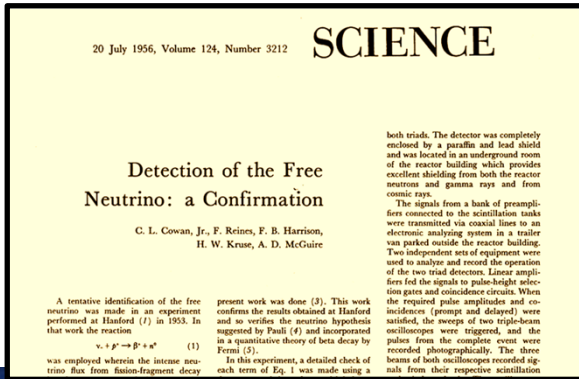


# NEUTRINOS AT 67

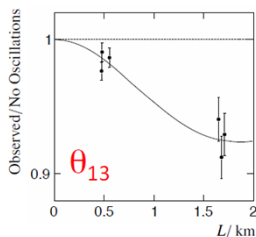
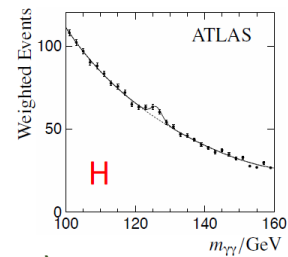


**Gabriela Barenboim**  
**UV-IFIC**  
**Brookhaven Forum**  
**Advancing Searches for New Physics**  
**(BF2023)**  
**October 6, 2023**



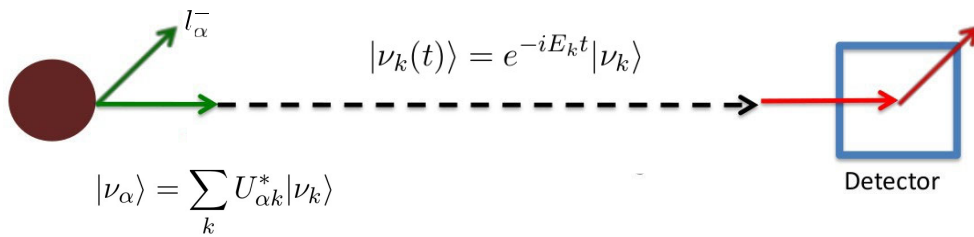
~~Two~~ 2012 One major discovery ~~ies~~ in particle physics

- A SM-like Higgs boson (ATLAS, CMS)  
 The key to EWSB and a possible window to



- $\theta_{13} \sim 10^\circ$  (T2K, MINOS, Daya Bay, RENO)  
 about as large as it could have been !  
 The door to CP Violation in the leptonic sector

### Neutrino oscillations

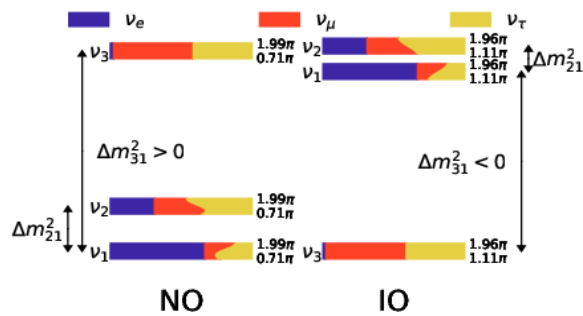


$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{k>j} \text{Re}[W_{\alpha\beta}^{jk}] \sin^2 \left( \frac{\Delta m_{jk}^2 L}{4E_\nu} \right) \pm 2 \sum_{k>j} \text{Im}[W_{\alpha\beta}^{jk}] \sin \left( \frac{\Delta m_{jk}^2 L}{2E_\nu} \right)$$

