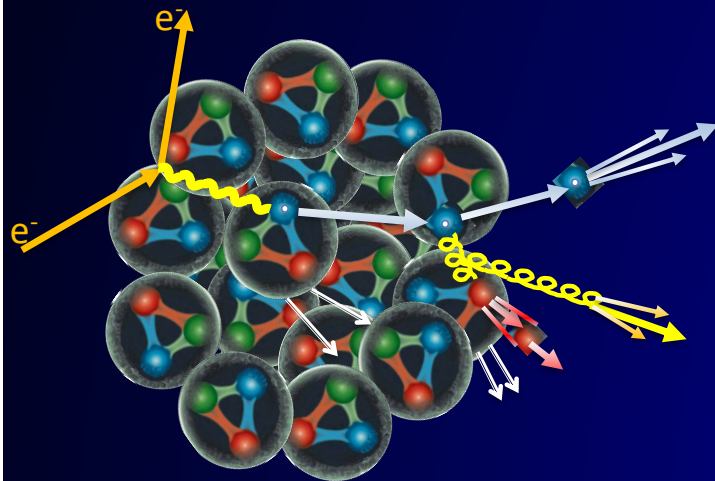




SURGE Collaboration meeting and workshop, June 28-30, 2023

# Overview of the Final State WG



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# Final State WG: Physics goals and timelines

## Physics focus:

- $p_T$  broadening and medium-induced bremsstrahlung
- Hadronization in a dense gluon environment
- Final state hadronic interaction

## Members:

- Faculty: Jaki Noronha-Hostler, Zhongbo Kang, Dima Kharzeev , Alex Kovner, Bjoern Schenke, Vladimir Skokov, Xin-Nian Wang
- Postdoc: Weiyao Ke, Farid Salazar, Wenbin Zhao
- Student: Jordi Salinas

Welcome joining our Final State WG



# Final State WG: Physics goals and timelines

## Year 1:

- Explore improved hadronization prescriptions for dense gluon environments (BS);
- Formulate multiple parton interaction and induced gluon bremsstrahlung within generalized high-twist or opacity approach. Find out the connection to the gluon saturation processes in the initial state (XW)

## Year 2:

- Model TMD gluon distributions inside nuclei consistent with saturation picture to use in transverse momentum broadening and induced gluon bremsstrahlung (XW);
- Provide first hadron level results in processes in e+A and p+A collisions using simplified color flow and study systematic uncertainties (BS)
- Implement improved descriptions of hadronization in dense media via modification of vacuum calculations (BS)

## Year 3:

- Implement multiple parton scattering and induced bremsstrahlung into a MC simulation of parton showering in nuclear medium with proper inclusion of the LPM interference (W)
- Consider the NLO corrections to the jet transport coefficient and the medium-induced gluon radiation with LPM effect (XW)
- Begin implementation of SMASH final state hadronic interactions with various ansatz for the interpolation between hadronic and partonic cross sections based on the formation times (JNH)



# Final State WG: Physics goals and timelines

## Year 4:

- Develop and validate the Monte Carlo code for final state effects and combine it with the hadronization scheme(s); Combine all components into one final state package ranging from sampling partonic cross sections, MC description of final state effects and hadronization, to hadronic rescattering (JNH, BS, VS, XW)
- Incorporate smooth transitions from partonic cross sections into hadronic cross sections using SMASH (JNH)

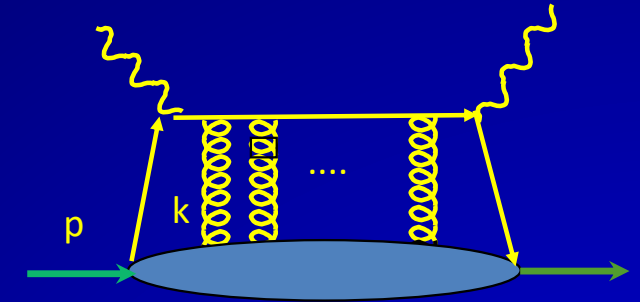
## Year 5:

