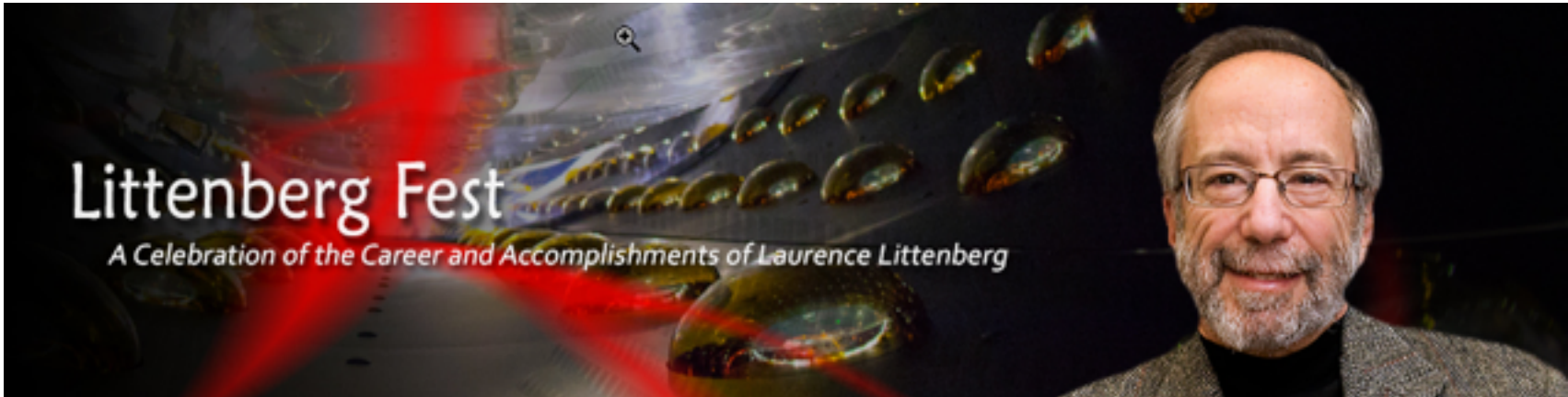


Rare Kaon Decays

German Valencia



Littenberg Fest

A Celebration of the Career and Accomplishments of Laurence Littenberg



$$K \rightarrow \pi \nu \bar{\nu}$$

- At the Littenberg fest we have to talk about the 'Littenberg mode'.
- We have already heard about this in this FEST, but I will try to add a theory perspective
- precise determination of SM parameters
- or: **ruling out** new physics for over 25 years

G. Valencia, Monash University

reviews on rare kaon decays

- SUSY John Hagelin

Rare Kaon Decays Prog.Part.Nucl.Phys. 23 (1989) 1

JOHN S. HAGELIN* and LAURENCE S. LITTENBERG†

**Maharishi International University, Fairfield, IA 52556, U.S.A.*

†Brookhaven National Laboratory, Upton, NY 11973, U.S.A.

- ChPT, long distance

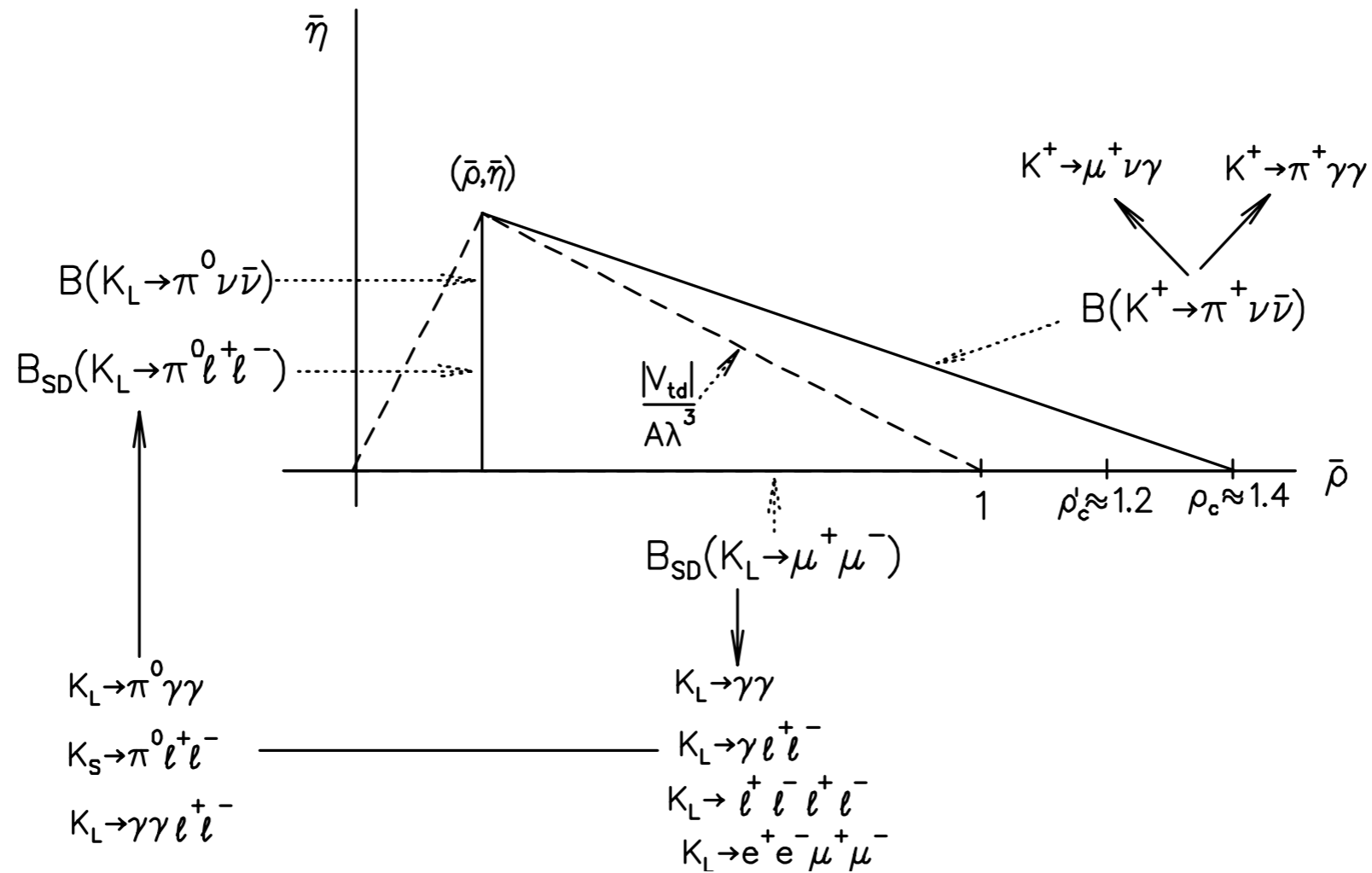
**RARE AND RADIATIVE
KAON DECAYS** Ann.Rev.Nucl.Part.Sci. 43 (1993) 729-792

L. Littenberg¹ and G. Valencia²

¹Physics Department, Brookhaven National Laboratory, Upton, NY 11973;

²Theoretical Physics, Fermi National Accelerator Laboratory, Batavia, IL
60510

Rare Kaon Decays - PDB

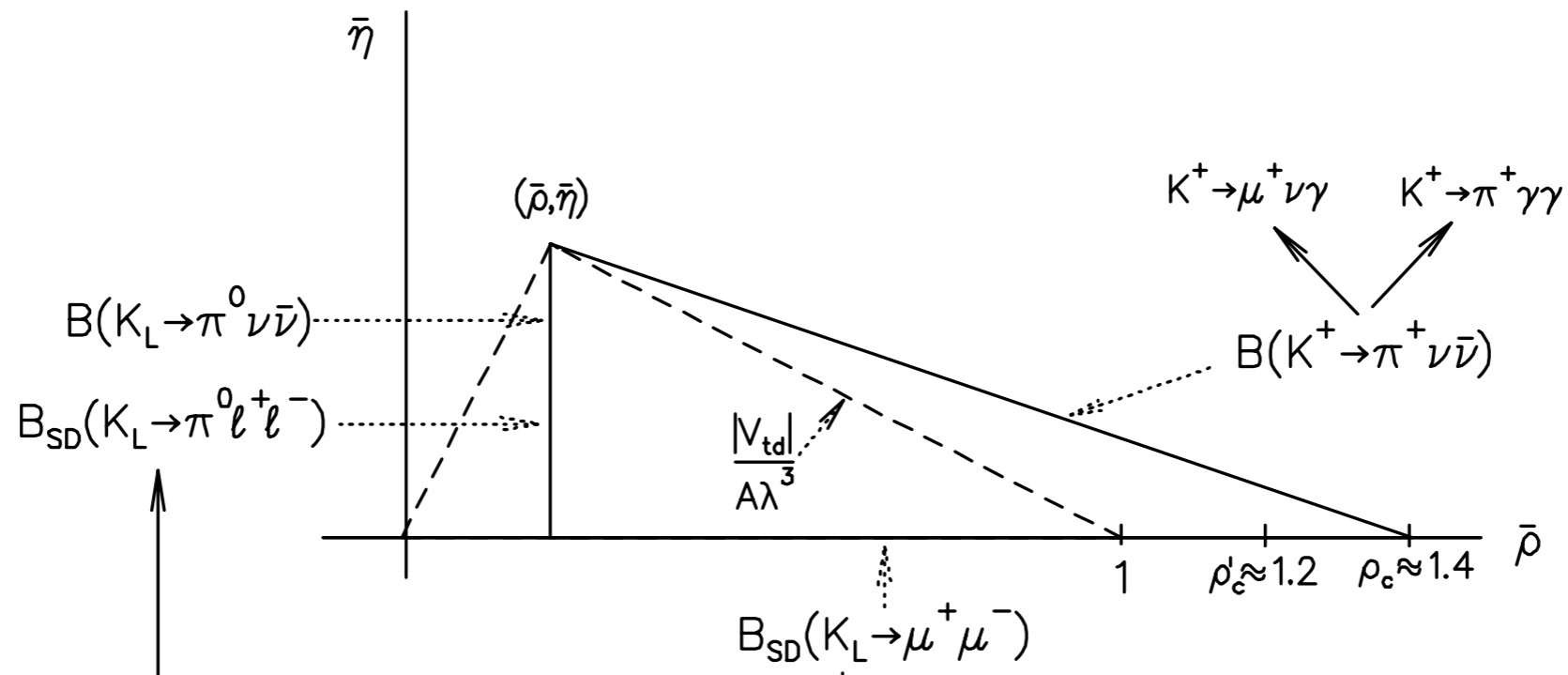


Mode	90% CL upper limit	Exp't	Yr./Ref.
$K^+ \rightarrow \pi^+ e^- \mu^+$	1.2×10^{-11}	BNL-865	2005/Ref. 21
$K^+ \rightarrow \pi^+ e^+ \mu^-$	5.2×10^{-10}	BNL-865	2000/Ref. 18
$K_L \rightarrow \mu e$	4.7×10^{-12}	BNL-871	1998/Ref. 22
$K_L \rightarrow \pi^0 e \mu$	7.6×10^{-11}	KTeV	2008/Ref. 23
$K_L \rightarrow \pi^0 \pi^0 e \mu$	1.7×10^{-10}	KTeV	2008/Ref. 23

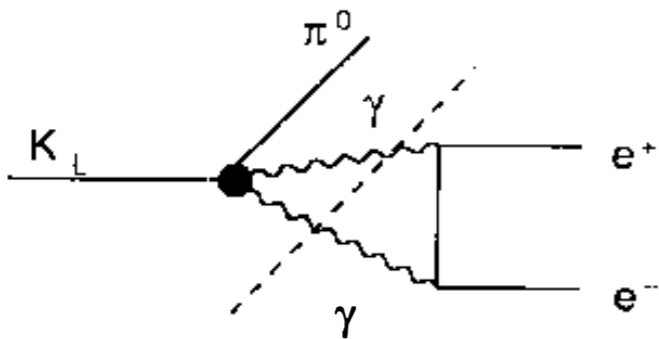
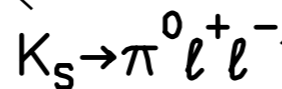
$\Lambda_{NP} > 100 \text{ TeV}$

CMS $h \rightarrow \mu \tau$??

Rare Kaon Decays



$$B_{CPV} \approx 10^{-12} \left[15.7 |a_S|^2 \pm 1.4 \left(\frac{|V_{cb}|^2 \bar{\eta}}{10^{-4}} \right) |a_S| + 0.12 \left(\frac{|V_{cb}|^2 \bar{\eta}}{10^{-4}} \right)^2 \right] \approx (3.1 \pm 0.9) \times 10^{-11}$$



