



Universität Regensburg

# Anomalous Higgs boson couplings in WBF Higgs boson production

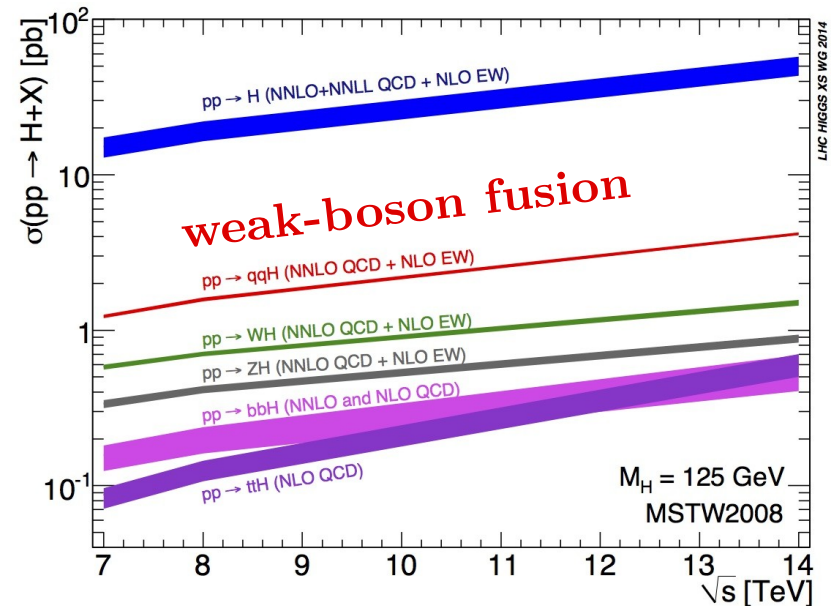
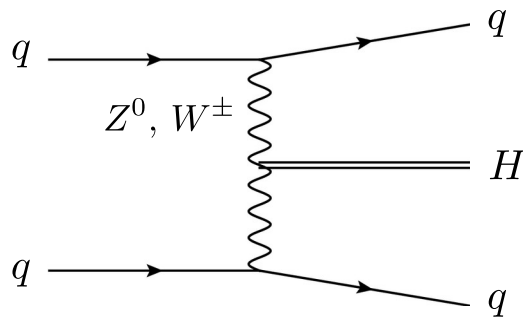
Konstantin Asteriadis | 10/04/2023

BROOKHAVEN FORUM 2023

For more details see Phys. Rev. D 107 (2023) 3, 034034.

Work done at BNL in collaboration with Fabrizio Caola, Kirill Melnikov and Raoul Röntsch.

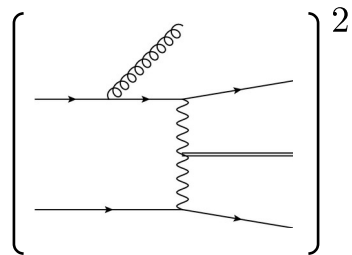
# Higgs-boson production in weak-boson fusion (WBF)



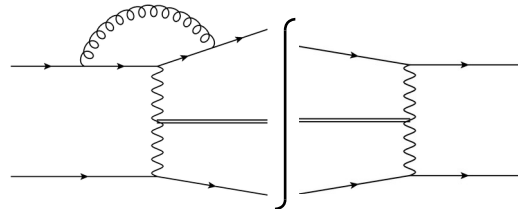
- Important production channel of Higgs boson @LHC (second highest cross section @14TeV)
- Probes electro-weak sector
- Very distinct signature

# Higher order QCD correction to vector-boson fusion

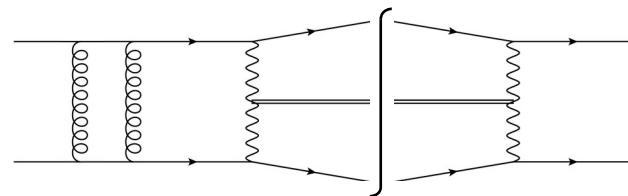
- 2 classes of corrections to the amplitude squared:



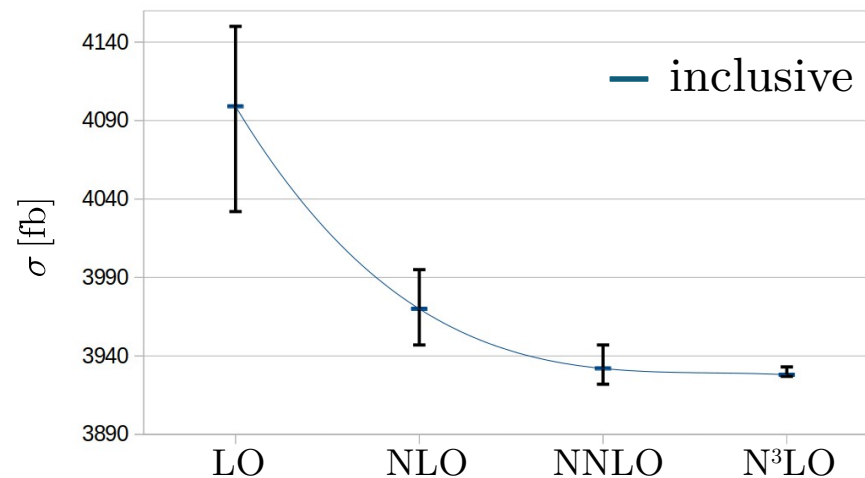
*factorizable (in the following)*



*non-factorizable*

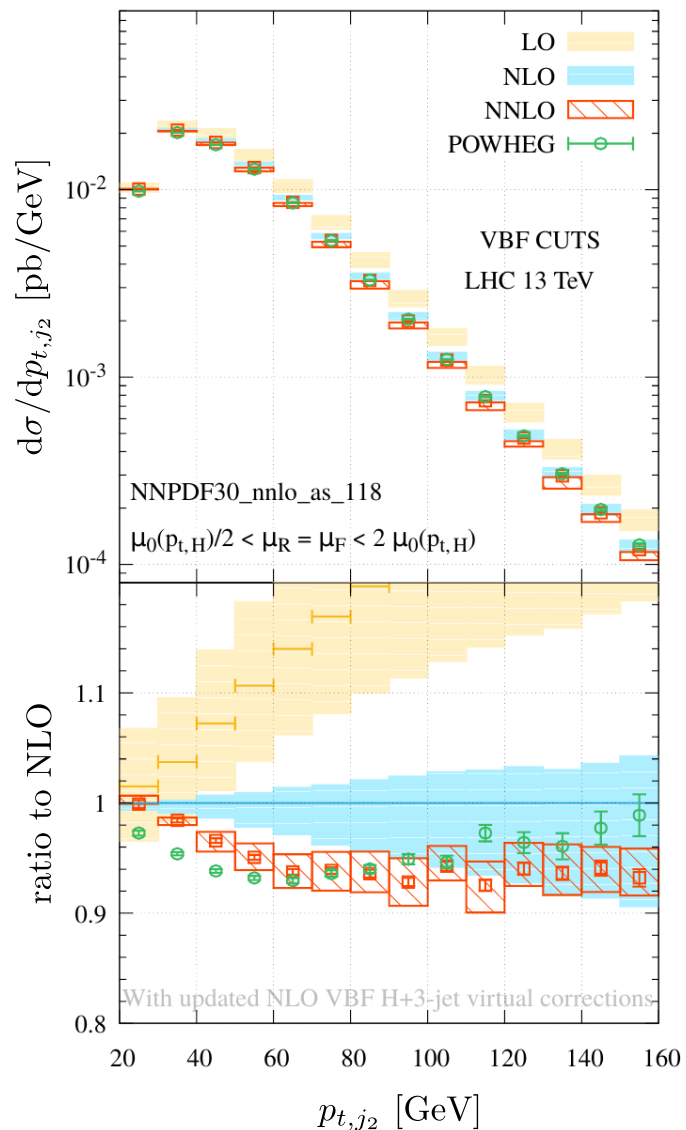


- **Inclusive** known till **N<sup>3</sup>LO** [Dreyer, Karlberg '16]  
→ Nicely converging, N<sup>3</sup>LO within residual scale uncertainties
- **Fully differential** known till **NNLO** [Cacciari, Dreyer, Karlberg, Salam, Zanderighi '15; Cruz-Martinez, Glover, Gehrmann, Huss '18]  
→ **Fiducial cuts:** NNLO corrections outside of residual NLO scale uncertainties

