GENERALIZED PARTON DISTRIBUTIONS THROUGH UNIVERSAL MOMENT PARAMETERIZATION (GUMP): THE GLUONIC SECTOR WITH DEEPLY VIRTUAL  $J/\psi$  PRODUCTION AT NLO

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PAPER IN PREPARATION



## OUTLINE

- GPD Review
- GUMP Program
  - Conformal moment parameterization
- Review of Previous Global Analysis: u and d quarks
  - Simplified GPD moment ansatz
  - Experimental and lattice input
- Gluons with  $J/\psi$ 
  - NRQCD treatment
  - NLO corrections
  - Hybrid collinear-NRQCD scheme
- Gluon GPD fits
  - Comparison to data
  - Small-x vs Moderate-x
- Moving Forward
- Conclusions

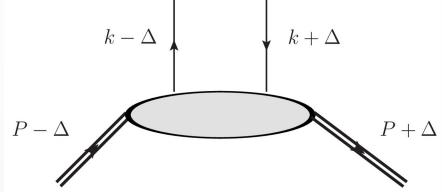
#### GPDS

$$f(x) \to F(x,\xi,t)$$

 $x \sim \text{parton momentum fraction}, \ \xi \sim \text{longitudinal momentum transfer},$ 

 $t = \Delta^2 \sim \text{momentum transfer squared}$ 

 GPDs generalize the well known PDFs to encode full 3 dimensional information on the quarks and gluons within hadrons



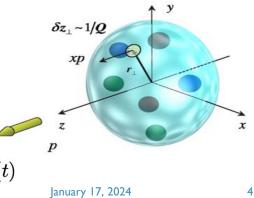
## GPDS

- Polarization of the hadron and its parton constituents connects GPDs to the distribution of angular momentum within hadrons (X. Ji 1997)
  - I sum rule  $J_i = rac{1}{2} \int\limits_0^1 \mathrm{d}x \, x \left[ H_i(x,\xi) + E_i(x,\xi) 
    ight]$
- Related via a Fourier transform to the impact parameter distribution of partons (M. Burkardt 2003)

$$ho(x,r_{\perp}) = \int rac{\mathrm{d}^2 \Delta_{\perp}}{(2\pi)^2} e^{-i\Delta_{\perp}\cdot r_{\perp}} H(x,0,\Delta_{\perp}^2)$$

Related to bulk properties of hadron states encoded in form factors

$$\int \mathrm{d}x \, x H_i(x,\xi,t) = A_i(t) + (2\xi)^2 C_i(t), \ \int \mathrm{d}x \, x E_i(x,\xi,t) = B_i(t) - (2\xi)^2 C_i(t)$$



#### **GUMP PROGRAM: MOMENT PARAMETERIZATION**

 Parameterize GPDs by directly parameterizing their conformal moments and resumming with a Mellin-Barnes integral

$$F(x,\xi,t) = rac{1}{2i} \int_{c-i\infty}^{c+i\infty} \mathrm{d}j rac{p_j(x,\xi)}{\sin(\pi[j+1])} \mathcal{F}_j(\xi,t)$$
 (D. Mueller and A. Schafer 2006)

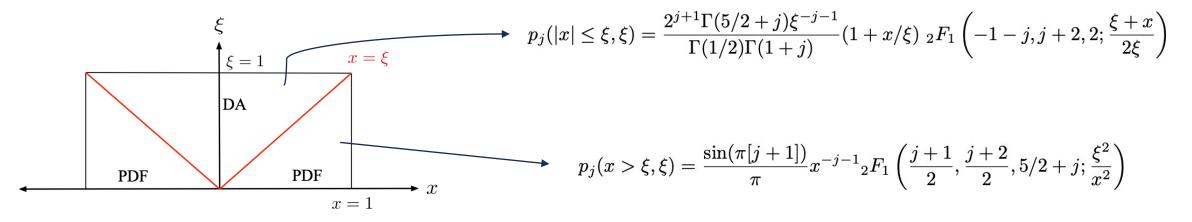
Expansion based on eigenfunctions of evolution – Gegenbauer polynomials

$$(-1)^{j} p_{j}(x,\xi) = \xi^{-j-1} \frac{2^{j} \Gamma(\frac{5}{2}+j)}{\Gamma(\frac{3}{2}) \Gamma(j+3)} \left[ 1 - \left(\frac{x}{\xi}\right)^{2} \right] C_{j}^{3/2} \left(\frac{x}{\xi}\right)$$
conformal wave
function
$$\int_{-1}^{1} \frac{dx'}{|\xi|} \mathcal{K} \left(\frac{x}{\xi}, \frac{x'}{\xi}\right) C_{j}^{3/2} \left(\frac{x}{\xi}\right) = \gamma_{j} C_{j}^{3/2} \left(\frac{x}{\xi}\right)$$
GPD evolution
kernel