- Finalize final state and hadronization framework and make it user-friendly; Study the effect of transverse momentum broadening, induced gluon bremsstrahlung and final hadronic interaction in the final hadron spectra, investigate how to disentangle these effects from the initial state gluon saturation (JNH, BS, XW)
- Produce final state results for processes in different collision systems. Study systematic uncertainties of the complete calculation (JNH, FO, BS, XW)
- Incorporate cold nuclear matter effects, e.g. 2-body interactions in SMASH (JNH)



# Multiple parton scattering in nuclear medium

$$f_A^q(x, \vec{k}_\perp) \approx \frac{A}{\pi\Delta} \int d^2q_\perp \exp\left[-\frac{(\vec{k}_\perp - \vec{q}_\perp)^2}{\Delta}\right] f_N^q(x, \vec{q}_\perp)$$



Liang, XNW & Zhou, *PRD* 77 (2008) 125010

$$\Delta = \int dy \hat{q}(y)$$

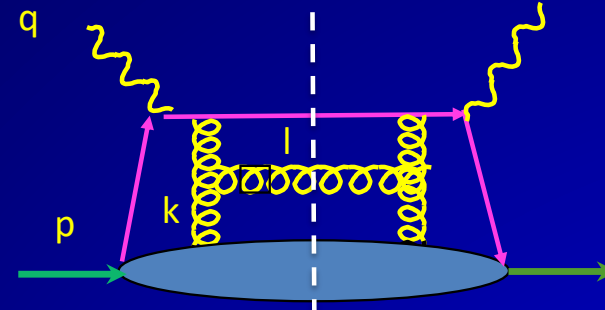
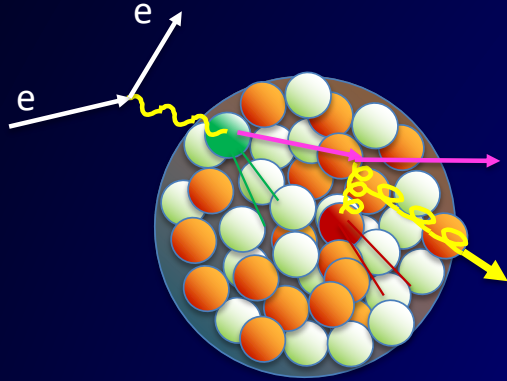
$p_T$  broadening and Jet transport coefficient:

$$\hat{q}(y) = \frac{4\pi^2 C_A}{N_c^2 - 1} \rho(y) \int \frac{d^2k_\perp}{(2\pi)^2} \alpha_s(\mu) \phi(x_G, k_\perp, \mu^2), \quad \longleftrightarrow \quad Q_s^2 = \int dy \hat{q}(y)$$

$$x_G = \frac{x_B k_\perp^2}{Q^2}$$

Saturation scale probed by jet

# Parton energy loss in generalized high-twist approach



Zhang, Qin and XNW, *PRD* 100 (2019) 7, 074031

$$\frac{dN_g}{dl_{\perp}^2 dz} = \int_{y^-}^{\infty} dy_1^- \left[ \rho_A(y_1^-, \vec{y}_{\perp}) \frac{2\pi\alpha_s}{N_c} \pi \int \frac{dk_{\perp}^2}{(2\pi)^2} \frac{\phi_g(0, \vec{k}_{\perp})}{k_{\perp}^2} \right] \pi \frac{\alpha_s}{2\pi} P_{qg}(z) \frac{C_A}{l_{\perp}^2} \mathcal{N}_g(\vec{l}_{\perp}, \vec{k}_{\perp})$$

Nucleon TMD gluon distr.

$$\mathcal{N}_g^{static+soft} = \int \frac{d\varphi}{2\pi} \frac{2\vec{k}_{\perp} \cdot \vec{l}_{\perp}}{(\vec{l}_{\perp} - \vec{k}_{\perp})^2} \left( 1 - \cos \left[ \frac{(\vec{l}_{\perp} - \vec{k}_{\perp})^2}{2q^- z(1-z)} y_1^- \right] \right) \longrightarrow \text{GLV}$$