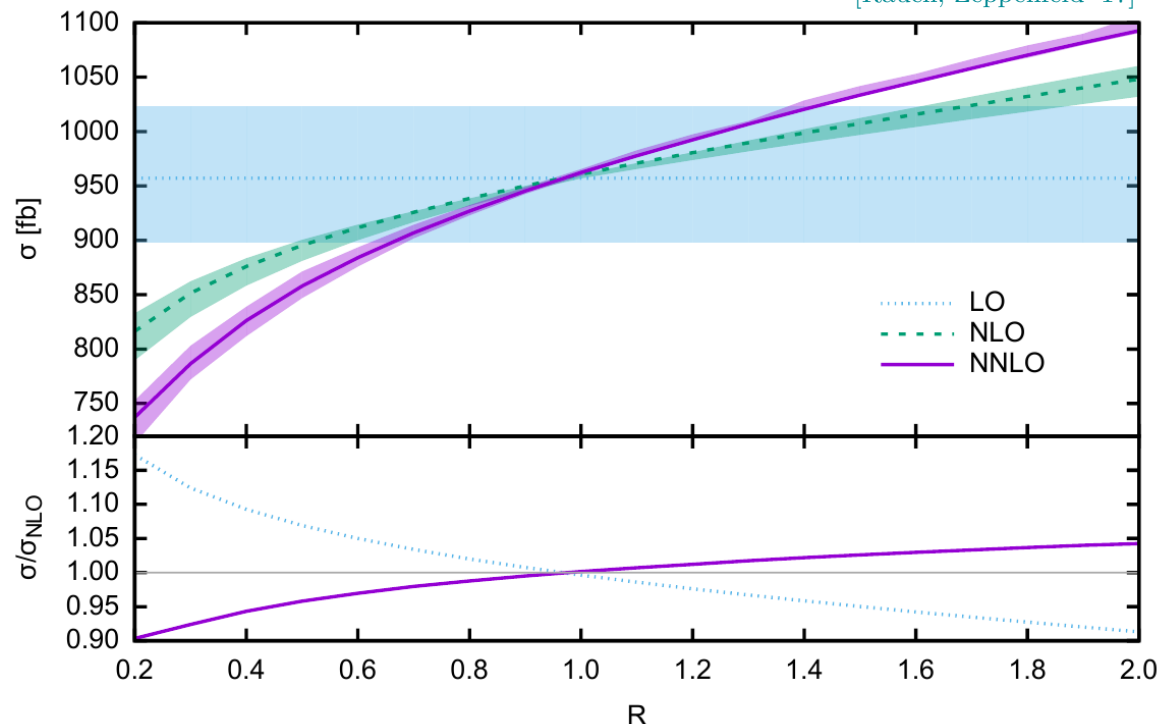


# Effect of fiducial cuts

[Cacciari, Dreyer, Karlberg, Salam, Zanderighi '15]



[Rauch, Zeppenfeld '17]



- **Non-trivial jet dynamics in WBF Higgs boson production**
- **New Physics:**
  - New operators  $\rightarrow$  New tensor structures
  - Studied at NLO QCD [Hankela, Klämke, Zeppenfeld '06]
    - $\rightarrow$  Potential interplay with real radiation at higher orders
    - $\rightarrow$  Can we trust NLO analysis?
  - Higgs coupling to weak bosons measured to  $O(30\%)$

# Anomalous HVV interactions

- Most general tensor structure of the HVV vertex (Lorentz invariance / Bose symmetry)

$$H \text{---} \bullet \text{---} \bar{V}_\nu \text{---} V_\mu = i \left[ g^{\mu\nu} A(p_1^2, p_2^2, p_1 \cdot p_2) + p_1^\nu p_2^\mu B(p_1^2, p_2^2, p_1 \cdot p_2) + i \epsilon^{\mu\nu\rho\sigma} p_{1,\rho} p_{2,\sigma} C(p_1^2, p_2^2, p_1 \cdot p_2) \right]$$

only dimension 6 SMEFT [Helset, Martin, Trott '20]

$$= i g_{HVV}^{(SM)} \left[ g^{\mu\nu} \left( 1 + \frac{m_H^2}{\Lambda^2} c_{HVV}^{(2)} \right) + \frac{p_1^2 + p_2^2}{\Lambda^2} c_{HVV}^{(1)} + \frac{2p_1^\nu p_2^\mu}{\Lambda^2} c_{HVV}^{(1)} - \tilde{c}_{HVV} (6\pi) \epsilon^{\mu\nu\rho\sigma} \frac{p_{1,\rho} p_{2,\sigma}}{\Lambda^2} \right]$$

“rescaling” of SM

CP-even coupling

CP-odd coupling

- $(6\pi)$  in CP-odd contribution such that  $\tilde{c}_{HVV} = 1 \rightarrow \mathcal{O}(1\%)$  deviation of the LO fiducial cross section
- Consider “symmetric” model where non-SM couplings to W and Z are identical (main difference accounted for via factoring out SM coupling)

# Fiducial cross section at any order

$$\begin{aligned}\sigma_{\text{fid}} = & \left(1 + \frac{m_H^2}{\Lambda^2} c_{HVV}^{(2)}\right)^2 X_1 + \left(c_{HVV}^{(1)}\right)^2 X_2 + \left(\tilde{c}_{HVV}\right)^2 X_3 + \left(1 + \frac{m_H^2}{\Lambda^2} c_{HVV}^{(2)}\right) c_{HVV}^{(1)} X_4 \\ & + \left(1 + \frac{m_H^2}{\Lambda^2} c_{HVV}^{(2)}\right) \tilde{c}_{HVV} X_5 + c_{HVV}^{(1)} \tilde{c}_{HVV} X_6.\end{aligned}$$

where

$$X_i = X_i^{\text{LO}} + \frac{\alpha_s}{4\pi} X_i^{\text{NLO}} + \left(\frac{\alpha_s}{4\pi}\right)^2 X_i^{\text{NNLO}} + \mathcal{O}(\alpha_s^3)$$

- $X_5 = X_6 = 0$  for fiducial cross sections because it is integrate over the full angular phase space
- Compute  $X_{1,2,3,4}$  individually

