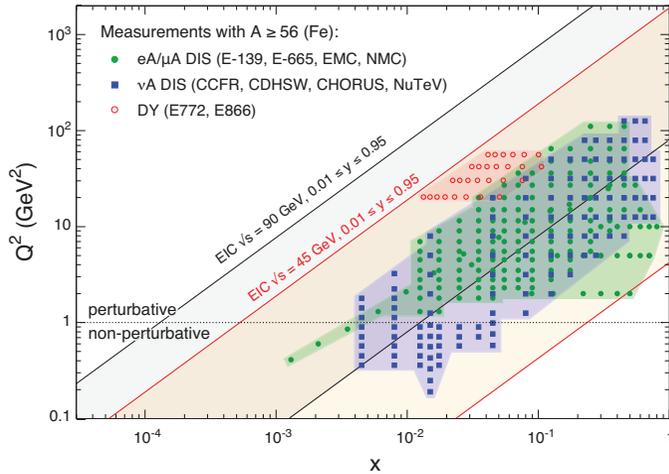
- Formulation of inclusive ep scattering: DIS to PHP

Transition from **high Q^2** to **low Q^2** to **photo production**

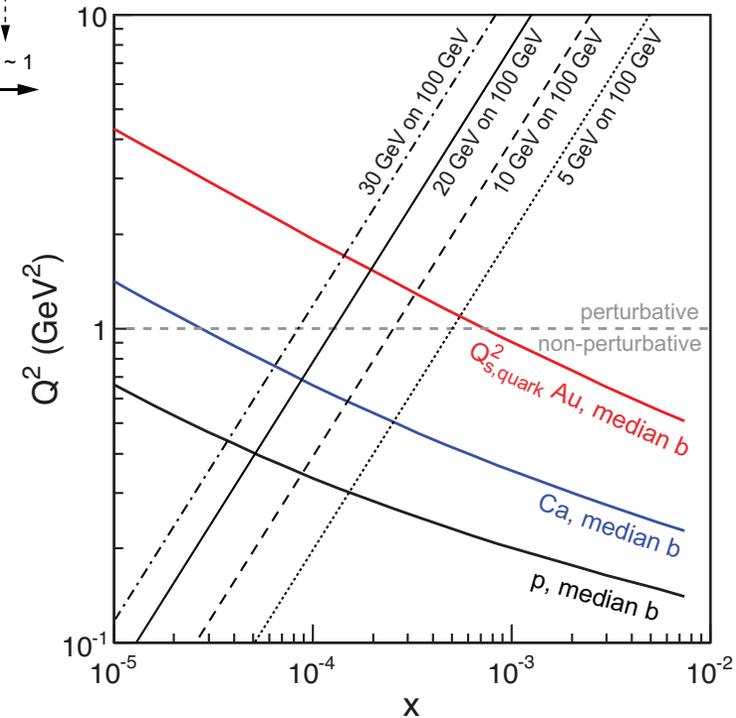
- HERA data
- Kinematic variable **resolution** / **precision** (Angular and Energy scale precision)
- Acceptance - ePIC
- Requirements
- Summary

Motivation

Exploring low-x physics / Onset of saturation phenomena at EIC



- Transition from **pert. to non-pert. region** around $Q^2 = 1 \text{ GeV}^2$
- **Partonic (Large Q^2) to hadronic behavior (Low Q^2)**, in particular in photoproduction limit, i.e. $Q^2 \rightarrow 1 \text{ GeV}^2$
- Formulation of **structure function $F_2(x, Q^2)$ to $\gamma^* p$ cross-section $\sigma_{\text{tot}}^{\gamma^* p}(W^2, Q^2)$** , in particular in photoproduction limit, i.e. $Q^2 \rightarrow 1 \text{ GeV}^2$
- Probing transition region requires measurements around $Q^2 = 1 \text{ GeV}^2$, above and below, down to at least $Q^2 = 0.1 \text{ GeV}^2$



Formulation of inclusive ep scattering: DIS to PHP

□ Process

$$s = (k + p)^2 \simeq 4E_e E_P$$

$$t = (p - p')^2$$

$$u = (k' - p)^2$$

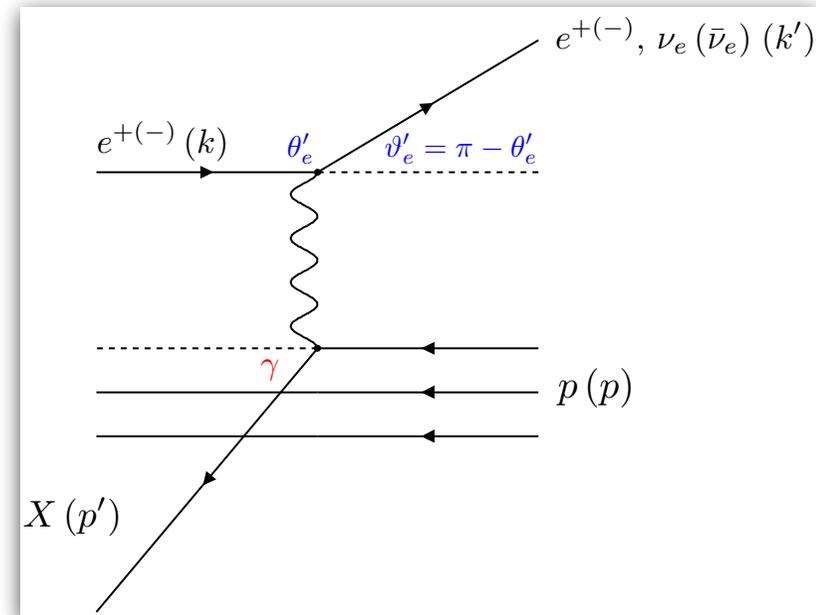
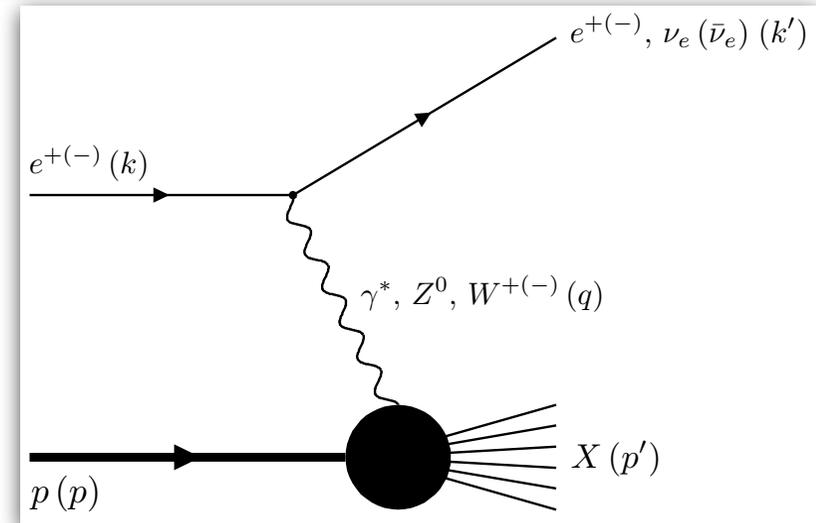
$$Q^2 = -(k - k')^2 = -(p - p')^2 = -t = -q^2$$

$$x = \frac{Q^2}{2(p \cdot q)} \simeq -\frac{t}{u+s} \quad 0 \leq x \leq 1$$

$$y = \frac{p \cdot q}{p \cdot k} \simeq \frac{u+s}{s} \quad 0 \leq y \leq 1$$

$$W^2 = (p + q)^2 = (p')^2 = m_p^2 + \frac{Q^2}{x}(1-x) \simeq s + t + u$$

- Large W^2 refers to **small x** / At very small x : $W^2 \approx Q^2/x!$
- **Small x** refers to **high-energy region (Large W^2)** in $\gamma^* p$ scattering!
- Coordinate system: Positive z-axis along proton direction / Sometimes angle $\vartheta'_e = \pi - \theta'_e$ is used instead of θ'_e !



