

# Di-hadron correlation in forward pA collisions at RHIC: how to correctly interpret the results?

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References: Stasto, Xiao, Yuan, PLB 2012;

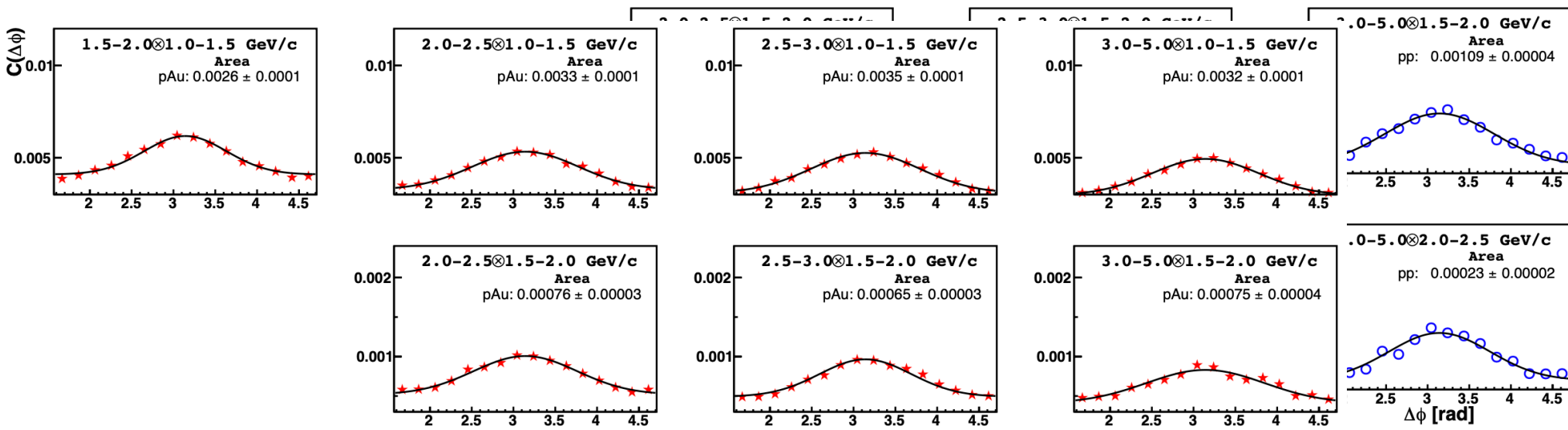
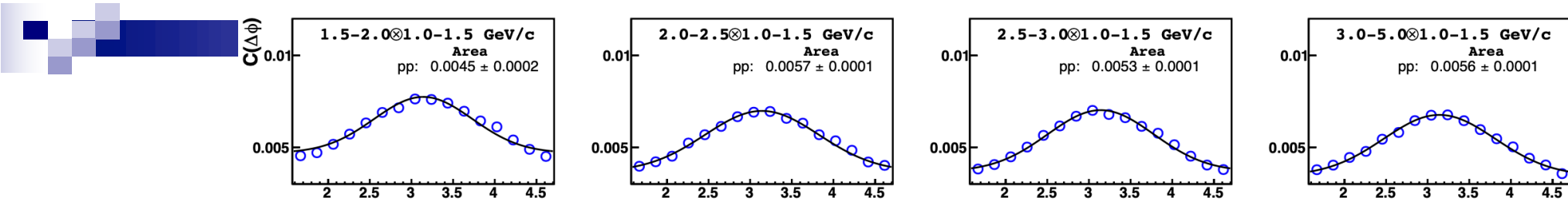
Stasto, Wei, Xiao, Yuan, PLB 2018; work in progress

Acknowledgement: discussions with Elke and Xiaoxuan

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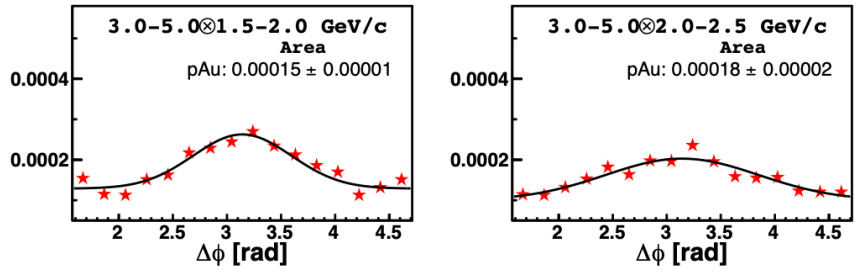
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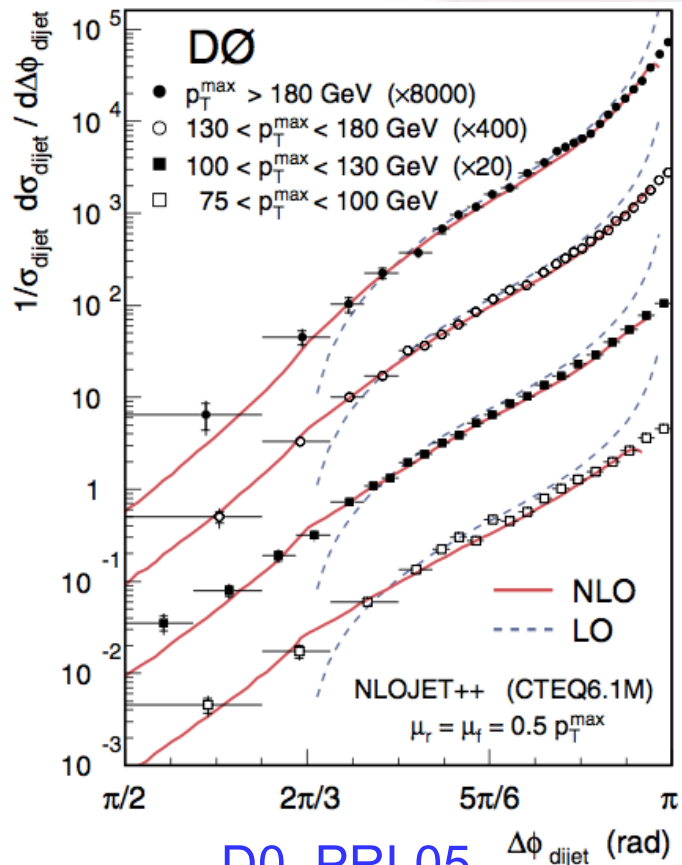


