

MULTI-SCALE NUCLEAR IMAGING AT THE EIC

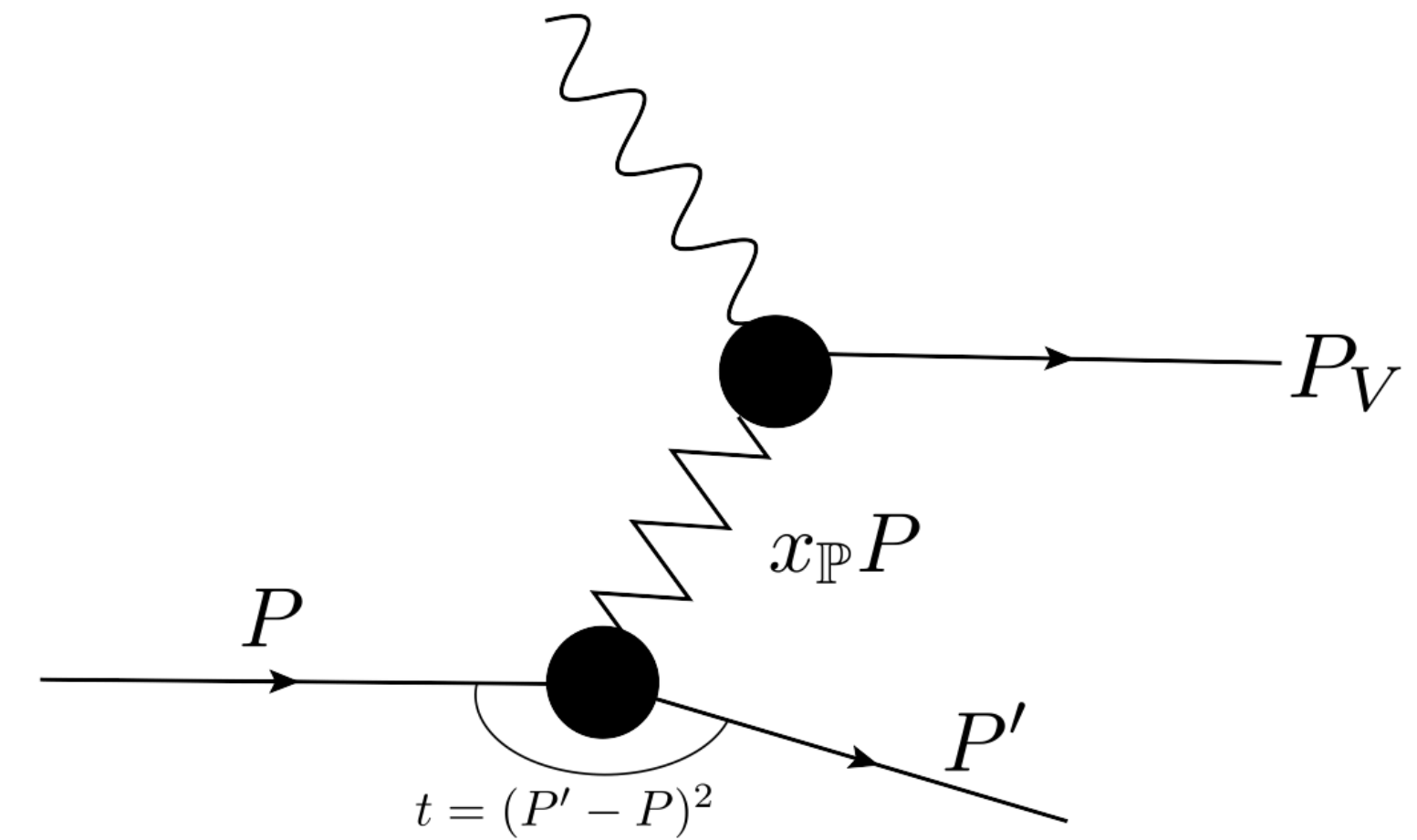
BJÖRN SCHENKE, BROOKHAVEN NATIONAL LABORATORY

EIC Detector 2 WG Meeting
03/21/2023

Diffractive vector meson production

— Coherent diffraction:
$$\frac{d\sigma^{\gamma^*p \rightarrow Vp}}{dt} = \frac{1}{16\pi} \left| \left\langle A^{\gamma^*p \rightarrow Vp} \left(x_P, Q^2, \vec{\Delta} \right) \right\rangle \right|^2$$

sensitive to the average size of the target



— Incoherent diffraction:
$$\frac{d\sigma^{\gamma^*p \rightarrow Vp^*}}{dt} = \frac{1}{16\pi} \left(\left\langle \left| A^{\gamma^*p \rightarrow Vp} \left(x_P, Q^2, \vec{\Delta} \right) \right|^2 \right\rangle - \left| \left\langle A^{\gamma^*p \rightarrow Vp} \left(x_P, Q^2, \vec{\Delta} \right) \right\rangle \right|^2 \right)$$

sensitive to fluctuations (including geometric ones)

H. Kowalski, L. Motyka, G. Watt, Phys.Rev. D 74 (2006) 074016

A. Caldwell, H. Kowalski, EDS 09, 190-192, e-Print: 0909.1254 [hep-ph]

M. L. Good and W. D. Walker, Phys. Rev. 120 (1960) 1857

H. I. Miettinen and J. Pumplin, Phys. Rev. D18 (1978) 1696

Y. V. Kovchegov and L. D. McLerran, Phys. Rev. D60 (1999) 054025

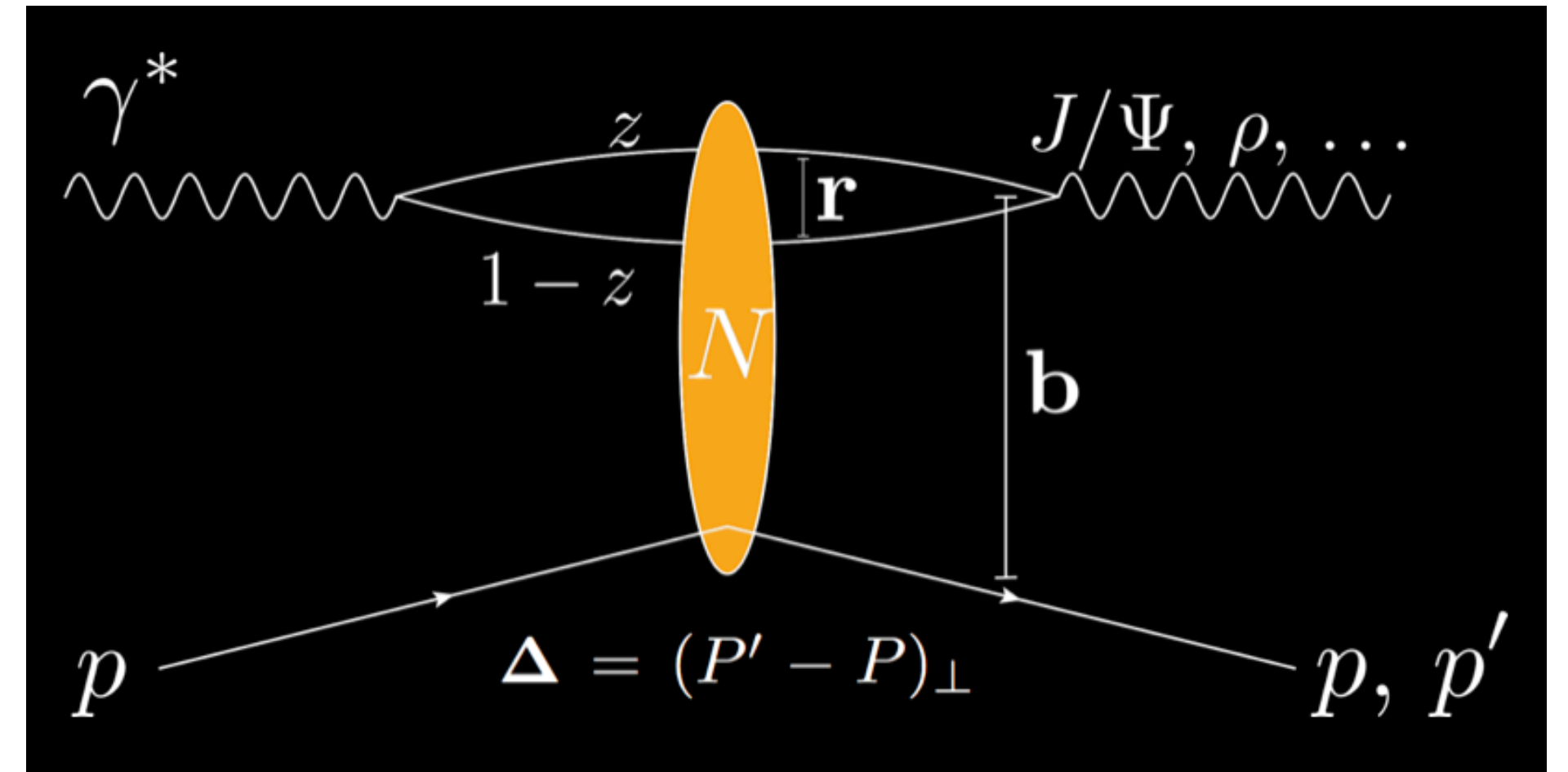
A. Kovner and U. A. Wiedemann, Phys. Rev. D64 (2001) 114002

Dipole picture: Scattering amplitude

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys.Rev. D94 (2016) 034042

High energy factorization:

- $\gamma^* \rightarrow q\bar{q} : \psi^\gamma(r, Q^2, z)$
- $q\bar{q}$ dipole scatters with amplitude N
- $q\bar{q} \rightarrow V : \psi^V(r, Q^2, z)$



$$A \sim \int d^2b dz d^2r \psi^* \psi^V(\vec{r}, z, Q^2) e^{-i\vec{b} \cdot \vec{\Delta}} N(\vec{r}, x, \vec{b})$$

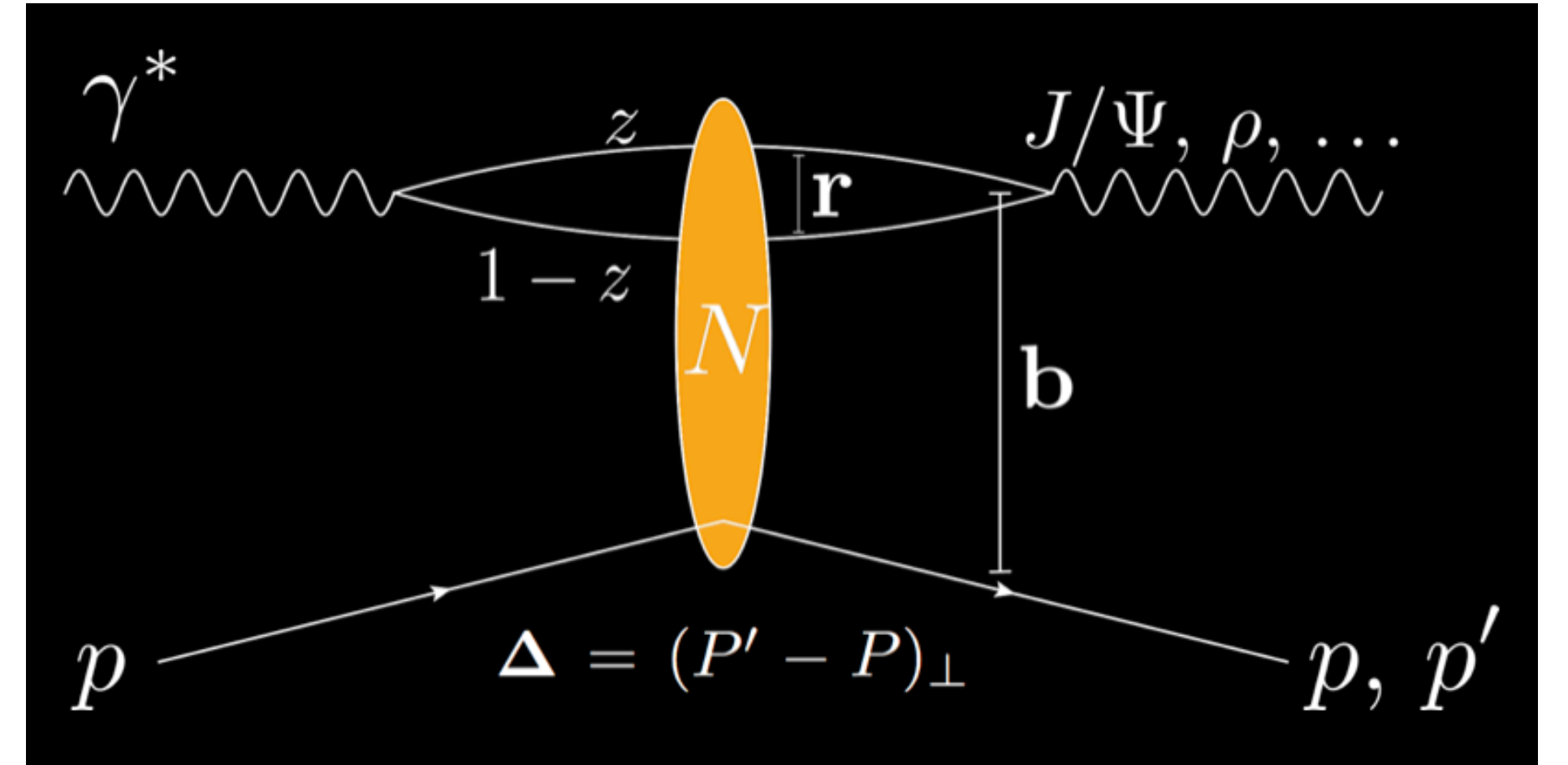
- Impact parameter \mathbf{b} is the Fourier conjugate of transverse momentum transfer $\mathbf{\Delta} \rightarrow$ Access to spatial structure ($t = -\Delta^2$)

Color glass condensate formalism

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys.Rev. D94 (2016) 034042

Compute the Wilson lines using color charges whose correlator depends on \vec{b}_\perp

$$\langle \rho^a(\mathbf{b}_\perp) \rho^b(\mathbf{x}_\perp) \rangle = g^2 \mu^2(x, \mathbf{b}_\perp) \delta^{ab} \delta^{(2)}(\mathbf{b}_\perp - \mathbf{x}_\perp)$$



$$N(\vec{r}, x, \vec{b}) = N(\vec{x} - \vec{y}, x, (\vec{x} + \vec{y})/2) = 1 - \text{Tr}(\mathbf{V}(\vec{x}) \mathbf{V}^\dagger(\vec{y})) / N_c$$

The trace appears at the level of the amplitude, because we project on a **color singlet**

$$A \sim \int d^2b dz d^2r \psi^* \psi^V(\vec{r}, z, Q^2) e^{-i\vec{b} \cdot \vec{\Delta}} N(\vec{r}, x, \vec{b})$$

Model impact parameter dependence (proton, nucleon)

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys.Rev. D94 (2016) 034042

1) Assume Gaussian proton shape:

$$T(\vec{b}) = T_p(\vec{b}) = \frac{1}{2\pi B_p} e^{-b^2/(2B_p)}$$

2) Assume Gaussian distributed and Gaussian shaped hot spots:

$$P(b_i) = \frac{1}{2\pi B_{qc}} e^{-b_i^2/(2B_{qc})} \quad (\text{angles uniformly distributed})$$

$$T_p(\vec{b}) = \frac{1}{N_q} \sum_{i=1}^{N_q} T_q(\vec{b} - \vec{b}_i) \quad \text{with } N_q \text{ hot spots;} \quad T_q(\vec{b}) = \frac{1}{2\pi B_q} e^{-b^2/(2B_q)}$$

Diffractive J/ψ production in e+p at HERA

Nucleon parameters $B_{q'}$, $B_{qc'}$ can be constrained by e+p scattering data from HERA

Exclusive diffractive J/ψ production in e+p:

Incoherent x-sec sensitive to fluctuations

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301

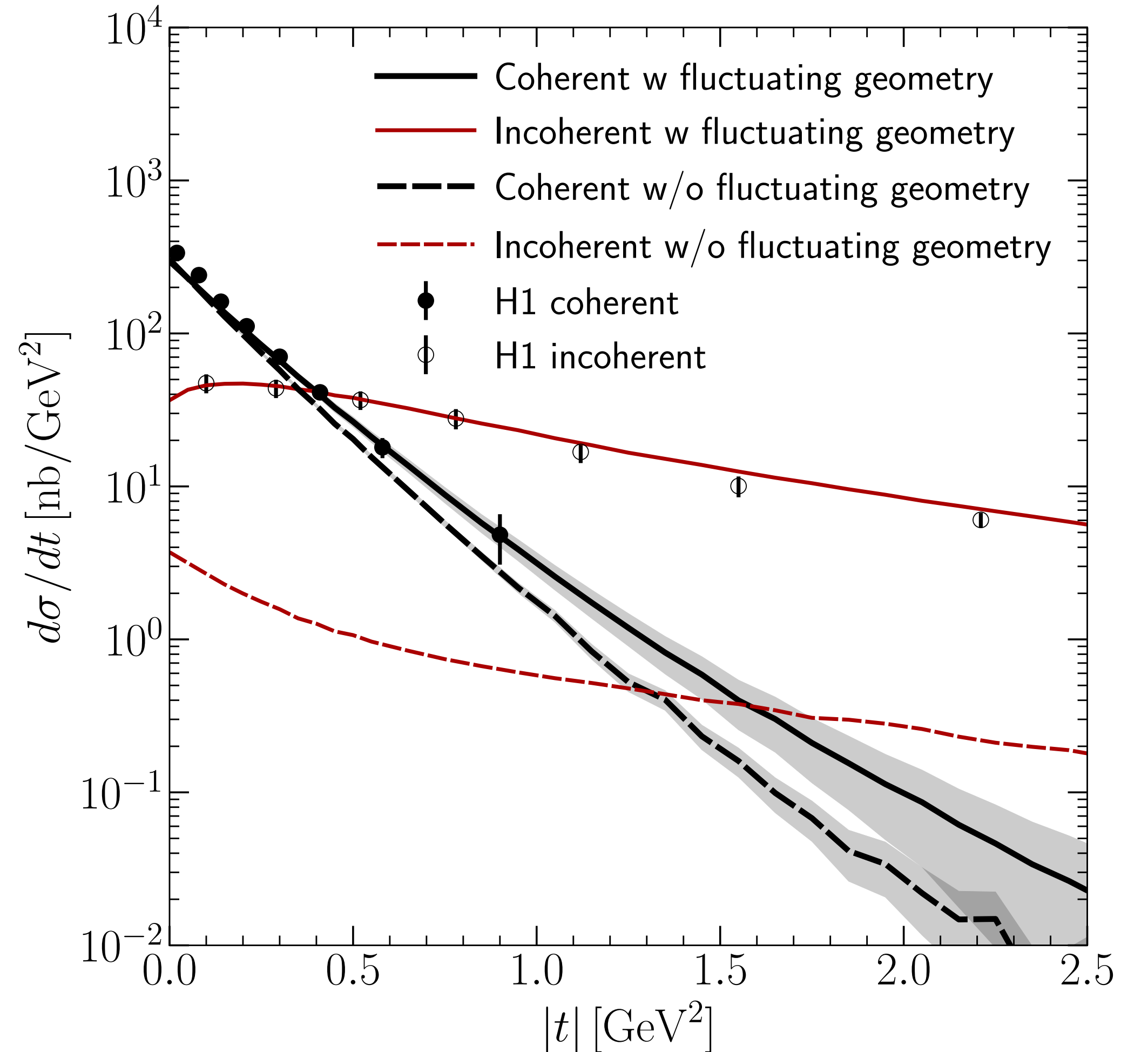
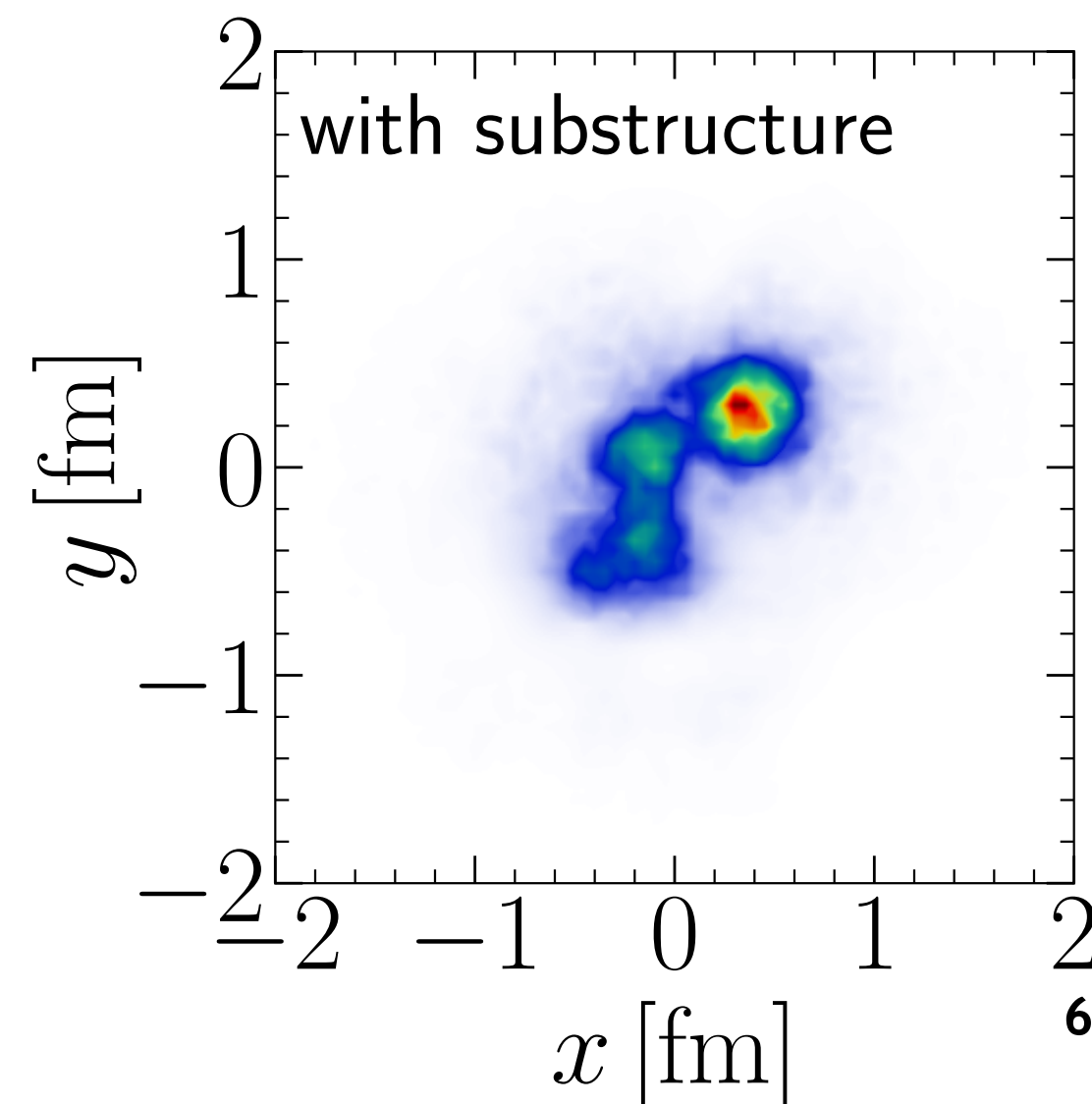
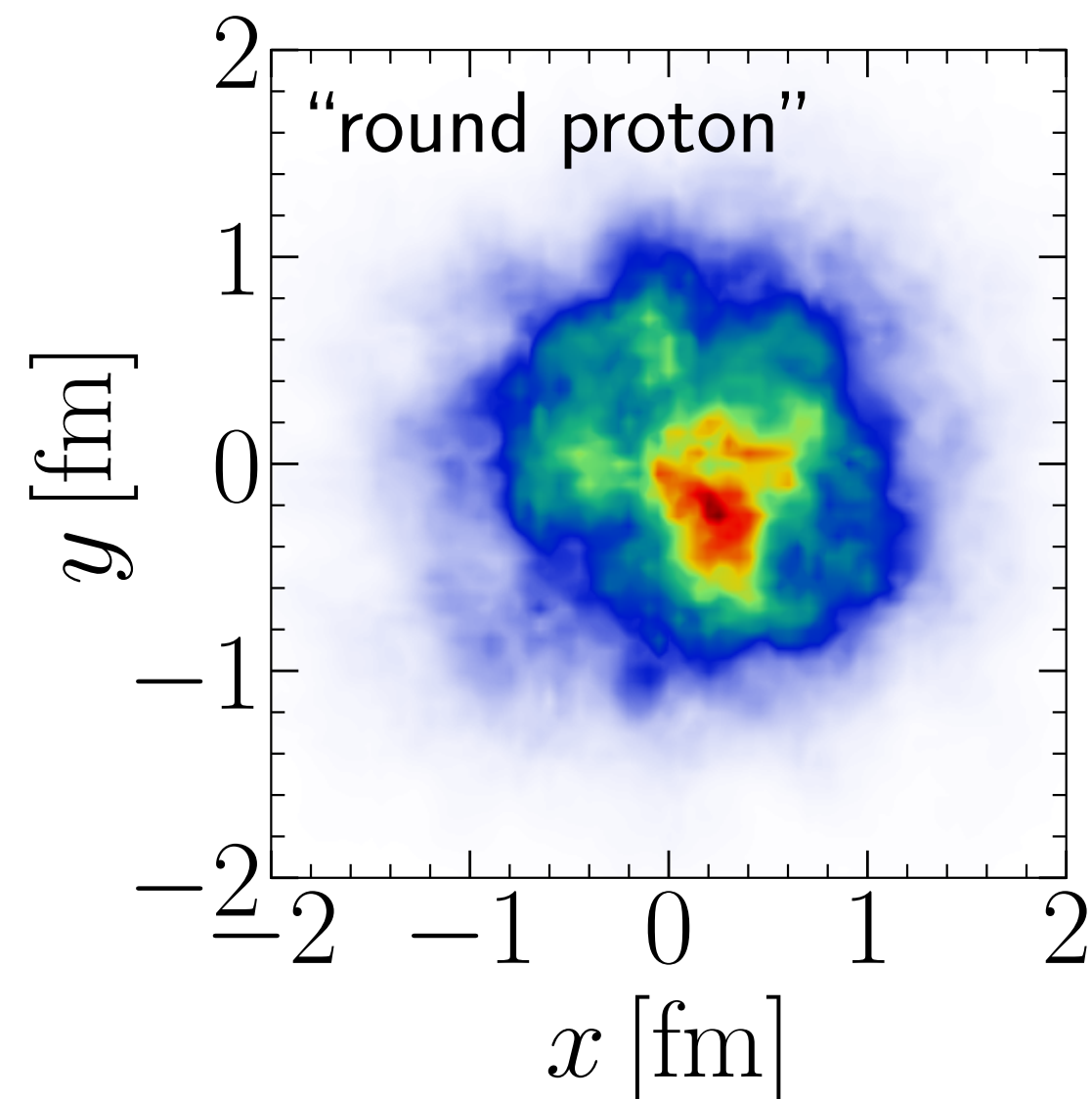
Phys.Rev. D94 (2016) 034042

