

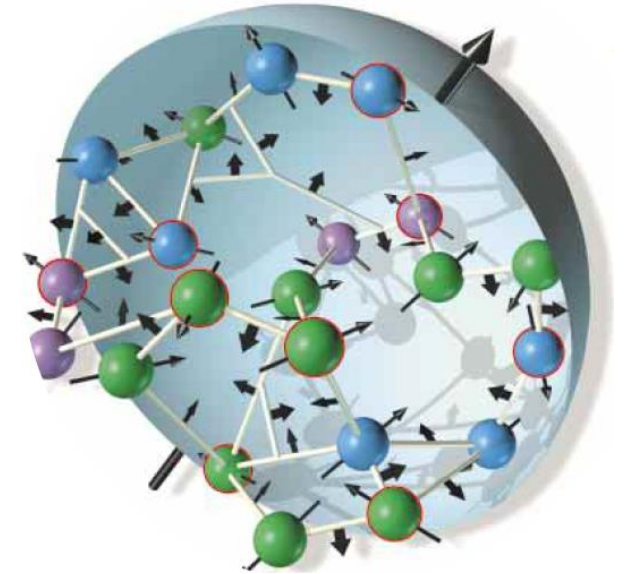
Spin physics at the EIC

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The proton spin problem

The proton has spin $\frac{1}{2}$.

The proton is not an elementary particle.



➔

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L^q + L^g$$
$$= \frac{1}{2} \Delta\Sigma + L_{kin}^q + J_g$$

Jaffe-Manohar sum rule

Ji sum rule

$\Delta\Sigma = 1$ in the naïve quark model

$\Delta\Sigma$ from polarized DIS

Longitudinal double spin asymmetry in polarized DIS

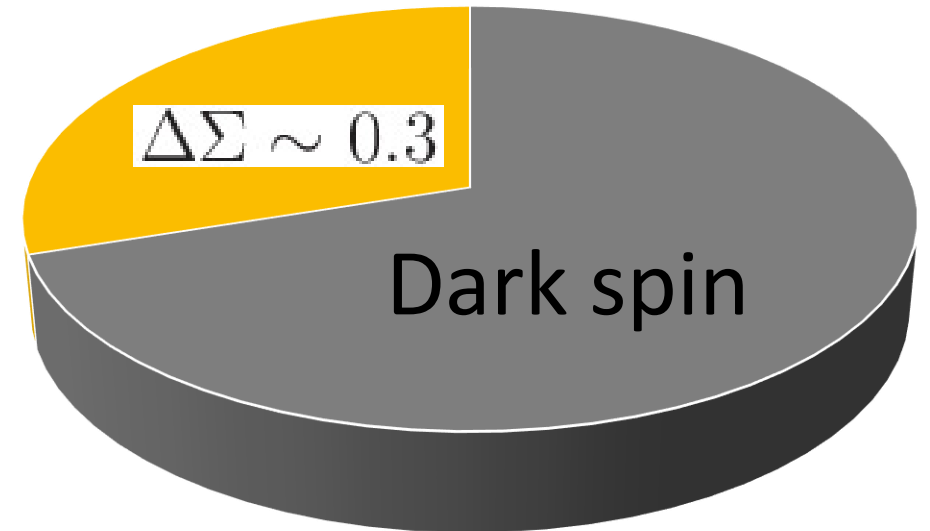
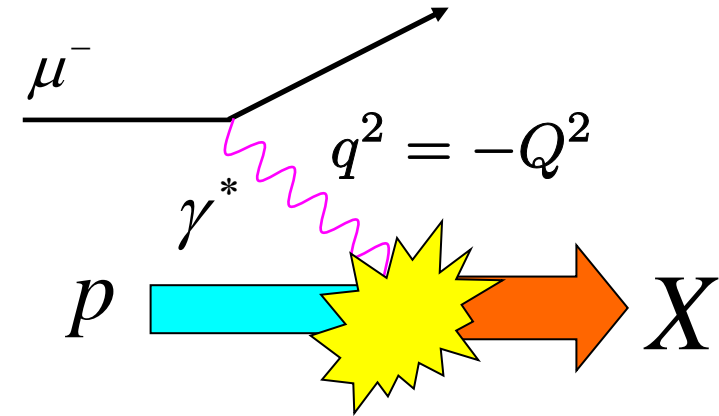
$$A_{LL} = \frac{\mu^\uparrow p^\downarrow - \mu^\uparrow p^\uparrow}{\mu^\uparrow p^\uparrow + \mu^\uparrow p^\downarrow}$$

$$\sim \left(1 + \frac{\sigma_L}{\sigma_T}\right) \frac{2xg_1}{F_2}$$

$$\int_0^1 dx g_1(x) = \frac{1}{9}(\Delta u + \Delta d + \Delta s)$$

$$+ \frac{1}{12}(\Delta u - \Delta d)$$

$$+ \frac{1}{36}(\Delta u + \Delta d - 2\Delta s) + \mathcal{O}(\alpha_s)$$



Helicity pQCD precision frontier

4-loop evolution of $\Delta\Sigma$

De Florian, Vogelsang (2019)