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## ANALYTIC CONTINUATION OF MOMENTS

- Gegenbauer polynomials are only defined in the DA-like, only give a formal sum for the full GPD
- Analytic continuation to all values of x/ξ and complex values of conformal spin j yields two bases for the DA-like and PDF-like regions and allows for reconstruction of GPD across all (x, ξ)



#### **GUMP PROGRAM: MOMENT PARAMETERIZATION**

- Conformal moment parameterization has nice features for fitting GPDs
- Can analytically calculate convolutions in scattering amplitudes just one Mellin-Barnes integral to compute
- Simple and fast evolution implementation conformal moments are multiplicatively renormalized at LO
  - Follows from using eigenfunctions of evolution kernel
- Polynomiality condition (X. Ji 1998) automatically enforced on conformal moments

Theory constraints can be encoded directly in the moment parameterization!

 $\begin{array}{ll} f(x) = \sum_{i=0, \ i \neq n}^{1} \mathrm{d}x \, x^{n-1} F(x,\xi,t) = \sum_{k=0, \ i \neq n}^{n} \xi^{k} F_{i,n,k}(t) \\ f(x) = \sum_{i=0, \ i \neq n}^{j+1} \xi^{k} \mathcal{F}_{i,j,k}(t) \end{array}$ 

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## FLEXIBLE MOMENT PARAMETERIZATION

- Our starting point is a relatively simple model for the conformal moments
- Parameterize each GPD moment with five parameters

$$\begin{split} F_{i,j,0} &= N_i B(j+1-\alpha_i,1+\beta_i) \frac{j+1-\alpha_i}{j+1-\alpha_i(t)} \beta(t) & \beta(t) = e^{-b|t|} \\ & \uparrow & \\ & \text{Euler Beta} & \uparrow & \\ & \text{Function} & \text{Regge trajectory} & \alpha(t) = \alpha + \alpha' t \end{split}$$

Take each moment to be a power series in skewness – polynomiality condition

$$F_{i,j} = F_{i,j,0}(t) + \xi^2 R_{\xi^2} F_{i,j,0}(t) + \xi^4 R_{\xi^4} F_{i,j,0}(t) \dots$$

## FIRST STEP TOWARD GLOBAL GPD ANALYSIS

- The number of parameters needed for modelling all the species of GPD grows very quickly
- We impose extra constraints for simplicity

			Proportional
GPDs species and flavors	Fully parameterized	y parameterized GPDs linked to	
$H_{u_V}$ and $\widetilde{H}_{u_V}$	~	-	-
$E_{u_V}$ and $\widetilde{E}_{u_V}$	~	-	-
$H_{d_V}  ext{ and } \widetilde{H}_{d_V}$	~	-	-
$E_{d_V}$ and $\widetilde{E}_{d_V}$	×	$E_{u_V}$ and $\widetilde{E}_{u_V}$	$R^{E/\widetilde{E}}_{d_V}$
$H_{\bar{u}}$ and $\widetilde{H}_{\bar{u}}$	~	-	-
$E_{ar{u}}$ and $\widetilde{E}_{ar{u}}$	×	$H_{\bar{u}}$ and $\widetilde{H}_{\bar{u}}$	$R^{E/\widetilde{E}}_{ m sea}$
$H_{ar{d}}$ and $\widetilde{H}_{ar{d}}$	~	-	-
$E_{ar{d}}  ext{ and } \widetilde{E}_{ar{d}}$	×	$H_{\bar{d}} \mbox{ and } \widetilde{H}_{\bar{d}}$	$R^{E/\widetilde{E}}_{ m sea}$
$H_g$ and $\widetilde{H}_g$	~	-	-
$E_g$ and $\widetilde{E}_g$	×	$H_g$ and $\widetilde{H}_g$	$R^{E/\widetilde{E}}_{ m sea}$

## NON-ZERO SKEWNESS GLOBAL FIT

- Even with constraints, lots of parameters!
  - Very high dimensional space to navigate for best fit
  - Very computationally demanding to do error propagation
- We employ a sequential fit, starting with forward (PDF, t-dependent PDF) constraints for each GPD species then apply the off-forward constraints from DVCS data