### Three-neutrino oscillations

Neutrino mixing matrix

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

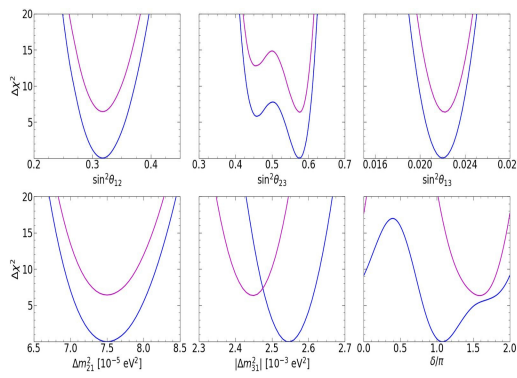


Parameter	Main contribution	Other contributions
$\theta_{12}$	SOL	KamLAND
$\theta_{13}$	REAC	ATM+LBL and SOL+KamLAND
$\theta_{23}$	ATM+LBL	-
$\delta_{CP}$	LBL	ATM
$\Delta m_{21}^2$	KamLAND	SOL
$ \Delta m_{31}^2 $	LBL+ATM+REAC	-
MO	LBL+REAC and ATM	-

SOL: Solar  
ATM: Atmospheric neutrinos

LBL: Long baseline accelerator experiments  
REAC: Short-baseline reactor experiments

<https://globalfit.astroparticles.es/>



de Salas et al, JHEP 02 (2021) 071 [arXiv:2006.11237]

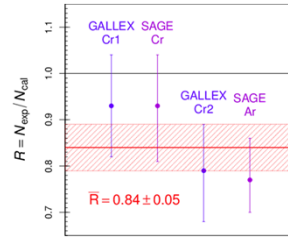
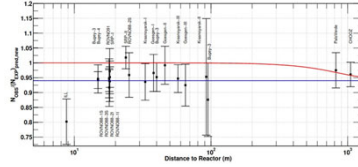
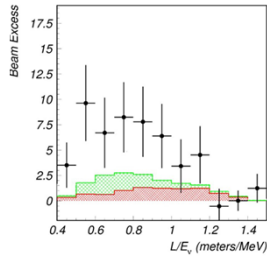
parameter	best fit $\pm 1\sigma$	$2\sigma$ range	$3\sigma$ range
$\Delta m_{21}^2 [10^{-5} \text{eV}^2]$	$7.50^{+0.22}_{-0.20}$	7.12–7.93	6.94–8.14
$ \Delta m_{31}^2  [10^{-3} \text{eV}^2]$ (NO)	$2.55^{+0.02}_{-0.03}$	2.49–2.60	2.47–2.63
$ \Delta m_{31}^2  [10^{-3} \text{eV}^2]$ (IO)	$2.45^{+0.02}_{-0.03}$	2.39–2.50	2.37–2.53
$\sin^2 \theta_{12}/10^{-1}$	$3.18 \pm 0.16$	2.86–3.52	2.71–3.69
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.74 \pm 0.14$	5.41–5.99	4.34–6.10
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.78^{+0.10}_{-0.17}$	5.41–5.98	4.33–6.08
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.200^{+0.069}_{-0.062}$	2.069–2.337	2.000–2.405
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.225^{+0.064}_{-0.070}$	2.086–2.356	2.018–2.424
$\delta/\pi$ (NO)	$1.08^{+0.13}_{-0.12}$	0.84–1.42	0.71–1.99
$\delta/\pi$ (IO)	$1.58^{+0.15}_{-0.16}$	1.26–1.85	1.11–1.96

Relative  $1\sigma$  uncertainty

2.7% **PRECISION**  
1.1% **ORDERING?**  
5.2% **PRECISION**  
5.1% **OCTANT?**  
3.0% **PRECISION**  
20% **CPV?**  
9.0%



## Anomalies

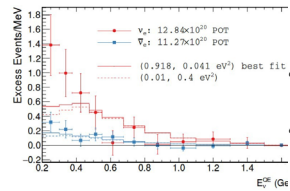


Need extra states !!!

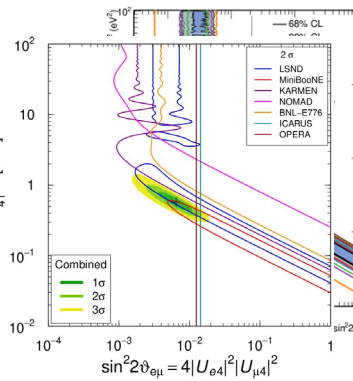
## MiniBooNE

MiniBooNE was built to check the LSND results with a different baseline, but similar L/E

MiniBooNE has no near det



MiniBooNE sees an excess at  $\sim 5\sigma$  at low energies



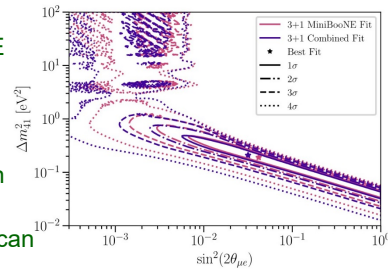
## MicroBooNE

MicroBooNE was built to check the MiniBooNE results!

