## Semi-leptonic $B$ and $B_{s}$-decays with charming hadronic final state

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## Motivation: CKM unitarity triangle fit


$\left|V_{c b}\right|$ enters crucially as normalization of the unitarity triangle

$$
\varepsilon_{K} \propto\left|V_{c b}\right|^{4}
$$

## Motivation

- Form factors for $B \rightarrow D^{(*)} \ell \nu$
$\rightarrow$ Allow to determine the CKM matrix-element $\left|V_{c b}\right|$
$\rightarrow\left|V_{c b}\right|$ enters as normalization in the unitary triangle fit
$\rightarrow 2-3 \sigma$ discrepancey between $\left|V_{c b}\right|^{\text {incl }}$ and $\left|V_{c b}\right|^{\text {excl }}$
$\rightarrow$ Atlas, CMS, LHCb and Belle II will improve experimental results
- $2-3 \sigma$ tension in $R_{D^{(*)}}$ ratio - independent of $\left|V_{c b}\right|$
[Fajfer et al. PRD 85 (2012) 094025],[J. Bailey et al. PRL 109 (2012) 071802], [BaBar PRL 109 (2012) 101802]

$$
R_{D^{(*)}}=\mathcal{B}\left(B \rightarrow D^{(*)} \tau \nu_{\tau}\right) / \mathcal{B}\left(B \rightarrow D^{(*)} \ell \nu_{\ell}\right) \text {, with } \ell=e, \mu
$$

$\rightarrow$ Due to its mass $\tau$ is sensitive to both form factors $f_{+}\left(q^{2}\right)$ and $f_{0}\left(q^{2}\right)$, $\ell=e, \mu$ are dominated by $f_{+}\left(q^{2}\right)$
$\rightarrow$ Anomaly in $R_{D^{*}}$ is seen by BaBar, LHCb, and Belle
$\rightarrow$ New physics?

## Motivation: $R_{D^{(*)}}$

## $B \rightarrow D^{(*)} T V$



Very preliminary \& unofficial average including


Figure: [Talk by T. Gershon at MIAPP June 2015]

## Our RHQ Project

- Use domain-wall light quarks and nonperturbatively tuned relativistic
$b$-quarks to compute at few-percent precision
- Nonperturbative tuning of RHQ parameters [PRD 86 (2012) 116003]
- Decay constants $f_{B}$ and $f_{B_{s}}$ [PRD 91 (2015) 054502]
- $B \rightarrow \pi \ell \nu$ and $B_{s} \rightarrow K \ell \nu$ form factors [PRD 91 (2015) 074510]
- $g_{B^{*} B \pi}$ coupling constant [PRD 93 (2016) 014510]
- $B^{0}-\overline{B^{0}}$ mixing
- Rare $B$ decays [arXiv:1511.06622]
- $f_{B}, f_{B_{s}}$, and semi-leptonic form factors
- $O$ (a) improvement at 1-loop and mostly nonperturbative renormalization
- Correction factors and coefficients computed at 1-loop
- $B$ mixing
- Tree-level $O(a)$ improvement
- Perturbative or mostly nonperturbative renormalization
$B_{(s)} \rightarrow D_{(s)}^{(*)}$ form factors

- Re-use DWF point-source light and strange quark propagators
- Generate Gaussian smeared MDWF charm quark propagators (on the fly)
- Create Gaussian smeared-source sequential heavy quark propagators
- Compute all possible contractions for pseudoscalar or vector final states
- General building blocks code incl. terms for 1-loop $O\left(\alpha_{S} a\right)$ improvement
- Coefficients to be computed in lattice perturbation theory


## 2+1 Flavor Domain-Wall Iwasaki ensembles

| L | $a^{-1}(\mathrm{GeV})$ | $a m_{l}$ | $a m_{s}$ | $M_{\pi}(\mathrm{MeV})$ | \# configs. | \#sources |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 24 | 1.785 | 0.005 | 0.040 | 338 | 1636 | 1 | [PRD 78 (2008) 114509] |
| 24 | 1.785 | 0.010 | 0.040 | 434 | 1419 | 1 | [PRD 78 (2008) 114509] |
| 32 | 2.383 | 0.004 | 0.030 | 301 | 628 | 2 | [PRD 83 (2011) 074508] |
| 32 | 2.383 | 0.006 | 0.030 | 362 | 889 | 2 | [PRD 83 (2011) 074508] |
| 32 | 2.383 | 0.008 | 0.030 | 411 | 544 | 2 | [PRD 83 (2011) 074508] |
| 48 | 1.730 | 0.00078 | 0.0362 | 139 | 40 | $81 / 1^{\star}$ | [PRD 93 (2016) 074505] |
| 64 | 2.359 | 0.000678 | 0.02661 | 139 | - | - | [PRD 93 (2016) 074505] |
| 48 | $\sim 2.7$ | 0.002144 | 0.02144 | $\sim 250$ | $>50$ | 24 | [in progress] |