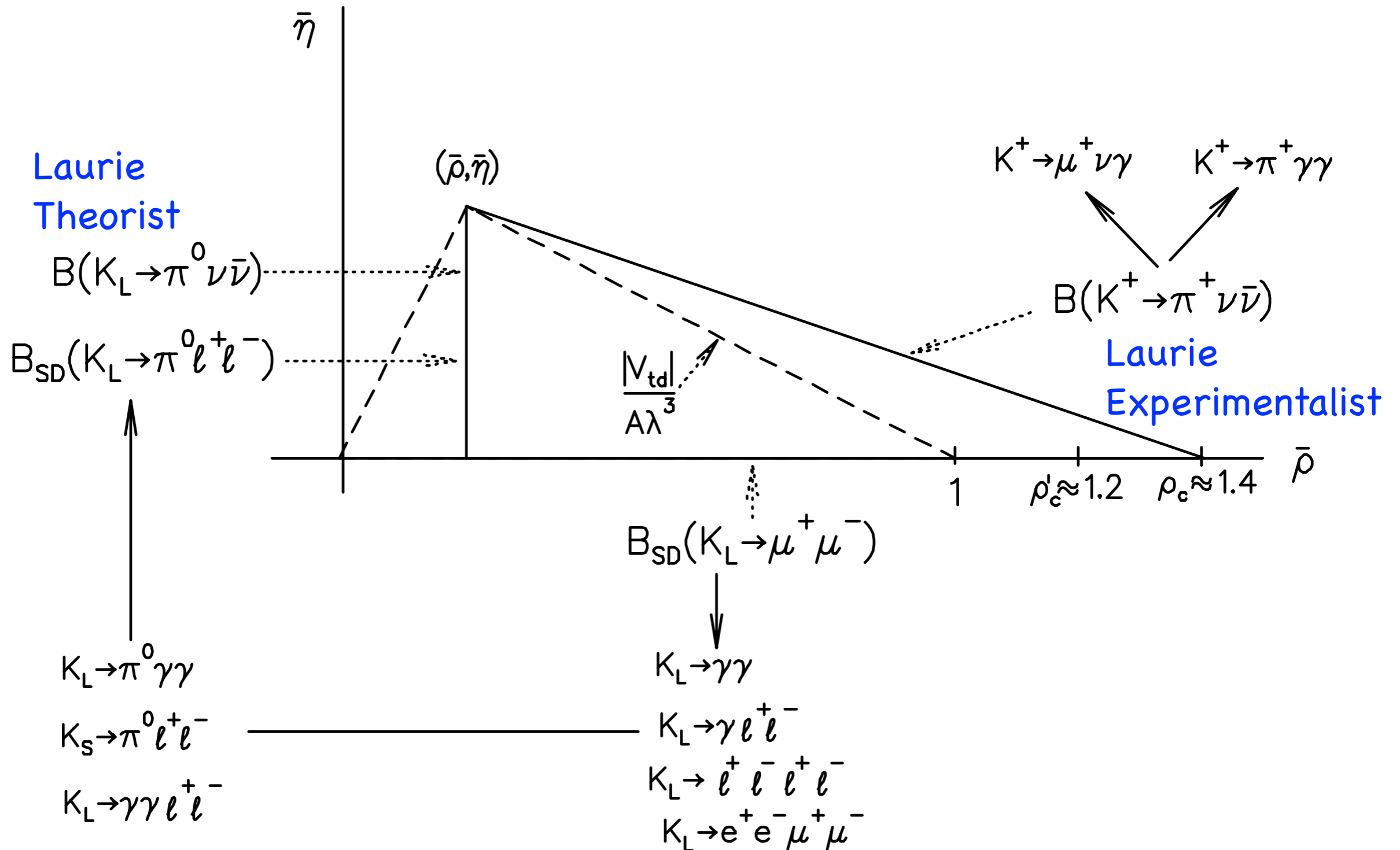
B_{CP} around 10^{-13}

background

$$K_L \rightarrow \pi^0 \gamma e^+ e^-$$

$$K_L \rightarrow \pi^0 \gamma \gamma e^+ e^- \sim \mathcal{O}(10^{-10})$$

Rare Kaon Decays



Laurie's paper

PHYSICAL REVIEW D

VOLUME 39, NUMBER 11

1 JUNE

CP-violating decay $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$

Laurence S. Littenberg

Department of Physics, Brookhaven National Laboratory, Upton, New York 11973

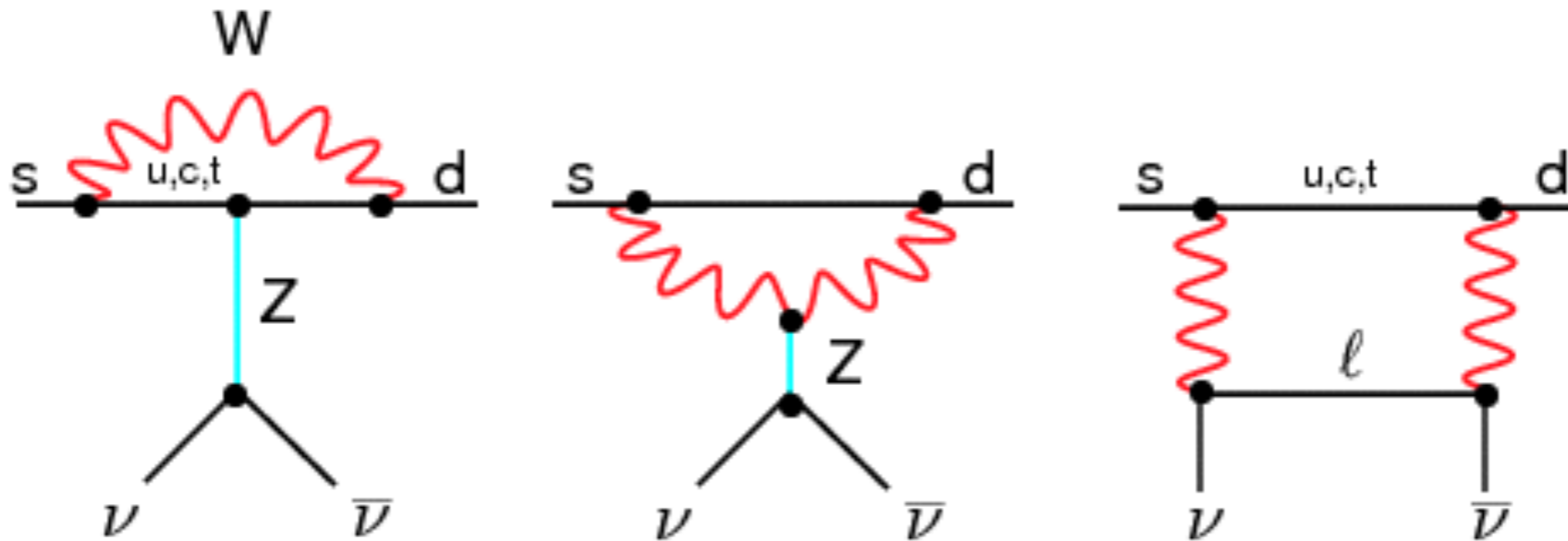
(Received 6 January 1989)

The process $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ offers perhaps the clearest window yet proposed into the origin of *CP* violation. The largest expected contribution to this decay is a direct *CP*-violating term at $\approx \text{few} \times 10^{-12}$. The indirect *CP*-violating contribution is some 3 orders of magnitude smaller, and *CP*-conserving contributions are also estimated to be extremely small. Although this decay has never been directly probed, a branching ratio upper limit of $\sim 1\%$ can be extracted from previous data on $K_L^0 \rightarrow 2\pi^0$. This leaves an enormous range in which to search for new physics. If the Kobayashi-Maskawa (KM) model prediction can be reached, a theoretically clean determination of the KM product $\sin\theta_2 \sin\theta_3 \sin\delta$ can be made.

$$\begin{aligned} B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu})_{\epsilon} &= 5.18 \times 10^{-6} \times 4.18 \times 3 \\ &\quad \times 0.70 \times 10^{-6} (10.99 \times 10^{-3})^2 \\ &\approx 5.5 \times 10^{-15} \\ B(K_L^0 \rightarrow \pi^0 \nu \bar{\nu})_{\text{direct}} &= 4.18 \times 3 \\ &\quad \times 0.70 \times 10^{-6} (1.07 \times 10^{-3})^2 \\ &\approx 10^{-11} . \end{aligned}$$

Basics in SM

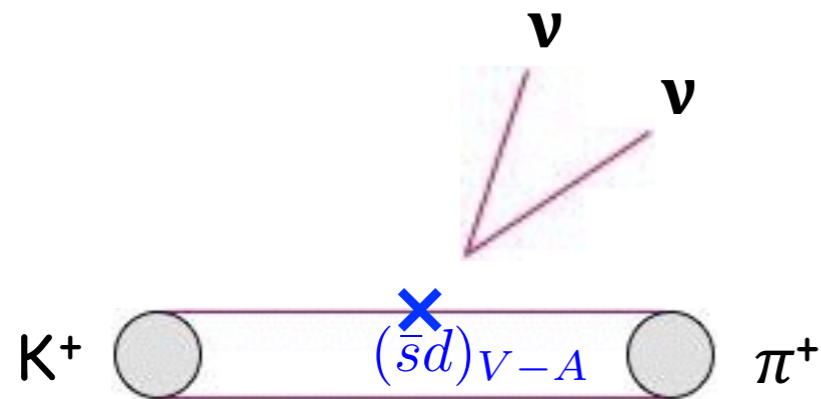
Inami-Lim



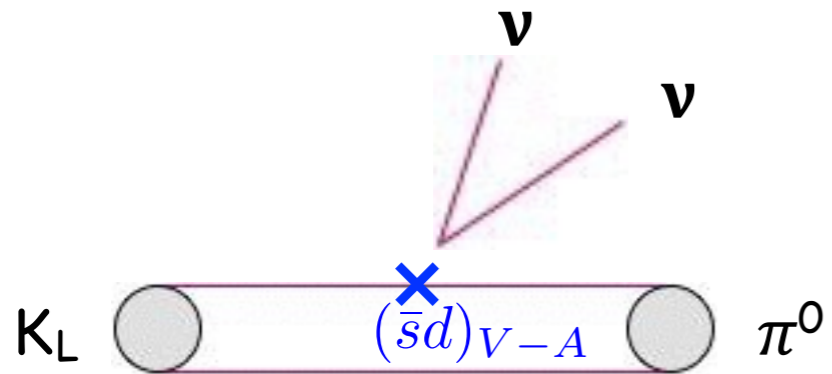
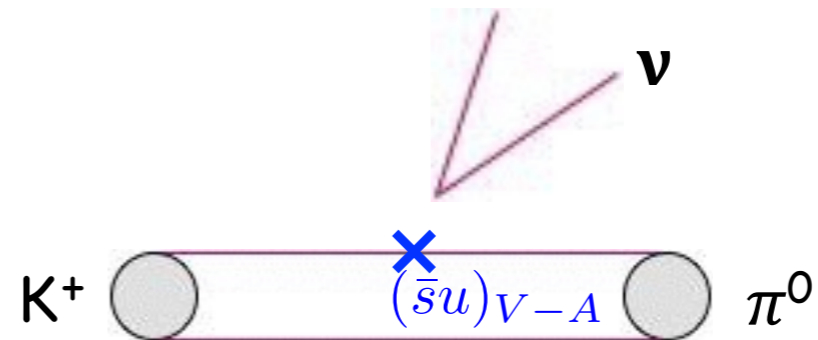
$$\mathcal{A}_q(s \rightarrow d\nu\bar{\nu}) \propto \lambda_q m_q^2 \propto \begin{cases} m_t^2 (\lambda^5 + i\lambda^5), & q = t, \\ m_c^2 (\lambda + i\lambda^5), & q = c, \\ \Lambda_{\text{QCD}}^2 \lambda, & q = u, \end{cases}$$

charm contributes to real part, K^+
but irrelevant for imaginary part K_L

Isospin and isospin breaking



$$\langle \pi^+ | (\bar{s}d)_{V-A} | K^+ \rangle = \sqrt{2} \langle \pi^0 | (\bar{s}u)_{V-A} | K^+ \rangle.$$



$$\langle \pi^0 | (\bar{d}s)_{V-A} | \bar{K}^0 \rangle = \langle \pi^0 | (\bar{s}u)_{V-A} | K^+ \rangle$$

- isospin breaking corrections: quark masses, electroweak radiative corrections
- reduce $B(K^+ \rightarrow \pi^+ \nu\nu)$ and $B(K_L \rightarrow \pi^0 \nu\nu)$ relative to $B(K^+ \rightarrow \pi^0 e^+ \nu)$ by 10% and 5.6%, respectively

W.J. Marciano, Zohreh Parsa Phys.Rev. D53 (1996) 1-5

Latest (?) results

$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}(\gamma)) = \kappa_+ (1 + \Delta_{\text{EM}}) \left[\left(\frac{\text{Im}(V_{ts}^* V_{td})}{\lambda^5} X_t \right)^2 + \left(\frac{\text{Re}(V_{cs}^* V_{cd})}{\lambda} (P_c + \delta P_{c,u}) + \frac{\text{Re}(V_{ts}^* V_{td})}{\lambda^5} X_t \right)^2 \right].$$

$$\kappa_+ = r_{K^+} \frac{3\alpha^2 \text{Br}(K^+ \rightarrow \pi^0 e^+ \nu)}{2\pi^2 \sin^4 \Theta_W} \lambda^8$$

NNLO QCD, 2 loop EW

long distance

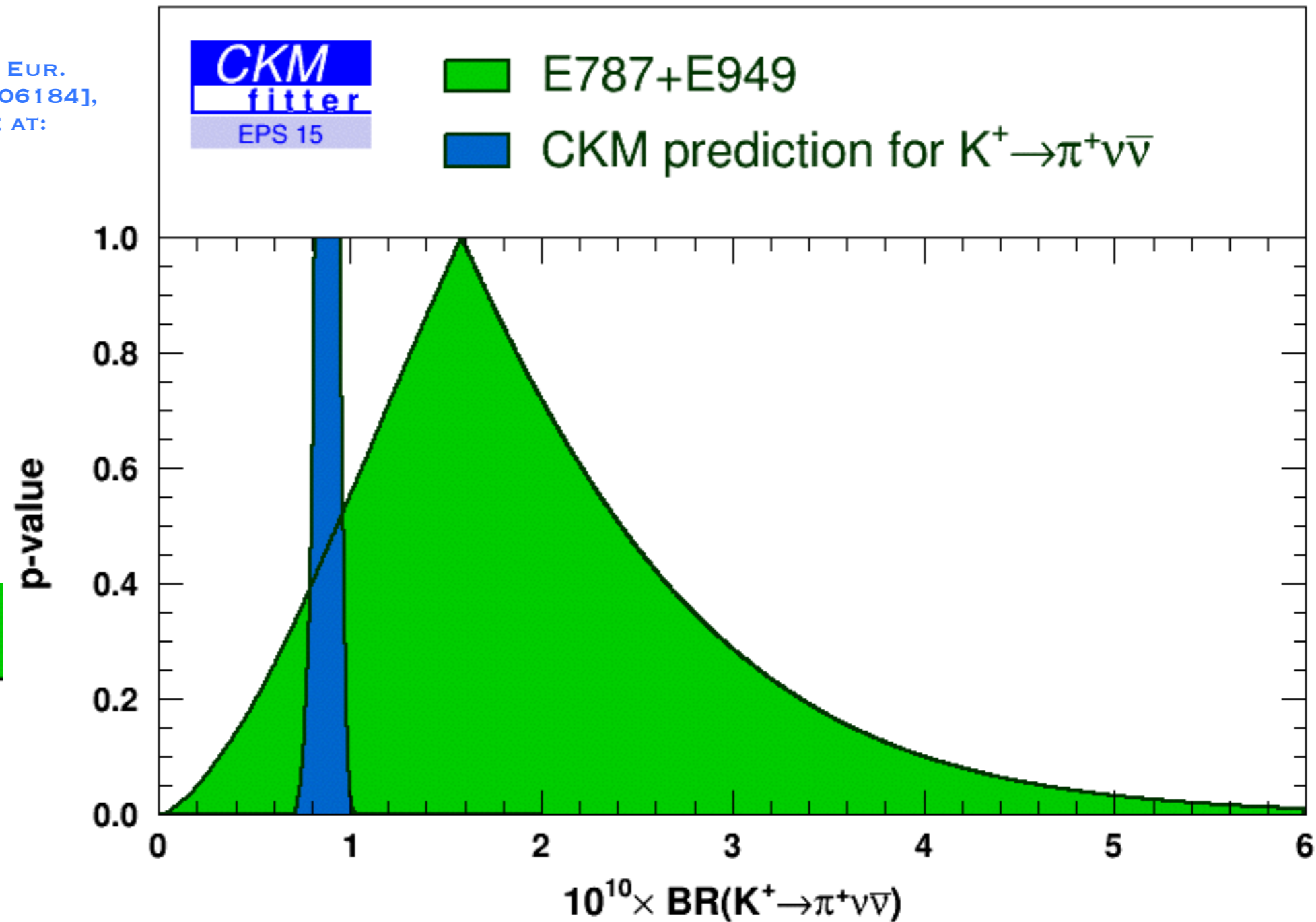
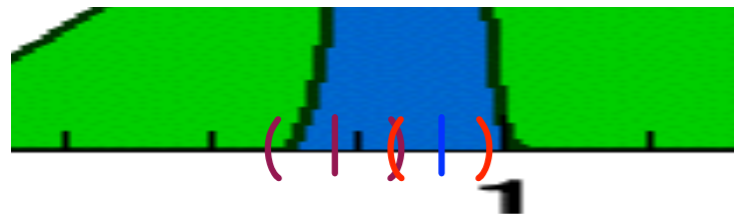
NLO QCD and 2 loop EW

$$B(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \kappa_L \left(\frac{\text{Im}(V_{ts}^* V_{td})}{\lambda^5} X_t \right)^2$$

$$\kappa_L = \frac{r_{K_L}}{r_{K^+}} \frac{\tau(K_L)}{\tau(K^+)} \kappa_+ = 1.80 \cdot 10^{-10}$$

