

# Precision jet substructure studies for the Relativistic Heavy Ion Collider with the sPHENIX detector

In collaboration with Yang-Ting Chien, Daniel Reichelt and Steffen Schumann

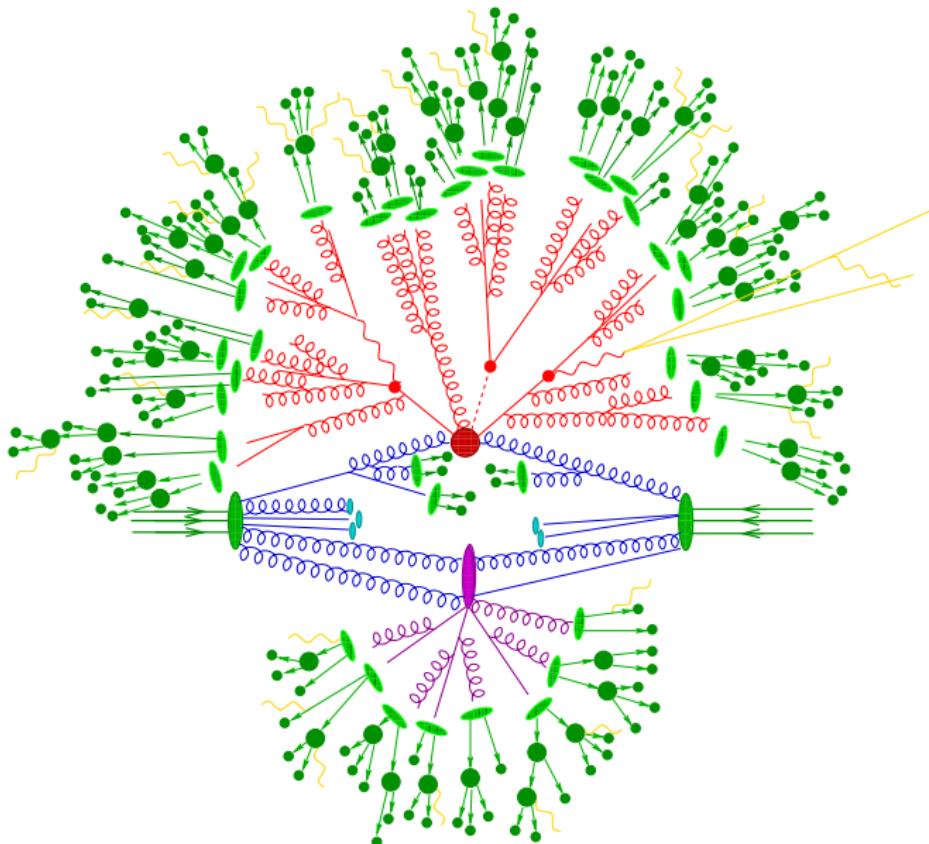
Oleh Fedkevych

Physics and Astronomy Department, Georgia State University, Atlanta, GA  
Center for Frontiers in Nuclear Science, Stony Brook University, Stony Brook, NY  
Jefferson Lab, Newport News, VA

October 16, 2023

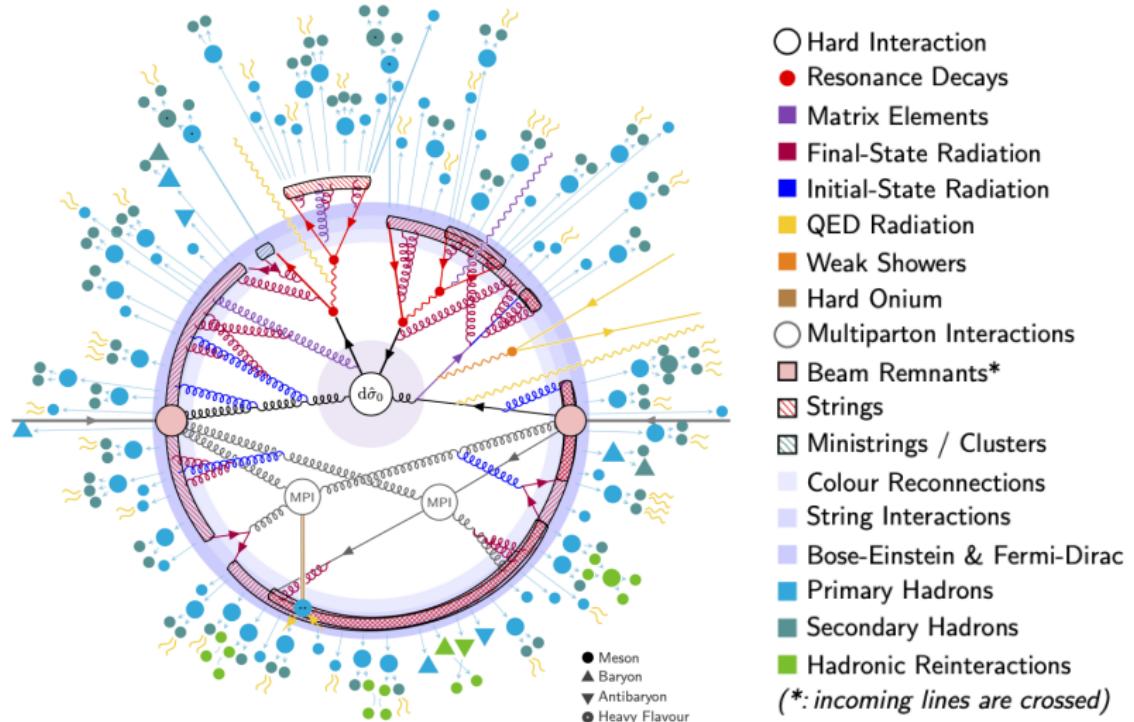


QCD is complicated!



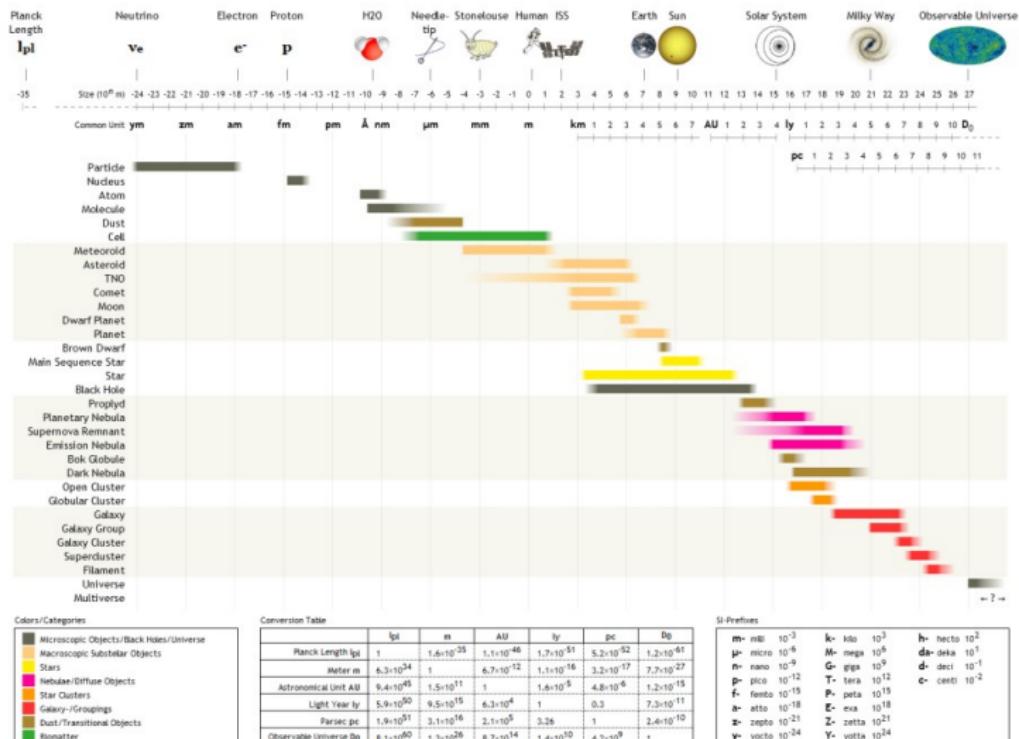
"Old event representation", credit: [arXiv:0811.4622](https://arxiv.org/abs/0811.4622).

# QCD is very complicated!



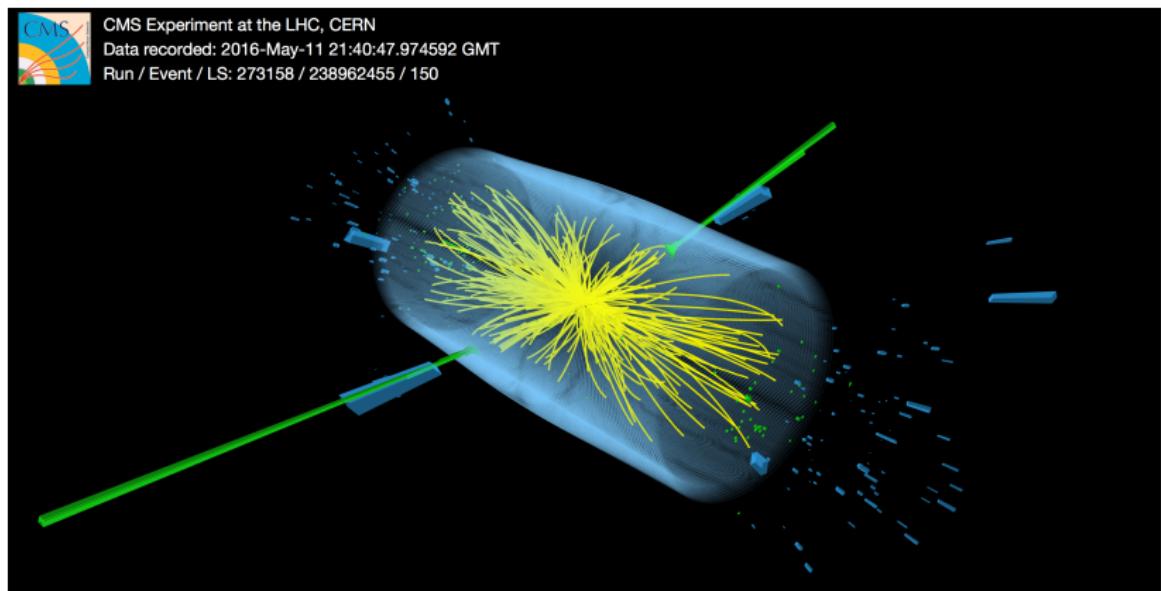
“New event representation”, credit: Peter Skunds.

# Physics is all about scales!



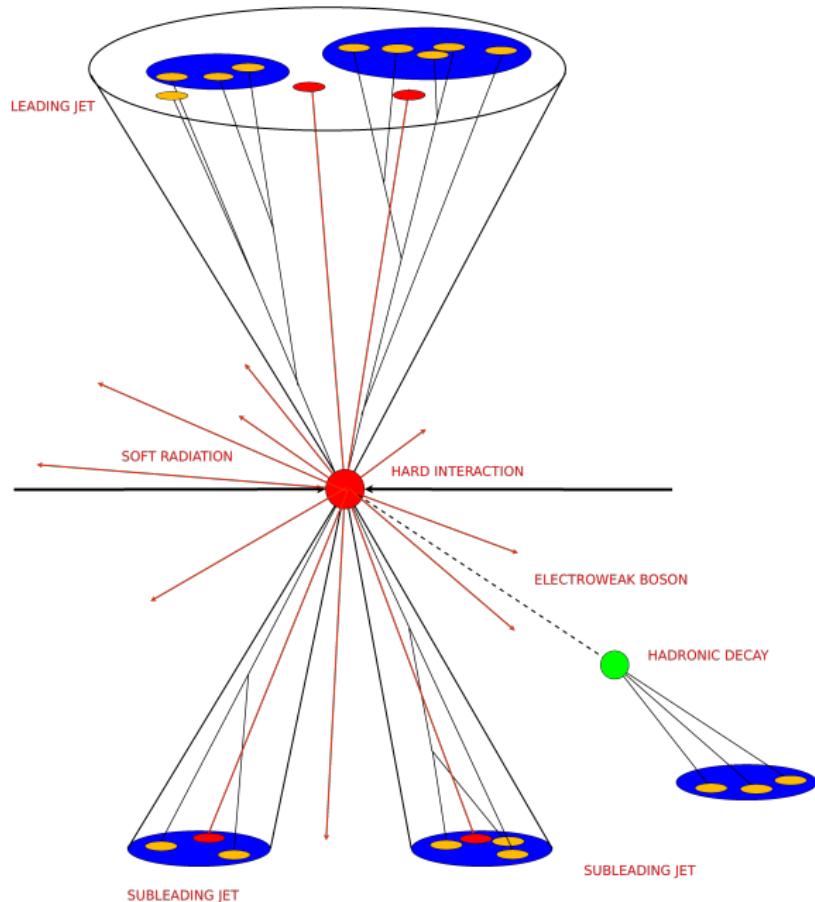
Typical scales of this Universe (credits: Wikipedia)