STAR Coll., PRL 2022,  
arXiv:2111.10396

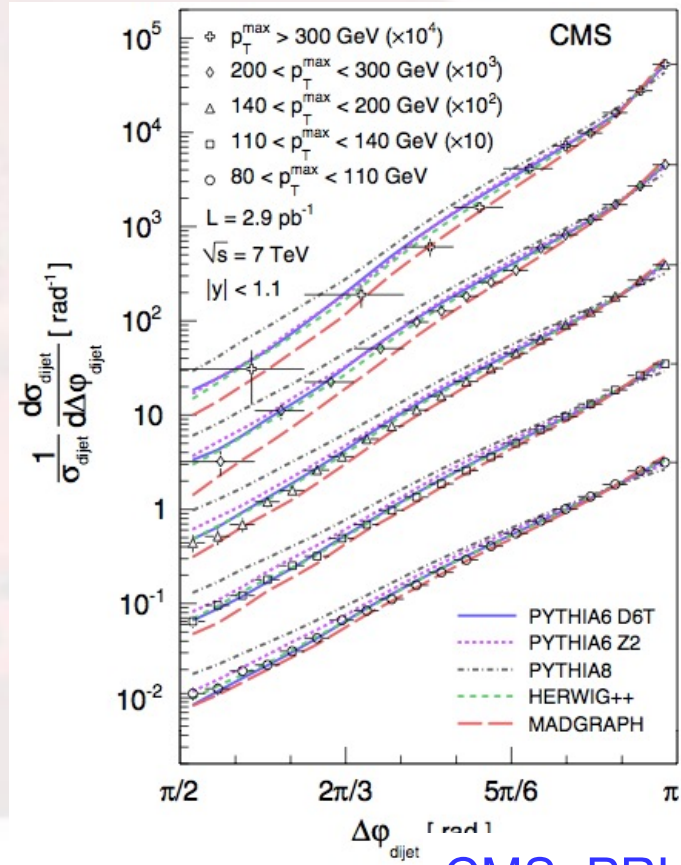
STAR,  $\sqrt{s_{NN}} = 200$  GeV  
pAu  $\rightarrow \pi^0 \pi^0$   
 $2.6 < \eta < 4$   
★ data  
— fit



# Dijet correlation at colliders: beautiful data from Tevatron/LHC



DØ, PRL05



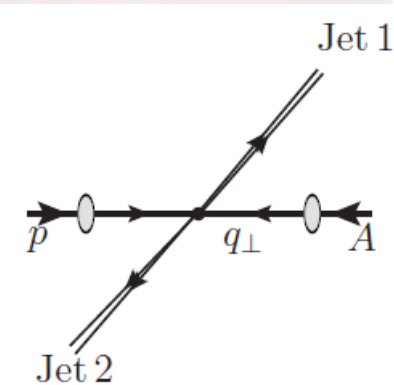
CMS, PRL11 3



# Two particle correlations as probe to the CGC gluon distributions

- Dilute + Dense scattering

$$B + A \rightarrow H_1(k_1) + H_2(k_2) + X$$

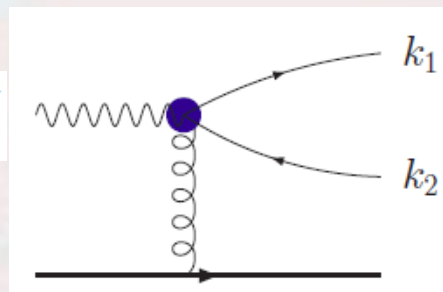


- Correlation limit:

$$|\vec{k}_{1\perp} + \vec{k}_{2\perp}| \ll P_{\perp} \quad (\vec{k}_{1\perp} - \vec{k}_{2\perp})/2$$

# DIS dijet probes $WW$ gluons

$$\gamma_T^* A \rightarrow q(k_1) + \bar{q}(k_2) + X$$

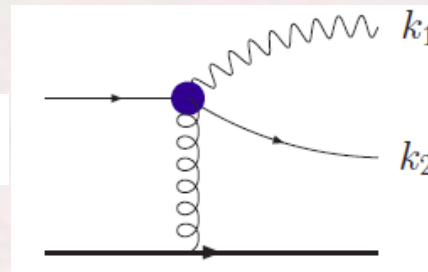


- Hard interaction includes the gluon attachments to both quark and antiquark
- The  $q_t$  dependence probes the  $WW$  gluon distribution at small- $x$

Dominguez-Marquet-Xiao-Yuan 2011;  
See Tomasz and Farid's talks

# Photon-jet correlation probes the dipole gluon distribution

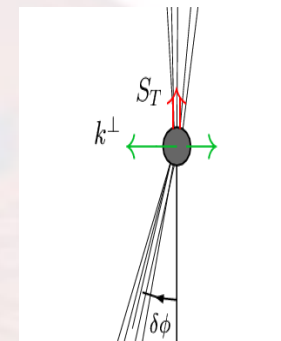
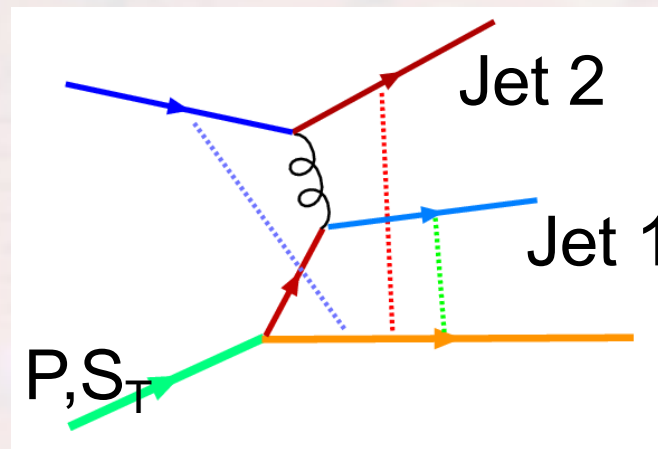
$$pA \rightarrow \gamma(k_1) + q(k_2) + X$$



- Naïve kt-factorization would predict the same  $q_t$ -dependence

# Dijet-correlation at RHIC

- Initial state and/or final state interactions



Boer-Vogelsang 03

**Standard (naïve) Factorization breaks!**

Becchetta-Bomhof-Mulders-  
Pijlman, 04-06

Collins-Qiu 08; Vogelsang-Yuan 08

Rogers-Mulders 10; Xiao-Yuan, 10

# Modified factorization

- Dilute system on a dense target, in the large  $N_c$  limit,

$$\begin{aligned} & \frac{d\sigma(pA \rightarrow \text{Dijet} + X)}{d\mathcal{P} \cdot \mathcal{S}} \\ &= \sum_q x_1 q(x_1) \frac{\alpha_s^2}{\hat{s}^2} \left[ \mathcal{F}_{qg}^{(1)} H_{qg \rightarrow qg}^{(1)} + \mathcal{F}_{qg}^{(2)} H_{qg \rightarrow qg}^{(2)} \right] \\ &+ x_1 g(x_1) \frac{\alpha_s^2}{\hat{s}^2} \left[ \mathcal{F}_{gg}^{(1)} \left( H_{gg \rightarrow q\bar{q}}^{(1)} + H_{gg \rightarrow gg}^{(1)} \right) \right. \\ &\left. + \mathcal{F}_{gg}^{(2)} \left( H_{gg \rightarrow q\bar{q}}^{(2)} + H_{gg \rightarrow gg}^{(2)} \right) + \mathcal{F}_{gg}^{(3)} H_{gg \rightarrow gg}^{(3)} \right], \end{aligned}$$