latest numerical results K^+

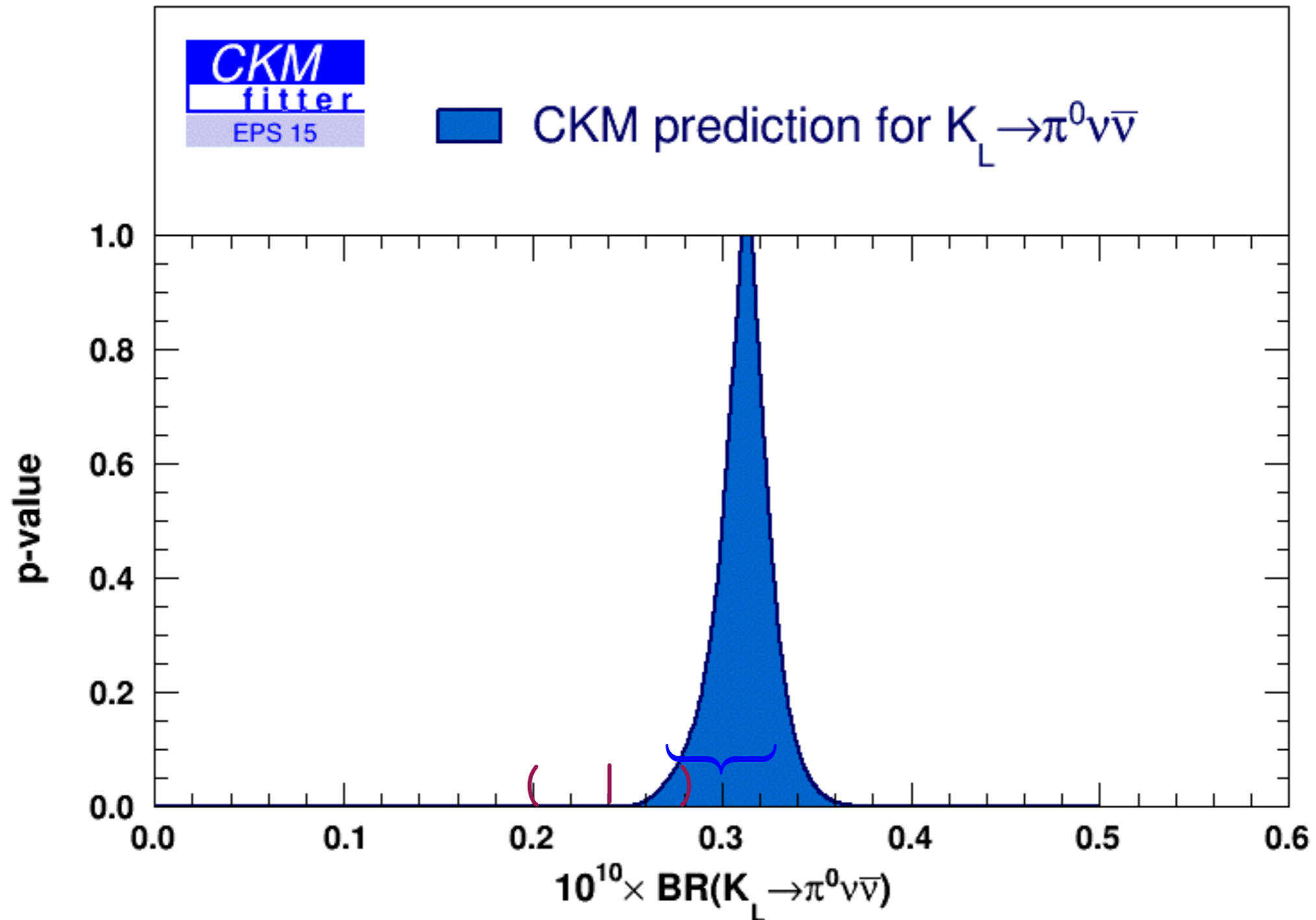
CKMFITTER GROUP (J. CHARLES ET AL.), EUR. PHYS. J. C41, 1-131 (2005) [HEP-PH/0406184],
UPDATED RESULTS AND PLOTS AVAILABLE AT:
[HTTP://CKMFITTER.IN2P3.FR](http://ckmfitter.in2p3.fr)



Brod, Gorbahn, Stamou 2011: $(7.81^{+0.80}_{-0.71} \pm 0.29) \times 10^{-11}$

Buras, Buttazzo, Girschbach-Noe, Knegjens 2015: $(9.11 \pm 0.72) \times 10^{-11}$

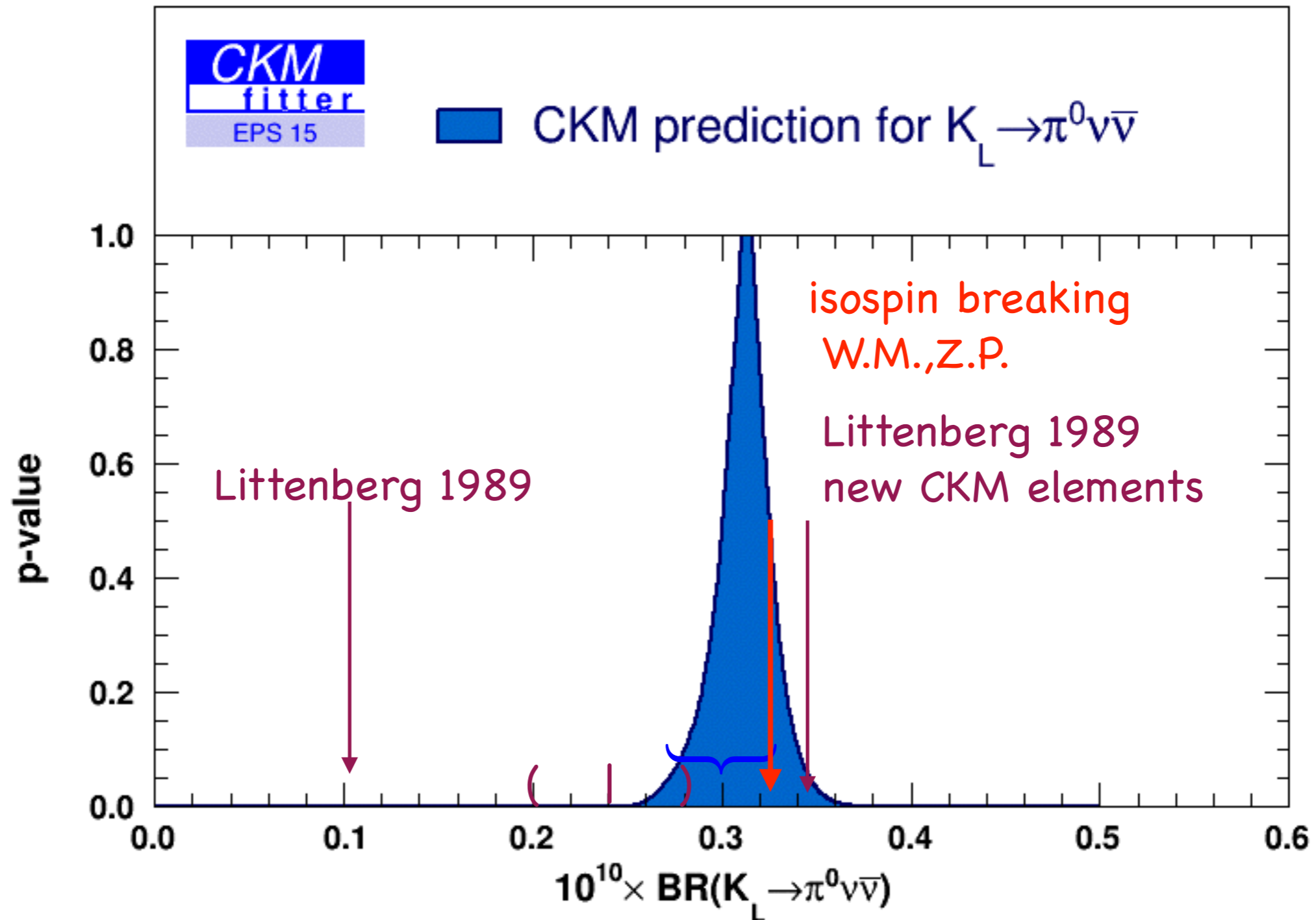
latest numerical results K_L



Brod, Gorbahn, Stamou 2011: $(2.43^{+0.40}_{-0.37} \pm 0.06) \times 10^{-11}$

Buras, Buttazzo, Girschbach-Noe, Knegjens 2015: $(3.00 \pm 0.30) \times 10^{-11}$