$\tau_f$  Formation time of the gluon emission  $y_1^- / \tau_f$



# Gluon Saturation and qhat in cold nuclei

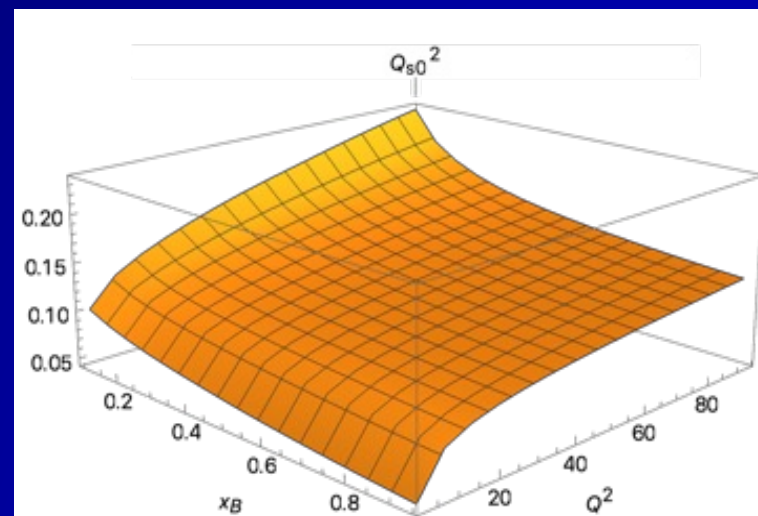
Yuanyuan Zhang & XNW [2104.04520](#)

$$Q_s^2(x_B, Q^2, b_\perp) = \frac{4\pi^2 C_A}{N_c^2 - 1} t_A(b_\perp) \int \frac{d^2 k_\perp}{(2\pi)^2} \alpha_s(\mu) \phi(x_G, k_\perp, \mu^2),$$

$$\phi(x_G, k_\perp, \mu^2) = \begin{cases} \phi^0\left(\frac{Q_s^2}{Q^2} x_B, Q_s, \mu^2\right) \Big|_{\mu^2=Q_s^2}, & k_\perp < Q_s; \\ \phi^0(x_G, k_\perp, \mu^2) \Big|_{\mu^2=k_\perp^2}, & k_\perp > Q_s, \end{cases}$$

$$Q_s^2(x_B, Q^2, b_\perp) \equiv \int dy^- \hat{q}_A(y^-)$$

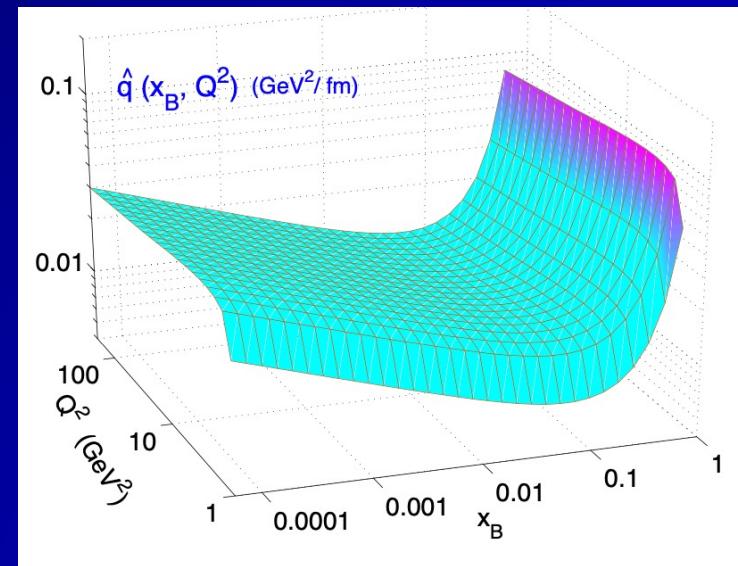
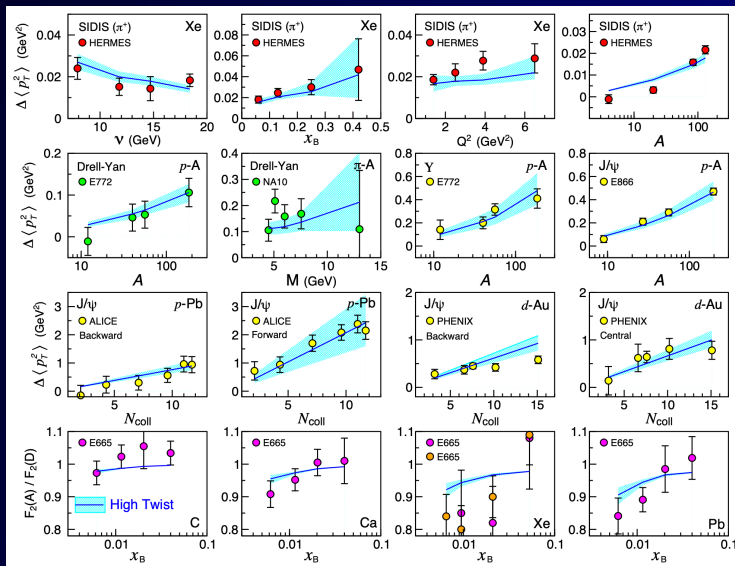
$$\approx Q_{s0}^2(x_B, Q^2) A^{1/3} \sqrt{1 - \frac{b_\perp^2}{R_A^2}}$$