## SEMI-FORWARD INPUTS

- JAM (2022) PDF global analysis results
  - Full global analysis should in principle fit to PDF sensitive data directly, but here we fit to JAM results
  - Limited number of points taken to avoid need for more sophisticated forward limit
- Globally extracted electromagnetic form factors (Z.Ye et al 2018)
- Lattice GPDs (Alexandrou et al 2020) and form factors (Alexandrou et al 2022)
  - x, t -dependent GPDs (semi-forward limit)

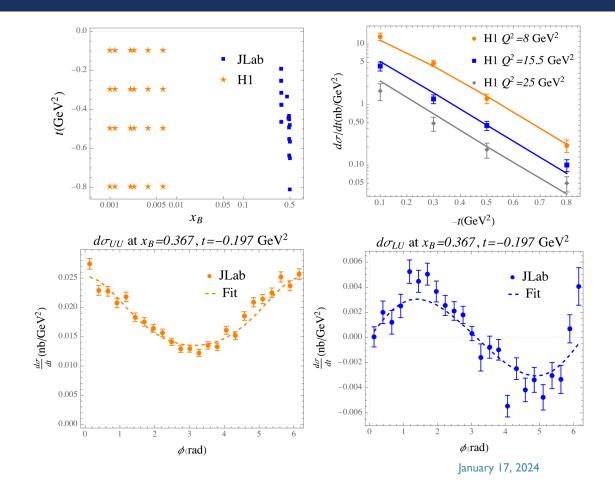
# **OFF-FORWARD INPUTS**

- DVCS measurements from JLab (CLAS 2019 & 2021, Hall A 2018 & 2022) and HERA (H1 2010)
- Only using t-dependent cross sections due to practical limitations
- Far more points from JLab data than from HERA from  $\varphi$ -dependence and both UU and LU polarization channels
- Off-forward lattice GPDs not used in fitting, but can supply crucial constraints for future work!

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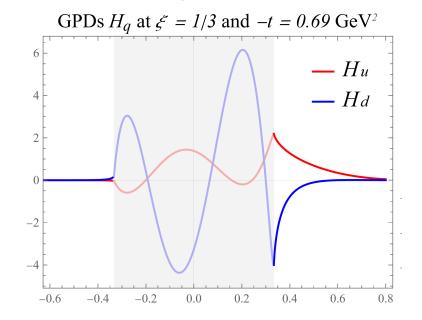
#### NON-ZERO SKEWNESS GLOBAL FIT

- Total  $\chi^2$ /dof is approximately 1.4
- Some agreement with both JLAB and H1 data
- Gluon GPDs not well constrained at non-zero skewness
  - Only contribute to DVCS through evolution at LO
- Error propagation is not yet implemented
  - Very computationally expensive with so many parameters!



#### EXTRACTED GPDS

- GPDs are mostly constrained on the  $\xi = x$  line and in the DGLAP region  $|\xi| < |x|$
- ERBL region shows large oscillations which are characteristic of the Gegenbauer polynomials used in the moment expansion

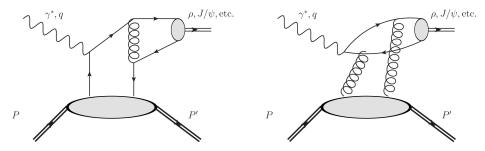


# MOVING FORWARD: ADDING IN GLUONS!



## **GLUON SENSITIVE PROCESSES**

- DVCS at LO is only sensitive to gluon GPDs through scale evolution
- Using Deeply Virtual Meson Production (DVMP) gives a direct probe of gluons at LO



- Light vector mesons have similar sensitivity to quarks and gluons
  - KM framework applied to produce simultaneous fits of DVCS and DVMP for  $\rho^0$  meson production with data from HERA (*arXiv:2310.13837*)
- Add heavy vector meson to obtain better constraints on gluon GPDs use  $J/\psi$  production!

# DEEPLY VIRTUAL $J/\psi$ PRODUCTION (DV $J/\psi$ P)

- Charm quark contribution for nucleon target is negligible direct probe of gluons
- Complementary with GUMP work on quark GPDs, but mostly sensitive to small- $x_B$  region whereas JLab data combined with HERA gives better constraint at moderate  $x_B$
- Caveat: mass of the  $J/\psi$  gives significant power corrections to collinear factorization

$$M_{J/\psi}^2/Q_{
m max\ bin}^2 \approx 9/20 
ightarrow {
m corrections\ of\ order}\, 1/2$$

Need to take heavy mass corrections into account – non-relativistic (NR) QCD!

