

# **R-matrix Analysis of $^8\text{Be}$ System**

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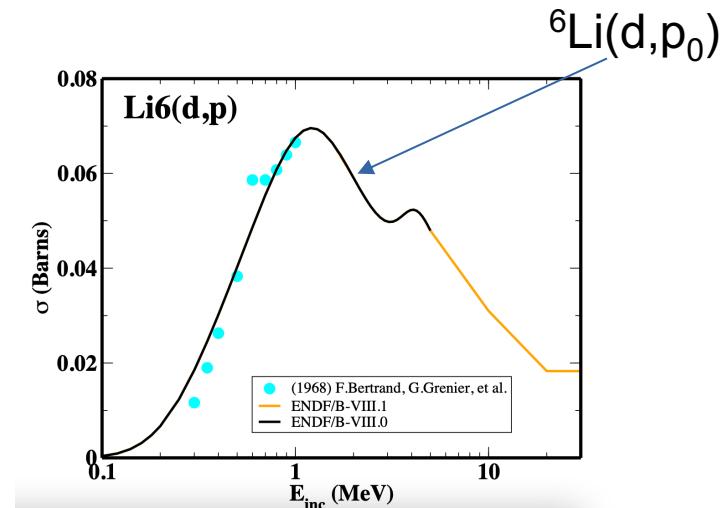
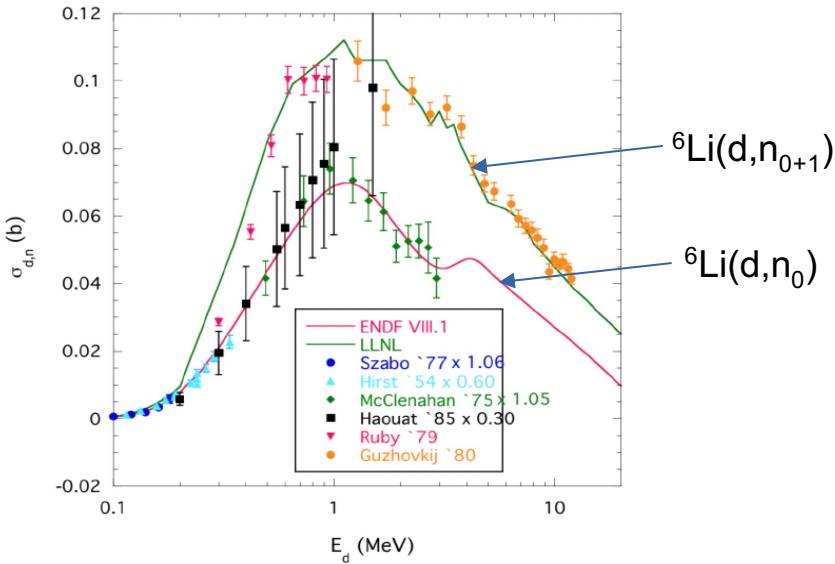
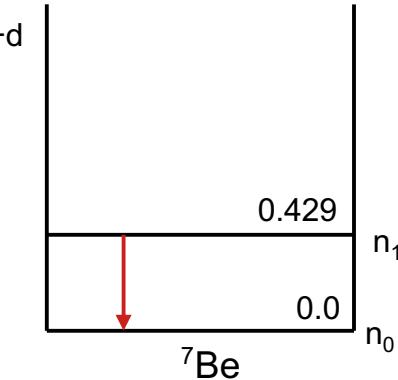
CSWEG Meeting 2023

# Outline

- Motivation
- New Measurement of deuterium induced reactions on  ${}^6\text{Li}$ 
  - Experimental details
  - Preliminary results
- $R$ -matrix analysis of  ${}^8\text{Be}$ 
  - Preliminary results
  - Comparisons with Energy Dependent Analysis (EDA) code from LANL

# Motivation

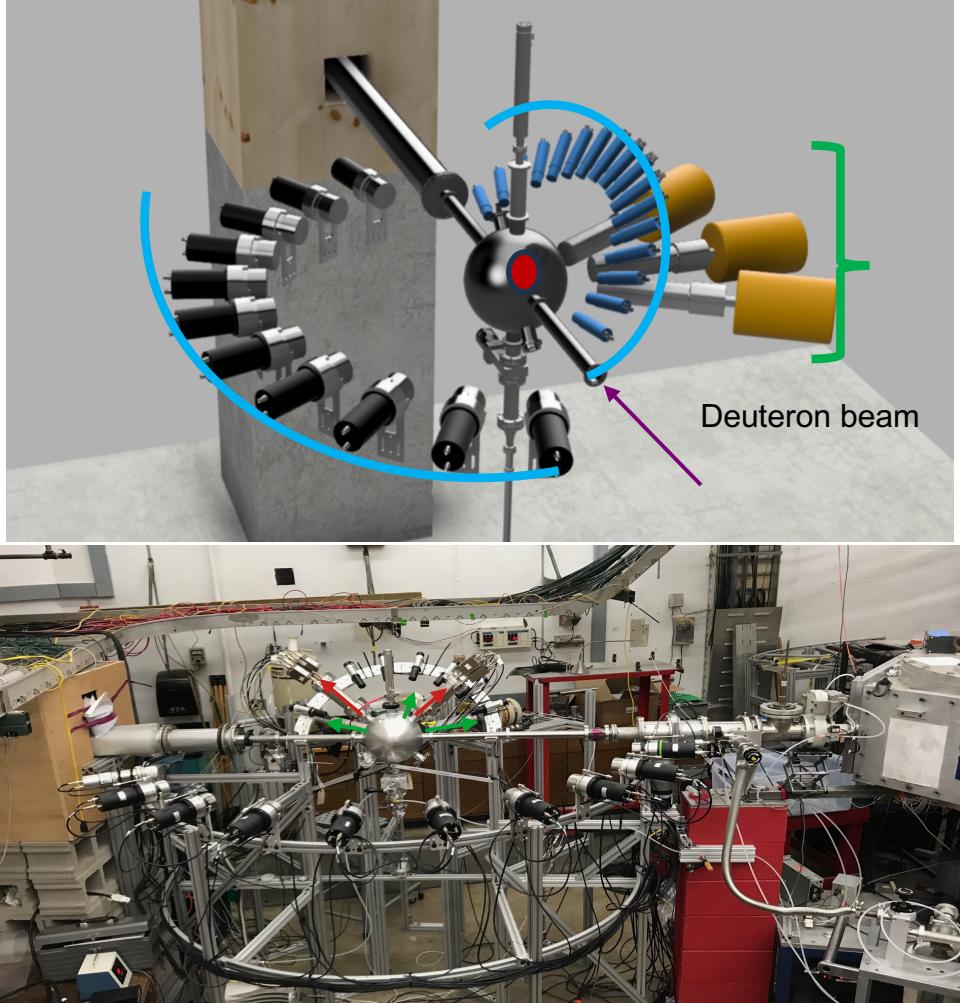
- Deuterium induced reactions on  ${}^6\text{Li}$  are important for nuclear structure and nuclear astrophysics.
- ENDF/LANL includes only  $(d,n_0)$  and  $(d,p_0)$  partial cross sections. LLNL-2010 is consistent describing  ${}^6\text{Li}(d,n_{0+1})$  but their  ${}^6\text{Li}(d,p)$  calculation seems to be only  ${}^6\text{Li}(d,p_0)$ .
- The inconsistencies in the  $R$ -matrix evaluations from literature demands new measurements and new  $R$ -matrix evaluation of  ${}^8\text{Be}$  system including more channels.