# Fiducial cross section at any order

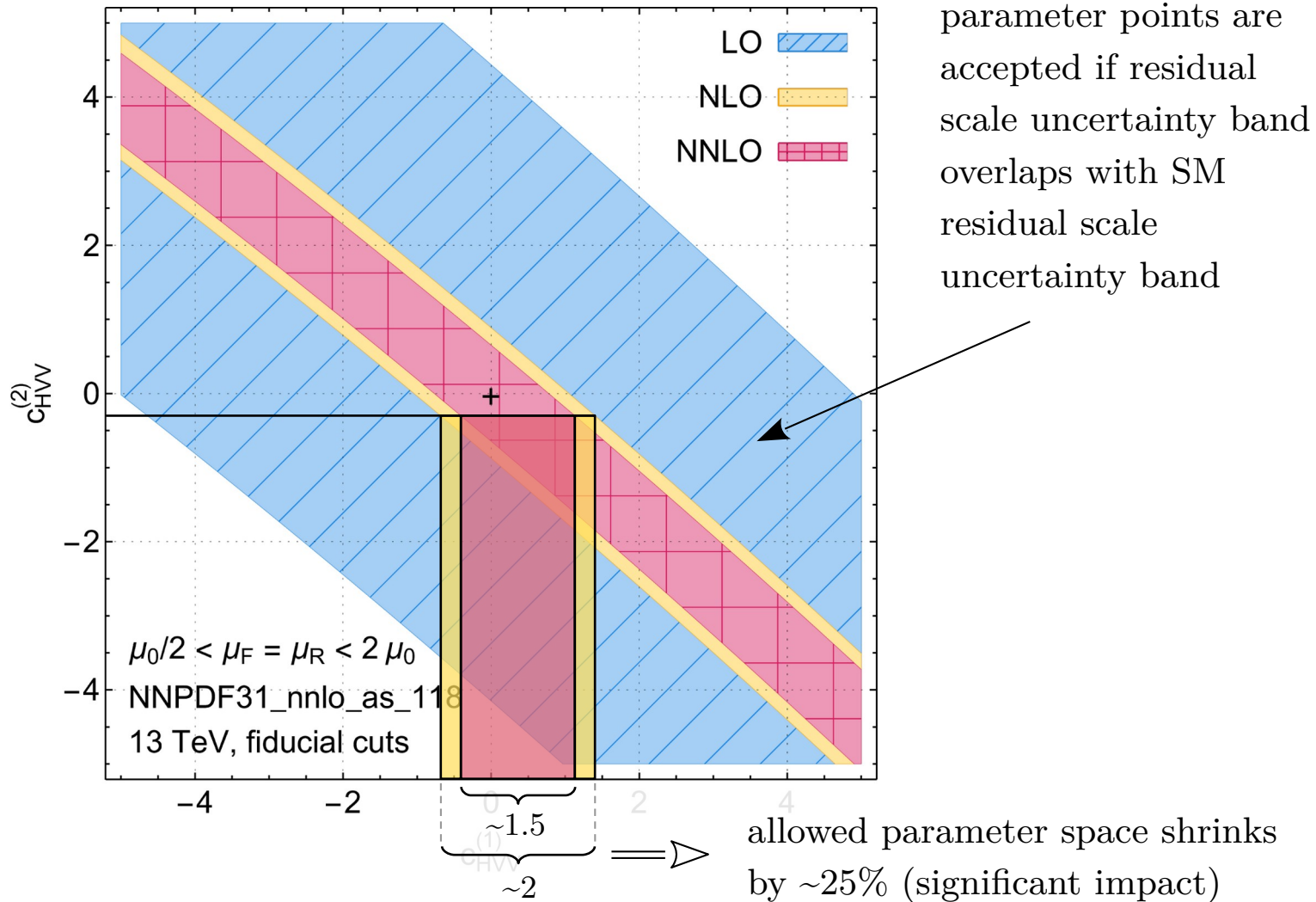
$$\sigma_{\text{fid}} = \left(1 + \frac{m_H^2}{\Lambda^2} c_{HVV}^{(2)}\right)^2 X_1 + \left(c_{HVV}^{(1)}\right)^2 X_2 + \left(\tilde{c}_{HVV}\right)^2 X_3 + \left(1 + \frac{m_H^2}{\Lambda^2} c_{HVV}^{(2)}\right) c_{HVV}^{(1)} X_4 \\ + \left(1 + \frac{m_H^2}{\Lambda^2} c_{HVV}^{(2)}\right) \tilde{c}_{HVV} X_5 + c_{HVV}^{(1)} \tilde{c}_{HVV} X_6.$$

- Results

$\sigma_{\text{fid}}$ (fb)	LO	NLO	NNLO
$X_1$	$971_{+69}^{-61}$	$890_{-18}^{+8}$	$859_{-10}^{+8}$
$X_2$	$0.413_{+0.039}^{-0.033}$	$0.398_{-0.005}^{-0.001}$	$0.383_{-0.005}^{+0.004}$
$X_3$	$19.57_{+2.22}^{-1.84}$	$19.64_{-0.07}^{-0.25}$	$19.25_{-0.18}^{+0.08}$
$X_4$	$26.43_{+1.80}^{-1.61}$	$23.45_{-0.66}^{+0.35}$	$22.53_{-0.42}^{+0.39}$

- $X_1$  largest (by construction since it corresponds to the SM contribution)
- Large scale uncertainty decrease from LO  $\rightarrow$  NLO; only  $\sim 20\%$  from NLO  $\rightarrow$  NNLO
- Similar k-factors for all  $X_{1,2,3,4}$  ( $\sim -4\%$  from NLO  $\rightarrow$  NNLO)
- Having  $X_{1,2,3,4}$  available allows to study the allowed parameter space

# Allowed parameter space: fiducial cross section



- Similar results for all pairs of anomalous couplings

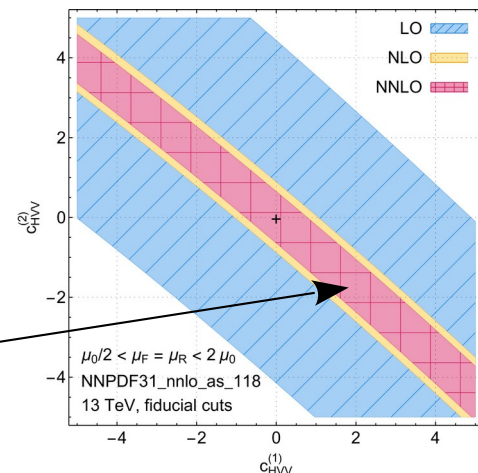


# Differential distributions

- Computing differential distributions is numerically expensive
- Hence instead of computing differential coefficients  $X_{1,2,3,4,5,6}$  we consider two fixed scenarios


Sc. A:  $c_{HVV}^{(1)} = +1.5$ ,  $c_{HVV}^{(2)} = -1.9$ ,  $\tilde{c}_{HVV} = +0.6$

Sc. B:  $c_{HVV}^{(1)} = -1.8$ ,  $c_{HVV}^{(2)} = -0.1$ ,  $\tilde{c}_{HVV} = -1.5$