Looking for signals using several final state channels

The collaboration did not perform an oscillation analysis

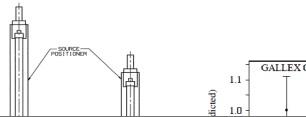
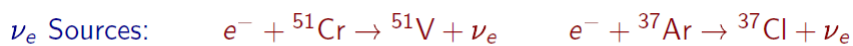
A combined analysis shows that MicroBooNE can not exclude the region of parameter space preferred by MiniBooNE



2201.01724

## The Gallium Anomaly

Tests of the solar neutrino detectors GALLEX (Cr1, Cr2) and SAGE (Cr, Ar)



Deficit could be due to overestimate of  $\sigma(\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-)$

Bahcall:

[Bahcall, PRC 56 (1997) 3391, hep-ph/9710491]

$$\sigma({}^{51}\text{Cr}) = 58.1 \times 10^{-46} \text{ cm}^2 \left( 1^{+0.036}_{-0.028} \right)_{1\sigma} \Rightarrow R_{\text{Ga}} = 0.86 \pm 0.05$$

[SAGE, PRC 73 (2006) 045805, nucl-ex/0512041]

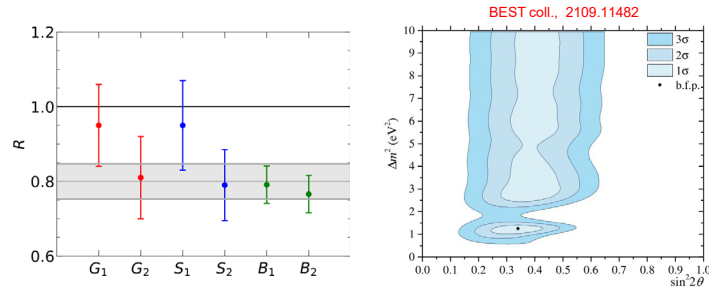
Haxton:

[Hata, Haxton, PLB 353 (1995) 422, nucl-th/9503017; Haxton, PLB 431 (1998) 110, nucl-th/9804011]

$$\sigma({}^{51}\text{Cr}) = 63.9 \times 10^{-46} \text{ cm}^2 (1 \pm 0.106)_{1\sigma} \Rightarrow R_{\text{Ga}} = 0.76^{+0.09}_{-0.08}$$

[SAGE, PRC 59 (1999) 2246, hep-ph/9803418]

## The Gallium anomaly



The Gallium anomaly is now at more than 5 $\sigma$  significance

## The Known Unknowns

★ Next generation Long-Baseline experiments (such as DUNE) can address three of these questions:

- Are neutrinos Dirac or Majorana ?
  - Is there a connection to the GUT scale?
- Are there light sterile neutrino states ? Breaks 3-flavor paradigm
  - No clear theoretical guidance on mass scale,  $M$ , ...
- What is the neutrino mass hierarchy ?
  - An important question in flavor physics, e.g. CKM vs. PMNS



- Is CP violated in the leptonic sector ?
  - Are  $\nu$ s key to understanding the matter-antimatter asymmetry?

## In principle, it is straightforward

- ★ CPV  $\Rightarrow$  different oscillation rates for  $\nu$ s and  $\bar{\nu}$ s

$$P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = 4s_{12}s_{13}c_{13}^2s_{23}c_{23}\sin\delta \leftarrow \boxed{\text{vacuum osc.}}$$

$$\times \left[ \sin\left(\frac{\Delta m_{21}^2 L}{4E}\right) \times \sin\left(\frac{\Delta m_{23}^2 L}{4E}\right) \times \sin\left(\frac{\Delta m_{31}^2 L}{4E}\right) \right]$$

- ★ Requires  $\{\theta_{12}, \theta_{13}, \theta_{23}\} \neq \{0, \pi\}$ 
  - now know that this is true,  $\theta_{13} \approx 9^\circ$
  - but, despite hints, don't yet know "much" about  $\delta$
- ★ So "just" measure  $P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$  ?
- ★ Not quite, there is a complication...