also see:

S. Schlichting, B. Schenke, Phys.Lett. B739 (2014) 313-319

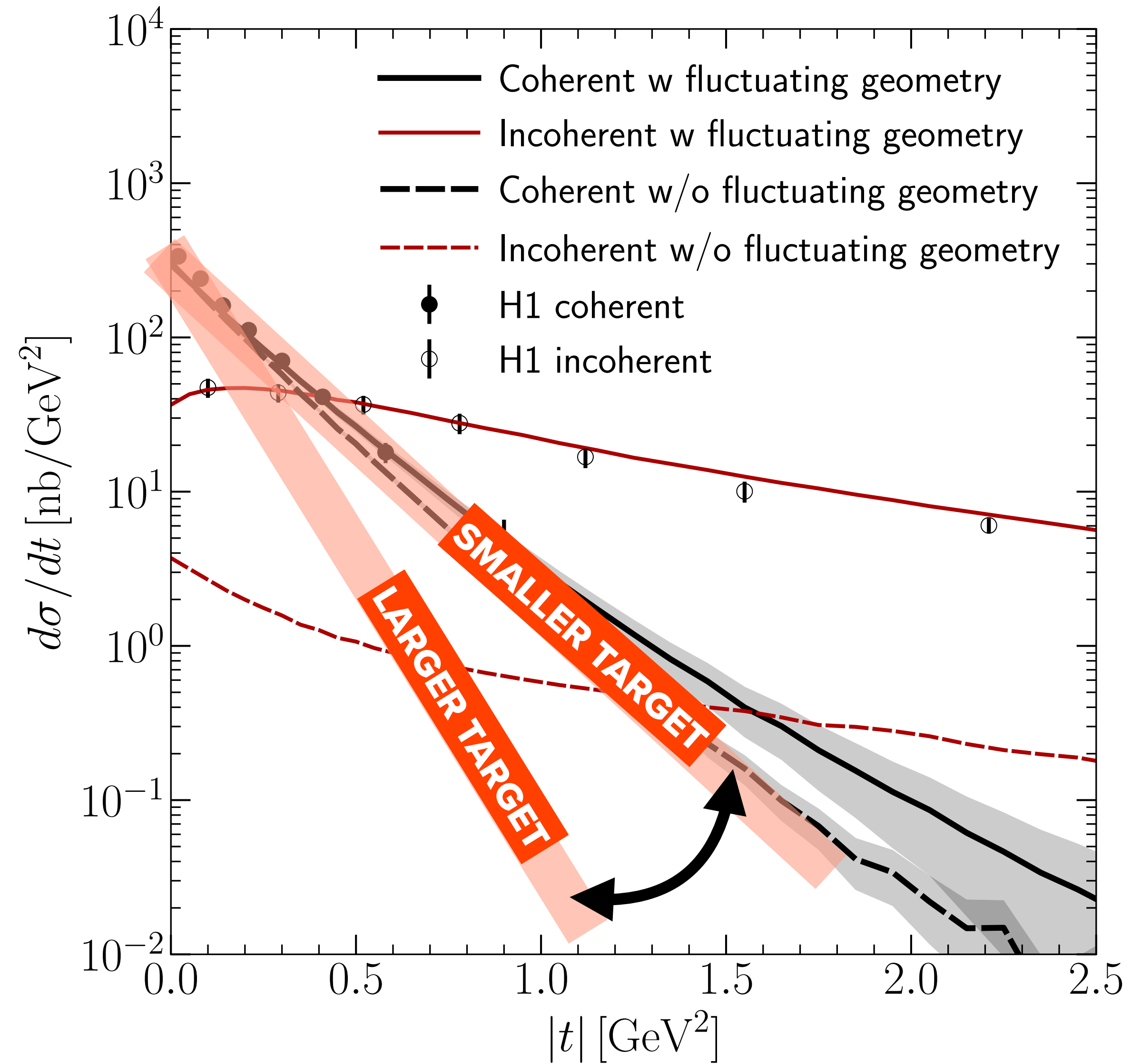
H. Mäntysaari, Rep. Prog. Phys. 83 082201 (2020)

B. Schenke, Rep. Prog. Phys. 84 082301 (2021)



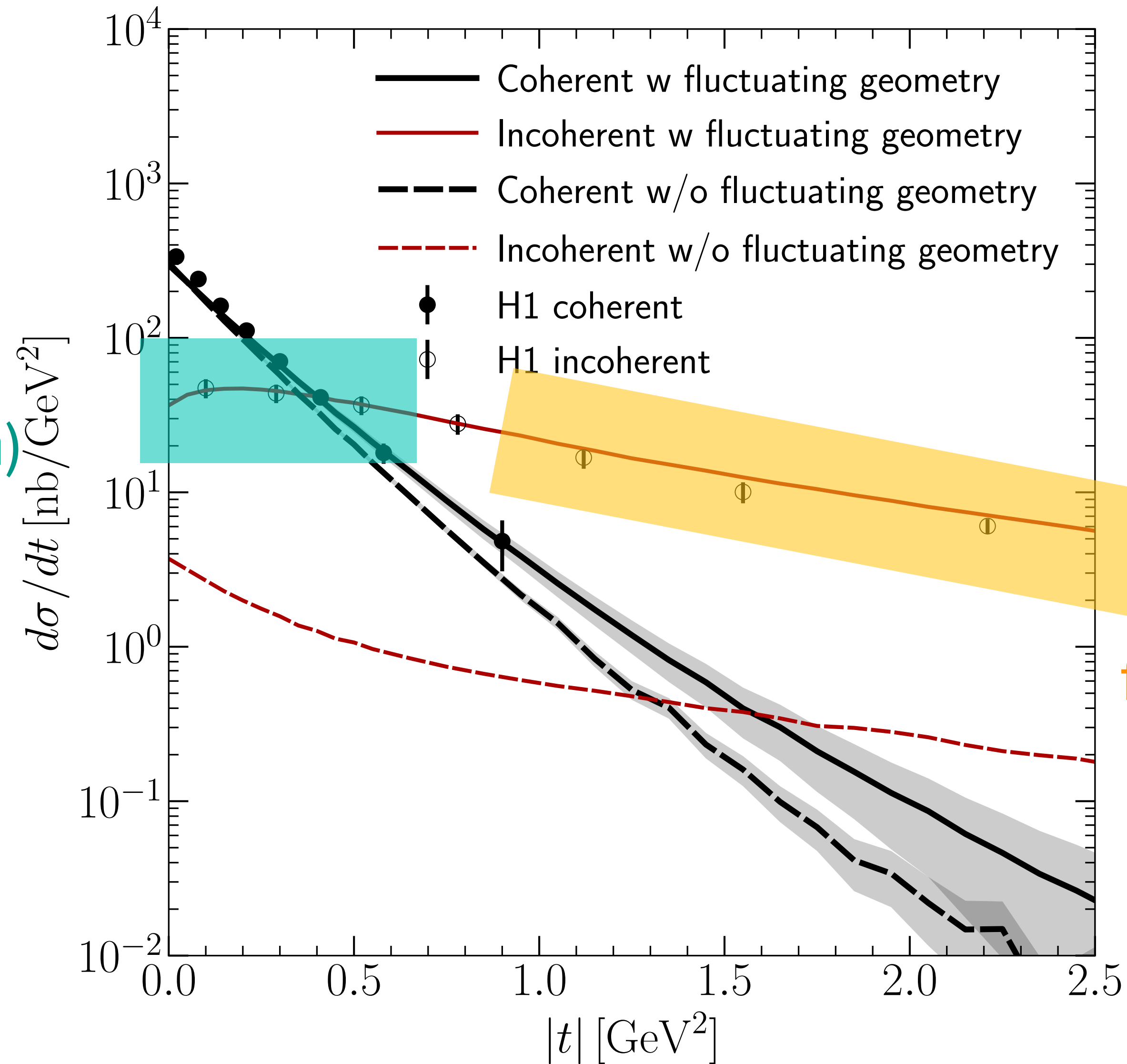
H1 Collaboration, Eur. Phys. J. C73 (2013) no. 6 2466

Information in the diffractive cross sections



Information in the diffractive cross sections

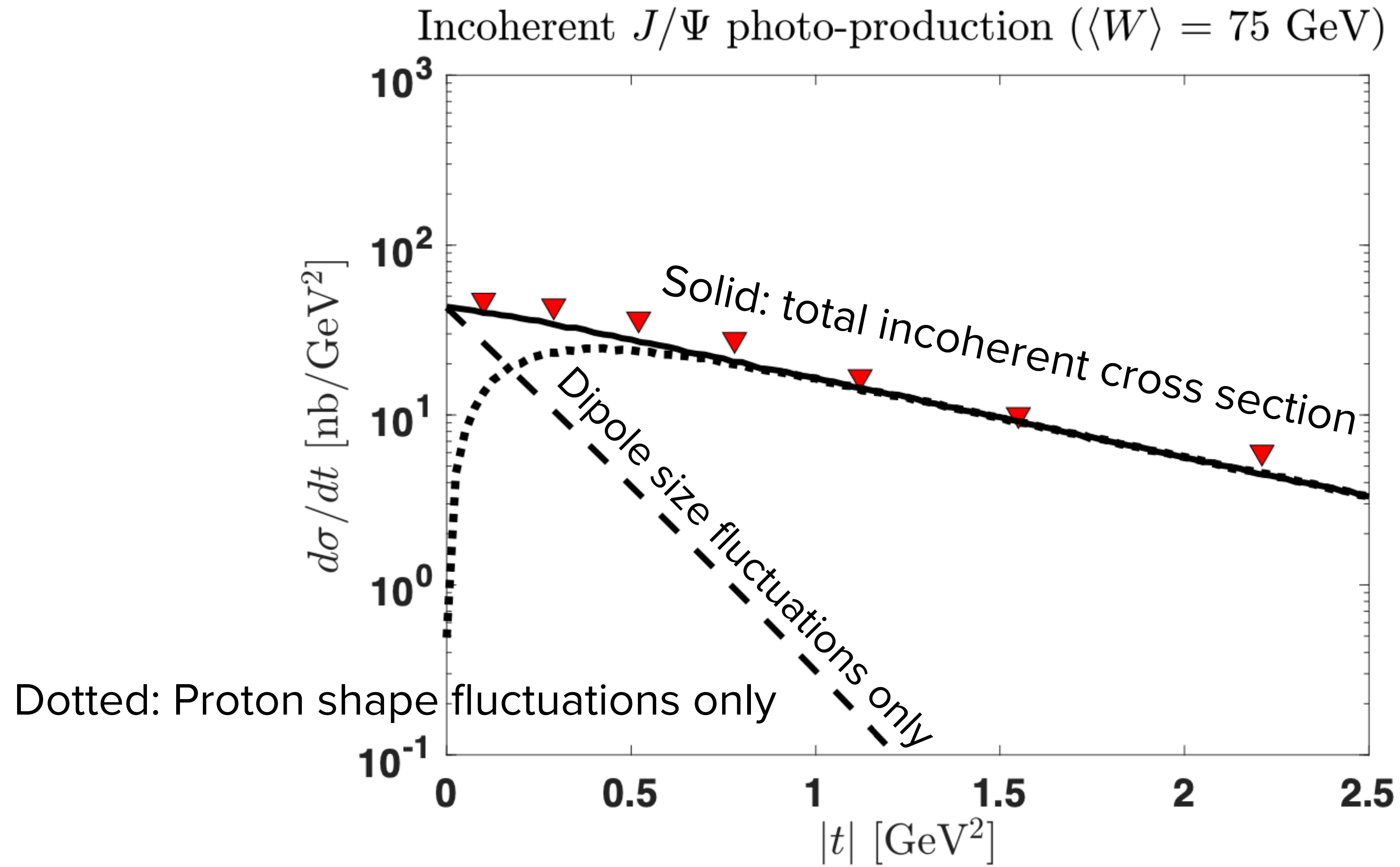
larger scale
fluctuations (>0.2 fm)



short scale
fluctuations (<0.2 fm)

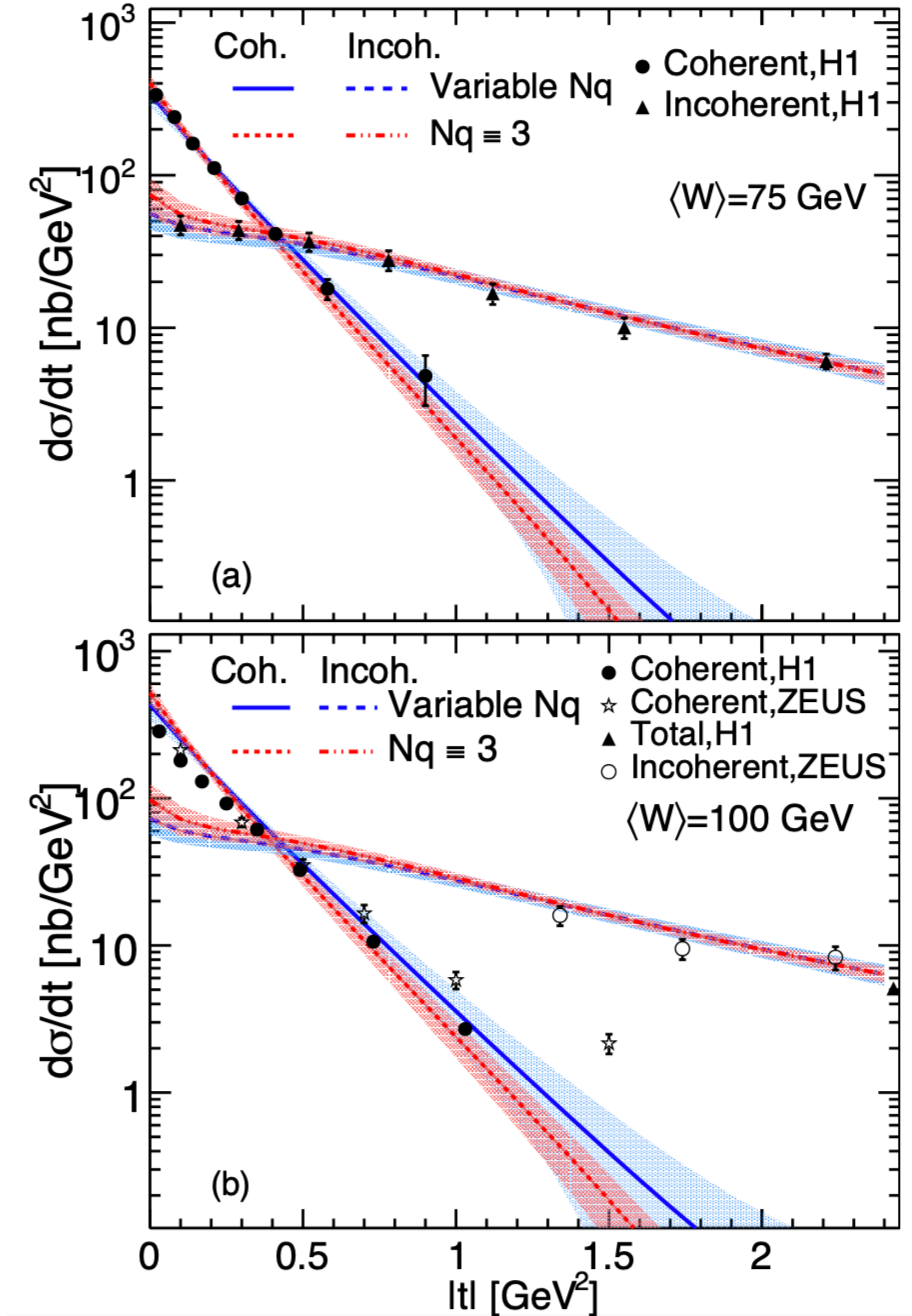
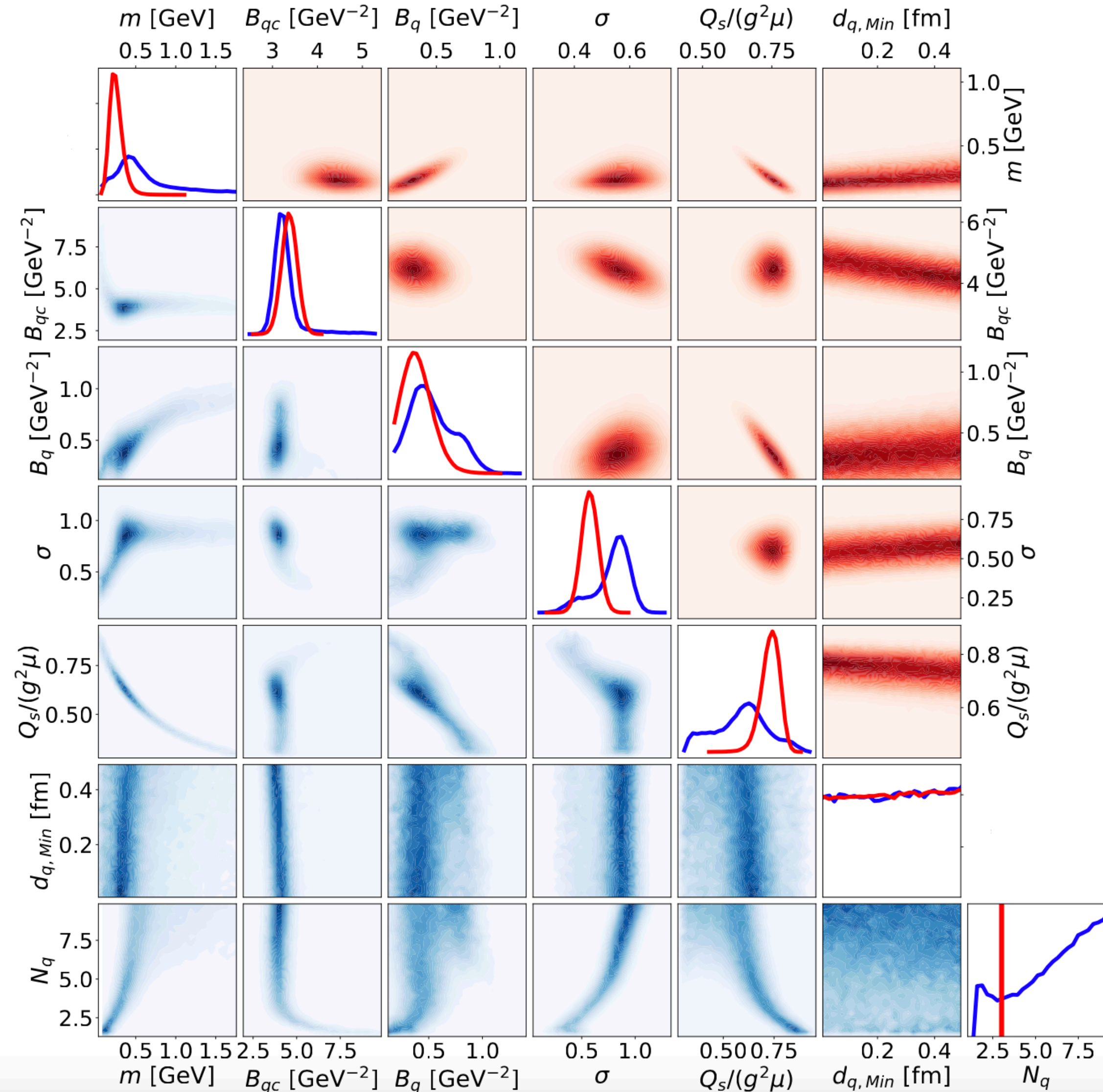
Dipole size fluctuations

Blaizot and Traini, 2209.15545 [hep-ph]



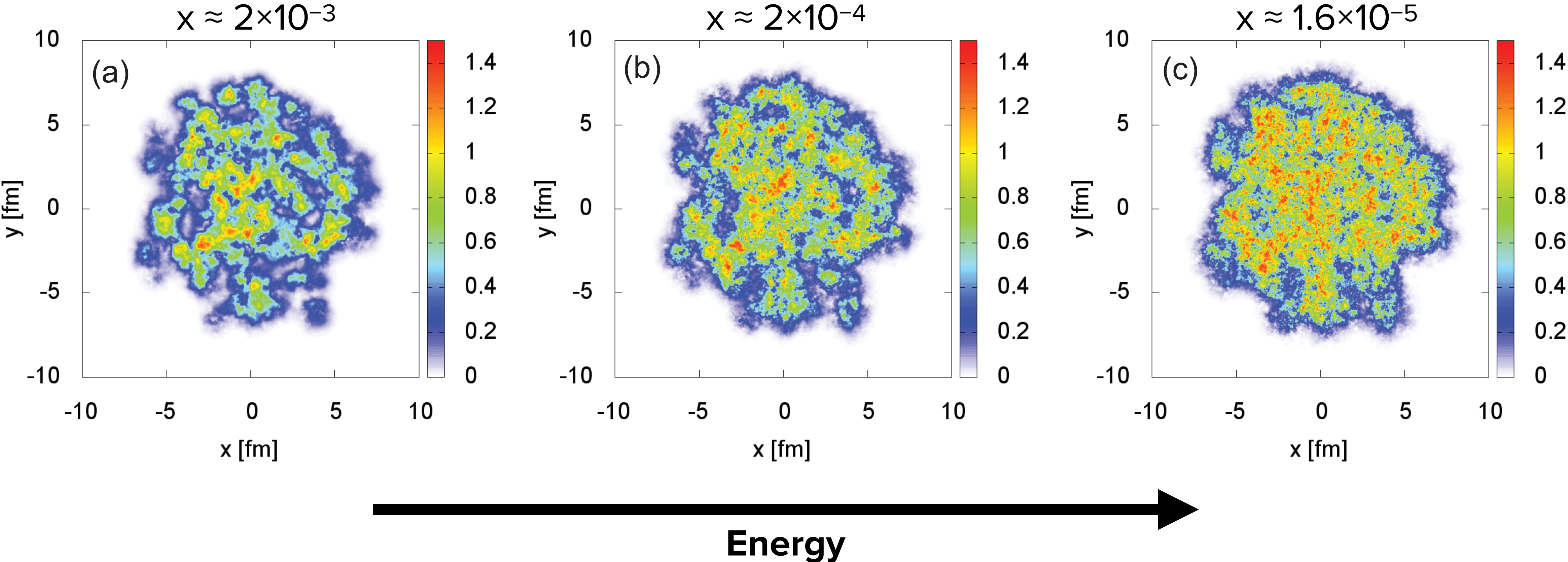
Extracting parameters using Bayesian inference

H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, Phys.Lett.B 833 (2022) 137348



JIMWLK evolution

How does energy evolution affect the nuclear structure?