# Jet transport coefficient in nuclei

A global extraction of the jet transport coefficient in nuclei

$$\hat{q}_0 \approx 0.02 \text{ GeV}^2/\text{fm}$$



Data on: DIS, SIDIS( $\pi$ ), Drell-Yan, J/ $\psi$  (pA), Y (pA)

Ru, Kang, Wang, Xing & Zhang *PRD* 103 (2021) 3, L031901





# eHIJING: electron Heavy Ion Jet Interaction Generator

Ke, Zhang, Xing & XNW e-Print: 2304.10779



- Pythia for  $\gamma^*+N \rightarrow$  jet shower processes
- Simple model for saturation in gluon TMD distribution
- Elastic scattering with TMD distr.

$$\alpha_s \phi_g(x_g, k_\perp^2, Q^2) = \frac{(1-x_g)^p x_g^\lambda}{q_\perp^2 + Q_s^2},$$

- Induced gluon emission

Kharzeev & Levin PLB 523 79-87]

$$\frac{dN_g}{dz dl_\perp^2} = \frac{P_{qq}^0(z)}{l_\perp^2} \left\{ 1 + \tilde{T}_A \int_0^L dt^+ \int \frac{d^2 k_\perp}{\pi} \frac{\alpha_s \phi_g(x_g, k_\perp^2)}{k_\perp^2} \frac{2\vec{k}_\perp \cdot \vec{l}_\perp}{(\vec{l}_\perp - \vec{k}_\perp)^2} \left[ 1 - \cos \frac{t^+}{\tau_f} \right] \right\}$$

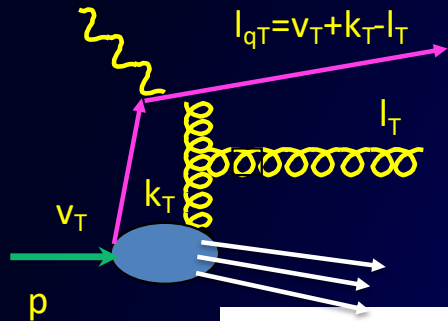
- Multi-scale evolution for multiple gluon emission
  - $Q^2, Q_s^2, \mu_0^2$
- String hadronization

$$\alpha_s \phi_g(x_g, k_\perp^2, Q^2) = \frac{(1-x_g)^p x_g^\lambda}{q_\perp^2 + Q_s^2},$$