## Neutrino Oscillations in Matter

- ★ Accounting for this potential term, gives a Hamiltonian that is not diagonal in the basis of the mass eigenstates

$$\mathcal{H} \begin{pmatrix} |\nu_1\rangle \\ |\nu_2\rangle \\ |\nu_3\rangle \end{pmatrix} = i \frac{d}{dt} \begin{pmatrix} |\nu_1\rangle \\ |\nu_2\rangle \\ |\nu_3\rangle \end{pmatrix} = \begin{pmatrix} E_1 & 0 & 0 \\ 0 & E_2 & 0 \\ 0 & 0 & E_3 \end{pmatrix} \begin{pmatrix} |\nu_1\rangle \\ |\nu_2\rangle \\ |\nu_3\rangle \end{pmatrix} + V|\nu_e\rangle \leftarrow \boxed{\text{ME}}$$

- ★ Complicates the simple picture !!!!

$$P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) =$$

$$\text{ME} \quad \frac{16A}{\Delta m_{31}^2} \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right) c_{13}^2 s_{13}^2 s_{23}^2 (1 - 2s_{13}^2)$$

$$\text{ME} \quad - \frac{2AL}{E} \sin\left(\frac{\Delta m_{31}^2 L}{4E}\right) c_{13}^2 s_{13}^2 s_{23}^2 (1 - 2s_{13}^2)$$

$$\text{CPV} \quad - 8 \frac{\Delta m_{21}^2 L}{2E} \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right) \sin\delta s_{13} c_{13}^2 c_{23} s_{23} c_{12} s_{12}$$

$$\text{with } A = 2\sqrt{2}G_F n_e E = 7.6 \times 10^{-5} \text{eV}^2 \cdot \frac{\rho}{\text{g cm}^{-3}} \cdot \frac{E}{\text{GeV}}$$

## Experimental Strategy

### EITHER:

- ★ Keep L small (~200 km): so that matter effects are insignificant

- First oscillation maximum:

$$\frac{\Delta m_{31}^2 L}{4E} \sim \frac{\pi}{2} \Rightarrow E_\nu < 1 \text{ GeV}$$

- Want high flux at oscillation maximum

⇒ **Off-axis beam:** narrow range of neutrino energies

### OR:

- ★ Make L large (>1000 km): measure the matter effects (i.e. MH)

- First oscillation maximum:

$$\frac{\Delta m_{31}^2 L}{4E} \sim \frac{\pi}{2} \Rightarrow E_\nu > 2 \text{ GeV}$$

- **Unfold CPV from Matter Effects through E dependence**

⇒ **On-axis beam:** wide range of neutrino energies

## Non standard neutrino interactions

They can be described by effective four-fermion operators of the form

$$2\sqrt{2}G_F \varepsilon_{\alpha\beta} (\bar{\nu}_\beta \gamma^\mu P_L l_\alpha) (\bar{f} \gamma_\mu P_{L,R} f')$$

normalizing the operator with the Fermi constant

$$\varepsilon_{\alpha\beta} = \frac{M_W^2}{M_{NSI}^2}$$



We are left “only” with neutral current NSNI

$$2\sqrt{2}G_F \varepsilon_{\alpha\beta} (\bar{\nu}_\beta \gamma^\mu P_L \nu_\alpha) (\bar{f} \gamma_\mu P_{L,R} f)$$

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \frac{1}{2E} \left[ U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} U^\dagger + a \begin{pmatrix} 1 + \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{e\mu}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{e\tau}^* & \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

$$a \equiv 2\sqrt{2}G_F n_e E$$

$$H = \frac{1}{2E} \left[ U \begin{pmatrix} 0 & & \\ & \Delta m_{32}^2 & \\ & & \end{pmatrix} U^\dagger + a \begin{pmatrix} \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix} \right]$$