NNLO jet production in polarized DIS

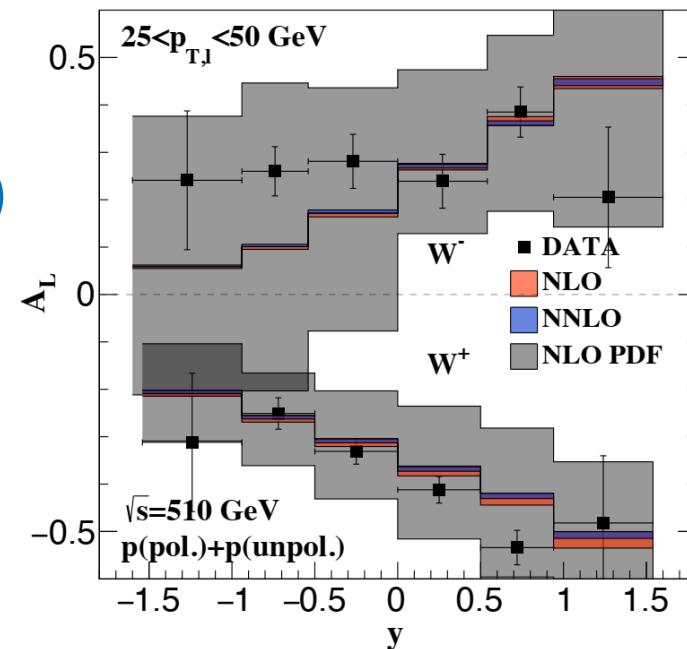
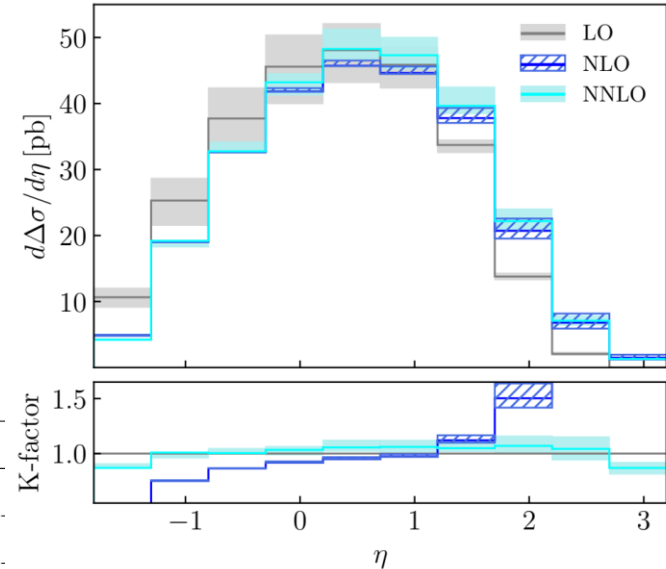
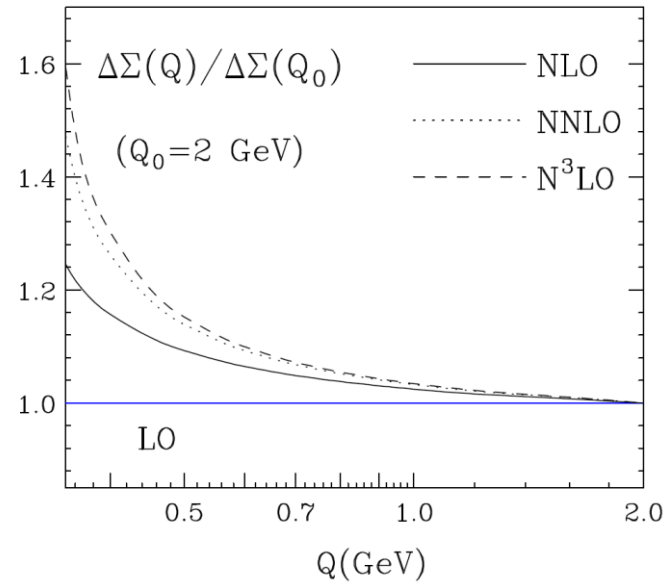
Borsa, de Florian, Pedron (2020)

NNLO longitudinal spin asymmetry of W at RHIC

Boughezal, Li, Petriello (2021)

3-loop Wilson coefficients for $g_1(x)$

Blumlein, Marquard, Schneider, Schonwald (2022)



Evidence of nonzero gluon helicity $\Delta G = \int_0^1 dx \Delta G(x)$

A major achievement of the RHIC spin program!

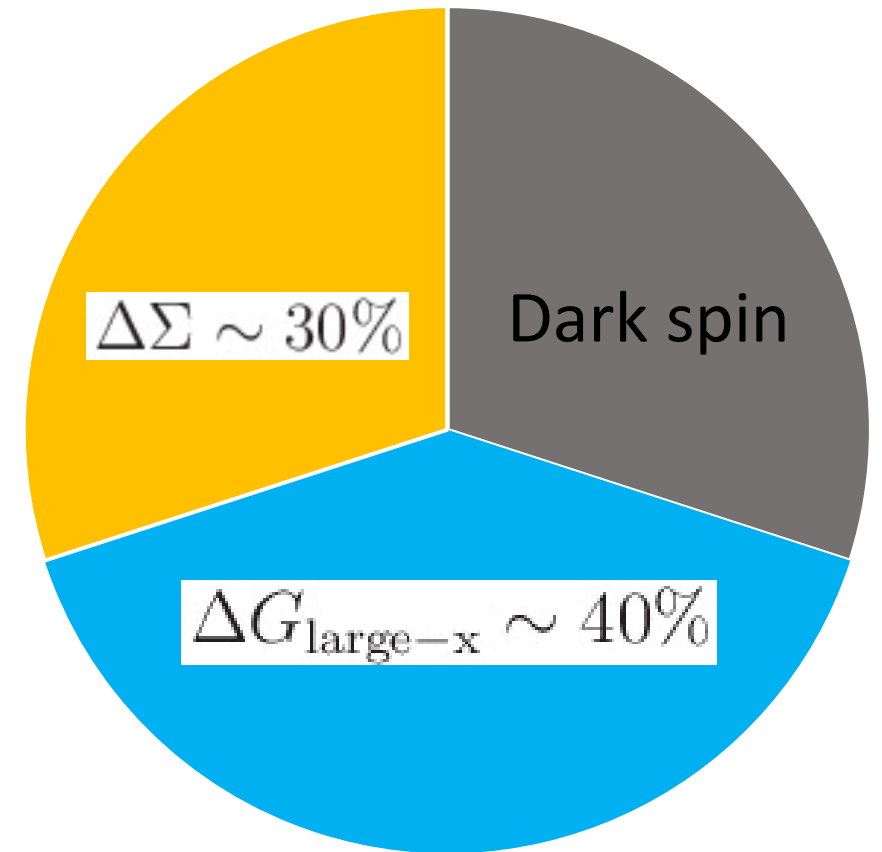
$$\int_{0.05}^1 dx \Delta G(x, Q^2 = 10 \text{GeV}^2) = 0.20_{-0.07}^{+0.06} \quad \text{DSSV}$$

$$\int_{0.05}^{0.2} dx \Delta G(x, Q^2 = 10 \text{GeV}^2) = 0.17 \pm 0.06 \quad \text{NNPDF}$$

$$\int_{0.05}^1 dx \Delta G(x, Q^2 = 10 \text{GeV}^2) = 0.23 \pm 0.03 \quad \text{JAM}$$