Dominguez-Marquet-Xiao-Yuan 2011



## ■ Hard partonic cross section

$$\begin{aligned}
 H_{qg \rightarrow qg}^{(1)} &= \frac{\hat{u}^2 (\hat{s}^2 + \hat{u}^2)}{-2\hat{s}\hat{u}\hat{t}^2}, & H_{qg \rightarrow qg}^{(2)} &= \frac{\hat{s}^2 (\hat{s}^2 + \hat{u}^2)}{-2\hat{s}\hat{u}\hat{t}^2} \\
 H_{gg \rightarrow q\bar{q}}^{(1)} &= \frac{1}{4N_c} \frac{2 (\hat{t}^2 + \hat{u}^2)^2}{\hat{s}^2 \hat{u} \hat{t}}, & H_{gg \rightarrow q\bar{q}}^{(2)} &= \frac{1}{4N_c} \frac{4 (\hat{t}^2 + \hat{u}^2)}{\hat{s}^2} \\
 H_{gg \rightarrow gg}^{(1)} &= \frac{2 (\hat{t}^2 + \hat{u}^2) (\hat{s}^2 - \hat{t}\hat{u})^2}{\hat{u}^2 \hat{t}^2 \hat{s}^2}, & H_{gg \rightarrow gg}^{(2)} &= \frac{4 (\hat{s}^2 - \hat{t}\hat{u})^2}{\hat{u} \hat{t} \hat{s}^2} \\
 H_{gg \rightarrow gg}^{(3)} &= \frac{2 (\hat{s}^2 - \hat{t}\hat{u})^2}{\hat{u}^2 \hat{t}^2},
 \end{aligned}$$

- Although the individual diagram depends on the gauge, the total contribution does not

Dominguez-Marquet-Xiao-Yuan 2011



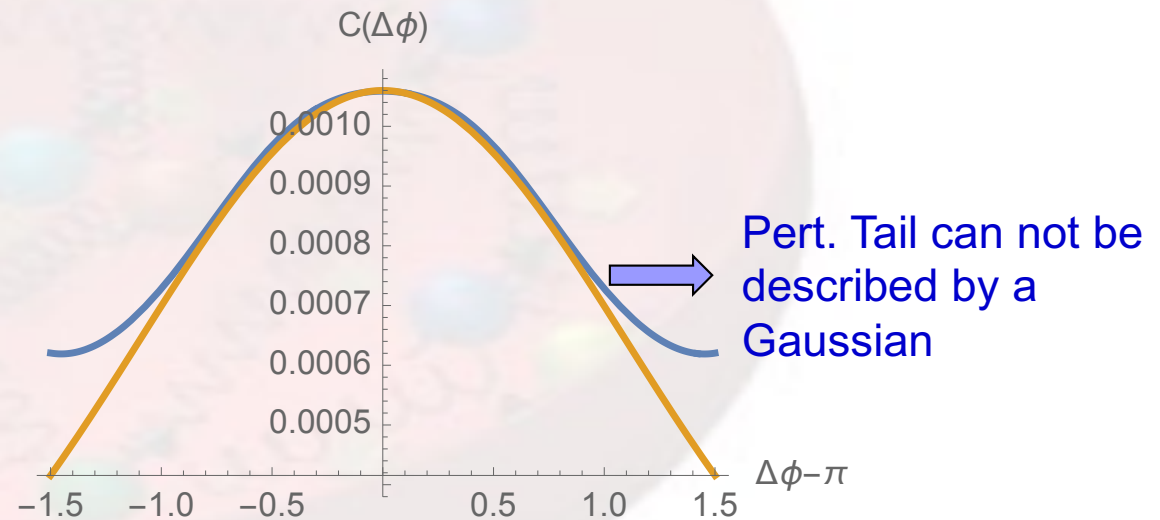
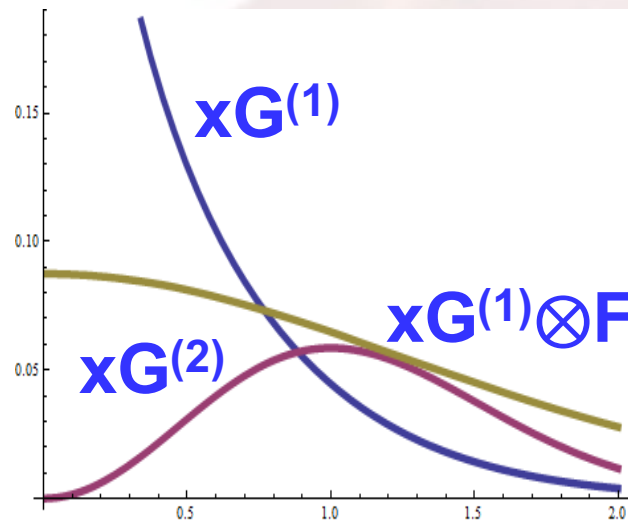
- Kt-dependent gluon distributions

$$\begin{aligned}\mathcal{F}_{qg}^{(1)} &= xG^{(2)}(x, q_{\perp}), \quad \mathcal{F}_{qg}^{(2)} = \int xG^{(1)}(q_1) \otimes F(q_2), \\ \mathcal{F}_{gg}^{(1)} &= \int xG^{(2)}(q_1) \otimes F(q_2), \quad \mathcal{F}_{gg}^{(2)} = \int \frac{q_{1\perp} \cdot q_{2\perp}}{q_{1\perp}^2} xG^{(2)}(q_1) \otimes F(q_2) \\ \mathcal{F}_{gg}^{(3)} &= \int xG^{(1)}(q_1) \otimes F(q_2) \otimes F(q_3),\end{aligned}$$

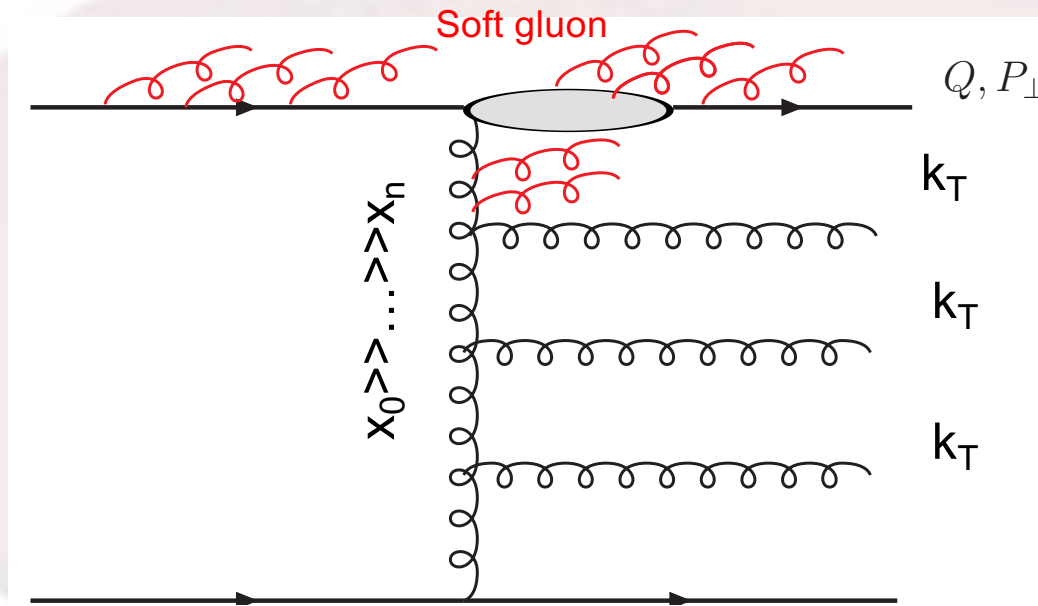
- Color-dipole/CGC agrees with the above results