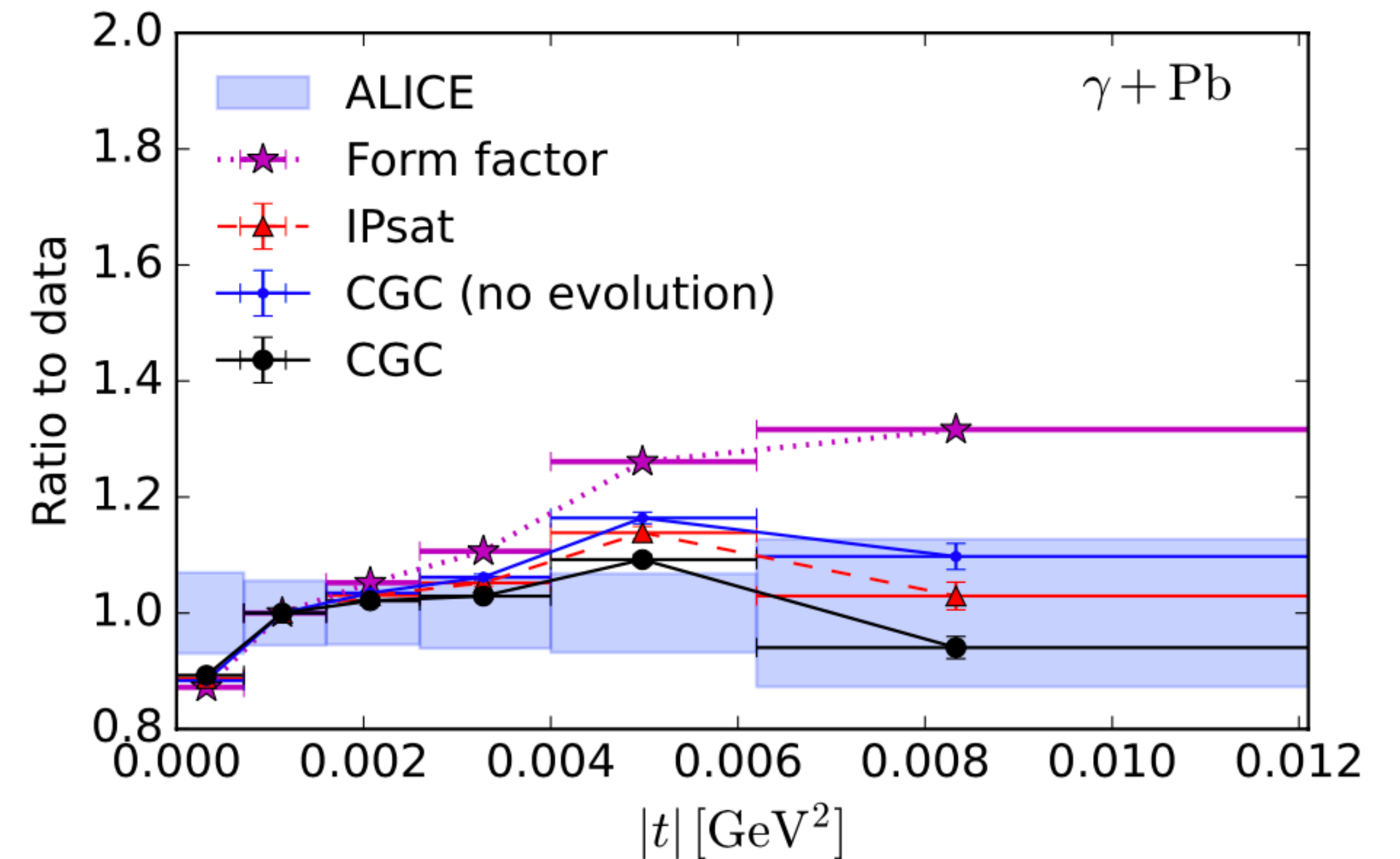
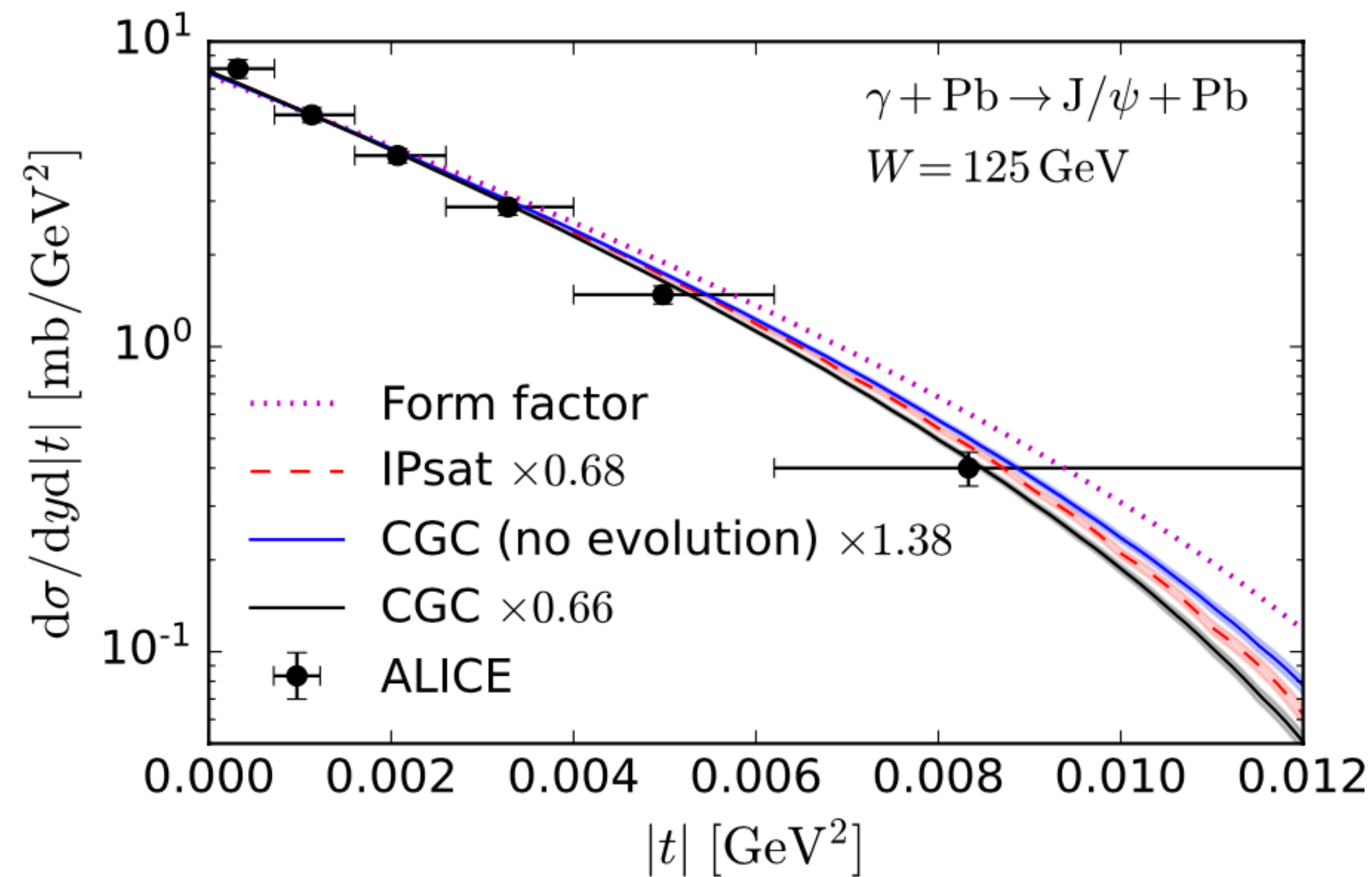


B. Schenke, S. Schlichting, Phys.Rev.C 94 (2016) 4, 044907

UPCs: γ +Pb measurement - Role of saturation effects

H. Mäntysaari, F. Salazar, B. Schenke, *Phys.Rev.D* 106 (2022) 7, 074019

Here, ALICE removed interference and photon k_T effects to get the γ +Pb cross section



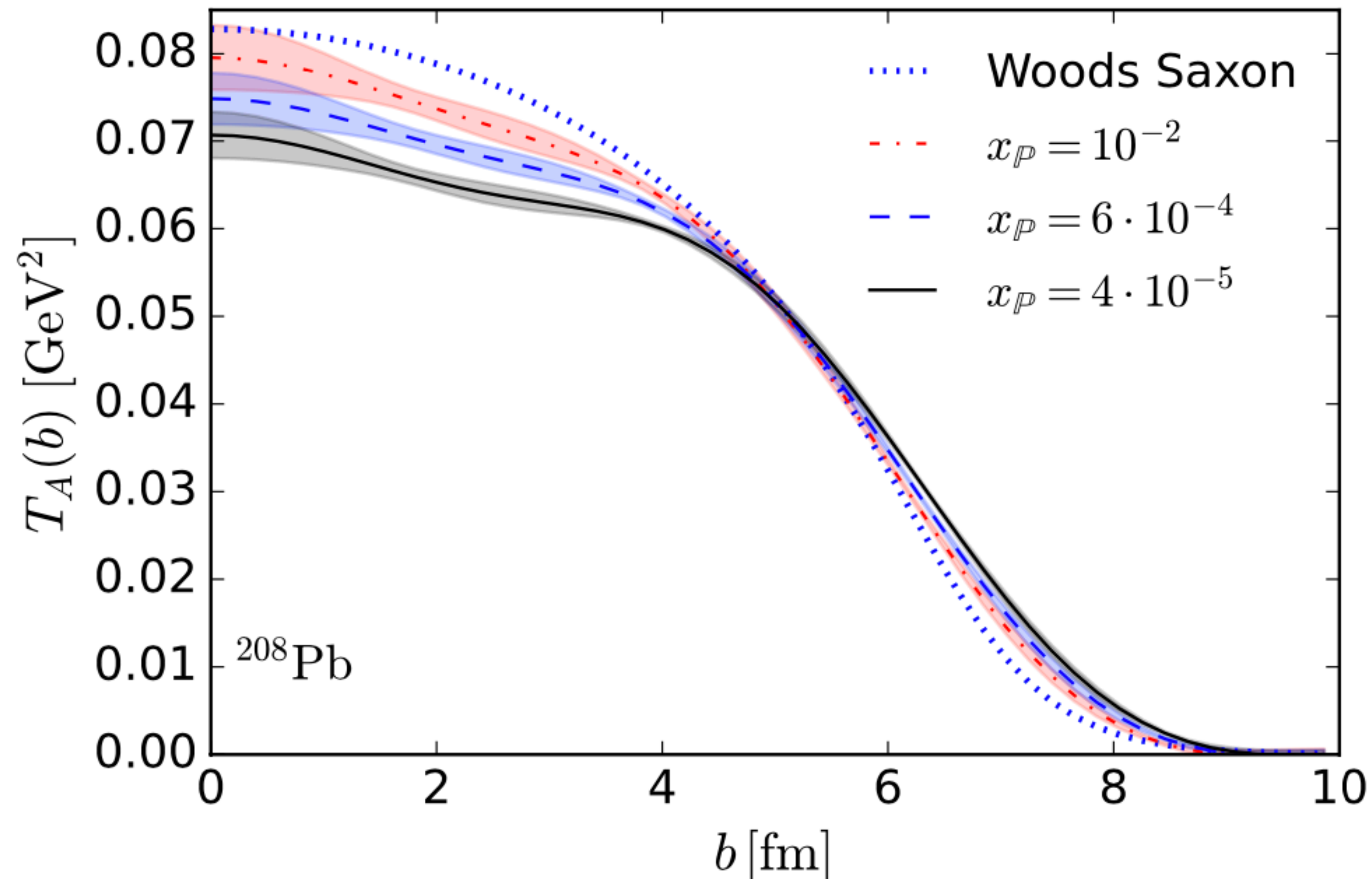
ALICE Collaboration, *Phys.Lett.B* 817 (2021) 136280

Saturation effects improve agreement with experimental data significantly

Saturation effects on nuclear geometry

H. Mäntysaari, F. Salazar, B. Schenke, Phys.Rev.D 106 (2022) 7, 074019

Fourier transform to coordinate space



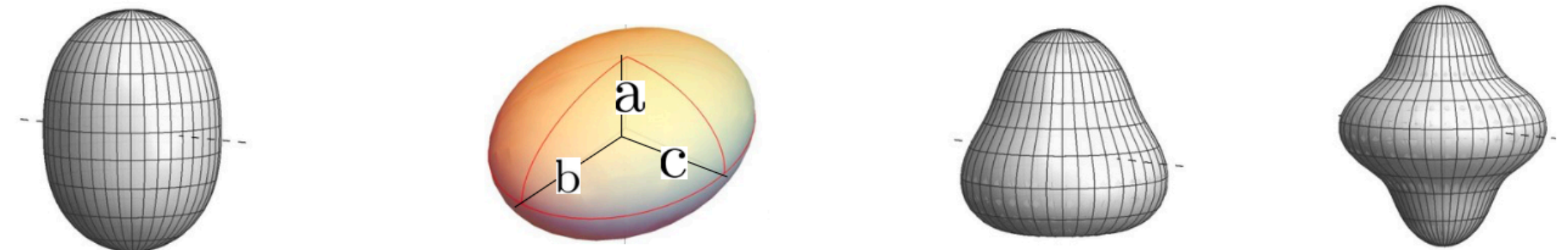
JIMWLK evolution leads to growth of the nucleus towards small x and depletion near the center (normalized so $\int d^2b T_A(b) = 208$)

Effects of deformation on diffractive cross sections

H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, arXiv:2303.04866

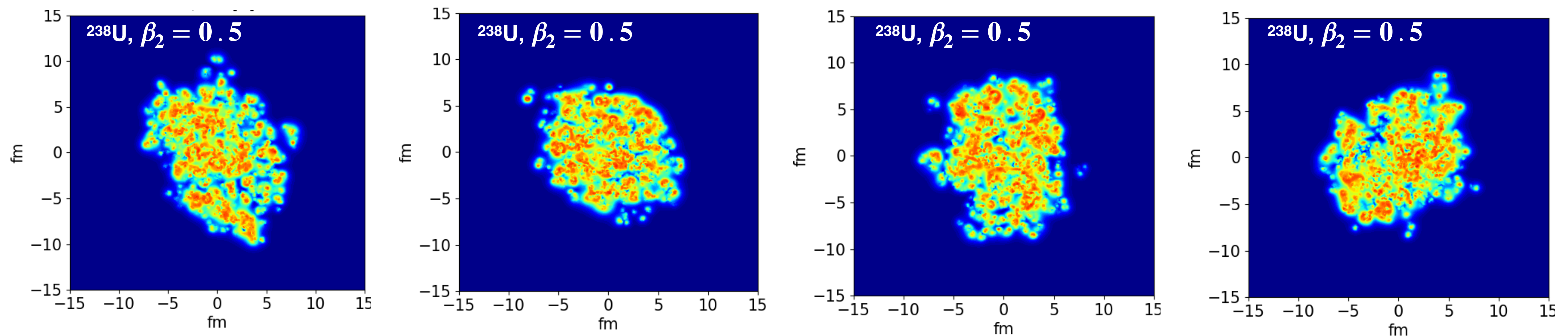
Implement deformation in the Woods-Saxon distribution:

$$\rho(r, \Theta, \Phi) \propto \frac{1}{1 + \exp([r - R(\Theta, \Phi)]/a)}, \quad R(\Theta, \Phi) = R_0 \left[1 + \beta_2 \left(\cos \gamma Y_{20}(\Theta) + \sin \gamma Y_{22}(\Theta, \Phi) \right) + \beta_3 Y_{30}(\Theta) + \beta_4 Y_{40}(\Theta) \right]$$



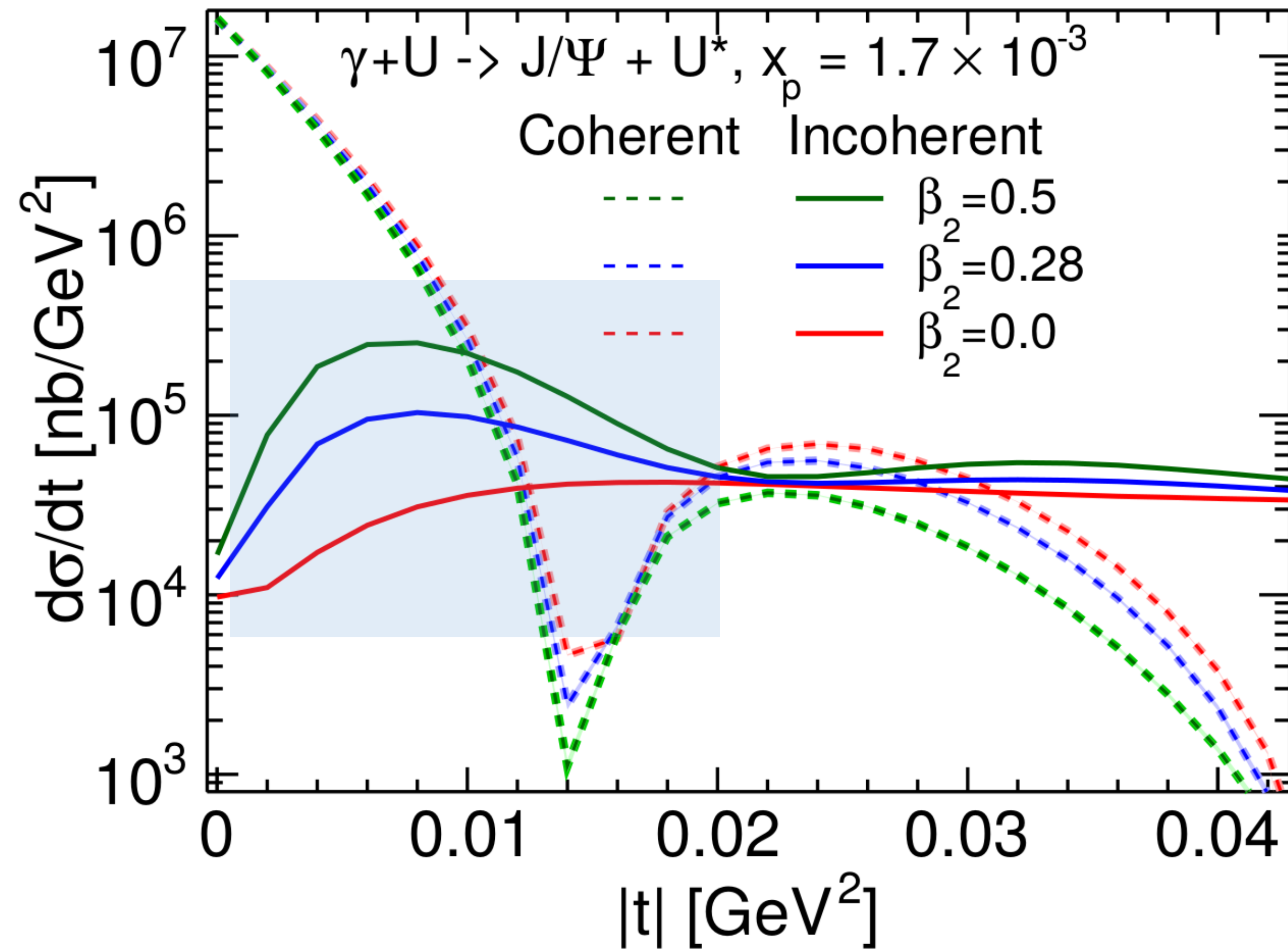
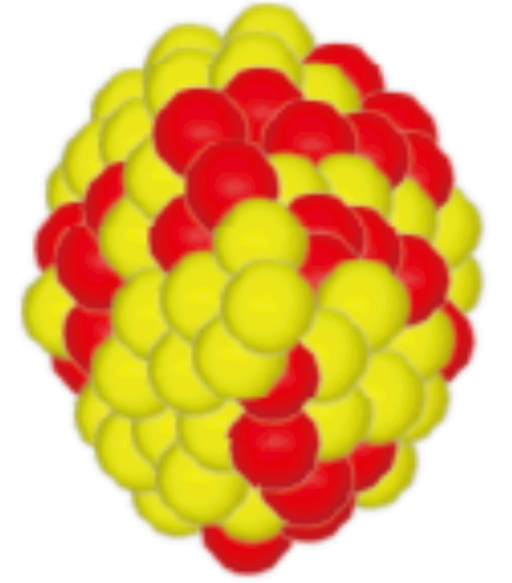
from G. Giacalone

Deformed nuclei exhibit larger fluctuation in the transverse projection:



Effects of deformation on diffractive cross sections: Uranium

H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, arXiv:2303.04866



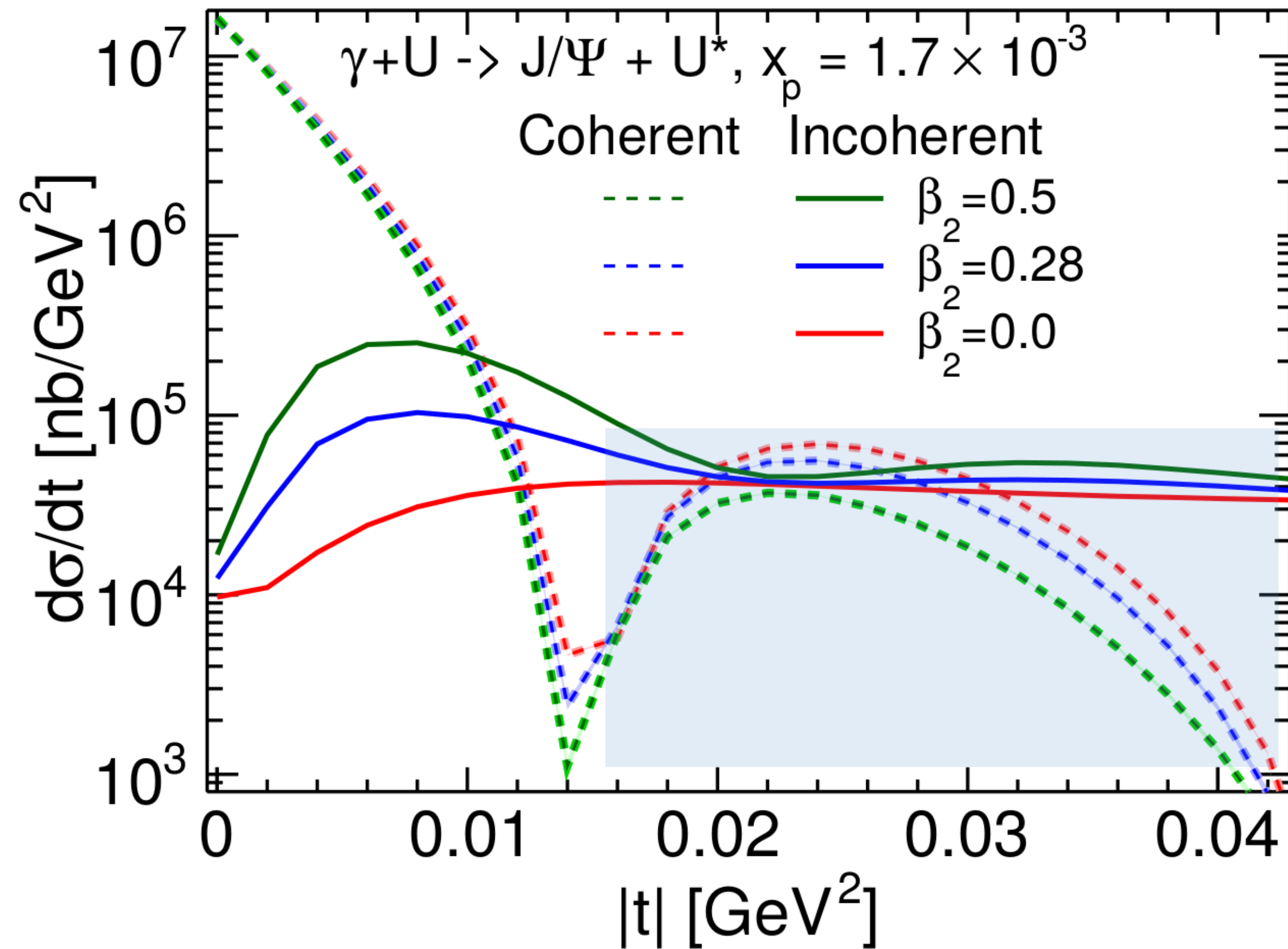
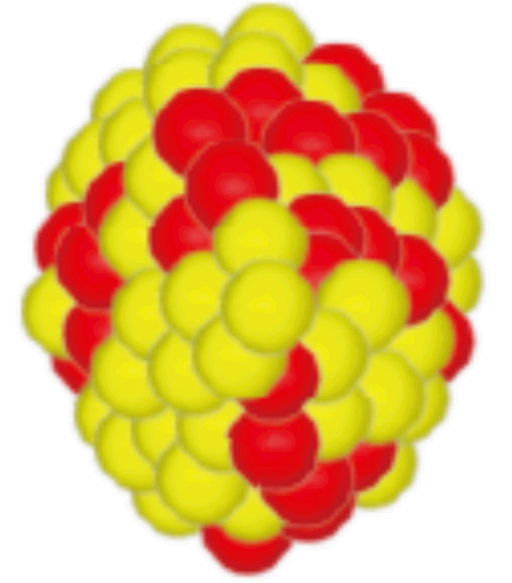
Deformation of the nucleus affects incoherent cross section at small $|t|$ (large length scales)

This observable provides direct information on the small x structure

$$Q^2 = 0$$

Effects of deformation on diffractive cross sections: Uranium

H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, arXiv:2303.04866



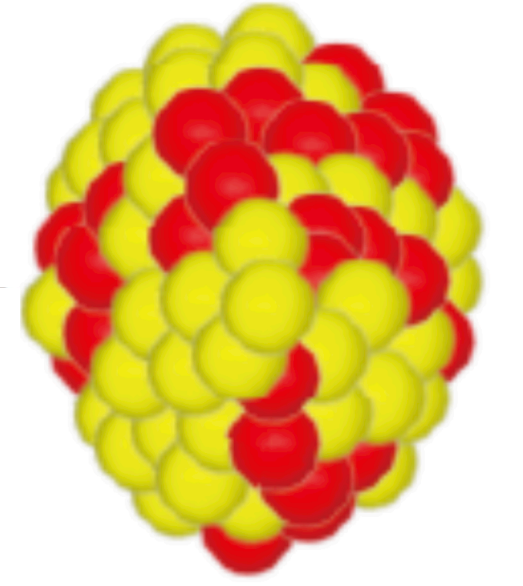
Deformation changes the shape of the average 2D projection of the nucleus



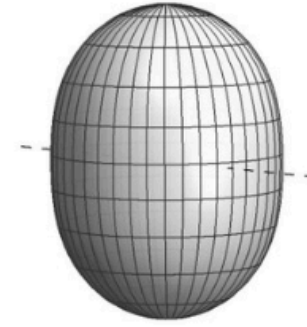
Modification of the coherent cross section

Effects of deformation on diffractive cross sections: Uranium

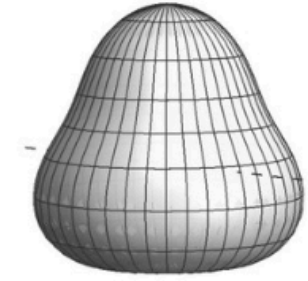
H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, arXiv:2303.04866



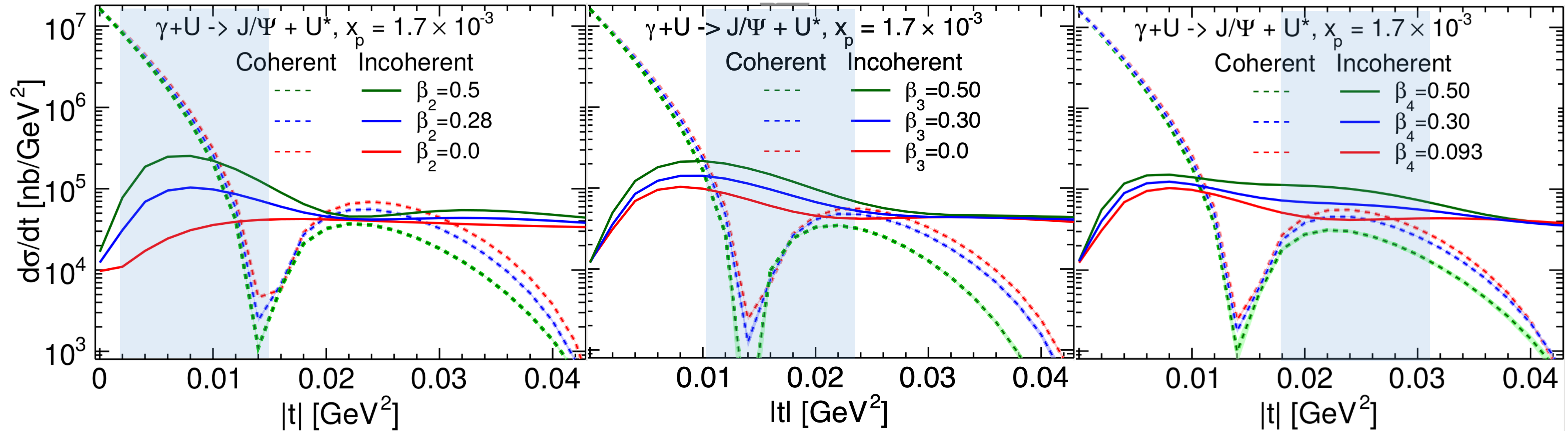
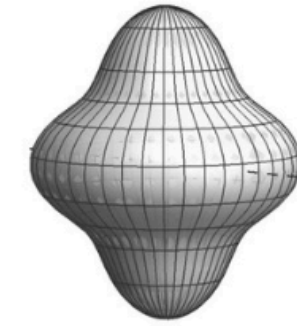
β_2



β_3



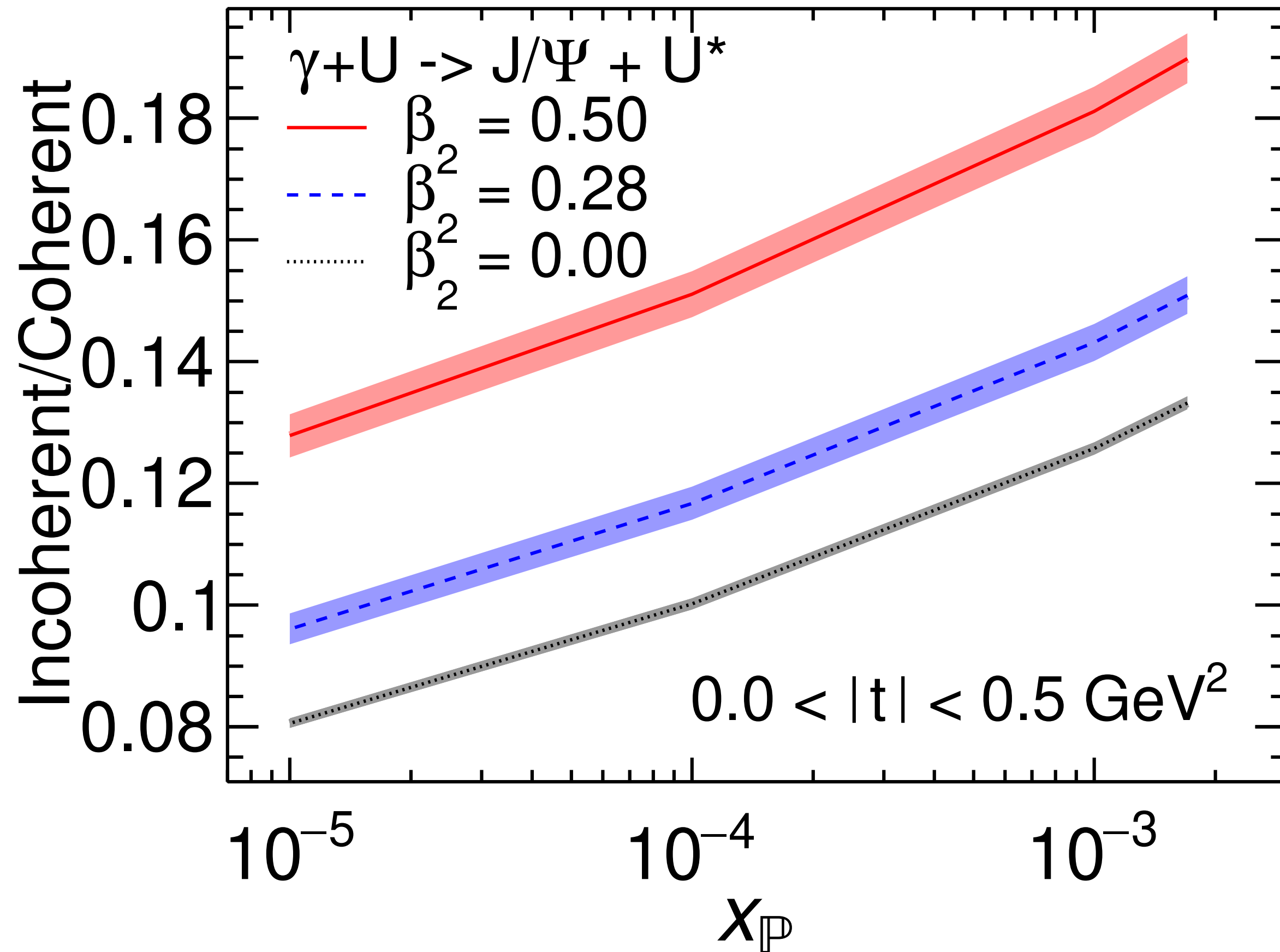
β_4



- β_2 , β_3 and β_4 modify fluctuations at different length scales:
Change incoherent cross section in different $|t|$ regions

Towards smaller x

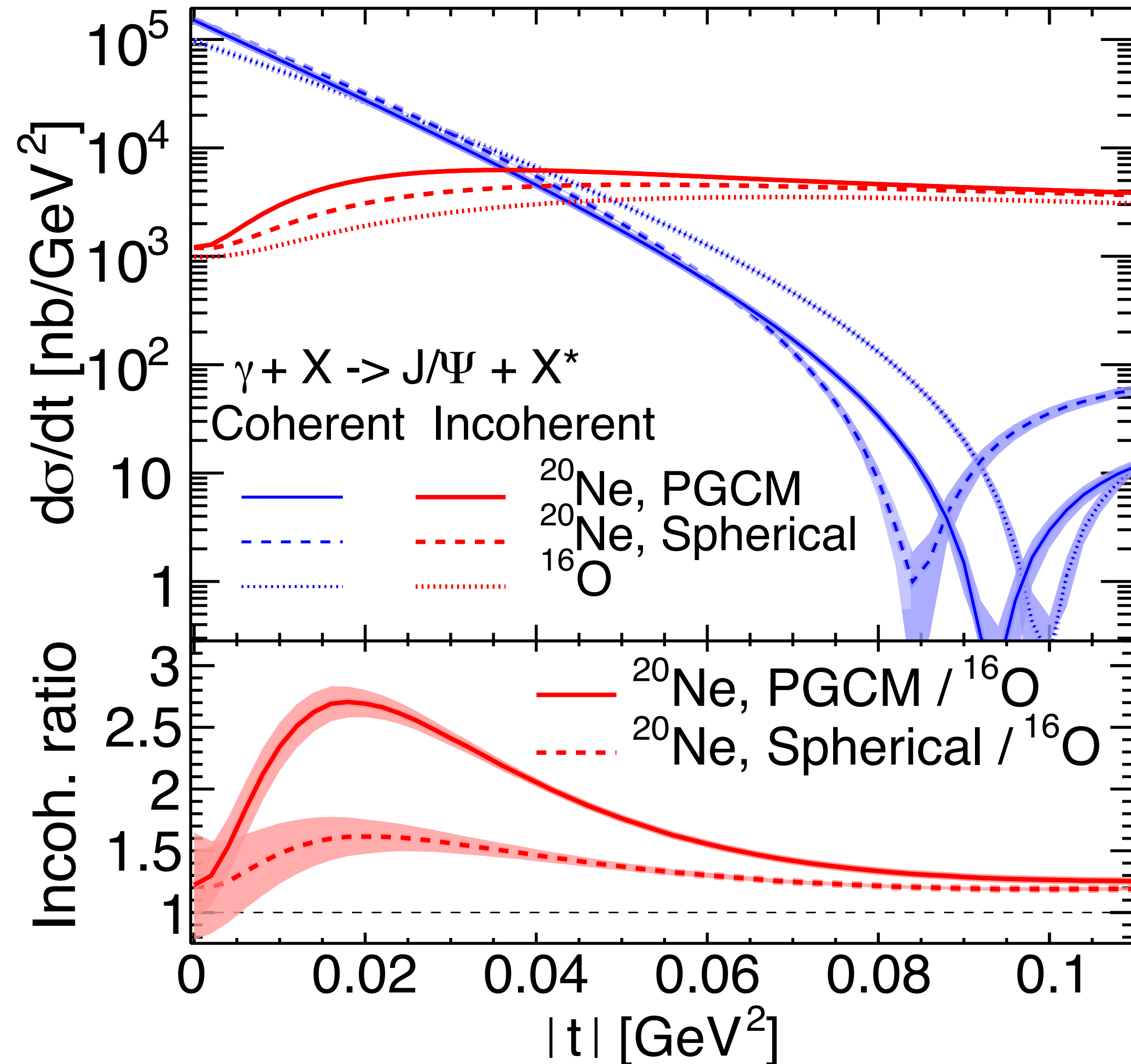
H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, arXiv:2303.04866



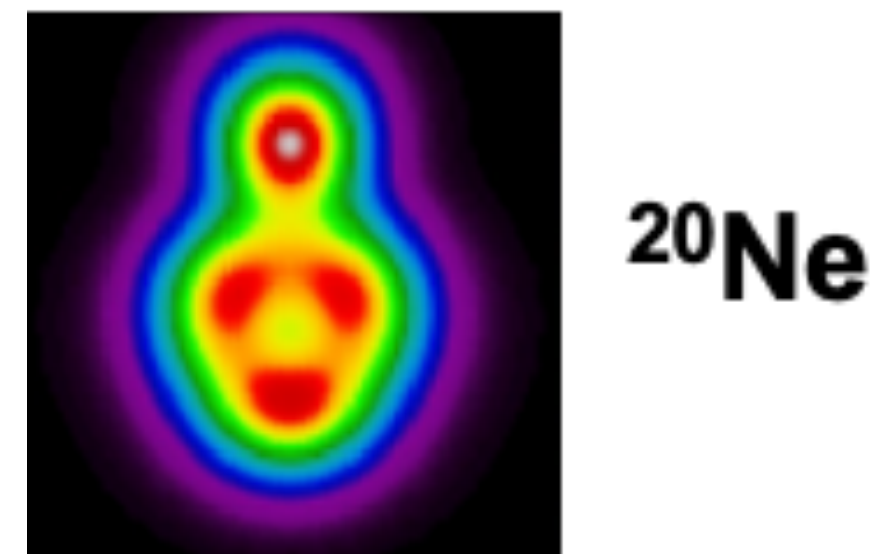
- JIMWLK evolution to smaller x
- Both cross sections increase
- Ratio incoherent/coherent decreases because fluctuations are reduced (nucleus becomes smoother)
- Difference between different β_2 does not decrease noticeably in this x range
- Is there a large enough x range we can cover at the EIC (at least $10^{-3} - 10^{-2}$)?

Neon and Oxygen targets

H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, arXiv:2303.04866



- ²⁰Ne has a bowling pin shape that leads to an increased incoherent cross section relative to an assumed spherical (on average) neon or a spherical oxygen

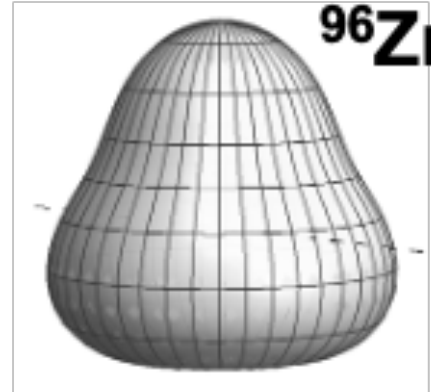


PGCM: Projected Generator Coordinate Method: B. Bally et al., “Deciphering small system collectivity with bowling-pin-shaped ²⁰Ne isotopes,” in preparation (2023); Mikael Frosini, Thomas Duguet, Jean-Paul Ebran, Benjamin Bally, Tobias Mongelli, Tomá’s R. Rodríguez, Robert Roth, and Vittorio Soma, Eur. Phys. J. A 58, 63 (2022)

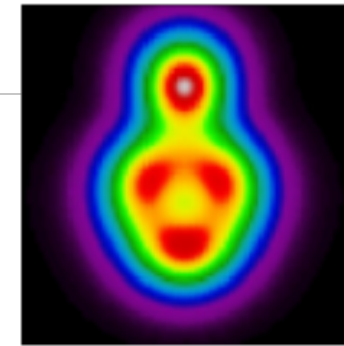
Multi-scale sensitivity

Nuclear deformations

^{238}U



^{96}Zr



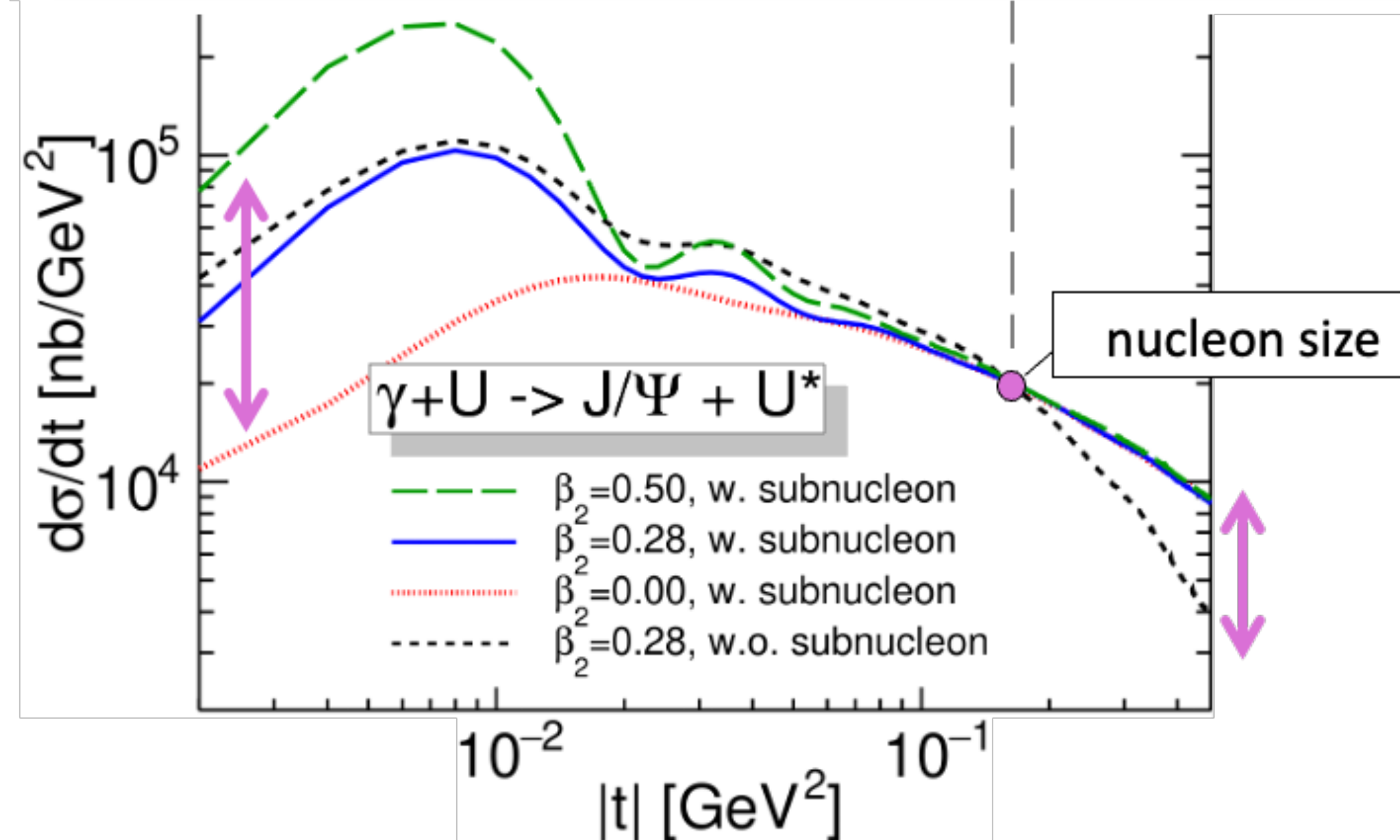
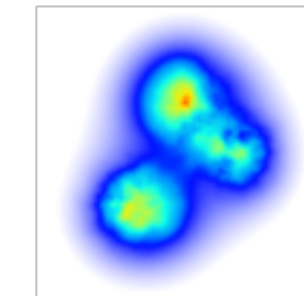
^{20}Ne

Short-range correlations

10 fm

1 fm

0.1 fm



Chiral effective field theory
(low-energy QCD)



CGC effective field theory
(high-energy QCD)

SUMMARY

- $|t|$ -differential incoherent cross section is sensitive to fluctuations at different length scales: Effects of deformation, nucleon-, and sub-nucleon fluctuations
- This means:
 1. Precision comparison of models to data requires taking deformation into account
 2. Access to nuclear structure over 2 orders of magnitude in length scales!
- What we need:
 - Separate incoherent from coherent in forward direction
 - Detect leptons between from mid rapidity to backward rapidity (cover some x -range); or study other vector mesons (like ρ and detect pions)

BACKUP

Good-Walker/Miettinen-Pumplin

M. L. Good and W. D. Walker, Phys. Rev. 120 (1960) 1857
H. I. Miettinen and J. Pumplin, Phys. Rev. D18 (1978) 1696

Discussing mainly diffractive scattering in p+p collisions, Miettinen and Pumplin ask two questions:

1. What are the states which diagonalize the diffractive part of the S-matrix, so that their interactions are described simply by absorption coefficients?