Huge uncertainty from the **small-x** region

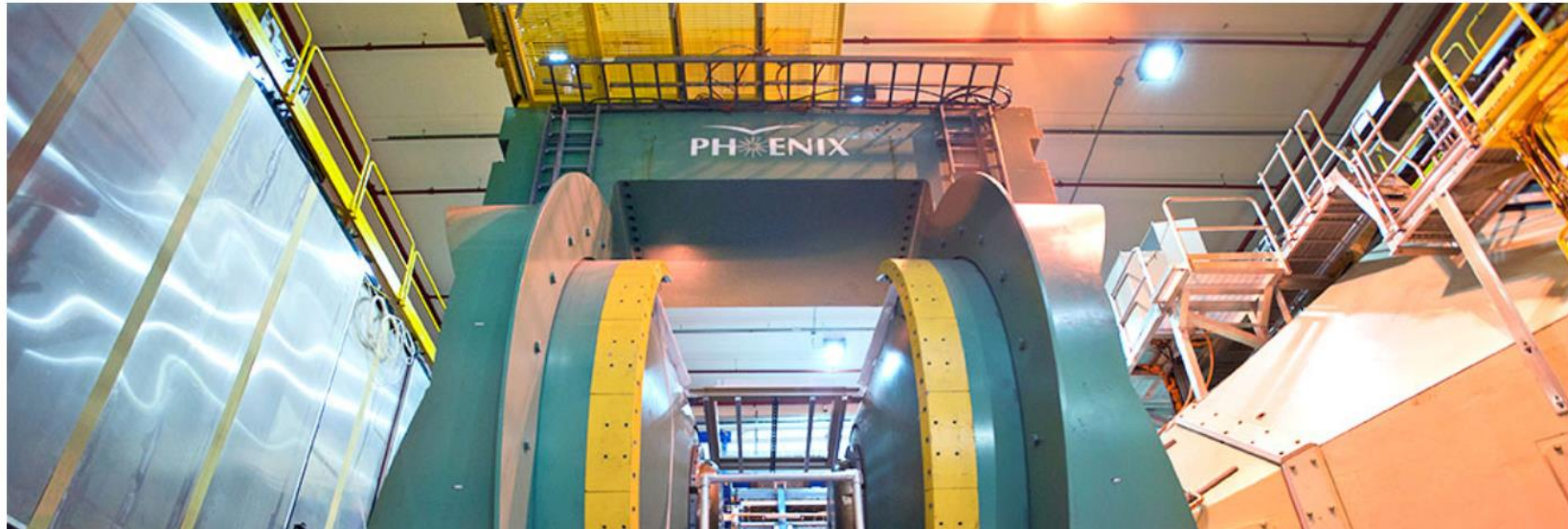
Does the remaining spin (**~30%**) come from the small-x region of $\Delta G(x)$?



Direct Photons Point to Positive Gluon Polarization

Results from 'golden measurement' at RHIC's PHENIX experiment show the spins of gluons align with the spin of the proton they're in

June 21, 2023



Helicity evolution at small-x

All-order resummation of small-x **double** logarithms
for helicity distributions $(\alpha_s \ln^2 1/x)^n$

Unlike BFKL, we need to include quark ladders

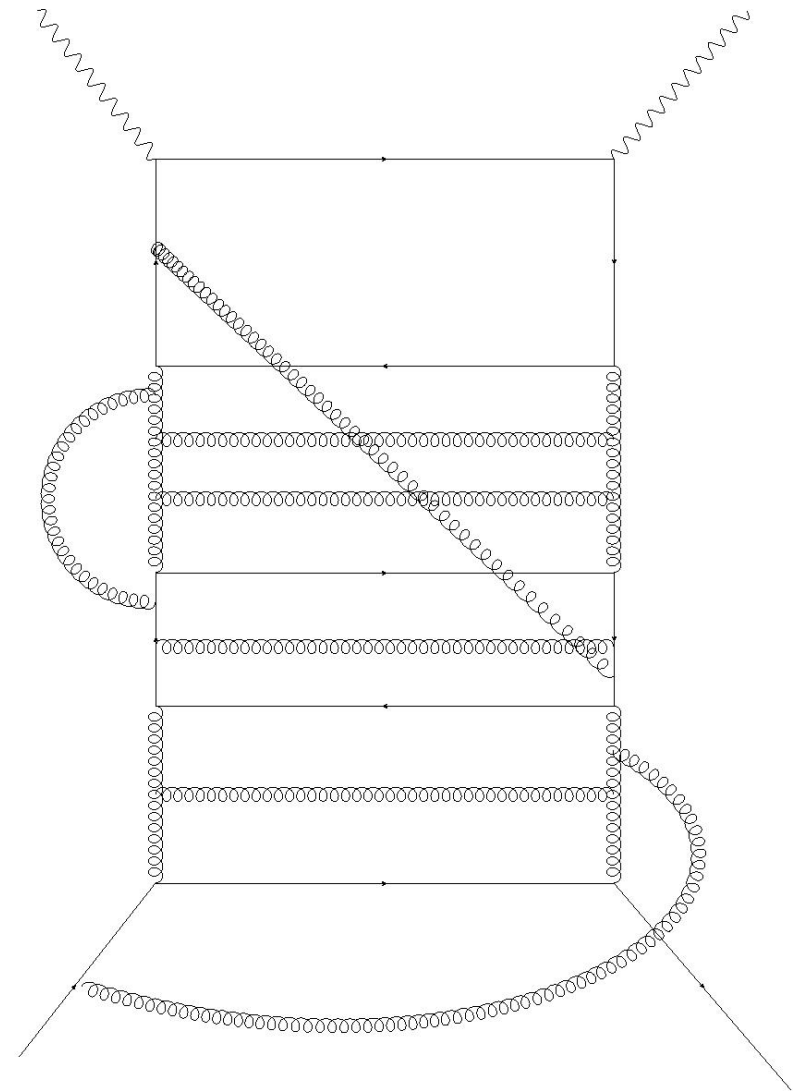
Unlike BFKL, we need to include non-ladder diagrams

Resummation very hard, but can be done!