Formulation of inclusive ep scattering: DIS to PHP

- Structure function
 - At large Q^2 , well above $Q^2 = 1 \text{ GeV}^2$, *partonic behavior dominates* / *Theoretical description of pQCD* in terms of unpolarized PDFs and evolution using *DGLAP evolution!*
 - The *formulation in terms of structure functions* is appropriate at large Q^2 with kinematic variables of: $x(y) / Q^2$
 - Double-differential cross-section:

$$\left(\frac{d^2\sigma}{dydQ^2} \right)_{\text{Born}} = \frac{2\pi\alpha^2 Y_+}{yQ^4} \left(F_2 - \frac{y^2}{Y_+} F_L \right)$$

with:

$$Y_+ = 1 + (1 - y)^2 \quad F_L = F_2 - 2xF_1$$

Formulation of inclusive ep scattering: DIS to PHP

□ Cross-section $\gamma^* p$ scattering

- Besides differential ep cross-section in terms of structure functions, one can interpret ep cross-section as the product of the **flux of virtual photons** and **$\gamma^* p$ cross-section**:

$$\sigma_{\text{tot}}^{\gamma^* p}(W^2, Q^2) \equiv \sigma_{\text{T}}^{\gamma^* p}(W^2, Q^2) + \sigma_{\text{L}}^{\gamma^* p}(W^2, Q^2)$$

- The **total virtual-photon proton cross-section** is given as follows: **At small x:**

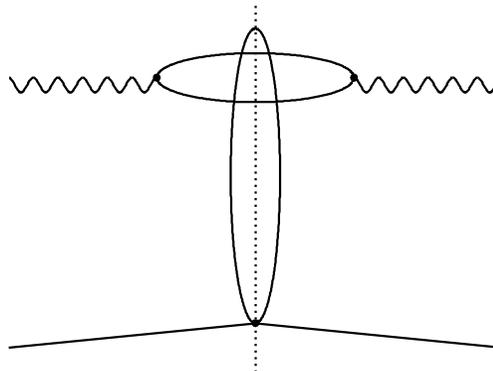
$$\sigma_{\text{tot}}^{\gamma^* p}(W^2, Q^2) = \frac{4\pi^2\alpha}{Q^2(1-x)} \frac{Q^2 + 4m_p^2x^2}{Q^2} \cdot F_2(x, Q^2)$$

$$\sigma_{\text{tot}}^{\gamma^* p}(W^2, Q^2) \approx \frac{4\pi^2\alpha}{Q^2} \cdot F_2(x, Q^2)$$

- The **formulation in terms of cross-sections** is appropriate at small Q^2 and small x ($x < 0.01$), requiring that the lifetime of the virtual photon is large compared to the interaction time. **Appropriate kinematic variables** are: **W^2 and Q^2**
- This is in particular true in the photoproduction limit $Q^2 \rightarrow 0$ for which $F_2 \rightarrow 0!$

Formulation of inclusive ep scattering: DIS to PHP

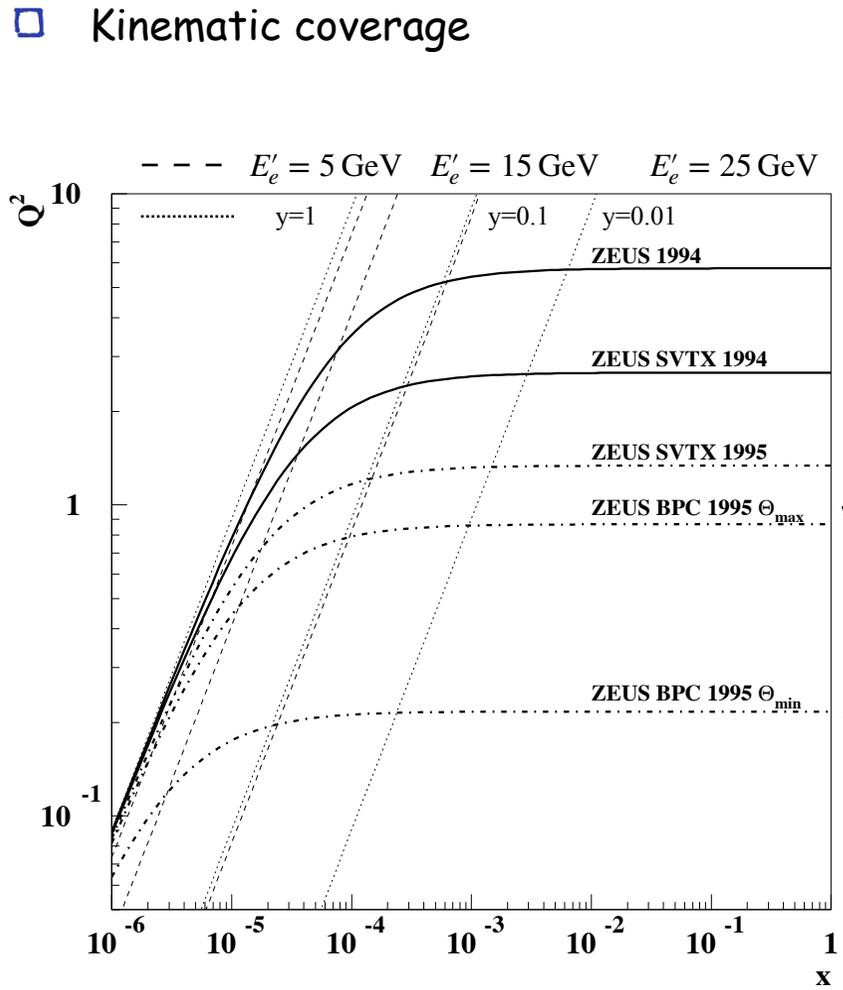
- Comments on formulation DIS to PHP
 - At large Q^2 , well above $Q^2 \approx 1 \text{ GeV}^2$, slope ($\lambda(Q^2)$) in $F_2 \sim x^{-\lambda(Q^2)}$ rises with Q^2 / Partonic behavior dominates, successfully described by pQCD / DGLAP evolution!
 - Below $Q^2 \approx 1 \text{ GeV}^2$, slope in $F_2 \sim x^{-\lambda(Q^2)}$ is flat in Q^2 / pQCD / DGLAP evolution breaks down / Hadronic behavior dominates with similar energy dependence (W^2) for $\sigma_{\text{tot}}^{\gamma^*p}(W^2, Q^2)$ as total photoproduction cross-section, $\sigma_{\text{tot}}^{\gamma p}(W^2)$!
 - New formulation of ep scattering at low x born out of HERA program: Color-dipole picture at low x ($x < 0.01$) by several groups



