

# Physics at High Baryon Density

- Study the QCD Phase Structure in High-Energy Nuclear Collisions

Nu Xu

LBL / GSI

# Outline

---

## 1) Introduction

## 2) Results from RHIC BES Program

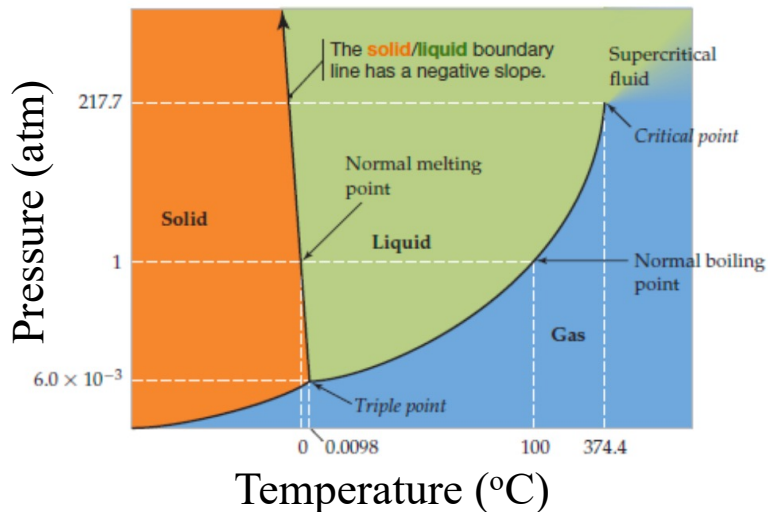
- i. Collectivity (EOS)
- ii. Criticality (EOS, CP)
- iii. Baryon Correlations (EOS, NN, YN)

## 3) Outlook

# Phase Structure of Strong Interactions

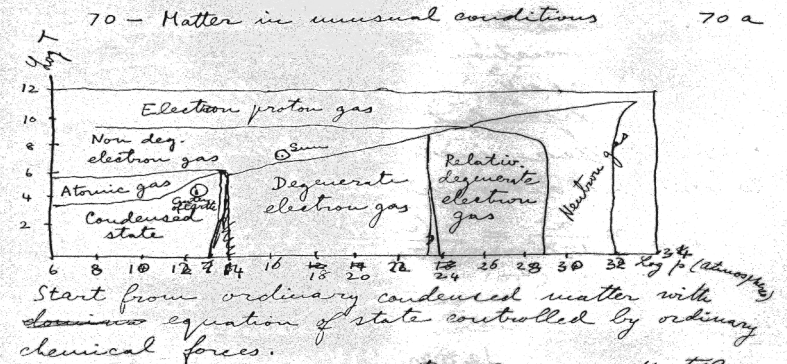
**Phase Diagram:** For given degrees of freedom, how matter (re)organizes itself under external conditions

Phase Diagram of Water: QED at Work



E. Fermi

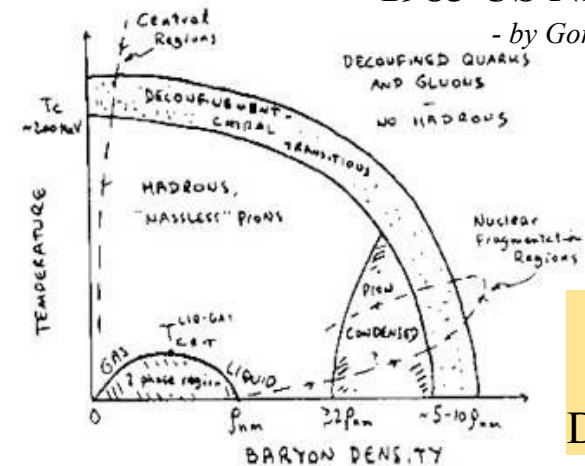
“Notes on Thermodynamics and Statistics” (1953)



Gordon Baym

1983 US NP LRP

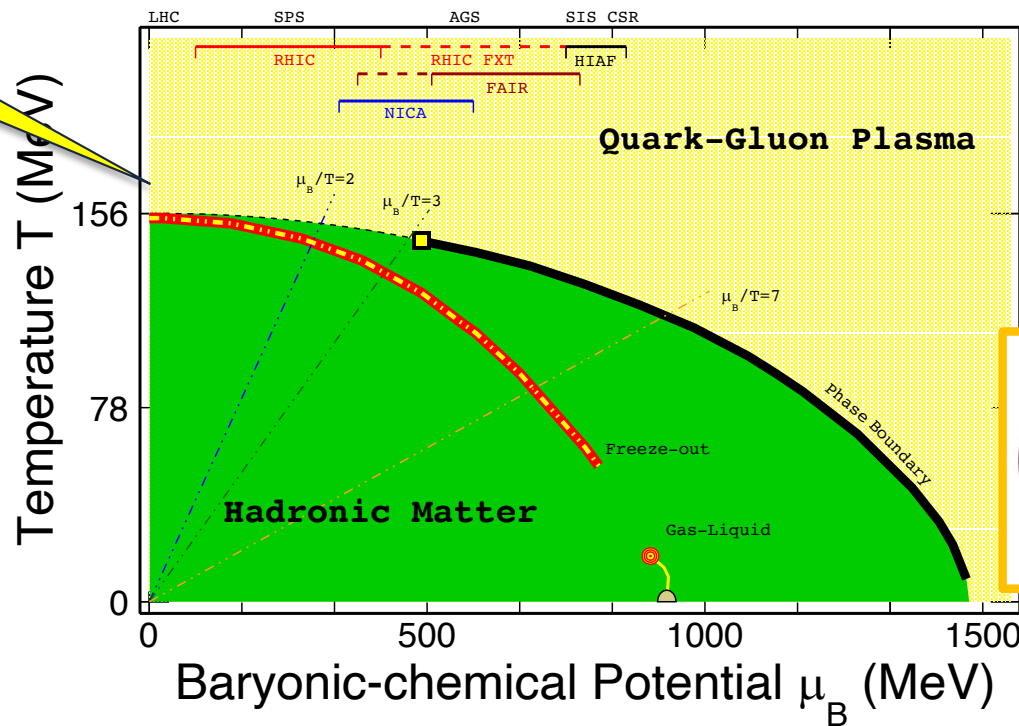
- by Gordon Baym



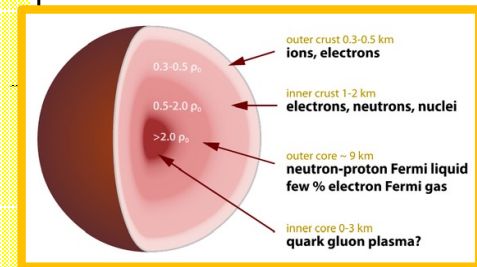
QCD  
Phase  
Diagram

# Nuclear Collisions and QCD Phase Diagram

Early Universe

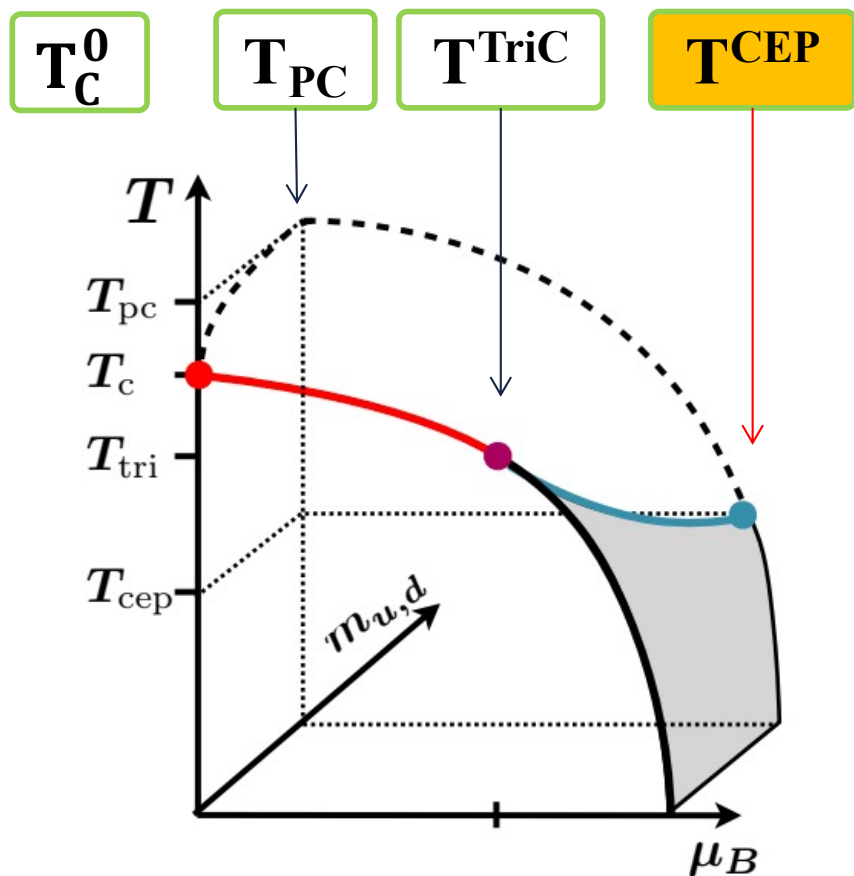


High baryon density:  
Inner structure of  
compact stars



- 1) RHIC BES: → search for 1<sup>st</sup>-order phase transition and **QCD critical point**;
- 2) Baryon interactions (e.g.  $N - N$ ,  $Y - N$ ) → inner structure of compact stars

# LGT Calculation: QCD Phase Structure



F. Karsch *et al.*, 2020

1) QCD transition temperature:

$$T_{PC} = 156.5 \pm 1.5 \text{ MeV}$$

2) Chiral crossover line

$$T_{PC}(\mu_B) = T_{PC}^0 \left[ 1 - \kappa_2 \left( \frac{\mu_B}{T_{PC}^0} \right)^2 - \kappa_4 \left( \frac{\mu_B}{T_{PC}^0} \right)^4 \right]$$

$$\kappa_2 = 0.012(4), \quad \kappa_4 = 0.00(4)$$

3) Chiral transition temperature:

$$T_C = 132_{-6}^{+3} \text{ MeV}$$

4) QCD critical end point, if exists:

$$T^{CEP} < T_C, \quad \mu_B^{CEP} \gtrsim 3T_C$$

HotQCD: Phys.Lett.**B795**, 15(2019);  
Phys. Rev. Lett. **123**, 062002(2019)