Bartels, Ermolaev, Ryskin (1996)

$$\Delta q(x), \Delta G(x) \sim \frac{1}{x^\alpha}$$

$$\alpha \approx 3.664 \sqrt{\frac{\alpha_s N_c}{2\pi}}$$



Regge intercept at small-x, revisited

Bartels, Ermolaev, Ryskin (1996)

$$\Delta\gamma_{GG}^{BER}(\omega) = \frac{4\bar{\alpha}_s}{\omega} + \frac{8\bar{\alpha}_s^2}{\omega^3} + \frac{56\bar{\alpha}_s^3}{\omega^5} + \frac{504\bar{\alpha}_s^4}{\omega^7} + \dots$$

Borden, Kovchegov (2023)

$$\Delta\gamma_{GG}^{us}(\omega) = \frac{4\bar{\alpha}_s}{\omega} + \frac{8\bar{\alpha}_s^2}{\omega^3} + \frac{56\bar{\alpha}_s^3}{\omega^5} + \frac{496\bar{\alpha}_s^4}{\omega^7} + \dots$$

Based on Cougoulic, Kovchegov, Tarasov, Tawabutr (2022)

Discrepancy at 4-loops!

$$\Delta q(x), \Delta G(x) \sim \frac{1}{x^\alpha}$$

$$\alpha_{BER} \approx 3.664 \sqrt{\frac{\alpha_s N_c}{2\pi}}$$

$$\alpha_{BK} \approx 3.661 \sqrt{\frac{\alpha_s N_c}{2\pi}}$$

An elephant in the room: Orbital angular momentum

It's an undeniable fact that experimentally we know **nothing** about OAM.

Of course, this doesn't mean that OAM is unimportant.

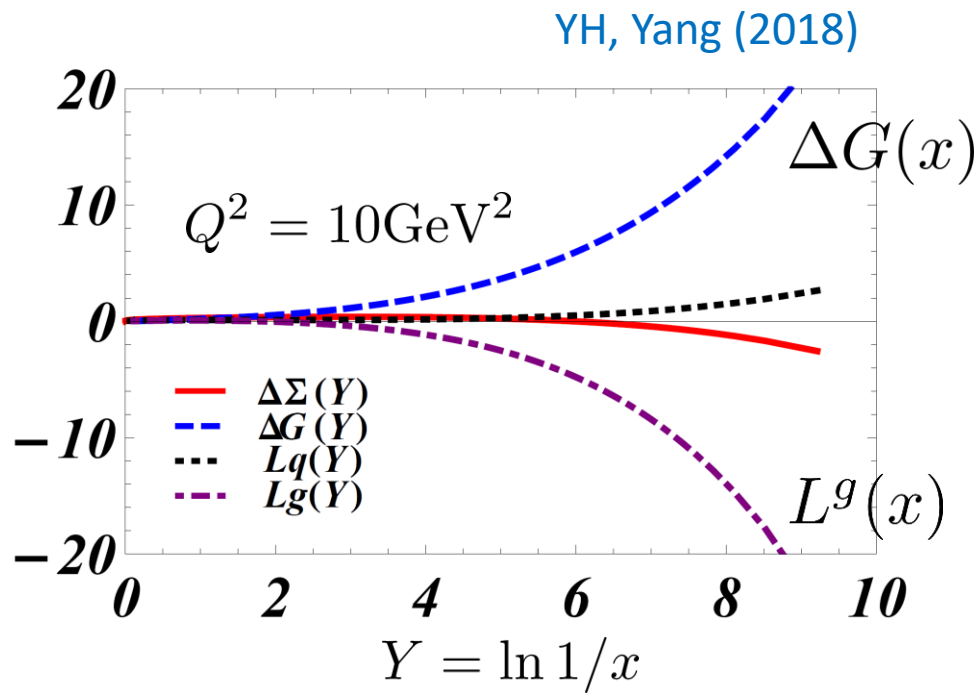
At small- x , helicity and OAM cancel.

$$\frac{d}{d \ln Q^2} L_g(x) = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dz}{z} (-2C_F + \dots) \Delta q(x/z)$$

$$\frac{d}{d \ln Q^2} \Delta G(x) = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dz}{z} (+2C_F + \dots) \Delta q(x/z)$$

Helicity-OAM cancellation at small-x

If $\Delta G(x) \sim \frac{1}{x^\alpha}$, then $L_g(x) \approx -\frac{2}{1+\alpha} \Delta G(x)$ Boussarie, YH, Yuan (2019)



There might be a sizable contribution to ΔG from the small-x region.

If so, there will be even larger L_g from the same x-region with an **opposite** sign.

Helicity is only half of the story.
Can EIC seriously address OAM?

OAM and the Wigner distribution

Wigner/GTMD distribution

Belitsky, Ji, Yuan (2004);

Phase space distribution of partons in QCD

$$W(x, \vec{k}_\perp, \vec{b}_\perp) = \int \frac{d^2 \Delta_\perp}{(2\pi)^2} \frac{dz^- d^2 z_\perp}{16\pi^3} e^{ixP^+ z^- - i\vec{k}_\perp \cdot \vec{z}_\perp} \langle P - \frac{\Delta}{2} | \bar{q}(b - z/2) \gamma^+ q(b + z/2) | P + \frac{\Delta}{2} \rangle$$

Define

$$L^{q,g} = \int dx \int d^2 b_\perp d^2 k_\perp (\vec{b}_\perp \times \vec{k}_\perp)_z W^{q,g}(x, \vec{b}_\perp, \vec{k}_\perp)$$

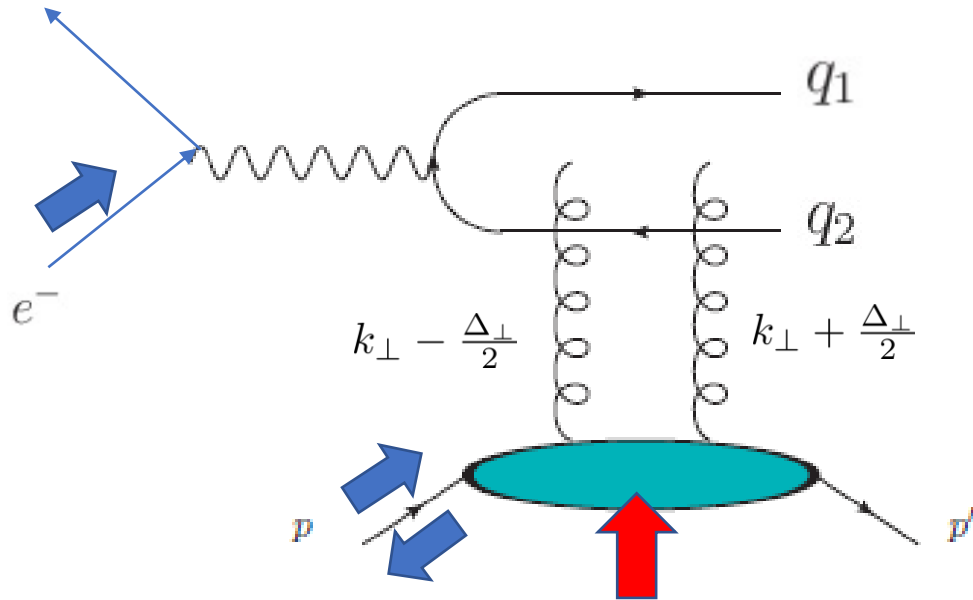
Lorce, Pasquini (2011);
YH (2011);
Ji, Xiong, Yuan (2012)

5D tomography encoded in the Wigner distribution—Holy grail of the nucleon structure
Can we probe it at the EIC?