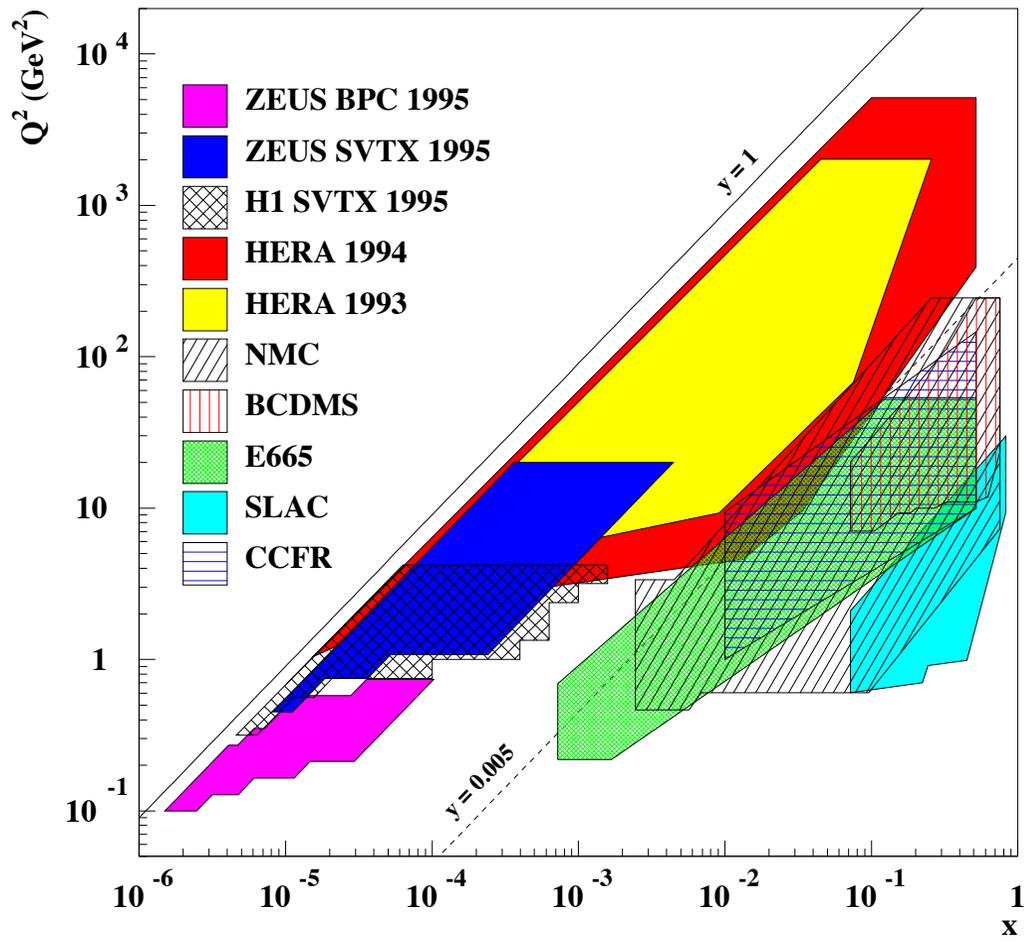


HERA data

Kinematic coverage



$\sim 35\text{mrad}$



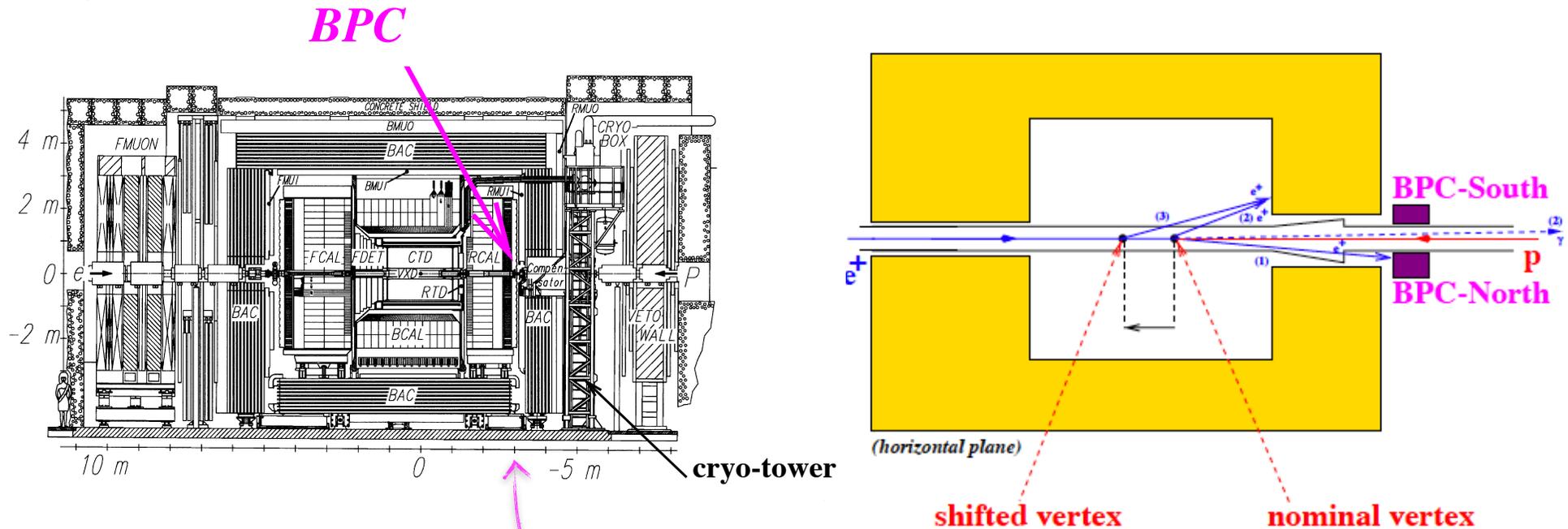
$\sim 17\text{mrad}$

$$Q^2 = 4E_e E_e' \sin^2 \left(\frac{\vartheta_e'}{2} \right) \simeq E_e E_e' \vartheta_e'^2$$

$$\vartheta_e' = \pi - \theta_e'$$

HERA data

- Extension towards small Q^2 : Example from ZEUS

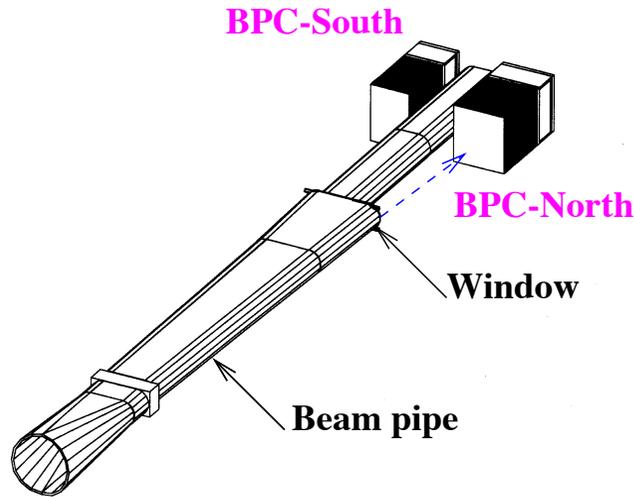


Distance of BPC to nominal IP: 3m

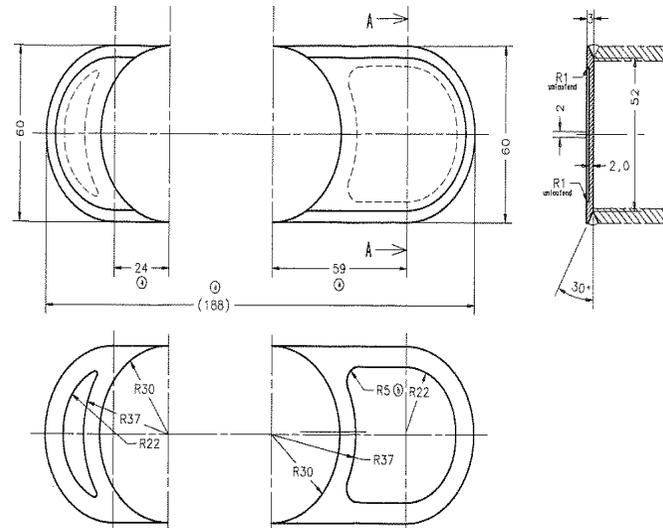
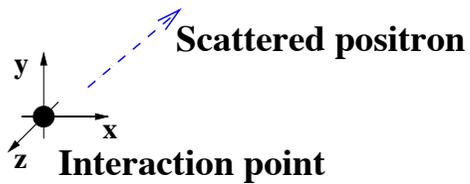
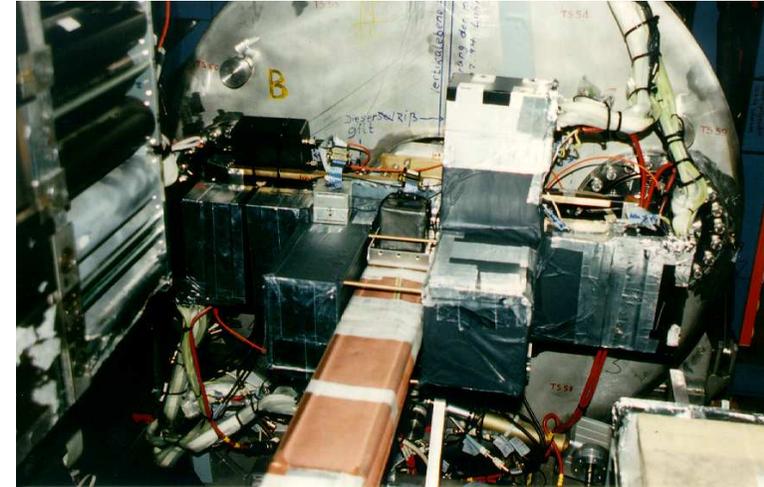
Angular coverage: $\sim 17-35$ mrad