#### NON-RELATIVISTIC MODEL APPROACH

• Encoding the  $J/\psi$  formation into NR matrix elements

$$\Gamma[J/\psi \to e^+e^-] = \frac{8\pi\alpha_{EM}^2}{27} \frac{f_{J/\psi}^2}{m_c} \to \frac{8\pi\alpha_{EM}^2}{27} \frac{\langle \mathcal{O}_1 \rangle_{J/\psi}}{m_c^2}$$

 Maintain the form of the factorization theorem for the process – still sensitive to leading twist GPDs (D.Y. Ivanov et al 2004)

$$\mathcal{A}_{\text{collinear}} \sim \int_{0}^{1} \mathrm{d}z \int_{-1}^{1} \mathrm{d}x C_{1}(x,\xi,z) F^{g}(x,\xi,t) \Phi(z) \longrightarrow \mathcal{A}_{\text{NR}} \sim \sqrt{\frac{\langle \mathcal{O}_{1} \rangle_{J/\psi}}{m_{c}}} \int_{-1}^{1} \mathrm{d}x C_{2}\left(x,\xi,\frac{m_{c}}{Q}\right) F^{g}(x,\xi,t)$$

$$\begin{array}{c} \mathsf{GPD} \\ \mathsf{GPD} \\ \mathsf{GPD} \\ \mathsf{hard scattering term} \end{array}$$

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pQCD!

## NON-RELATIVISTIC MODEL APPROACH

- Including the mass corrections means we have a hard scale even as  $Q^2 \rightarrow 0$ , so we can potentially include photoproduction data in future fits!
- The NRQCD treatment includes both photon polarizations eliminates largest source of uncertainty in data at the cost of model dependence

$$\begin{split} R &= \frac{\mathrm{d}\sigma_L}{\mathrm{d}\sigma_T} = \frac{Q^2}{M_{J/\psi}^2} \\ \Rightarrow \mathrm{d}\sigma_{total} &= \left(\varepsilon + \frac{M_{J/\psi}^2}{Q^2}\right) \mathrm{d}\sigma_L \end{split}$$

 $\varepsilon \sim {\rm longitudinal \ to} \ {\rm transverse \ photon} \ {\rm flux \ ratio}$ 

- Previous studies on  $J/\psi$  photoproduction have seen a poor description with LO calculations
  - NLO hard scattering corrections are large and improve the description
- Using the same LO treatment as for our previous global analysis, we see the problem persists for DV  $J/\psi$  P
  - Here we will add in both NLO hard scattering corrections and NLO GPD evolution!
- NLO GPD evolution kernel is known in conformal moment space (*Kumerički et al 2008*)
  - Allows for (relatively) fast numerical implementation!
- Finite mass corrections for hard scattering are only known in momentum fraction space (Flett et al 2021)
  - Mass corrections make the convolutions for converting to conformal moment space much more complicated
  - Converting these is crucial in order to include photoproduction in our global analysis framework

- We have implemented NLO GPD evolution for the sea quarks and gluons (valence quarks are insignificant for small x<sub>B</sub> HERA kinematics)
  - Huge thanks to Gepard package full NLO implementation of DVCS and DVMP for light vector mesons available!
- Conversion of NLO finite mass hard scattering terms to moment space is on going
- Collinear factorization NLO hard scattering terms are known in conformal moment space (Müller et al 2014)
  - Gives the large logs of  $1/x_B$  that are important for HERA data, mass corrections shouldn't be too significant for higher  $Q^2$  data points

 Matching between the NRQCD matrix element and the distribution amplitude in conformal moment space can introduce some ambiguity from expanding a delta function

$$\langle \mathcal{O}_1 \rangle_{J/\psi} \Rightarrow \Phi_{J/\psi}(z) \propto \delta(z - 1/2)$$
  
 $\Rightarrow \delta(z - 1/2) = \sum_{k=0}^{\infty} 6z(1 - z)C_k^{3/2}(2z - 1)\Phi_k,$ 

$$\Phi_k = \frac{2(2k+3)}{3(k+1)(k+2)} C_k^{3/2}(0)$$

Not clear how to extract size of truncation error!