Dominguez-Marquet-Xiao-Yuan 2011

# Various gluon distributions and their contributions to the two particle correlation



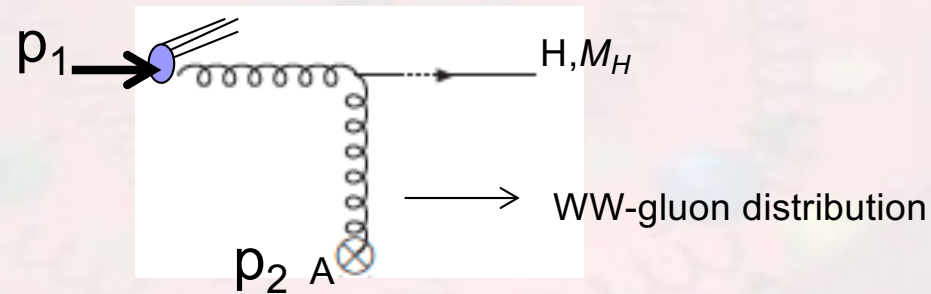
# Beyond leading order picture: additional dynamics comes in



- BFKL vs **Sudakov** resummations (LL)

# Sudakov resummation at small-x

- Take massive scalar particle production  $p+A \rightarrow H+X$  as an example to demonstrate the double logarithms, and resummation



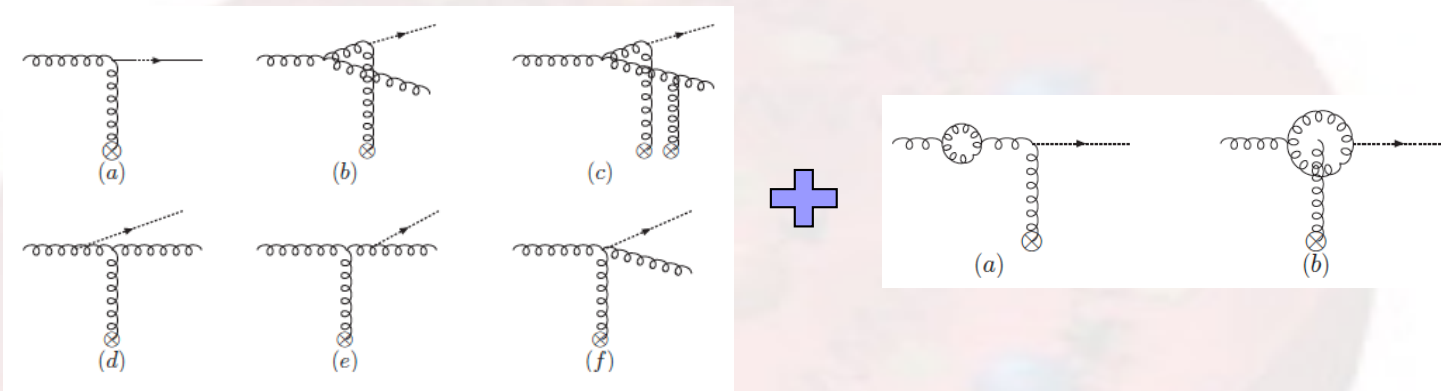
$$\frac{d\sigma^{(LO)}}{dyd^2k_{\perp}} = \sigma_0 \int \frac{d^2x_{\perp}d^2x'_{\perp}}{(2\pi)^2} e^{ik_{\perp} \cdot r_{\perp}} x_0 g_p(x_0) S^{(WW)}(x_{\perp}, x'_{\perp})$$

$$S_Y^{WW}(x_{\perp}, y_{\perp}) = - \left\langle \text{Tr} \left[ \partial_{\perp}^{\beta} U(x_{\perp}) U^{\dagger}(y_{\perp}) \partial_{\perp}^{\beta} U(y_{\perp}) U^{\dagger}(x_{\perp}) \right] \right\rangle_Y$$

6/28/23

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# Explicit one-loop calculations



$$x_0 g_p(x_0) \int \frac{d\xi}{\xi} \mathbf{K}_{DMMX} \otimes S^{WW}(x_\perp, y_\perp) + \left(-\frac{1}{\epsilon}\right) S^{WW}(x_\perp, y_\perp) \mathcal{P}_{g/g} \otimes x_0 g(x_0) ,$$

- Collinear divergence  $\rightarrow$  DGLAP evolution
- Small-x divergence  $\rightarrow$  BK-type evolution

Dominguiz-Mueller-Munier-Xiao, 2011

# Soft vs Collinear gluons

- Radiated gluon momentum

$$k_g = \alpha_g p_1 + \beta_g p_2 + k_{g\perp} ,$$

- Soft gluon,  $\alpha \sim \beta \ll 1$
- Collinear gluon,  $\alpha \sim 1, \beta \ll 1$
- Small-x collinear gluon,  $1 - \beta \ll 1, \alpha \rightarrow 0$ 
  - Rapidity divergence

# Final result

- Double logs at one-loop order


$$\frac{d\sigma^{(\text{LO+NLO})}}{dyd^2k_{\perp}} \Big|_{k_{\perp} \ll Q} = \sigma_0 \int \frac{d^2x_{\perp} d^2x'_{\perp}}{(2\pi)^2} e^{ik_{\perp} \cdot r_{\perp}} S_{Y=\ln 1/x_a}^{WW}(x_{\perp}, x'_{\perp}) x g_p(x, \mu^2 = \frac{c_0^2}{r_{\perp}^2}) \left\{ 1 + \frac{\alpha_s}{\pi} C_A \left[ \beta_0 \ln \frac{Q^2 r_{\perp}^2}{c_0^2} - \frac{1}{2} \left( \ln \frac{Q^2 r_{\perp}^2}{c_0^2} \right)^2 + \frac{\pi^2}{2} \right] \right\},$$

- Collins-Soper-Sterman resummation (**NLL**)

$$\frac{d\sigma^{(\text{resum})}}{dyd^2k_{\perp}} \Big|_{k_{\perp} \ll Q} = \sigma_0 \int \frac{d^2x_{\perp} d^2x'_{\perp}}{(2\pi)^2} e^{ik_{\perp} \cdot r_{\perp}} e^{-S_{\text{sud}}(Q^2, r_{\perp}^2)} S_{Y=\ln 1/x_a}^{WW}(x_{\perp}, x'_{\perp}) \times x g_p(x, \mu^2 = c_0^2/r_{\perp}^2) \left[ 1 + \frac{\alpha_s}{\pi} \frac{\pi^2}{2} N_c \right],$$