By studying hadrons inside jets we try to learn more about partons and their interactions

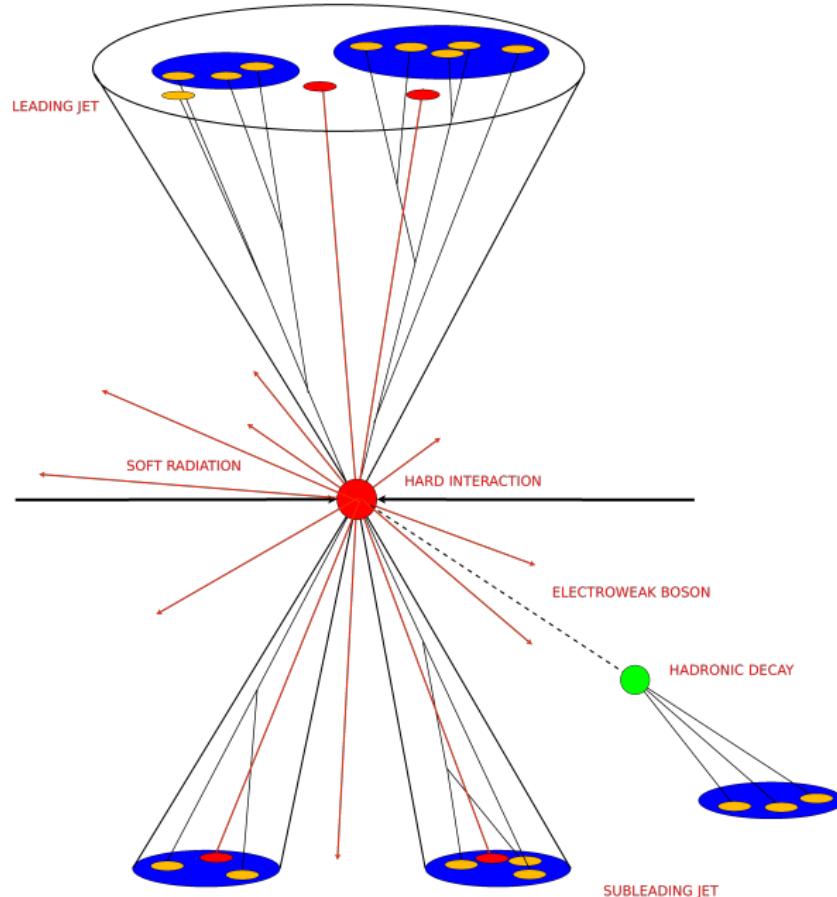


A di-jet event recorded by CMS collaboration (credits: CERN)

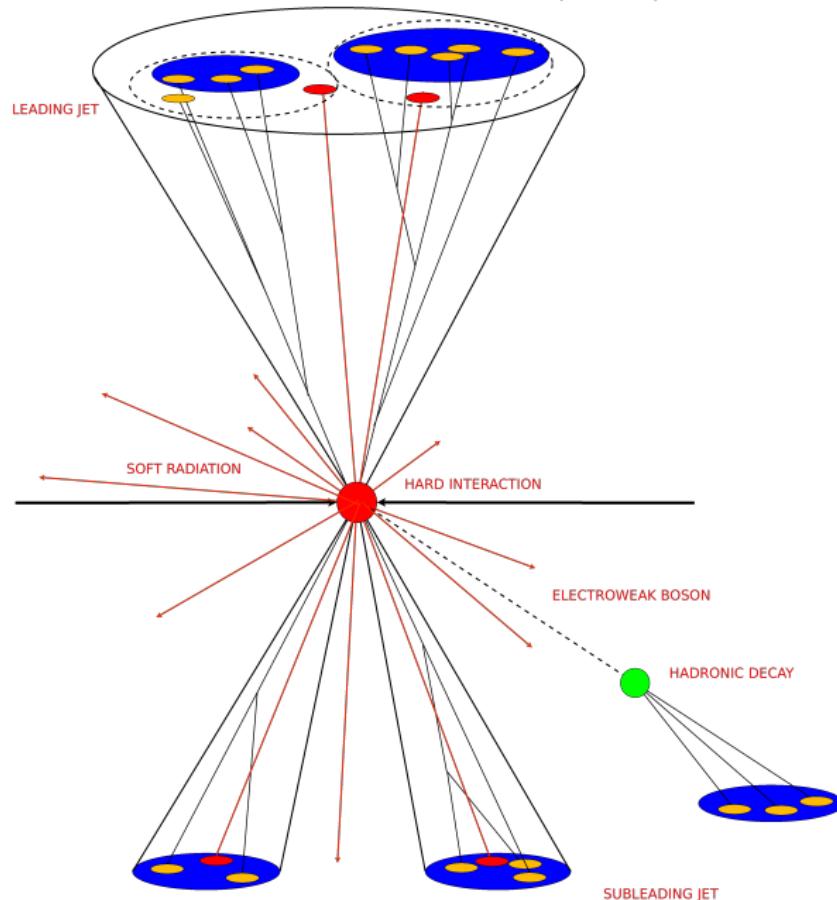
# Looking inside jets



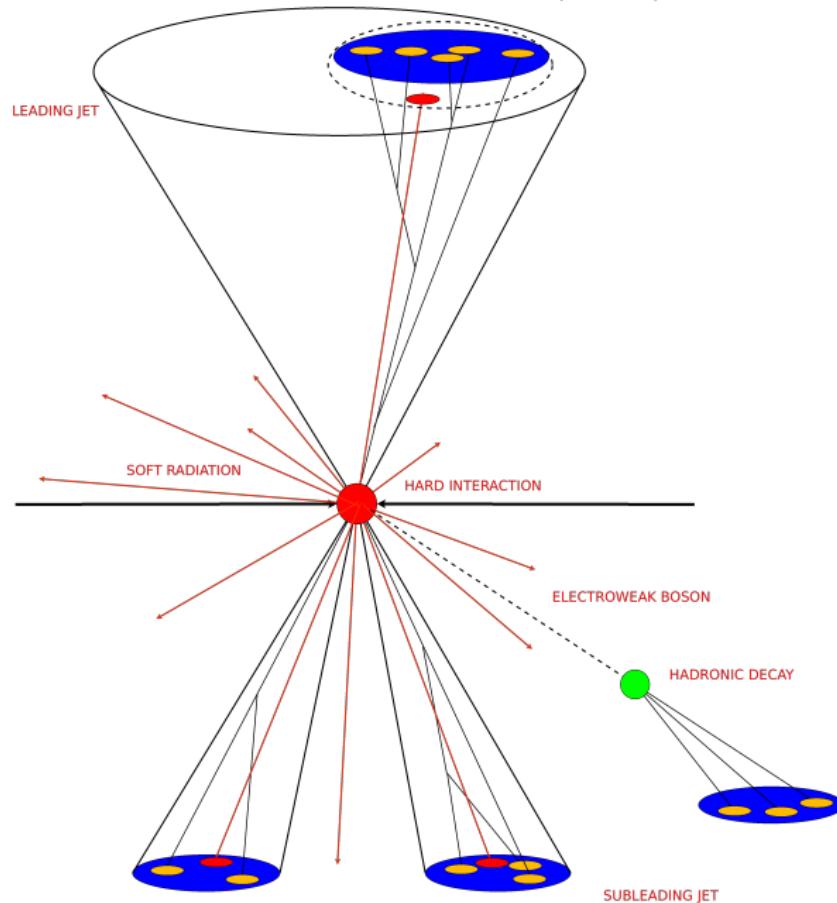
$$\text{SoftDrop groomer: } \frac{\min(p_{ti}, p_{tj})}{p_{ti} + p_{tj}} > z_{\text{cut}} \left( \frac{\Delta R_{ij}}{R} \right)^\beta$$