 For simplicity we keep only the first conformal moment (asymptotic DA), so we introduce an order one normalization factor into the amplitudes to absorb the mismatch

k = 0, 2, 4...

$$\Phi_{J/\psi}(z) = N^{DA} \Phi_{asymptotic}(z)$$

We can make a hybrid scheme by combining the NRQCD LO terms with collinear factorization NLO hard scattering and universal NLO GPD evolution

$$\mathcal{A}_{\mathrm{Hyb.}} \propto \sqrt{rac{\langle \mathcal{O}_1 
angle_{J/\psi}}{m_c}} \sum_{i=flavors,g} \int_0^1 \mathrm{d}z rac{\Phi_{asymptotic}(z)}{z(1-z)} \int_{-1}^1 \mathrm{d}x C_2^i(x,\xi,z) F^i(x,\xi,t)$$

Passing to moment space we write

$$\begin{split} \mathcal{A}_{\text{Hyb.}} &\propto \sqrt{\frac{\langle \mathcal{O}_1 \rangle_{J/\psi}}{m_c}} \sum_{i=flavors,g} \int_{c-i\infty}^{c+i\infty} \mathrm{d}j\xi^{-j-1} \left[ i + \tan\left(\frac{\pi j}{2}\right) \right] & \text{renormalization scales equal} \\ &\times \left[ C^{i,LO} E_j^{i,LO}(Q^2) + C^{i,NLO} E_j^{i,LO}(Q^2) + C^{i,LO} E_j^{i,NLO}(Q^2) \right] \mathcal{F}_j^i(\xi,t) \end{split}$$

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We set the factorization and

# GLUON GPD FIT INPUTS

- We use 17 *t*-dependent cross section points from H1 (2006) data
  - $< Q^2 >$  in range 7.0 22.4 GeV<sup>2</sup>,  $x_B$  in range  $9 \times 10^{-4} 6 \times 10^{-3}$ , and |t| in range 0.04 0.64 GeV<sup>2</sup>
  - The data has negligible sensitivity to the GPD E, so we only fit parameters coming from the GPD  $H: b^g$  and  $R_{\xi^2}$  as well as the DA normalization parameter  $N^{DA}$
- Given the small values of  $x_B$ , we redo the fit of our forward gluon PDF parameters in a simultaneous fit, using 9 points from the JAM22 global analysis with  $Q^2 = 4 \ GeV^2$  and  $x_B = 10^{-4} 10^{-3}$  to constrain  $N^g$ ,  $\alpha^g$ ,  $\beta^g$ 
  - Limited number of points constraining forward limit since we have a limited number of off-forward data points

## GLUON GPD PRELIMINARY FIT RESULTS

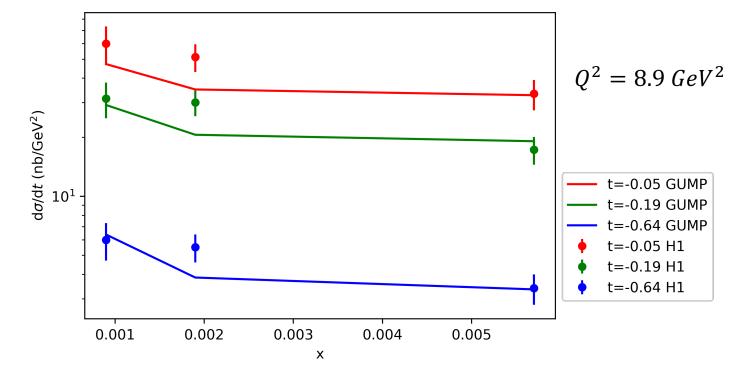
- Minimizing with Minuit2 gives  $\chi^2/dof \approx 0.98$  and the following best-fit parameters
- Only statistical uncertainties from Minuit2 right now, full error propagation left for future work

Best-Fit Parameters			
Parameter	Best-Fit Value	Statistical Uncertainty	
$N^g$	1.83	0.21	
$lpha^g$	1.097	0.015	
$\beta^{g}$	10	6	
$R^g_{\xi^2}$	-0.14	0.06	
$b^g$	1.80	0.12	
Namp	1.08	0.12	

Note the large uncertainty in  $\beta^g$  - expected from using small  $x_B$  PDFs but also correlation with normalization factors through  $B(j+1-\alpha,1+\beta)$ 