# STAR DETECTOR SYSTEM

**EEMC**

**iTOF**

**MTD**

**EMC**

**Mag.**

**TPC**

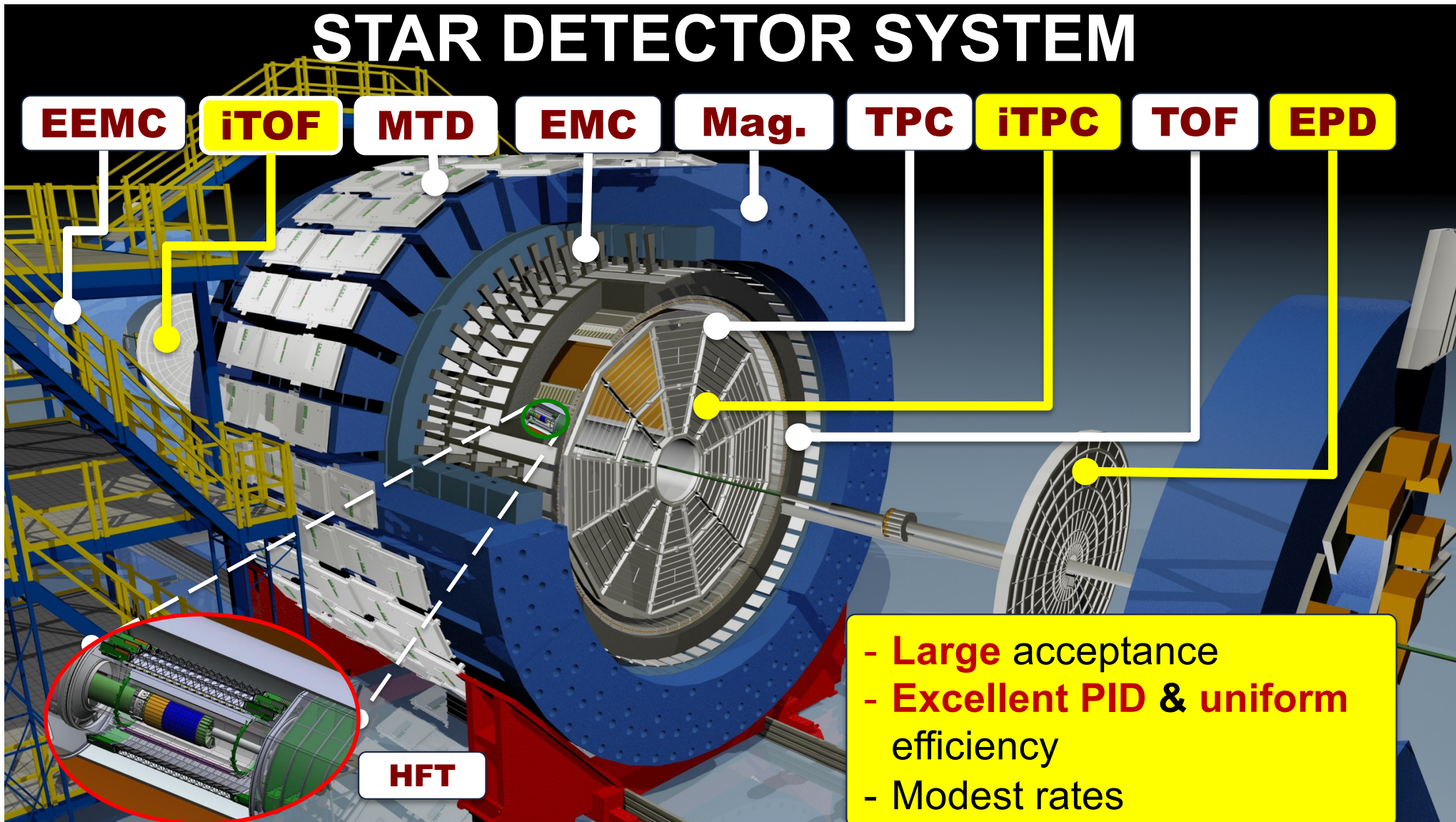
**iTPC**

**TOF**

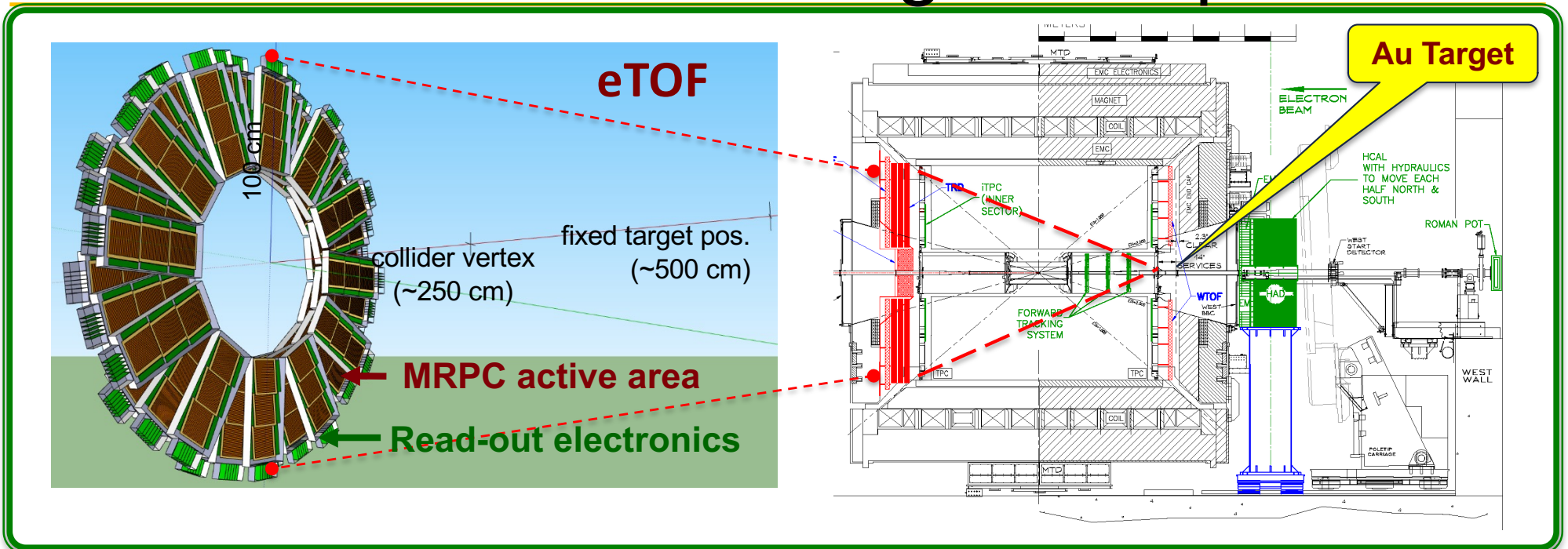
**EPD**

**HFT**

- **Large** acceptance
- **Excellent PID & uniform** efficiency
- Modest rates



# STAR Fixed Target Setup



## CBM participates in RHIC BES-II in 2019 – 2021:

- Complementary to CBM program:  $\sqrt{s_{NN}} = 3 - 7.2 \text{ GeV}$  ( $760 \geq \mu_B \geq 420 \text{ MeV}$ )
- Strange-hadron, hyper-nuclei and fluctuation at the high baryon density region

# STAR BES-I and BES-II Data Sets

## Au+Au Collisions at RHIC

Collider Runs						Fixed-Target Runs					
	$\sqrt{s_{NN}}$ (GeV)	#Events	$\mu_B$	$y_{beam}$	run		$\sqrt{s_{NN}}$ (GeV)	#Events	$\mu_B$	$y_{beam}$	run
1	<b>200</b>	<b>380 M</b>	<b>25 MeV</b>	5.3	Run-10, <b>19</b>	1	13.7 (100)	50 M	280 MeV	-2.69	Run- <b>21</b>
2	62.4	46 M	75 MeV		Run-10	2	11.5 (70)	50 M	320 MeV	-2.51	Run- <b>21</b>
3	54.4	1200 M	85 MeV		Run-17	3	9.2 (44.5)	50 M	370 MeV	-2.28	Run- <b>21</b>
4	39	86 M	112 MeV		Run-10	4	7.7 (31.2)	260 M	420 MeV	-2.1	Run- <b>18, 19, 20</b>
5	27	585 M	156 MeV	3.36	Run-11, <b>18</b>	5	7.2 (26.5)	470 M	440 MeV	-2.02	Run- <b>18, 20</b>
6	19.6	595 M	206 MeV	3.1	Run-11, <b>19</b>	6	6.2 (19.5)	120 M	490 MeV	1.87	Run- <b>20</b>
7	17.3	256 M	230 MeV		Run- <b>21</b>	7	5.2 (13.5)	100 M	540 MeV	-1.68	Run- <b>20</b>
8	14.6	340 M	262 MeV		Run-14, <b>19</b>	8	4.5 (9.8)	110 M	590 MeV	-1.52	Run- <b>20</b>
9	11.5	57 M	316 MeV		Run-10, <b>20</b>	9	3.9 (7.3)	120 M	633 MeV	-1.37	Run- <b>20</b>
10	9.2	160 M	372 MeV		Run-10, <b>20</b>	10	3.5 (5.75)	120 M	670 MeV	-1.2	Run- <b>20</b>
11	7.7	104 M	420 MeV		Run- <b>21</b>	11	3.2 (4.59)	200 M	699 MeV	-1.13	Run- <b>19</b>
						12	<b>3.0 (3.85)</b>	<b>260 + 2000 M</b>	<b>760 MeV</b>	-1.05	Run-18, <b>21</b>

**Most precise data to map the QCD phase diagram**

$$3 < \sqrt{s_{NN}} < 200 \text{ GeV}; \quad 760 > \mu_B > 25 \text{ MeV}$$



# Outline

---

## 1) Introduction

## 2) Results from RHIC BES Program

- i. Collectivity (EOS)
- ii. Criticality (EOS, CP)
- iii. Baryon Correlations (EOS, NN, YN)

## 3) Outlook

# Collectivity

$$\begin{aligned}\partial_\mu [(\varepsilon + p)u^\mu u^\nu - pg^{\mu\nu}] &= 0 \\ \partial_\mu [s u^\mu] &= 0\end{aligned}$$

$$\frac{d^2N}{p_T dp_T d\varphi} = \frac{1}{2\pi} \frac{dN}{p_T dp_T} \left\{ 1 + \sum_{n=1}^{\infty} 2v_n(p_T) \cos[n(\varphi - \Psi_R)] \right\}$$