See Weiyao Ke's talk on Friday



# LPM interference and rapidity & $R_A$ dependence

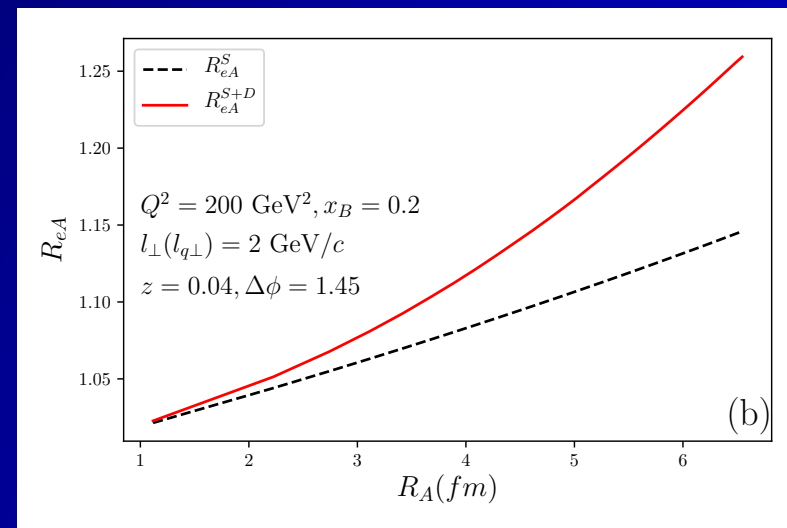
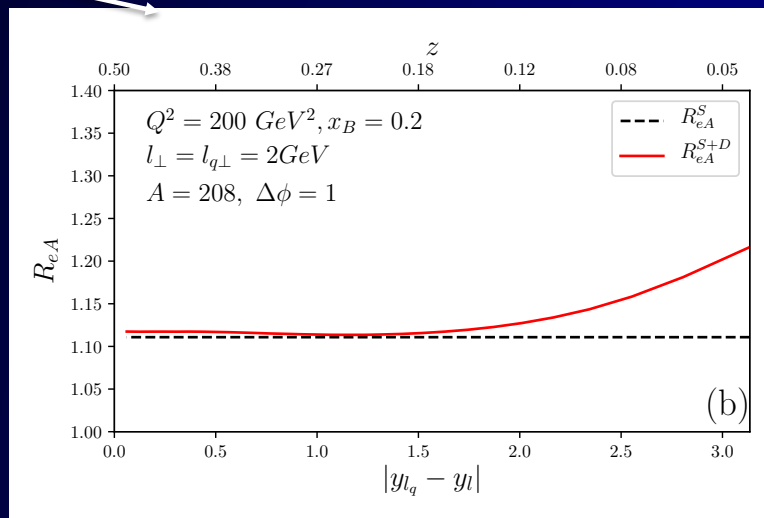


formation time:

$$\tau_f = \frac{2Ez(1-z)}{(\vec{l}_\perp - (1-z)\vec{v}_\perp - \vec{k}_\perp)^2}$$

Nuclear enhancement of dijet or dihedron cross section

Zhang & XNW [2104.04520](#)