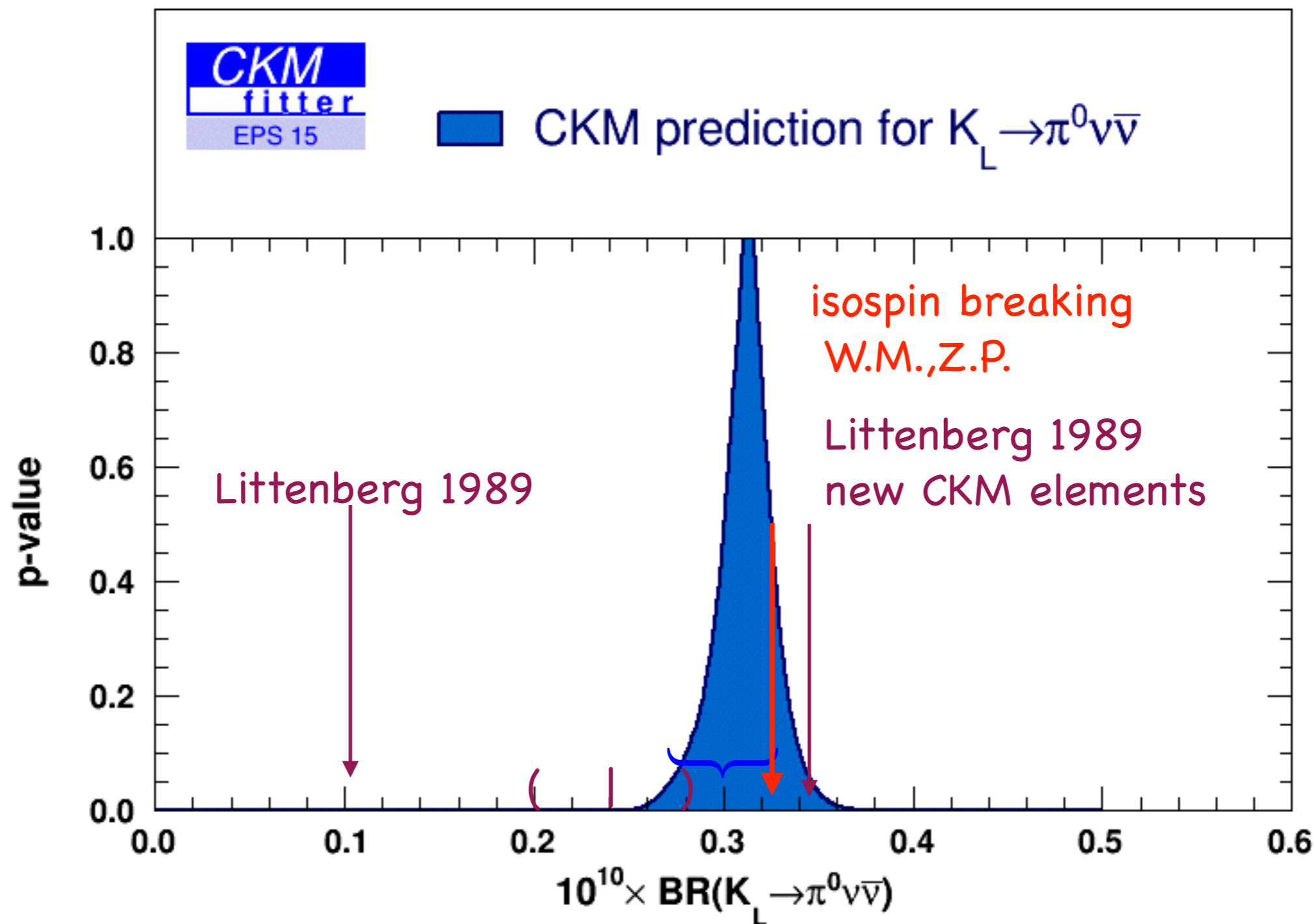
add Laurie's result



Brod, Gorbahn, Stamou 2011: $(2.43^{+0.40}_{-0.37} \pm 0.06) \times 10^{-11}$

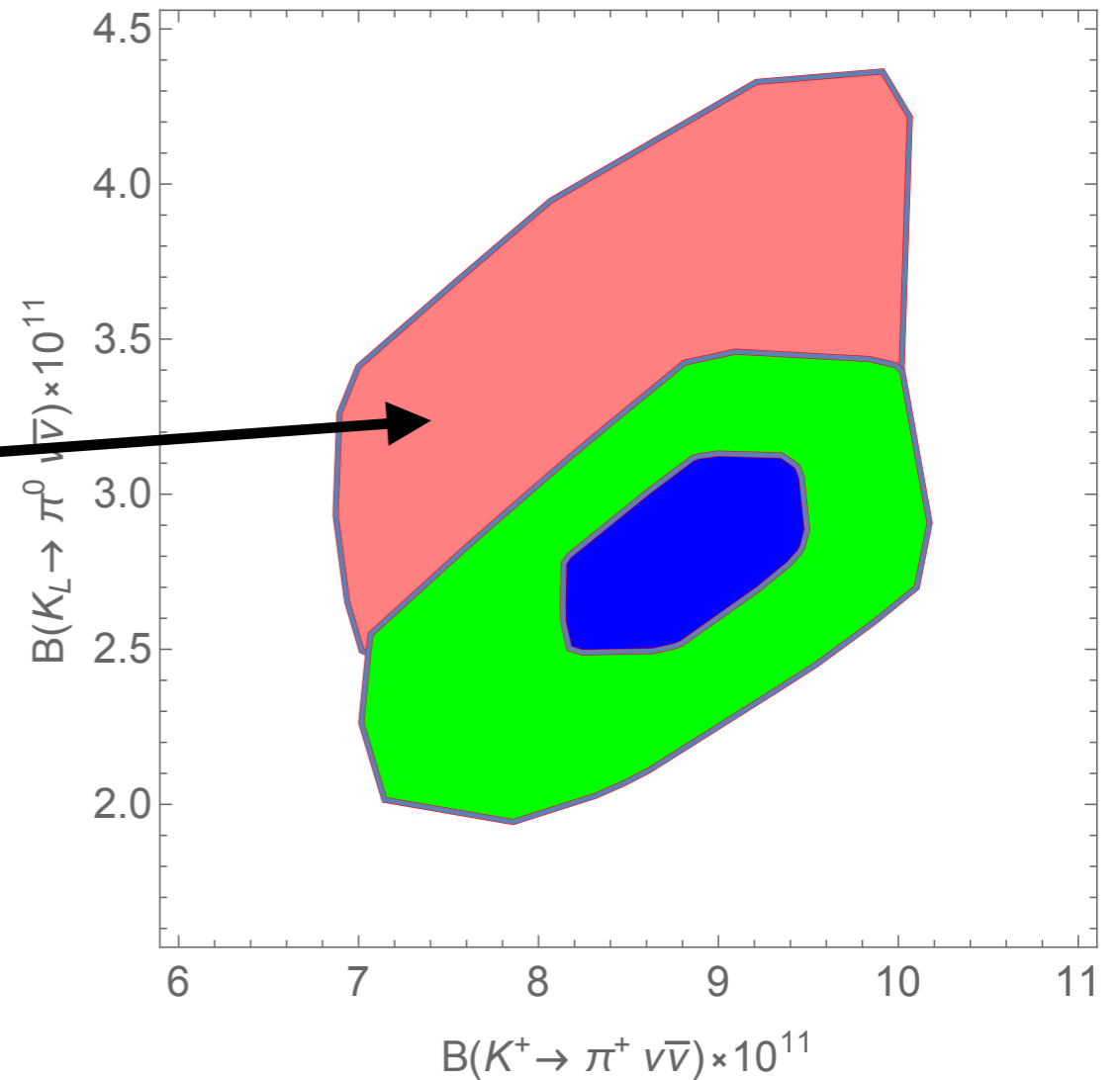
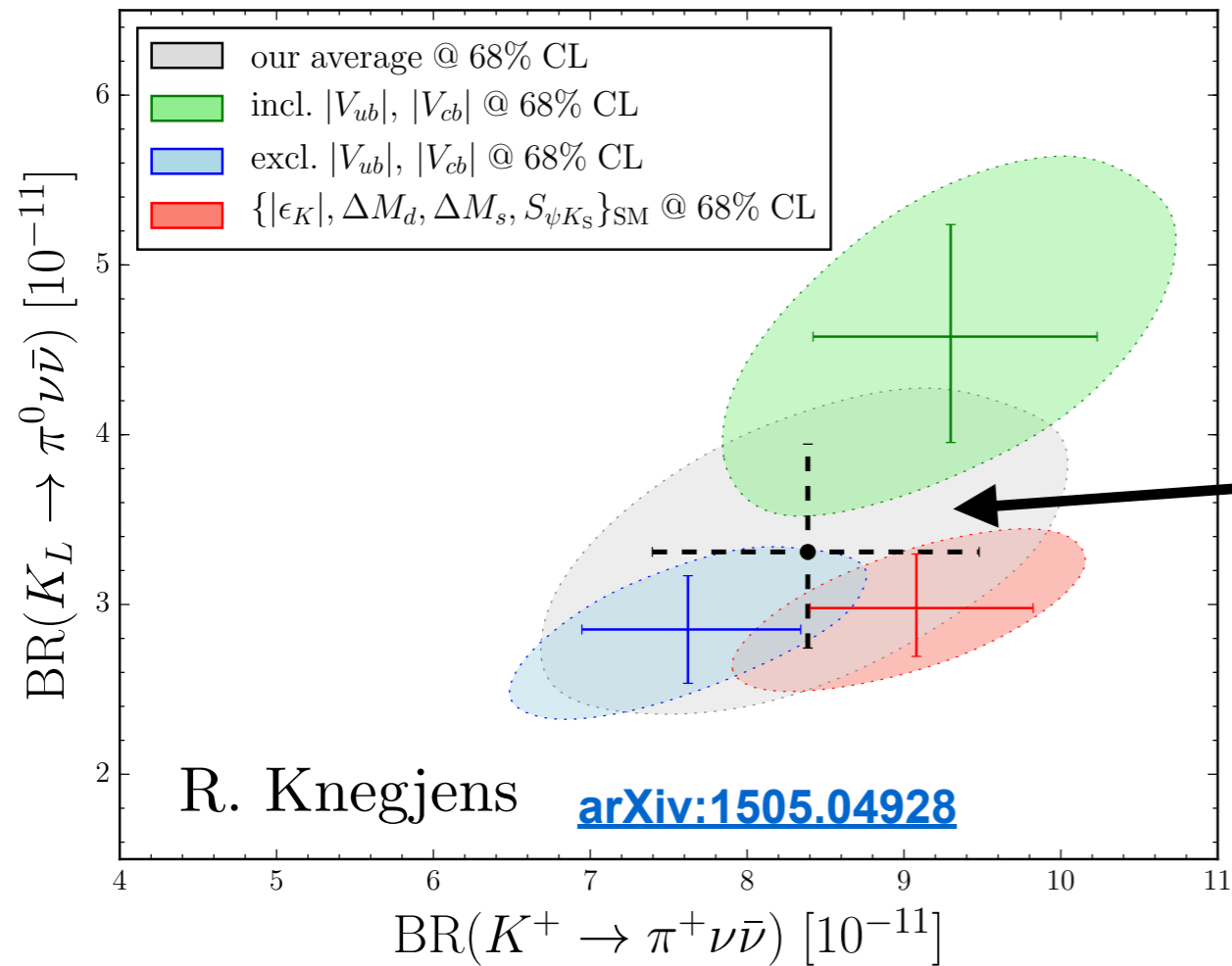
Buras, Buttazzo, Girschbach-Noe, Knegjens 2015: $(3.00 \pm 0.30) \times 10^{-11}$

paraphrase Milind Diwan according to Laurie



(calculation) so clean, theorists are not really needed!

SM parametric error



Buras group

$$|V_{ub}| = \begin{cases} (3.72 \pm 0.14) \times 10^{-3} & \text{excl} \\ (4.40 \pm 0.25) \times 10^{-3} & \text{incl} \\ (3.88 \pm 0.29) \times 10^{-3} & \text{avg} \end{cases},$$

$$|V_{cb}| = \begin{cases} (39.36 \pm 0.75) \times 10^{-3} & \text{excl} \\ (42.21 \pm 0.78) \times 10^{-3} & \text{incl} \\ (40.7 \pm 1.4) \times 10^{-3} & \text{avg} \end{cases}$$

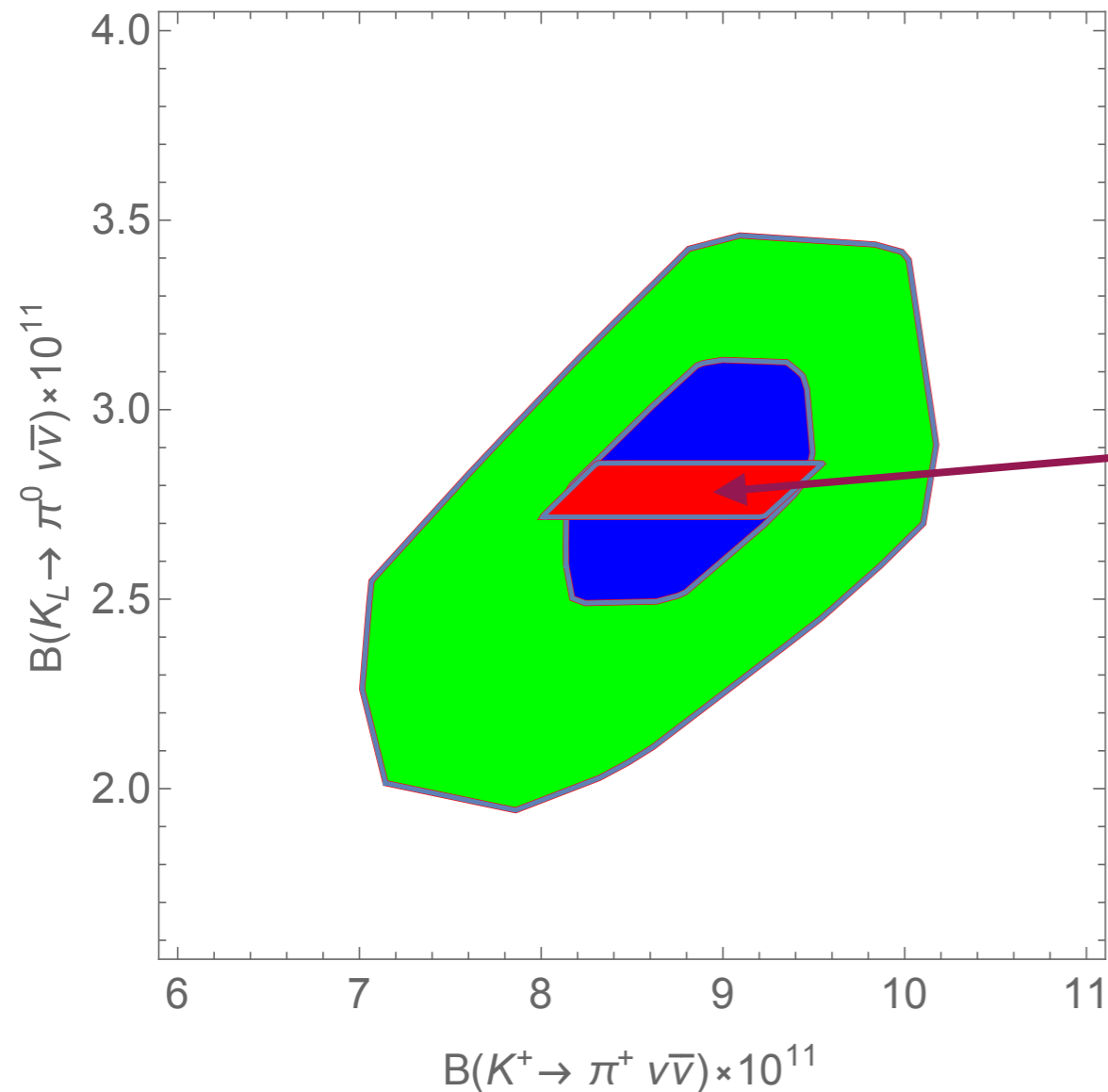
$$\gamma = (73.2_{-7.0}^{+6.3})^\circ.$$

Wolfenstein parameters and Jarlskog invariant:

Observable	Central $\pm 1 \sigma$	$\pm 2 \sigma$
A	0.810 [+0.018 -0.024]	0.810 [+0.025 -0.030]
λ	0.22548 [+0.00068 -0.00034]	0.22548 [+0.00096 -0.00068]
ρ bar	0.1453 [+0.0133 -0.0073]	0.145 [+0.032 -0.015]
η bar	0.343 [+0.011 -0.012]	0.343 [+0.022 -0.025]
J [10^{-5}]	2.96 [+0.19 -0.18]	2.96 [+0.30 -0.22]

CKMfitter

SM P_c and $X(x_t)$ error



Buras group

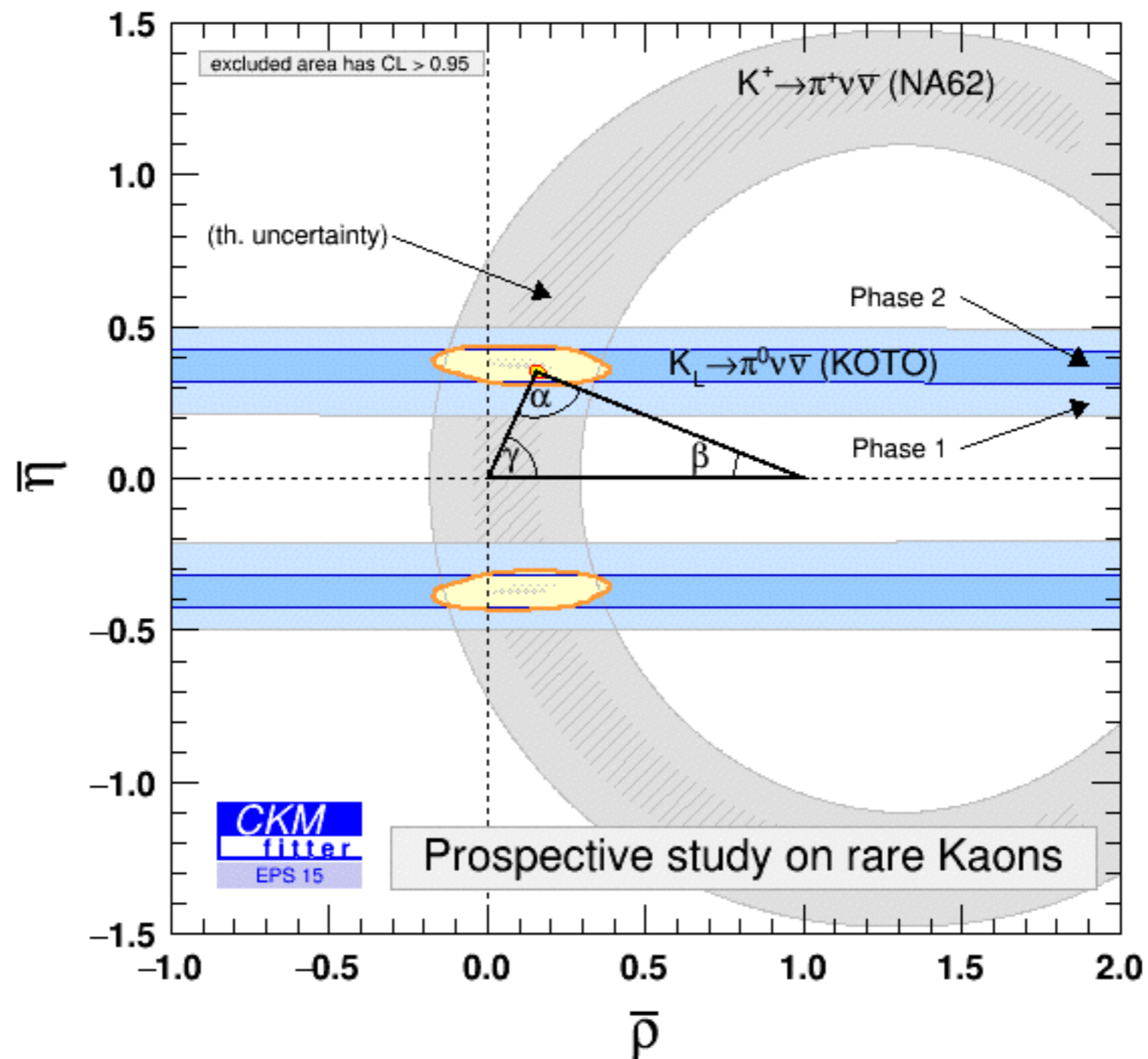
$$X(x_t) = 1.481 \pm 0.005|_{\text{th}} \pm 0.008|_{\text{exp}}$$

$\left\{ \begin{array}{l} \text{NLO QCD corrections} \\ \text{two-loop electroweak contributions} \end{array} \right.$