Gluon OAM from single/double spin asymmetry in diffractive dijet

Ji, Yuan, Zhao (2016) (single)

Bhattacharya, Boussarie, YH (2022) (double)



Wigner distribution

Expand the amplitude to linear order in k_{\perp} (twist-3 effect)

$$\int d^2 k_{\perp} k_{\perp}^i W_g(k_{\perp}, \Delta_{\perp}) \sim \epsilon^{ij} \Delta_{\perp}^j L_g$$

$$d\sigma^{h_p h_l} \sim h_p h_l \cos(\phi_{l_{\perp}} - \phi_{\Delta_{\perp}}) \text{Re} \mathcal{H}_g^{(1)*} \left(\tilde{\mathcal{H}}_g^{(2)} + \frac{q_{\perp}^2 - \mu^2}{q_{\perp}^2 + \mu^2} \mathcal{L}_g \right)$$

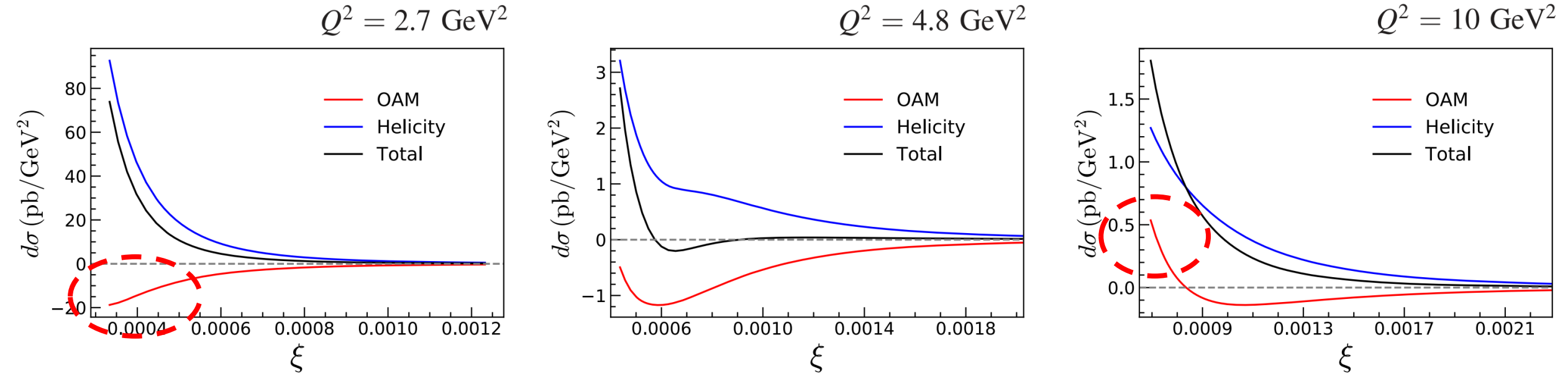
lepton angle

recoil proton angle

Compton form factors of gluon helicity and OAM

Prediction for EIC

Bhattacharya, Boussarie, YH (2022)



Depending on the sign of $q_{\perp}^2 - \frac{Q^2}{4}$, helicity and OAM add up/cancel.

First-ever quantitative prediction for an observable sensitive to OAM
To extract OAM, we need to know $\Delta G(x)$ precisely at small- x

In practice, jets at low momenta are hard to reconstruct.

Alternative measurement? [Bhattacharya, Boussarie, YH, in preparation](#)

Generalized Parton Distribution (GPD)

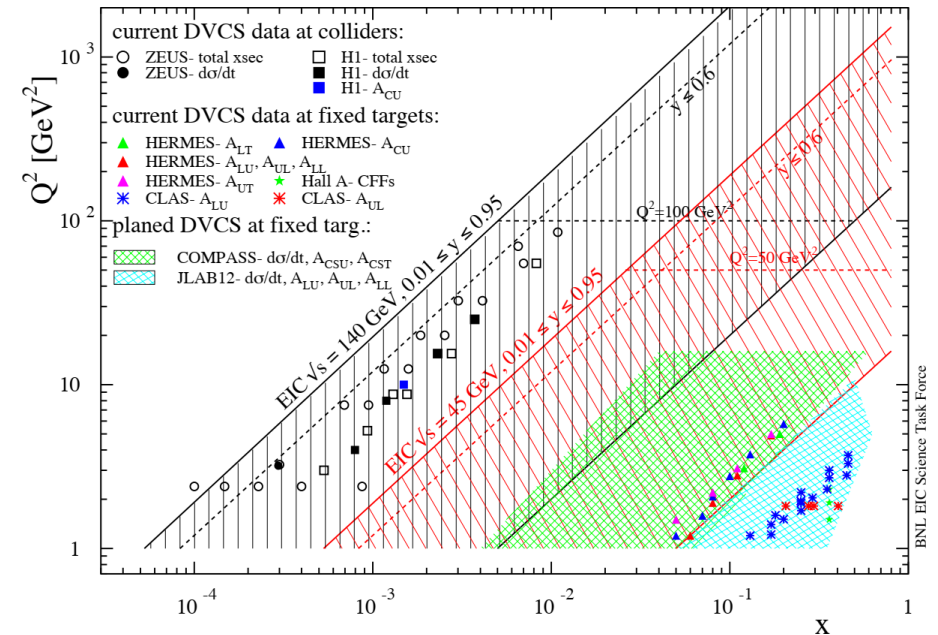
Off-forward generalization of PDF

$$\begin{aligned}
 & P^+ \int \frac{dy^-}{2\pi} e^{ixP^+y^-} \langle P' S' | \bar{\psi}(0) \gamma^\mu \psi(y^-) | PS \rangle \\
 &= H_q(x, \Delta) \bar{u}(P' S') \gamma^\mu u(PS) + E_q(x, \Delta) \bar{u}(P' S') \frac{i\sigma^{\mu\nu} \Delta_\nu}{2m} u(PS)
 \end{aligned}$$