## CPT violation



$$\frac{|m(K_0) - m(\overline{K}_0)|}{m_{K-av}} < 10^{-18}$$

$$m_{K-av} \approx \frac{1}{2} 10^9 \text{ eV}$$

$$(m(K_0) - m(\overline{K}_0))(m(K_0) + m(\overline{K}_0)) < 2 \cdot 10^{-18} m_{K-av}^2$$

$$|m^2(K_0) - m^2(\overline{K}_0)| \approx \frac{1}{2} \text{ eV}^2$$

## CPT tests

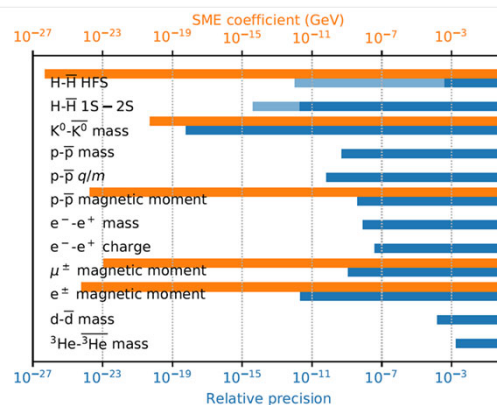
CPT invariance tested in several matter-antimatter systems:

neutral kaons

electron/positron

proton/antiproton

H/anti-H



E. Widmann, arXiv:2111.04056 [hep-ex]

Several experiments at the Antiproton Decelerator and ELENA (Extra Low Energy Antiproton) @CERN

## Current bounds

- We can use data of various experiments to calculate the neutrino and antineutrino oscillation parameters:

- Solar neutrino data:  $\theta_{12}, \Delta m_{21}^2, \theta_{13}$

- Neutrino mode in LBL:  $\theta_{23}, \Delta m_{31}^2, \theta_{13}$

- KamLAND data:  $\bar{\theta}_{12}, \Delta \bar{m}_{21}^2, \bar{\theta}_{13}$

- SBL reactors:  $\bar{\theta}_{13}, \Delta \bar{m}_{31}^2$

- Antineutrino mode in LBL:  $\bar{\theta}_{23}, \Delta \bar{m}_{31}^2, \bar{\theta}_{13}$

- No bounds on CP-phases since all values are allowed

Parameter	Main contribution	Other contributions
$\theta_{12}$	SOL	KamLAND
$\theta_{13}$	REAC	ATM+LBL and SOL+KamLAND
$\theta_{23}$	ATM+LBL	-
$\delta_{CP}$	LBL	ATM
$\Delta m_{21}^2$	KamLAND	SOL
$ \Delta m_{31}^2 $	LBL+ATM+REAC	-
MO	LBL+REAC and ATM	-

SOL: Solar  
ATM: Atmospheric neutrinos

LBL: Long baseline accelerator experiments  
REAC: Short-baseline reactor experiments

## Current bounds

- We use the same data (except atmospheric neutrinos) as for the global fit to obtain

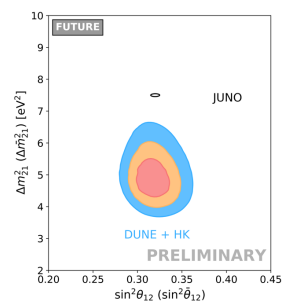
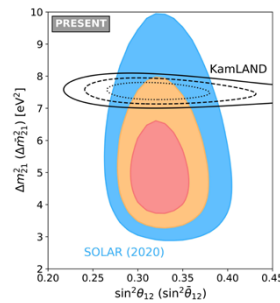
$$|\Delta m_{21}^2 - \Delta \bar{m}_{21}^2| < 4.7 \times 10^{-5} \text{ eV}^2,$$

$$|\Delta m_{31}^2 - \Delta \bar{m}_{31}^2| < 2.5 \times 10^{-4} \text{ eV}^2,$$

$$|\sin^2 \theta_{12} - \sin^2 \bar{\theta}_{12}| < 0.14,$$

$$|\sin^2 \theta_{13} - \sin^2 \bar{\theta}_{13}| < 0.029,$$

$$|\sin^2 \theta_{23} - \sin^2 \bar{\theta}_{23}| < 0.19.$$



G.B., C. Ternes and M. Tortola, 2005.05975, JHEP2020



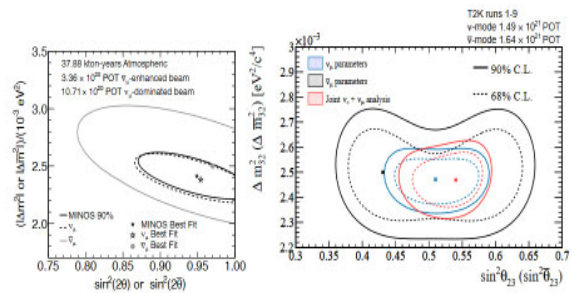
## T2K results, a hint ?