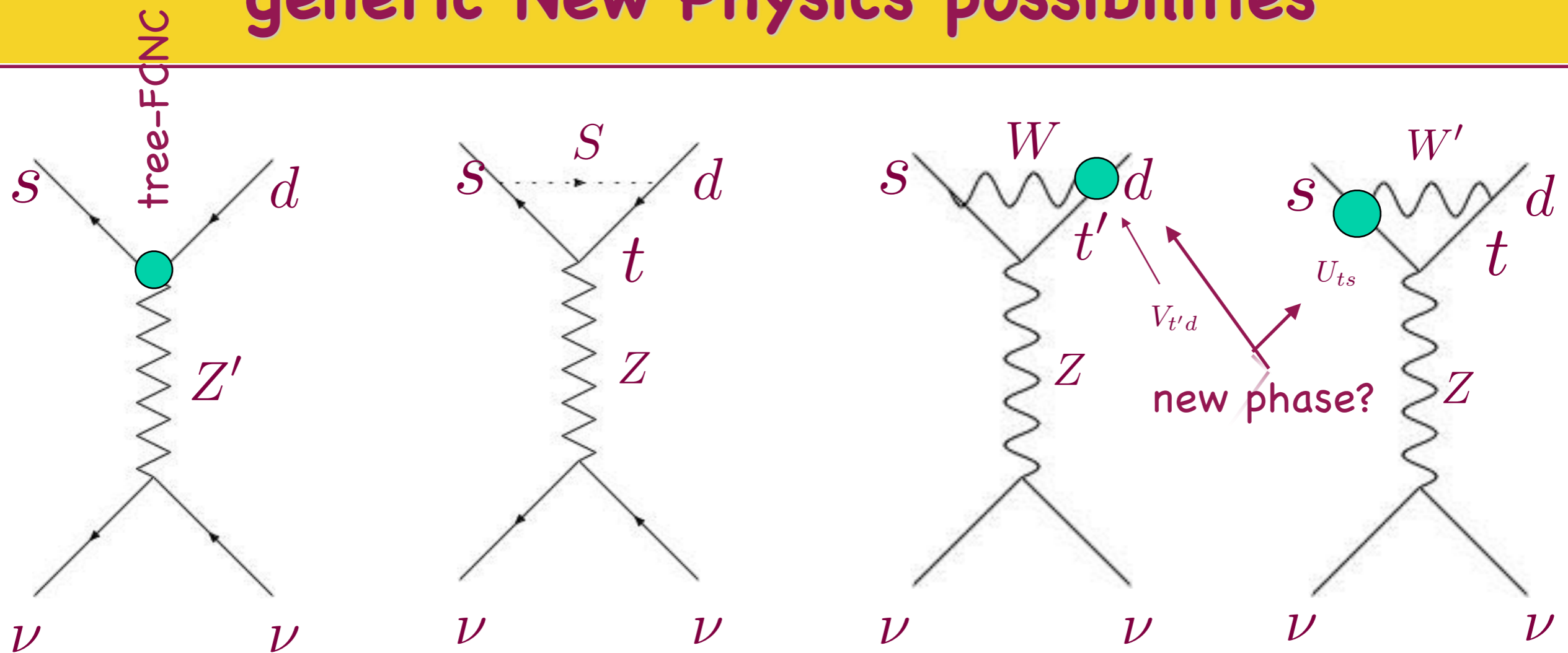
$$P_c(X) = 0.404 \pm 0.024,$$

$\left\{ \begin{array}{l} \text{NLO and NNLO QCD corrections} \\ \text{two-loop electroweak contributions} \\ \text{long distance contribution} \\ 0.04 \pm 0.02, \end{array} \right.$

future projections

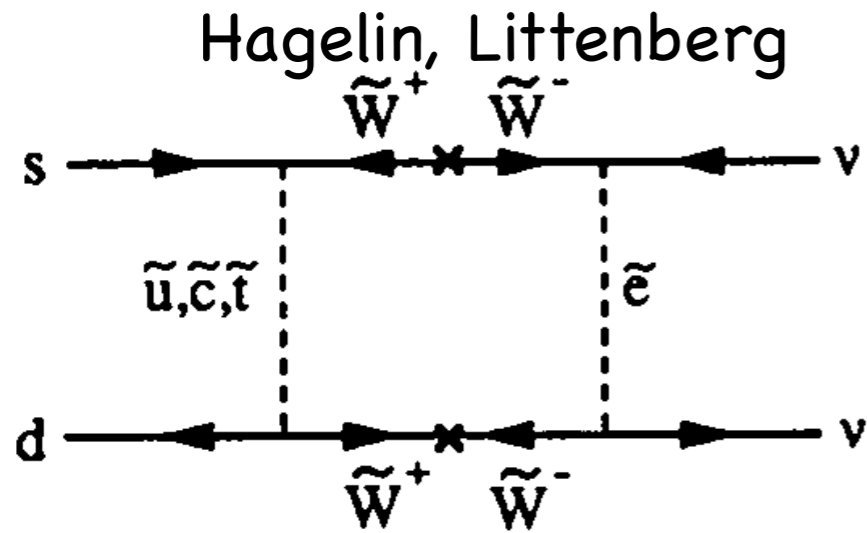


generic New Physics possibilities



- tree-level FCNC in new neutral bosons
- new charged scalars or vectors
- new heavy fermions

specific New Physics models



'Trivial' SUSY

Prog.Part.Nucl.Phys. 23 (1989) 1

Grossman, Isidori, Murayama LFV

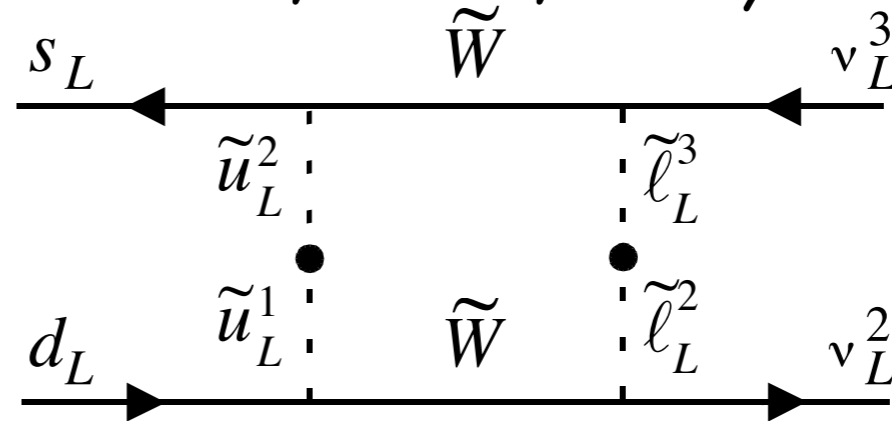
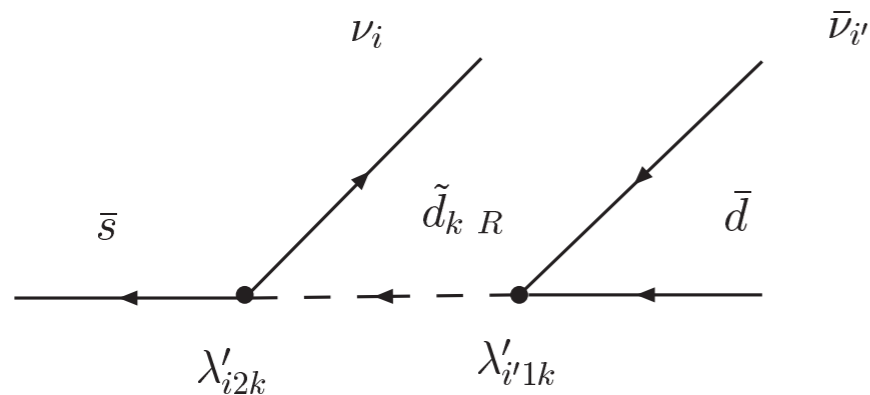


Figure 1: Wino-Wino box diagram.

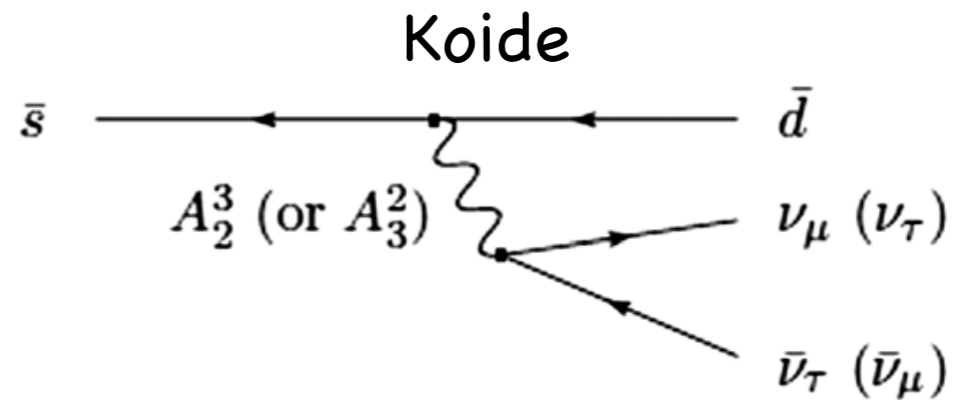
Phys.Lett. B588 (2004) 74-80

Deandrea, Welzel, Oertel



R parity violation

JHEP 0410:038,2004



Family gauge boson

PHYSICAL REVIEW D 92, 036009 (2015)

... (not as many as for the 750 GeV diphoton)



10 April 1997

PHYSICS LETTERS B

Physics Letters B 398 (1997) 163–168

$K_L \rightarrow \pi^0 \nu \bar{\nu}$ beyond the Standard Model [★]

Yuval Grossman ^a, Yosef Nir ^b

^a Stanford Linear Accelerator Center, Stanford University, Stanford, CA 94309, USA

^b Department of Particle Physics, Weizmann Institute of Science, Rehovot 76100, Israel

Received 29 January 1997

Editor: M. Dine

Abstract

We analyze the decay $K_L \rightarrow \pi^0 \nu \bar{\nu}$ in a model independent way. If lepton flavor is conserved the final state is (to a good approximation) purely CP even. In that case this decay mode goes mainly through CP violating interference between mixing and decay. Consequently, a theoretically clean relation between the measured rate and electroweak parameters holds in any given model. Specifically, $\Gamma(K_L \rightarrow \pi^0 \nu \bar{\nu}) / \Gamma(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \sin^2 \theta$ (up to known isospin corrections), where θ is the relative CP violating phase between the $K - \bar{K}$ mixing amplitude and the $s \rightarrow d \nu \bar{\nu}$ decay amplitude. The experimental bound on $\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$ provides a model independent upper bound: $\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 1.1 \times 10^{-8}$. In models with lepton flavor violation, the final state is not necessarily a CP eigenstate. Then CP conserving contributions can dominate the decay rate. © 1997 Published by Elsevier Science B.V.

- simplified notation

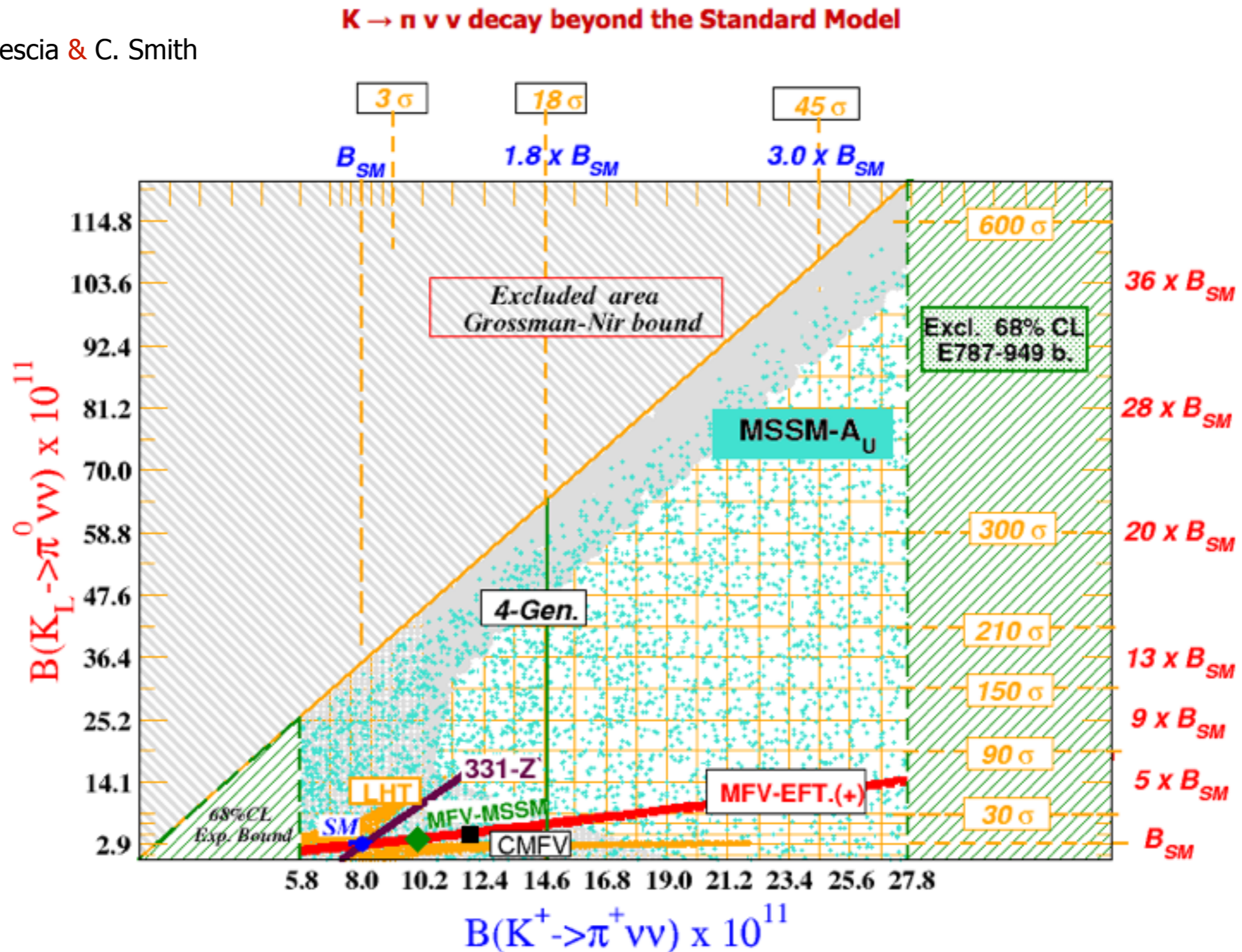
$$\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \kappa_+ |\xi X - P_{(u,c)}|^2, \quad \text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \kappa_L \text{Im}(\xi X)^2,$$

- beyond SM modifies the complex quantity X
- $\text{Im}(X) \leq |X|$ combined with known isospin corrections

$$\begin{aligned} \mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) &\lesssim 4.3 \times \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \\ &< 1.4 \times 10^{-9}. \quad (\text{GN bound}) \end{aligned}$$

sample of recent models

June 2010 by F. Mescia & C. Smith

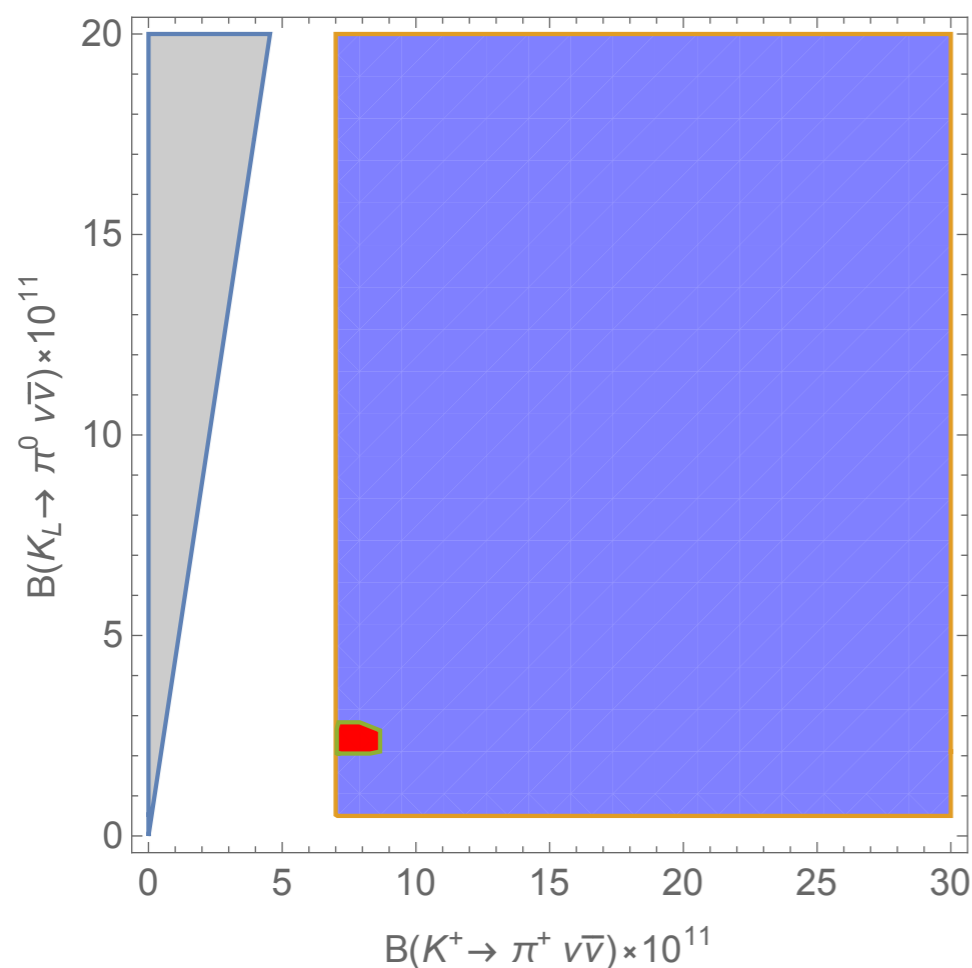


the fourth generation

- perfect example of complementarity between flavour physics and LHC
- kaons constraining 4th generation parameters until 2012
- Higgs found in 2012: 4th generation ruled out