Second moments relevant to Ji sum rule

$$J_{q,g} = \frac{1}{2} \int_0^1 dx x (H_{q,g}(x) + E_{q,g}(x))$$

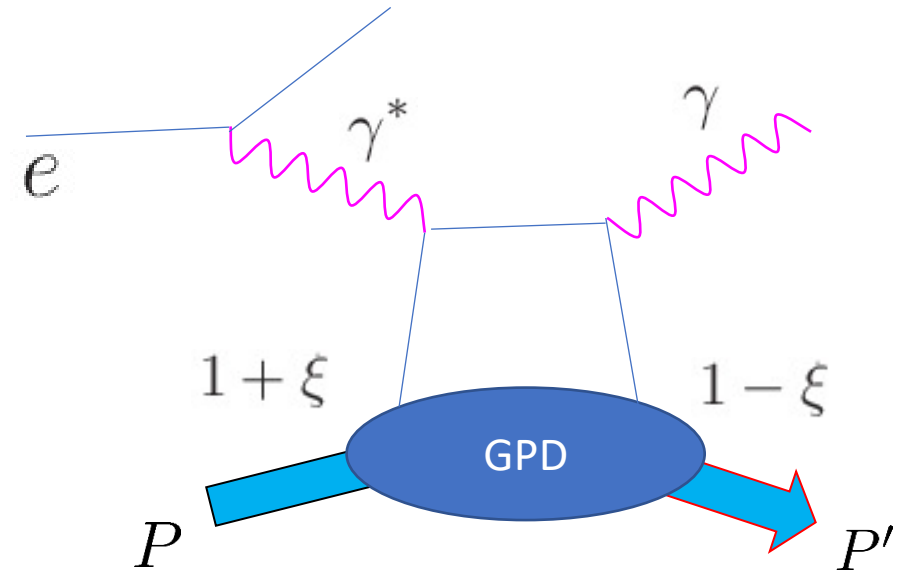
EIC offers an unprecedented kinematical coverage for DVCS and other exclusive processes. New era of GPD studies.



Deeply Virtual Compton Scattering

$$i \int d^4y e^{iqy} \langle P' | T \{ J^\mu(y) J^\nu(0) \} | P \rangle$$

$$= \frac{g_\perp^{\mu\nu}}{2P^+} \bar{u}(P_2) \left[\gamma^+ \mathcal{H} + \frac{i\sigma^{+\nu} \Delta_\nu}{2M} \mathcal{E} \right] u(P_2) + \dots$$



Compton form factors

$$\begin{pmatrix} \mathcal{H}(\xi) \\ \mathcal{E}(\xi) \end{pmatrix} = \int_{-1}^1 dx C_q(x, \xi) \begin{pmatrix} H_q(x, \xi) \\ E_q(x, \xi) \end{pmatrix} + \alpha_s \int_{-1}^1 dx C_g(x, \xi) \begin{pmatrix} H_g(x, \xi) \\ E_g(x, \xi) \end{pmatrix} + \dots$$

Ingredients for NNLO global analysis ready in near future [Braun, Ji, Schoenleber \(2023\)](#)

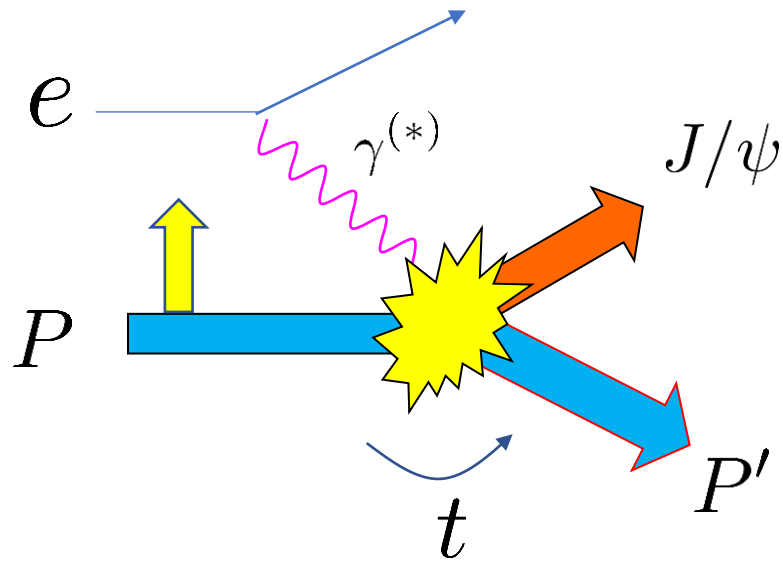
In practice, NLO global analysis is already a challenge [Kumericki,...](#)

Very hard to access GPD E, especially the gluon one.

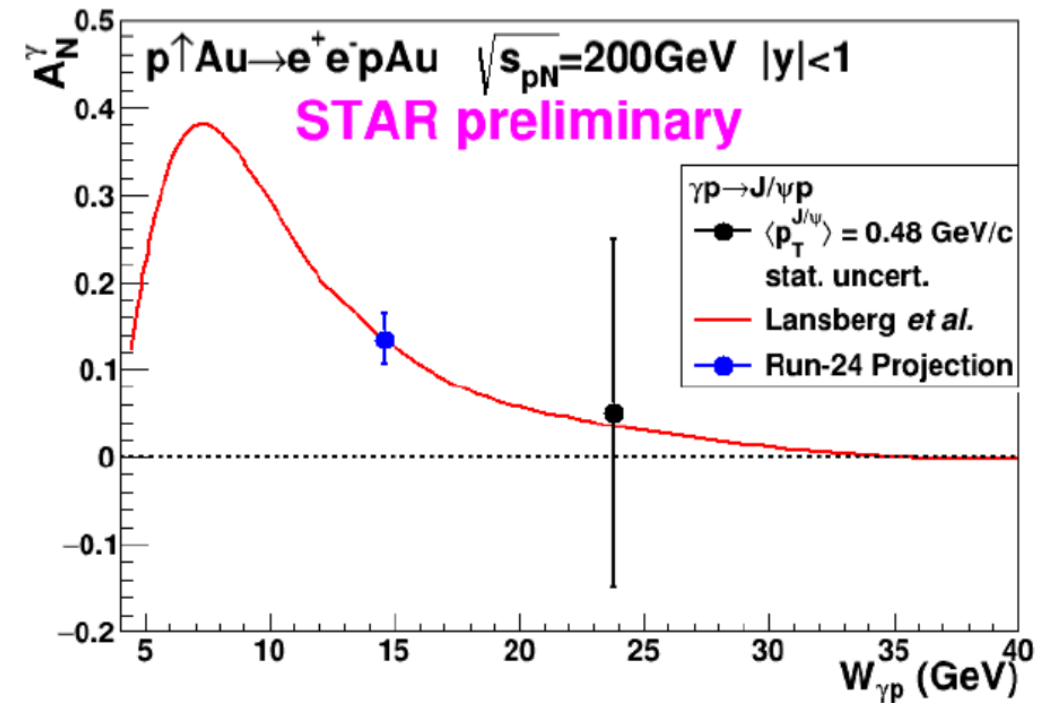
GPD E_g from J/ψ single spin asymmetry

Koempel, Kroll, Metz, Zhou (2012)