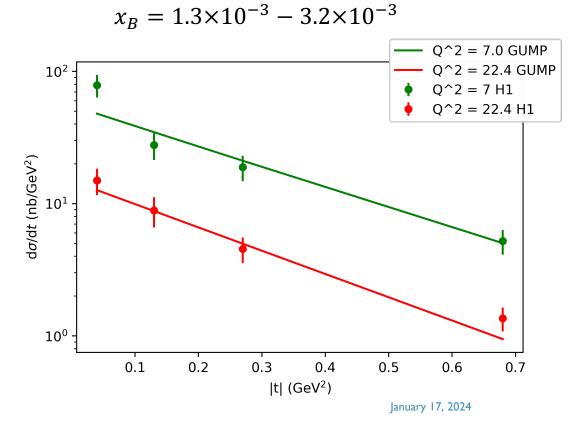
## GLUON GPD PRELIMINARY FIT RESULTS

- For  $Q^2 \sim M_{J/\psi}^2$  or larger our hybrid scheme describes the data relatively well
- The x<sub>B</sub>-dependence here crucially relies on the large logarithms entering the NLO corrections in our framework



#### GLUON GPD PRELIMINARY FIT RESULTS

- Going to lower Q<sup>2</sup> we start to see discrepancy with the data
  - Lower Q<sup>2</sup> brings in higher twist effects, same issue for DVCS
  - Lower  $M_{J/\psi}^2/Q^2$  enhances power corrections which we have dropped in the NLO terms



## FUTURE IMPROVEMENTS/ADDITIONS FOR GLUONS IN GUMP

- Simultaneous fit with  $DV\rho^0P$  data from HERA
- Further analysis of fit results
  - Uncertainty from renormalization/factorization scale setting
  - Skewness ratio H(x, x, 0)/H(x, 0, 0)
- Conversion of NLO mass corrections to moment space
  - Can add photoproduction data to fits
- More sophisticated moment ansatz
  - Inclusion of lattice calculations and moderate  $x_B$  experimental data requires more complicated ansatz
- Full DVCS and DVMP global analysis with NLO correctios

## FUTURE ADDITIONS TO GUMP

- Full uncertainty propagation
- Add threshold  $J/\psi$  production potentially constrain D-term/DA-terms
- Implement *t*-integrated cross sections
- Add quark flavors and implement  $\phi$  electroproduction
  - Could examine  $N_f$  dependence so far just u and d quarks
- Add other processes like TCS or recently proposed SDHEP (Qiu and Yu 2022-2023)

## CONCLUSIONS

- Fit DV  $J/\psi$  P data from HI using gluon GPD H parameters in hybrid collinear-NRQCD factorization
- Further analysis of fits and  $DV\rho^0P$  fits in progress
- Several directions for future improvements available both for gluon sector and GUMP overall

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# **BACKUP SLIDES**



## ANALYTIC CONTINUATION OF MOMENTS

- Gegenbauer moments from ERBL region only give a formal sum for the full GPD
- Analytic continuation to all values of  $x/\xi$  yields two bases for the ERBL and DLGAP regions

$$p_j(|x| \le \xi, \xi) = \frac{2^{j+1} \Gamma(5/2+j) \xi^{-j-1}}{\Gamma(1/2) \Gamma(1+j)} (1+x/\xi) \, _2F_1\left(-1-j, j+2, 2; \frac{\xi+x}{2\xi}\right)$$

$$p_j(x > \xi, \xi) = \frac{\sin(\pi[j+1])}{\pi} x^{-j-1} {}_2F_1\left(\frac{j+1}{2}, \frac{j+2}{2}, 5/2+j; \frac{\xi^2}{x^2}\right)$$

 These conformal wave functions can then be used to reconstruct the GPD from its conformal moments with a Mellin-Barnes integral

$$F(x.\xi,t) = \frac{1}{2i} \int_{c-i\infty}^{c+i\infty} \mathrm{d}j \frac{p_j(x,\xi)}{\sin(\pi[j+1])} \mathcal{F}_j(\xi,t)$$

#### CONFORMAL MOMENT POLYNOMIALITY

• We can expand the Gegenbauer polynomials in a power series, connecting them to the Mellin moment expansion  $C^{(\lambda)}(x) = \sum_{k=1}^{j} e^{(\lambda)} x^{k}$ 