Answer in their paper: States of the parton model (fixed number N , positions \vec{b}_i , fixed x)

2. What causes the large variations in the absorption coefficients at a given impact parameter, which are implied by the large cross section for diffractive production?

Answer in their paper: Fluctuations in N , \vec{b}_i , x between the states. “Among the parton states which describe a high-energy hadron, there are some which are rich in wee partons, and are therefore likely to interact, while other states have few or no wee partons, and correspond to the transparent channels of diffraction.”

Miettinen-Pumplin: Optical Model Formulation

H. I. Miettinen and J. Pumplin, *Phys. Rev. D*18 (1978) 1696

Target: Average optical potential

Beam particle: $|B\rangle = \sum_k C_k |\psi_k\rangle$ (linear combination of the eigenstates of diffraction $|\psi_k\rangle$)

With $\text{Im}T = 1 - \text{Re}S$ the imaginary part of the scattering amplitude operator, we have

$$\text{Im}T |\psi_k\rangle = t_k |\psi_k\rangle$$

with t_k the probability for eigenstate $|\psi_k\rangle$ to interact with the target (absorption coefficients)

$$\text{Normalize: } \langle B | B \rangle = \sum_k |C_k|^2 = 1$$

$$\text{Elastic scattering: } \langle B | \text{Im}T | B \rangle = \sum_k |C_k|^2 t_k = \langle t \rangle$$

Miettinen-Pumplin: Cross Sections

H. I. Miettinen and J. Pumplin, Phys. Rev. D18 (1978) 1696

Total cross section:

$$d\sigma_{\text{tot}}/d^2\vec{b} = 2\langle t \rangle$$

Elastic cross section:

$$d\sigma_{\text{el}}/d^2\vec{b} = \langle t \rangle^2$$

Incoherent diffractive cross section:

$$\begin{aligned} d\sigma_{\text{diff}}/d^2\vec{b} &= \sum_k |\langle \psi_k | \text{Im}T | B \rangle|^2 - d\sigma_{\text{el}}/d^2\vec{b} = \sum_k |\langle \psi_k | \text{Im}T | \sum_i C_i |\psi_i\rangle|^2 - d\sigma_{\text{el}}/d^2\vec{b} \\ &= \sum_{k,i} |\langle \psi_k | C_i t_i | \psi_i \rangle|^2 - d\sigma_{\text{el}}/d^2\vec{b} = \sum_{k,i} \delta_{ik} |C_i t_i|^2 - d\sigma_{\text{el}}/d^2\vec{b} = \sum_k |C_k|^2 t_k^2 - \langle t \rangle^2 = \langle t^2 \rangle - \langle t \rangle^2 \end{aligned}$$

$$d\sigma_{\text{diff}}/d^2\vec{b} = \langle t^2 \rangle - \langle t \rangle^2$$

Color Glass Condensate calculation

- We study diffractive production in e+p/A (not p+p)
- The projectile can be understood as a quark anti-quark dipole (splitting from the incoming virtual photon)
- The fluctuations are included in the target wave function: Fluctuating spatial distribution of the gluon fields (normalization fluctuations correspond to N fluctuations, spatial fluctuations to \vec{b}_i fluctuations)
(see [Blaizot and Traini, 2209.15545 \[hep-ph\]](#) for the effect of fluctuations of the dipole size)

Fluctuations in the target

Define

$$\hat{T}_p(\vec{b}) = \sum_i^{N_q} T_G(\vec{b}_i - \vec{b}) = \int d^2\vec{x} \hat{\rho}(\vec{x}) T_G(\vec{x} - \vec{b}) \quad T_G \text{ is the gluon distribution in a hot spot}$$

$$\hat{\rho}(\vec{x}) = \sum_i^{N_q} \delta(\vec{x} - \vec{b}_i) \text{ is the hot spot density operator in the transverse plane}$$

The dipole cross section can be written as

$$N = \exp \left[-\frac{1}{2} \sigma_{\text{dip}}(x, \vec{r}) \hat{T}_p(\vec{b}) \right] \approx 1 - \frac{1}{2} \sigma_{\text{dip}}(x, \vec{r}) \hat{T}_p(\vec{b}) \text{ in the weak field limit}$$

$$\text{The dipole cross section then is } \frac{d\sigma_{q\bar{q}}}{d^2\vec{b}} = 2[1 - N] = \sigma_{\text{dip}}(x, \vec{r}) \hat{T}_p(\vec{b})$$

Fluctuations in the target

The dipole cross section then is $\frac{d\sigma_{q\bar{q}}}{d^2\vec{b}} = 2[1 - N] = \sigma_{\text{dip}}(x, \vec{r})\hat{T}_p(\vec{b})$

This operator is diagonal in the basis of states $|\vec{b}_1, \dots, \vec{b}_{N_q}\rangle$, where the \vec{b}_i are the positions of the individual hot spots, frozen during the collision process:

These states can be considered the diffractive eigenstates

Coherent diffractive cross section:

$$\int d^2\vec{b}d^2\vec{b}'e^{-i\vec{\Delta}\cdot(\vec{b}-\vec{b}')} \left\langle \frac{d\sigma^{q\bar{q}}}{d^2\vec{b}} \right\rangle \left\langle \frac{d\sigma^{q\bar{q}}}{d^2\vec{b}'} \right\rangle = \langle \Sigma_{q\bar{q}}(\vec{\Delta}) \rangle^2$$

with $\Sigma_{q\bar{q}}(\vec{\Delta}) = \int d^2\vec{b}e^{-i\vec{\Delta}\cdot\vec{b}}\frac{d\sigma^{q\bar{q}}}{d^2\vec{b}}$ and $\langle \cdot \rangle$ is the average over the ground state wave function

Fluctuations in the target

Total diffractive cross section:

Allow all possible diffractive eigenstates $|\alpha\rangle$ as intermediate states (assume dilute limit here)

$$\int d^2\vec{b} d^2\vec{b}' e^{-i\vec{\Delta}\cdot(\vec{b}-\vec{b}')} \sigma_{\text{dip}}^2 \sum_{\alpha} \left| \langle \alpha | \hat{T}_p(\vec{b}) | \psi_0 \rangle \right|^2 = \langle \Sigma_{q\bar{q}}^2(\vec{\Delta}) \rangle$$

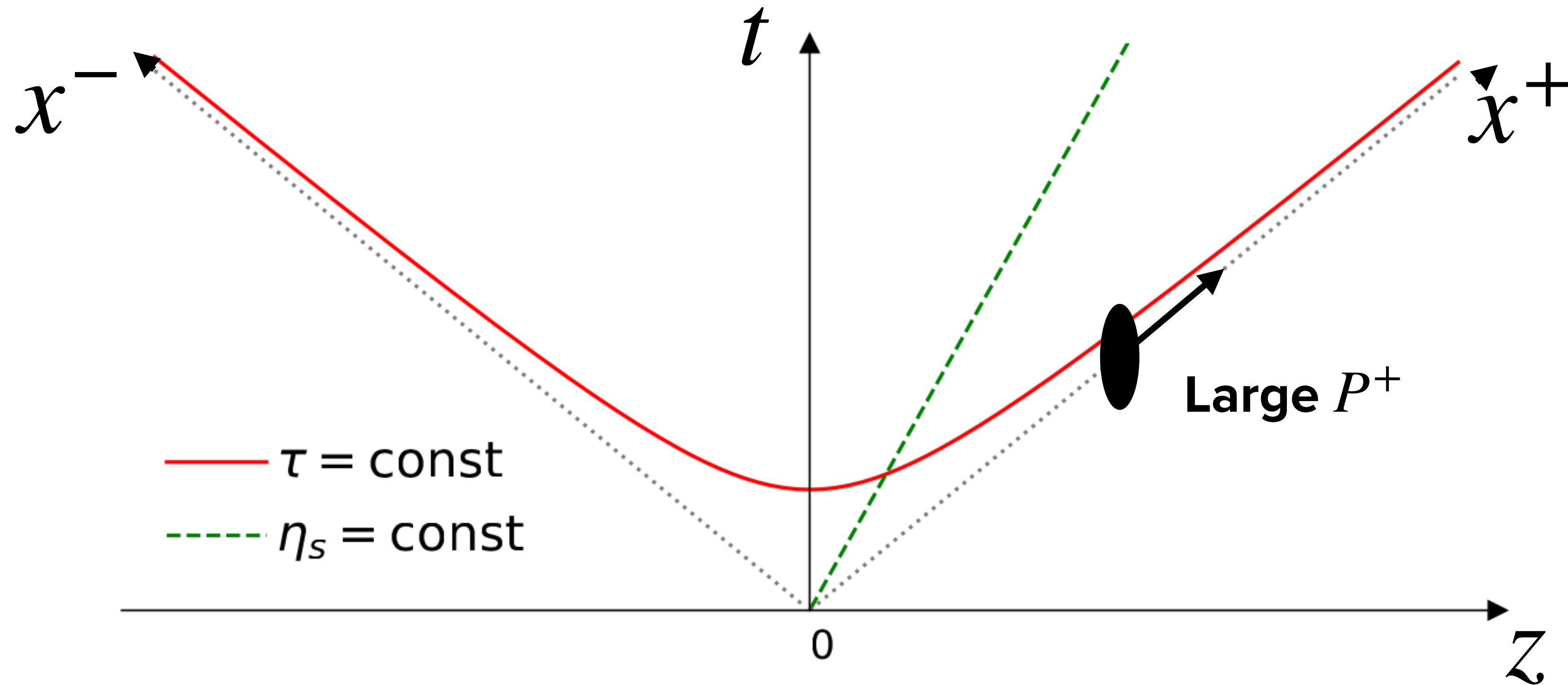
in analogy to the optical model example

This also shows the relation to the density-density correlation function $\langle \hat{T}_p(\vec{b}) \hat{T}_p(\vec{b}') \rangle$

and how we are sensitive to different distance scales via $\vec{b} - \vec{b}'$

See [Blaizot and Traini, 2209.15545 \[hep-ph\]](#) for a more detailed discussion

The scenario: Hadron moving at high momentum



Probe hadron (or nucleus) moving with large P^+ at scale $x_0 P^+$ with $x_0 \ll 1$

Separate partonic content based on longitudinal momentum $k^+ = x P^+$

Large $x > x_0$: Static and localized color sources ρ

Dynamic color fields

The moving color sources generate a current, independent of light cone time z^+ :

$$J^{\mu,a}(z) = \delta^{\mu+} \rho^a(z^-, z_T) \quad a \text{ is the color index of the gluon}$$

This current generates delocalized dynamical fields $A^{\mu,a}(z)$ described by the Yang-Mills equations

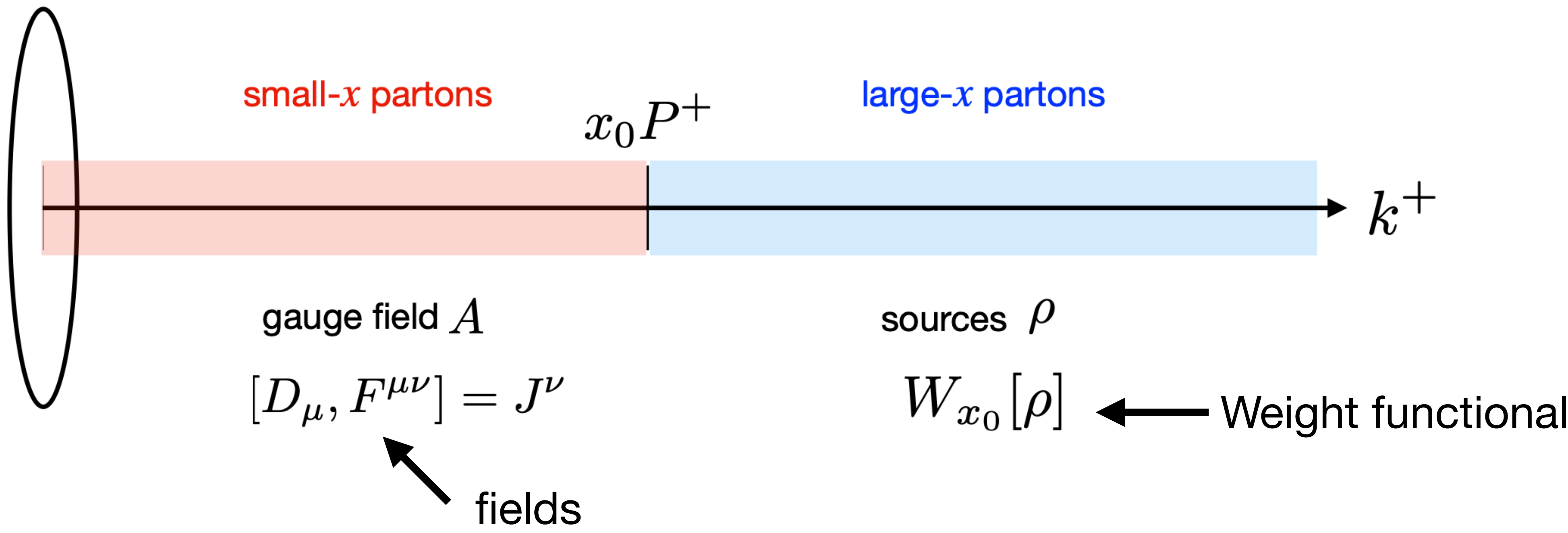
$$[D_\mu, F^{\mu\nu}] = J^\nu$$

with $D_\mu = \partial_\mu + igA_\mu$ and $F_{\mu\nu} = \frac{1}{ig}[D_\mu, D_\nu] = \partial_\mu A_\nu - \partial_\nu A_\mu + ig[A_\mu, A_\nu]$

These fields A are the small $x < x_0$ degrees of freedom

They can be treated classically, because their occupation number is large $\langle AA \rangle \sim 1/\alpha_s$

Color Glass Condensate (CGC): Sources and fields



When $x \lesssim x_0$ the path integral $\langle \mathcal{O} \rangle_\rho$ is dominated by classical solution and we are done

For smaller x we need to do quantum evolution

Wilson lines

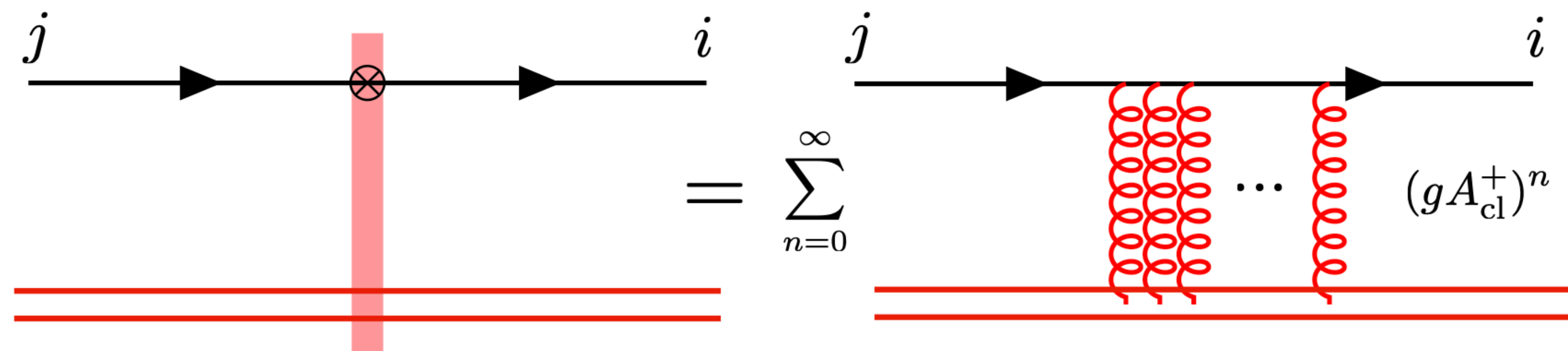
Interaction of high energy color-charged probe with large k^- momentum (and small $k^+ = \frac{k_T^2}{2k^-}$)

with the classical field of a nucleus can be described in the **eikonal approximation**:

The scattering rotates the color, but keeps k^- , transverse position \vec{x}_T , and any other quantum numbers the same.

The color rotation is encoded in a light-like Wilson line, which for a quark probe reads

$$V_{ij}(\vec{x}_T) = \mathcal{P} \left(ig \int_{-\infty}^{\infty} A^{+,c}(z^-, \vec{x}_T) t_{ij}^c dz^- \right)$$



MULTIPLE INTERACTIONS NEED TO BE RESUMMED, BECAUSE $A^+ \sim 1/g$

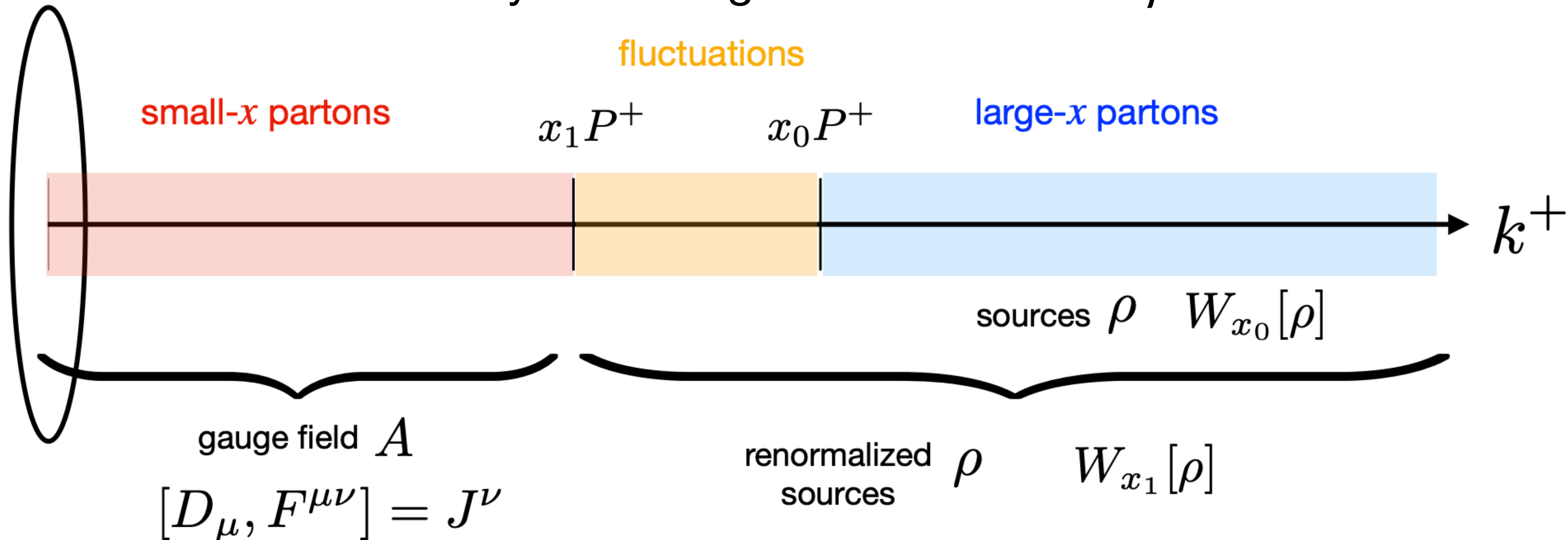
JIMWLK evolution

Jalilian-Marian, J.; Kovner, A.; McLerran, L.D.; Weigert, H., Phys. Rev. D 1997, 55, 5414–5428, [hep-ph/9606337]
 Jalilian-Marian, J.; Kovner, A.; Weigert, H., Phys. Rev. D 1998, 59, 014015, [hep-ph/9709432]
 Kovner, A.; Milhano, J.G.; Weigert, H., Phys. Rev. D 2000, 62, 114005, [hep-ph/0004014]
 Iancu, E.; Leonidov, A.; McLerran, L.D., Nucl. Phys. A 2001, 692, 583–645, [hep-ph/0011241]
 Iancu, E.; Leonidov, A.; McLerran, L.D., Phys. Lett. B 2001, 510, 133–144, [hep-ph/0102009]
 Ferreiro, E.; Iancu, E.; Leonidov, A.; McLerran, L., Nucl. Phys. A 2002, 703, 489–538, [hep-ph/0109115]

LO Small- x evolution resums logarithmically enhanced terms $\sim \alpha_s \ln(x_0/x)$

$$\frac{dW_x[\rho]}{d \ln(1/x)} = - \mathcal{H}_{\text{JIMWLK}} W_x[\rho]$$

Physically, one absorbs the quantum fluctuations in the interval $[x_0 - dx, x_0]$ into stochastic fluctuations of the color sources by redefining the color sources ρ



JIMWLK evolution

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Evolution is done using the Langevin formulation of the JIMWLK equations on the level of Wilson lines

K. Rummukainen and H. Weigert Nucl. Phys. A739 (2004) 183; T. Lappi, H. Mäntysaari, Eur. Phys. J. C73 (2013) 2307

Long distance tails are tamed by imposing a regulator in the JIMWLK kernel, m

S. Schlichting, B. Schenke, Phys.Lett. B739 (2014) 313-319

Connection between the initial state of heavy ion collisions and the EIC

- These Wilson lines are the building blocks of the CGC
- In heavy ion collisions, one can compute the initial state by determining Wilson lines after the collision from the Wilson lines of the colliding nuclei
- At the EIC (and HERA, and in UPCs), cross sections will be calculated as convolutions of Wilson line correlators with perturbatively calculable and process-dependent impact factors
- This allows the computation of rather direct constraints for the initial state of heavy ion collisions from electron-nucleus (γ -nucleus) or electron-proton collisions