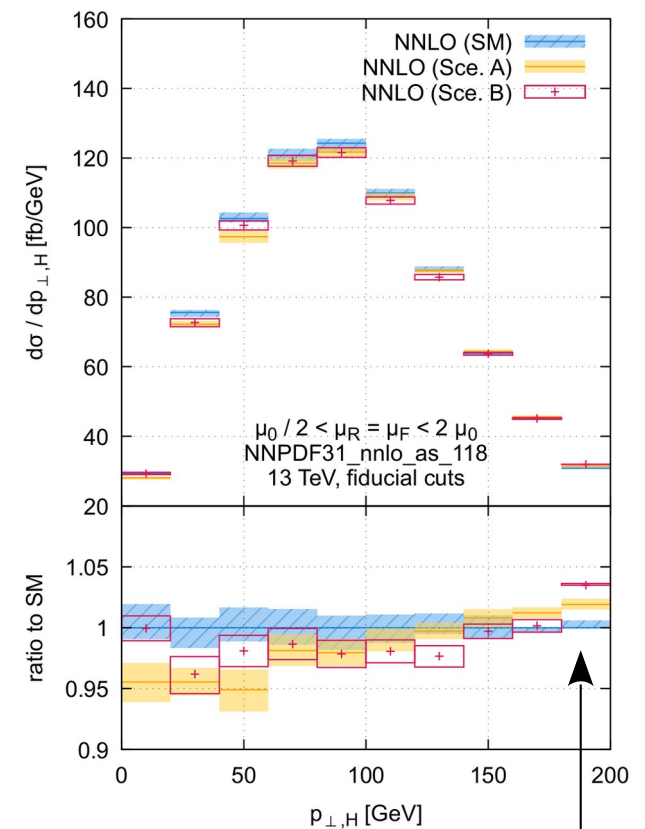
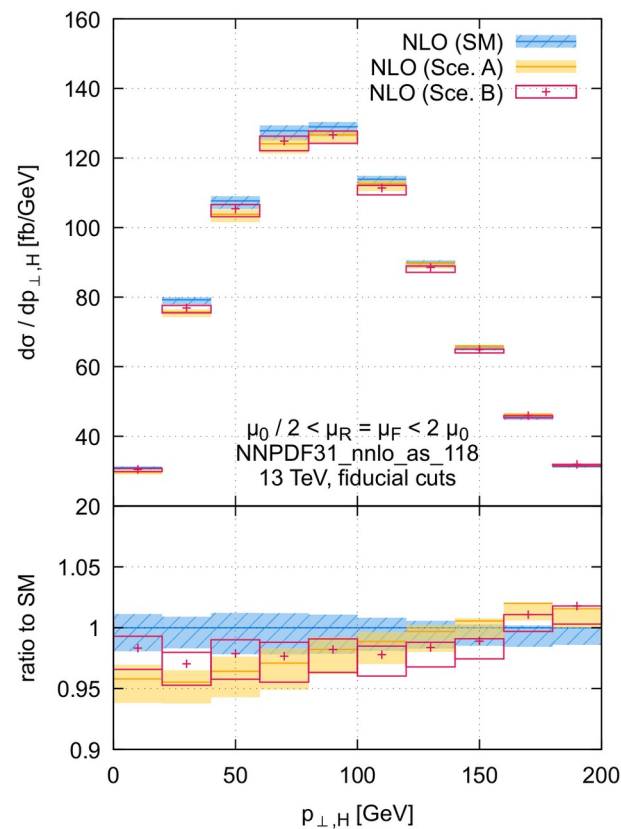
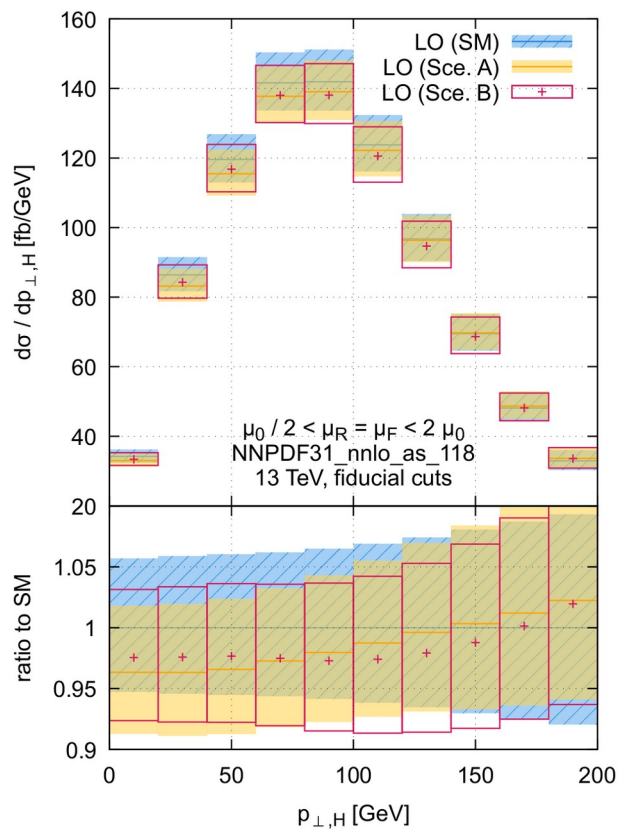
- They are chosen such that fiducial cross section are indistinguishable

$\sigma_{\text{fid}}$ (fb)	SM	Sc. A	Sc. B
LO	$971_{+69}^{-61}$	$960_{+68}^{-61}$	$965_{+71}^{-63}$
NLO	$890_{-18}^{+8}$	$882_{-17}^{+7}$	$890_{-17}^{+6}$
NNLO	$859_{-10}^{+8}$	$851_{-8}^{+9}$	$860_{-8}^{+8}$

  
 $\leq 1\%$  and covered by  
 residual scale uncertainties

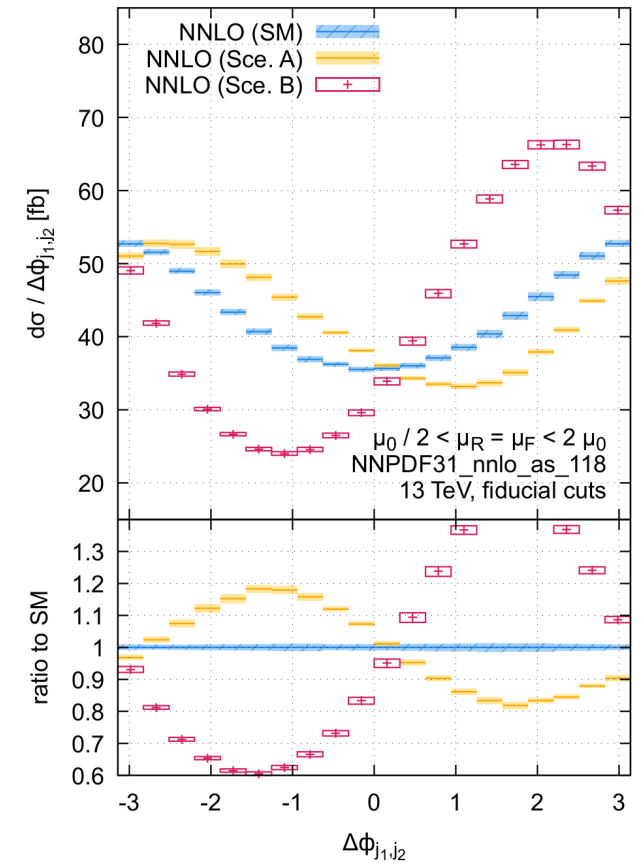
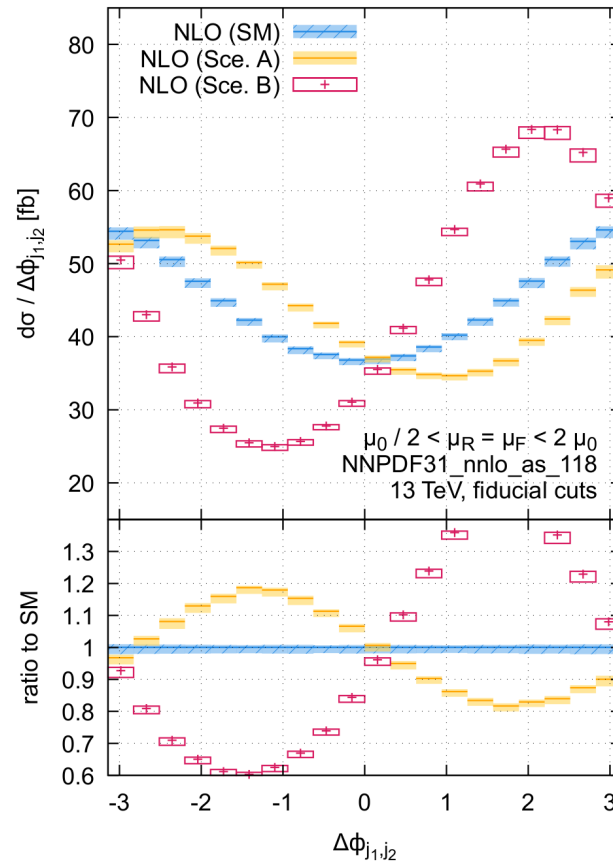
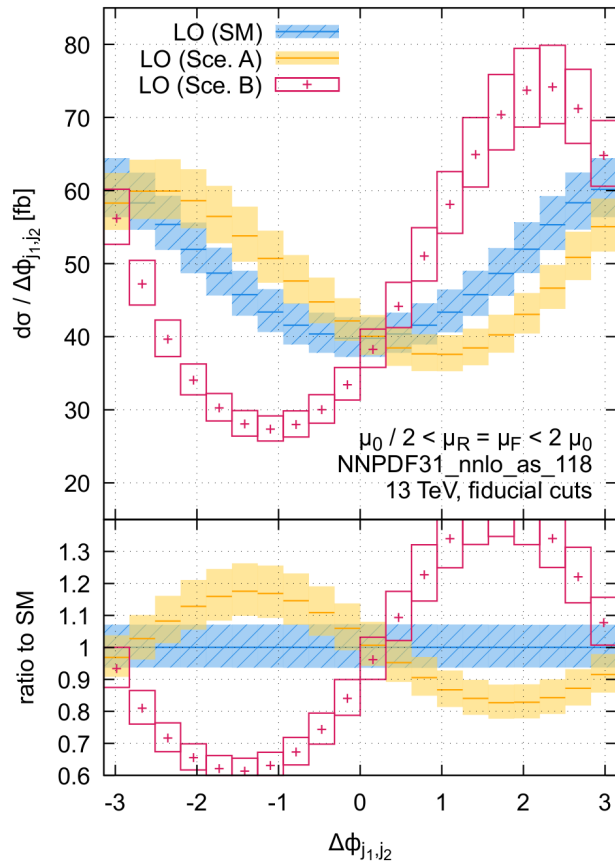
# Differential distributions