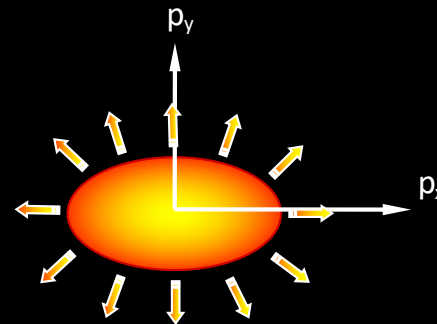
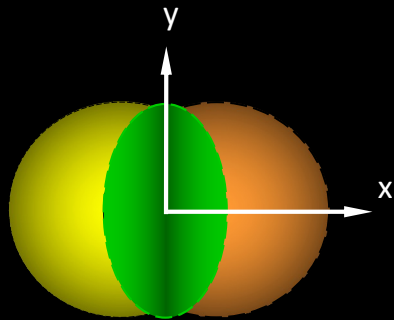
- $v_1$  Directed flow;
- $v_2$  Elliptic flow;
- $v_3$  Triangle flow

# Anisotropy Parameter $v_2$

coordinate-space-anisotropy



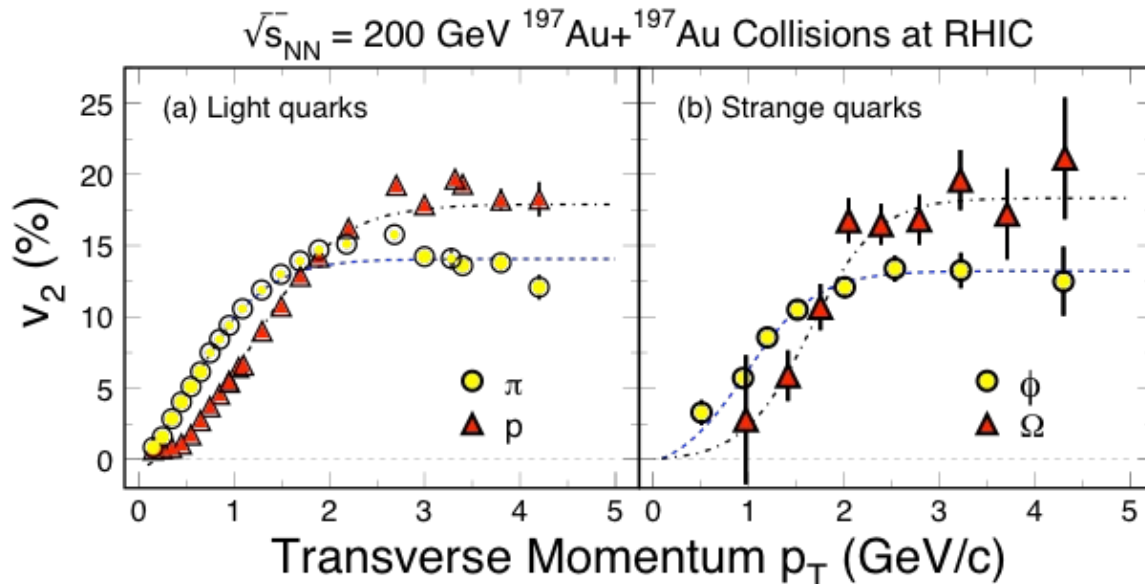
momentum-space-anisotropy



$$\varepsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle} \quad v_2 = \langle \cos 2\varphi \rangle, \quad \varphi = \tan^{-1} \left( \frac{p_y}{p_x} \right)$$

**Sensitive to initial/final conditions, EoS and degrees of freedom**

# Partonic Collectivity at RHIC



STAR: PRL116, 62301(2016)

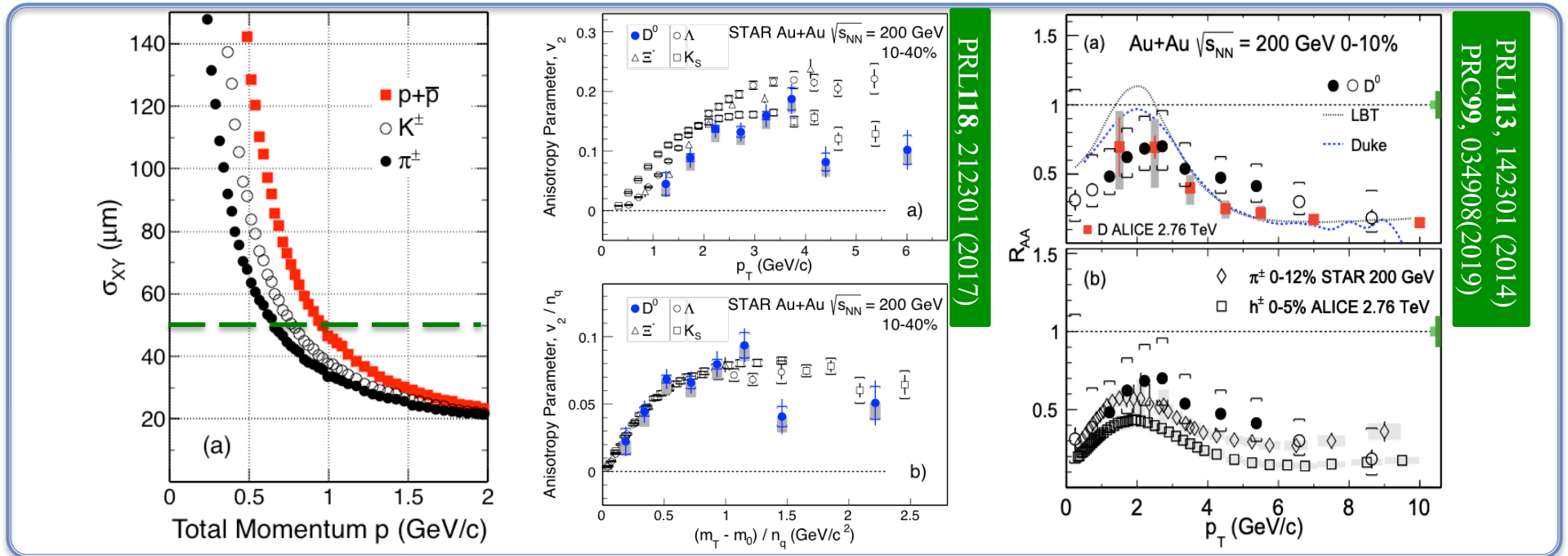
- ✓ Low  $p_T$  ( $\leq 2 \text{ GeV}/c$ ): hydrodynamic mass ordering
- ✓ High  $p_T$  ( $> 2 \text{ GeV}/c$ ): **number of quarks scaling (NCQ)**

u-, d-, and s-quarks flow!

- **Partonic Collectivity!**
- **De-confinement Au+Au collisions at RHIC!**

STAR: PRL116, 62301(2016)

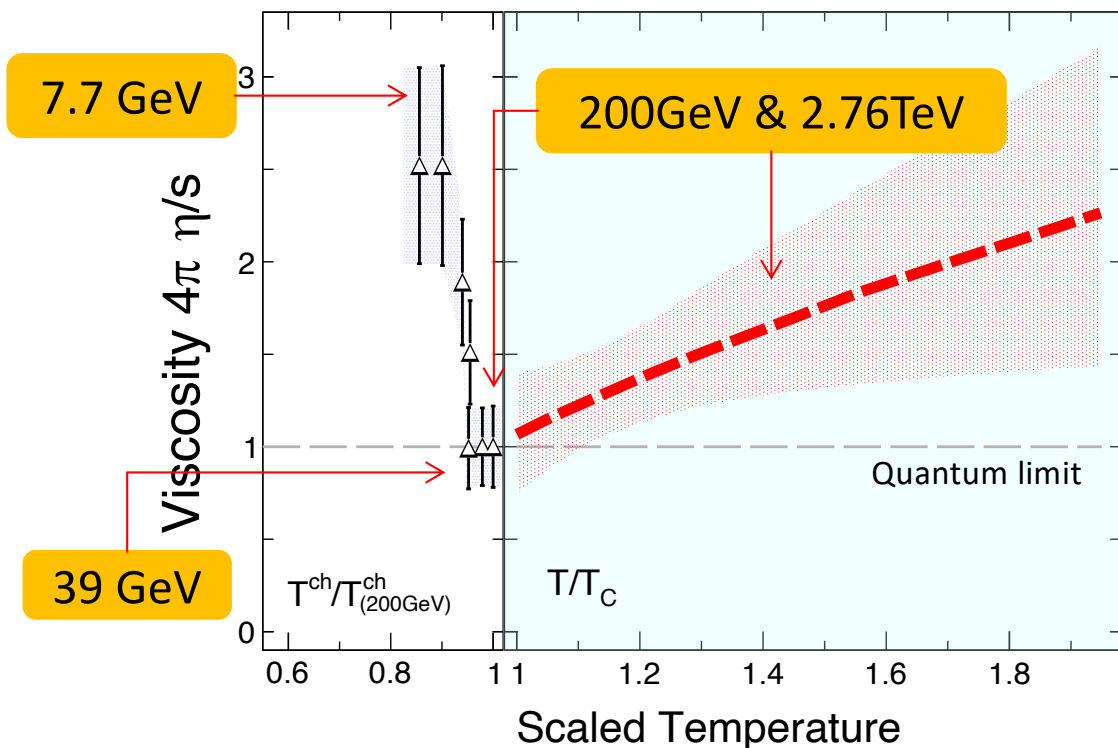
# Heavy Flavor $D^0$ Collectivity at HRIC



- 1) First application of MAPS technology in high energy collisions, excellent position resolution;
  - “These results suggest that charm quarks have achieved **local thermal equilibrium** with the medium created in such (200GeV Au+Au) collisions”
  - Hadronization via **quark coalescence** process

STAR: PRL113, 142301(14); PRC99, 034908(19); PRL118, 212301(17); PRL123, 162301(19); PRL124, 172301(20)