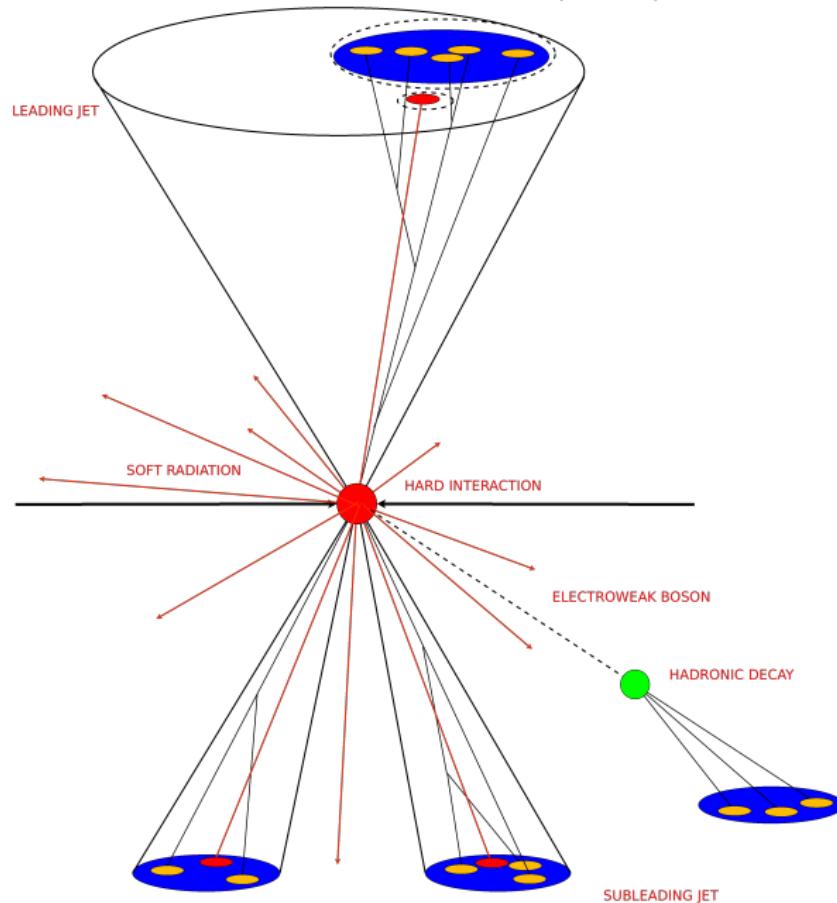
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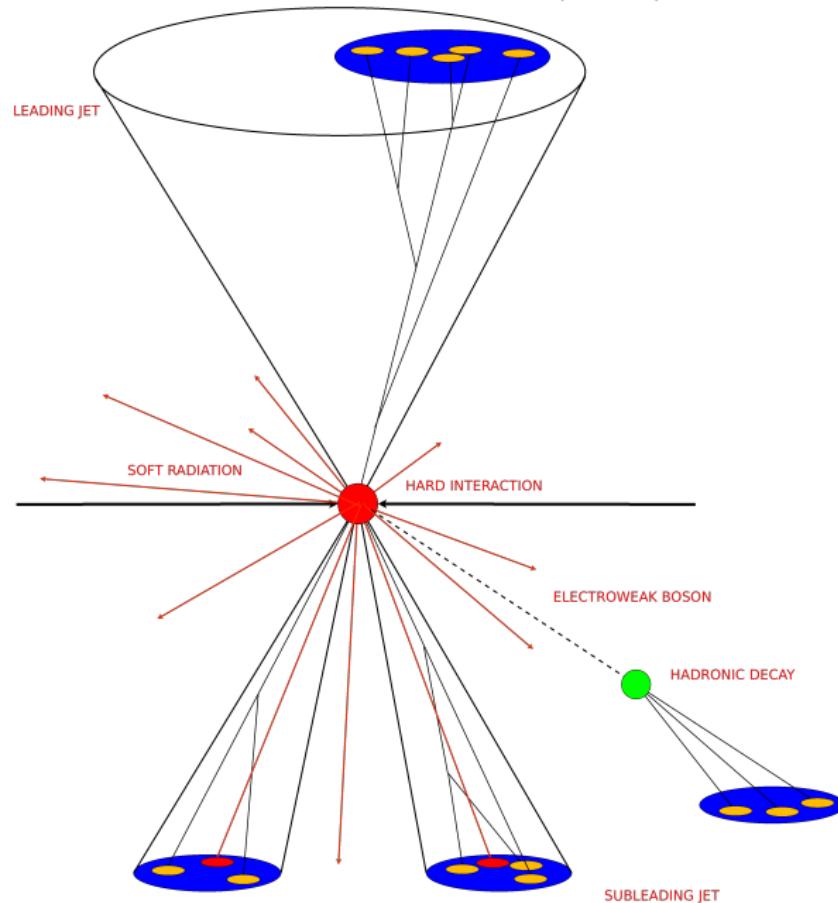
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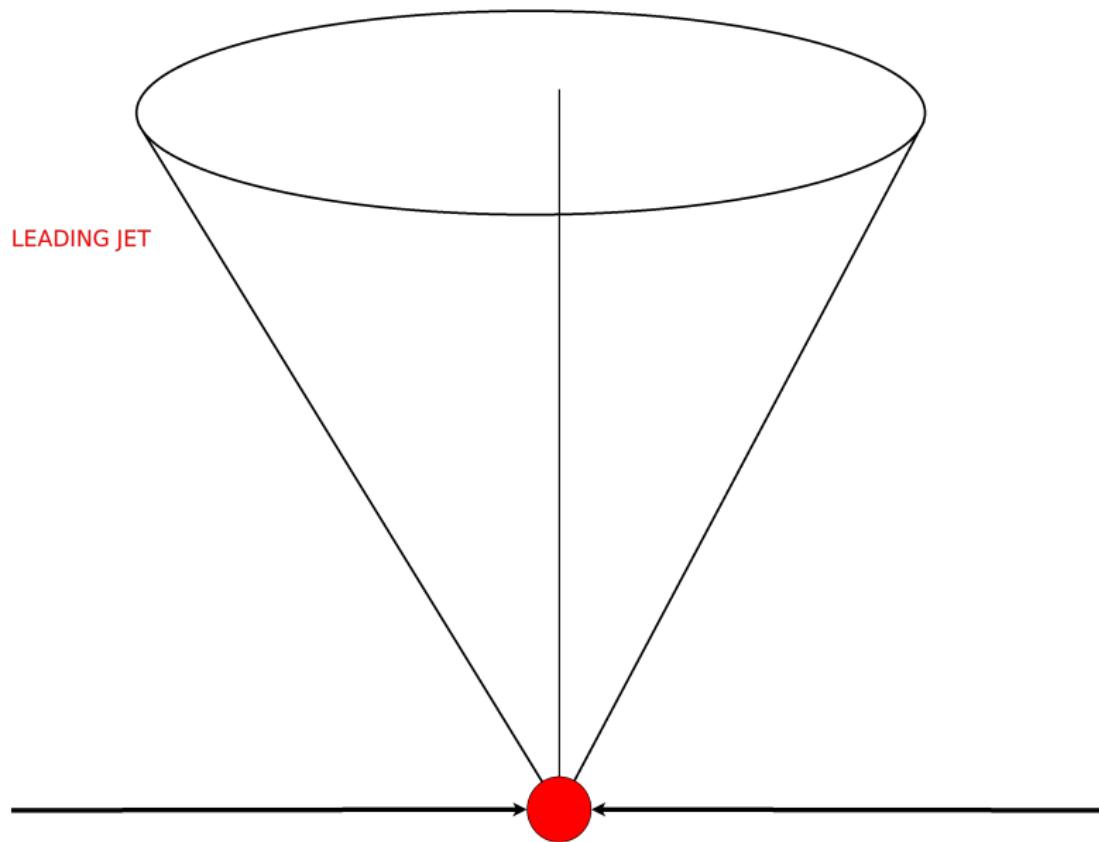
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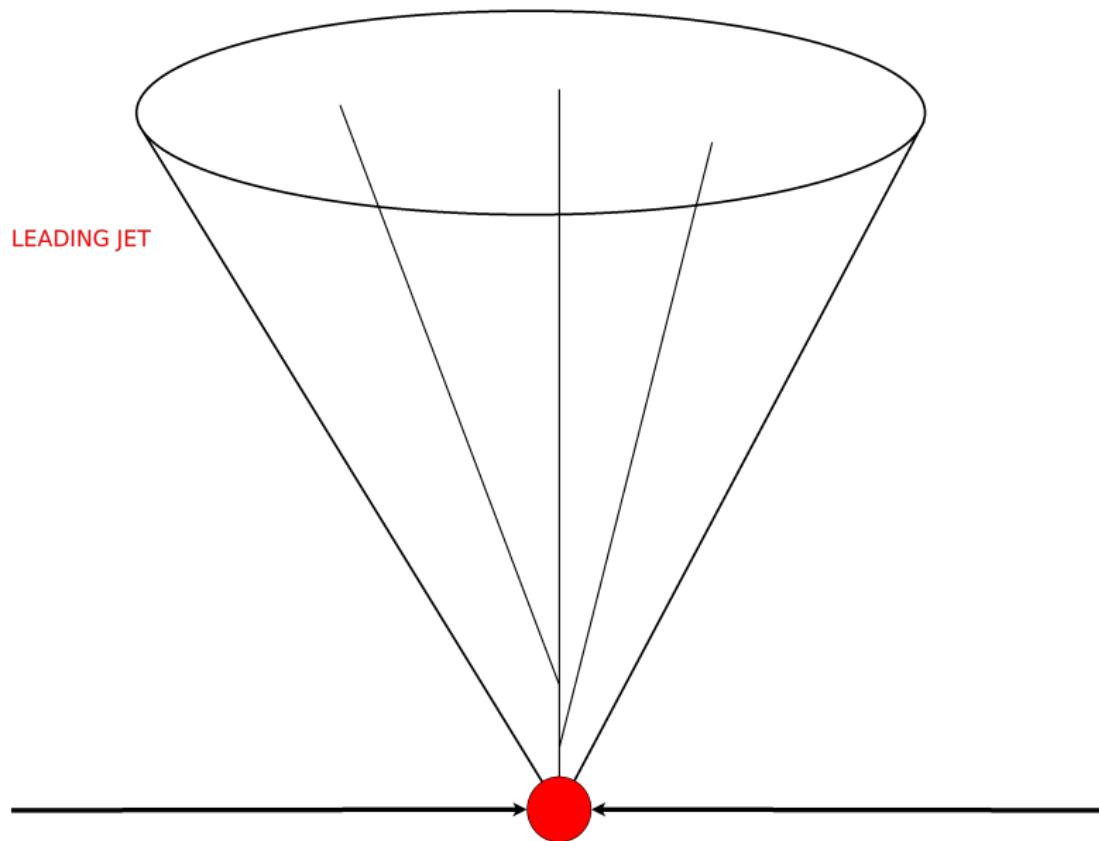
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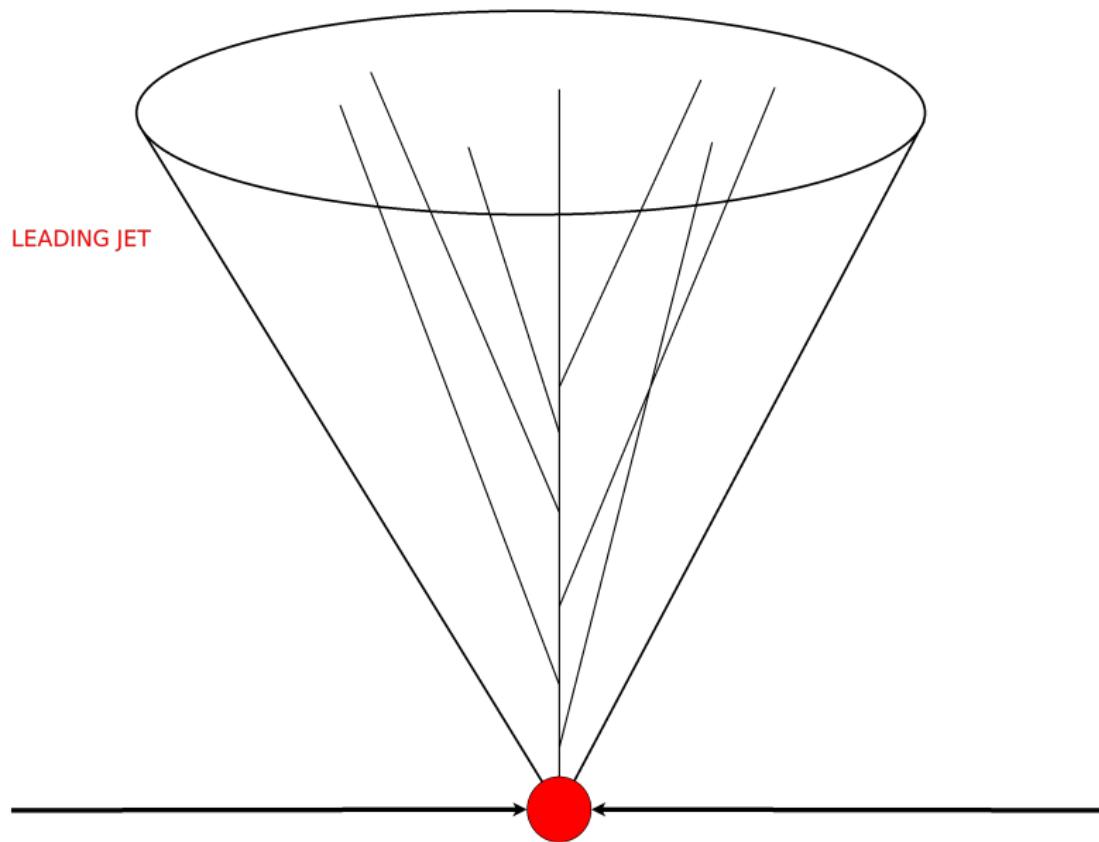
## Resummation vs. Monte Carlo