# Sudakov resummation in CGC: other examples

- Dijet production in DIS (NLL)
  - Caucal-Salazar-Schenke-Venugopalan 2022, 2023
  - Paels-Altinoluk-Beuf-Marquet 2022
- Sudakov logs can be re-summed consistently in the small-x formalism
- Kinematics of Sudakov logs and small-x evolution are well separated
  - Soft vs collinear gluons

## Extend to dijet in hadronic processes: count the leading double logs

- Each incoming parton contributes to a half of the associated color factor
  - Initial gluon radiation, aka, TMDs
- Soft gluon radiation in collinear calculation also demonstrates this rule
  - Sterman, et al
  - Sub-leading logs will be much complicated, usually a matrix form

## Beyond the leading double logs: collinear

- Jet size-dependence is computed by averaging the azimuthal angle between the soft gluon and leading jet
- Matrix form due to colored final state [Kidonakis-Sterman 1997](#)

$$x_1 f_a(x_1, \mu = b_0/b_\perp) x_2 f_b(x_2, \mu = b_0/b_\perp) e^{-S_{\text{Sud}}(Q^2, b_\perp)} \\ \text{Tr} \left[ \mathbf{H}_{ab \rightarrow cd} \exp\left[-\int_{b_0/b_\perp}^Q \frac{d\mu}{\mu} \gamma^{s^\dagger}\right] \mathbf{S}_{ab \rightarrow cd} \exp\left[-\int_{b_0/b_\perp}^Q \frac{d\mu}{\mu} \gamma^s\right] \right]$$

(Sun, C.-P. Yuan, F. Yuan, PRL 2014)

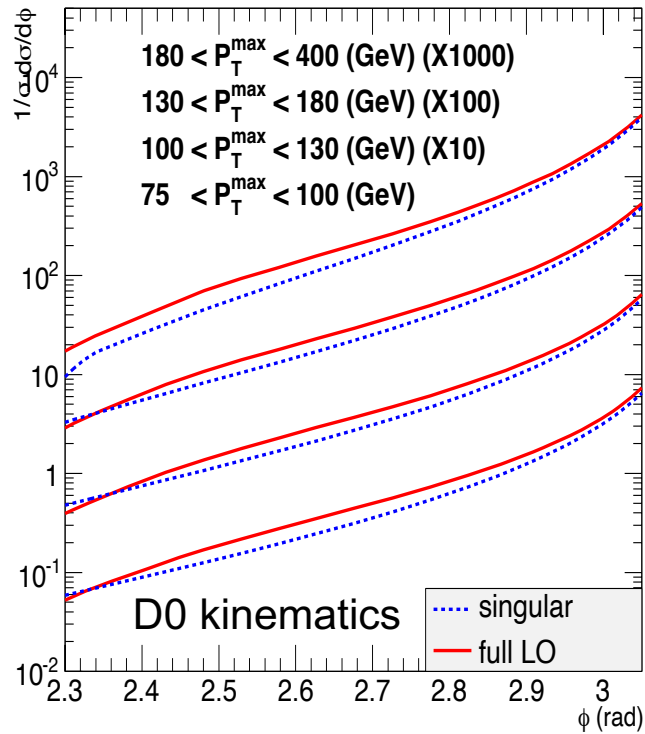
$$S_{\text{Sud}}(Q^2, b_\perp) = \int_{b_0^2/b_\perp^2}^{Q^2} \frac{d\mu^2}{\mu^2} \left[ \ln\left(\frac{Q^2}{\mu^2}\right) A + B + D_1 \ln \frac{Q^2}{P_T^2 R_1^2} + D_2 \ln \frac{Q^2}{P_T^2 R_2^2} \right]$$

D: color-factor for the jet

R: jet size



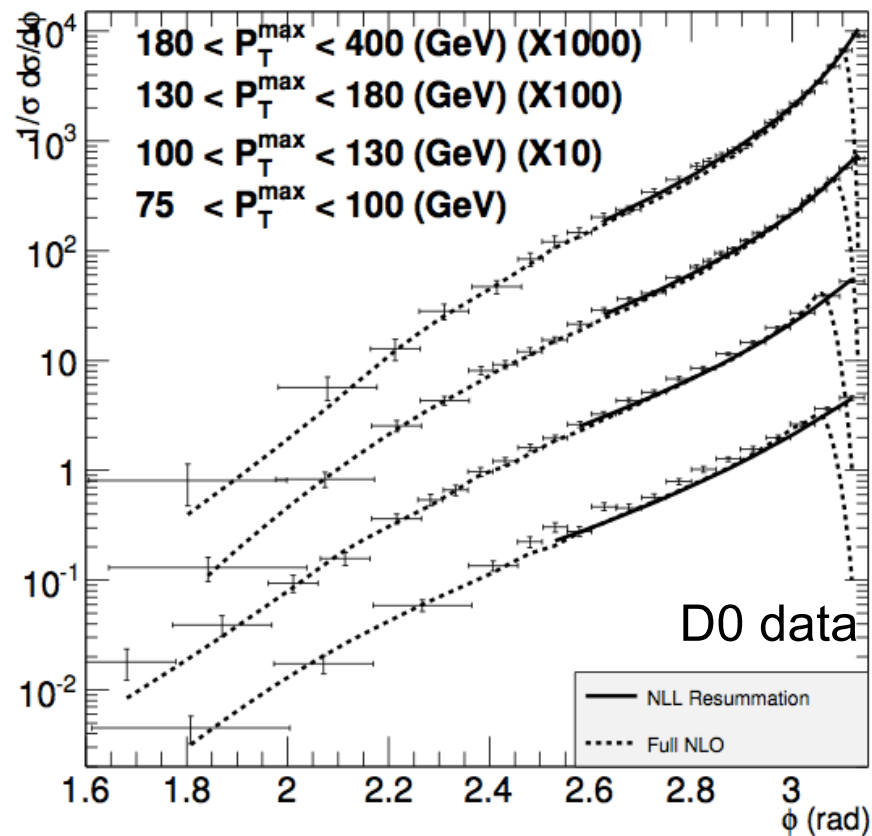
# Compare to the full calculations



$$\begin{aligned}
 & \frac{\alpha_s}{2\pi^2} \frac{1}{q_{\perp}^2} \sum_{ab,a'b'} \sigma_0 \int \frac{dx'_1}{x'_1} \frac{dx'_2}{x'_2} x'_1 f_a(x'_1, \mu) x'_2 f_b(x'_2, \mu) \\
 & \times \left\{ h_{a'b' \rightarrow cd}^{(0)} \left[ \xi_1 \mathcal{P}_{a'/a}(\xi_1) \delta(1 - \xi_2) + \xi_2 \mathcal{P}_{b'/b}(\xi_2) \delta(1 - \xi_1) \right. \right. \\
 & \left. \left. + \delta(1 - \xi_1) \delta(1 - \xi_2) \delta_{aa'} \delta_{bb'} \left( (C_a + C_b) \ln \frac{Q^2}{q_{\perp}^2} + C_c \ln \frac{1}{R_1^2} + C_d \ln \frac{1}{R_2^2} \right) \right] \right. \\
 & \left. + \delta(1 - \xi_1) \delta(1 - \xi_2) \delta_{aa'} \delta_{bb'} \Gamma_{sn}^{ab \rightarrow cd} \right\} , \tag{10}
 \end{aligned}$$