2010 LLNL vs 2004 LANL (from CSEWG talk by Ian Thompson c.a. 2017)

# Experimental Details

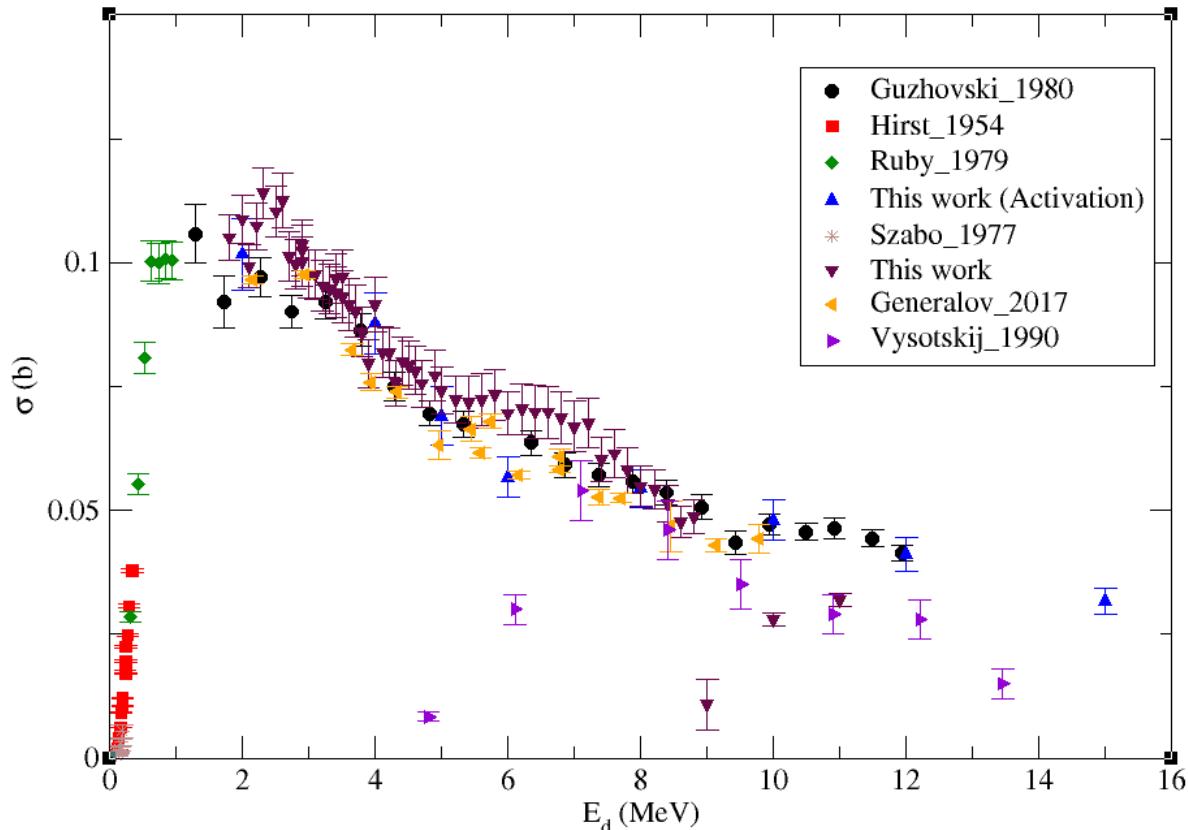
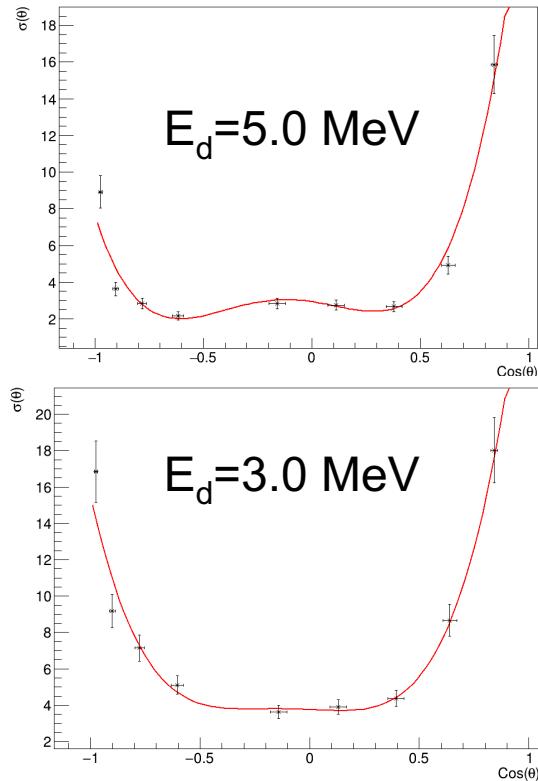
- Performed at University of Notre Dame using FN Tandem in collaboration with ORNL and LANL.
- Thin target: 200  $\mu\text{g}/\text{cm}^2$  metallic  ${}^6\text{Li}$  on 20  $\mu\text{g}/\text{cm}^2$  C backing.
- $E_d = 1.8\text{--}15.0 \text{ MeV}$
- **Neutrons:** detected by Deuterated Liquid Scintillator Array (ODeSA)
  - Angular coverage 10 – 170 degrees
  - TOF spectra
- **Charged Particles:** detected by Silicon detectors placed at 45° and 135°.
  - Set up as E-dE1-dE2 array.
- **Gammas:** detected by 3 detectors
  - (HpGe+ GEANIE) at 45°, 90° and 135° degrees.
- **Also had 20 stilbene neutron detectors**
- Activation measurement was also performed.  
(Results included in *R*-matrix fit)



# ${}^6\text{Li}(\text{d},\text{n}_{0+1}){}^7\text{Be}$ Analysis

## Integrated Cross Sections

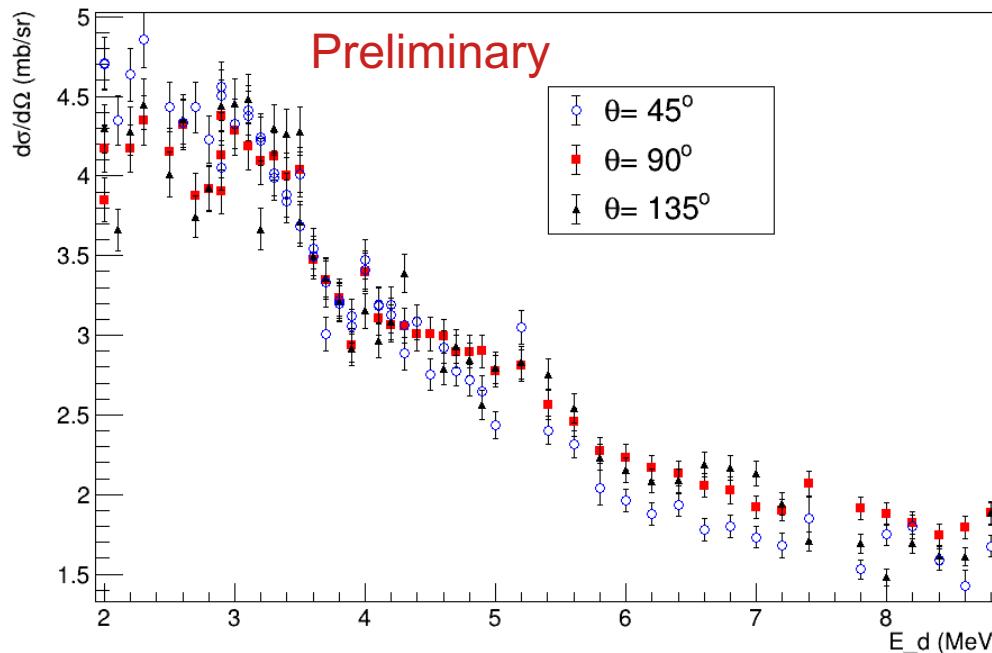
### Angular distributions



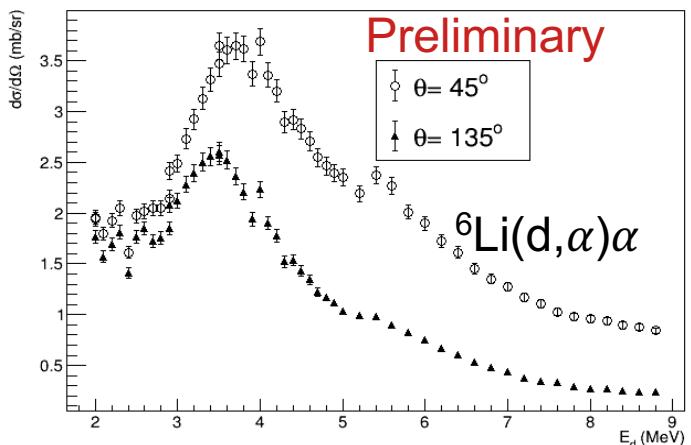
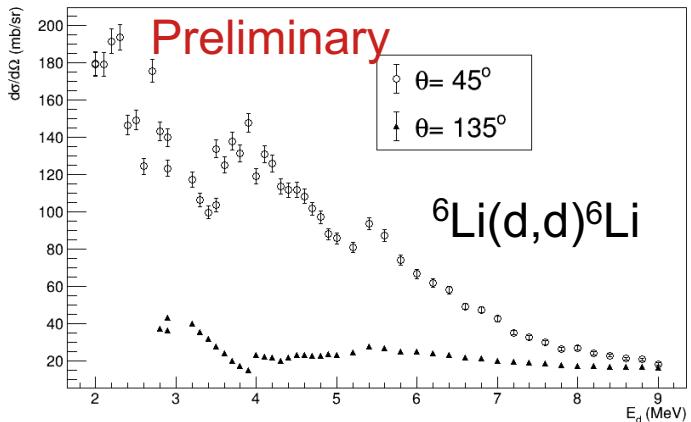
Results: statistical error bar only

# Gamma Angular distributions from ${}^6\text{Li}(\text{d},\text{n}_1){}^7\text{Be}$

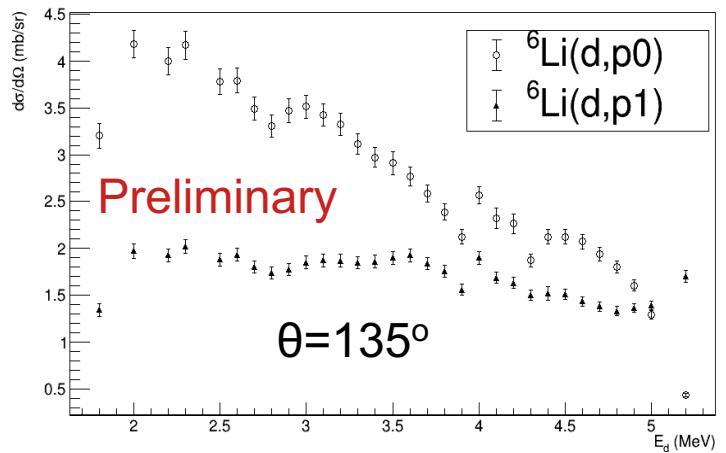
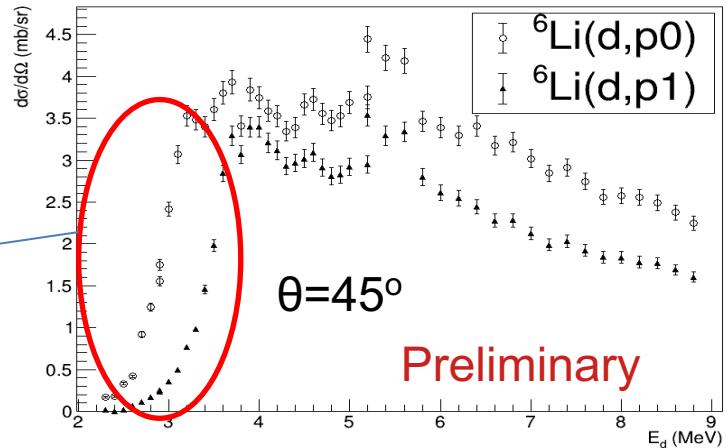
- ${}^6\text{Li}(\text{d},\text{n}_1){}^7\text{Be}$  produces 429-keV gammas, detected by three gamma detectors.
- The integrated cross section would provide the  ${}^6\text{Li}(\text{d},\text{n}_1){}^7\text{Be}$  component which could be subtracted from  ${}^6\text{Li}(\text{d},\text{n}_{0+1}){ }^7\text{Be}$  to determine  ${}^6\text{Li}(\text{d},\text{n}_0){ }^7\text{Be}$  cross sections.