# Equation of State for Strong Interaction

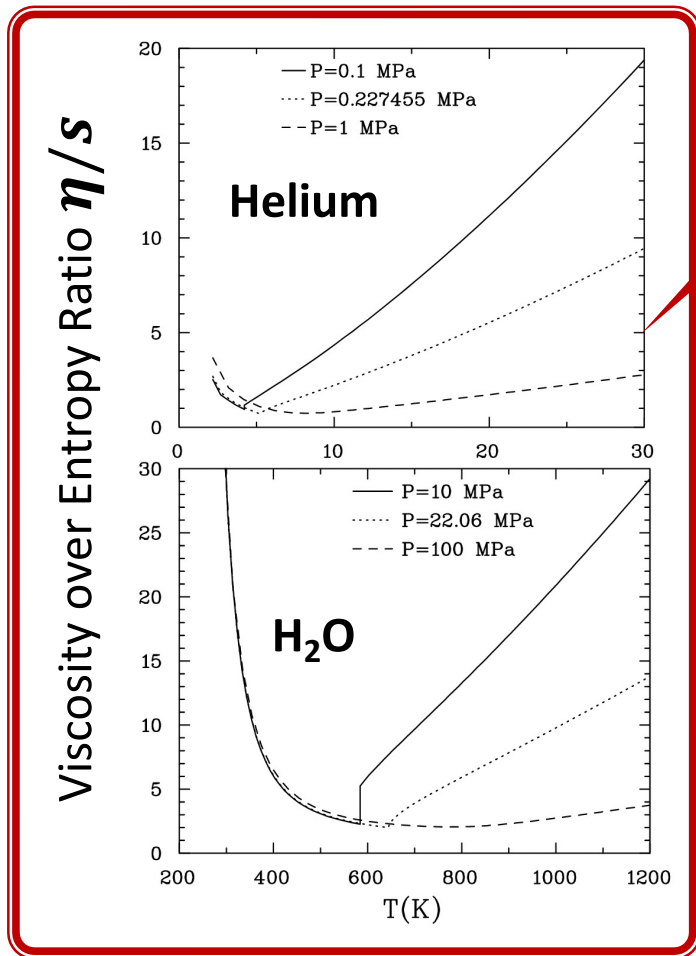


- 1) Left-plot: Energy dependence of  $\eta/s$  extracted from light-flavor hadron  $v_2$  and  $v_3$ . Right-plot: extracted from Bayesian fits to  $R_{AA}$  and  $v_2$  at 200GeV collisions;
- 2) Both sides meet at the unity of the scaled temperature;
- 3) The values of  $\eta/s$  increase quickly below  $\sqrt{s_{NN}} = 39$  GeV  $\rightarrow$  QGP dominants in higher energies;

## 4) Evidence of the QCD transition!

- 1) L.P. Csernai, J.I. Kapusta, L.D. McLerran, PRL **97** (2006) 152303
- 2) X.Dong, Y.J. Lee & R.Rapp, ARNPS, **69** (2019) 417
- 3) J.E.Bernhard, J.S.Moreland & S. Bass, Nat. Phys. **15** (2015) 1113
- 4) I. Karpenko, P. Huovinen, H. Petersen, and M. Bleicher, Phys.Rev. **C91**, 064901 (2015).
- 5) G.Nijs, W.van der Schee, U. Gürsoy and R. Snellings, PRL **126**, (2021) 202301

# Strongly-Interacting Low-Viscosity Matter

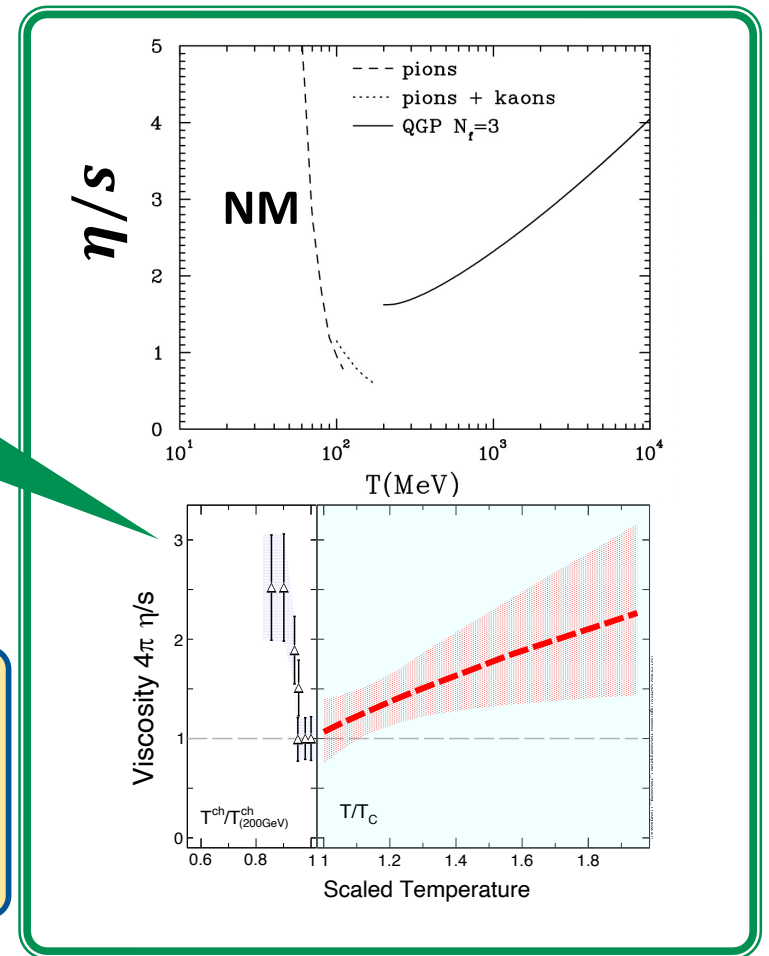


**EM interaction**  
 $\eta/s \sim 1$

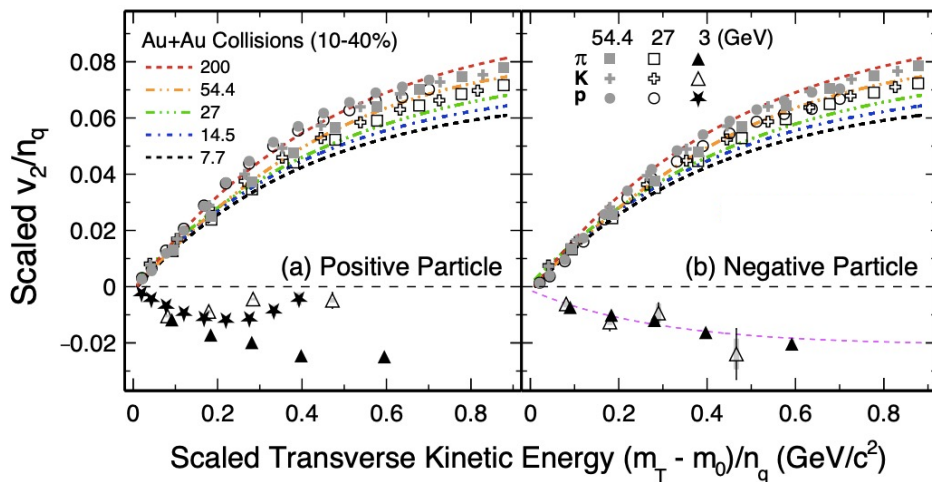
L.P. Csernai, J.I. Kapusta, L.D. McLerran, PRL **97** (2006) 152303

**Strong Interaction**  
 $\eta/s \sim 0.1$

- QGP matter in  $\sqrt{s_{NN}} \geq 39$  GeV collisions!
- Universal behavior for phase transition!



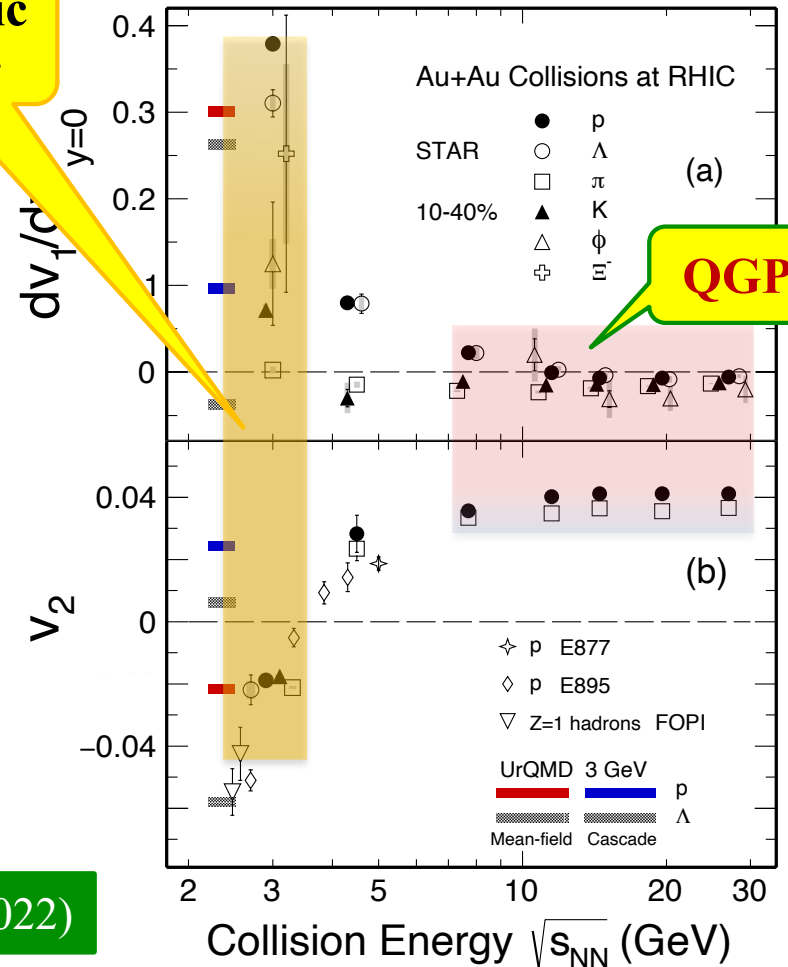
# Disappearance of Partonic Collectivity



**Hadronic Matter**

- At **3 GeV**, NCQ scaling is absent;
- Transport model calculations, with baryonic mean field, reproduce both  $v_1$  and  $v_2$  results;
- **hadronic interactions dominant!**

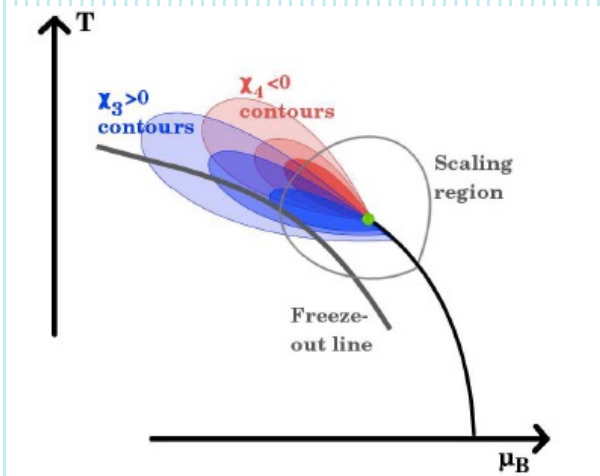
STAR: PLB827, 137003(2022)





*The emergent properties of QCD matter*

# Criticality



# Conserved Quantities (B, Q, S)

- 1) In strong interactions, baryons (B), charges (Q) and strangeness (S) are conserved;
- 2) Higher order moments/cumulants describe the shape of distributions and quantify fluctuations. They are sensitive to the correlation length  $\xi$ , phase structure;
- 3) Direct connection to theoretical calculations of susceptibilities.