[-ph/9804412](#)

Toshihiko Hattori, Tsutom Hasuike, Seichi Wakaizumi

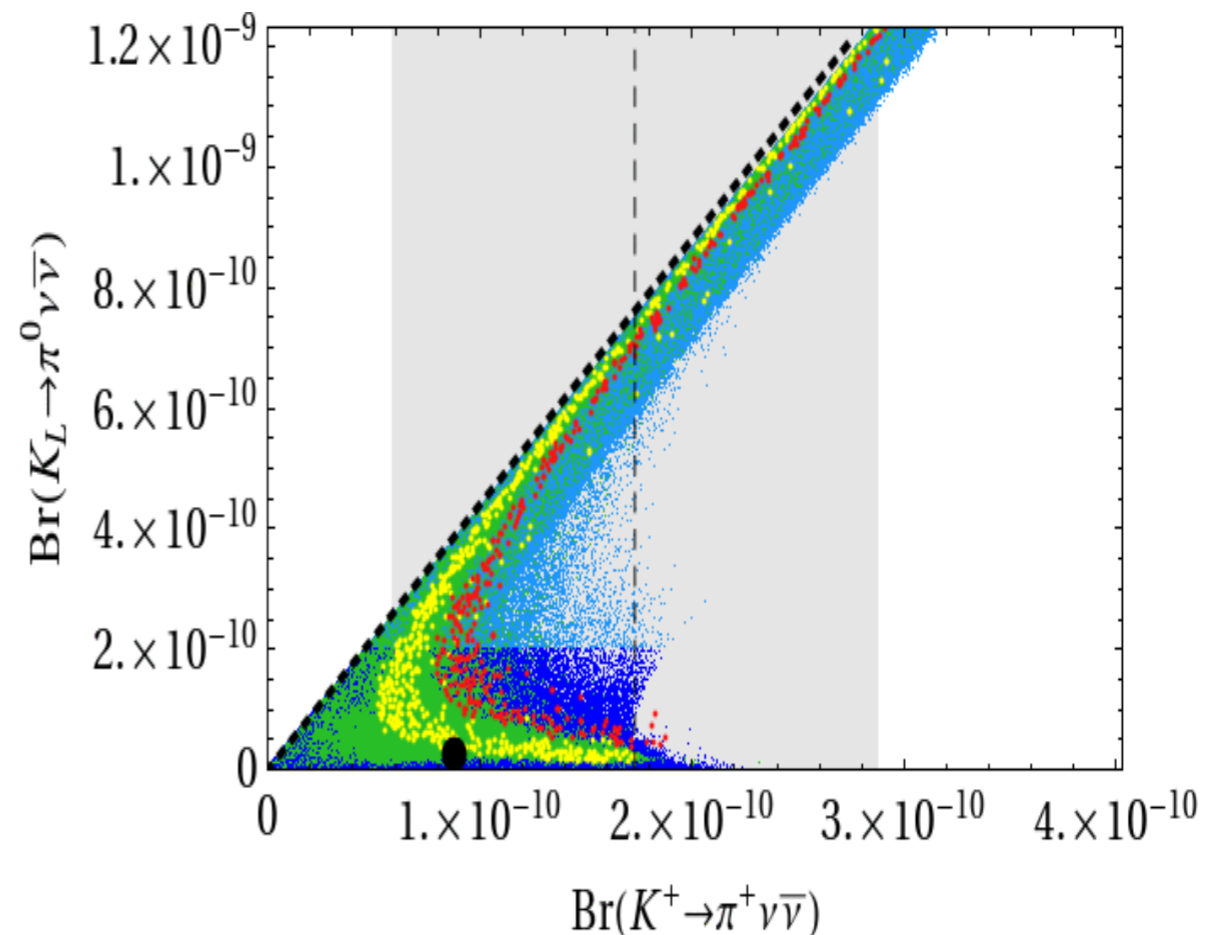


TILLMANN HEIDSIECK¹

SM4 with

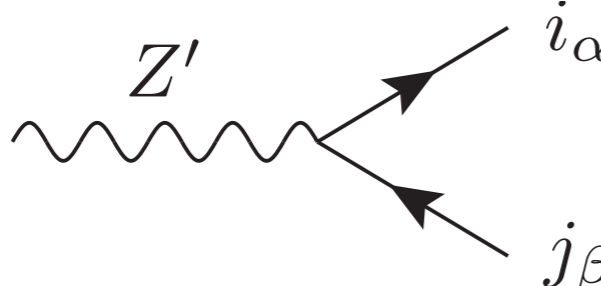
2010 global fit

$$B(B_s \rightarrow \mu^+ \mu^-) = (3.2 \pm 0.2) \times 10^{-9}$$



Buras-MFV

- start with a Z' :



A Feynman diagram showing a wavy line labeled Z' on the left, which splits into two straight lines with arrows pointing to the right. The upper line is labeled i_α and the lower line is labeled j_β .

$$i\gamma_\mu\delta_{\alpha\beta}\left[\Delta_L^{ij}(Z')P_L + \Delta_R^{ij}(Z')P_R\right]$$

- write NP in terms of SM:

$$X(x_t) \rightarrow X(x_t)_{\text{SM}} + \frac{\pi^2}{2M_W^2 G_F^2} \frac{\Delta_L^{\nu\nu}(Z^{(l)})}{V_{ts}^* V_{td} M_Z^{(l)2}} \left[\Delta_L^{sd}(Z^{(l)}) + \Delta_R^{sd}(Z^{(l)}) \right]$$

- define MFV as

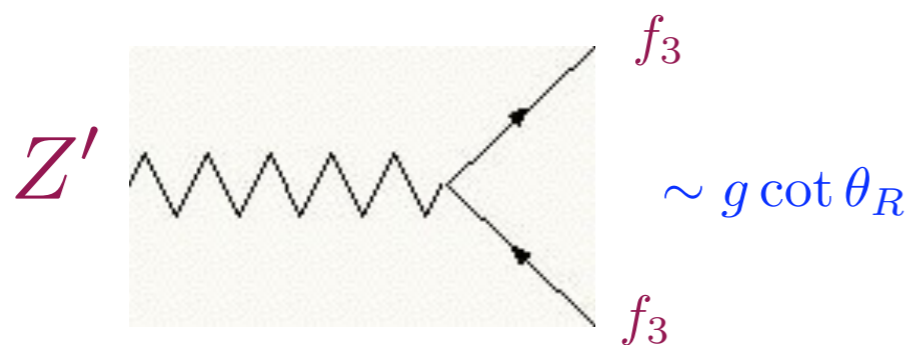
$$\Delta_R^{sd}(Z') = 0, \quad \Delta_L^{sd}(Z') = |\Delta_L^{sd}(Z')| e^{i\phi_{\lambda_t}}$$

- scan `reasonable' parameters

Non-universal Z'

- based on $SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$
- Single out the third generation
- generically this produces a pattern of couplings:

$$\tan \theta_R = \frac{g}{g_R}$$



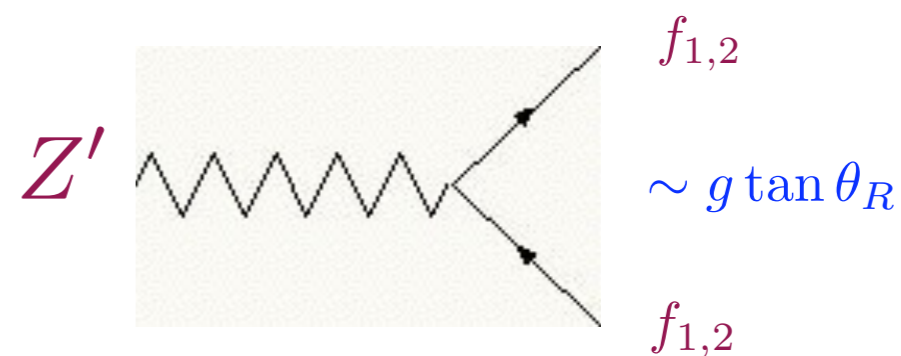
- From LEP and LEP II using R_b , A_{FB}^b , and $\sigma(e^+e^- \rightarrow \tau^+\tau^-)$:

$$\cot \theta_R \tan \theta_W \left(\frac{M_W}{M_{Z'}} \right) \leq 1$$

- For $\cot \theta_R \sim 10 \implies M_{Z'} > 450 \text{ GeV}$

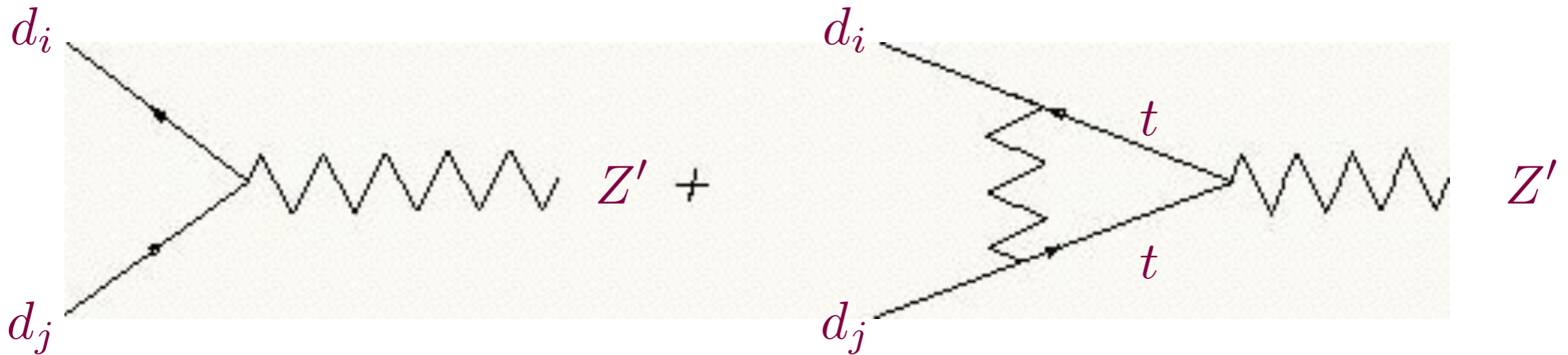
- Perturbative unitarity

$$\cot \theta_R \leq 20$$



Z' couplings and FCNC operators

Couplings enhanced by $\cot \theta_R$ $\frac{g}{2 \cos \theta_W} \bar{q}_i \gamma^\mu (a_{ij} P_L + b_{ij} P_R) q_j Z'_\mu$



$$b_{ij} = \sin \theta_W \cot \theta_R \cos \xi_Z V_{Rbi}^{D*} V_{Rbj}^D$$

$$a_{ij} = \frac{\alpha}{2\pi \sin \theta_W} I(\lambda_t, \lambda_H) \cot \theta_R V_{ti}^* V_{tj}$$

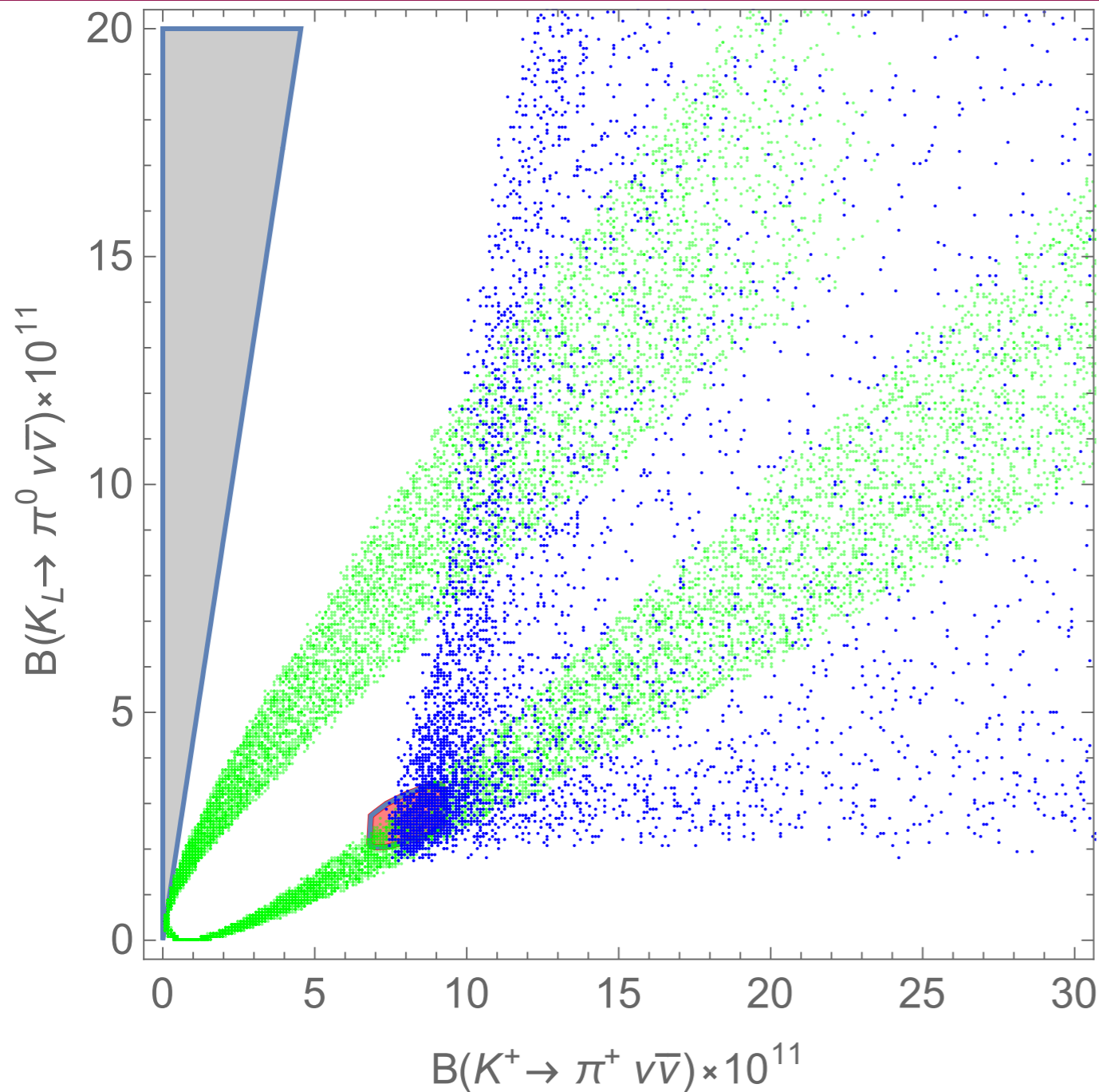
$$\xi_Z = 0 \quad (\text{no mixing})$$

$$5.5 \leq I(\lambda_t, \lambda_H) \left| \frac{V_{tb}^* V_{ts}}{0.04} \right| \leq 6.5 \quad (\Delta M_{B_s})$$