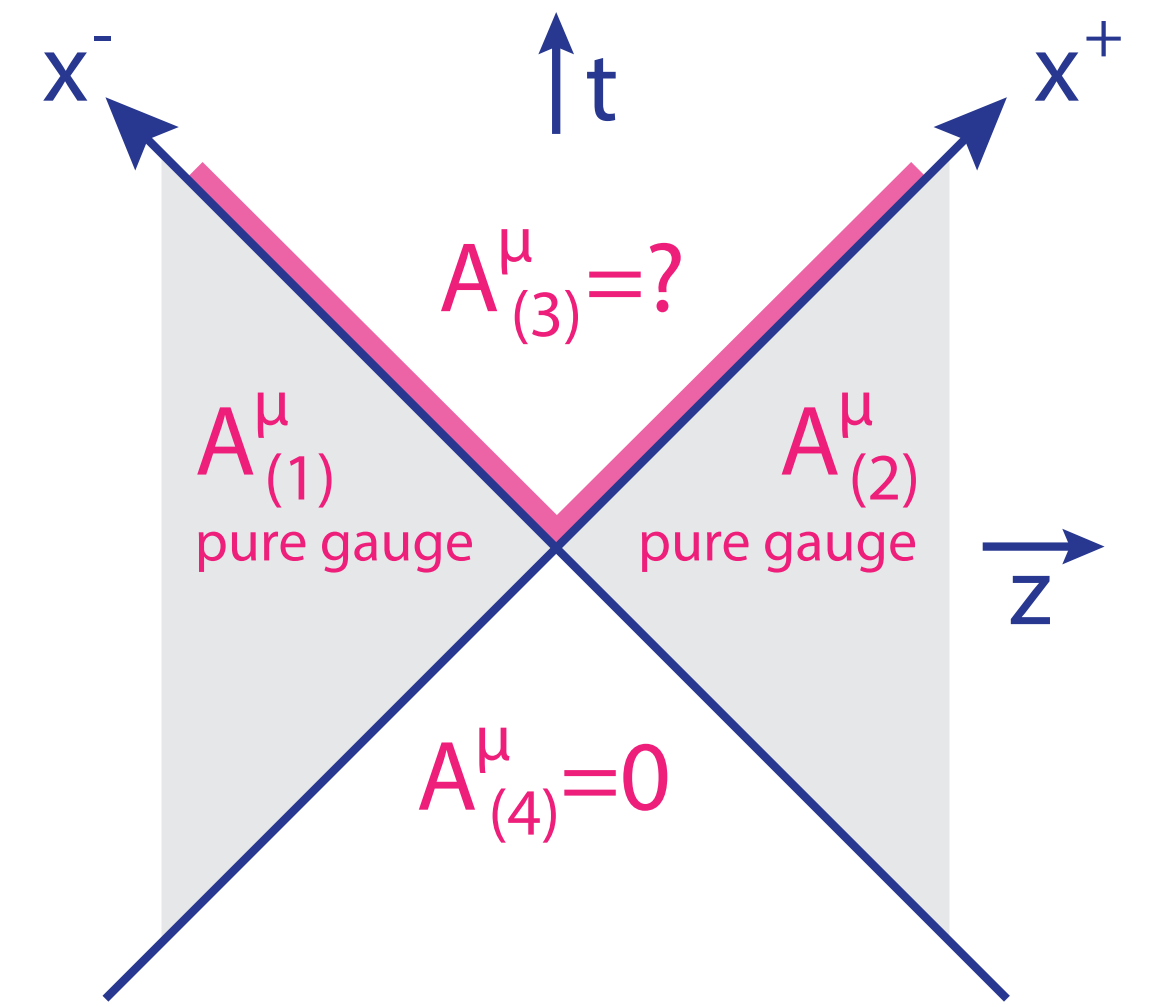
Heavy ion collision

Compute gluon fields after the collision using light cone gauge:

$A^+ = 0$ for a right moving nucleus, $A^- = 0$ for a left moving nucleus

gauge transformation: $A_\mu(x) \rightarrow V(x) \left(A_\mu(x) - \frac{i}{g} \partial_\mu \right) V^\dagger(x)$

using our Wilson lines $V^\dagger(x^-, \mathbf{x}_\perp) = \mathcal{P} \exp \left(-ig \int_{-\infty}^{x^-} dz^- A^+(z^-, \mathbf{x}_\perp) \right)$ (for the right moving nucleus)



Then, the gauge fields read (choosing $A^\mu = 0$ for the quadrant for $x^- < 0$ and $x^+ < 0$)

$$A^i(x) = \theta(x^+) \theta(x^-) \alpha^i(\tau, \mathbf{x}_\perp) + \theta(x^-) \theta(-x^+) \alpha_P^i(\mathbf{x}_\perp) + \theta(x^+) \theta(-x^-) \alpha_T^i(\mathbf{x}_\perp)$$

$$A^\eta(x) = \theta(x^+) \theta(x^-) \alpha^\eta(\tau, \mathbf{x}_\perp) \quad \text{with } \alpha_P^i(\mathbf{x}_\perp) = \frac{1}{ig} V_P(\mathbf{x}_\perp) \partial^i V_P^\dagger(\mathbf{x}_\perp) \text{ and } \alpha_T^i(\mathbf{x}_\perp) = \frac{1}{ig} V_T(\mathbf{x}_\perp) \partial^i V_T^\dagger(\mathbf{x}_\perp)$$

$A^\tau = 0$, because we chose Fock-Schwinger gauge $x^+ A^- + x^- A^+ = 0$

Heavy ion collision

Plugging this ansatz

$$A^i(x) = \theta(x^+)\theta(x^-)\alpha^i(\tau, \mathbf{x}_\perp) + \theta(x^-)\theta(-x^+)\alpha_P^i(\mathbf{x}_\perp) + \theta(x^+)\theta(-x^-)\alpha_T^i(\mathbf{x}_\perp)$$

$$A^\eta(x) = \theta(x^+)\theta(x^-)\alpha^\eta(\tau, \mathbf{x}_\perp)$$

into YM equations leads to singular terms on the boundary from derivatives of θ -functions

Requiring that the singularities vanish leads to the solutions

$$\alpha^i = \alpha_P^i + \alpha_T^i \quad \alpha^\eta = -\frac{ig}{2} \left[\alpha_{Pj}, \alpha_T^j \right] \quad \begin{aligned} \partial_\tau \alpha^i &= 0 \\ \partial_\tau \alpha^\eta &= 0 \end{aligned}$$

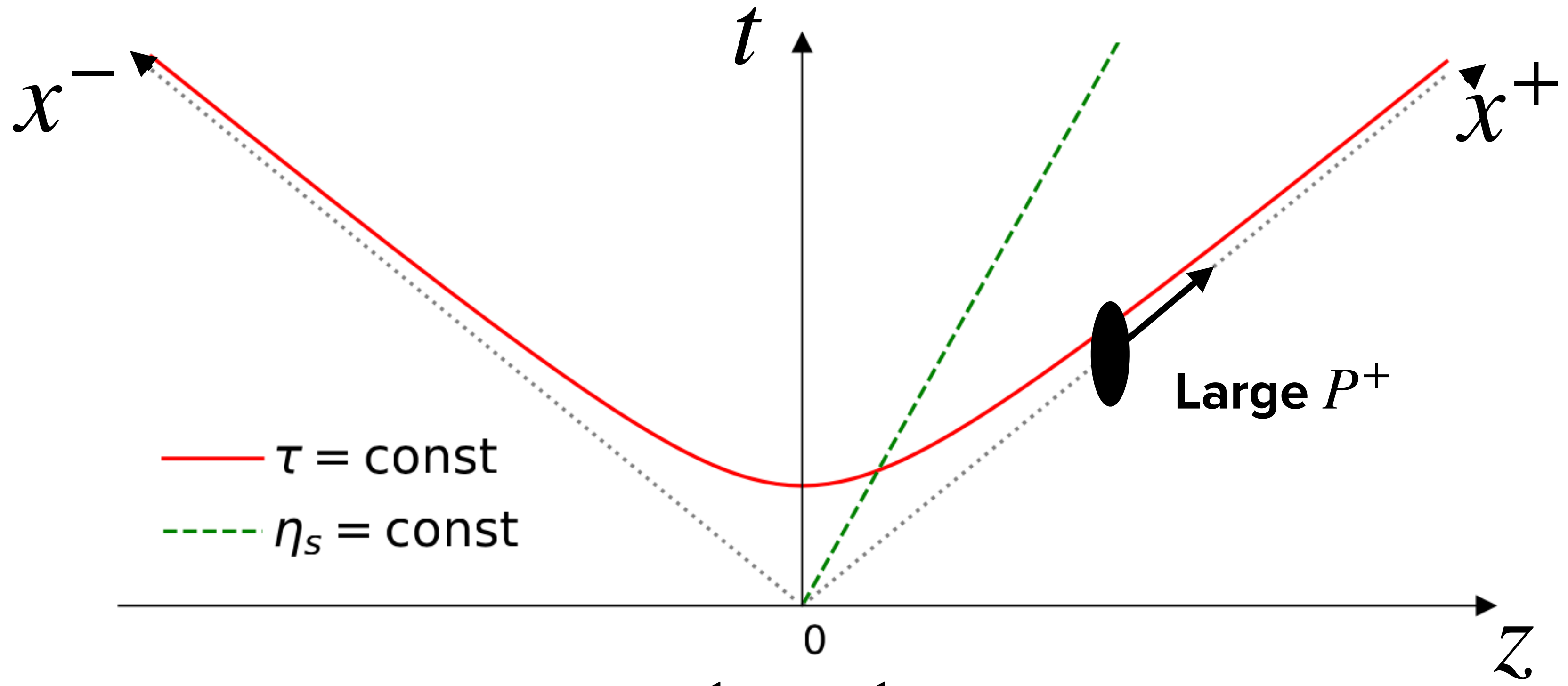
These are the gauge fields in the forward light cone.

We can compute $T^{\mu\nu}$ from it, providing an initial condition for hydrodynamics.

Geometry, fluctuations, ...

- All the information on geometry and nucleon and sub-nucleon fluctuations is contained in the distribution of color charges $\rho_{P/T}^a(x^\mp, \mathbf{x}_\perp)$
- Typically, use the MV model, which gives
$$\langle \rho^a(\mathbf{b}_\perp) \rho^b(\mathbf{x}_\perp) \rangle = g^2 \mu^2(x, \mathbf{b}_\perp) \delta^{ab} \delta^{(2)}(\mathbf{b}_\perp - \mathbf{x}_\perp)$$
- The color charge distribution $g^2 \mu(x, \mathbf{b}_\perp)$ depends on the longitudinal momentum fraction x and the transverse position \mathbf{b}_\perp . The latter needs to be modeled, the former can be modeled or obtained from e.g. JIMWLK evolution
- We factorize $\mu(x, \mathbf{b}_\perp) \sim T(\mathbf{b}_\perp) \mu(x)$ and constrain the impact parameter \mathbf{b}_\perp dependence using input from a process sensitive to geometry, such as diffractive VM production
- The cross section for that process can be expressed with the Wilson lines of the target
The same quantities we have used to initialize the heavy ion collision

Color sources

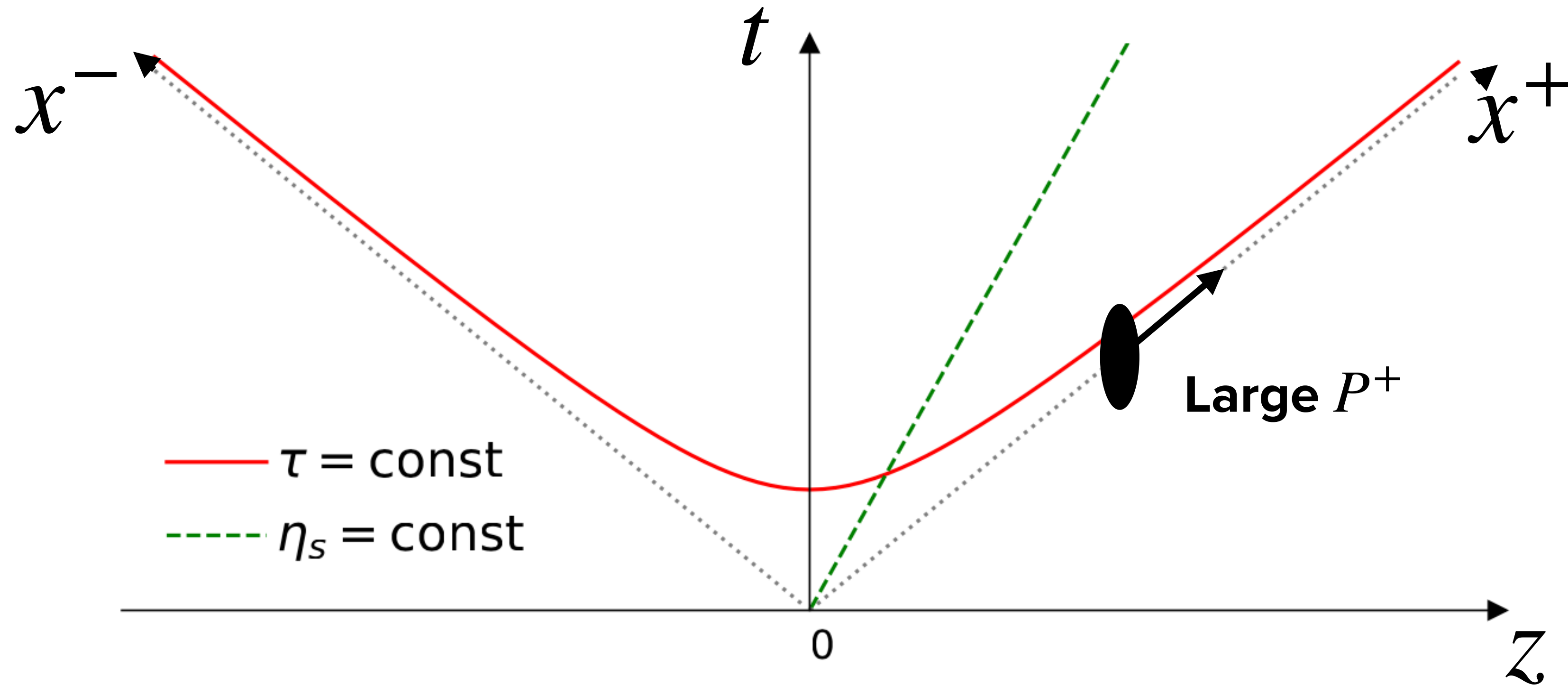


How localized are these sources? $\Delta z^- \sim \frac{1}{k^+} = \frac{1}{xP^+}$

What is the resolution scale of the probe? $\frac{1}{x_0P^+} > \frac{1}{xP^+}$ for $x > x_0$

→ Color sources look fully localized to the probe in z^-

Color sources



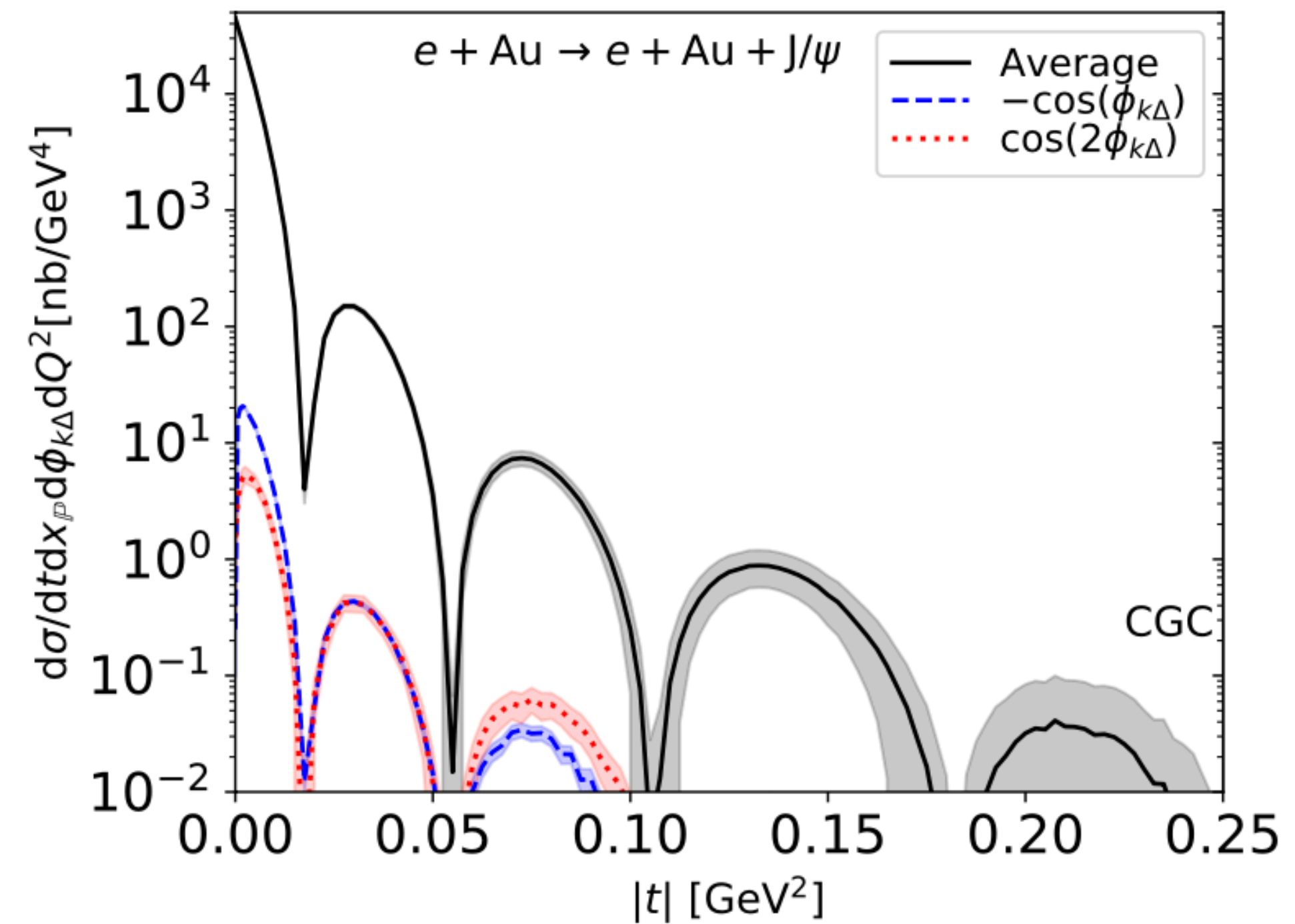
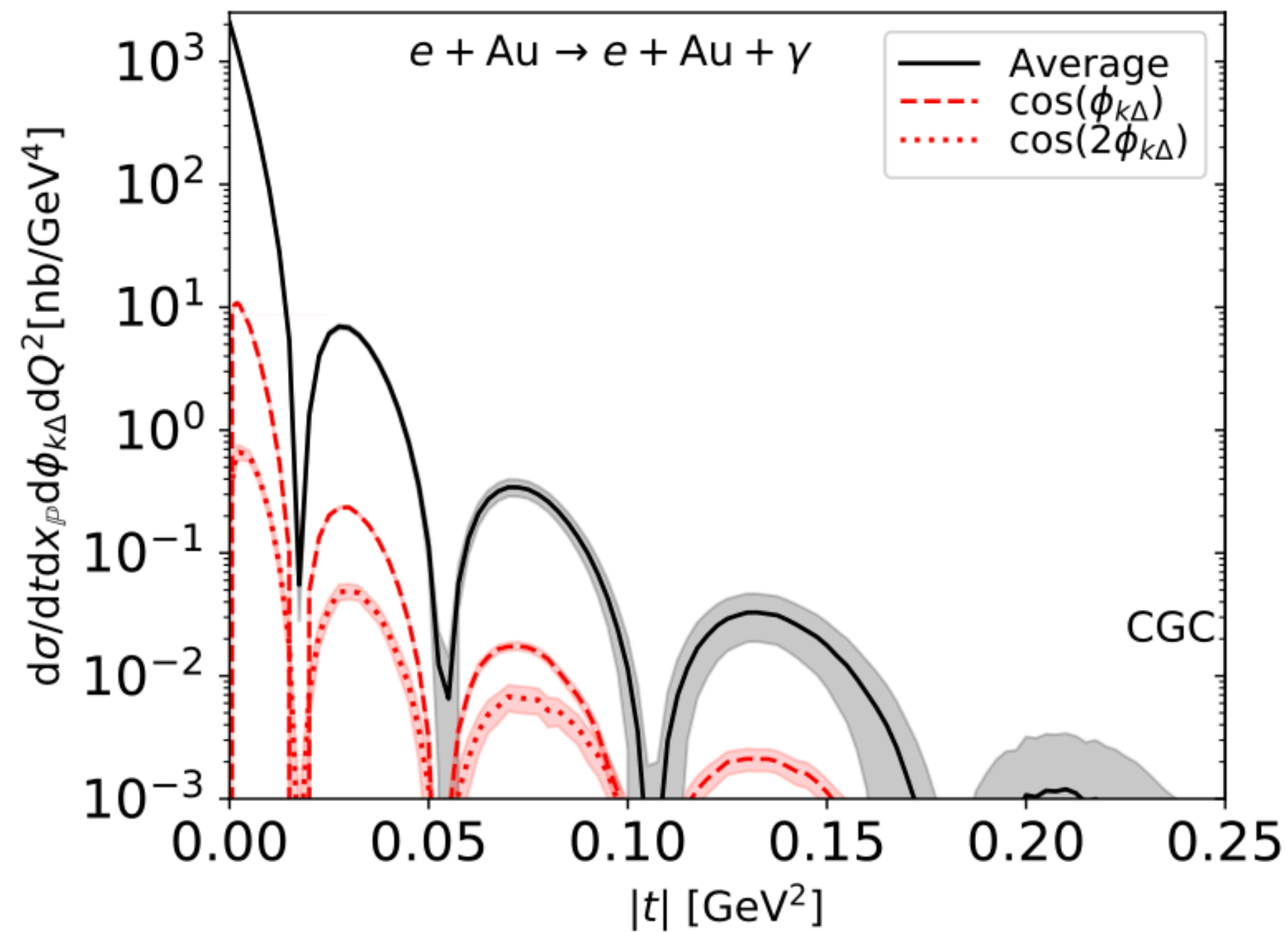
How fast do they evolve? $\Delta z^+ \sim \frac{1}{k^-} = \frac{2k^+}{k_T^2} = \frac{2xP^+}{k_T^2}$ (because $a_\mu b^\mu = a^+ b^- + a^- b^+ - \vec{a}_T \cdot \vec{b}_T$)

What is the time scale of the probe? $\tau \approx \frac{2x_0 P^+}{k_T^2} < \frac{2xP^+}{k_T^2}$