Measured multiplicity  $N$ ,  $\langle \delta N \rangle = N - \langle N \rangle$

mean:  $M = \langle N \rangle = C_1$

variance:  $\sigma^2 = \langle (\delta N)^2 \rangle = C_2$

skewness:  $S = \langle (\delta N)^3 \rangle / \sigma^3 = C_3 / C_2^{3/2}$

kurtosis:  $\kappa = \langle (\delta N)^4 \rangle / \sigma^4 - 3 = C_4 / C_2^2$

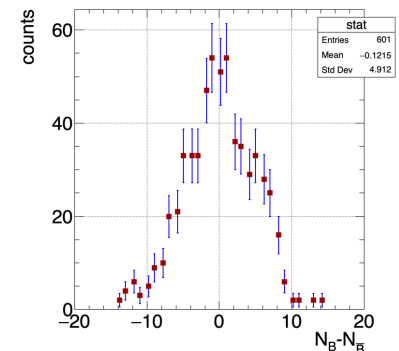
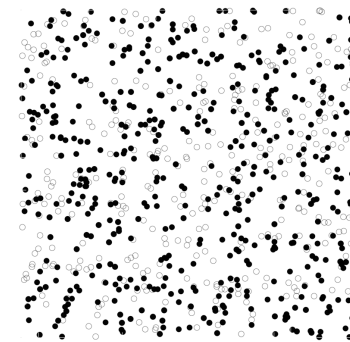
Moments, cumulants and susceptibilities:

2<sup>nd</sup> order:  $\sigma^2 / M \equiv C_2 / C_1 = \chi_2 / \chi_1$

3<sup>rd</sup> order:  $S \sigma \equiv C_3 / C_2 = \chi_3 / \chi_2$

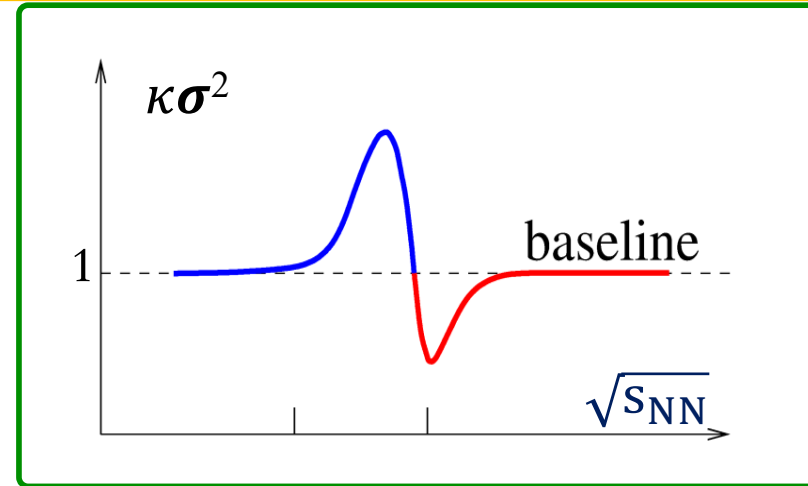
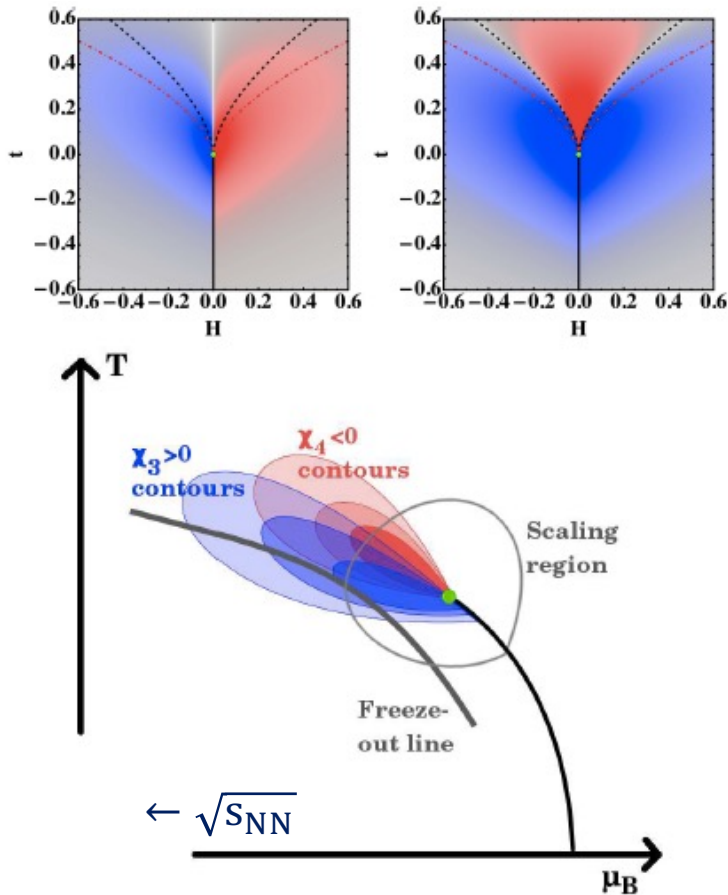
4<sup>th</sup> order:  $\kappa \sigma^2 \equiv C_4 / C_2 = \chi_4 / \chi_2$

Animation: A.Rustamov



INT 2008-2b : The QCD Critical Point

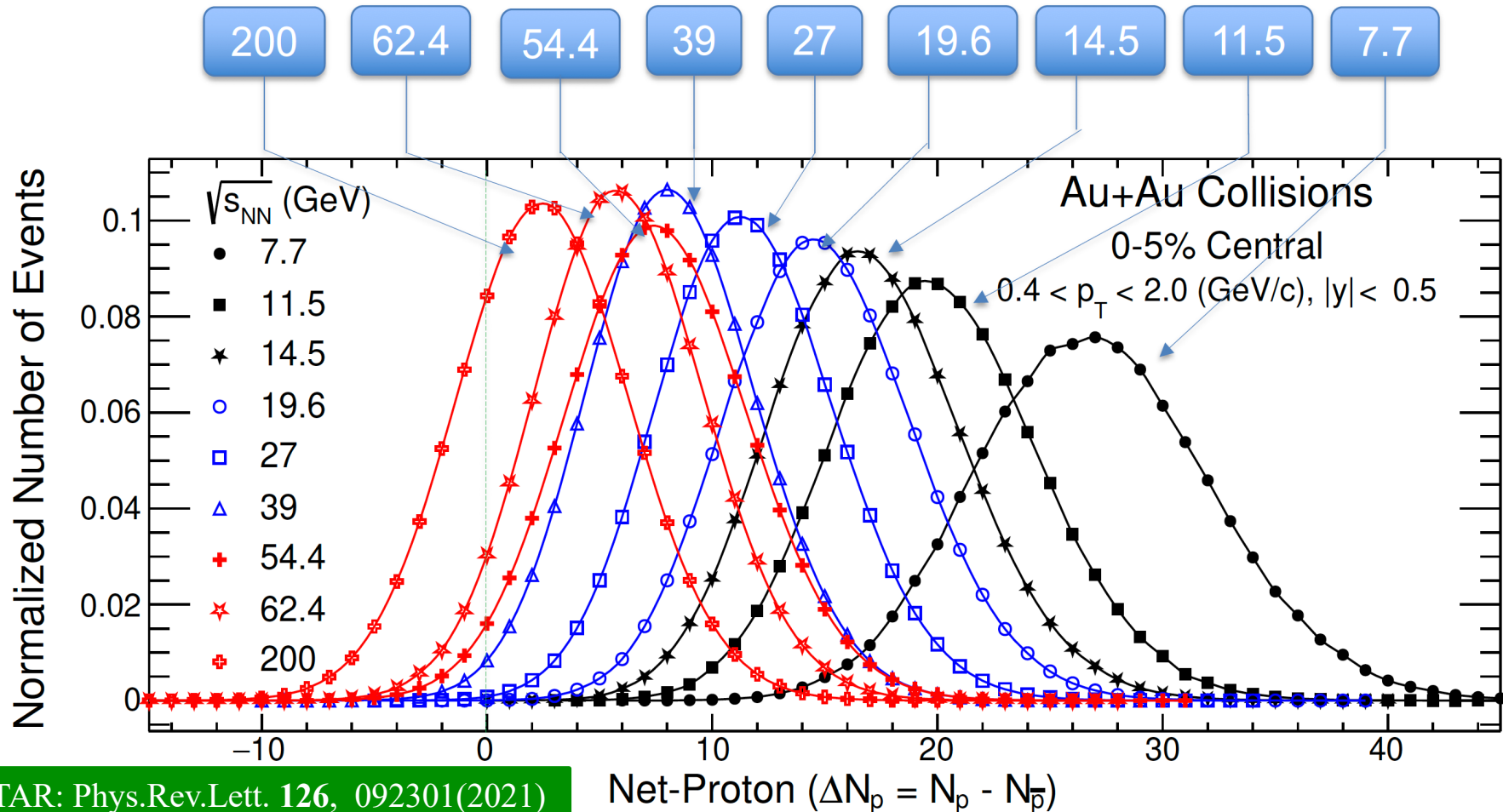
# Expectations for Models



- Characteristic “Oscillating pattern” is expected for the QCD critical point but **the exact shape depends on the location of freeze-out with respect to the location of CP**
- Critical Region (CR)