HERA data

- Technical realization for ZEUS Beam-Pipe Calorimeter (BPC)

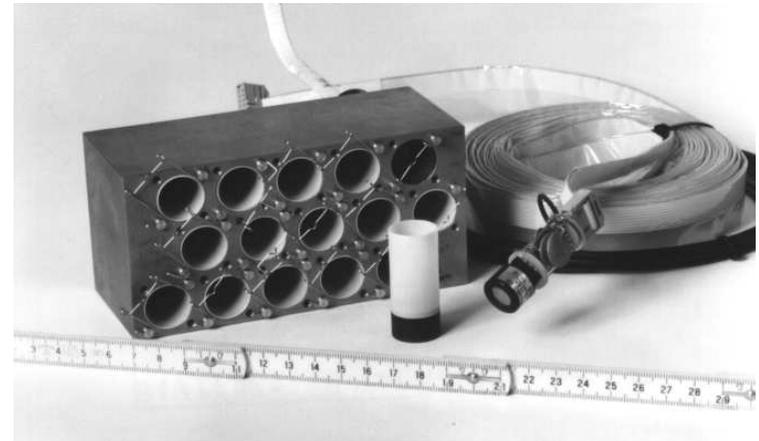
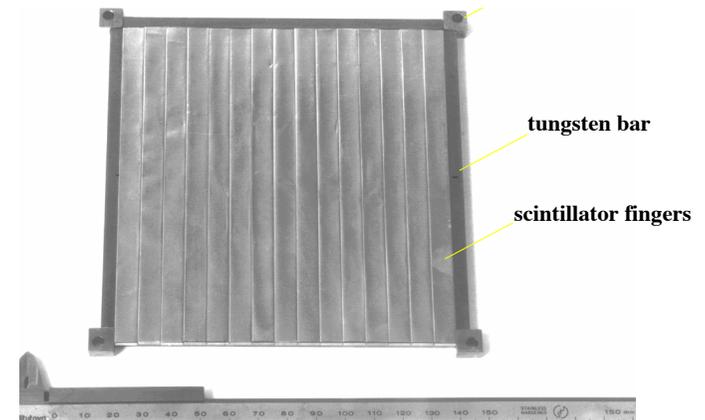
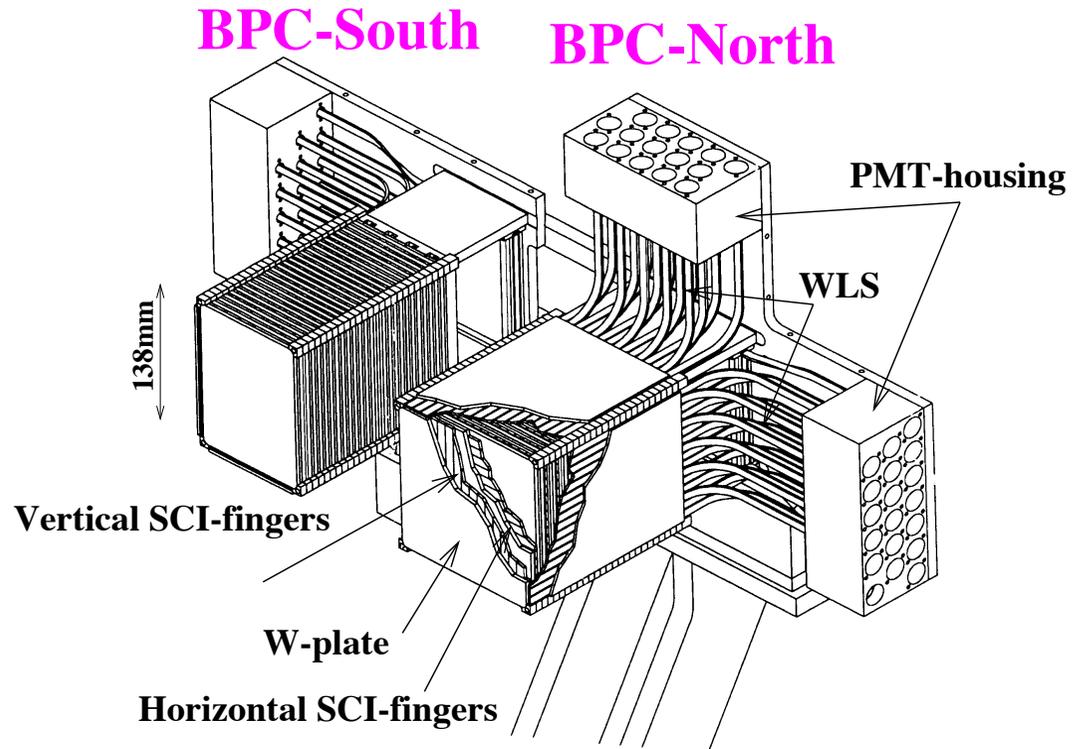


Beam pipe window
(AL): 1.5mm at
2.5m



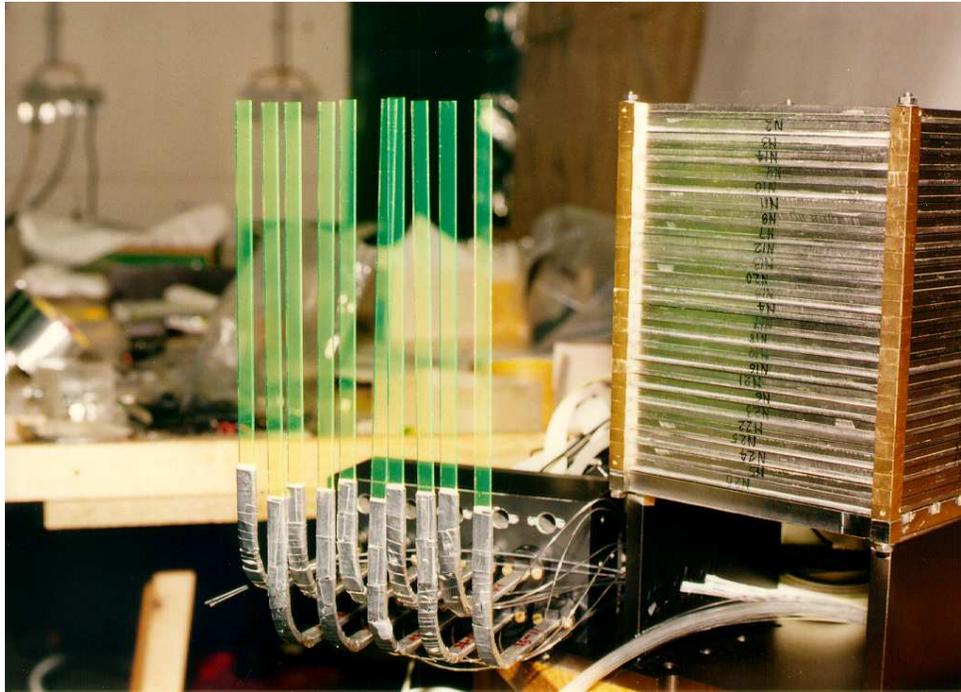
HERA data

- Technical realization for ZEUS Beam-Pipe Calorimeter (BPC)