Leading  $P_T$   
 Total  $q_T \approx P_T \sin(\Delta\phi)$   
 full LO: Nagy 2002, NLOJET++

# Compare to the data



NLL Resummation:  
Sun, C.P. Yuan, F. Yuan, PRL2014

$$x_1 f_a(x_1, \mu = b_0/b_\perp) x_2 f_b(x_2, \mu = b_0/b_\perp) e^{-S_{\text{Sud}}(Q^2, b_\perp)}$$

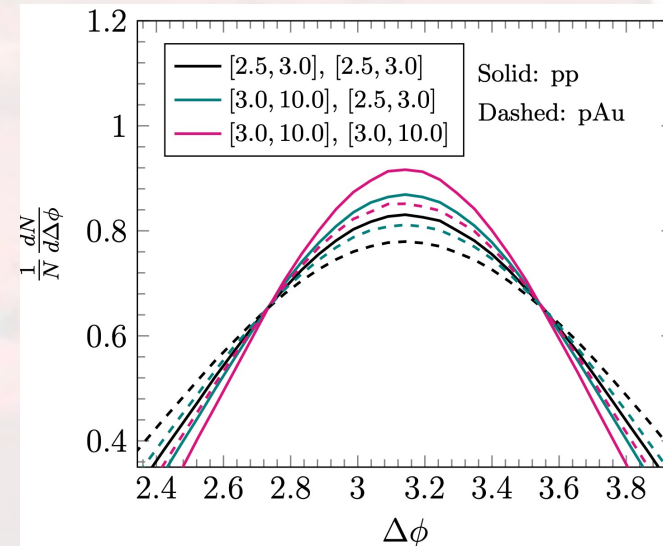
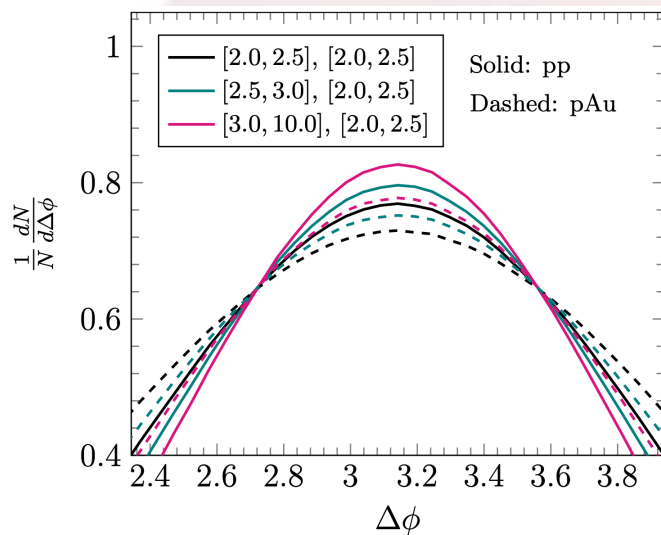
$$\text{Tr} \left[ \mathbf{H}_{ab \rightarrow cd} \exp \left[ - \int_{b_0/b_\perp}^Q \frac{d\mu}{\mu} \gamma^{s\dagger} \right] \mathbf{S}_{ab \rightarrow cd} \exp \left[ - \int_{b_0/b_\perp}^Q \frac{d\mu}{\mu} \gamma^s \right] \right]$$

Full NLO: Nagy 2002, NLOJET++

# Include Sudakov effects in the CGC for di-hadron correlations

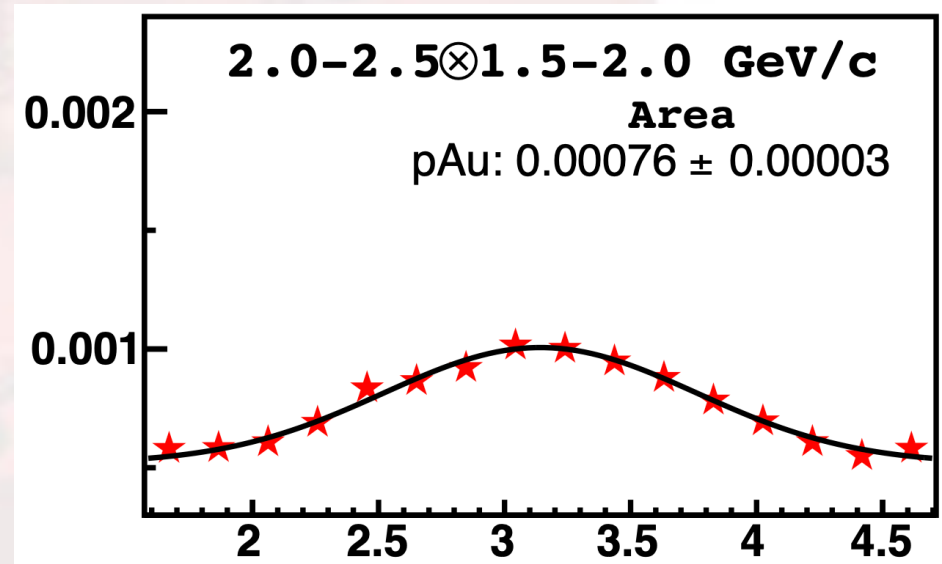
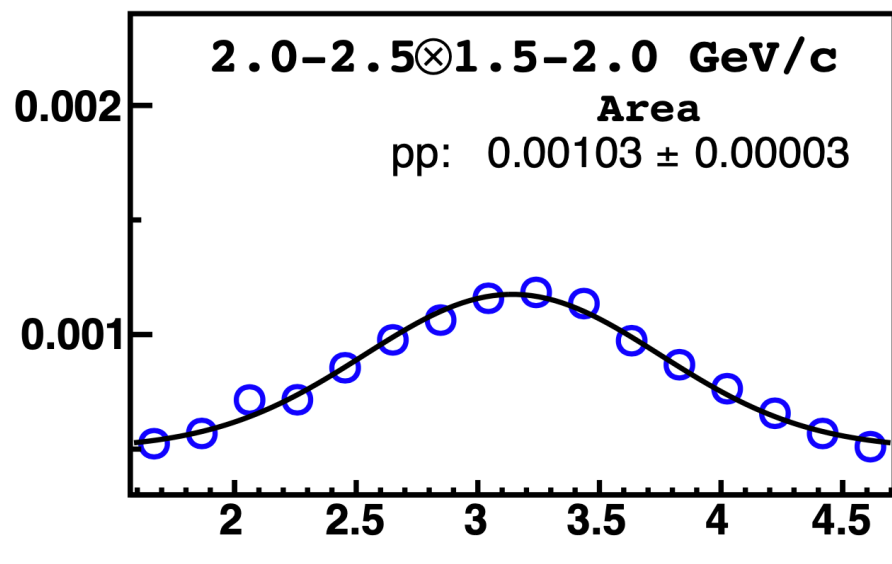
- Unintegrated gluon distributions w/ Sudakov, e.g.,

$$\mathcal{F}_{qg}^{(a)}(x_g, q_\perp) = \frac{-N_c S_\perp}{2\pi^2 \alpha_s} \int_0^\infty \frac{b_\perp db_\perp}{2\pi} J_0(q_\perp b_\perp) e^{-S_{\text{Sud}}^{q+g \rightarrow q+g}(b_\perp)} \nabla_{b_\perp}^2 S_{x_g}(b_\perp)$$