* All mode averaging: 81 "sloppy" and 1 "exact" solve [Blum et al. PRD 88 (2012) 094503]
- Lattice spacing determined from combined analysis [Blum et al. PRD 93 (2016) 074505]
- $a: \sim 0.11 \mathrm{fm}, \sim 0.08 \mathrm{fm}, \sim 0.07 \mathrm{fm}$


## Up, down, and strange quarks

- Domain-wall fermions with same parameters as in the sea-sector (domain-wall hight $M_{5}$, extension of $5^{\text {th }}$ dimension $L_{s}$ )
- Unitary and partially quenched quark masses
- Strange quarks at/near physical the physical value


## Charm quarks

- Möbius DWF optimized for heavy quarks [Boyle et al. JHEP 1604 (2016) 037]
- $M_{5}=1.6, L_{s}=12$
- Discretization errors well under control for $a m_{c}<0.45$
$\rightarrow$ On coarse ( $a^{-1}=1.785 \mathrm{GeV}$ ) ensembles we simulate just below $m_{c}^{\text {phys }}$
$\rightarrow$ Simulate 3-4 charm-like masses and then extrapolate/interpolate
$\rightarrow$ Linear extrapolation is small and benign; interpolation is safe


## Charm extrapolation



Figure: [Boyle et al. arXiv:1511.09328]

- Open triangles: simulated data with mistuned valence strange quark mass
- Squares: data after correcting valence strange quark
- Circles: interpolation to reference masses


## MDWF charm quarks

Advantages

- Very similar setup for computing $B_{s} \rightarrow D_{s}$ as for $B_{s} \rightarrow K$
$\rightarrow$ Only minor modifications for the perturbative calculations
- No nonperturbative tuning of the RHQ action for charm quarks
- Allows to explore new concept of heavy DWF for semileptonic decays
$\rightarrow$ Fully nonperturbative renormalization of $f_{D}$ in progress


## Disadvantages

- Larger numerical costs than RHQ charm
- On coarse ensembles small extrapolation needed


## Bottom quarks

- Relativistic Heavy Quark action developed by Christ, Li, and Lin [Christ et al. PRD 76 (2007) 074505], [Lin and Christ PRD 76 (2007) 074506]
- Allows to tune the three parameters ( $m_{0} a, c_{P}, \zeta$ ) nonperturbatively [PRD 86 (2012) 116003]
- Builds upon Fermilab approach [El-Khadra et al. PRD 55 (1997) 3933] by tuning all parameters of the clover action non-perturbatively; close relation to the Tsukuba formulation [S. Aoki et al. PTP 109 (2003) 383]
- Heavy quark mass is treated to all orders in $\left(m_{b} a\right)^{n}$
- Expand in powers of the spatial momentum through $O(\vec{p} a)$
- Resulting errors will be of $O\left(\vec{p}^{2} a^{2}\right)$
- Allows computation of heavy-light quantities with discretization errors of the same size as in light-light quantities
- Applies for all values of the quark mass
- Has a smooth continuum limit
- Recently re-tuned to account for updated values of $a^{-1}$


## Proposal 2016/17

- Request: 16.0 M Jpsi core hours for computing +3.8 M Jpsi core hours for storage
- Aim: compute $B_{(s)} \rightarrow D_{(s)}$ form factors and determine $\left|V_{c b}\right|$ as well as $R_{D^{(*)}}$ ratios
- Provide results based on different gauge fields and actions and thus with uncorrelated statistical and different systematic errors to existing results in the literature
- Explore semileptonic decays with heavy MDWF


## Questions from the SPC (shortend)

1) Expectations for the precision of your calculation (stat. and sys.)

- We target statistical and systematic errors to be both less than $2 \%$

2) Controlling the error of the charm extrapolation and expected size

- The charm extrapolation is small and we expect a sub-percent error

3) Plan to use double-ratios like Fermilab/MILC

- Double ratios roughly double the costs so we did not propose to use them; we are however investigating the advantages and may refine our computational strategy

4) Have you considered a multi-mass inverter for DW charm propagators?

- Multi-mass solvers do not exist for DWF

5) Have you considered performing a blind analysis?

- Yes, we look into adding a blinding factor to our PT computed factors

6) Can you run on the new Jlab machine, if a) cpu, b) GPU, c) KNL?

- Sorry, transferring 200 TB will neither make the site managers nor us happy


## Resources and Acknowledgements

- Simulations on $24^{3}, 32^{3}$, and the $48^{3}$ ensemble with physical pions USQCD: kaon, J/psi, Ds, Bc, and pi0 cluster at Fermilab BNL and Columbia U: small local clusters
- Simulations on the $a^{-1} \sim 2.7 \mathrm{GeV} 48^{3}$ ensemble ARCHER UoE: Cray XC30
DiRAC UoE: BG/Q



## Extra: Heavy MDWF



Figures: [Boyle et al. JHEP 1604 (2016) 037]

- $M_{5}=1.6$ has smallest discretization errors
- For $a m \gtrsim 0.4 m_{\text {res }}$ does not plateau