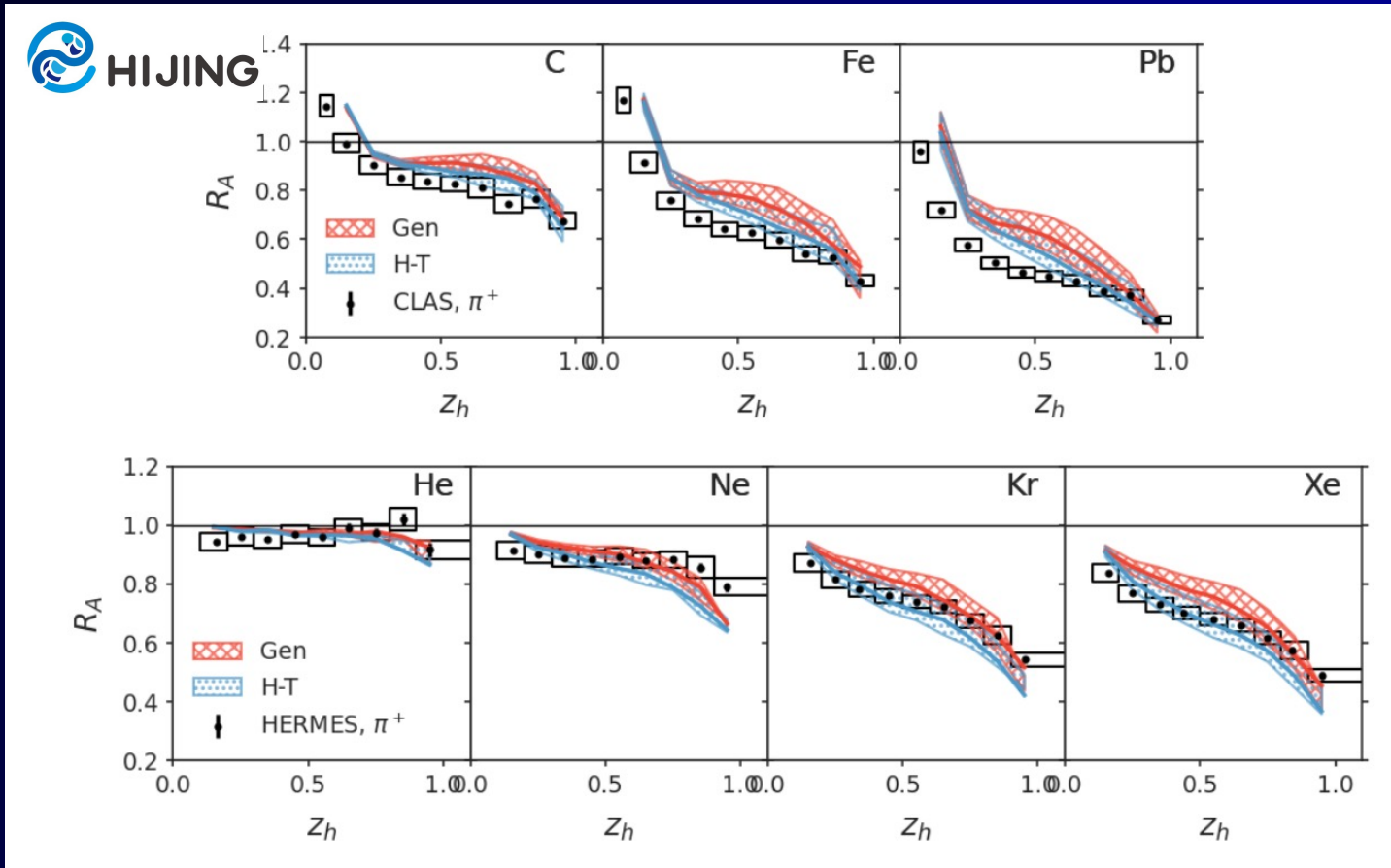


Dijet rapidity gap:  $\Delta y = \log \frac{z}{1-z}$

Quadratic nuclear-size dependence  
due to LPM interference

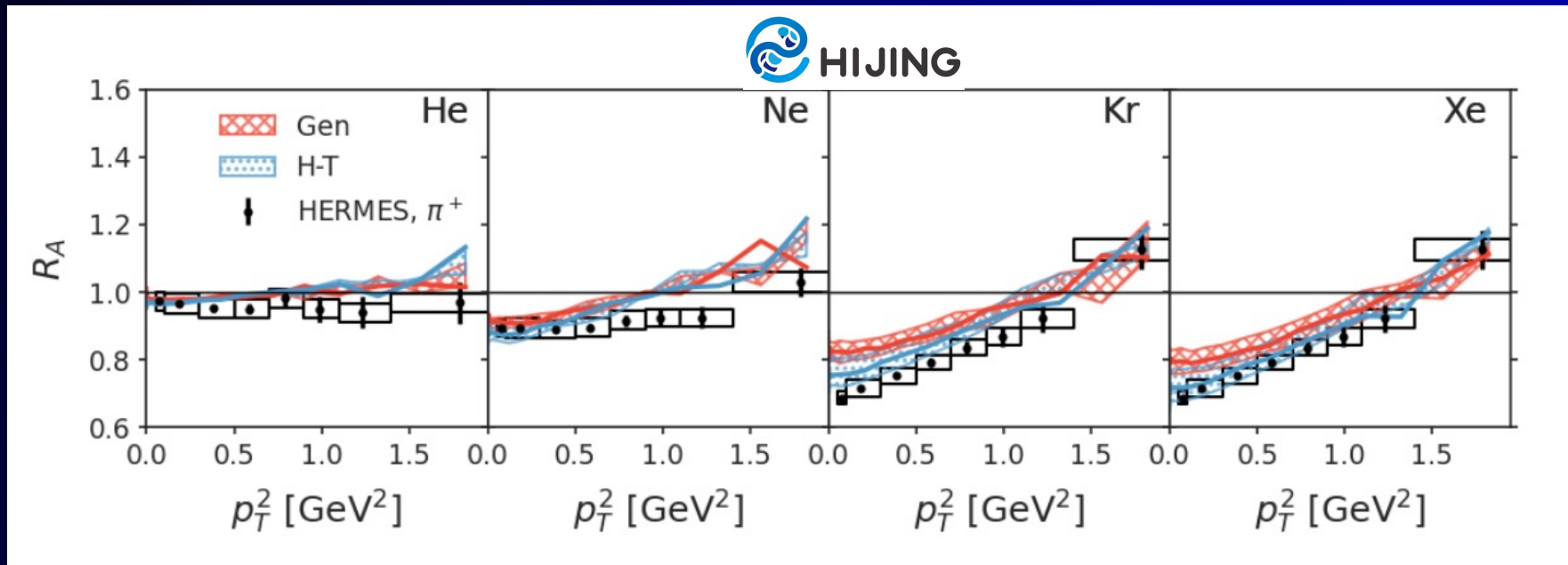
$$\frac{\Delta\sigma_{e+A}}{A\sigma_{e+p}} \propto A^{2/3}$$