HERA data

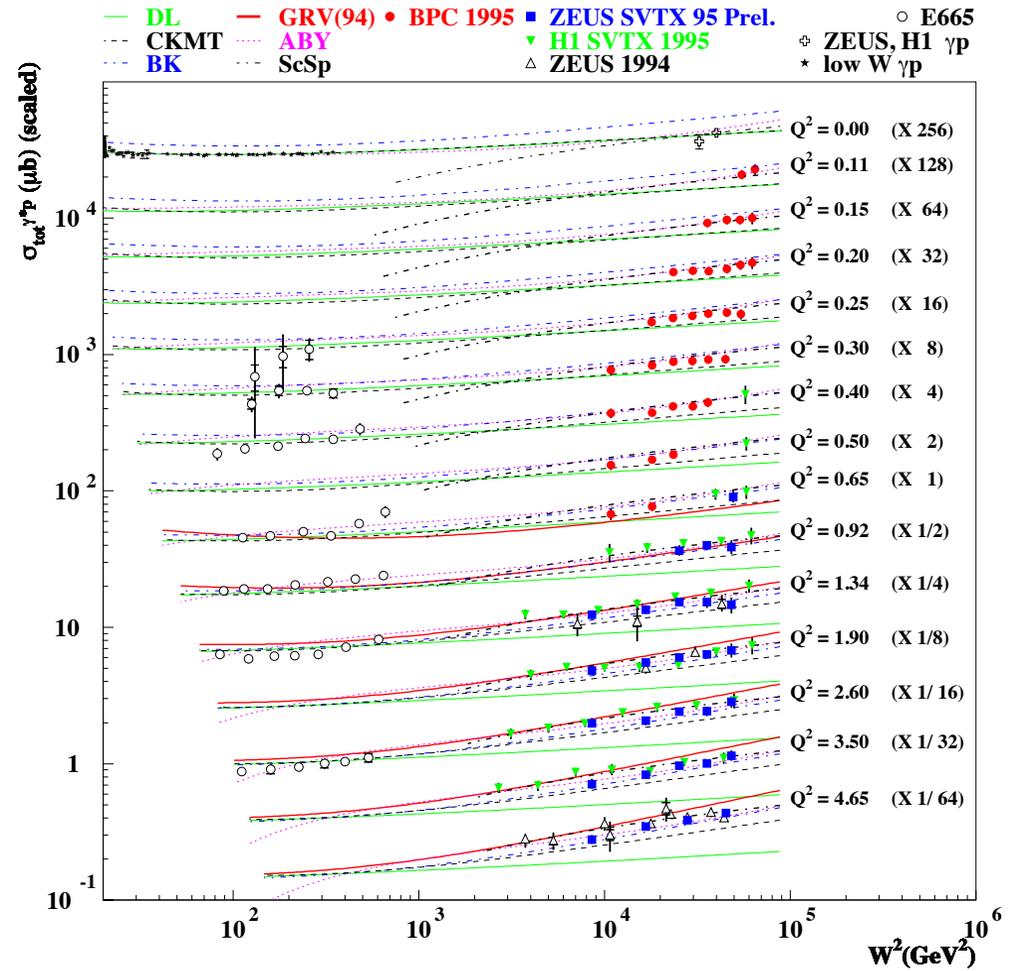
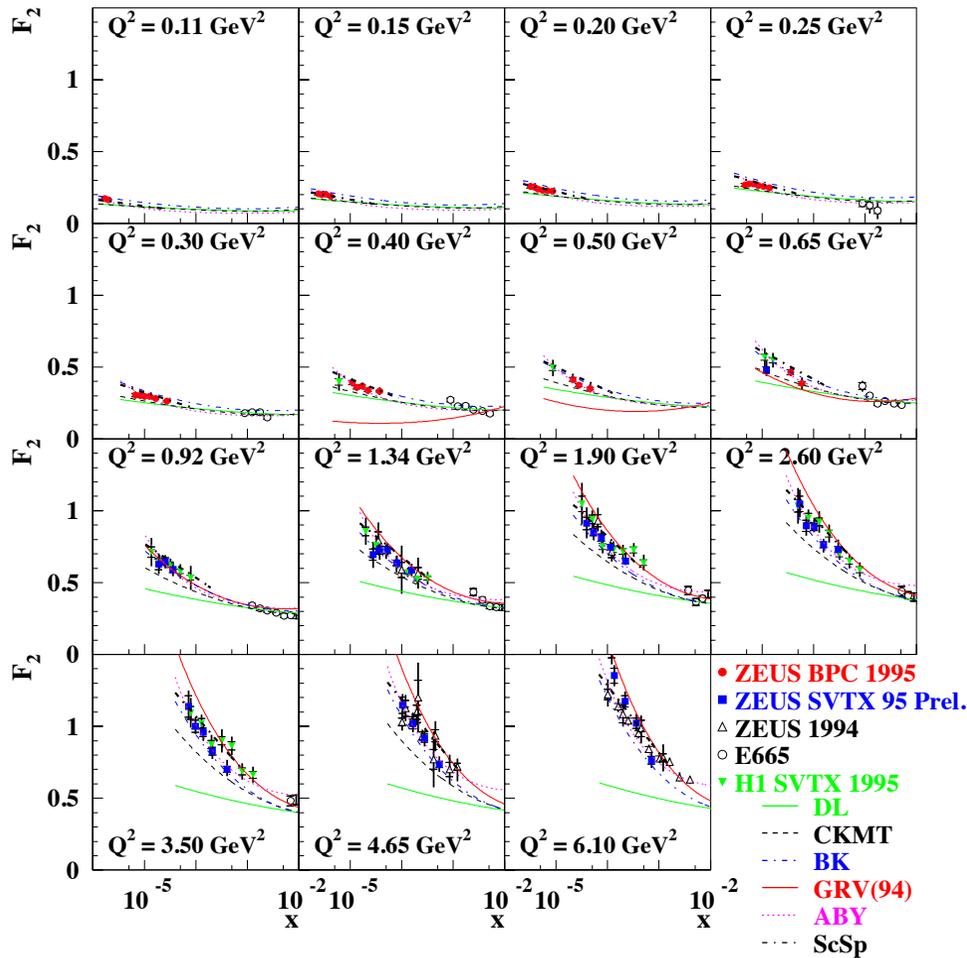
- Technical realization for ZEUS Beam-Pipe Calorimeter (BPC)