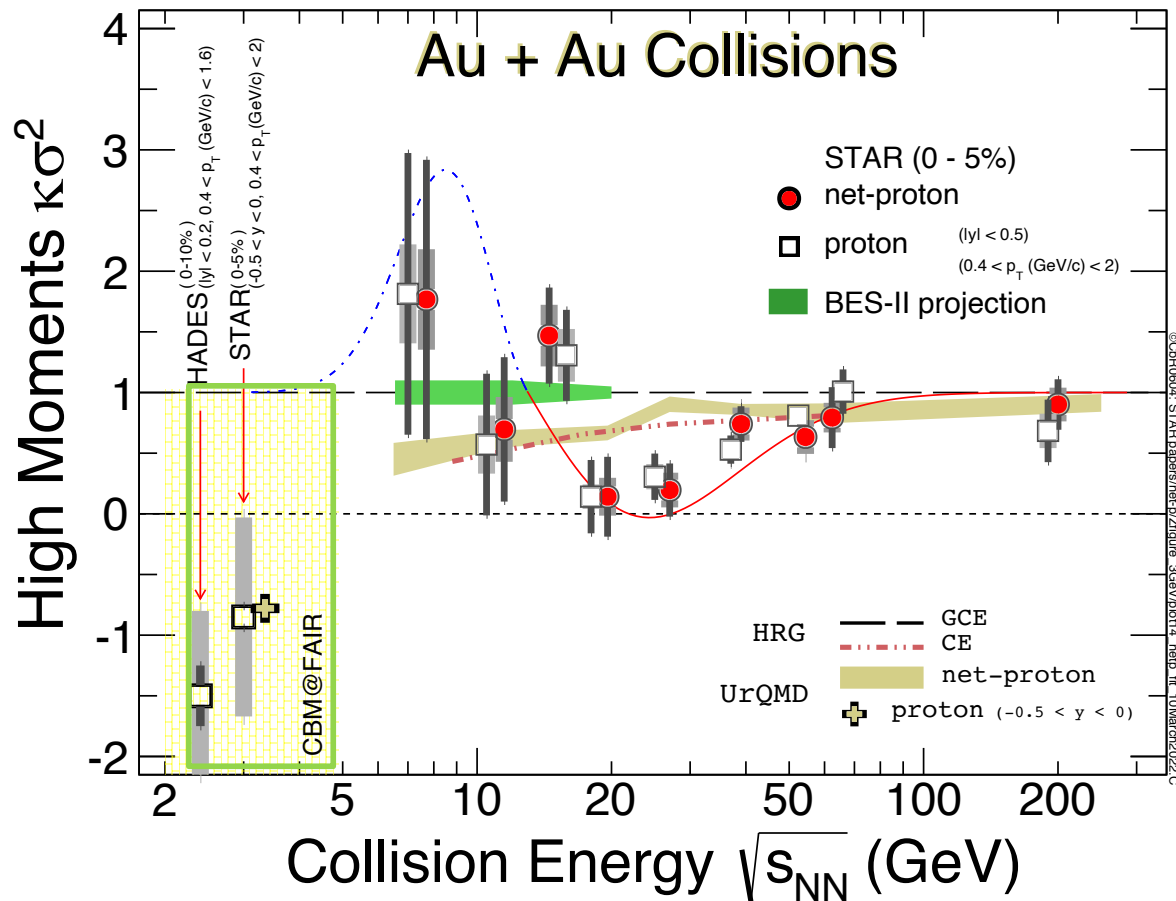
- M. Stephanov, PRL **107**, 052301(2011) - V. Skokov, Quark Matter 2012  
 - J.W. Chen, J. Deng, H. Kohyama, Phys. Rev. **D93** (2016) 034037

# Event-by-Event Net-Proton Distributions (raw)



STAR: Phys.Rev.Lett. 126, 092301(2021)

# Energy Dependence of the Net-p $\kappa\sigma^2$

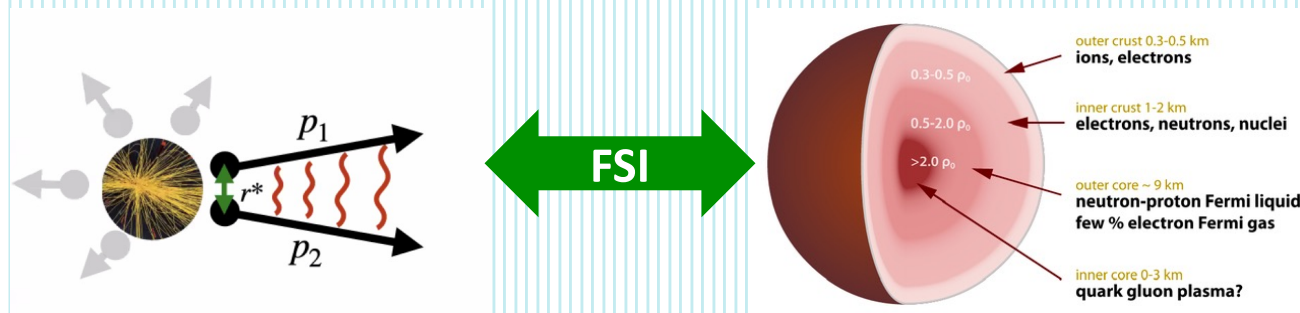


- 1) Non-monotonic energy dependence;
- 2) 3 GeV proton high moments data → **Hadronic interaction dominant!**
- 3) Energy gap between 3 and 7.7 GeV, important for **Critical Point search**

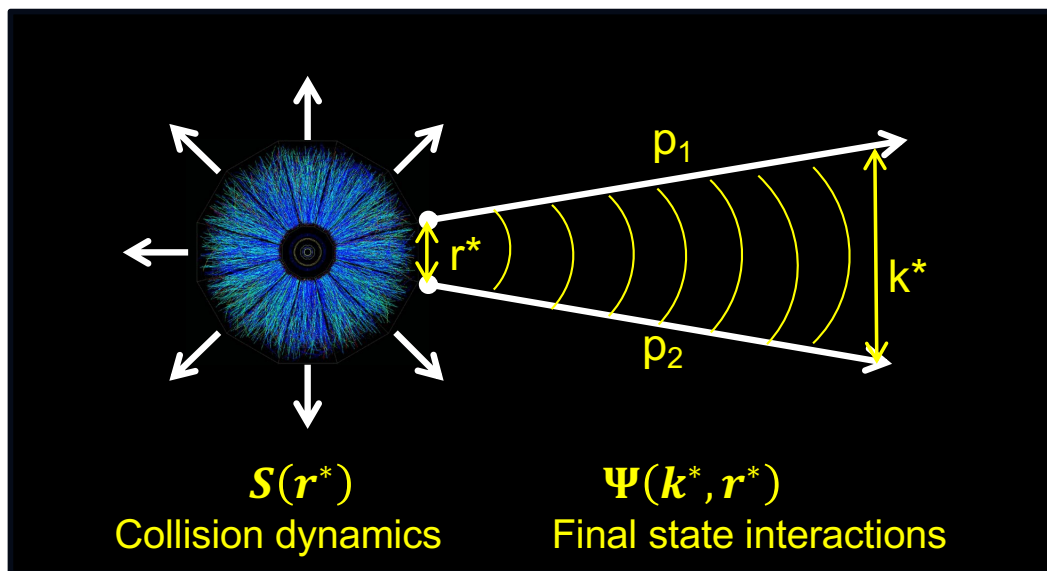
STAR: PRL126, 92301(2021)  
 PRL128, 202303(2022)  
 HADES: PRC102, 024914(2020)

*The emergent properties of QCD matter*

# Baryon Correlations



# Baryon Correlation Functions



## STAR:

(1) Meson HBT:  $\pi - \pi$ ,  $K - K$ ;

(2) Baryon correlations:

$p - p$		reference
$p - \Lambda$ ,	$p - \Xi^-$	YN
$p - d$ ,	$d - d$	NNN
$d - \Lambda$		YNN

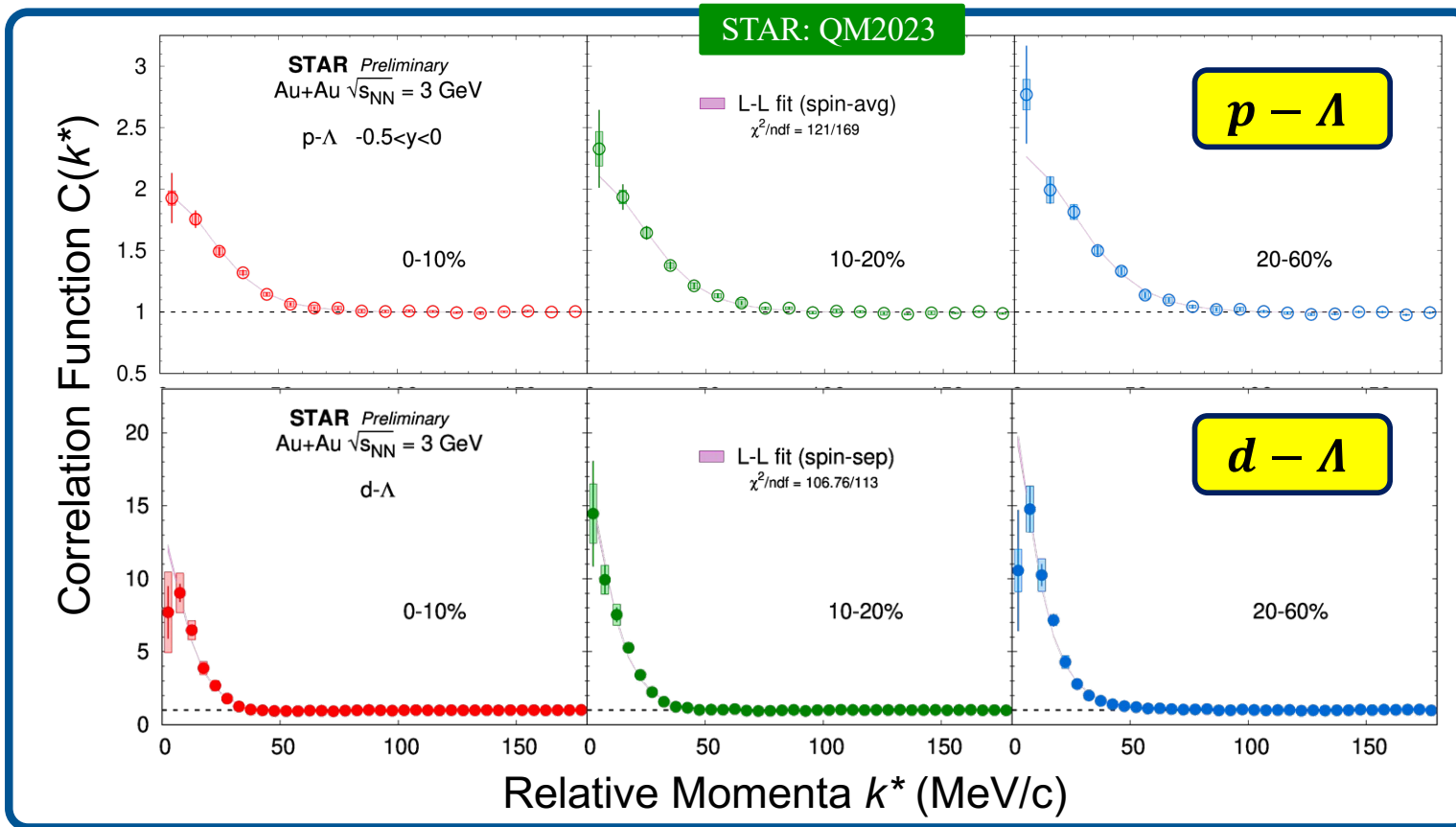
$$C_{the}(k^*) = \int d^3r^* S(r^*) |\Psi(r^*, k^*)|^2$$