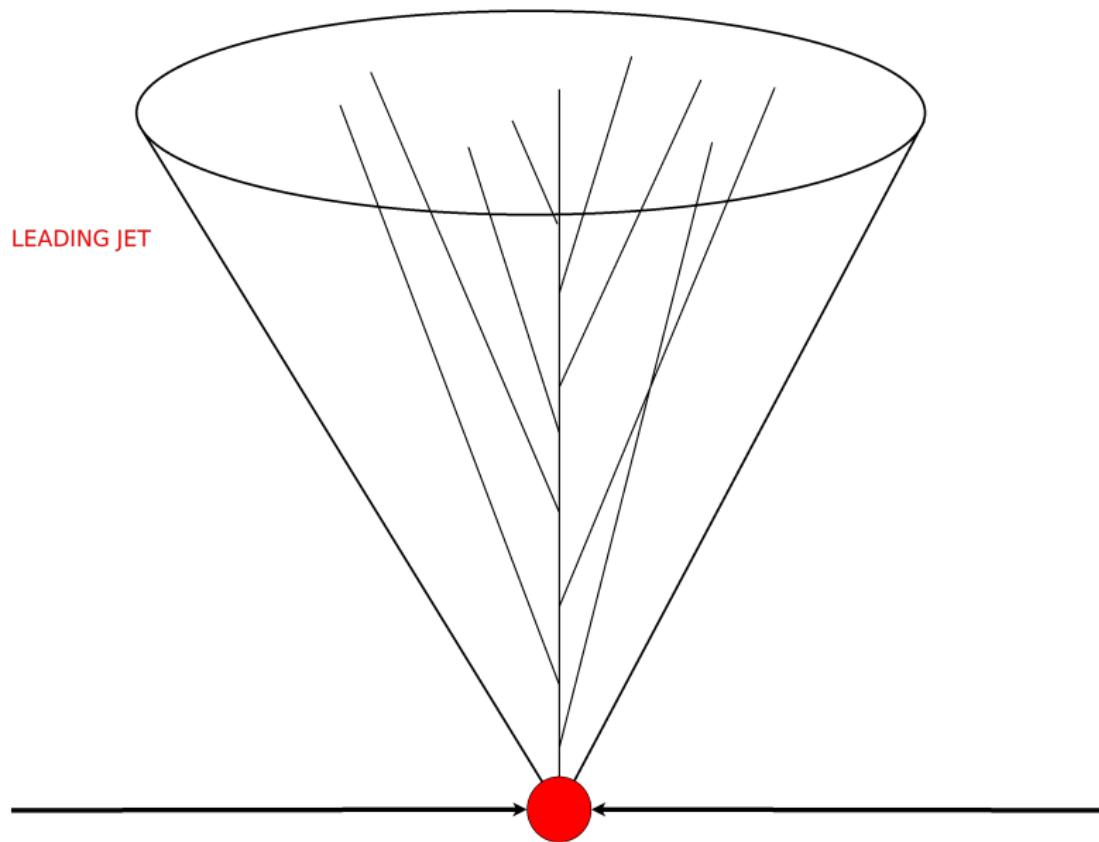
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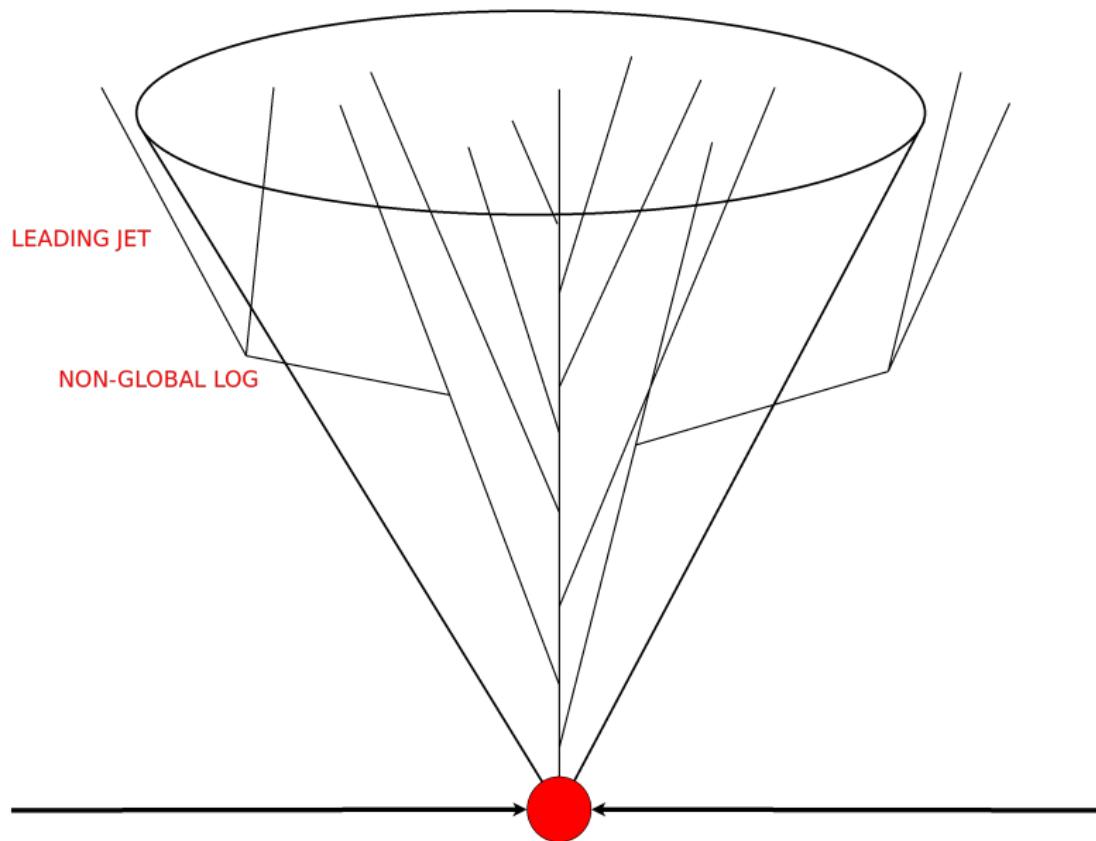
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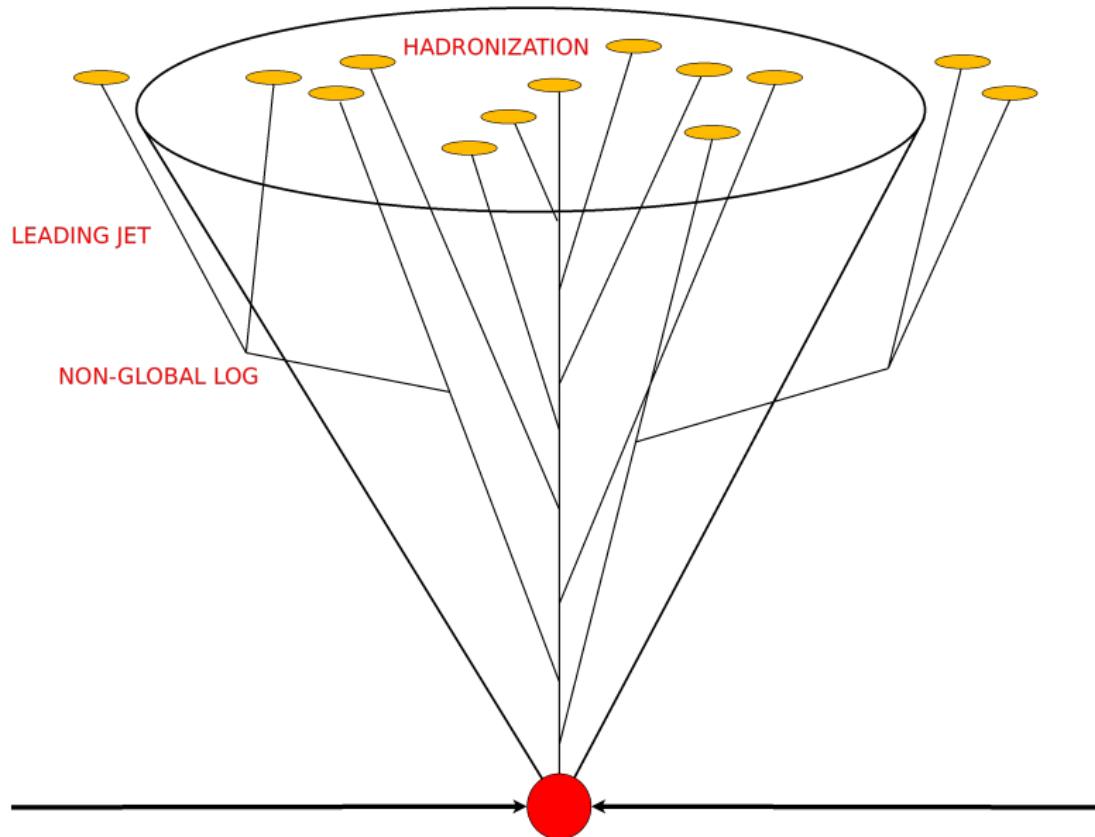
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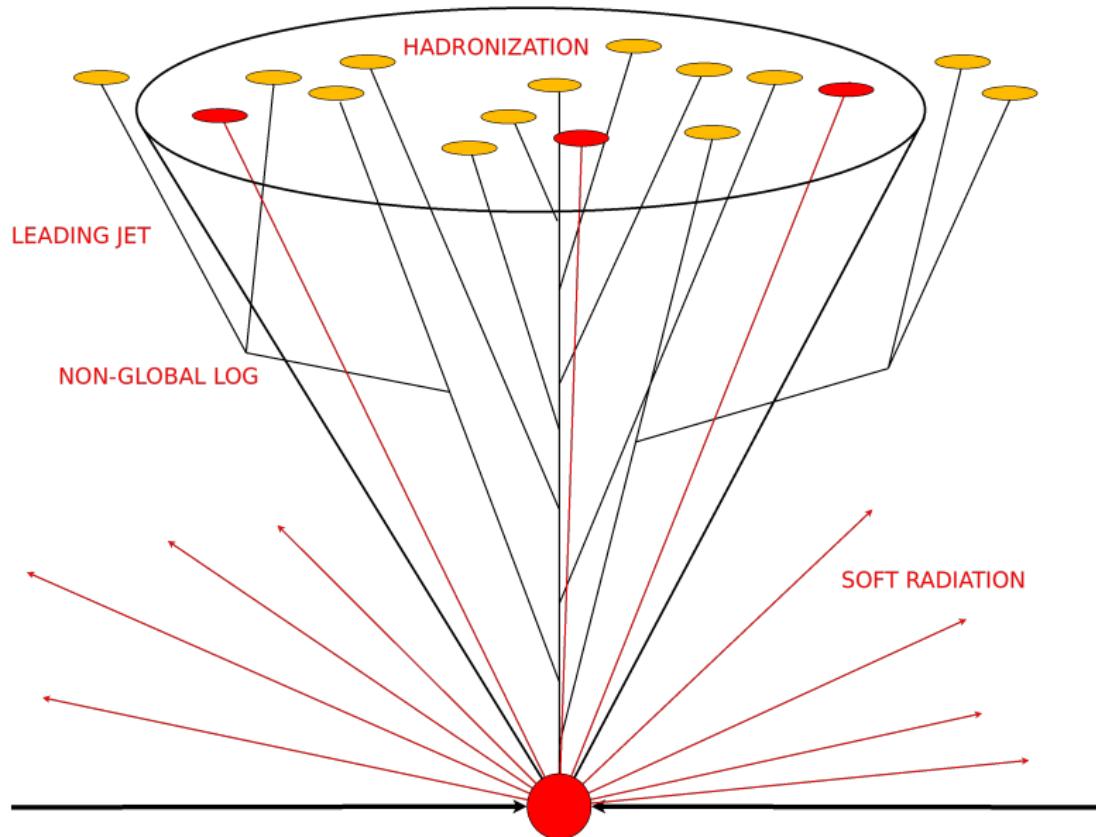
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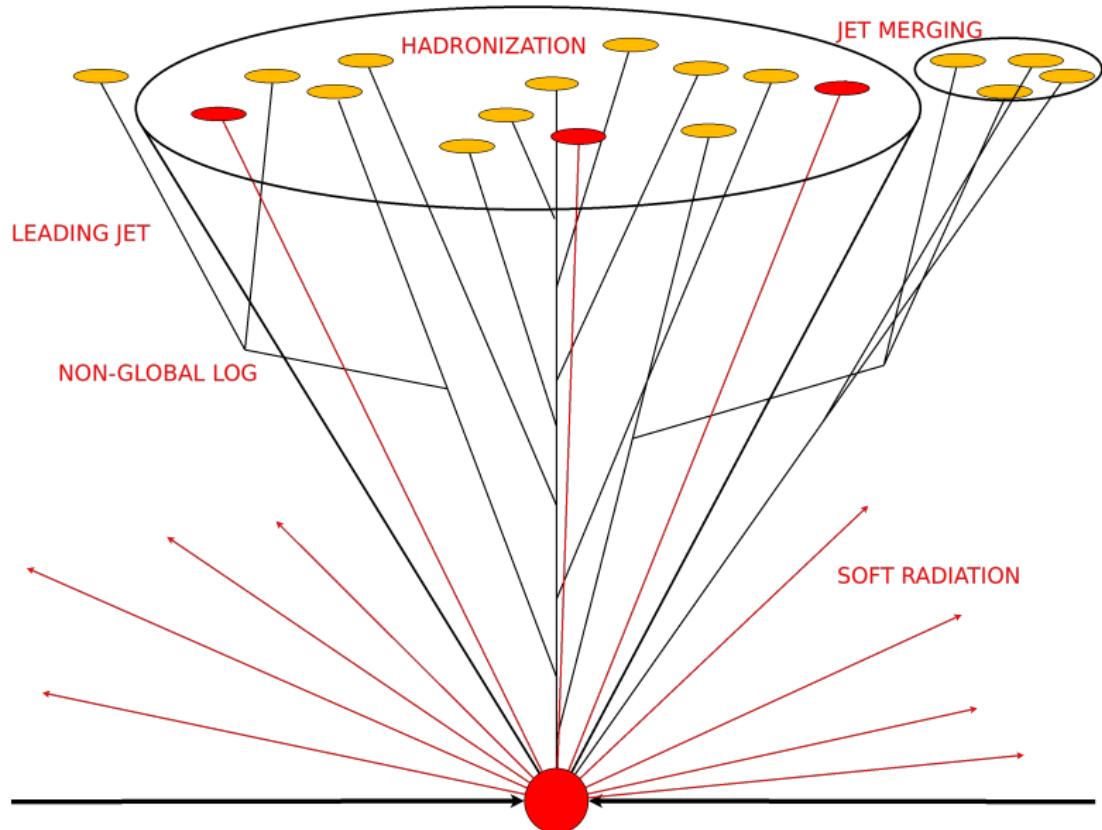
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# Resummation vs. Monte Carlo



# Resummation vs. Monte Carlo

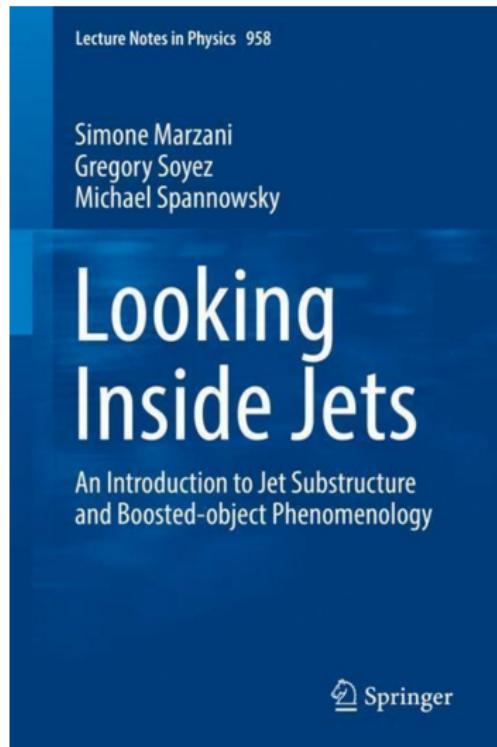


# Looking inside jets



Various observables exist:

- ▶ N-subjettiness,
- ▶ **Jet angularities**,
- ▶ Energy-correlation functions,
- ▶ Lund plane projection,
- ▶ **Angular decorrelation**,
- ▶ and many others!