- Most distributions are **NOT** sensitive to anomalous couplings [Hankele, Klämke, Zeppenfeld '06]
- For example consider Higgs transverse momentum distribution



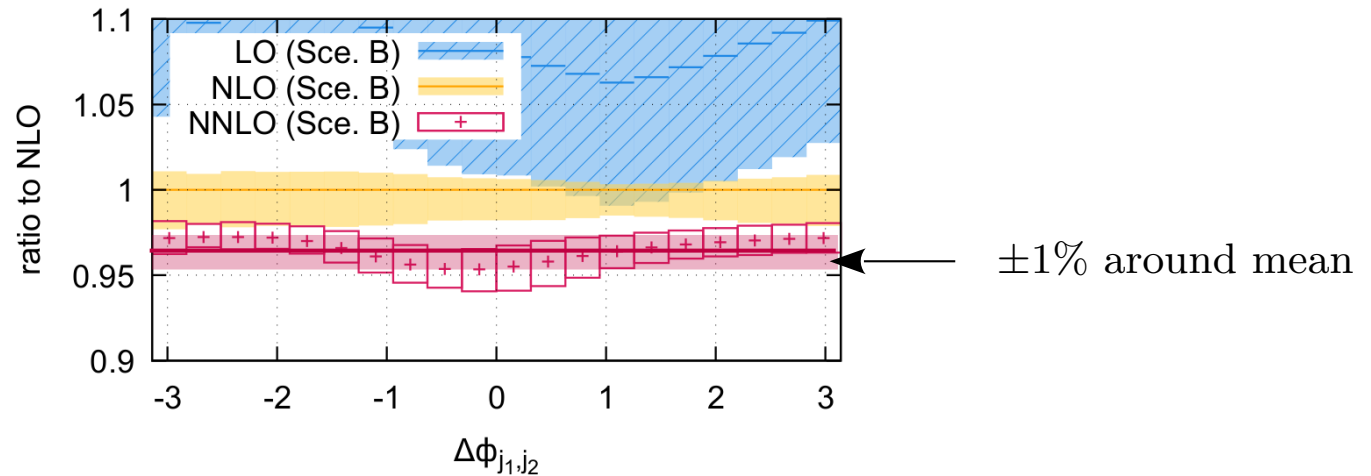
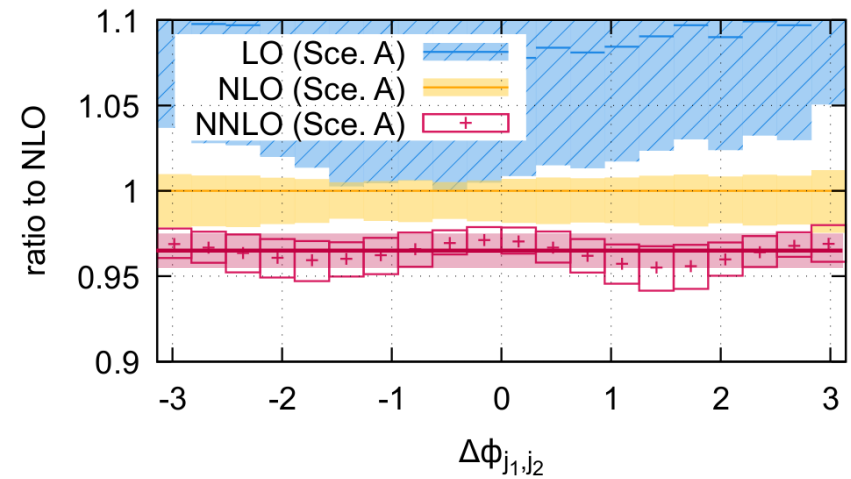
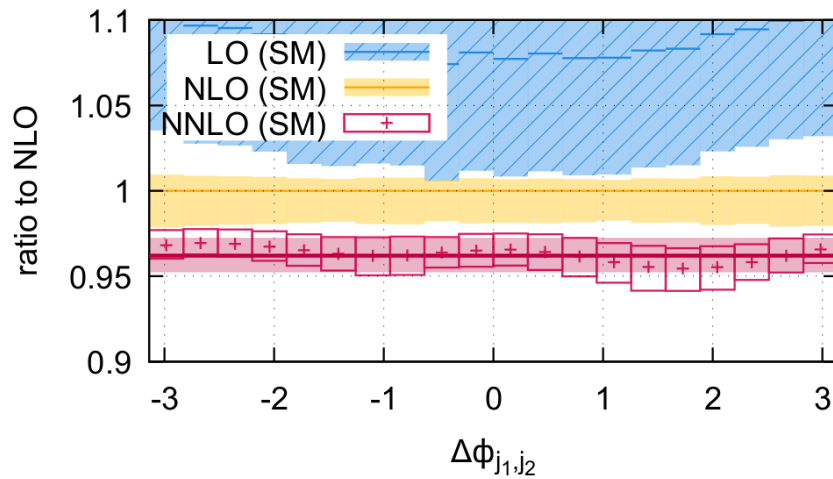
start of diverging distributions, expected  
but cross section already down by an order

# $\Delta\varphi$ a CP sensitive observable



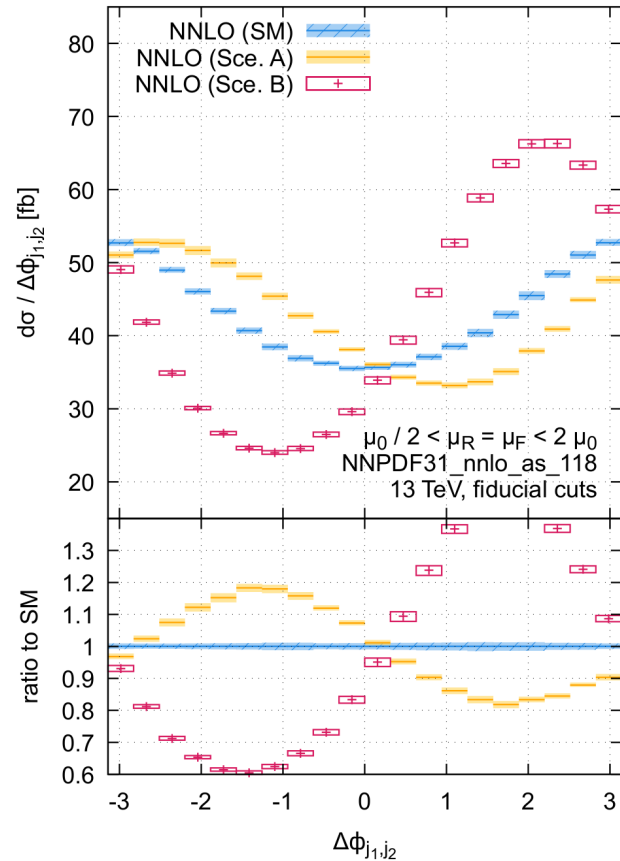
- At LO: Sce. B and SM distinguishable, Sce. A and SM just covered by scale variation
- Similar to fiducial cross section: no significant reduction of scale uncertainties from NLO  $\rightarrow$  NNLO