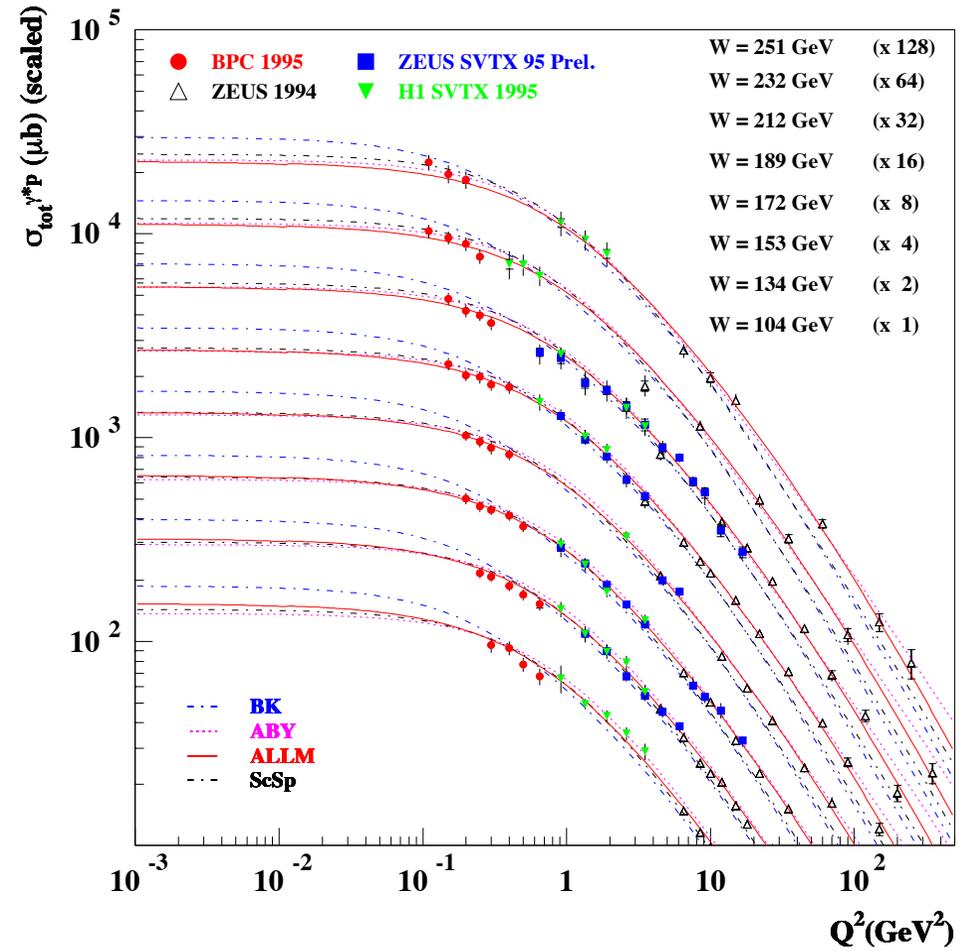
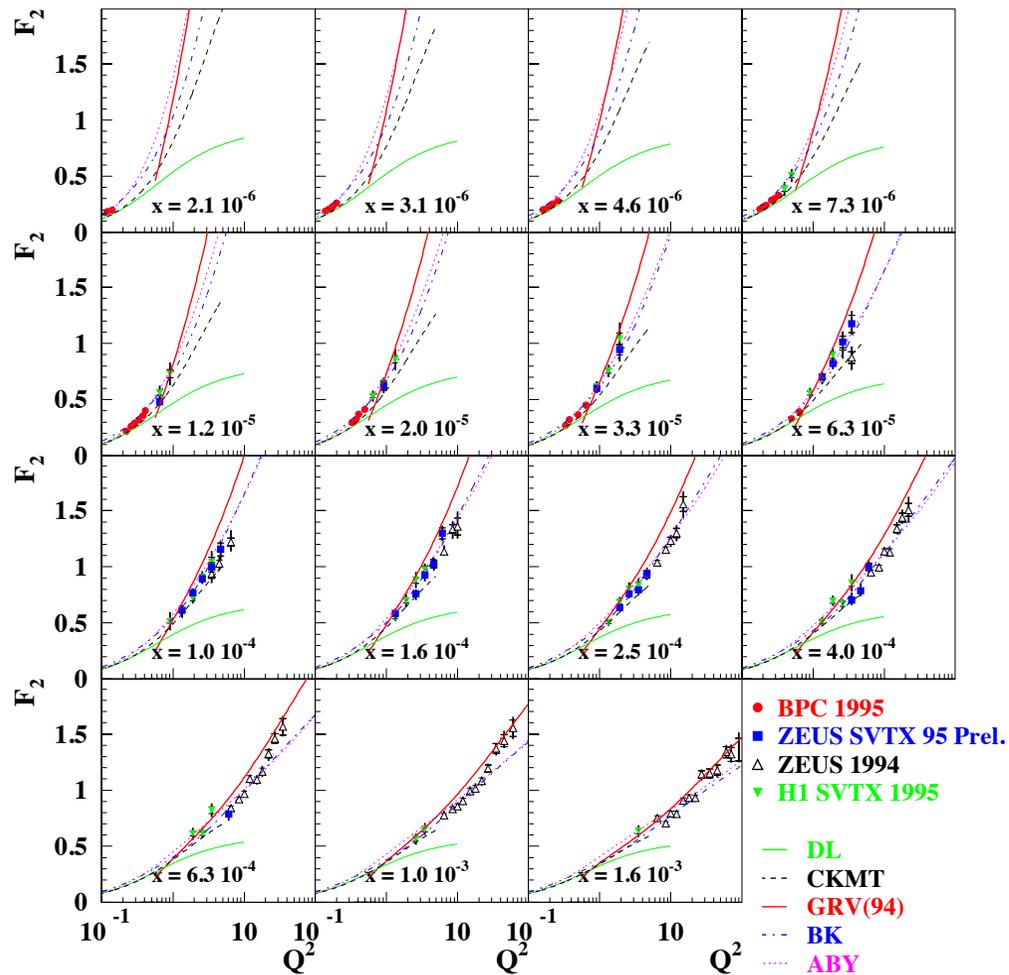
HERA data