More info can be found [here](#)

## Observable definition

The jet angularity is defined as

$$\lambda_\alpha = \sum_{i \in \text{jet}} \frac{p_{t,i}}{p_{t,\text{jet}}} \left( \frac{\Delta R_{ij}}{R} \right)^\alpha, \quad \alpha > 0$$

The angular decorrelation is defined as

$$\Delta\phi_{p_1, p_2} = \arccos \left( \frac{\vec{p}_1 \cdot \vec{p}_2}{|\vec{p}_1| |\vec{p}_2|} \right)$$

SoftDrop grooming condition:

$$\frac{\min(p_{ti}, p_{tj})}{p_{ti} + p_{tj}} > z_{\text{cut}} \left( \frac{\Delta R_{ij}}{R} \right)^\beta$$

- ▶ The LHC measurements LHA ( $\lambda_{1/2}$ ), Jet Width ( $\lambda_1$ ), Jet Thrust ( $\lambda_2$ ), see, for example, [2109.03340](#)
- ▶ The theoretical predictions, see, for example [2112.09545](#), [2104.06920](#) and [2005.12279](#)
- ▶ RHIC measurements?

## CAESAR formalism

The cumulative cross section for a generic observable  $v$  can be written as a sum over partonic channels  $\delta$ :

$$\Sigma_{\text{res}}(v) = \sum_{\delta} \Sigma_{\text{res}}^{\delta}(v), \text{ with}$$

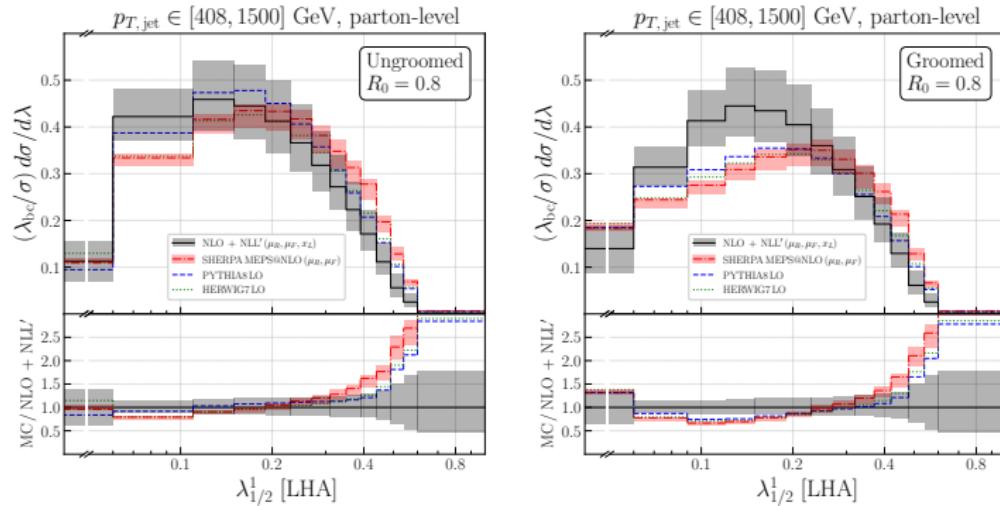
$$\Sigma_{\text{res}}^{\delta}(v) = \int d\mathcal{B}_{\delta} \frac{d\sigma_{\delta}}{d\mathcal{B}_{\delta}} \exp \left[ - \sum_{l \in \delta} R_l^{\mathcal{B}_{\delta}}(L) \right] \mathcal{P}^{\mathcal{B}_{\delta}}(L) \mathcal{S}^{\mathcal{B}_{\delta}}(L) \mathcal{F}^{\mathcal{B}_{\delta}}(L) \mathcal{H}^{\delta}(\mathcal{B}_{\delta}),$$

where  $L = -\ln(v)$ ,  $\frac{d\sigma_{\delta}}{d\mathcal{B}_{\delta}}$  is the differential Born cross section,  $R_l$  is the collinear radiator for the hard legs  $l$ ,  $\mathcal{P}$  is the ratio of PDFs,  $\mathcal{S}$  is the soft function,  $\mathcal{F}$  is the multiple emission function and  $\mathcal{H}$  stands for the corresponding kinematic cuts on the Born process.

## CAESAR resummation plugin to Sherpa

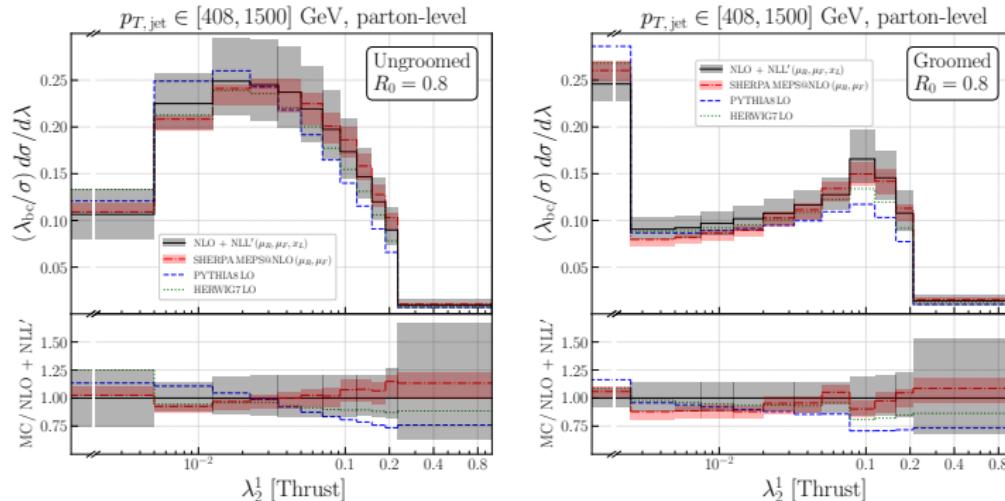
- ▶ Is using Comix matrix element generator as well as Sherpa machinery for phase-space integration and event generation.
- ▶ The NLO computations are performed using Catani-Seymour dipole subtraction.
- ▶ For the loop computations we use Recola and OpenLoops libraries.
- ▶ The resummed results are matched to the fixed order NLO computations using the multiplicative matching scheme.
- ▶ The final result is at NLO+NLL' accuracy level + corrections for the non-perturbative effects.

# Monte Carlo results: LHA



Comparison of hadron-level predictions for ungroomed and groomed jet-angularities in  $Zj$  production from Pythia and Herwig (both based on the LO  $Zj$  matrix element), and MEPS@LO as well as MEPS@NLO results from Sherpa. Here we use SoftDrop with  $\beta = 0$  and  $z_{cut} = 0.1$ .

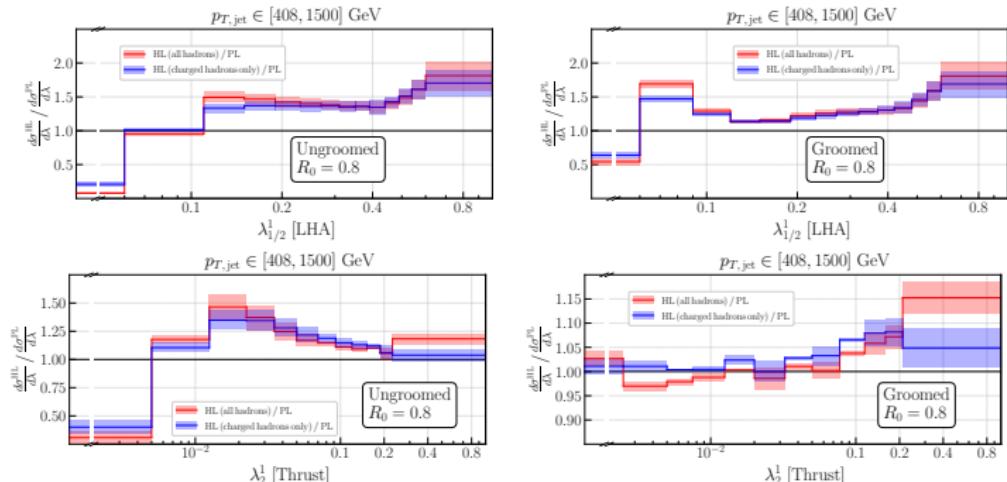
# Monte Carlo results: Jet Thrust



Comparison of hadron-level predictions for ungroomed and groomed jet-angularities in  $Zj$  production from Pythia and Herwig (both based on the LO  $Zj$  matrix element), and MEPS@LO as well as MEPS@NLO results from Sherpa. Here we use SoftDrop with  $\beta = 0$  and  $z_{cut} = 0.1$ .

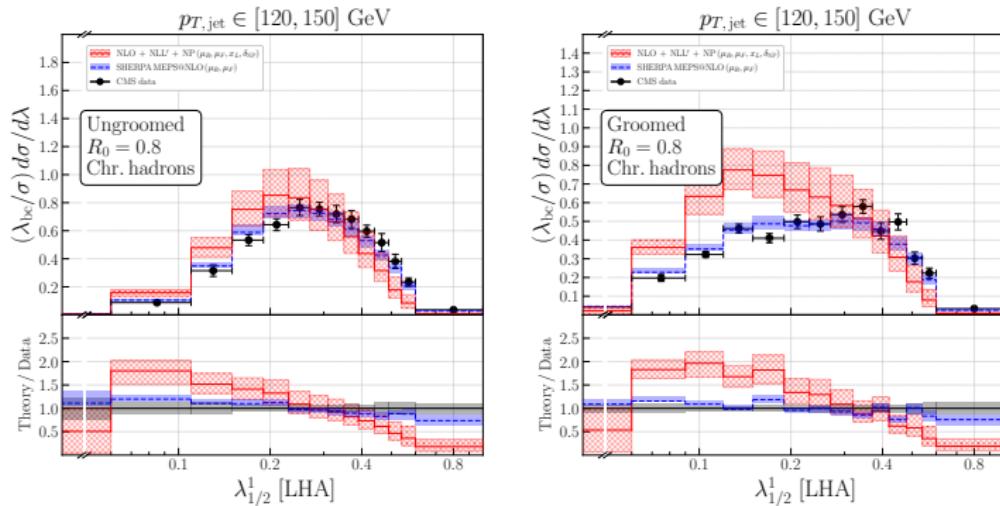
# Impact of NP-corrections

One can estimate the impact of non-perturbative corrections using Monte Carlo simulations



Hadron-to-parton-level ratios with associated uncertainties extracted from MC simulations (Pythia, Herwig and Sherpa). To some extent can be seen as a jet fragmentation function.

# Theory vs. CMS data

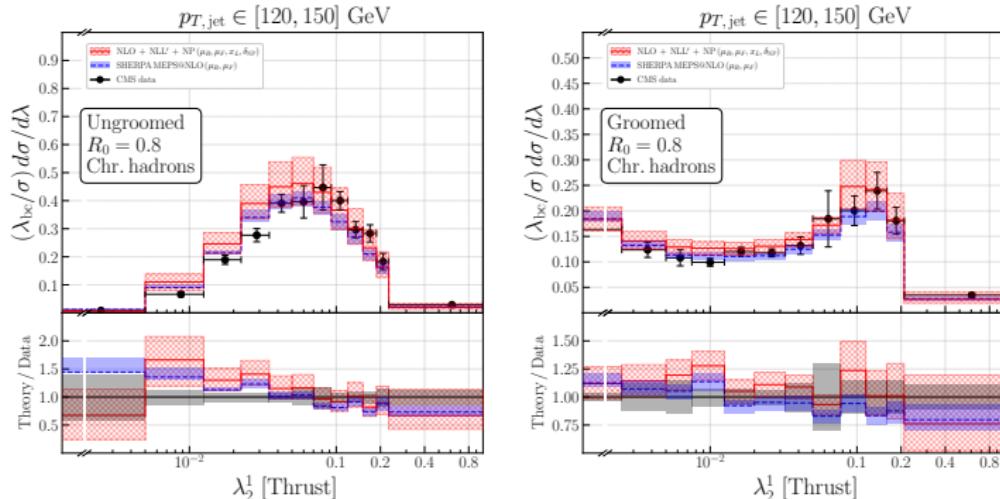


Comparison against recent CMS data for the LHA angularity,  
 $p_{T,\text{jet}} \in [120, 150] \text{ GeV}$ .