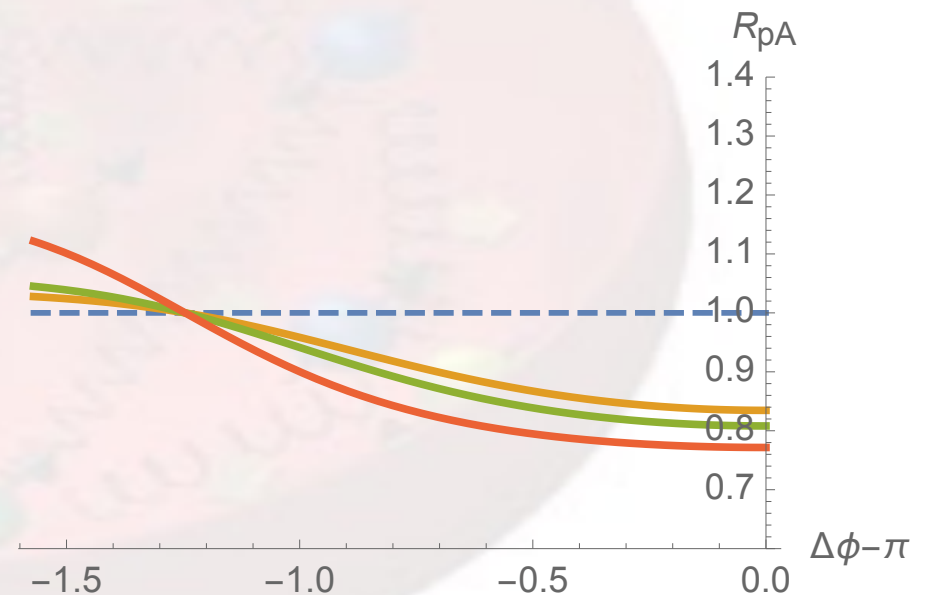
# Real data teach us more on the physics

- Compare pp to pA



# Simple extraction of nuclear suppression indicates a Pt-broadening effects

- Suppression factor depends on the background subtraction
  - STAR fit: constant background+simple Gaussian shows no Pt-broadening
- Pt-broadening is not as profound as our previous predictions
  - It may change if different background subtraction used





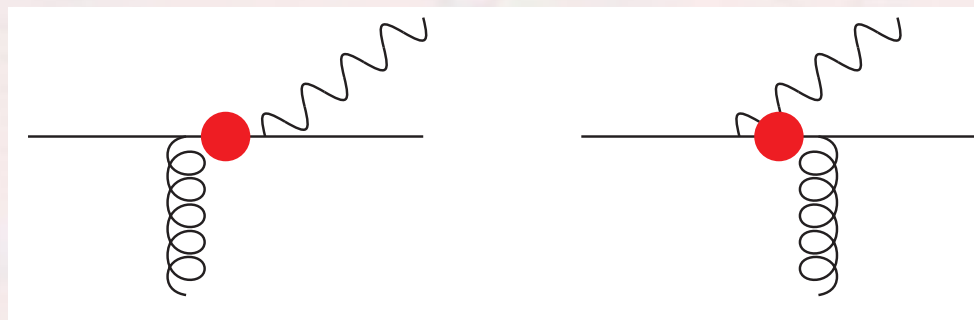


# Looking forward

- We need more data
  - Cross check the background! E.g., through charged particle pairs, mixed pairs etc., and photon+hadron correlations
- We need theory developments
  - Complete NLL resummation for dijet in hadronic collisions in CGC (**collinear framework done**)
  - Need BK-JIMWLK evolution for all different UGDs, at least qualitatively