- $W-W'$ and $Z-Z'$ mixing near zero from $b \rightarrow s \gamma$ and $Z \rightarrow \tau^+ \tau^-$

Z' coupling to tau-neutrino is enhanced, and it is right-handed

An example Z'



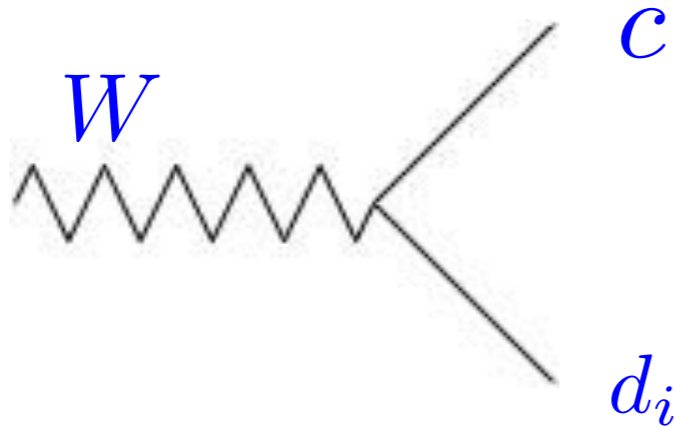
SM : 2 sigma parameter scan

Z' MFV Buras group

Z' Non-universal (RH): He, GV

$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}(\gamma)) = \kappa_+ (1 + \Delta_{\text{EM}}) \left[\left(\frac{\text{Im}(V_{ts}^* V_{td})}{\lambda^5} X_t \right)^2 + \left(\frac{\text{Re}(V_{cs}^* V_{cd})}{\lambda} (P_c + \delta P_{c,u}) + \frac{\text{Re}(V_{ts}^* V_{td})}{\lambda^5} X_t \right)^2 \right].$$

New Physics in charm?



$$-\frac{g}{\sqrt{2}} V_{ci} \gamma^\mu \left((1 + \kappa_{ci}^L) P_L + \kappa_{ci}^R P_R \right)$$

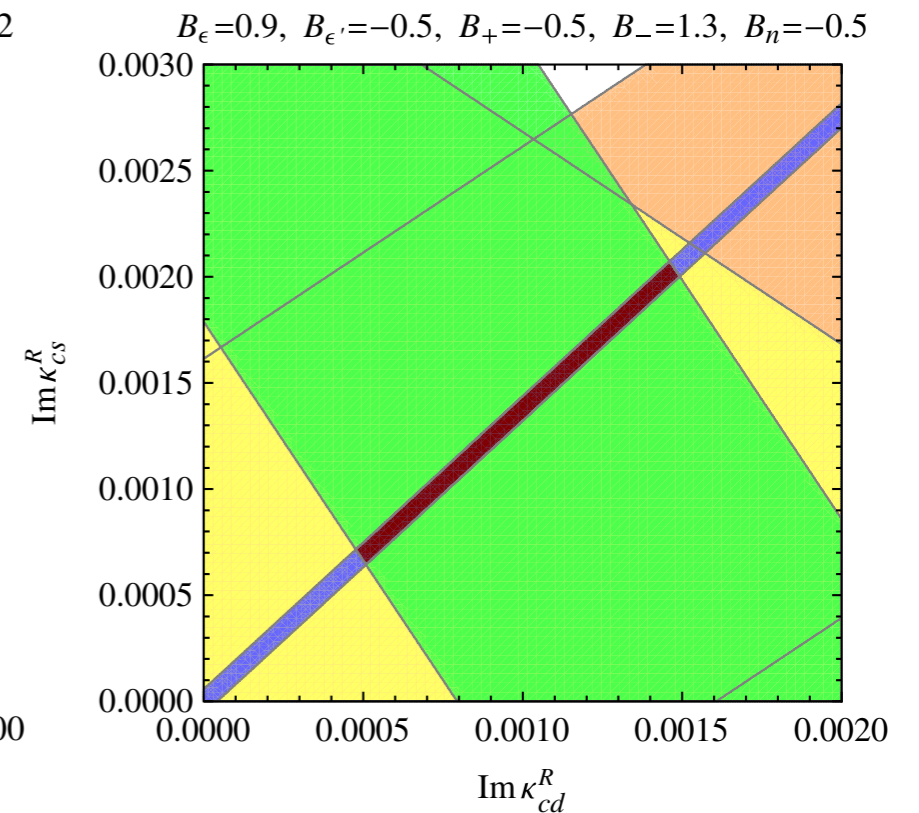
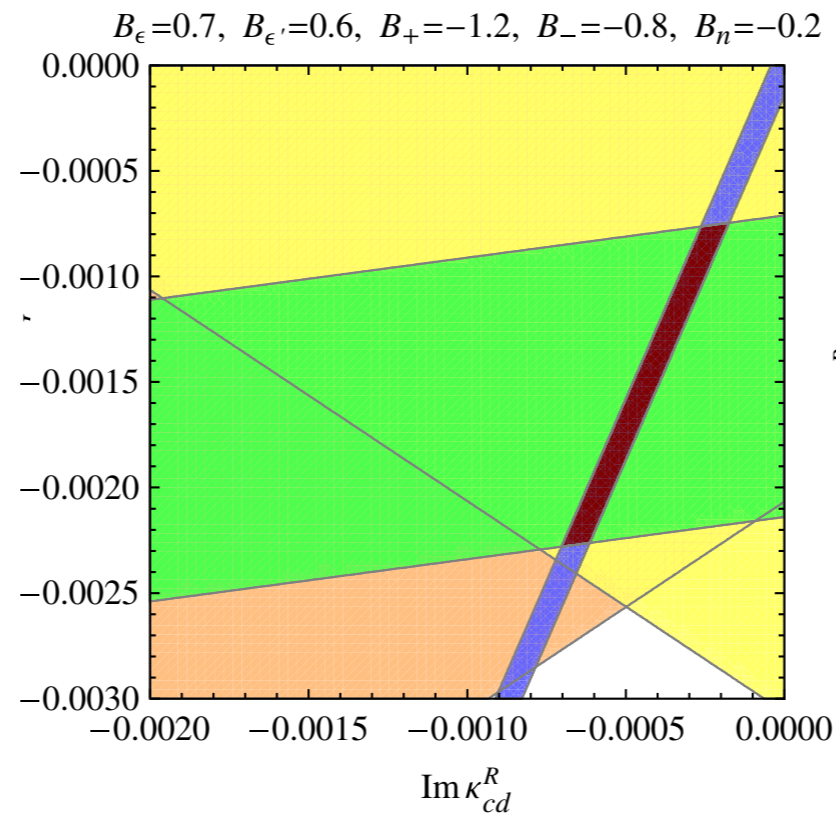
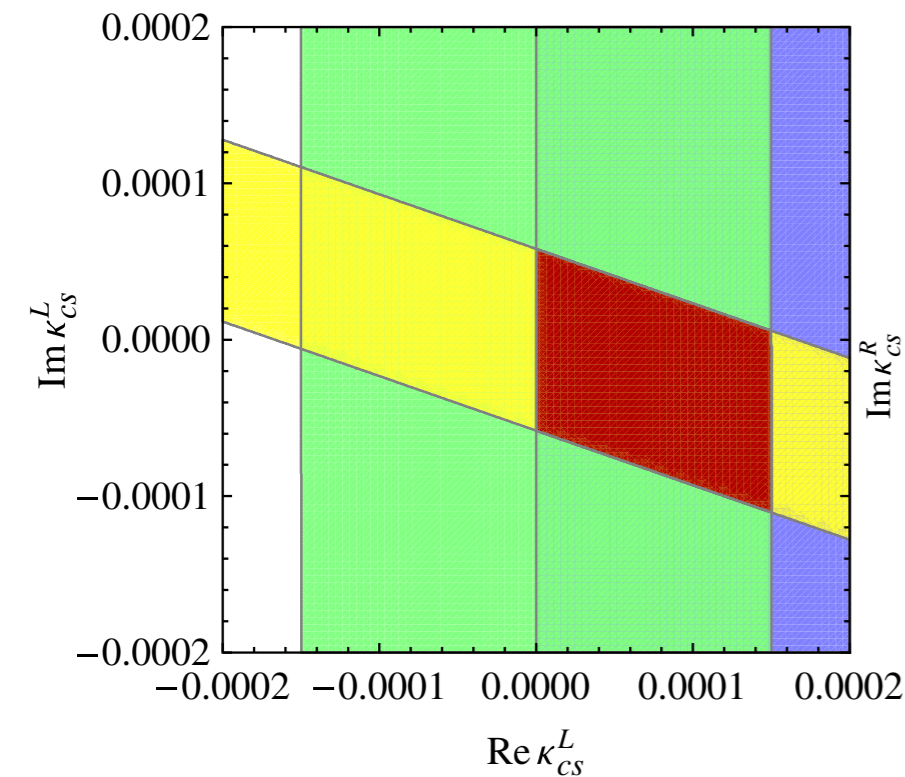
$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu} (\gamma)) = \kappa_+ (1 + \Delta_{\text{EM}}) \left[\left(\frac{\text{Im}(V_{ts}^* V_{td})}{\lambda^5} X_t \right)^2 + \left(\frac{\text{Re}(V_{cs}^* V_{cd})}{\lambda} X'(x_c) |\kappa_{cd}^R \kappa_{cs}^{*R}| \right)^2 \right. \\ \left. + \left(\frac{\text{Re}(V_{cs}^* V_{cd})}{\lambda} (P_c + \delta P_{c,u}) + \frac{\text{Re}(V_{ts}^* V_{td})}{\lambda^5} X_t \right)^2 \right]. \quad (1)$$

$$P_c \rightarrow P_c + (\kappa_{cd}^L + \kappa_{cs}^{*L}) X'(x_c)$$

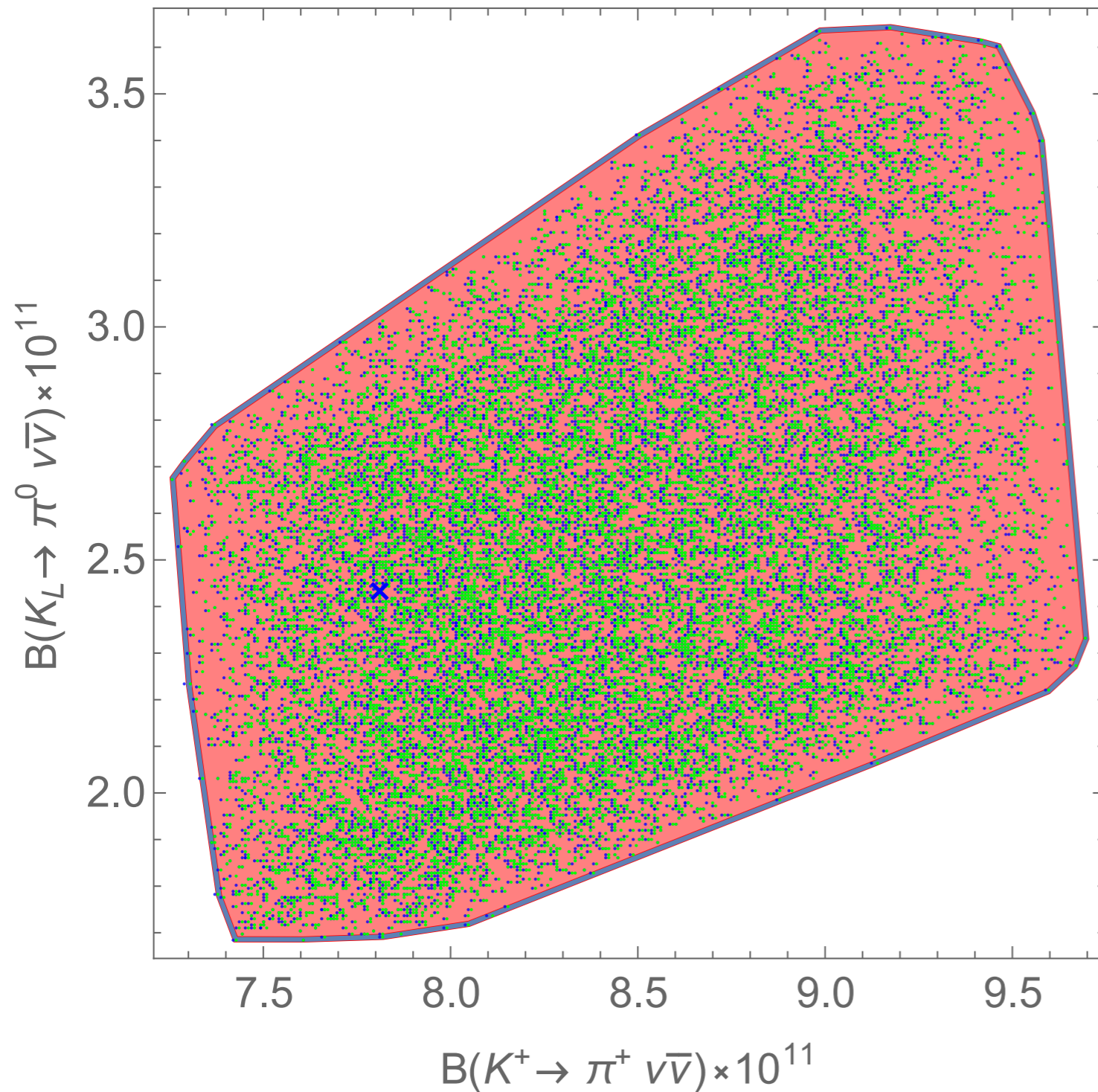
$$B(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \kappa_L \left(\frac{\text{Im}(V_{ts}^* V_{td})}{\lambda^5} X_t \right)^2 + \left(\frac{\text{Re}(V_{cs}^* V_{cd})}{\lambda} X'(x_c) \text{Im}(\kappa_{cd}^R \kappa_{cs}^{*R}) \right)^2 \\ + \frac{\text{Re}(V_{cs}^* V_{cd})}{\lambda} X'(x_c) \text{Im}(\kappa_{cd}^L + \kappa_{cs}^{*L})$$

menu of constraints

Process	Eq.	Constraint	#
$D \rightarrow \ell \nu$	(14)	$ \text{Re}(\kappa_{cd}^L - \kappa_{cd}^R) \leq 0.04$	1
$D_s \rightarrow \ell \nu$	(15)	$0 \leq \text{Re}(\kappa_{cs}^L - \kappa_{cs}^R) \leq 0.1$	2
$b \rightarrow c \ell \bar{\nu}$	(22)	$-0.13 \leq \text{Re} \kappa_{cb}^R \leq 0$	3
$B \rightarrow J/\psi K, \eta_c K$	(31)	$-5 \times 10^{-4} \leq \text{Im}(\kappa_{cb}^R + \kappa_{cs}^R) \leq 0.04$	4
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	(58)	$-1.3 \times 10^{-3} \leq \text{Re}(\kappa_{cd}^L + \kappa_{cs}^L) + 0.42 \text{Im} \kappa_{cs}^L \leq 2.5 \times 10^{-4}$	5
$K_L \rightarrow \mu^+ \mu^-$	(63)	$ \text{Re}(\kappa_{cs}^L + \kappa_{cd}^L) + 6 \times 10^{-4} \text{Im} \kappa_{cs}^L \leq 1.5 \times 10^{-4}$	6
ΔM_K	(67)	$ 0.043 \text{Re}(\kappa_{cd}^L + \kappa_{cs}^L) - 0.015 \text{Im} \kappa_{cs}^L - \text{Re}(\kappa_{cd}^{R*} \kappa_{cs}^R) + 0.28 \text{Im}(\kappa_{cd}^{R*} \kappa_{cs}^R) \leq 8.5 \times 10^{-4}$	7
ϵ (mixing)	(69)	$ 0.015 \text{Re}(\kappa_{cs}^L + \kappa_{cd}^L) + 0.043 \text{Im} \kappa_{cs}^L - 0.28 \text{Re}(\kappa_{cd}^{R*} \kappa_{cs}^R) - \text{Im}(\kappa_{cd}^{R*} \kappa_{cs}^R) \leq 2.5 \times 10^{-6}$	8
ΔM_d	(73)	$-0.031 \leq \text{Re}(\kappa_{cb}^L + \kappa_{cd}^L) + 0.4 \text{Im} \kappa_{cb}^L \leq 0.003$	9
$\sin(2\beta)$ (mixing)	(77)	$-1.5 \times 10^{-3} \leq 0.4 \text{Re}(\kappa_{cb}^L + \kappa_{cd}^L) - 0.69 \text{Im} \kappa_{cb}^L - 0.31 \text{Im} \kappa_{cs}^L \leq 0.012$	10
ΔM_s	(81)	$-0.014 \leq \text{Re}(\kappa_{cs}^L + \kappa_{cb}^L) + 0.018 \text{Im}(\kappa_{cs}^L - \kappa_{cb}^L) \leq 0.015$	11
$\sin(2\beta_s)$ (mixing)	(85)	$-0.09 \leq 0.026 \text{Re}(\kappa_{cb}^L + \kappa_{cs}^L) + \text{Im}(\kappa_{cb}^L - \kappa_{cs}^L) \leq 7 \times 10^{-4}$	12