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Theory: [2112.09545](#), [2104.06920](#) (in collaboration with S. Caletti, S. Marzani, D. Reichelt, S. Schumann, G. Soyez, V. Theeuwes); CMS: [2109.03340](#)

# Theory vs. CMS data

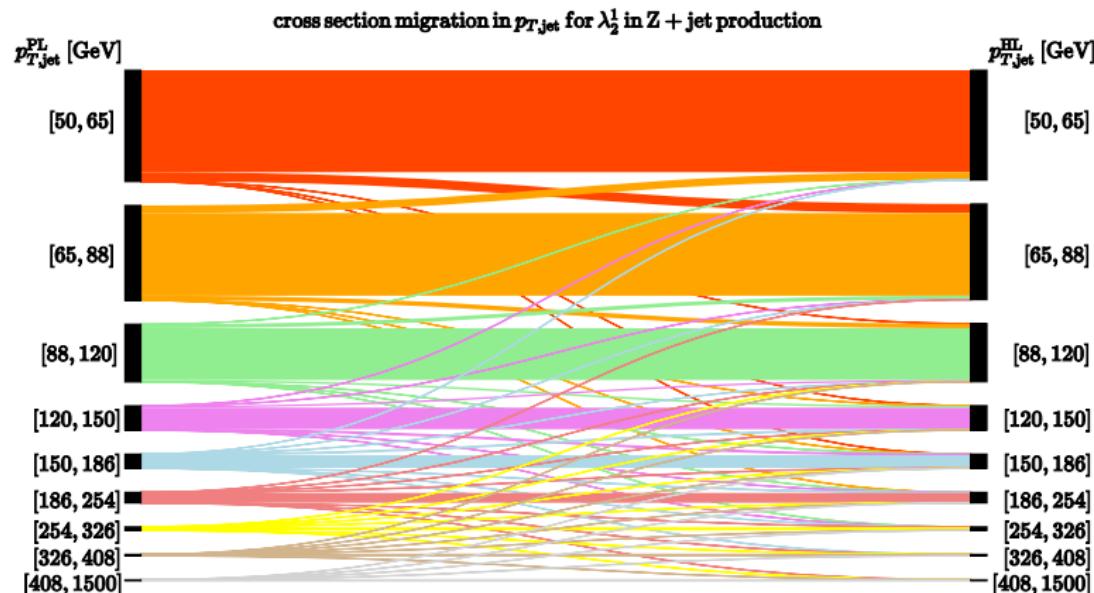


Comparison against recent CMS data for the Jet Thrust angularity,  
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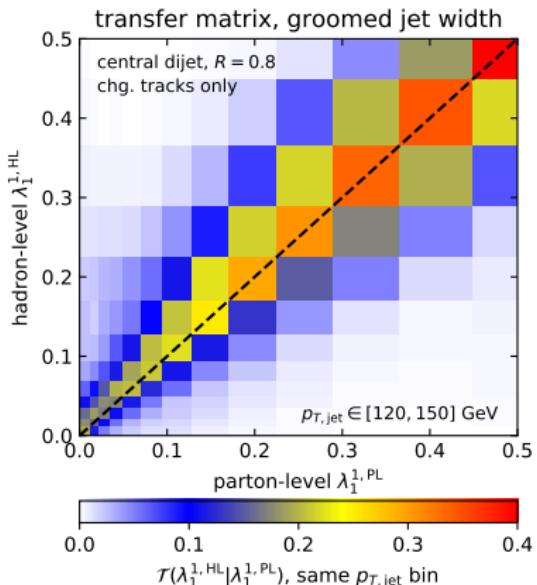
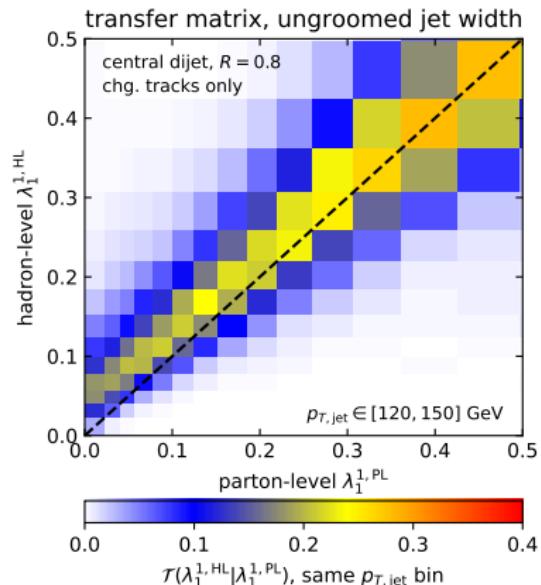
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# Migration between different $p_T$ -bins; credit S. Schumann



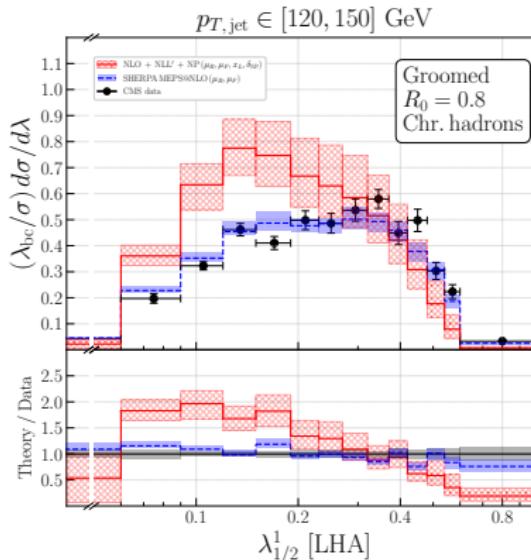
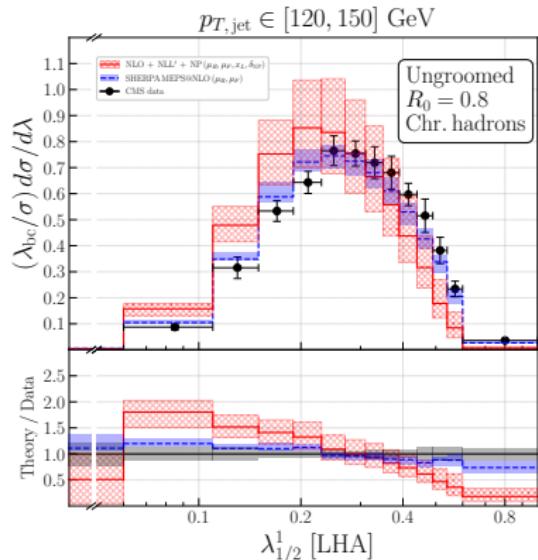
Hadronization can cause migration between different  $p_T$ -bins.

# Parton to hadron level transition; credit G. Soyez



Transfer matrix  $\mathcal{T}(\lambda_1^{1,\text{HL}}|\lambda_1^{1,\text{PL}})$  for the jet-width angularity for central dijet events with  $R = 0.8$  and  $p_{T,\text{jet}} \in [120, 150]$  GeV.

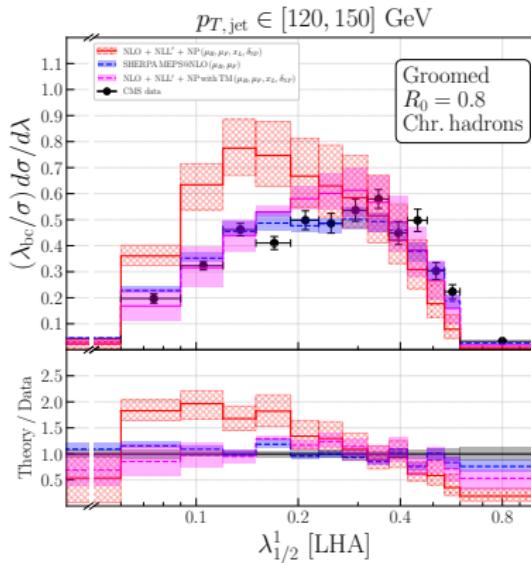
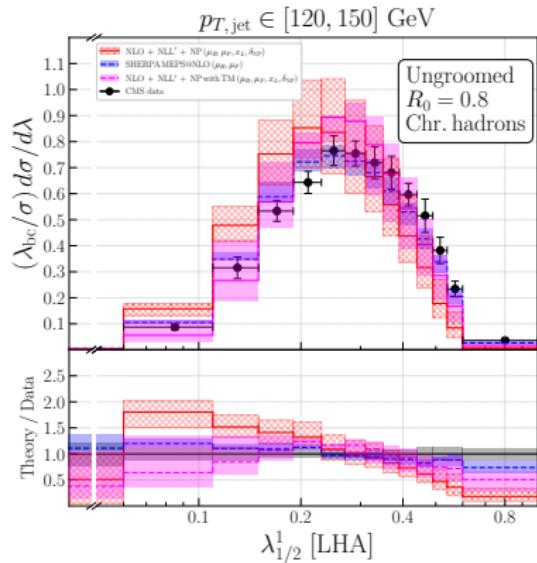
# Theory (including TM) vs. CMS data



Comparison against recent CMS data for the Jet Thrust angularity,  $p_{T,\text{jet}} \in [120, 150] \text{ GeV}$ . Magenta band correspond to transfer matrix approach.

Theory: [2112.09545](#), [2104.06920](#) (in collaboration with S. Caletti, S. Marzani, D. Reichelt, S. Schumann, G. Soyez, V. Theeuwes); CMS: [2109.03340](#)

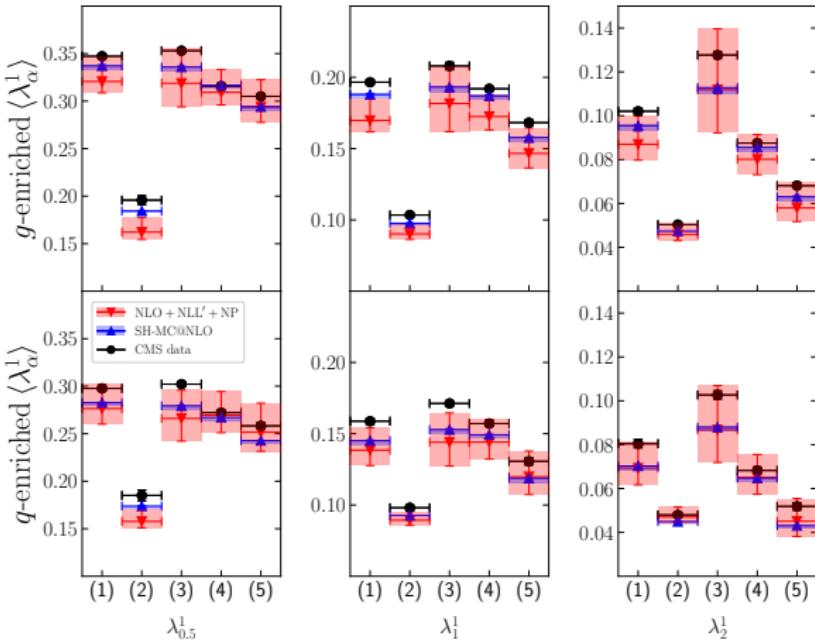
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Comparison against recent CMS data for the Jet Thrust angularity,  $p_{T,\text{jet}} \in [120, 150] \text{ GeV}$ . Magenta band correspond to transfer matrix approach.