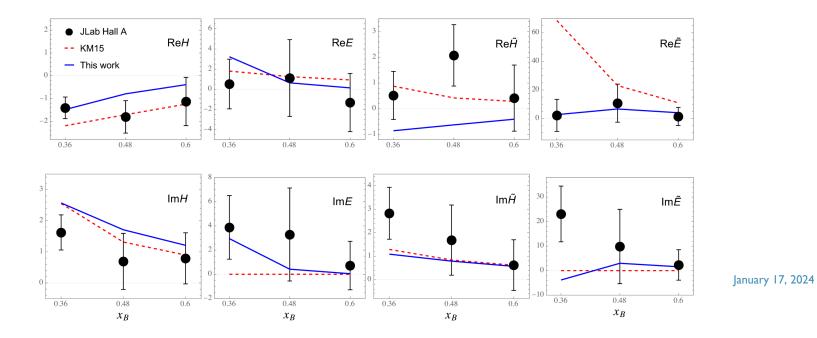
$$C_j^{(\lambda)}(x) = \sum_{k=0}^j c_{j,k}^{(\lambda)} x^k$$

Then using the polynomiality of the Mellin moments we obtain a polynomiality condition on the conformal moments

$$\mathcal{F}_{j}(\xi,t) \propto \int_{-1}^{1} \mathrm{d}x \ \xi^{j} C_{j}^{\frac{3}{2}} \left(\frac{x}{\xi}\right) F(x,\xi,t)$$
$$= \int_{-1}^{1} \mathrm{d}x \sum_{k=0}^{j} c_{j,k}^{\frac{3}{2}} \xi^{j-k} x^{k} F(x,\xi,t)$$
$$= \sum_{k=0}^{j} c_{j,k}^{\frac{3}{2}} \xi^{j-k} \int_{-1}^{1} \mathrm{d}x x^{k} F(x,\xi,t)$$

#### NON-ZERO SKEWNESS GLOBAL FIT: CFFS

- CFFs from fit are mostly consistent with local extraction from JLAB Hall A data as well as KMI5 extractions
- Some inconsistencies can be expected from degeneracies in CFF contribution to cross sections – need more polarization configurations!



## AMBIGUITY IN ERBL REGION

• We can add terms in the moment expansion which only contribute to the ERBL region

$$(-1)^{j} p_{j}(x,\xi) = \xi^{-j-1} \frac{2^{j} \Gamma(\frac{5}{2}+j)}{\Gamma(\frac{3}{2}) \Gamma(j+3)} \left[ 1 - \left(\frac{x}{\xi}\right)^{2} \right] C_{j}^{3/2} \left(\frac{x}{\xi}\right), \quad |x| < |\xi|$$

 This suggests an interpretation of the GPDs in terms of quark and antiquark pieces as well as a ERBL region distribution amplitude (DA) piece

## CONNECTION TO D-TERM

- These DA terms don't have a large affect on CFFs, but they do contain information related to the various D-terms in QCD, ex.
  - Gravitational form factor C/D

$$\int_{-1}^{1} \mathrm{d}x \, x H_q(x,\xi,t) = A_q(t) + (2\xi)^2 C_q(t)$$

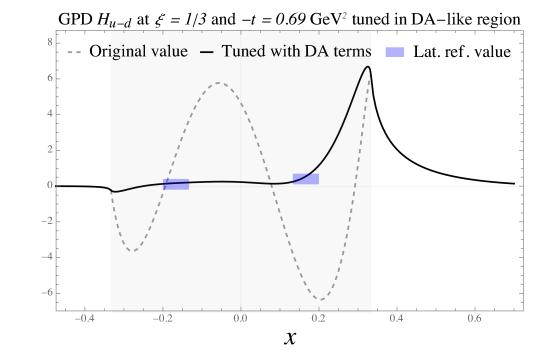
Dispersion relation subtraction term

$$F(\xi, t, Q^2) = \frac{1}{\pi} \int_0^1 \mathrm{d}\xi' \left( \frac{1}{\xi - \xi'} \mp \frac{1}{\xi + \xi'} \right) \operatorname{Im} \left[ F(\xi' - i0, t, Q^2) \right] + \mathcal{C}(t, Q^2)$$

By constraining the DA terms with further experimental data and lattice calculations, we can access the mechanical properties of hadrons contained in these D-terms!