# $\Delta\varphi$ a CP sensitive observable



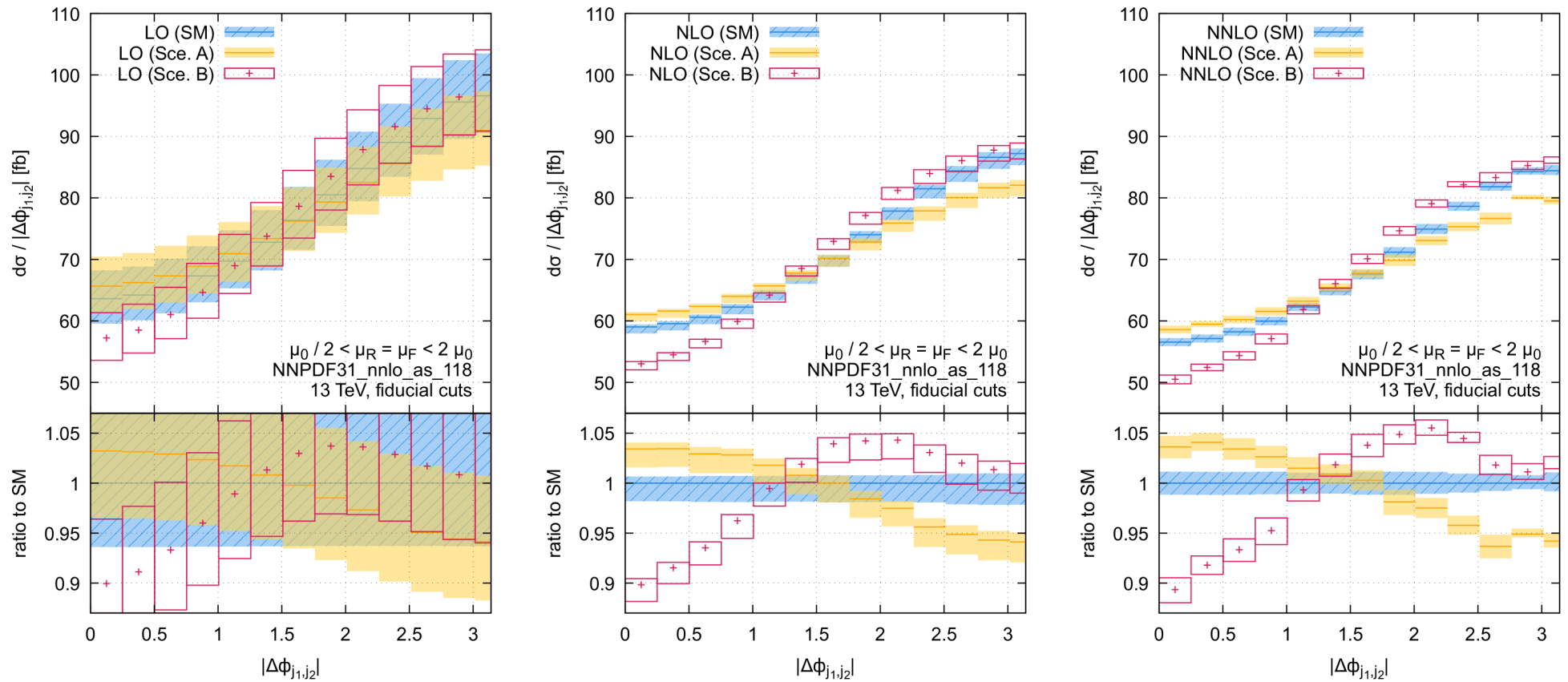
- K-factor rather flat and almost independent of anomalous couplings
- K-factors rather flat  $\rightarrow$  global rescaling from NLO to NNLO should be sufficient for  $O(1\%)$

# $\Delta\varphi$ a CP sensitive observable



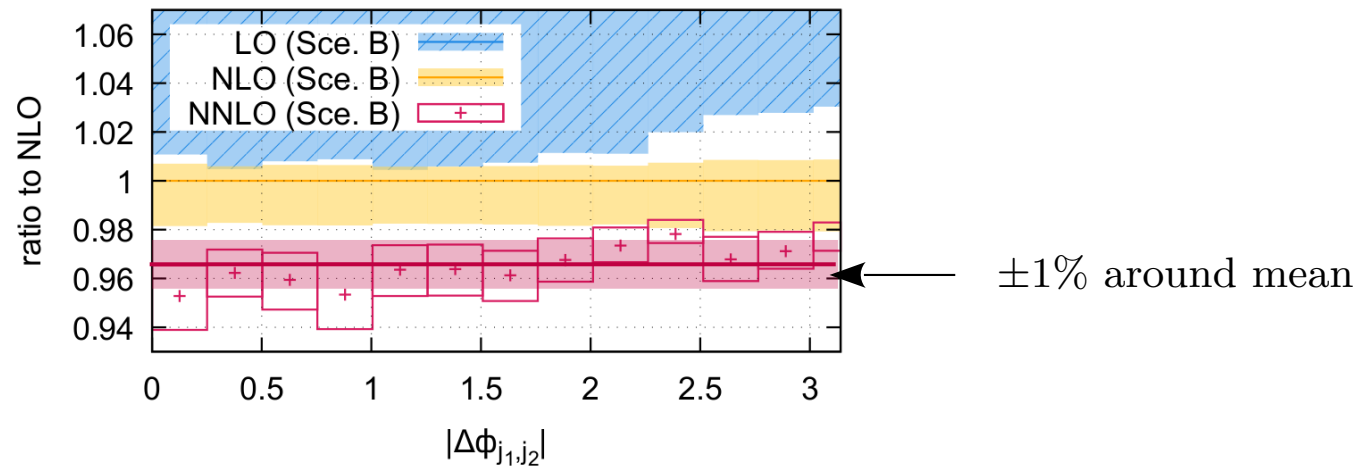
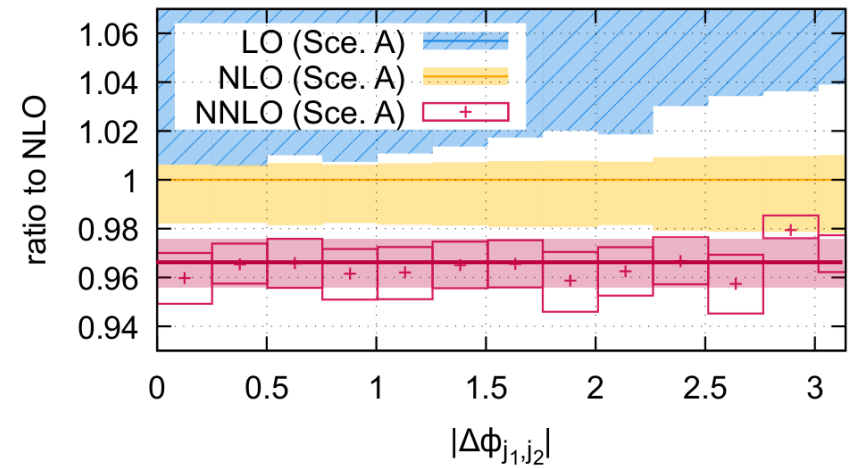
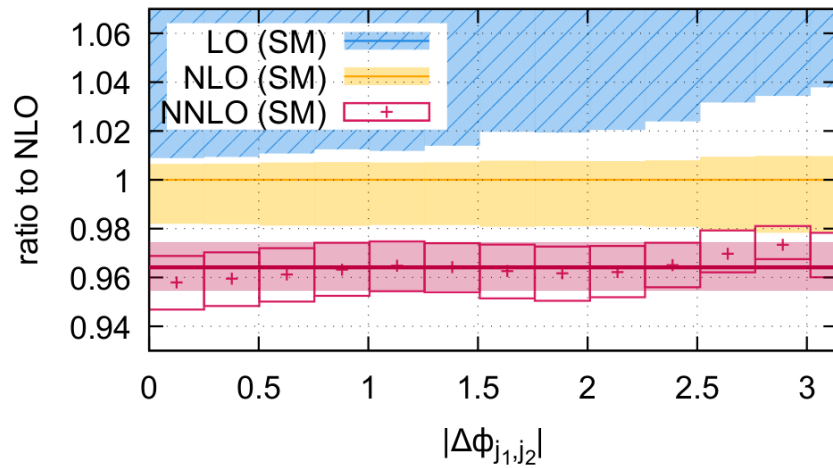
- Deviation(s) from SM dominated by antisymmetric contributions  $\rightarrow$  CP-odd / CP-even interference
- Ratio of events with  $\Delta\varphi < 0$  and  $\Delta\varphi > 0$  might be useful to include differential data in exclusion plots in a efficient way (cut-and-count approach)
- To study CP-even couplings, consider absolute value of  $\Delta\varphi$  where CP-odd / CP-even interference again drops out