Source  
Interaction potential

$$C_{exp}(k^*) = \lambda \frac{N_{same}(p_1, p_2)}{N(p_1)N(p_2)} \rightarrow \text{Source and FSI}$$

$$k^* = \frac{1}{2} |p_1^* - p_2^*|$$

# $p - \Lambda$ , $d - \Lambda$ Correlation Functions



## Corrections:

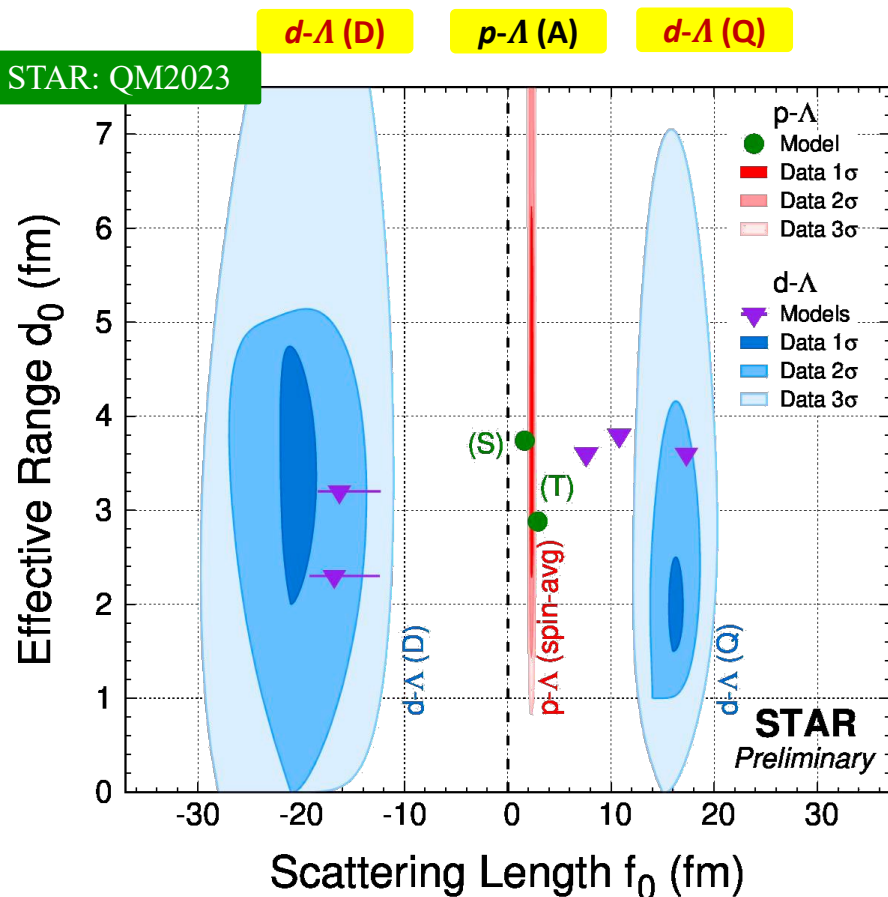
- 1) Track merging;
- 2) Track splitting;
- 3) Resonance decays;
- 4) Purity;
- 5) Momentum smearing;
- 6) Contribution of  ${}^3_{\Lambda}H$

## Acceptance:

- All:  $0.5 < y < 0$ ;
- $p$ :  $0.25 < p_T < 2$  (GeV/c);
- $d$ :  $0.25 < p_T < 3$  (GeV/c);
- $\Lambda$ :  $0.25 < p_T < 2$  (GeV/c)



# $d - \Lambda$ Correlation Function: Final State Interactions



Forward scattering amplitude:  $f(k^*) = \left\{ \frac{1}{f_0} + \frac{1}{2} d_0 k^{*2} - ik^* \right\}^{-1}$

$$p-\Lambda: \frac{1}{4} {}^1S_0 + \frac{3}{4} {}^2S_1$$

$$d-\Lambda: \frac{1}{3} {}^2S_{1/2} + \frac{2}{3} {}^4S_{3/2}$$

- 1) Scattering amplitude shrinks once s-quark hadrons are involved. For  $d-\Lambda$ , the spin-averaged  $f_0$  is very close to zero, evidence for interference between different spin states;
- 2) When  $f_0 < 0$ , bound state becomes available:  
 ${}^3\text{He}, {}^4\text{He}, {}^3_\Lambda\text{H}$ ;

**First experimental data on identified scattering length for spin-states!**

References: Hildenbrand, HWH, PRC100 (2019) 034002

# Outline

---

## 1) Introduction

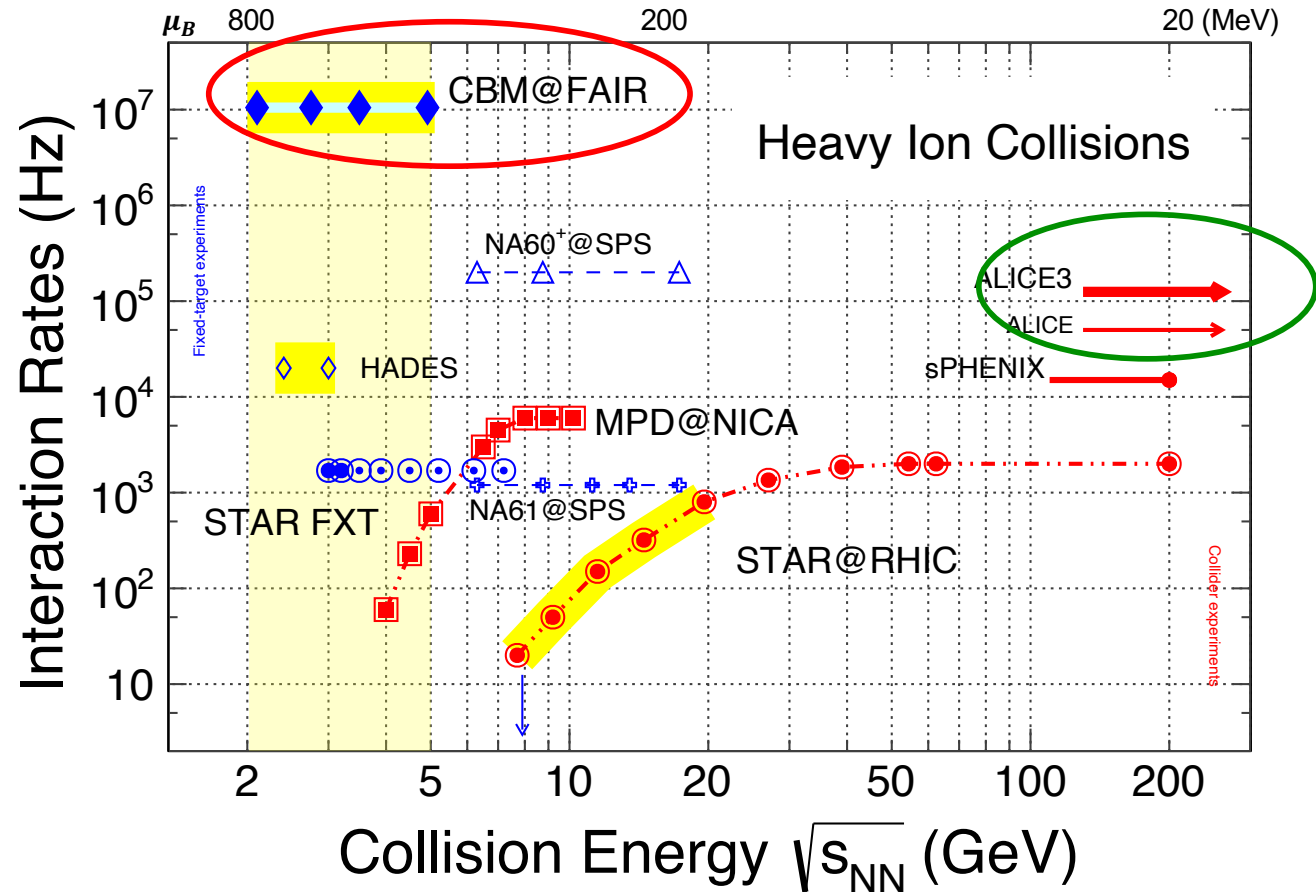
## 2) Results from RHIC BES Program

- i. Collectivity (EOS)
- ii. Criticality (EOS, CP)
- iii. Baryon Correlations (EOS, NN, YN)