# Charged Particle Channels



Threshold effects in  
Si detector



These results will be included in the *R*-matrix analysis of  ${}^8\text{Be}$  system.

## R-matrix Analysis of ${}^8\text{Be}$ System with AZURE2

- Goal: Multichannel  $R$ -matrix analysis to describe the  ${}^8\text{Be}$  system.
- Ongoing Work: Simultaneous fitting of data for  ${}^8\text{Be}$  compound nucleus including various channels.
- The data included so far are for these reaction channels:

${}^6\text{Li}(\text{d},\text{d}){}^6\text{Li}$	${}^7\text{Li}(\text{p},\text{p}){}^7\text{Li}^*$
${}^6\text{Li}(\text{d},\alpha)\alpha$	${}^7\text{Li}(\text{p},\text{n}_0){}^7\text{Be}$
$\alpha(\alpha,\alpha)\alpha$	${}^7\text{Li}(\text{p},\text{n}_1){}^7\text{Be}$
${}^6\text{Li}(\text{d},\text{n}_0){}^7\text{Be}$	${}^7\text{Li}(\text{p},\alpha)\alpha$
${}^6\text{Li}(\text{d},\text{n}_1){}^7\text{Be}$	$\alpha(\alpha,\text{p}){}^7\text{Li}$
${}^6\text{Li}(\text{d},\text{p}_1){}^7\text{Li}$	$\alpha(\alpha,\text{p}){}^7\text{Li}^*$
${}^6\text{Li}(\text{d},\text{p}_1){}^7\text{Li}$	${}^7\text{Be}(\text{n},\text{p}){}^7\text{Li}$
${}^7\text{Li}(\text{p},\text{p}){}^7\text{Li}$	${}^7\text{Be}(\text{n},\gamma){}^8\text{Be}$

Channel	Channel Radius (fm)
${}^6\text{Li}+\text{d}$	6.4639
$\alpha+\alpha$	4.0
${}^7\text{Be}+\text{n}_0$	4.15
${}^7\text{Be}+\text{n}_1$	5.0
${}^7\text{Li}+\text{p}_0$	4.15
${}^7\text{Li}+\text{p}_1$	5.0

- Channel radius values for different channels taken from EDA calculations.
- Sensitivity to channel radius needs to be studied.
- The absolute normalizations of data are fixed at 1.

# <sup>8</sup>Be Levels Information

- Taken from NNDC
- The levels highlighted in red have not been included so far.
- The 22.63 MeV level was introduced with 1<sup>+</sup> spin, parity assignment.
- The 22.98 MeV level was introduced with 2<sup>+</sup> spin, parity assignment.
- The 21.5 MeV state used have negative parity.
- Max orbital angular momentum, l=4

## Background Levels

0<sup>+</sup> at 32 MeV

2<sup>+</sup> at 32 MeV

4<sup>+</sup> at 32 MeV

## Data Sources:

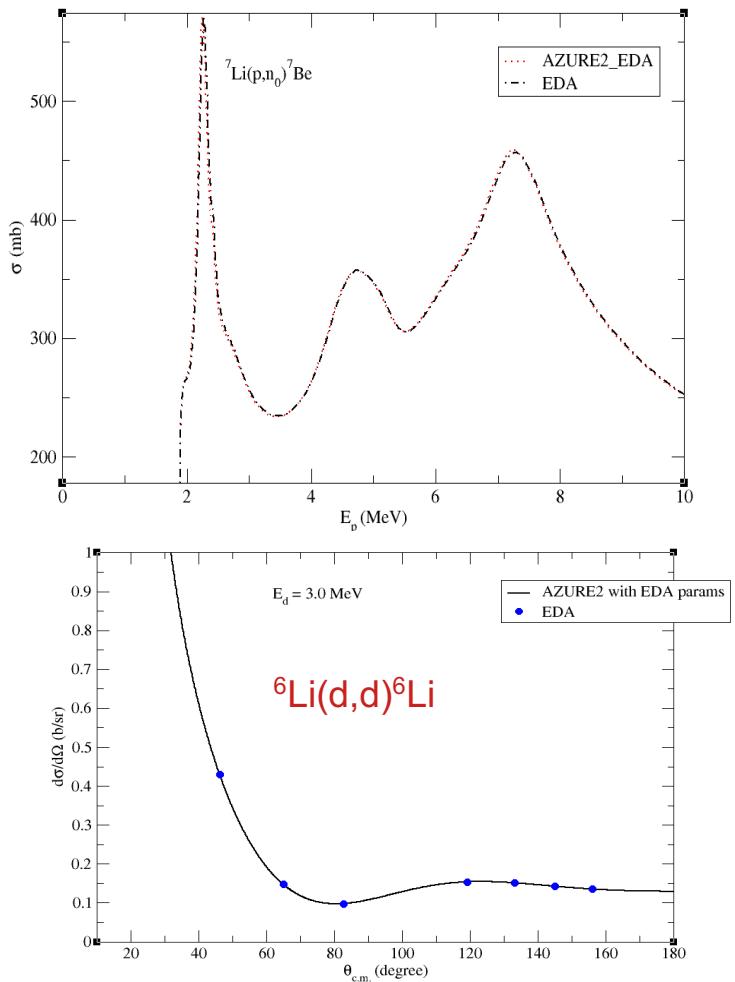
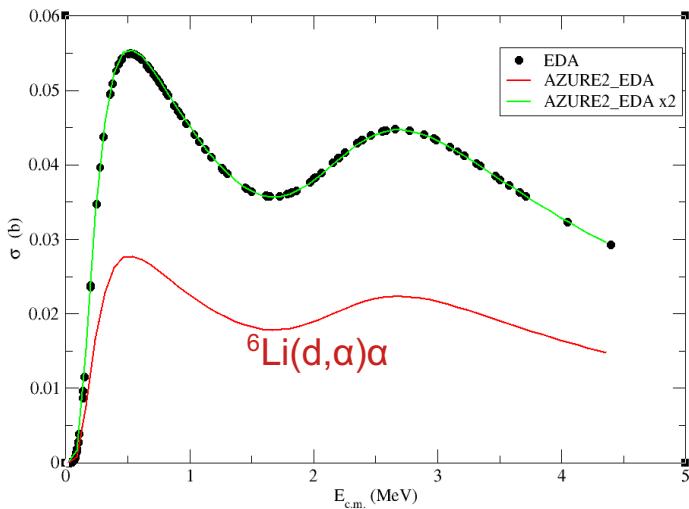
- EXFOR
- <sup>6</sup>Li(d,n)<sup>7</sup>Be activation data from University of Notre Dame, 2022.
- Total data points: 1837

E(level) (keV)	XREF						J <sup>n</sup> (level)
0.0	ABCDE	HIJKL	PQRS	UVW	YZ	abcde	0+
3030 10	ABCDE	HIJKL	PQRS	UVW	YZ	abcd f	2+
11.35E+3 15	CD	JK	P R	UVW	Z	bcd	4+
16626 3	BCD	HI KL	PQR	UVW	YZ	abc	2+
16922 3	CD	HI KL	PQR	UVW	YZ	abc	2+
17640.0 10	E	I L N	PQ	UVW	Za	c	1+
18150 4	I	L N	PQ	UV	Za		1+
18810	I	LMN	P	T			2-
19069 10	I	L N	P	UV			3+
19235 10	MN	P	TUW	Z	e		3+
E(level) (keV)	XREF						J <sup>n</sup> (level)
19400	I	MN	U				1-
19860 50	D	I K	O RS	VW	Z		4+
20100	D	MNOP	S V	Z			2+
20200	D	M P		Z			0+
20.9E+3	N						4-
21.5E+3	LM	T	Z				3(+)
22000	L						1-
22.05E+3 10	U W						2+
22.63E+3 10	K						1+
22.98E+3 10	W						2+
E(level) (keV)	XREF						J <sup>n</sup> (level)
24000	L O			Z			(1, 2)-
25200	D G	O		Z			2+
25500	D G						4+
27494.1 18	EFG		X				0+
28600?	L						
32E3?			Z				
≈41E3?	G						

- States highlighted in red are not used so far.

# Comparisons with EDA

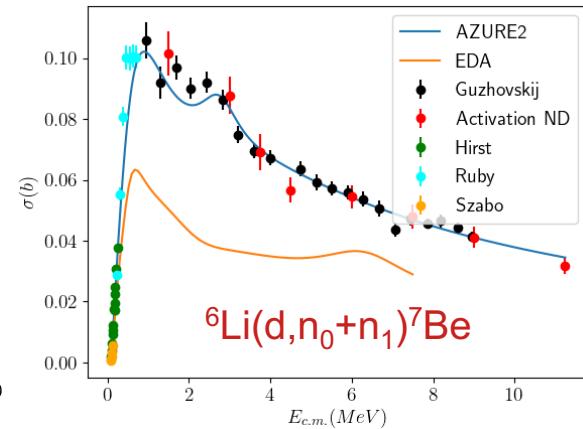
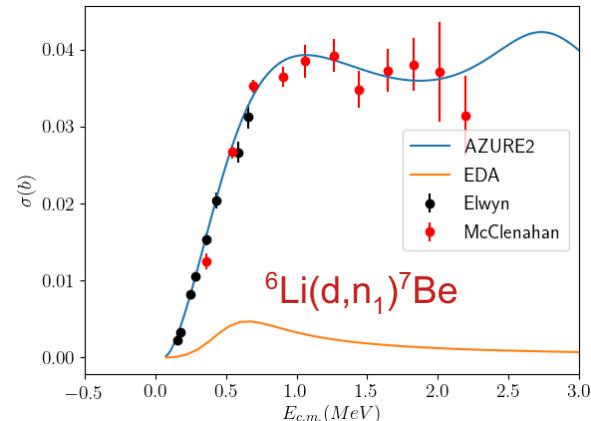
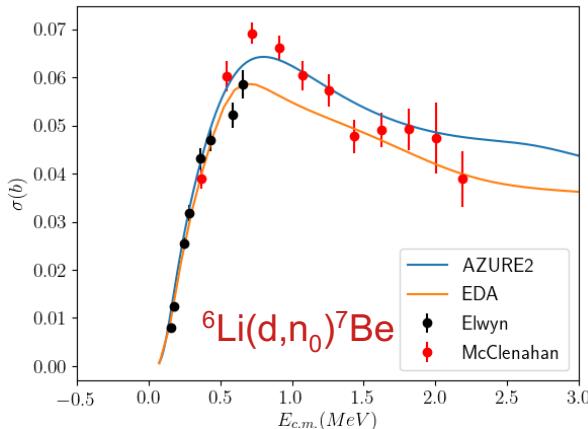
- M.Paris provided the EDA parameters.
- These parameters were converted into AZURE2 parameters by C. Brune (Ohio University).
- Benchmarked the calculation for various channels.
- Identical particles in the exit channel: EDA calculates (or fits) the production data whereas AZURE uses the reaction cross section data. Data are scaled accordingly for these channels only!!!