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# Comparison against CMS data



configuration	type of jet	$p_T$ _jet [GeV]	$g$ -enriched	$q$ -enriched
(1)	ungroomed $R = 0.4$	[120,150]	dijet central	$Z + \text{jet}$
(2)	ungroomed $R = 0.4$	[1000,4000]	dijet central	dijet forward
(3)	ungroomed $R = 0.8$	[120,150]	dijet central	$Z + \text{jet}$
(4)	ungroomed $R = 0.4$ (tracks only)	[120,150]	dijet central	$Z + \text{jet}$
(5)	SoftDrop ( $\beta = 0$ , $z_{\text{cut}} = 0.1$ ) $R = 0.4$	[120,150]	dijet central	$Z + \text{jet}$

# What about RHIC?

And Now for Something Completely Different

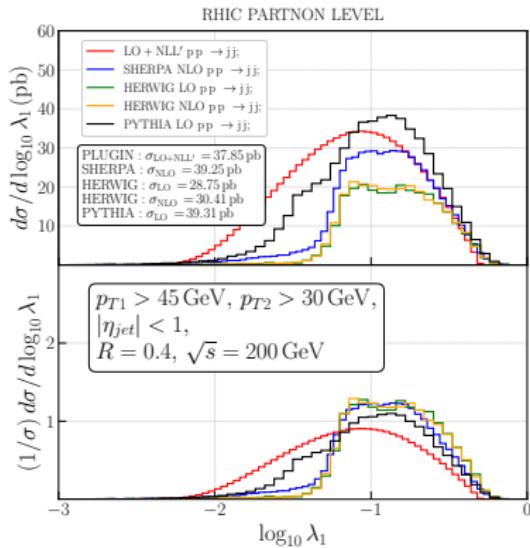
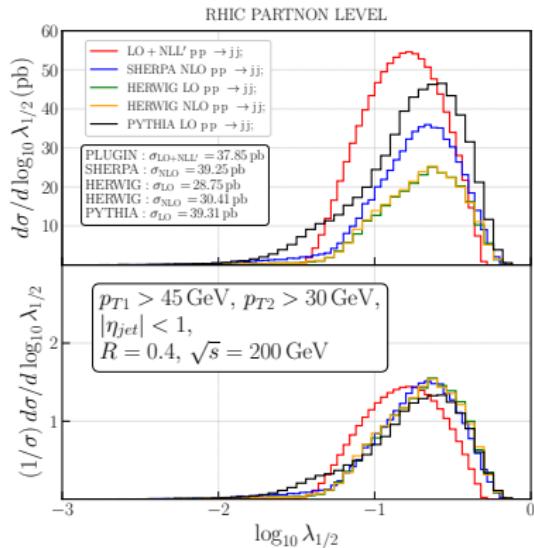
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*Monty Python's Flying Circus*

## At RHIC

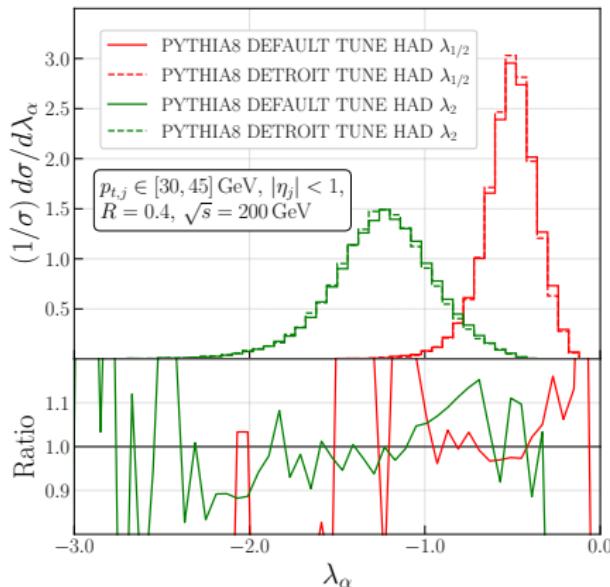
- ▶ MPIs are less relevant ( $\sqrt{S}$  is small comparing to the LHC)
- ▶ Hadronization is more important (small  $\sqrt{S}$  and small jet  $p_T$ )
- ▶ Completely different energy regime
- ▶ One can study jets in pp and AA
- ▶ Only few jet substructure studies (STAR) are available  
[1705.01974](#)
- ▶ The sPHENIX data can be used to produce new tunes, to test currently available precise predictions, to get better understanding of hadronization

$$\lambda_\alpha = \sum_i z_i \left( \frac{\Delta_{i,jet}}{R} \right)^\alpha \text{ at RHIC energy, Res. vs. MC}$$



Comparison between resummed predictions matched to fixed order results (SHERPA LO + NLL' accuracy level) against MC simulations (preliminary)

$$\lambda_\alpha = \sum_i z_i \left( \frac{\Delta_{i,jet}}{R} \right)^\alpha \text{ at RHIC energy, Detroit PYTHIA tune}$$

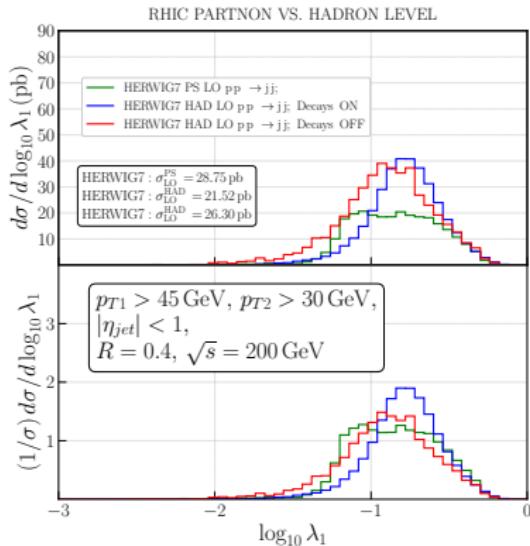
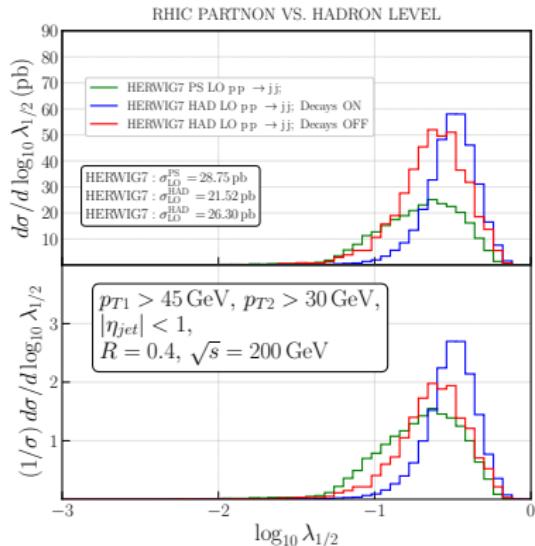


(preliminary)

Shall one make new tunes?

- ▶ There is a Detroit PYTHIA tune [2110.09447](#) for RHIC, but it mostly affect MPI
- ▶ However, MPI are almost absent at RHIC energies
- ▶ Main contribution comes from hadronization

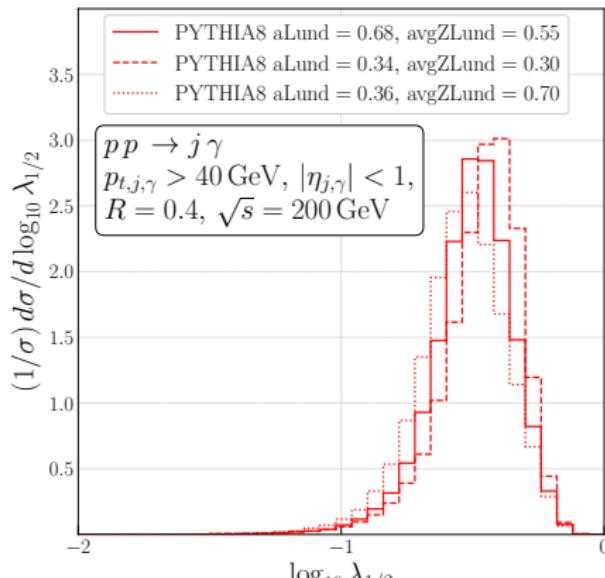
$$\lambda_\alpha = \sum_i z_i \left( \frac{\Delta_{i,jet}}{R} \right)^\alpha \text{ at RHIC energy, hadronisation and decays}$$



Angularities at RHIC energies are strongly affected by hadronization and decay of produced hadrons in case of jets containing a single hadron, see also Lee *et al* in [1901.09095](#). (preliminary)

# Hadronization and Lund string model

## New tunes?



(preliminary)

- ▶ There is a Detroit PYTHIA tune [2110.09447](#) designed to describe RHIC data, but it mostly affect MPI
- ▶ However, MPI are almost absent at RHIC energies  $\sqrt{S}$  is too small.
- ▶ Lund symmetric fragmentation function

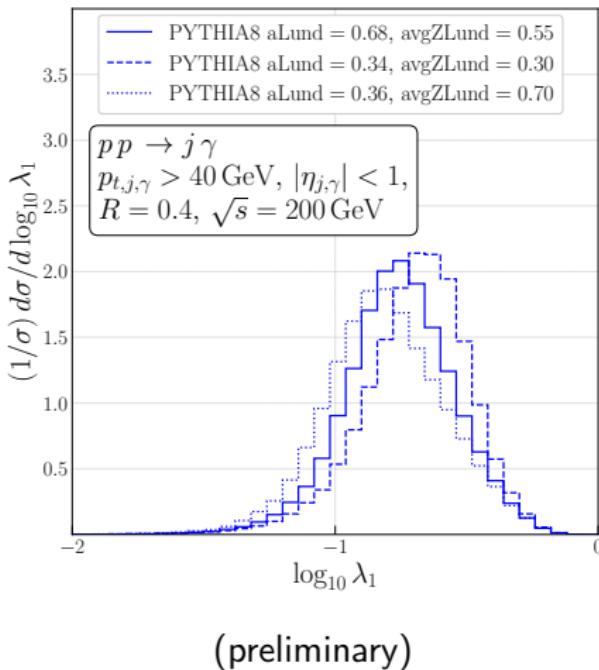
$$f(z) \sim \frac{(1-z)^a}{z} \exp(-bm^2/z)$$

- ▶ Hadron formation time

$$\langle \tau^2 \rangle = \frac{1+a}{b\kappa^2} \approx 2 \text{ fm}$$

# Hadronization and Lund string model

## New tunes?



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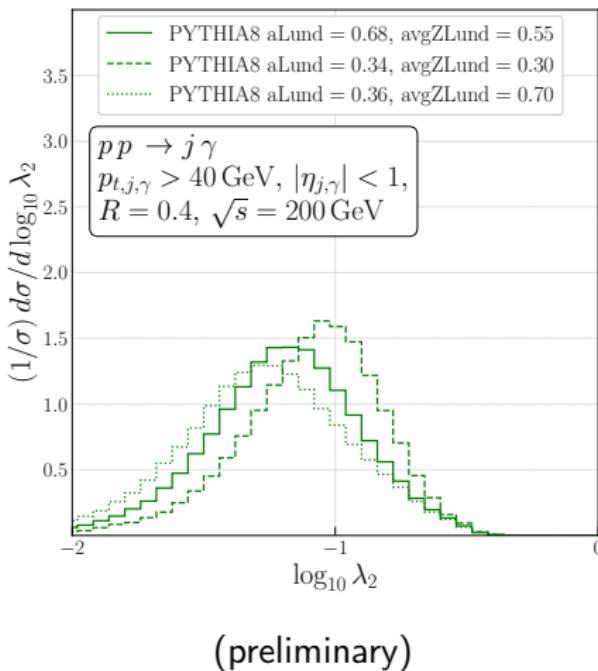
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# Hadronization and Lund string model

## New tunes?



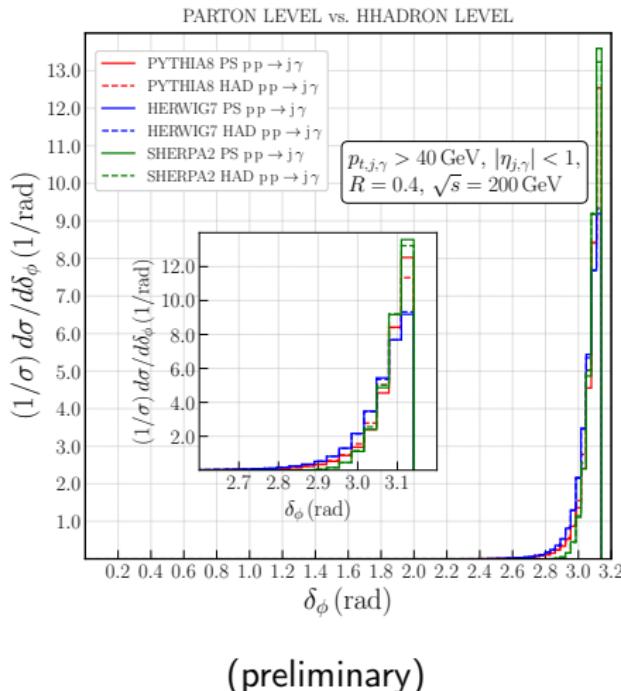
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# Is $\delta\phi$ affected by NP-corrections?



## Angular decorrelation

- ▶  $\Delta\phi$  is an azimuthal angle between two most energetic jets (or between a leading jet and a leading photon)
- ▶ Unlike  $\lambda_\alpha$  is more sensitive to radiation pattern
- ▶ Which PS-model would work better?