Lansberg, Massacrier, Szymanowski, Wagner (2018)



$$A_N \sim \frac{\text{Im}(\mathcal{H}_g^* \mathcal{E}_g)}{|\mathcal{H}_g|^2}$$



Will be measured by the STAR collaboration in UPC

Can be continued at the EIC

Gluon GPD $E_g(x)$ at small- x

YH, Zhou (2022)

Nucleon **helicity non-flip** $xH_g(x) = xG(x) = \int d^2k_{\perp} \mathcal{G}(x, k_{\perp})$

$$\sim \left(\frac{1}{x}\right)^{4 \ln 2 \bar{\alpha}_s} \quad \text{BFKL pomeron}$$

Nucleon **helicity flip** $xE_g(x) = \int d^2k_{\perp} \mathcal{E}(x, k_{\perp})$

$$\sim \left(\frac{1}{x}\right)^{??}$$

Introduce k_{\perp} -dependence in GPD \rightarrow GTMD

Recent theory developments in GTMD help solve this problem

Small-x evolution equation for $E_g(x)$

YH, Zhou (2022)

$$\partial_Y \mathcal{E}(k_\perp) = \frac{\bar{\alpha}_s}{\pi} \int \frac{d^2 k'_\perp}{(k_\perp - k'_\perp)^2} \left[\mathcal{E}(k'_\perp) - \frac{k_\perp^2}{2k'_\perp{}^2} \mathcal{E}(k_\perp) \right] - 4\pi^2 \alpha_s^2 \bar{\mathcal{F}}_{1,1}(k_\perp) \mathcal{E}(k_\perp)$$

$$Y = \ln 1/x$$

$$xE_g(x) \sim xG(x) \propto \left(\frac{1}{x}\right)^{\bar{\alpha}_s 4 \ln 2}$$

BFKL Pomeron behavior, the **same** as unpol gluon PDF
Eventually reaches **gluon saturation**.

$$J_g = \frac{1}{2} \int_0^1 dx \, x [H_g(x, \xi) + E_g(x, \xi)]$$

Nucleon electric dipole moment (EDM)

If nonvanishing, both P and CP are violated.

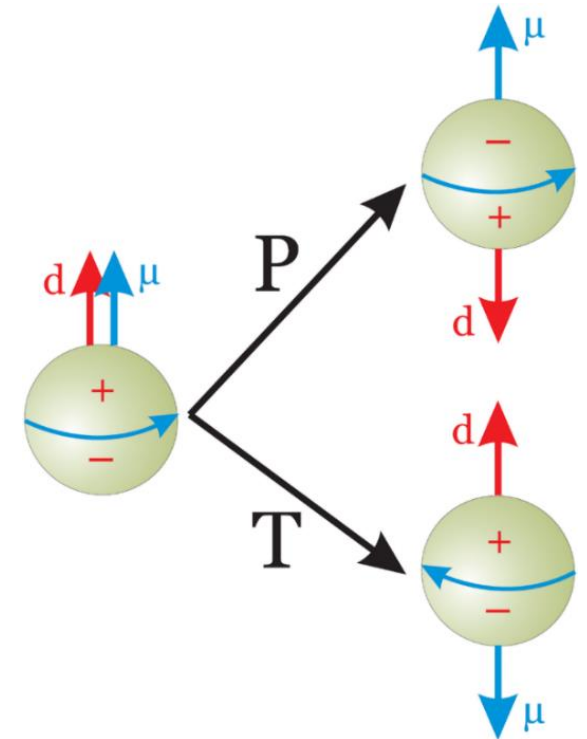
CKM mechanism gives a too small value of nucleon EDM,

CP violation from BSM physics?

Various CP-violating operators studied

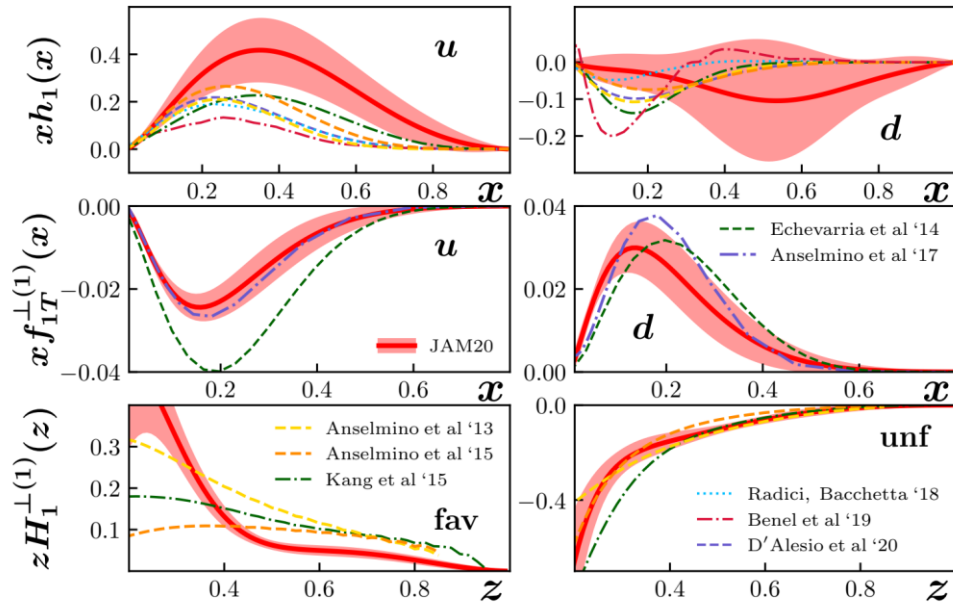
- Theta term $\frac{\theta\alpha_s}{8\pi} F\tilde{F}$
- Quark EDM operator $m_q\bar{\psi}_q F^{\mu\nu}\sigma_{\mu\nu}i\gamma_5\psi_q$
- Weinberg operator $f_{abc}\tilde{F}_{\mu\nu}^a F_b^{\mu\rho} F_{c\rho}^\nu$
- ...