# Results and comparisons with EDA

## ${}^6\text{Li}(\text{d},\text{n}_0){}^7\text{Be}$ and ${}^6\text{Li}(\text{d},\text{n}_1){}^7\text{Be}$

- › AZURE2 produces both  ${}^6\text{Li}(\text{d},\text{n}_0){}^7\text{Be}$  and  ${}^6\text{Li}(\text{d},\text{n}_1){}^7\text{Be}$  quite well and even the  ${}^7\text{Be}$  production data.
- › EDA reproduced the  ${}^6\text{Li}(\text{d},\text{n}_0){}^7\text{Be}$  data quite well but not  ${}^6\text{Li}(\text{d},\text{n}_1){}^7\text{Be}$ .



Data Used:  ${}^6\text{Li}(\text{d},\text{n}_{0,1}){}^7\text{Be}$ : Elwyn *et. al.* (Phys. Rev. C, 16, 1977)

McClennahan *et. al.* (Nucl. Phys, 11, 1975)

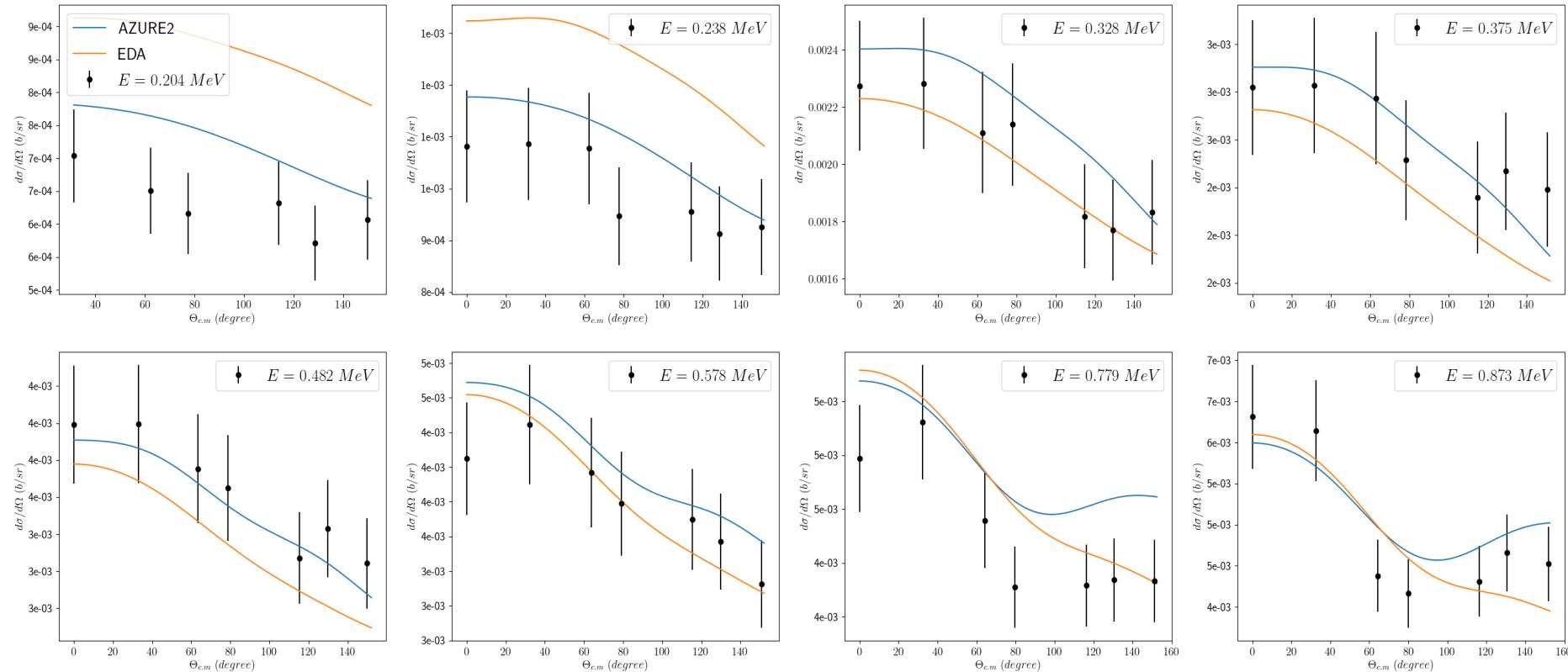
${}^6\text{Li}(\text{d},\text{n}_{0+1}){}^7\text{Be}$ : Hirst *et. al.* (Philosophical Magazine, Vol.45, Issue.366, 1954)

Ruby *et. al.* (Nuclear Science and Engineering, Vol.71, 1979)

Szabo *et. al.* (Nuclear Physics, Section A, Vol.289, 1977)

Guzhevskij *et. al.* (Izv. Rossiiskoi Akademii Nauk, Ser.Fiz., Vol.44 (1980))

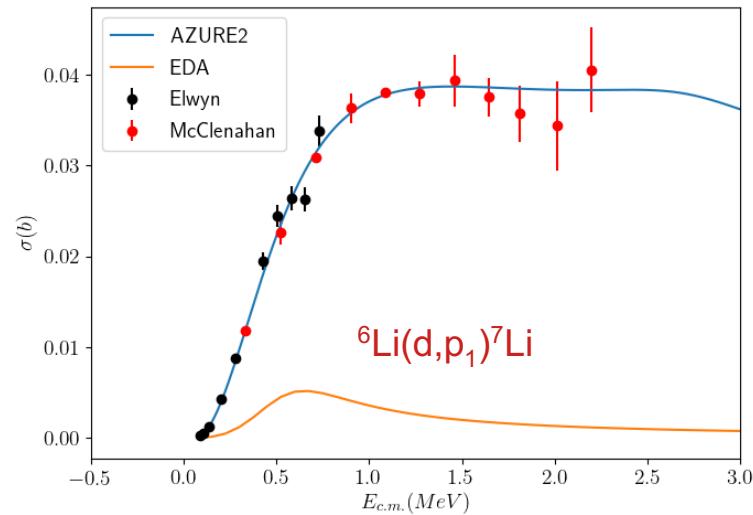
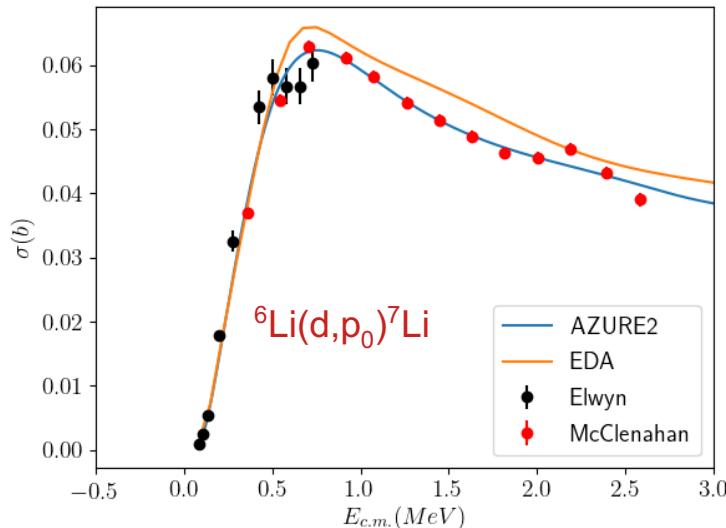
# ${}^6\text{Li}(\text{d},\text{n}_0){}^7\text{Be}$



Data Used:  ${}^6\text{Li}(\text{d},\text{n}_0){}^7\text{Be}$ : Elwyn et. al. (Phys. Rev. C, 16, 1977)

# ${}^6\text{Li}(\text{d},\text{p}_0){}^7\text{Li}$ and ${}^6\text{Li}(\text{d},\text{p}_1){}^7\text{Li}$

- › AZURE2 produces both  ${}^6\text{Li}(\text{d},\text{p}_0){}^7\text{Li}$  and  ${}^6\text{Li}(\text{d},\text{p}_1){}^7\text{Li}$  quite well.
- › EDA reproduces the  ${}^6\text{Li}(\text{d},\text{p}_0){}^7\text{Li}$  data but  ${}^6\text{Li}(\text{d},\text{p}_1){}^7\text{Li}$  is not well constrained.