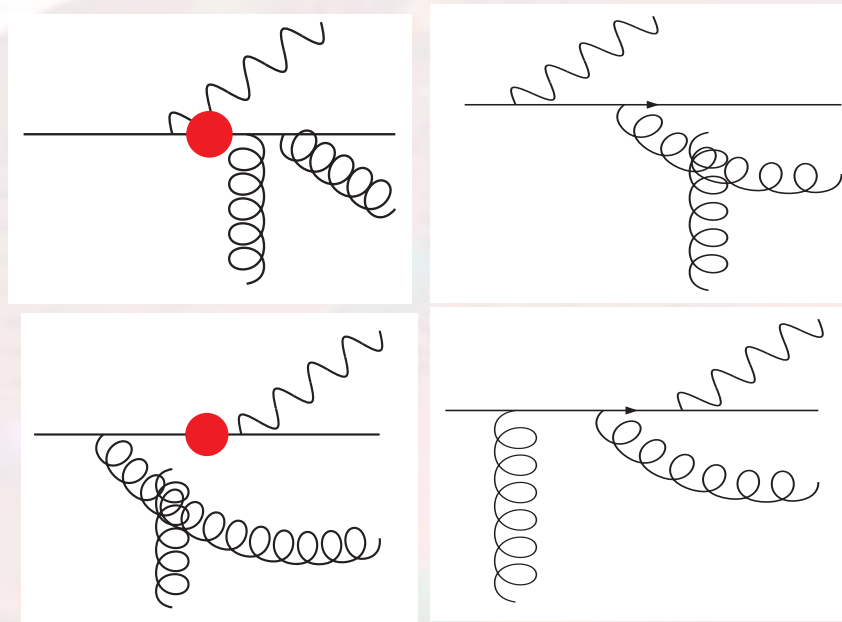
# Photon-Jet correlation

- Leading order



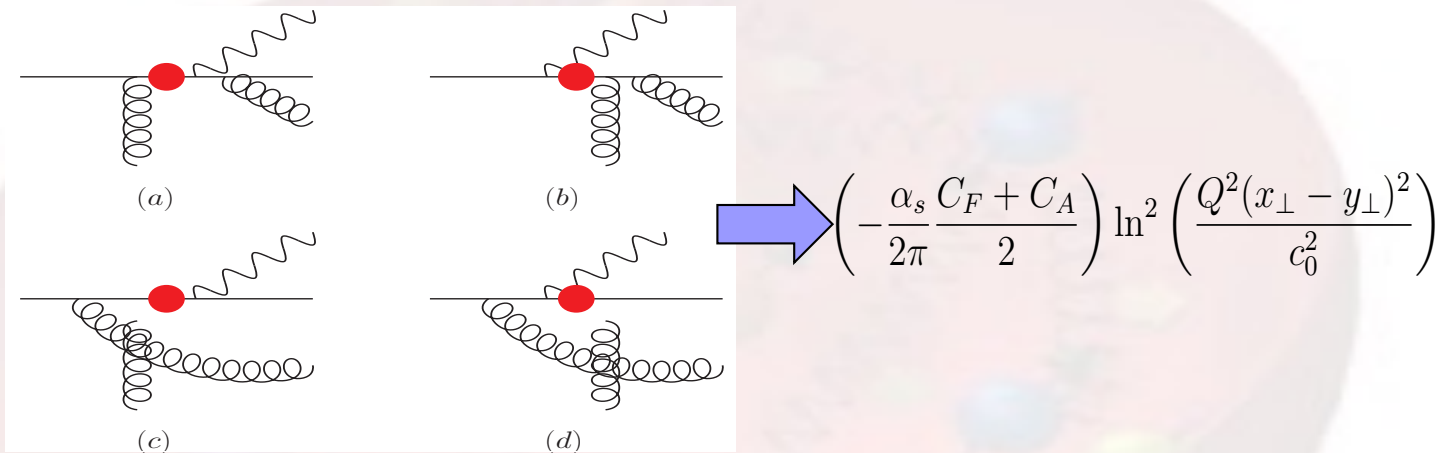
Dipole gluon distribution

# BK-evolution



$$\frac{\partial}{\partial Y} S_Y^{(2)}(x_\perp, y_\perp) = -\frac{\alpha_s N_c}{2\pi^2} \int \frac{d^2 b_\perp (x_\perp - y_\perp)^2}{(x_\perp - b_\perp)^2 (y_\perp - b_\perp)^2} \left[ S_Y^{(2)}(x_\perp, y_\perp) - S_Y^{(4)}(x_\perp, b_\perp, y_\perp) \right]$$

# Soft gluon radiation



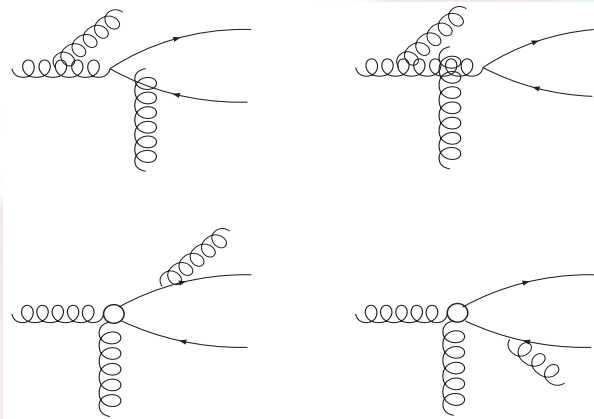
- $A^2$  from (a,b) contribute to  $C_F/2$  (jet)
- $A^2$  from (c,d) contribute to  $C_F$
- Interference contribute to  $1/2N_c$

# Di-jet correlations in pA

- Effective kt-factorization

$$\begin{aligned} & \frac{d\sigma^{(pA \rightarrow \text{Dijet} + X)}}{d\mathcal{P} \cdot \mathcal{S}} \\ &= \sum_q x_1 q(x_1) \frac{\alpha_s^2}{\hat{s}^2} \left[ \mathcal{F}_{qg}^{(1)} H_{qg \rightarrow qg}^{(1)} + \mathcal{F}_{qg}^{(2)} H_{qg \rightarrow qg}^{(2)} \right] \\ &+ x_1 g(x_1) \frac{\alpha_s^2}{\hat{s}^2} \left[ \mathcal{F}_{gg}^{(1)} \left( H_{gg \rightarrow q\bar{q}}^{(1)} + H_{gg \rightarrow gg}^{(1)} \right) \right. \\ &\left. + \mathcal{F}_{gg}^{(2)} \left( H_{gg \rightarrow q\bar{q}}^{(2)} + H_{gg \rightarrow gg}^{(2)} \right) + \mathcal{F}_{gg}^{(3)} H_{gg \rightarrow gg}^{(3)} \right] , \end{aligned}$$

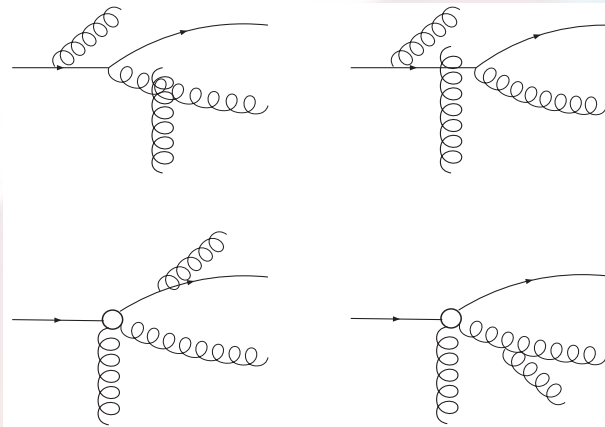
# $gg \rightarrow qq$



$$\rightarrow \left(-\frac{\alpha_s}{2\pi} N_c\right) \ln^2 \left(\frac{Q^2(x_\perp - y_\perp)^2}{c_0^2}\right)$$

- $|A_1|^2 \rightarrow C_A, |A_2|^2 \rightarrow C_F/2, |A_3|^2 \rightarrow C_F/2$
- $2A_1^*(A_2 + A_3) \rightarrow -N_c/2$
- $2A_2^*A_3, 1/N_c$  suppressed

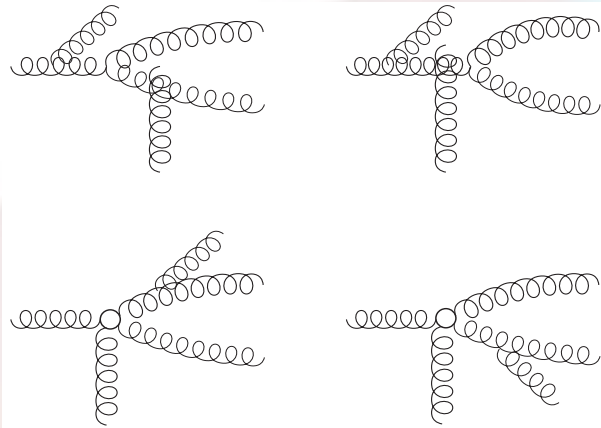
# $qg \rightarrow qg$



$$\left( -\frac{\alpha_s}{2\pi} \frac{C_F + C_A}{2} \right) \ln^2 \left( \frac{Q^2(x_\perp - y_\perp)^2}{c_0^2} \right)$$

- $|A_1|^2 \rightarrow C_F, |A_2|^2 \rightarrow C_F/2, |A_3|^2 \rightarrow C_A/2$
- $2A_3^*(A_1 + A_2) \rightarrow -N_c/2$
- $2A_1^*A_2$ , large  $N_c$  suppressed

$gg \rightarrow gg$



$$\rightarrow \left(-\frac{\alpha_s}{2\pi} N_c\right) \ln^2 \left(\frac{Q^2(x_\perp - y_\perp)^2}{c_0^2}\right)$$

- $|A_1|^2 \rightarrow C_A, |A_2|^2 \rightarrow C_A/2, |A_3|^2 \rightarrow C_A/2$
- $2A_1^*(A_2 + A_3) + 2A_2^*A_3 \rightarrow -N_c$