# $|\Delta\varphi|$ a CP insensitive observable



- At LO differences are swamped by scale uncertainty
- Starting from NLO scale uncertainties sufficiently reduced to distinguish between different scenarios and SM; NNLO might help to distinguish from SM
- Ratio of events with  $|\Delta\varphi| < \pi/2$  and  $|\Delta\varphi| > \pi/2$  might be useful to include differential data in exclusion plots in a efficient way (cut-and-count approach)

# $|\Delta\varphi|$ a CP insensitive observable



- K-factor rather flat and almost independent of anomalous couplings
- K-factors rather flat  $\rightarrow$  global rescaling from NLO to NNLO should be sufficient for  $O(1\%)$

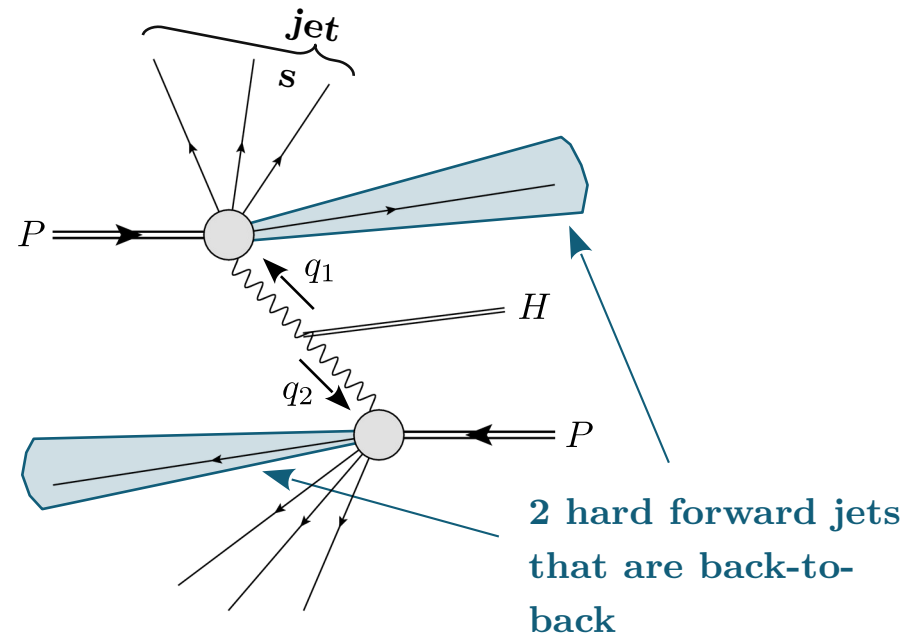
# Conclusion and Outlook

- Higher order QCD corrections in New Physics scenarios similar to SM
  - No significant shape change from NLO → NNLO
  - May be captured with global K-factor
- NLO and NNLO have similar “discriminating power”
  - NNLO study indicates analysis at NLO is robust
- **Future work:** Include differential data into exclusion plots
- **Future work:** Include higher order operators (In particular once that are directly affected by QCD) radiation; allow for different HZZ and HWW couplings