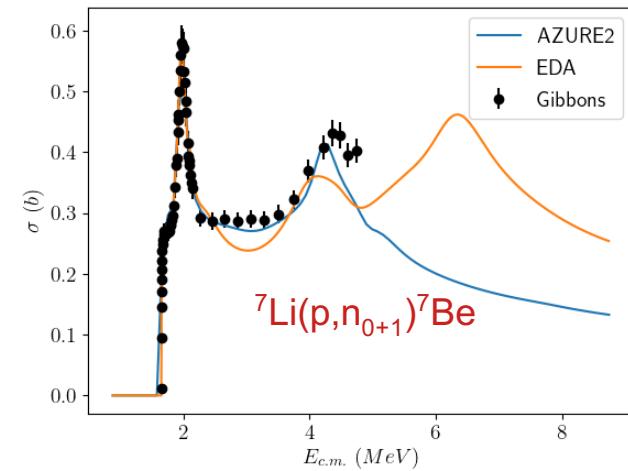
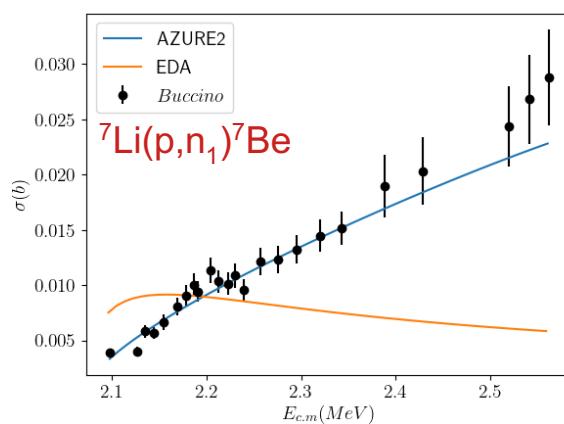
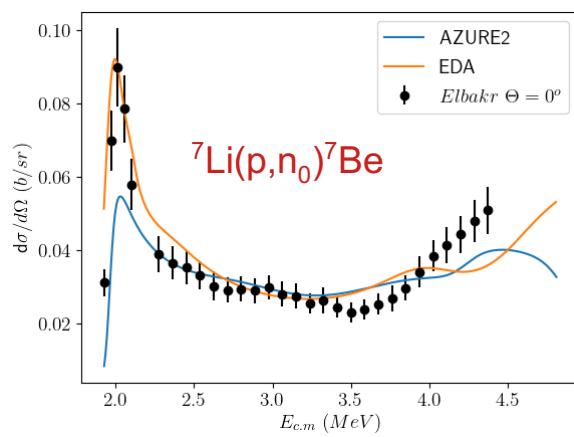


Data Used:  ${}^6\text{Li}(\text{d},\text{p}_{0,1}){}^7\text{Li}$ : Elwyn *et. al.* (Phys. Rev. C, 16, 1977)

McClennan *et. al.* (Nucl. Phys., 11, 1975)

# ${}^7\text{Li}(\text{p},\text{n}_0){}^7\text{Be}$ and ${}^7\text{Li}(\text{p},\text{n}_1){}^7\text{Be}$

- AZURE2 produces both  ${}^7\text{Li}(\text{p},\text{n}_0){}^7\text{Be}$  and  ${}^7\text{Li}(\text{p},\text{n}_1){}^7\text{Be}$  quite well.
- EDA reproduces the  ${}^7\text{Li}(\text{p},\text{n}_0){}^7\text{Be}$  data quite well  ${}^7\text{Li}(\text{p},\text{n}_1){}^7\text{Be}$  data is not included.

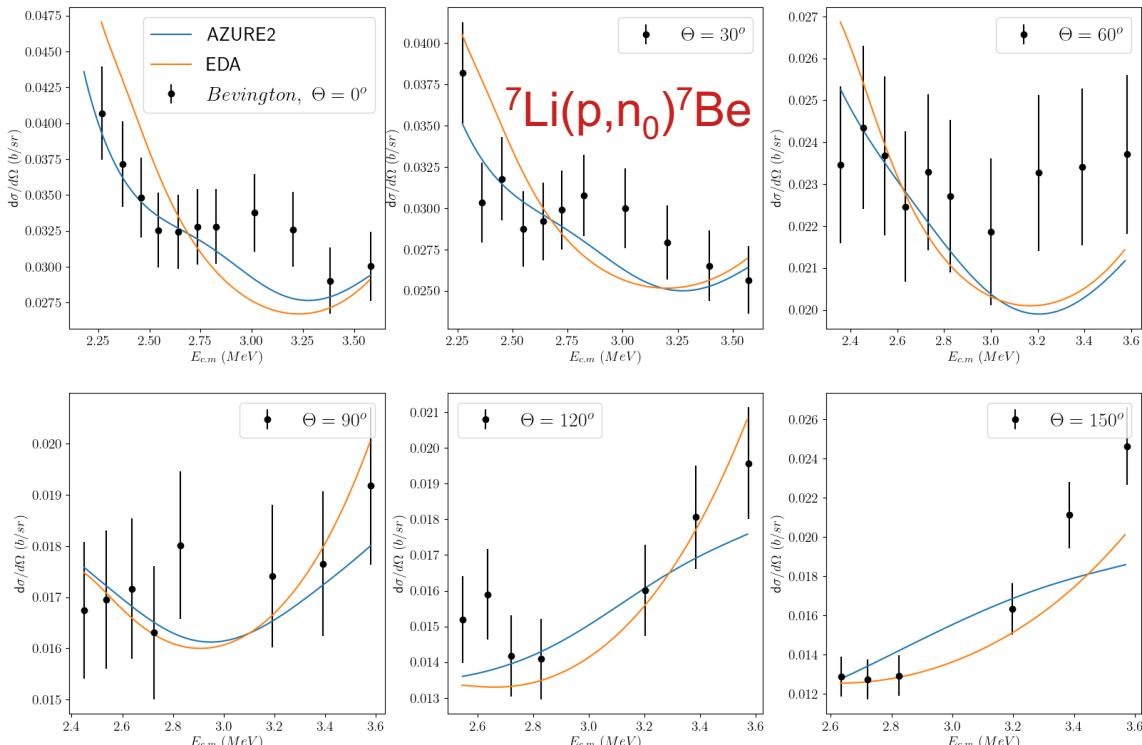
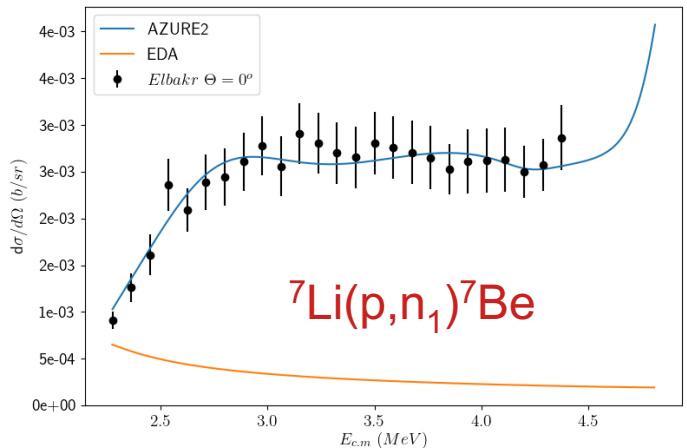


Data Used:  ${}^7\text{Li}(\text{p},\text{n}_0){}^7\text{Be}$  : Angular distribution: Elbakr *et. al.* (Nuclear Instrum.and Methods in Physics Res., Vol.105, p.519 (1972))

${}^7\text{Li}(\text{p},\text{n}_1){}^7\text{Be}$  : Integrated cross section: Buccino *et. al.* (Nuclear Physics, Vol.53, Issue.3, p.375 (1964))

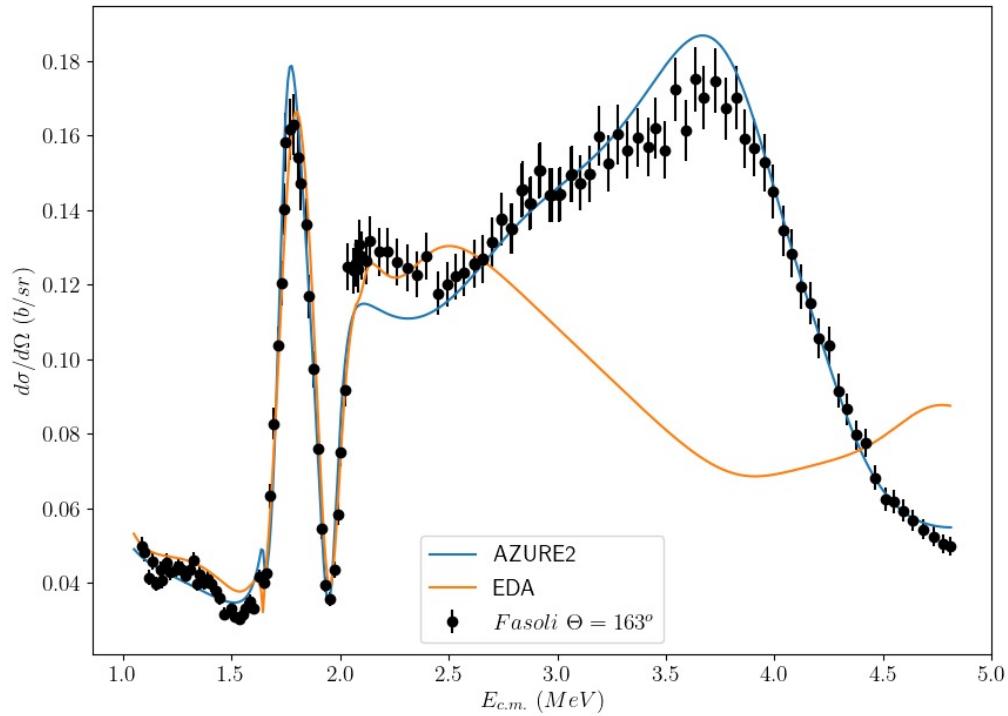
${}^7\text{Li}(\text{p},\text{n}_{0+1}){}^7\text{Be}$ : Integrated Cross section: Gibbons *et. al.* (Physical Review, Vol.114, p.571 (1959))

# $^7\text{Li}(\text{p},\text{n}_0)^7\text{Be}$ and $^7\text{Li}(\text{p},\text{n}_1)^7\text{Be}$



Data Used:  $^7\text{Li}(\text{p},\text{n}_1)^7\text{Be}$  : Angular distribution: Elbakr et. al. (Nuclear Instrum.and Methods in Physics Res., Vol.105, p.519 (1972))  
 :Angular distribution: Bevington et. al. (Physical Review, Vol.121, Issue.3, p.871 (1961))