- T2K studied neutrino and anti-neutrino oscillations separated

$$\sin^2 \theta_{23} = 0.51, \quad \Delta m_{32}^2 = 2.53 \times 10^{-3} \text{eV}^2$$

$$\sin^2 \bar{\theta}_{23} = 0.42, \quad \Delta \bar{m}_{32}^2 = 2.55 \times 10^{-3} \text{eV}^2$$

- Results are consistent with
- CPT-conservation



- In experiments and in fits normally you assume CPT-conservation
- If CPT is not conserved this leads to impostor (fake) solutions in the fits
- To perform the standard fit you would calculate

$$\chi_{\text{total}}^2 = \chi^2(\nu) + \chi^2(\bar{\nu})$$

and then minimize this function

$$h(x, y) = f(x) + g(y)$$

$$\partial_x f(x) = 0 \quad \partial_y g(y) = 0$$

$$x = y$$

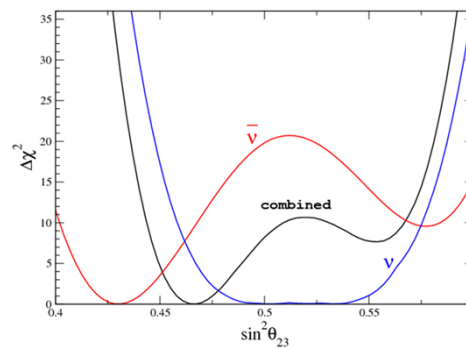
$$h(x) = f(x) + g(x)$$

$$\partial_x f(x) = \partial_x g(x) = 0$$

$$\partial_x f(x) = -\partial_x g(x)$$

## Obtaining impostor solutions

- This was done for  $\sin^2(\theta_{23}) = 0.5$ ,  $\sin^2(\bar{\theta}_{23}) = 0.43$



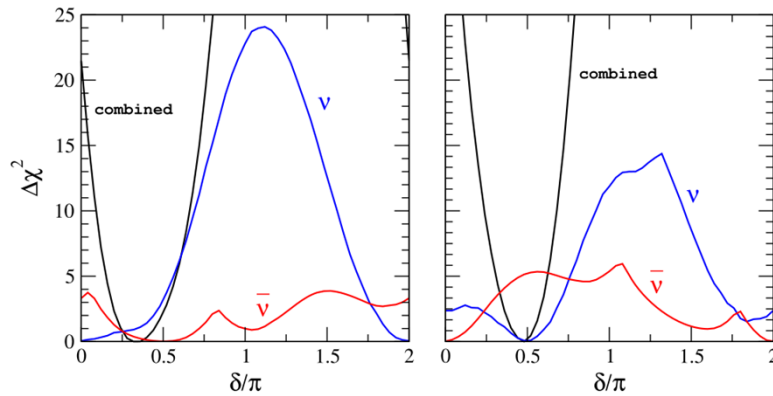
Combined best fit value is now

$$\sin^2(\theta_{23}^{\text{comb}}) = 0.467$$

Real true values are disfavored at close to  $3\sigma$  and more  $5\sigma$  confidence levels

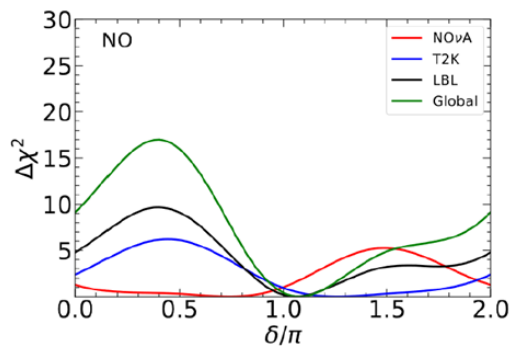
This can also happen

$$\delta = \begin{cases} \pi/2 \\ 0 \end{cases} \text{ and } \bar{\delta} = \begin{cases} 0 \\ \pi/2 \end{cases}$$