EDM is a vector, must be proportional to nucleon spin
Any connection to high energy QCD spin physics at EIC?



Global analysis of SSA

Cammarota, Gamberg, Kang, Miller, Pitonyak, Prokudin, Rogers, Sato (2020)

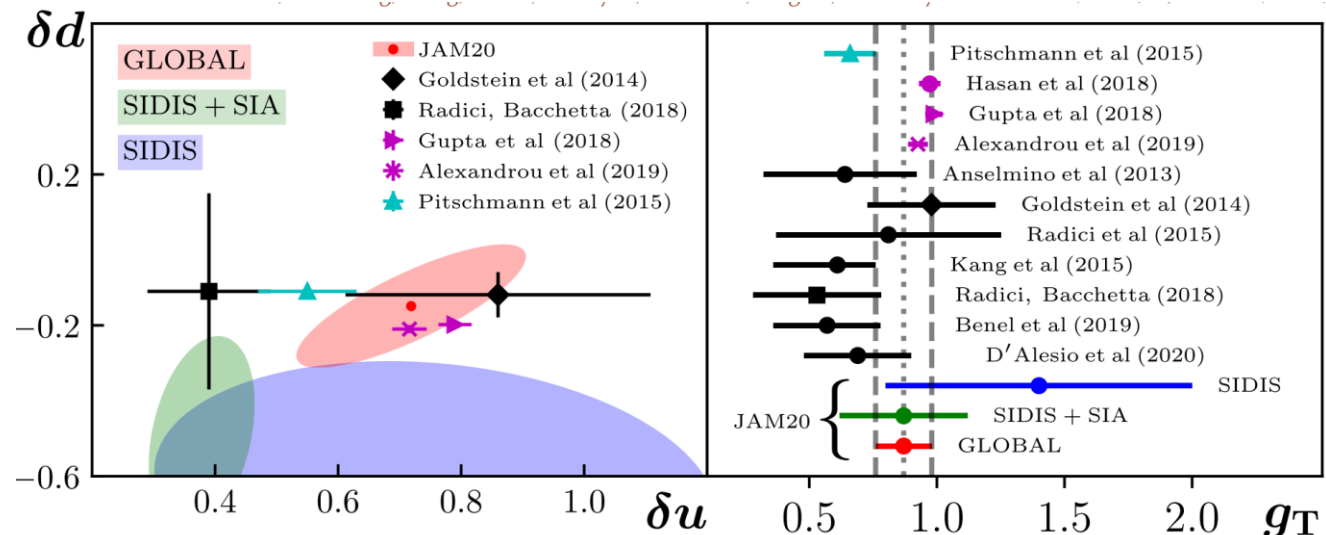


Simultaneous fit of

e+e- (BELLE, BaBar, BESIII)
 SIDIS (COMPASS, HERMES, Jlab) ← input from EIC in future
 Drell-Yan (COMPASS, STAR)
 pp (STAR, PHENIX, BRAHMS)

At the moment, the only viable way to generate O(10%) asymmetry seems to be **twist-3 FFs** convoluted with the **transversity** distribution.

- Constraints on the nucleon **tensor charge**.
- Constraints on the quark EDM operator



Connecting Weinberg operator to higher-twist effect in polarized DIS

YH (2020)

Exact identity

$$gf_{abc}\tilde{F}_{\mu\nu}^a F_b^{\mu\alpha} F_{c\alpha}^\nu = -\partial^\mu (\tilde{F}_{\mu\nu} \overleftrightarrow{D}_\alpha F^{\nu\alpha}) - \frac{1}{2} \tilde{F}_{\mu\nu} \overleftrightarrow{D}^2 F^{\mu\nu}$$

$$\langle p' | \mathcal{O}_W | p \rangle \approx i\Delta^\mu \langle p | \bar{\psi} g \tilde{F}_{\mu\nu} \gamma^\nu \psi | p \rangle + \dots$$

This matrix element enters the twist-4 correction in polarized DIS [Shuryak, Vainshtein \(1982\)](#)

First moment of g1

$$\int_0^1 g_1^{p,n}(x, Q^2) dx = \left(\pm \frac{1}{12} g_A + \frac{1}{36} a_8 \right) \left(1 - \frac{\alpha_s}{\pi} + \mathcal{O}(\alpha_s^2) \right) + \frac{1}{9} \Delta\Sigma \left(1 - \frac{33 - 8N_f}{33 - 2N_f} \frac{\alpha_s}{\pi} + \mathcal{O}(\alpha_s^2) \right) - \frac{8}{9Q^2} \left[\left\{ \pm \frac{1}{12} f_3 + \frac{1}{36} f_8 \right\} \left(\frac{\alpha_s(Q_0^2)}{\alpha_s(Q^2)} \right)^{-\frac{\gamma_{NS}^0}{2\beta_0}} + \frac{1}{9} f_0 \left(\frac{\alpha_s(Q_0^2)}{\alpha_s(Q^2)} \right)^{-\frac{1}{2\beta_0} (\gamma_{NS}^0 + \frac{4}{3} N_f)} \right],$$

An estimate of EDM

YH (2021)

'One-nucleon reducible' contribution to EDM [Bigi, Uraltsev \(1990\)](#)

$$d \sim \mu \frac{\langle p' | w \mathcal{O}_W | p \rangle}{m_N \bar{u}(p') i \gamma_5 u(p)} \equiv 4\mu m_N^2 E$$

↑
magnetic moment

Vary E in the window $0.5f_0 < E < 1.3f_0$

f_0 from instanton model. [Balla, Polyakov, Weiss \(1998\)](#)

$$-12w' e \text{ MeV} < d_p < -32w' e \text{ MeV} \quad 22w' e \text{ MeV} < d_n < 8.4w' e \text{ MeV}$$

Can we measure f_0 at the EIC?

New connection between EIC spin and BSM physics

Summary

- Spin is one of the core science cases of EIC
- OAM is the key to fulfill the JM spin sum rule. Lagging far behind in both theory and experiment, but a glimmer of hope.
- EIC offers great opportunities for GPD studies. From spin physics perspective, extraction of GPD E is a major challenge.