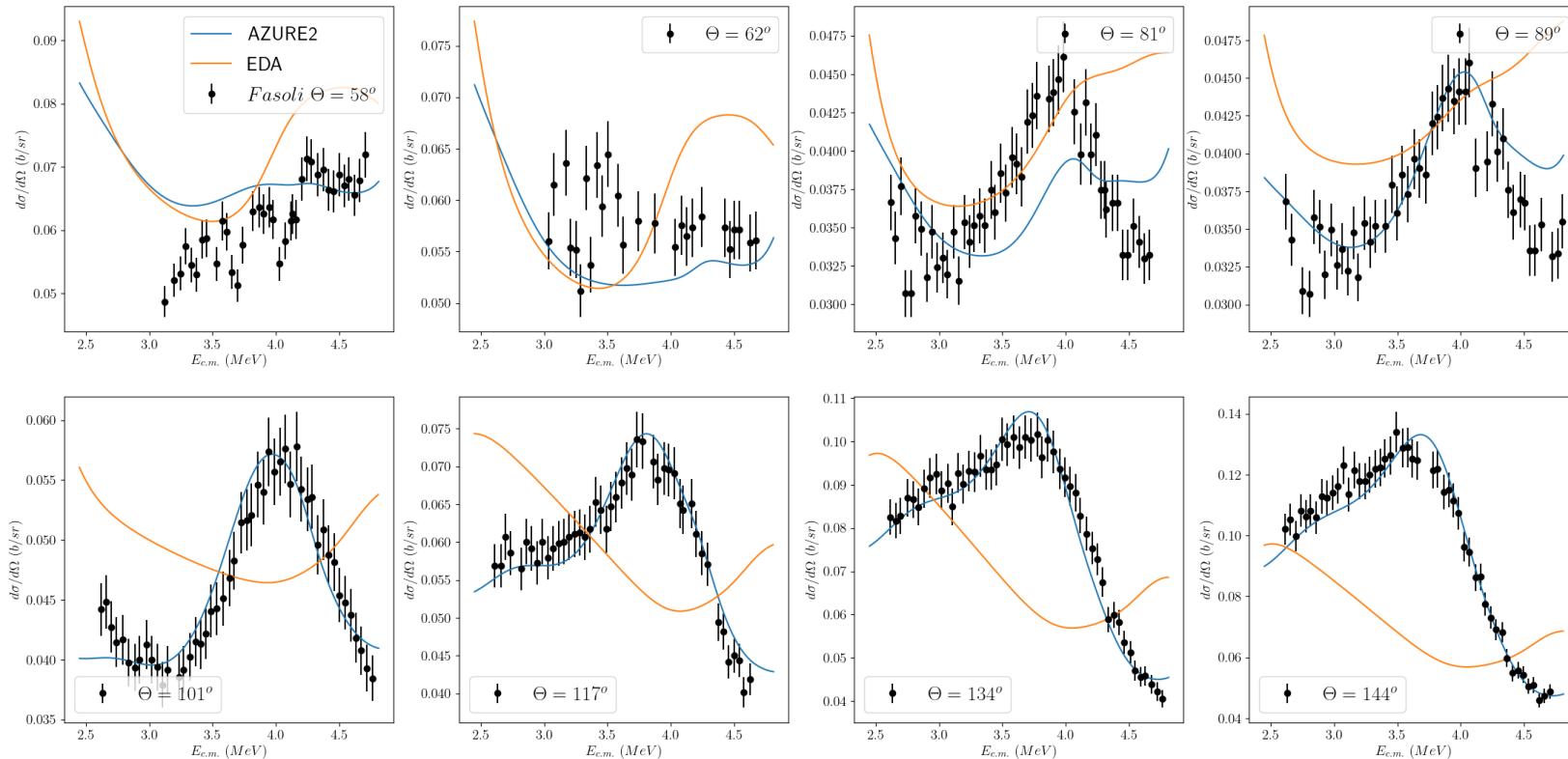
# $^7\text{Li}(\text{p},\text{p})^7\text{Li}$



Data Used:  $^7\text{Li}(\text{p},\text{p})^7\text{Li}$  : Differential cross section: Fasoli *et. al.* (Nuovo Cimento, Vol.34, Issue.3, p.542 (1964))

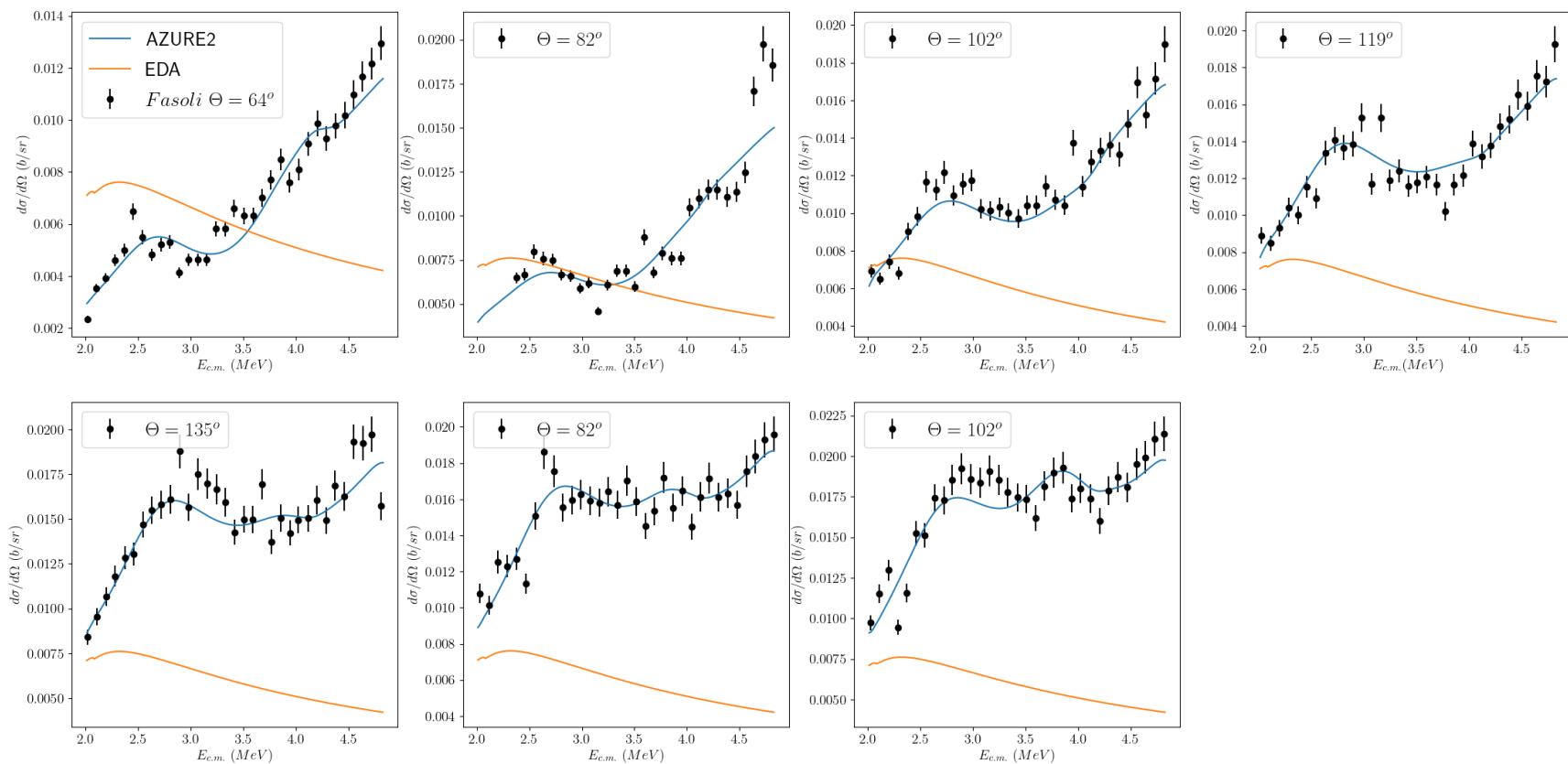
# $^7\text{Li}(\text{p},\text{p})^7\text{Li}$

- Fitting at forward angles is not good.



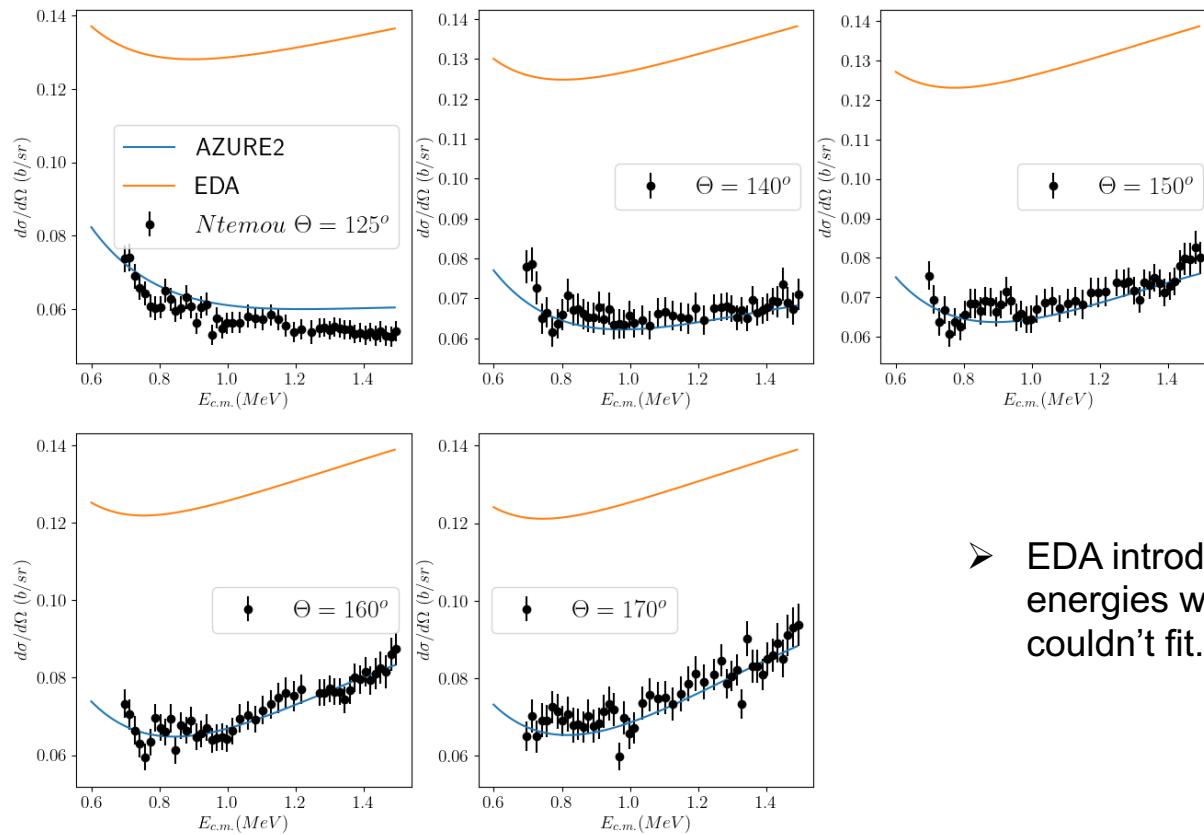
Data Used:  $^7\text{Li}(\text{p},\text{p})^7\text{Li}$  : Differential cross section: Fasoli et. al. (Nuovo Cimento, Vol.34, Issue.3, p.542 (1964))