□ F_2 vs. x / Cross-section vs. W^2



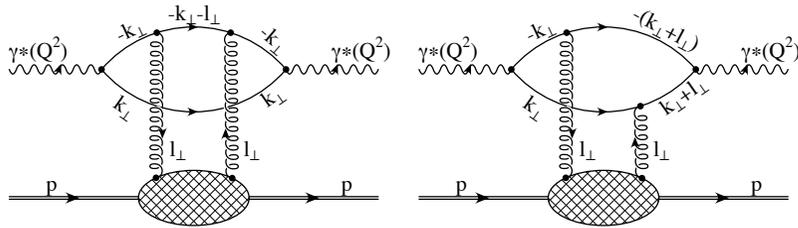
HERA data

□ F_2 vs. Q^2 / Cross-section vs. Q^2



HERA data

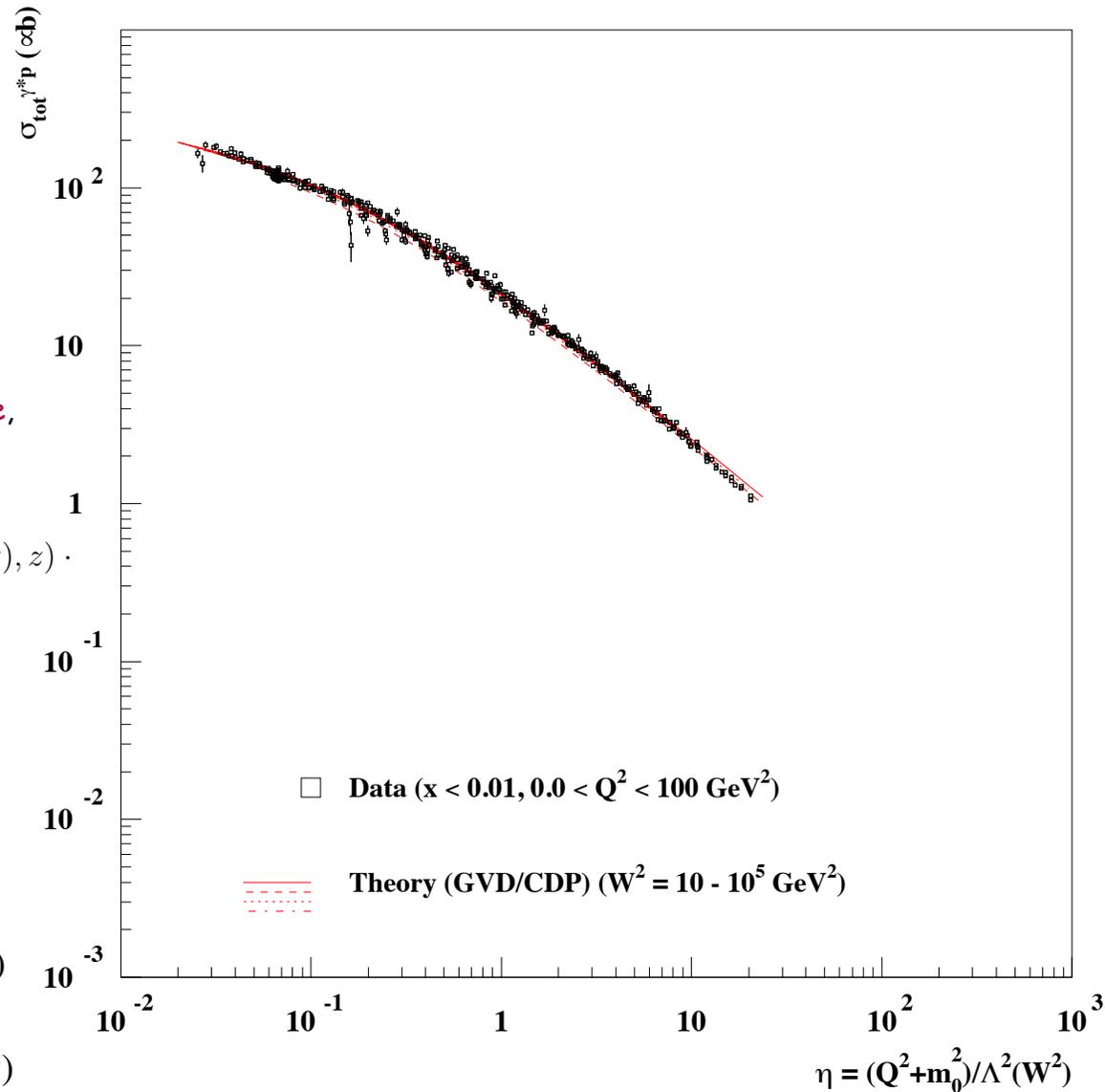
Color-dipole model formulation



- Formulation of $\sigma_{\text{tot}}^{\gamma^*p}(W^2, Q^2)$ in color-dipole picture, including photoproduction limit:

$$\sigma_{\gamma^*p}(W^2, Q^2) = \int dz \int d^2r_{\perp} |\psi|^2(r_{\perp}^2 Q^2 z(1-z), Q^2 z(1-z), z) \cdot \sigma_{(q\bar{q})p}(r_{\perp}^2, z(1-z), W^2).$$

- η -variable:
$$\eta(W^2, Q^2) = \frac{Q^2 + m_0^2}{\Lambda^2(W^2)}$$
- HERA data for $x < 0.01$ exhibit **scaling behavior!**
- Two limits:
 - Q^2 : PHP limit $\lim_{Q^2 \rightarrow 0} \sigma_{\text{tot}}^{\gamma^*p}(W^2, Q^2) = \sigma_{\text{tot}}^{\gamma p}(W^2)$
 - W^2 : HE limit $\lim_{W^2 \rightarrow \infty} \sigma_{\text{tot}}^{\gamma^*p}(W^2, Q^2) = \sigma_{\text{tot}}^{\gamma p}(W^2)$



Kinematic variable resolution and precision

- Mathematical formulation: At low x / high y consider only e -method!

$$Q^2[E'_e, \theta'_e] = 2E_e E'_e (1 + \cos \theta'_e)$$

$$y[E'_e, \theta'_e] = 1 - \frac{E'_e}{2E_e} (1 - \cos \theta'_e)$$

$$\frac{\partial Q^2}{\partial E'_e} = 2E_e (\cos \theta'_e + 1) \quad \frac{\partial y}{\partial E'_e} = \frac{\cos \theta'_e - 1}{2E_e}$$

$$\frac{\partial Q^2}{\partial \theta'_e} = -2E_e E'_e \sin \theta'_e \quad \frac{\partial y}{\partial \theta'_e} = -\frac{E'_e \sin \theta'_e}{2E_e}$$

$$(\delta Q^2)^2 = \left(\frac{\partial Q^2}{\partial E'_e}\right)^2 (\delta E'_e)^2 + \left(\frac{\partial Q^2}{\partial \theta'_e}\right)^2 (\delta \theta'_e)^2$$

$$(\delta y)^2 = \left(\frac{\partial y}{\partial E'_e}\right)^2 (\delta E'_e)^2 + \left(\frac{\partial y}{\partial \theta'_e}\right)^2 (\delta \theta'_e)^2$$

$$\theta'_e = 176.5407^\circ / \eta = 3.5 \rightarrow \tan\left(\frac{\theta'_e}{2}\right) \approx 33$$

$$\left(\frac{\delta Q^2}{Q^2}\right) = \frac{\delta E'_e}{E'_e} \oplus \tan\left(\frac{\theta'_e}{2}\right) \delta \theta'_e$$

Q² resolution worsens for large θ'_e , need excellent θ' resolution!

$$\left(\frac{\delta y}{y}\right) = \left(1 - \frac{1}{y}\right) \frac{\delta E'_e}{E'_e} \oplus \left(\frac{1}{y} - 1\right) \cot\left(\frac{\theta'_e}{2}\right) \delta \theta'_e$$

y resolution worsens for small y, need excellent E' resolution!

Acceptance ePIC

□ ePIC Central detector vs. low Q^2 tagger

$$Q^2[x, E'_e] = \frac{xs \left(1 - \frac{E'_e}{E_e}\right)}{1 - \frac{xs}{4E_e^2}}$$

Fixed E'_e

2GeV steps:
2GeV-100GeV

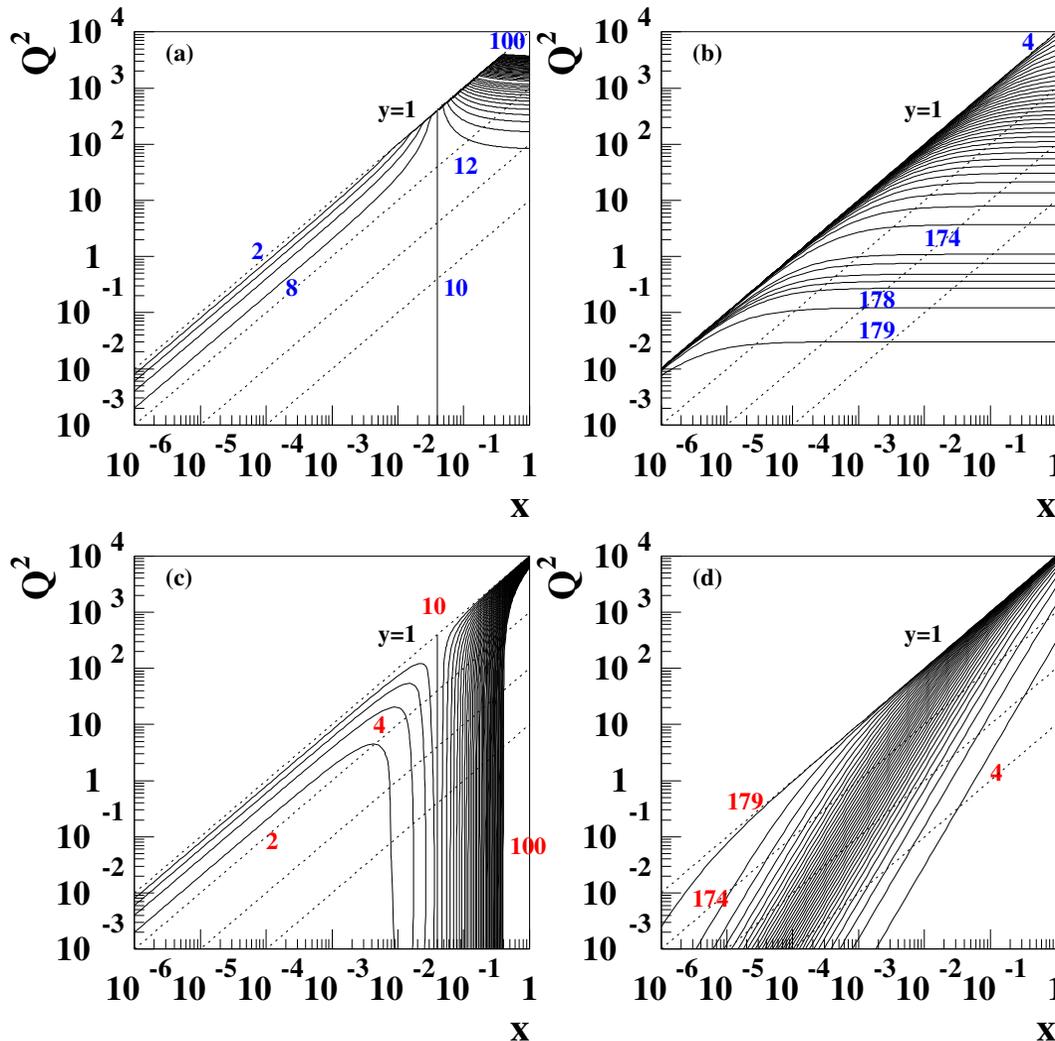
$E_e = 10$ GeV
 $E_p = 250$ GeV

Fixed F

2GeV steps:
2GeV-100GeV

$$Q^2[x, F] = \frac{4E_e F - sx}{\frac{4E_e^2}{sx} - 1}$$

EIC kinematics ($E_e=10$ GeV, $E_p=250$ GeV)