G.B., C. Ternes and M. Tortola, JHEP 07 (2020) 155

$\theta_{13} \neq \bar{\theta}_{13}$  can account for different behavior in neutrino and antineutrino channels



all values of  $\delta$  and  $\bar{\delta}$  remain allowed at  $\sim 1\sigma$

Tension between NOνA, T2K and SK atm. and  $\delta_{\text{bf}} = 1.08\pi$

- Disfavours:
  - $\delta = \pi/2$  at  $4.0\sigma$
  - $\delta = 0$  at  $3.0\sigma$
  - $\delta = 3\pi/2$  with  $\Delta\chi^2 = 4.9$

The increasing precision in neutrino oscillation measurements requires a thorough analysis of the assumptions considered.



## Distinguishing CPT violation from NSNI

The muon neutrino survival probability in matter can be written as

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta_\nu \sin^2 \left( \frac{\Delta m_\nu^2 L}{4E} \right).$$

in matter

$$\begin{aligned} \Delta m_\nu^2 \cos 2\theta &= 4\Delta m^4 = \Delta m_\nu^4 + \Delta m_\bar{\nu}^4 + 2\Delta m_\nu^2 \Delta m_\bar{\nu}^2 \cos(2\theta_\nu - 2\theta_\bar{\nu}) - \epsilon_{\tau\tau} A, \\ \Delta m_\nu^2 \sin 2\theta &= -2\epsilon_{\mu\tau} A. \end{aligned}$$

$$\sin^2(2\theta) = \frac{(\Delta m_\nu^2 \sin(2\theta_\nu) + \Delta m_\bar{\nu}^2 \sin(2\theta_\bar{\nu}))^2}{\Delta m_\nu^4 + \Delta m_\bar{\nu}^4 + 2\Delta m_\nu^2 \Delta m_\bar{\nu}^2 \cos(2\theta_\nu - 2\theta_\bar{\nu})}$$

$$2\epsilon_{\tau\tau}^m A = \Delta m_\nu^2 \cos(2\theta_\nu) - \Delta m_\bar{\nu}^2 \cos(2\theta_\bar{\nu})$$

$$4\epsilon_{\mu\tau}^m A = \Delta m_\nu^2 \sin(2\theta_\nu) - \Delta m_\bar{\nu}^2 \sin(2\theta_\bar{\nu})$$

G.B., C. Ternes and M. Tortola, Eur.Phys.J.C 79 (2019) 5, 390

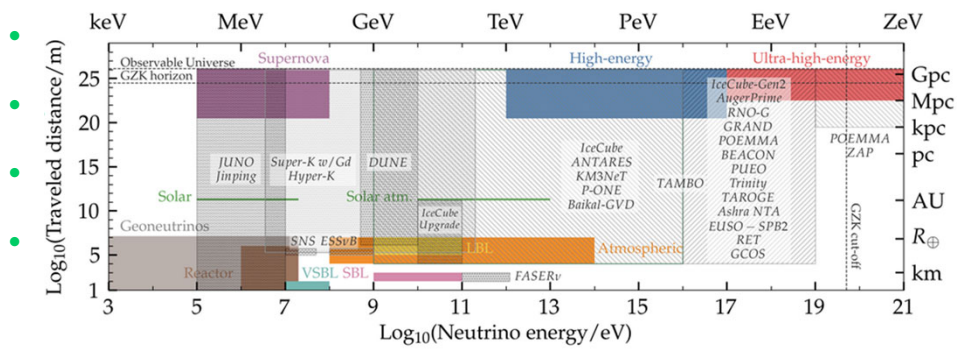


## Violations of Lorentz invariance

$$(h_{\text{eff}})_{ab} = \frac{m_{ab}^2}{2E} + \frac{1}{E} [(a_L)^\alpha p_\alpha - (c_L)^{\alpha\beta} p_\alpha p_\beta]_{ab}$$

↻ standard Lorentz covariant term     
 ↻ violates both CPT and Lorentz invariance     
 ↻ Lorentz violation

## Conclusions: Neutrino physics will continue delivering results



precision  
 Extraordinary ~~claims~~ requires extraordinary ~~evidence~~ caution