# $^7\text{Li}(\text{p},\text{p}')^7\text{Li}$



Data Used:  $^7\text{Li}(\text{p},\text{p}')^7\text{Li}$  : Differential cross section: Fasoli et. al. (Nuovo Cimento, Vol.34, Issue.3, p.542 (1964))

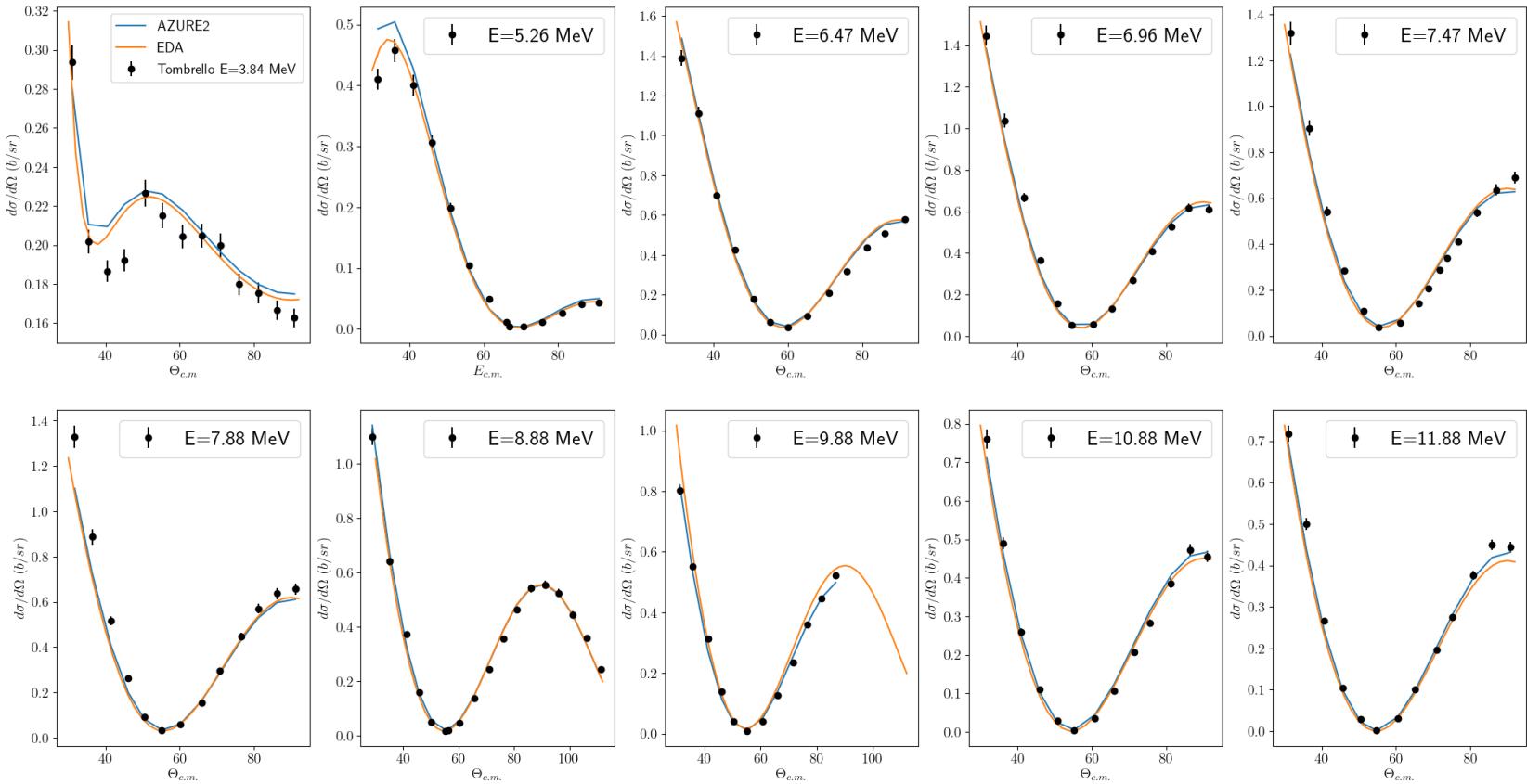
# ${}^6\text{Li}(\text{d},\text{d}){}^6\text{Li}$



- EDA introduces data at high energies which AZURE2 couldn't fit.

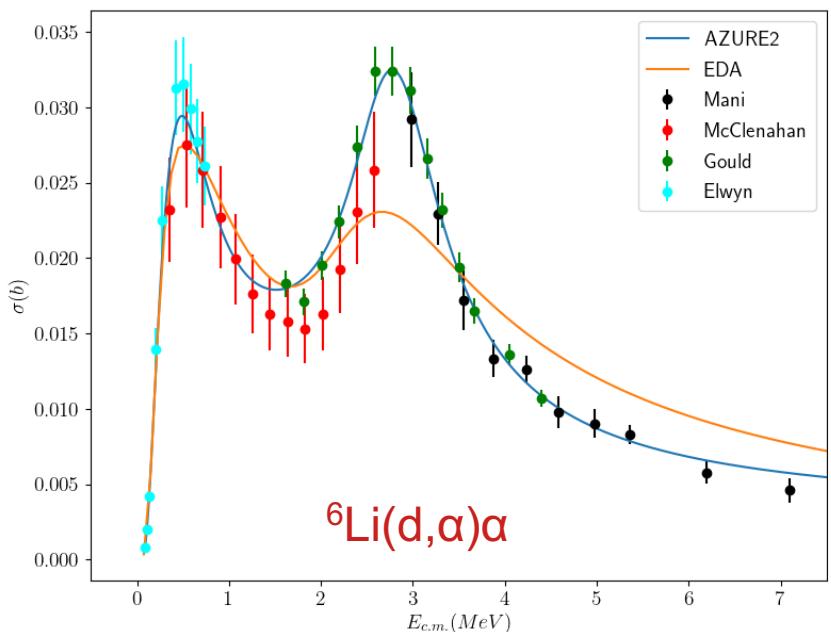
Data Used:  ${}^6\text{Li}(\text{d},\text{d}){}^6\text{Li}$  : Angular distribution: Ntemou *et. al.* (Nucl. Instrum. Methods in Physics Res., Sect.B, Vol.407, p.34 (2017))

# $\alpha(\alpha,\alpha)\alpha$



Data Used: $\alpha(\alpha,\alpha)\alpha$  : Differential cross section: T.A. Tombrello et. al.. (Phys. Rev. 129,2252,1963)

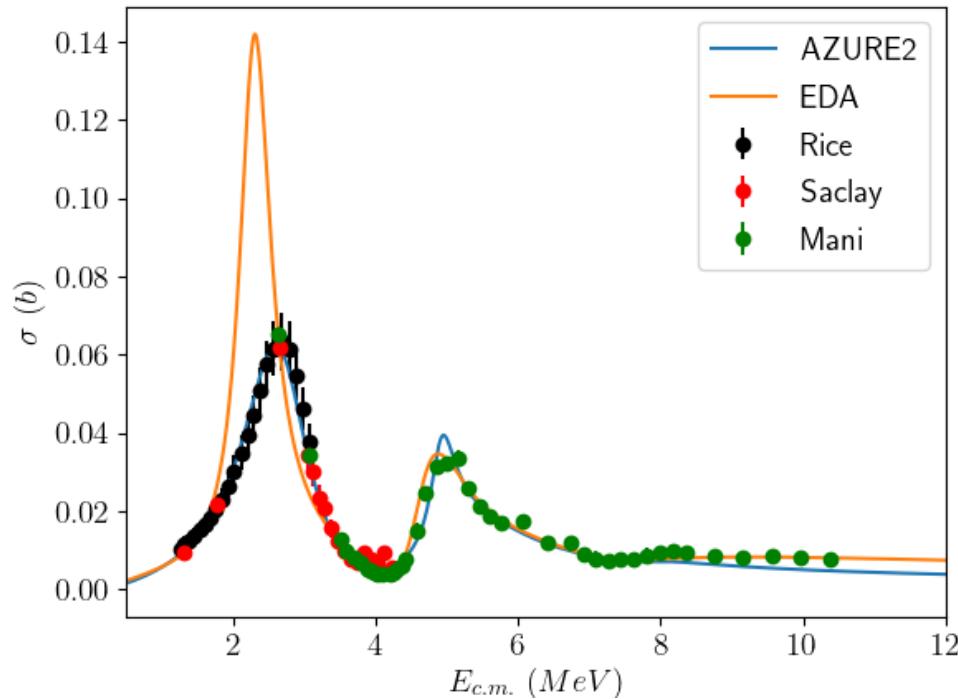
# ${}^6\text{Li}(\text{d},\alpha)\alpha$