$$Q^2[x, \theta'_e] = \frac{xs}{\frac{xs}{4E_e^2} \tan^2 \frac{\theta'_e}{2} + 1}$$

Fixed θ'_e

5° steps: 4°-174°
1° steps to 179°

plus

$$\theta'_e = 176.5407^\circ / \eta = 3.5$$

Fixed γ

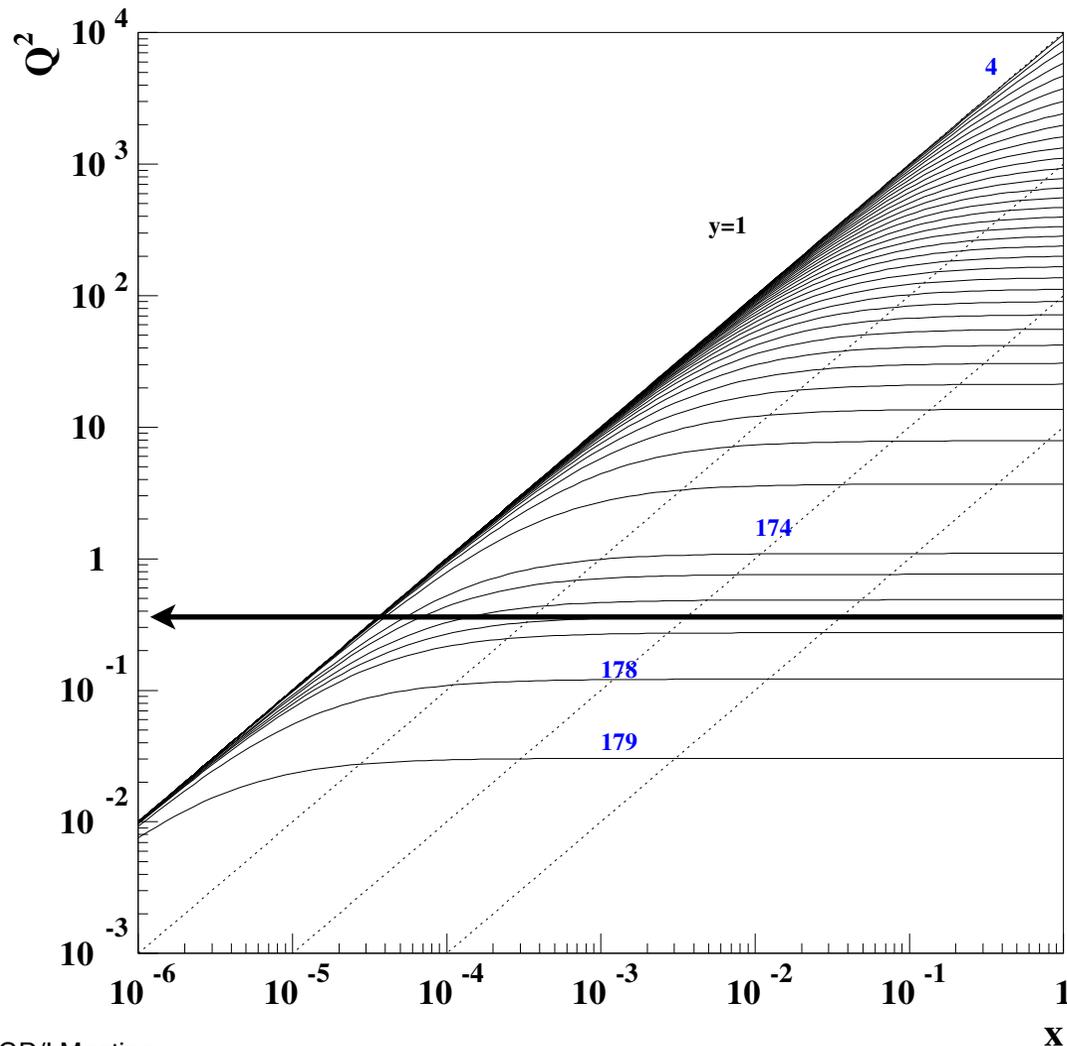
5° steps:
4°-179°

$$Q^2[x, \gamma] = \frac{sx}{\frac{4E_e^2}{sx} \cot^2 \frac{\gamma}{2} + 1}$$

Acceptance ePIC

- ePIC Central detector vs. low Q^2 tagger: Focus on angular acceptance

EIC kinematics ($E_e=10$ GeV, $E_p=250$ GeV)



$$Q^2[x, \theta'_e] = \frac{xs}{\frac{xs}{4E_e^2} \tan^2 \frac{\theta'_e}{2} + 1}$$

Fixed θ'_e

5° steps:
4°-174°
1° steps to
179° plus
176.5407°
 $\theta'_e = 176^\circ$

$$\theta'_e = 176.5407^\circ / \eta = 3.5$$

$\theta'_e = 177^\circ$

- Q^2 acceptance of Low- Q^2 tagger from collaboration meeting: Extremely small values in $Q^2 \rightarrow$ PHP tagger!
- At $\eta = 3.5$ we get: $\theta'_e = 176.5407^\circ$
- Concern:** No continuous coverage down to at least $Q^2=0.1\text{GeV}^2$
- Can we extend calorimetry/tracking/PID coverage down to $Q^2=0.1\text{GeV}^2$?
- No continuous coverage between $Q^2=0.1\text{GeV}^2$ and Low- Q^2 tagger!

Concluding remarks

- HERA program focused on various efforts to study the transition region:
 - Shifted vertex
 - Installation of flat beam pipe allowing to move top/bottom U-SCI calorimeter modules closer to beam (ZEUS)
 - Dedicated scintillating tracker to improve hit resolution (ZEUS)
 - Dedicated small-angle tagger: beam pipe calorimeter (ZEUS/H1)
- The physics program of exploring saturation phenomena requires continuous coverage below $Q^2=1\text{GeV}^2$, at least an order of magnitude below $Q^2=1\text{GeV}^2$, where pQCD description fails, i.e. to at least $Q^2=0.1\text{GeV}^2$
- ePIC low Q^2 tagger is a photoproduction tagger - critical for photoproduction physics and Q^2 acceptance well below $Q^2=0.1\text{GeV}^2$!

Concluding remarks

- Questions:
 - What is the **effective polar angle acceptance** for **backward calorimetry, tracking, and PID** of the central detector? Can we extend coverage to at least $Q^2=0.1\text{GeV}^2$?
 - What is the **respective precision for energy scale and angle (alignment)**, particularly at small angles and energies of the scattered electron $\sim 1\text{GeV}$? Energy scale calibration of at least 1% and better and precise alignment for precision angular accuracy is crucial!
 - Technical remark:
 - **Operation of detector components close to beam pipe is difficult** (Low Q^2 tagger!), requiring regular access - Operation inside beam vacuum should not be considered!
 - **Integrated active/passive radiation monitoring** is absolutely crucial and should be planned from the very beginning!