→ **Color sources look static to the probe in light cone time z^+**

Predictions for e-Au at the future EIC

DVCS and exclusive J/ψ : Spectra and azimuthal modulations

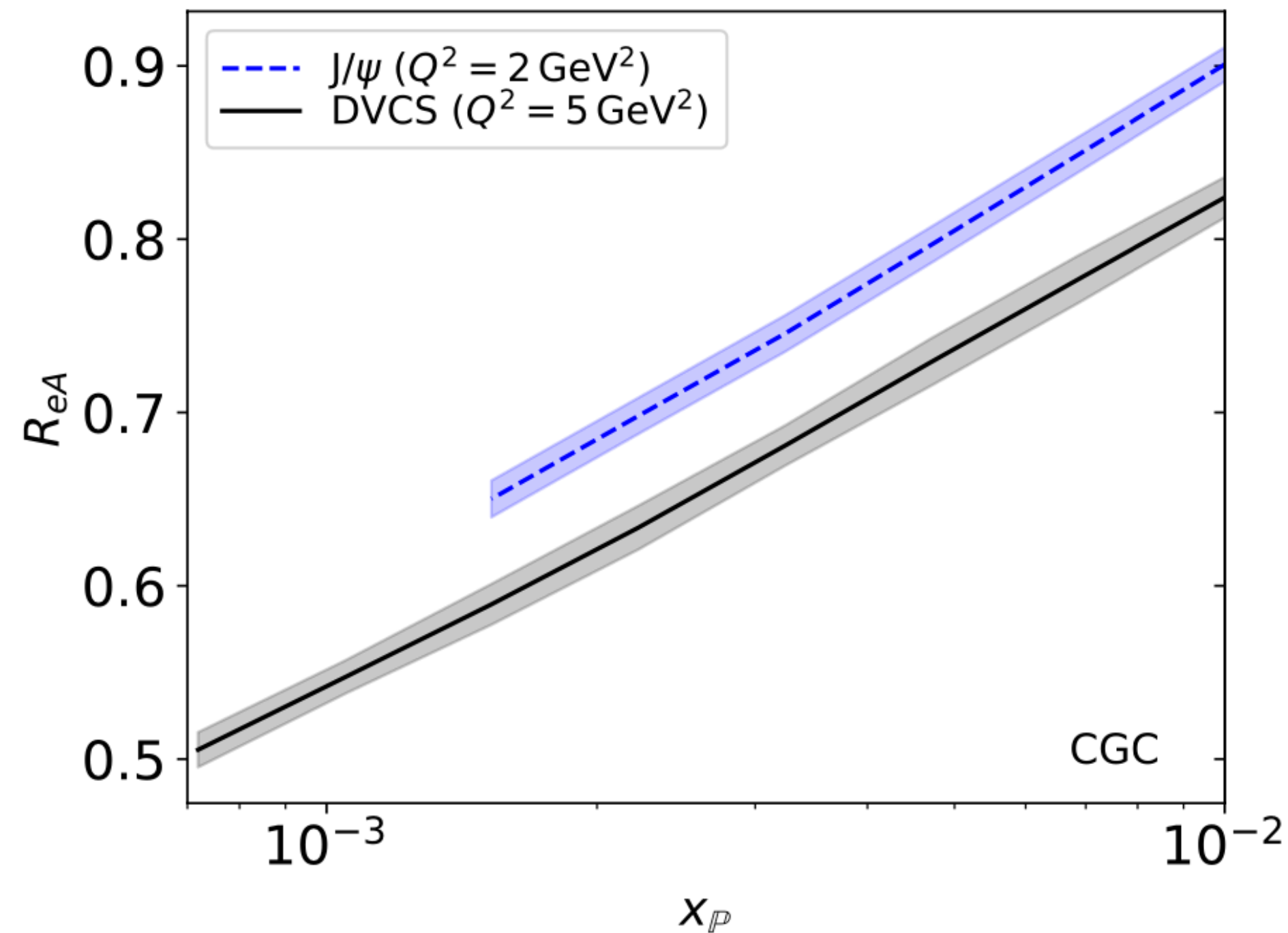


Characteristic dips in spectra due to Woods-Saxon nuclear profile

Azimuthal modulations v_n a few percent for DVCS, and less than 1% for J/ψ

Predictions for e-Au at the future EIC

Nuclear suppressions factor for DVCS and exclusive J/ψ



$$R_{eA} = \frac{d\sigma^{e+A \rightarrow e+A+V} / dt dQ^2 dx_{\mathbb{P}}}{A^2 d\sigma^{e+p \rightarrow e+p+V} / dt dQ^2 dx_{\mathbb{P}}} \Big|_{t=0}$$

Expect $R_{eA} = 1$ in the dilute limit.

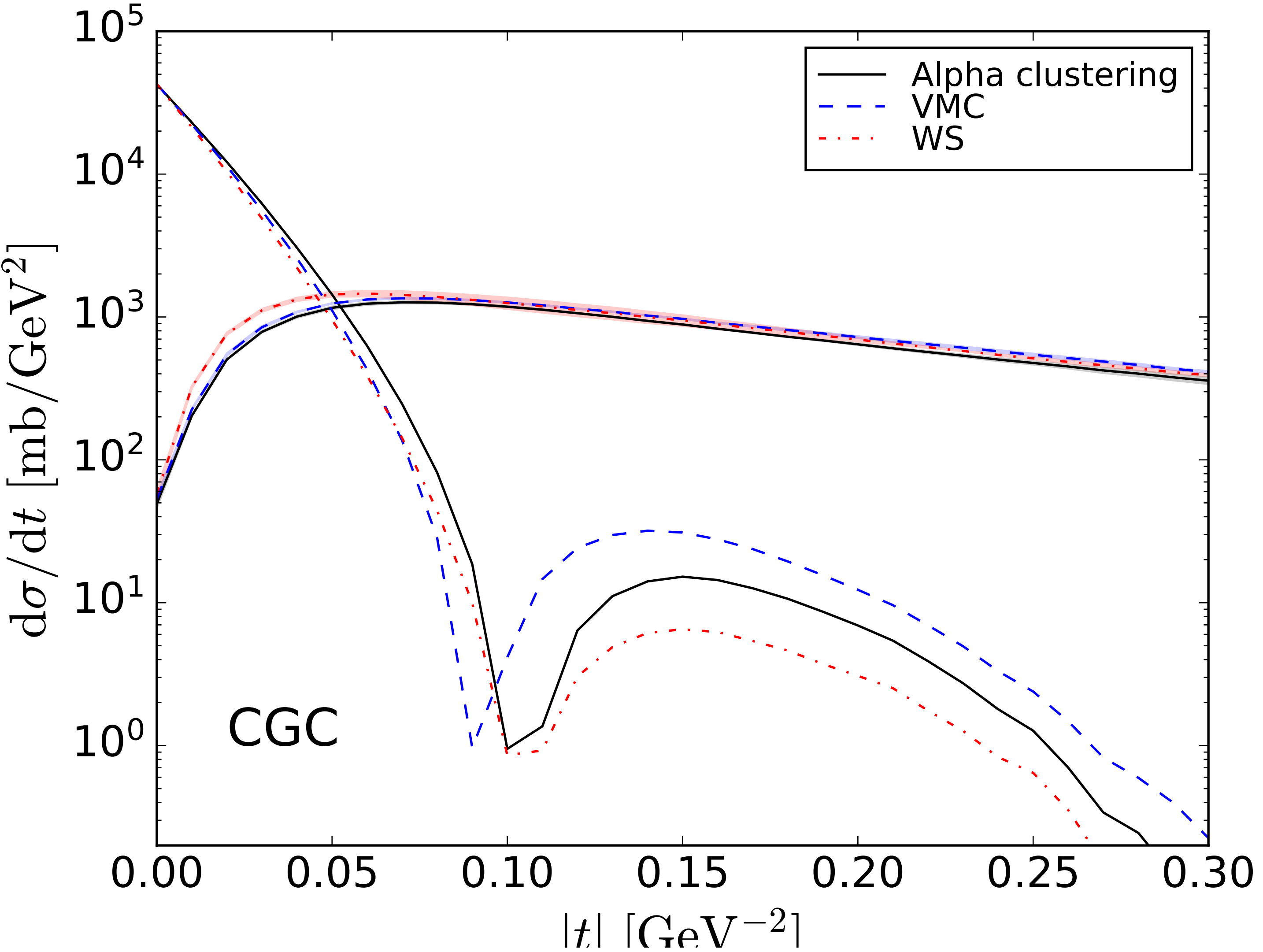
Mäntysaari, Venugopalan. [1712.02508](#)

Significant suppression that evolves with energy / $x_{\mathbb{P}}$

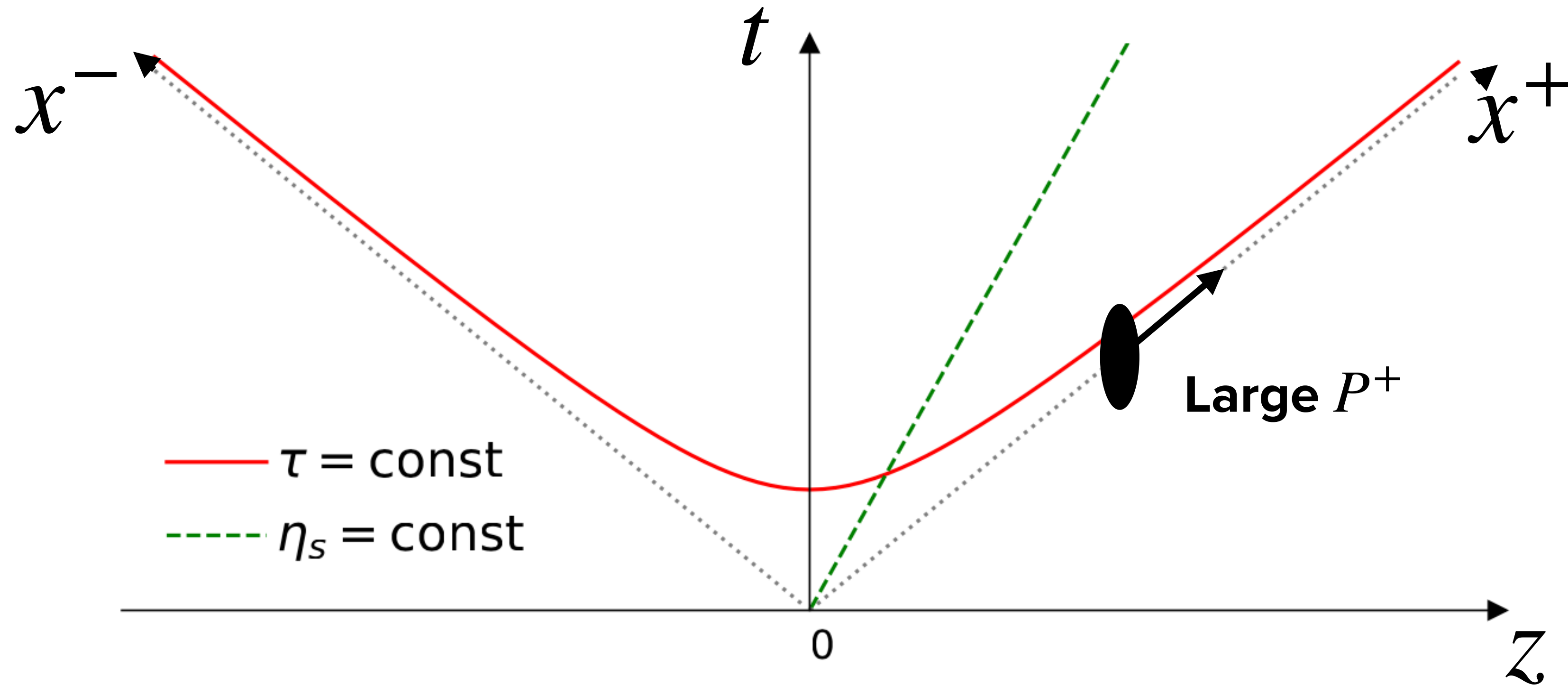
Larger suppression for DVCS due to larger dipole contributions.

e+O: Oxygen wave function dependence

oxygen



Light cone

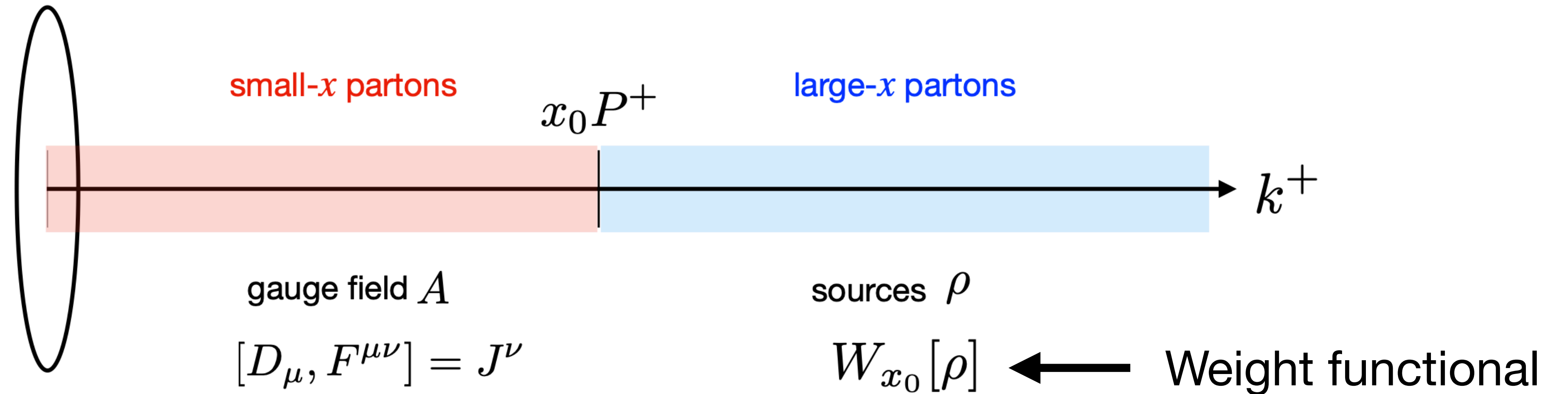


Light cone coordinates $v^\pm = (v^0 \pm v^3)/\sqrt{2}$

In the future light cone define $x^+ = \frac{\tau}{\sqrt{2}}e^{+\eta}$, and $x^- = \frac{\tau}{\sqrt{2}}e^{-\eta}$

or inverted $\tau = \sqrt{2x^+x^-}$, and $\eta = \frac{1}{2} \ln \left(\frac{x^+}{x^-} \right)$

Weight functional



What is the weight functional?

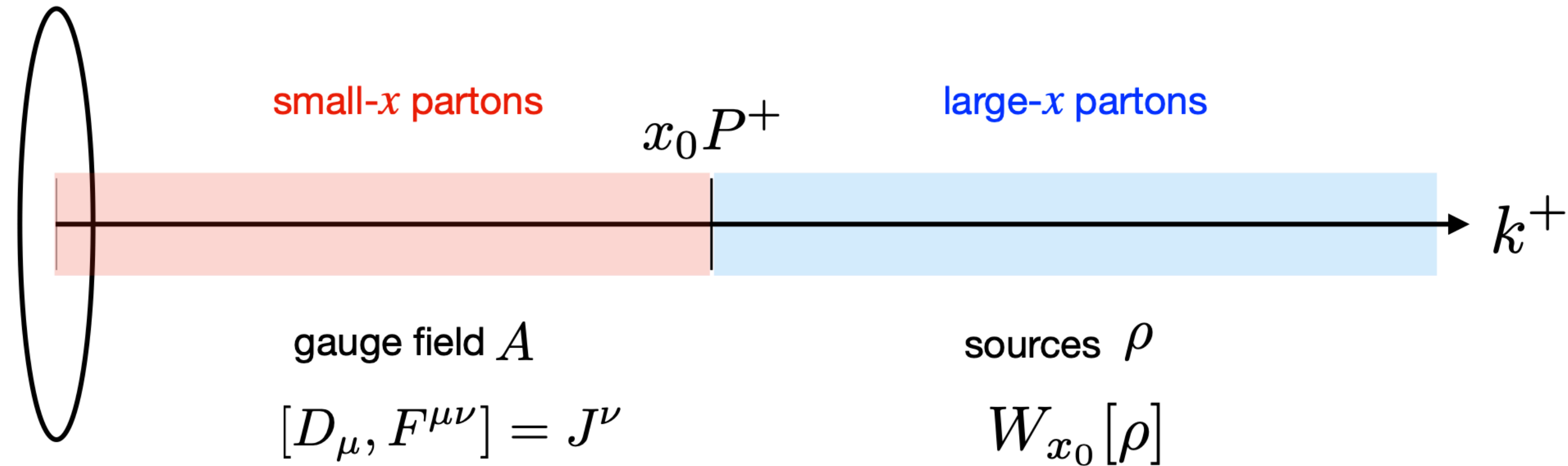
Need to model. E.g. the McLerran-Venugopalan model:

Assume a large nucleus, invoke central limit theorem. All correlations of ρ^a are Gaussian

$$W_{x_0}[\rho] = \mathcal{N} \exp \left(-\frac{1}{2} \int dx^- d^2x_T \frac{\rho^a(x^-, x_T) \rho^a(x^-, x_T)}{\lambda_{x_0}(x^-)} \right)$$

where $\lambda_{x_0}(x^-)$ is related to the transverse color charge density distribution of the nucleus

Weight functional



...where $\lambda_{x_0}(x^-)$ is related to the transverse color charge density distribution of the nucleus

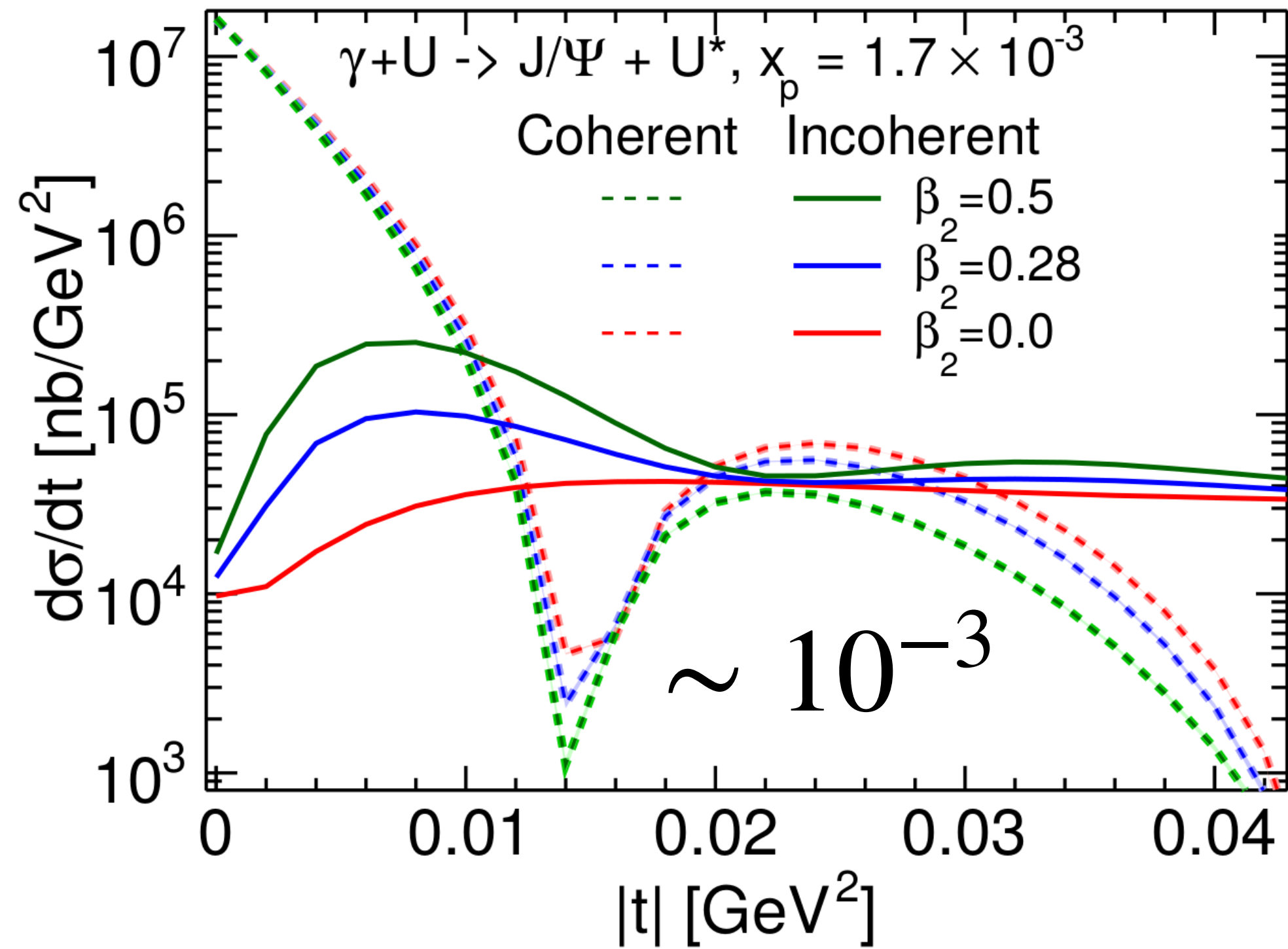
$$\mu^2 = \int dx^- \lambda_{x_0}(x^-) = \frac{(g^2 C_F)(A N_c)}{\pi R_A^2} \frac{1}{N_c^2 - 1} = \frac{g^2 A}{2\pi R_A^2} \sim A^{1/3}$$

That color charge density is related to Q_s , the saturation scale.

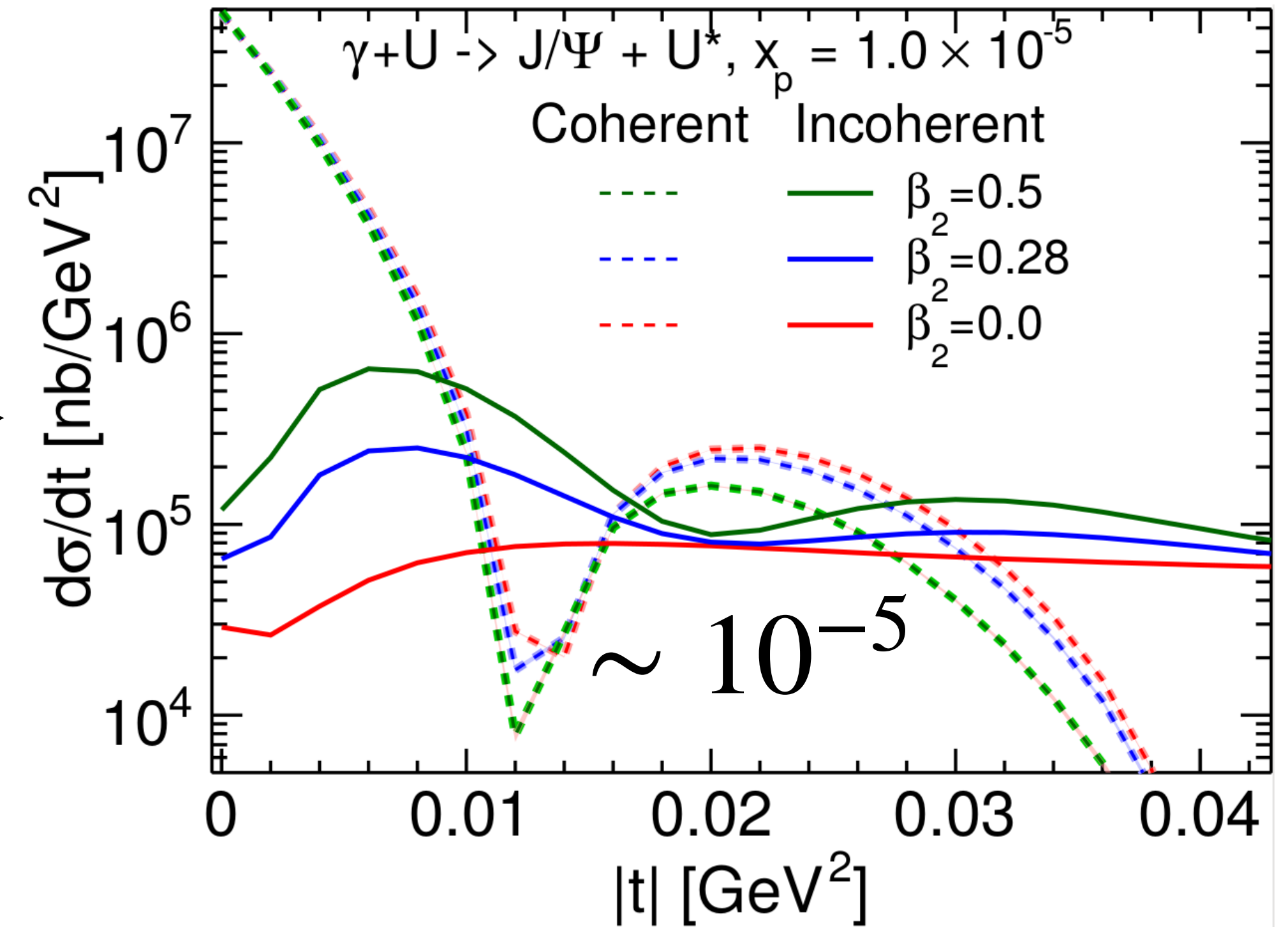
normalized per color degree of freedom

Towards smaller x : Do deformation effects survive?