**Scaling Factors:**  
**Mani:** 0.5  
**Foteinou:** 0.5

Data Used: Integrated Cross Section: Mani et al. (Proceedings of the Physical Society , Vol.85, 1965)  
 McClennan et al. (Physical Review, Part C, Nuclear Physics, Vol.11, 1975)  
 Gould et al. (Nuclear Science and Engineering, Vol.55, 1974)  
 Elwyn et al. (Physical Review, Part C, Nuclear Physics, Vol.16, 1977)  
 : Angular distribution data: Foteinou et al. (Nucl. Instrum. Methods in Physics Res., Sect.B, Vol.269, 2011)

# $^7\text{Li}(\text{p},\alpha)\alpha$



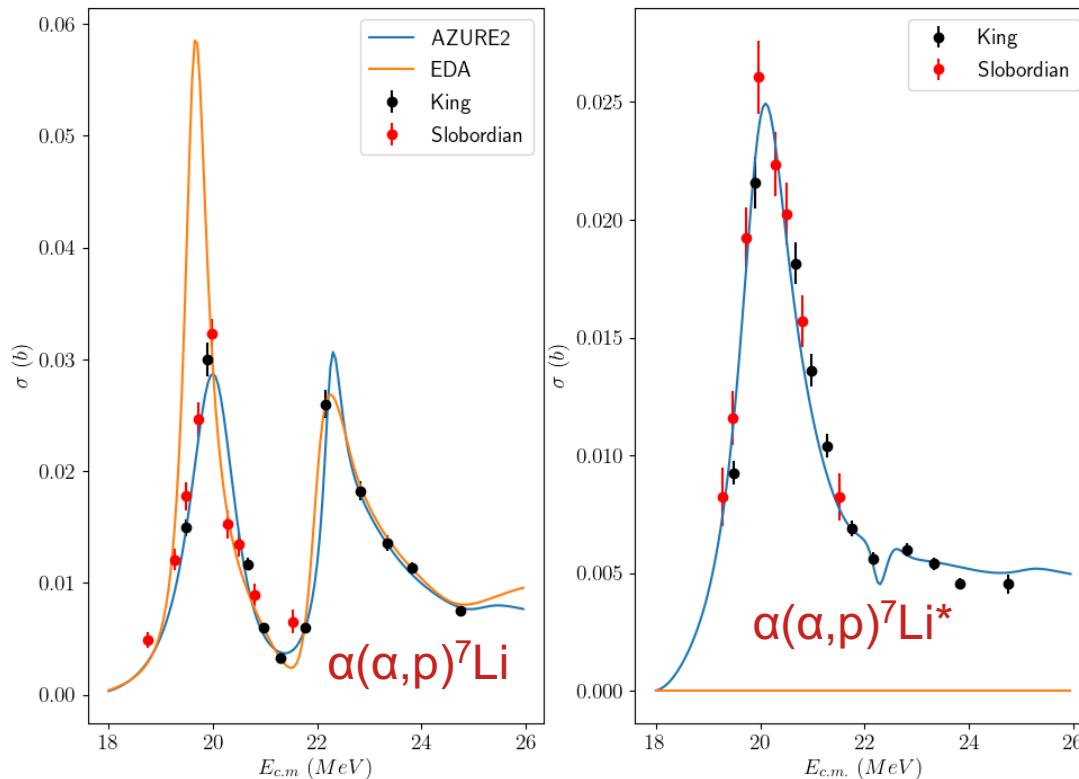
## Scaling Factors

Mani: 0.5

Rice and Saclay:  $(10/7)*0.5$   
(Erratum: Nuclear Physics 41 (1963) 176)

Data Used:  $^7\text{Li}(\text{p},\alpha)\alpha$  :Integrated cross section: Rice: Cassagnou *et. al.* (Nuclear Physics, Vol.33, Issue.3, p.449 (1962))  
Mani *et . al.* (Nuclear Physics, Vol.60, Issue.4, p.588 (1964))  
Saclay:Cassagnou *et. al.* (Nuclear Physics, Vol.33, Issue.3, p.449 (1962))

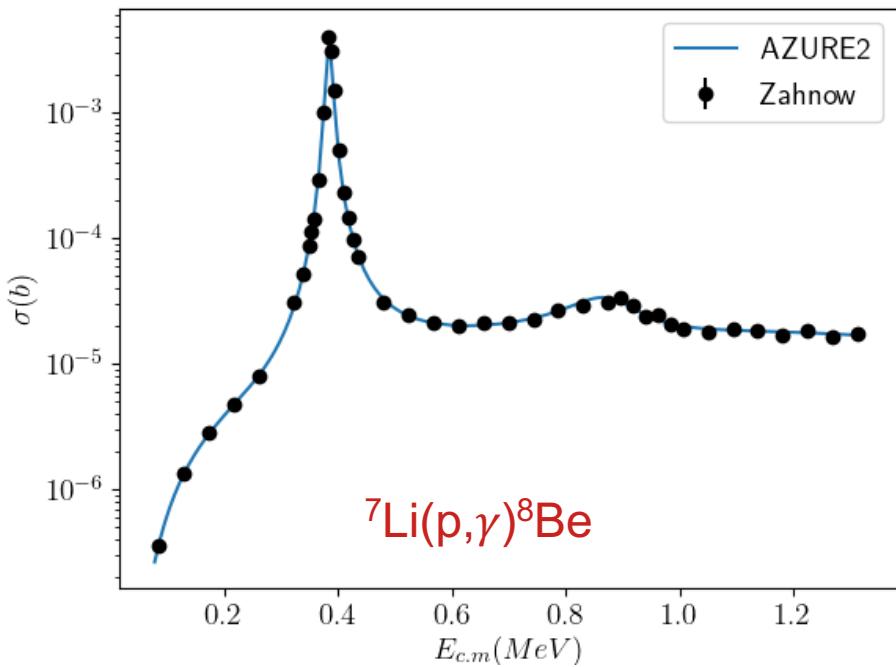
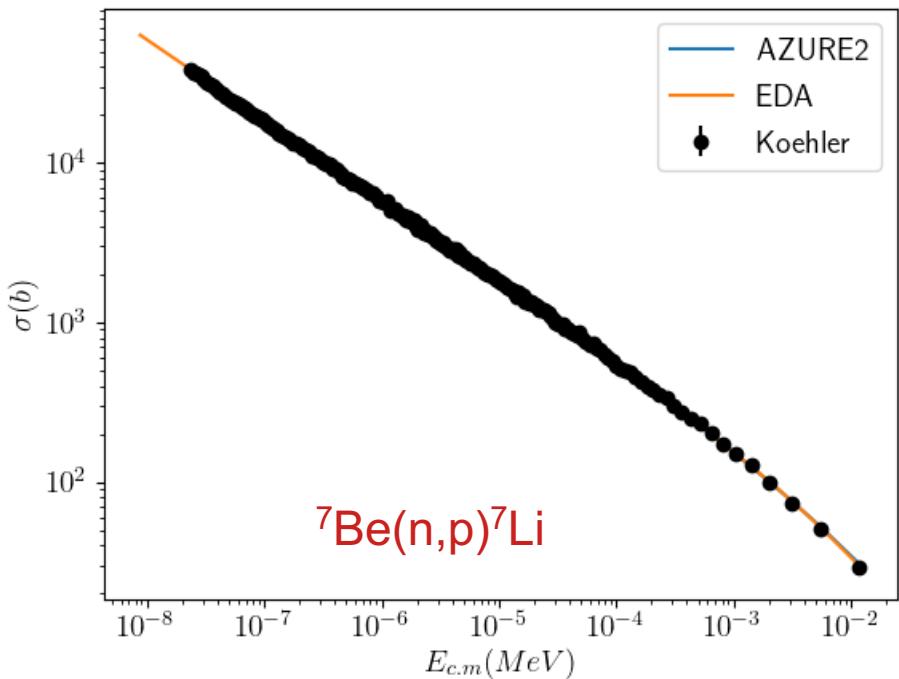
# $\alpha(\alpha,p)^7\text{Li}$ and $\alpha(\alpha,p)^7\text{Li}^*$



Data Used:  $\alpha(\alpha,p)^7\text{Li}, {}^7\text{Li}^*$  : Partial cross section: C.H.King et. al. (Phys. Rev. C, 16, 1712, 1977)

: Partial cross section: R. J. Slobodian et. al. (Zeitschrift fuer Physik A, Hadrons and Nuclei, Vol.308, Issue.1, p.15 (1982))

# $^7\text{Be}(\text{n},\text{p})^7\text{Li}$ and $^7\text{Li}(\text{p},\gamma)^8\text{Be}$



Data Used:  $^7\text{Be}(\text{n},\text{p})^7\text{Li}$  : Integrated cross section: Koehler et. al. (Phys. Rev. C, 37, 917, 1988)

$^7\text{Li}(\text{p},\gamma)^8\text{Be}$ : Partial Cross section: D. Zahnow et. al. (Zeitschrift fuer Physik A, Hadrons and Nuclei, Vol.351, p.229 (1995))

# Summary/Future Work

- Preliminary results from  $R$ -matrix analysis of  ${}^8\text{Be}$  system with AZURE2 was compared with EDA calculations.
- Use AZURE2 parameters as reference while updating EDA evaluations for  ${}^8\text{Be}$  system.
- Sensitivity studies for channel radius and background level dependence.
- Estimate the uncertainty bands.
- Check for overfitting and see if the parameters are actually constrained by the data.
- Angular distribution data for  ${}^6\text{Li}(\text{d},\text{n}){}^7\text{Be}$  from new measurement will be added to the fits.

# Collaborators

- C. Fichtl
- S. Kuvin
- H.Y. Lee
- M. Mosby
- C. Prokop

M. Febbraro  
J. Nattress

- R. J. deBoer  
K. Manukyan  
D. Robertson  
E. Stech  
W. Tan



Acknowledgements: M. Paris (LANL)  
G. Hale (LANL)  
K. Toshihiko (LANL)  
H. Sasaki (LANL)  
C. Brune (Ohio U)



Funded by:



# Thank You.