#### CONSTRAINING DA TERMS

- Adding in lattice GPD calculations can give us constrains directly in the ERBL region
- Adding just a few terms to the moment expansion can remove the unphysical oscillations



# BEST FIT $\chi^2$ BREAKDOWN

Sub-fits	$\chi^2$	$N_{ m data}$	$\chi^2_ u\equiv\chi^2/ u$
Semi-forward			
t PDF H	281.7	217	1.41
t PDF E	59.7	50	1.36
$t \mathrm{PDF}~\widetilde{H}$	159.3	206	0.84
$t \mathrm{PDF}~\widetilde{E}$	63.8	58	1.23
Off-forward			
JLab DVCS	1413.7	926	$\sim 1.53$
H1 DVCS	19.7	24	$\sim 0.82$
Off-forward total	1433	950	1.53
Total	2042	1481	1.40

Vector GPDs $H$ and $E$		Axial-vector GPDs $\widetilde{H}$ and $\widetilde{E}$		
Parameter	Value (uncertainty)	Parameter	Value (uncertainty)	
$N_{u_V}^H$	4.923(89)	$N^{\widetilde{H}}_{u_V}$	4.833(429)	
$lpha_{u_V}^H$	0.216(7)	$lpha_{u_V}^{\widetilde{H}}$	-0.264 (34)	
$eta^H_{u_V}$	3.229(23)	$eta^{\widetilde{H}}_{u_V}$	3.186 (122)	
$\alpha_{u_V}^{\prime H}$	2.347(51)	$\alpha_{u_V}^{\prime \widetilde{H}}$	2.182(175)	
$N^H_{ar{u}}$	0.163(8)	$N_{ar{u}}^{\widetilde{H}}$	0.070 (33)	
$lpha_{ar{u}}^H$	1.136(10)	$lpha_{ar{u}}^{\widetilde{H}}$	0.538(112)	
$eta_{ar{u}}^{H}$	6.894(207)	$eta_{ar{u}}^{\widetilde{H}}$	4.229(1320)	
$N^H_{d_V}$	3.359(170)	$N_{d_V}^{\widetilde{H}}$	-0.664 (170)	
$lpha_{d_V}^H$	0.184(18)	$lpha_{d_V}^{\widetilde{H}}$	0.248(76)	
$\beta^{H}_{d_{V}}$	4.418 (77)	$eta_{d_V}^{\widetilde{H}}$	3.572(477)	
$lpha_{d_V}^{\prime H}$	3.482(171)	$\alpha'_{d_V}^{\check{H}}$	0.542(103)	
$N_{\bar{d}}^H$	0.249(12)	$N^{ar{H}}_{ar{d}}$	-0.086 (42)	
$lpha_{ar{d}}^{H}$	1.052(10)	$\alpha_{ar{d}}^{\widetilde{H}}$	0.495(137)	
$eta^{H}_{ar{d}}$	6.554(216)	$eta_{ar{d}}^{ ilde{H}}$	2.554 (897)	
$N_g^H$	2.864(108)	$N_g^{\widetilde{H}}$	0.243(304)	
$\alpha_a^H$	1.052(8)	$lpha_g^{\widetilde{H}}$	0.631(330)	
$\beta_g^H$	7.413(165)	$\beta_g^{\widetilde{H}}$	2.717(2865)	
$N_{u_V}^E$	0.181 (38)	$N_{u_V}^{\widetilde{E}}$	7.993(3480)	
$lpha^E_{u_V}$	0.907(17)	$lpha_{u_V}^{\widetilde{E}}$	0.800 (116)	
$\beta_{u_V}^E$	1.102(245)	$\beta_{u_V}^{\widetilde{E}}$	6.415(1577)	
$lpha_{u_V}^{\prime E}$	0.461 (86)	$lpha_{u_V}^{\prime \widetilde{E}}$	2.076(933)	
$N_{d_V}^E$	-0.223 (47)	$N_{d_V}^{\widetilde{E}}$	-2.407(1239)	
$R^E_{ m sea}$	0.768~(169)	$R_{ m sea}^{\widetilde{E}}$	38 (8)	
$R_{u,2}^H$	0.229(0.032)	$R_{u,2}^{\widetilde{H}}$	0.246(81)	
$R_{d,2}^H$	-2.639 (202)	$R_{d,2}^{\widetilde{H}}$	1.656(375)	
$R_{u,2}^{E}$	0.799~(285)	$R_{u,2}^{\widetilde{E}}$	2.684(171)	
$R^{E}_{d,2}$	3.404 (1157)	$R_{d,2}^{\widetilde{E}}$	38 (2)	
$b_{\mathrm{sea}}^{H}$	3.448 (133)	$b_{ m sea}^{ ilde{H}}$	9.852 (1330)	

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