# Suppression of single hadron spectra



Effect of hadron absorption in CLAS?

# Transverse momentum broadening



modification of  $p_T$  spectra due to suppression of low  $p_T$  hadrons due to parton energy loss +  $p_T$  broadening

# Hadronic rescattering in DIS eA

- Incorporate SMASH in eHIJING for final state hadronic rescattering
- Adopt the latest list of resonances (immediate states) from PDG
- Compare thermodynamics of HRG with LQCD results
- Time-dependent hadronic cross sections with formation time
- Test with on CLAS12 data at low energies

See talk by Jordi Salinas

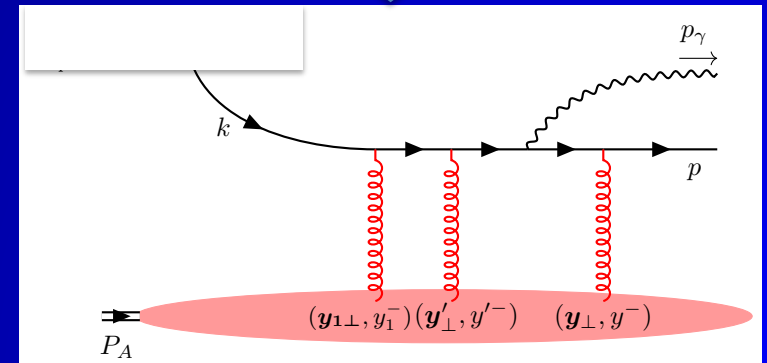
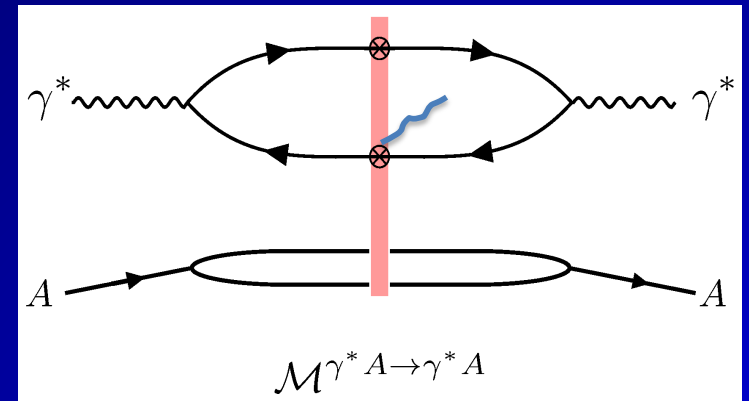


# Next improvement of eHIJING

- Extension to small  $x_B$ 
  - dipole approximation of multiple scattering
  - Initial state evolution: gluon saturation
  - LPM interference: finding back the phases

See Farid Salazar's talk

- Inclusion of final-state hadronic scattering
  - Adopt SMASH in eHIJING
  - Hadronization, Baryon junctions





# Summary

- eHIJING
  - Multiple parton scattering in the final state
  - Modified DGLAP evolution with medium-induced emission
  - LPM effect in induced gluon bremsstrahlung
  - Validation with existing eA data
  - Next step: include dipole multiple scattering at small  $x_B$
- Adopt SMASH for eHIJING
  - Latest list resonances from PDG
  - Next step: couple to eHIJING for final state hadronic interaction



**Welcome joining our Final State WG**