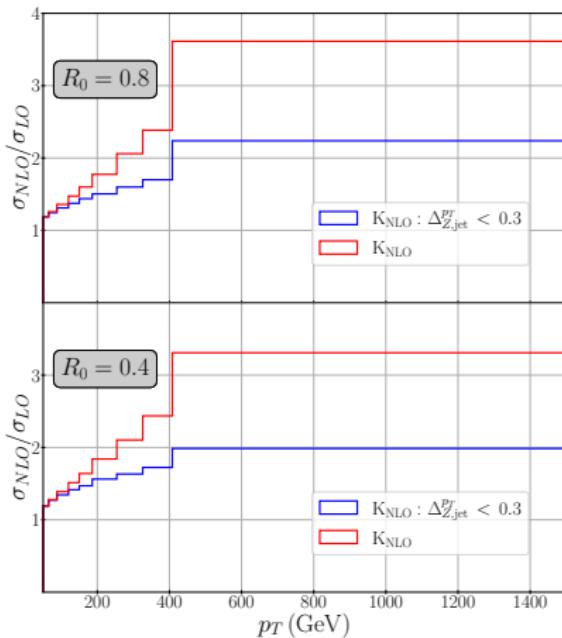
## Summary and next steps:

### Current results

- ▶ Resummed predictions for both groomed and ungroomed angularities  $\lambda_\alpha$  ( $\alpha \in [1/2, 1, 2]$ ) at LO + NLL' are ready, the NLO + NLL' requires some more (a way more) CPU time
- ▶ We found that angularities  $\lambda_\alpha$  at RHIC energies can be used to study hadronization and potentially to produce new MC tunes
- ▶ On the other hand, angular decorrelation  $\delta_\phi$ , can be used to test various parton shower models
- ▶  $\delta\phi$  simulated with JEWEL shows strong dependence on the medium temperature
- ▶ Correct the resummed predictions for non-perturbative effects using corresponding parton-to-hadron transition matrices
- ▶ What about 2D observables, say primary Lund Plane?
- ▶ The sPHENIX data is needed!

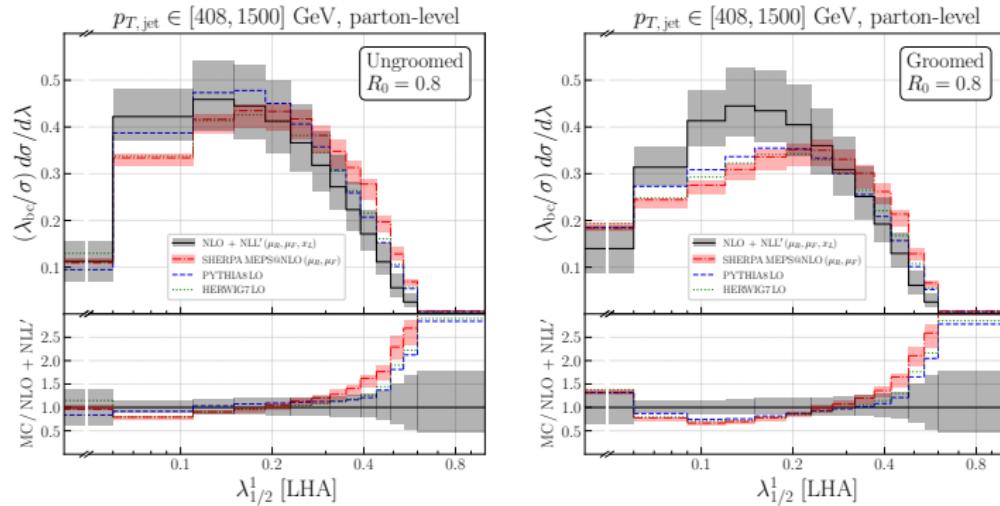
Thank you for your attention!

# Monte Carlo result: K-factor



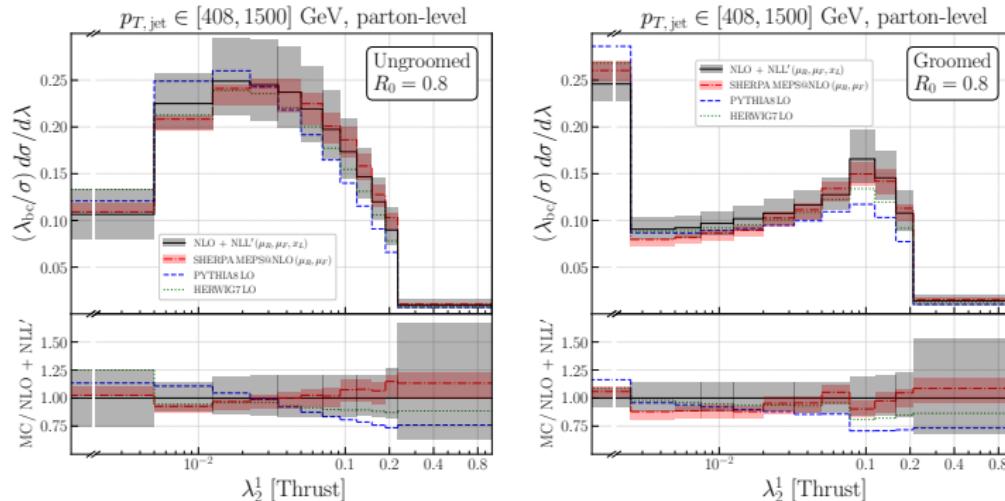
The NLO K-factor as a function of the  $p_{TJ}$  with and without  $\Delta_{Z,\text{jet}}^{p_T} = |(p_{T,\text{jet}} - p_{T,\mu^+\mu^-})/(p_{T,\text{jet}} + p_{T,\mu^+\mu^-})| < 0.3$  cut.

# Monte Carlo results: LHA



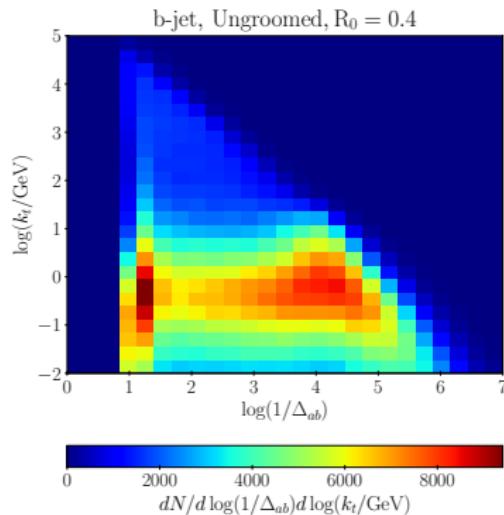
Comparison of hadron-level predictions for ungroomed and groomed jet-angularities in  $Zj$  production from Pythia and Herwig (both based on the LO  $Zj$  matrix element), and MEPS@LO as well as MEPS@NLO results from Sherpa. Here we use SoftDrop with  $\beta = 0$  and  $z_{cut} = 0.1$ .

# Monte Carlo results: Jet Thrust



Comparison of hadron-level predictions for ungroomed and groomed jet-angularities in  $Zj$  production from Pythia and Herwig (both based on the LO  $Zj$  matrix element), and MEPS@LO as well as MEPS@NLO results from Sherpa. Here we use SoftDrop with  $\beta = 0$  and  $z_{cut} = 0.1$ .

# Lund plane projection



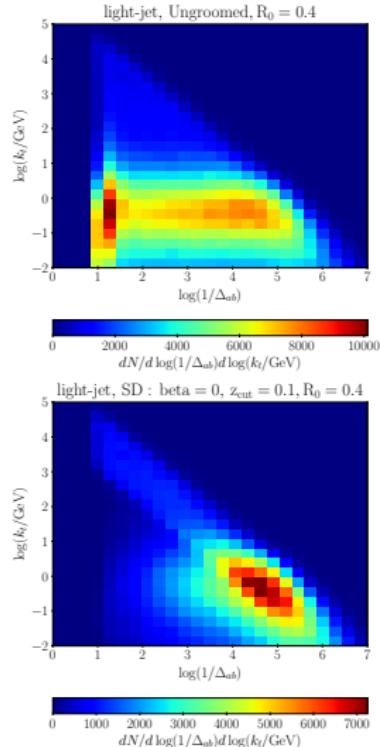
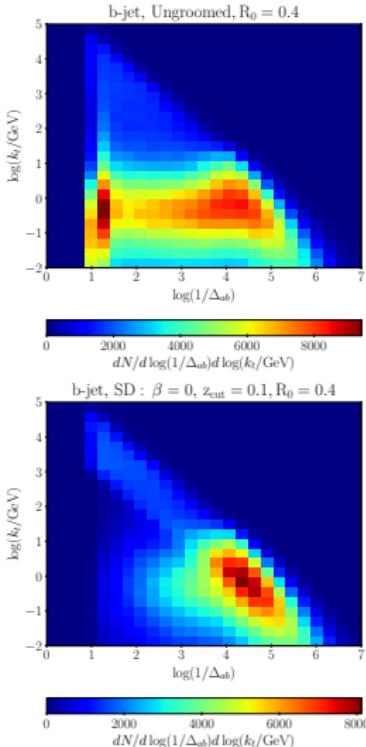
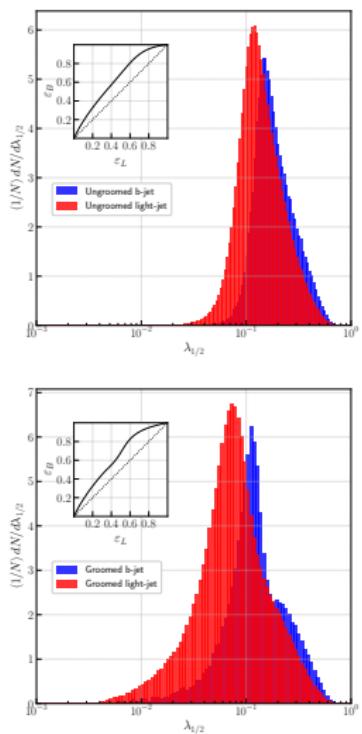
To build a Lund plane:

- ▶ Recluster your jet using CA algorithm
- ▶ Then compute:

$$\begin{aligned}\Delta_{ab} &\equiv \sqrt{(y_a - y_b)^2 + (\phi_a - \phi_b)^2}, \\ k_t &\equiv p_{Tb} \Delta_{ab}.\end{aligned}$$

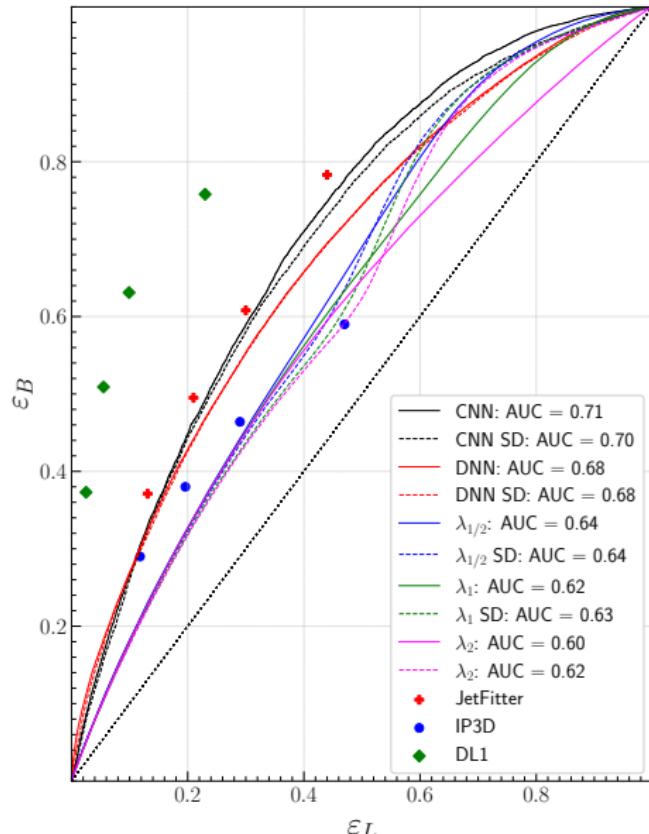
- ▶ Discard softest branch and repeat.

# Lund plane projection



Observables we consider as an input for our DNN / CNN. Note that jet flavour is defined in an experimental way here.

# Performance of our CNN / DNN



The ROC curves obtained for one-dimensional angularity distributions, multivariable DNN classification and Lund plane CNN classification. The single points correspond to ATLAS SV1, IP3D and DL1  $b$ -tagging performance from CERN-EP-2019-132.