New physics in charm?



x SM central values from Brod et.al

SM : 2 sigma parameter scan

modified charm RH couplings

modified charm LH couplings

at the moment overlaps with
SM within uncertainty

a loophole in GN?- George Hou

Kaori Fuyuto, Wei-Shu Hou, Masaya Kohda.
Phys.Rev.Lett. 114 (2015) 171802

- the PDB mini-review is 'more or less the same' every 2 years...
- simple enough to a theorist: the K^+ experiments cut a section of the kinematic region that the K_L experiments do not. If NP falls in that gap, the GN bound doesn't apply...
- Laurie not satisfied... very long discussion on different acceptance for 2 body mode vs 3 body mode in the two experiments (that's where I can contribute 😊 to the collaboration... 😊)
- short story: it took a month to produce the sentence:

It was pointed out in a recent paper that there is a kinematic gap in the Grossman-Nir bound that makes the $K_L \rightarrow \pi^0 \nu \bar{\nu}$ mode interesting for new physics searches at the current sensitivity level

a loophole in GN? - George Hou

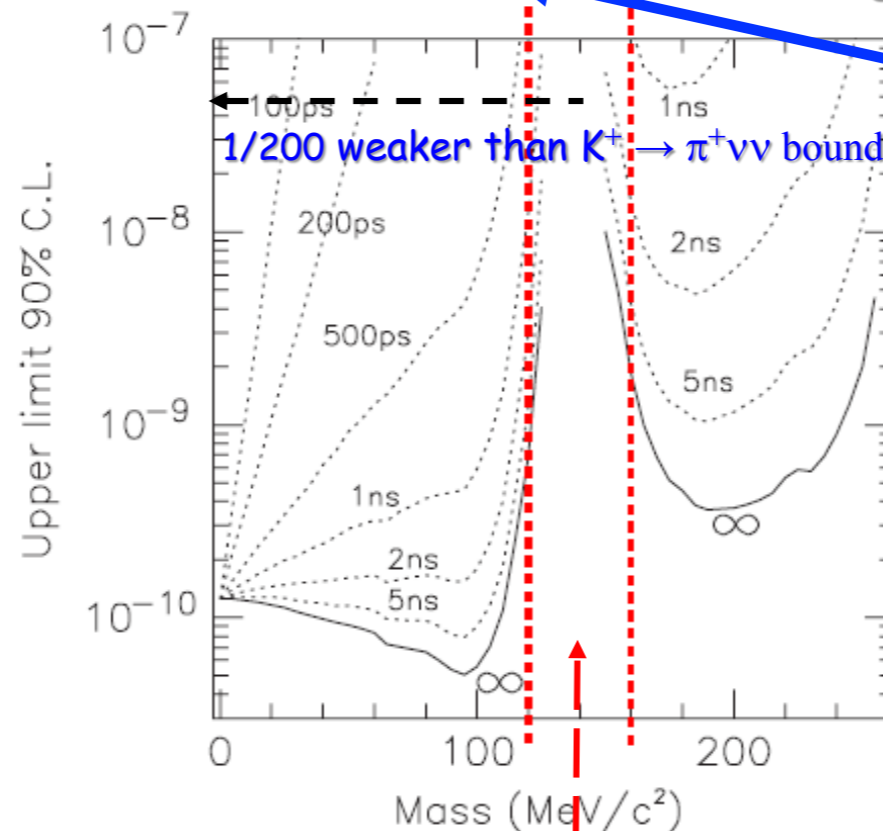
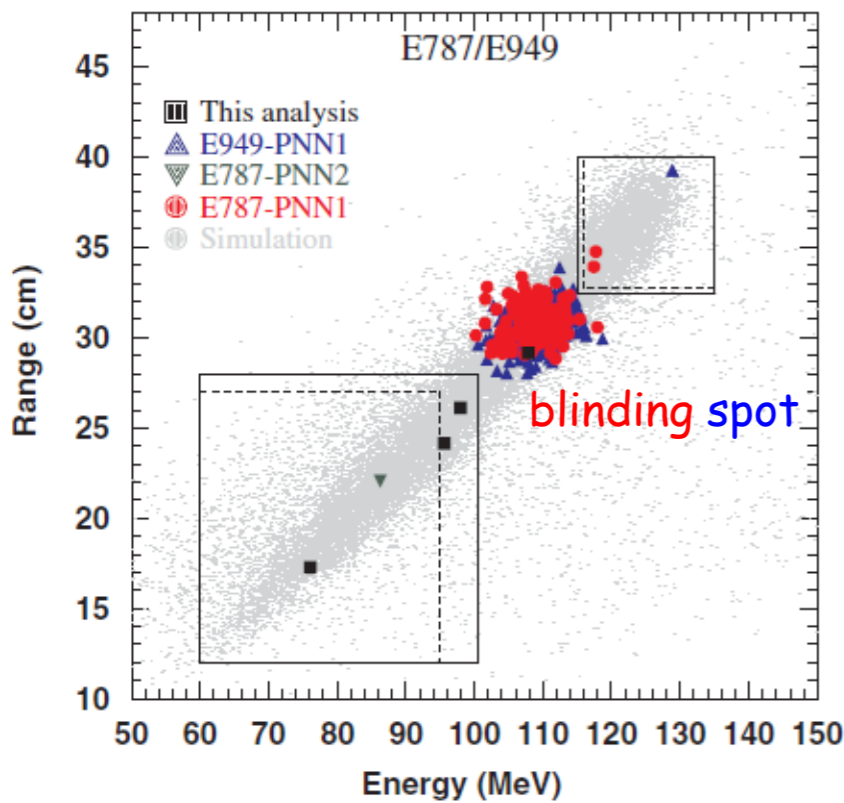


Bound on $K \rightarrow \pi X^0$



BV. The E949 limit of $\mathcal{B}(\pi^0 \rightarrow \nu\bar{\nu}) < 2.7 \times 10^{-7}$ at 90% C.L. [60] can be combined with the world average value of $\mathcal{B}(K^+ \rightarrow \pi^+ \pi^0)$ [24] to set a 90% C.L. limit of $\mathcal{B}(K^+ \rightarrow \pi^+ X) < 5.6 \times 10^{-8}$ for $M_X = M_{\pi^0}$ with X stable

PHYSICAL REVIEW D 79, 092004 (2009)



very useful too!
now dark γ or Z

FIG. 18. The solid lines represent the 90% C.L. upper limit on $\mathcal{B}(K^+ \rightarrow \pi^+ X)$ as a function of the mass of X assuming X is

more on the loophole- George Hou



$$K^+ \rightarrow \pi^+ \text{“}\pi^0\text{” Loophole} \quad \text{vs} \quad K_L \rightarrow \pi^0 X^0$$



Window basically Same as E787/949 @ BNL

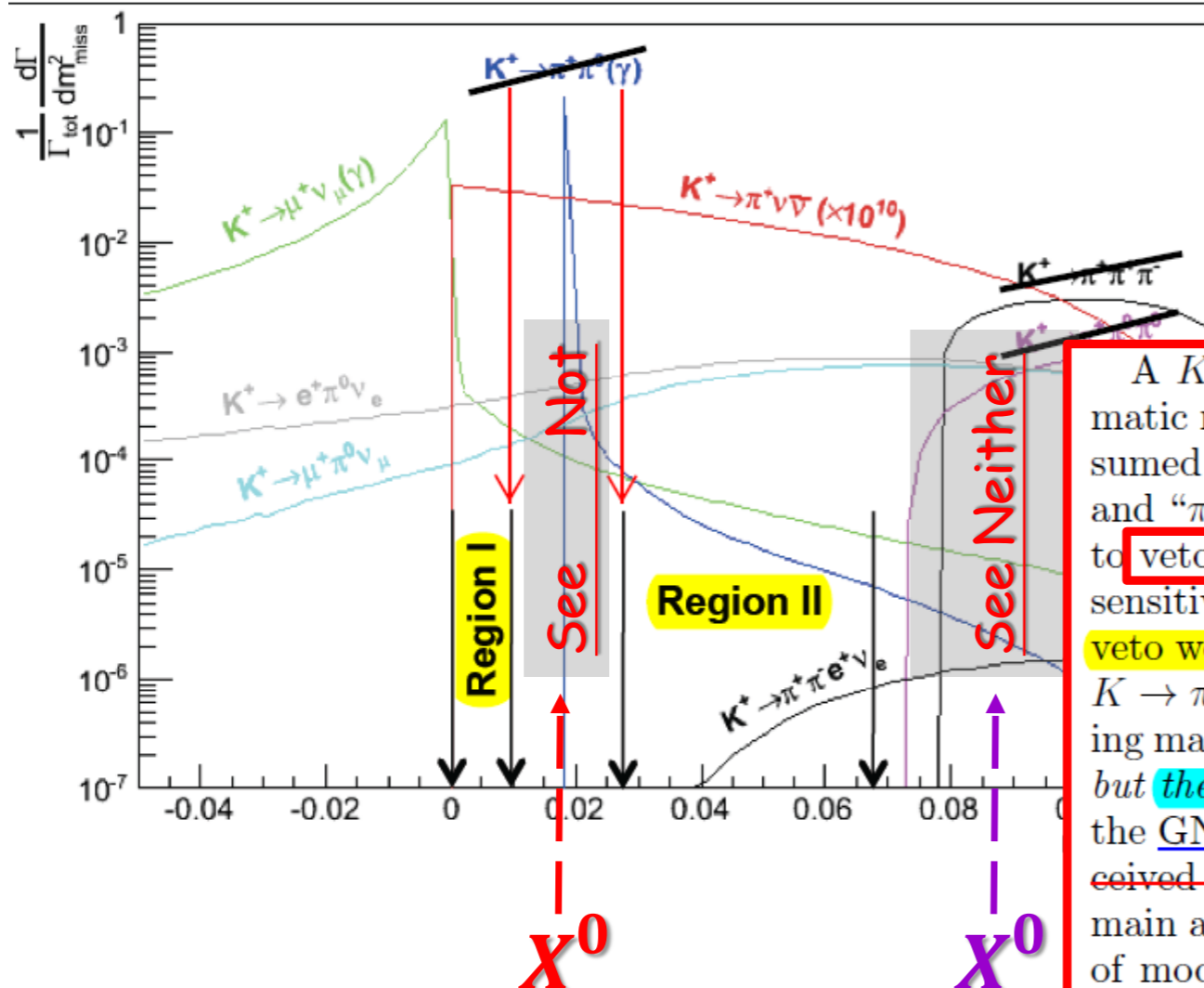
The KOTO Expt at J-PARC can discover $K_L \rightarrow \pi^0 X^0$ above the Grossman-Nir Bound!

@ CERN

Kinematic exclusion:

$$\text{exclude } 0.01 - 0.025 \text{ GeV}^2 \quad [(100)^2 - (160)^2 \text{ MeV}^2]$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \lesssim 4.3 \times \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) < 1.4 \times 10^{-9} \quad (\text{GN bound})$$



“Blind man Blessed by Senses.”

A Surprise! “Trivial”

A $K_L \rightarrow \pi^0 \nu \bar{\nu}$ experiment, however, cannot do kinematic reconstruction: besides detecting two photons (assumed as π^0), it measures “nothing to nothing”. The K_L and “ π^0 ” momenta are not known. The approach is thus to veto everything and to learn while pushing down the sensitivity. However, the $\nu \bar{\nu}$ being the target, one cannot veto weakly interacting light particles (WILP). Thus, for $K \rightarrow \pi X^0$ where X^0 is any WILP that falls into the missing mass window, the K^+ experiment would be oblivious, but the K_L experiment can have a blunt feel! Although the GN relation of Eq. (4) is in no way violated, the perceived GN bound of Eq. (2) does not apply. This is the main and rather simple point of this Letter, independent of model discussion. The X^0 need not be the leptonic force, as it simply goes undetected. Fuyoto, WSH, Kohda

$K_L \rightarrow \pi^0 \nu \bar{\nu} > \text{GN?}$

George W.S. Hou

Our other collaboration

- a piggyback on Laurie's mode (add a pion)

Phys.Lett. B385 (1996) 379-384

Abstract

We study the reactions $K \rightarrow \pi\pi\nu\bar{\nu}$ within the minimal standard model. We use isospin symmetry to relate the matrix elements to the form factors measured in $K_{\ell 4}$. We argue that these modes are short distance dominated and can be used for precise determinations of the CKM parameters ρ and η . Depending on the value of the CKM angles we find branching ratios in the following ranges: $B(K_L \rightarrow \pi^+\pi^-\nu\bar{\nu}) = [2-5] \times 10^{-13}$; $B(K_L \rightarrow \pi^0\pi^0\nu\bar{\nu}) = [1-3] \times 10^{-13}$; $B(K^+ \rightarrow \pi^+\pi^0\nu\bar{\nu}) = [1-2] \times 10^{-14}$. We also discuss a possible CP -odd observable.

Phys.Rev. D84 (2011) 052009

The rare decay $K_L^0 \rightarrow \pi^0\pi^0\nu\bar{\nu}$ was studied with the E391a detector at the KEK 12-GeV proton synchrotron. Based on 9.4×10^9 K_L^0 decays, an upper limit of 8.1×10^{-7} was obtained for the branching fraction at 90% confidence level. We also set a limit on the $K_L^0 \rightarrow \pi^0\pi^0 X$ ($X \rightarrow$ invisible particles) process; the limit on the branching fraction varied from 7.0×10^{-7} to 4.0×10^{-5} for the mass of X ranging from 50 MeV/ c^2 to 200 MeV/ c^2 .

conclusion

- Laurie's contributions to rare kaon decays have been improving our knowledge of SM parameters and **'ruling out'** new physics for more than 25 years
 - really, pushing them into smaller and smaller regions of allowed parameter space
- We expect them to continue doing so for many years to come