H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, in progress



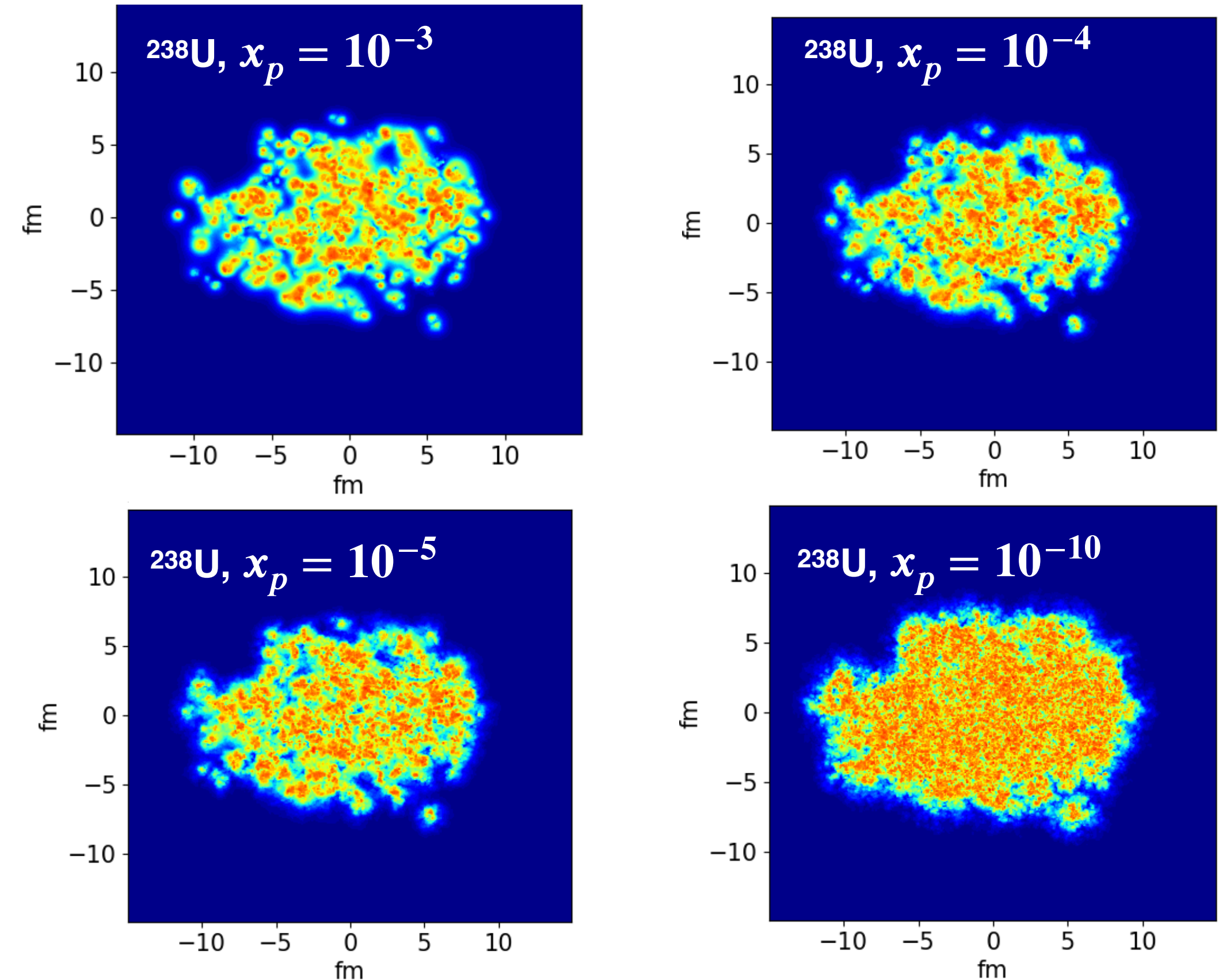
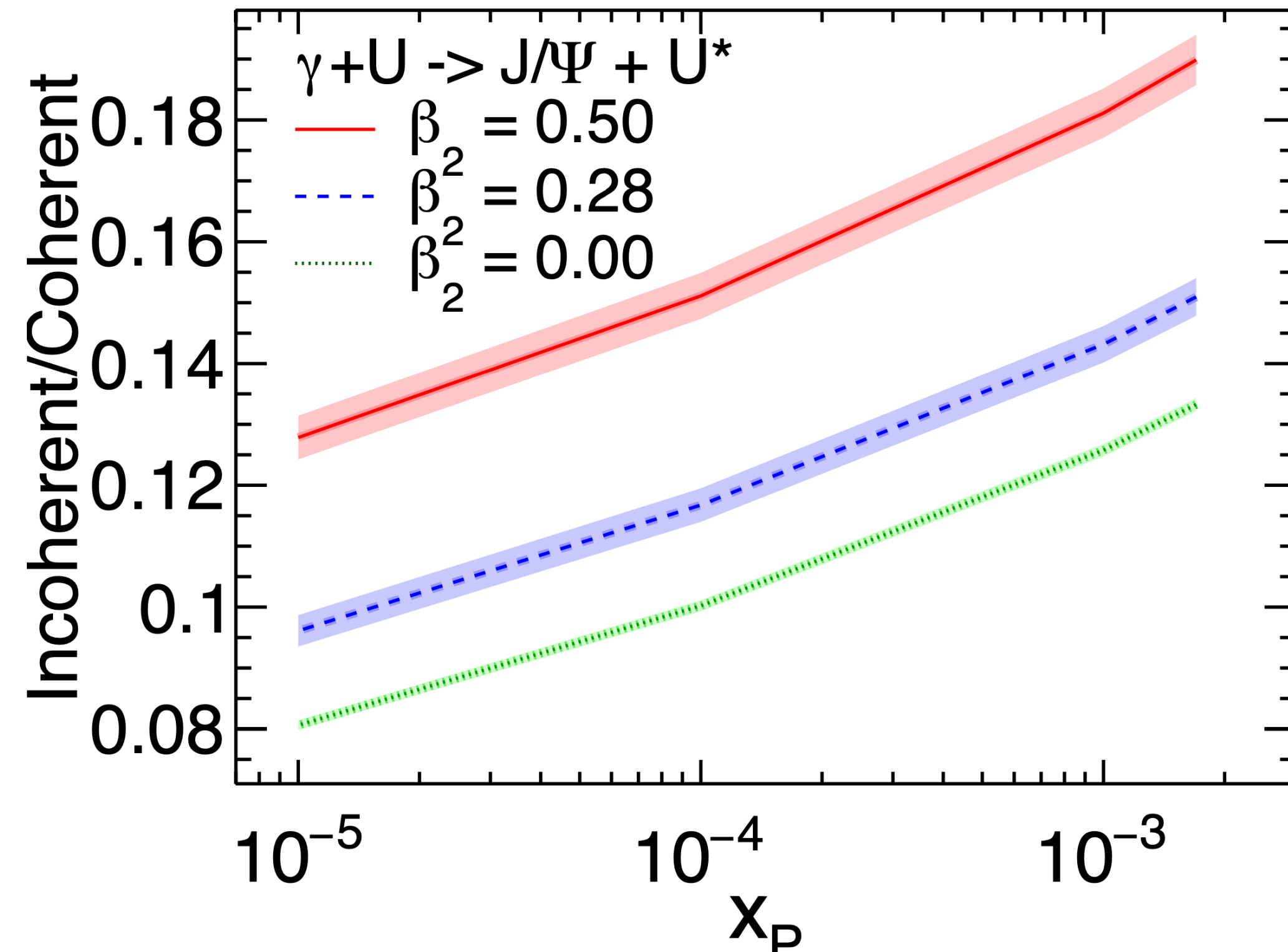
JIMWLK



Some changes in the cross section, but deformation effects survive

Towards smaller x : Incoherent / coherent ratio

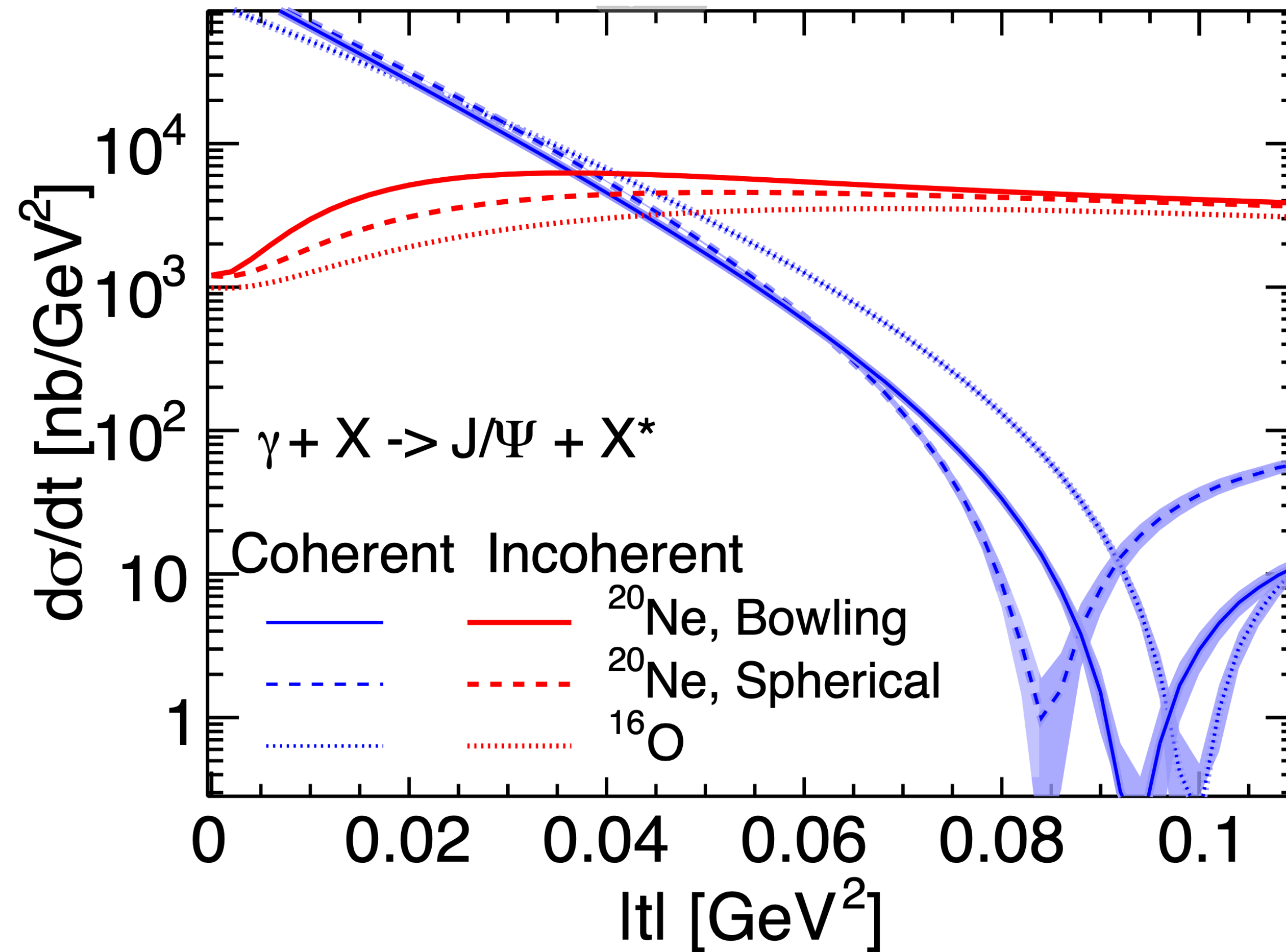
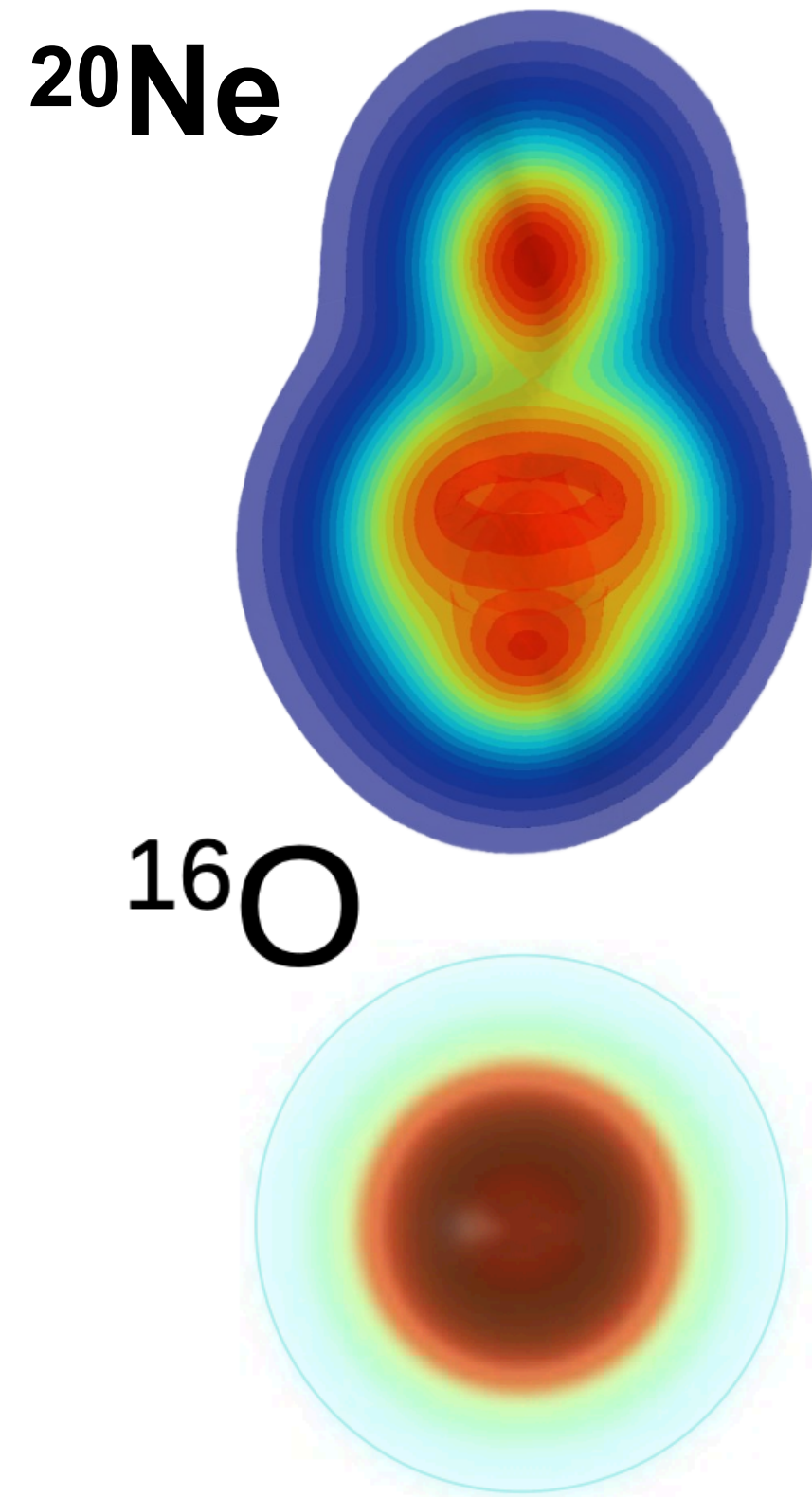
H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, in progress



- Both cross sections grow for decreasing x
- Because fluctuations are reduced, incoherent/coherent ratio decreases
- Effects of deformation not noticeably reduced

Comparing Neon and oxygen

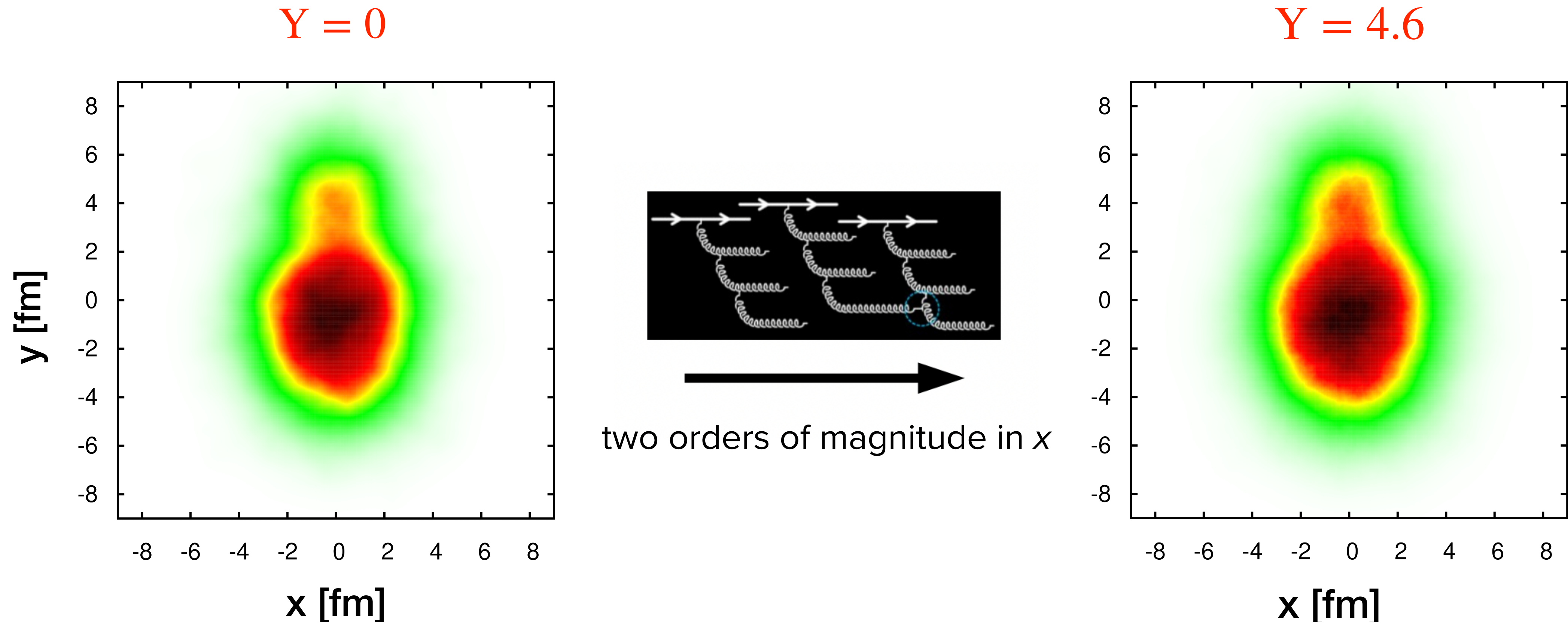
H. Mäntysaari, B. Schenke, C. Shen, W. Zhao, in progress



- Incoherent cross section at small $|t|$ captures the deformation of ^{20}Ne
- Significant difference between ^{20}Ne and ^{16}O diffractive cross sections

Neon - JIMWLK evolution

G. Giacalone, B. Schenke, S. Schlichting, P. Singh, in progress

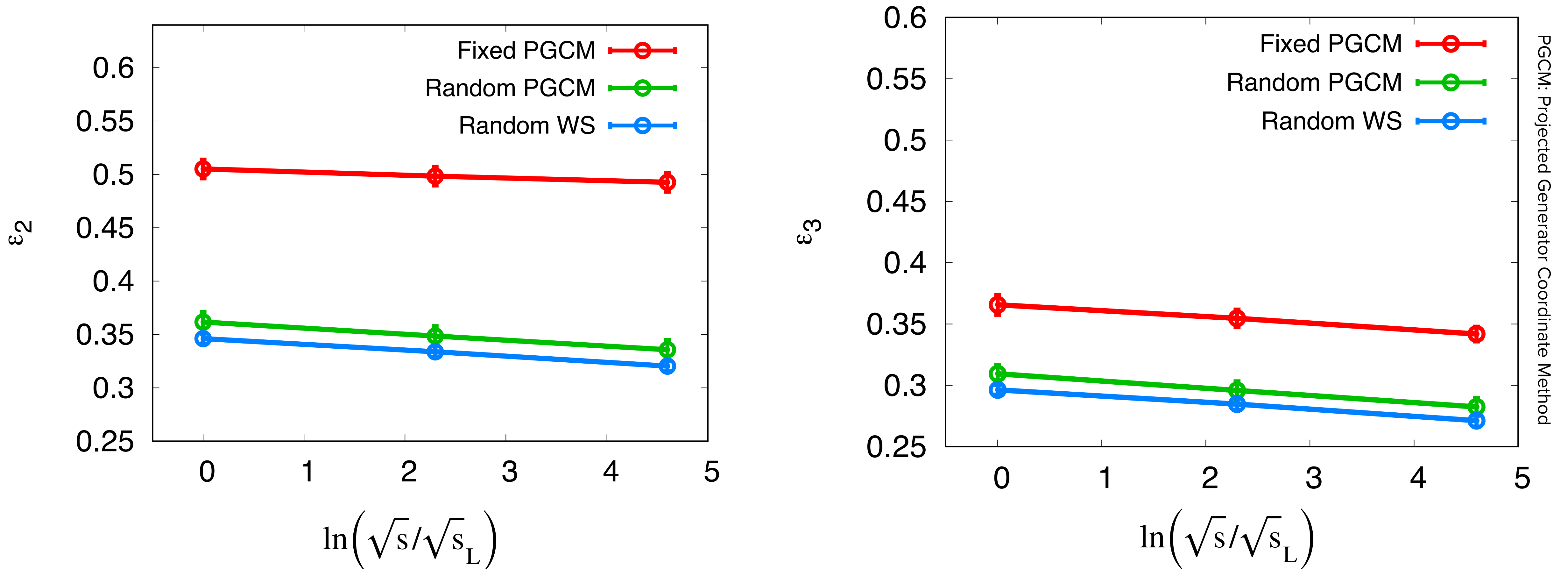


- Small- x evolution does not melt the bowling pin shape

Neon+Neon collisions - JIMWLK evolution

G. Giacalone, B. Schenke, S. Schlichting, P. Singh, in progress

- After the collision at different energies (x), measure the spatial eccentricities



- Expected reduction - smoother distributions, but no large change

Isobar shapes - JIMWLK evolution

G. Giacalone, B. Schenke, S. Schlichting, P. Singh, in progress