**Miscellaneous**

# $\Delta\varphi$ a CP sensitive observable

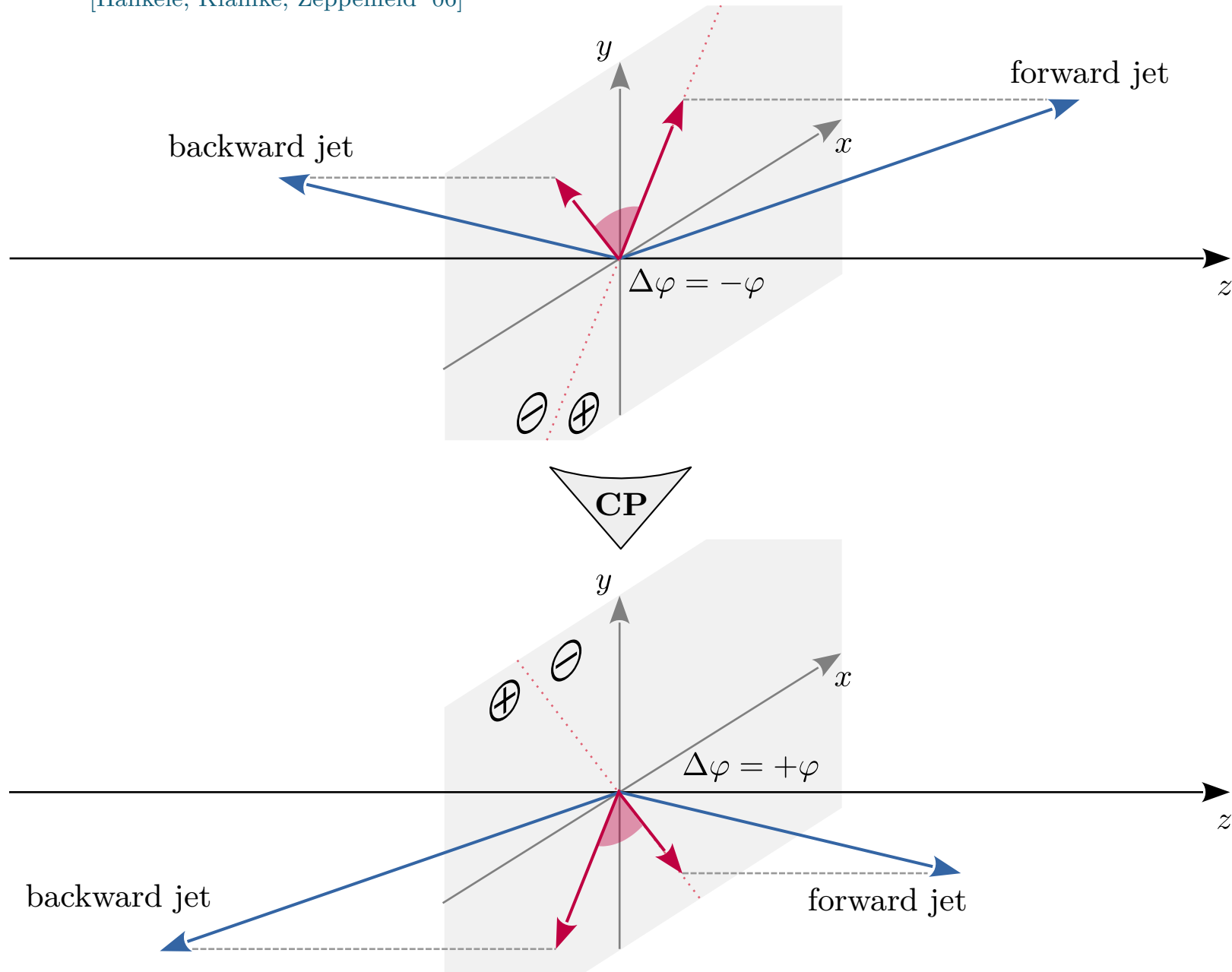


## Typical VBF cuts:

- At least 2 resolved “tag” jets with  $p_{\perp,j} > 25 \text{ GeV}$  and  $-4.5 < y_j < 4.5$
- Separated in rapidity  $|y_{j_1} - y_{j_2}| > 4.5$  and in different hemispheres  $y_{j_1} \times y_{j_2} < 0$
- Invariant mass  $\sqrt{(p_{j_1} + p_{j_2})^2} > 600 \text{ GeV}$
- Jets identified using anti-kt jet-algorithm with  $R = 0.4$

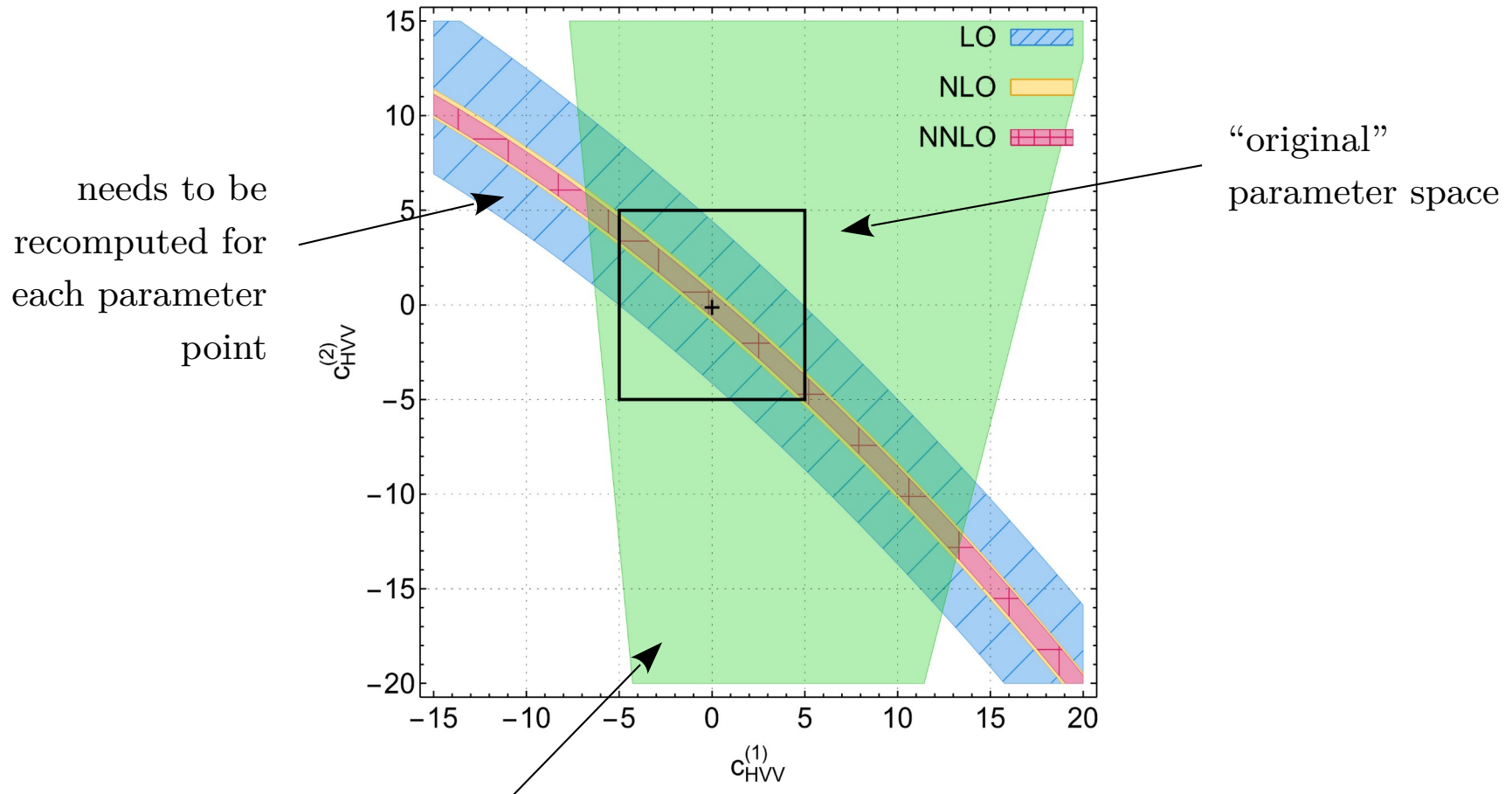
# $\Delta\varphi$ a CP sensitive observable

[Hankele, Klämke, Zeppenfeld '06]



# Numerical control and extrapolation to parameter space

- **Area** where numerical error is *smaller-equal* then the residual scale uncertainty



Is this enough? Yes! (c.f. differential distributions later)

# Connection to SMEFT Wilson coefficients in Warsaw basis

$$\begin{aligned}
 c_{HWW}^{(1)} &= \frac{C_{\phi W}}{\sqrt{2}G_f M_W^2}, & c_{HZZ}^{(1)} &= \frac{1}{\sqrt{2}G_f M_Z^4} \left[ C_{\phi B}(M_Z^2 - M_W^2) \right. \\
 & & & \left. + C_{\phi W}M_W^2 + C_{\phi WB}M_W\sqrt{M_Z^2 - M_W^2} \right], \\
 c_{HWW}^{(2)} &= -\frac{1}{\sqrt{2}G_f} \left[ \frac{C_{\phi W}}{M_W^2} + \frac{2C_{\phi l}^{(3)} - C_{ll}}{2m_H^2} - \frac{4C_{\phi\Box} - C_{\phi D}}{4m_H^2} \right], \\
 \tilde{c}_{HWW} &= -\frac{2C_{\phi\tilde{W}}}{(6\pi)\sqrt{2}G_f M_W^2}, \\
 c_{HZZ}^{(2)} &= -\frac{1}{\sqrt{2}G_f} \left[ \frac{C_{\phi B}(M_Z^2 - M_W^2)}{M_Z^4} + \frac{C_{\phi W}M_W^2}{M_Z^4} + \frac{C_{\phi WB}M_W\sqrt{M_Z^2 - M_W^2}}{M_Z^4} + \frac{2C_{\phi l}^{(3)} - C_{ll}}{2m_H^2} - \frac{4C_{\phi\Box} + C_{\phi D}}{4m_H^2} \right], \\
 \tilde{c}_{HZZ} &= -\frac{2}{(6\pi)\sqrt{2}G_f M_Z^4} \left[ C_{\phi\tilde{B}}(M_Z^2 - M_W^2) + C_{\phi\tilde{W}}M_W^2 + C_{\phi\tilde{W}B}M_W\sqrt{M_Z^2 - M_W^2} \right],
 \end{aligned}$$

For more details see Phys. Rev. D 107 (2023) 3, 034034.