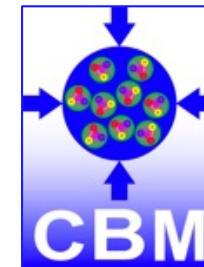
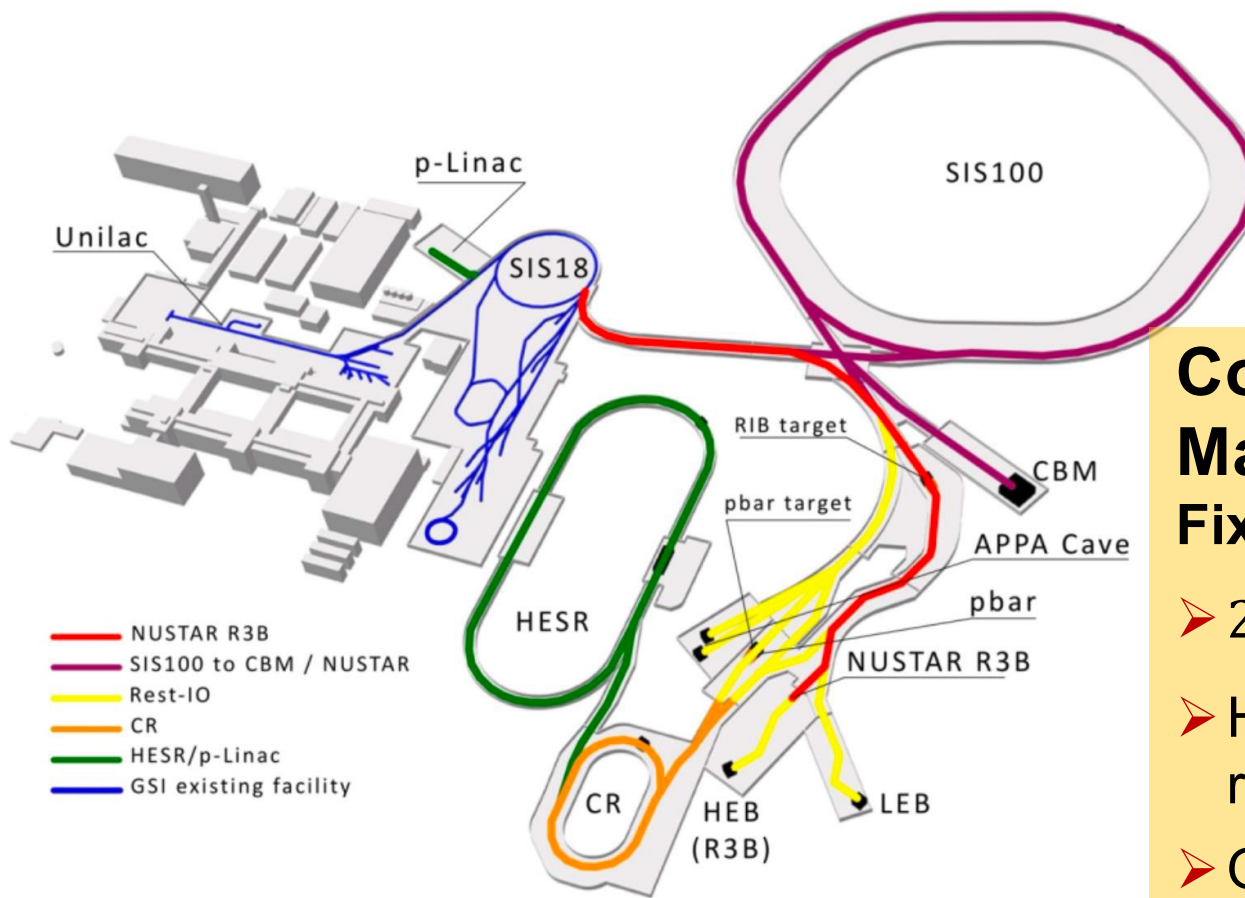
## 3) Outlook

# Future High Rates Experiments

- **ALICE3:**  $\mu_B \sim 0$  Properties of QGP!
  - **CBM:** Unprecedented rate capability and  $\mu_B \sim 800$  MeV
- 1) High order baryon fluctuation and correlation;
  - 2) 3D di-lepton spectra (collision centrality, pair mass and  $p_T$ );
  - 3) Hyper-nuclei production and Y-N interactions



# CBM Experiment at FAIR

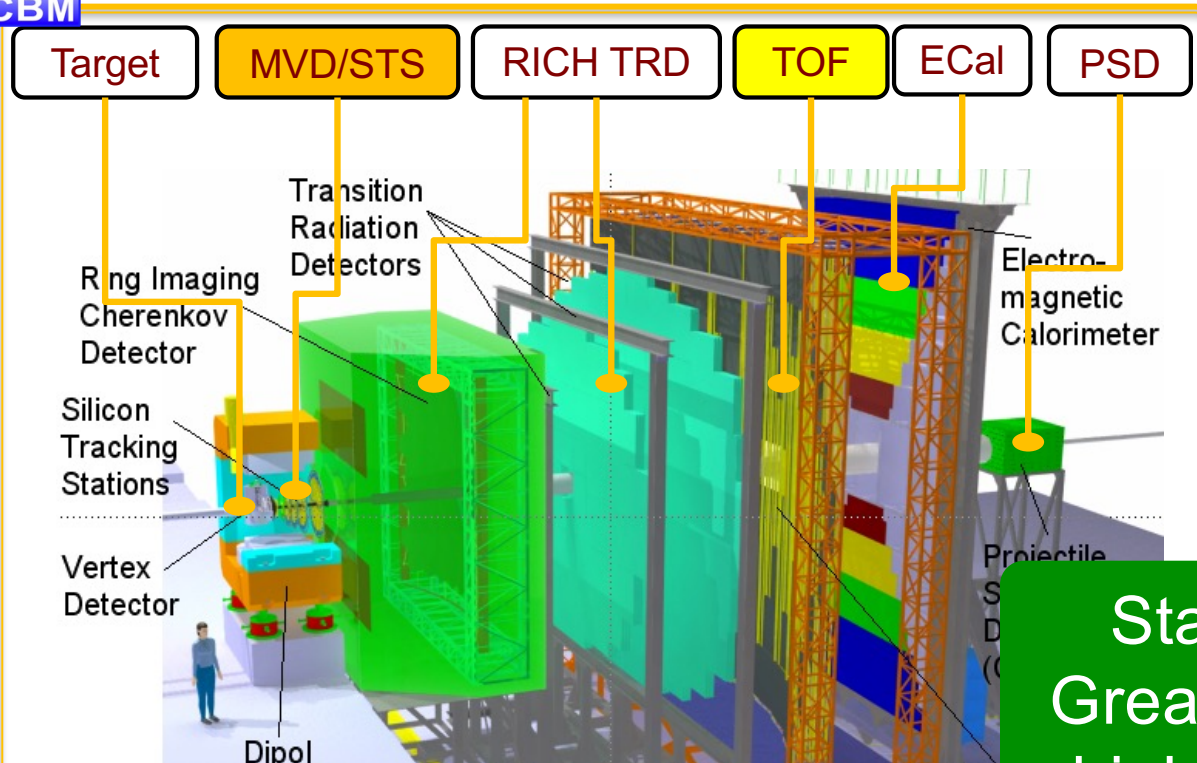
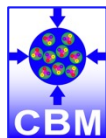


## Compressed Baryonic Matter (CBM)

Fixed-target experiment:

- $2.4 < \sqrt{s_{NN}} < 4.9$  GeV
- High intensity & collision rates up to 10MHz
- Operation starts in 2028

# CBM Experiment at FAIR



- FAIR: One of the brightest accelerator complexes
- Precision measurements at high baryon density region:
  - (i) Dileptons ( $e, \mu$ );
  - (ii) High order correlations;
  - (iii) Flavor productions ( $s, c$ )

State-of-the-art detector!  
Great discovery potentials at high baryon density region!

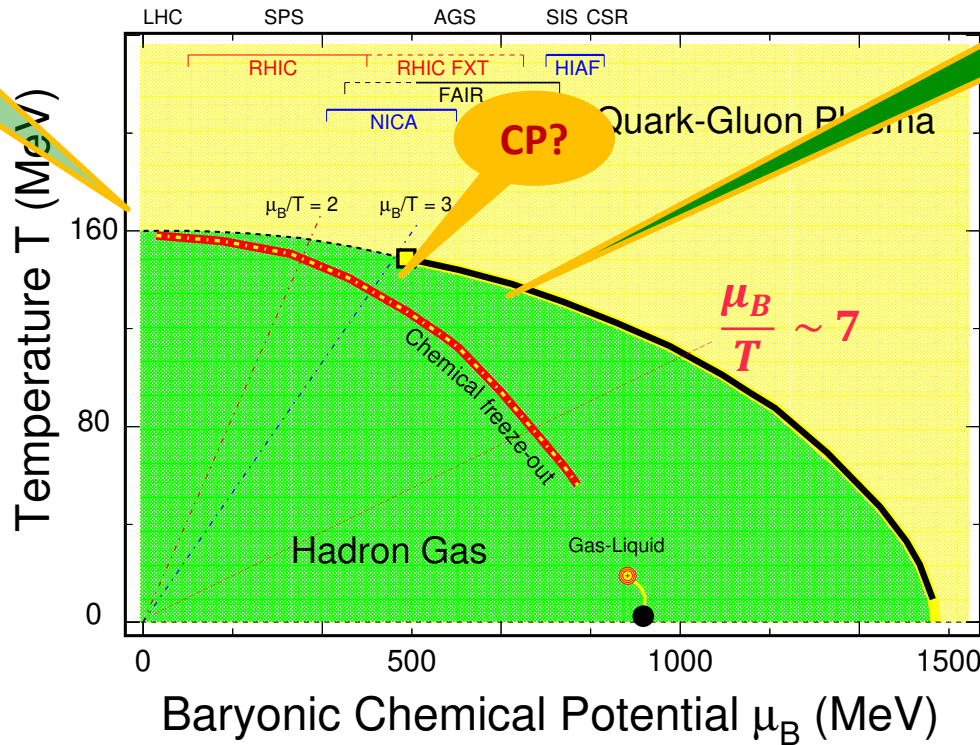
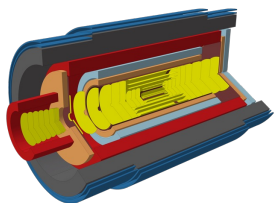
**A dream experiment!**

- 1) "The CBM Physics Book", B. Friman *et al.*, Lect.Notes Phys. **814**, 1 (2011)
- 2) "Challenges in QCD Matter Physics – The Scientific Program of the Compressed Baryonic Matter Experiment at FAIR", T. Abyazimov *et al.* Eur.Phys. J. **A53**, 3 (2017).

# Future Physics Programs

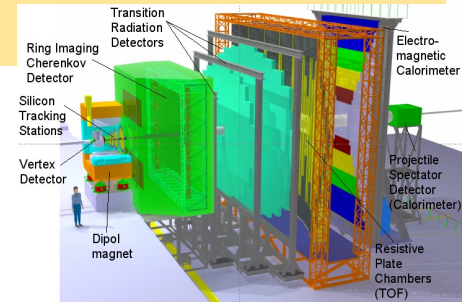
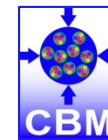
**ALICE**

- Properties of the smooth cross-over;
- p+p collisions;
- Full lepton distributions with **ALICE3**



**BES-II**  
**CBM (BES-III)**

- Critical point and phase boundary;
- Nuclear matter EOS at high baryon density;
- Y-N interactions, inner structure of compact stars



# Acknowledgements:

P. Braun-Munzinger, X. Dong, S. Esumi, V. Koch, XF. Luo, B. Mohanty, A. Pandav, K. Redlich, A. Rustamov, P. Senger, M. Stephanov, J. Stroth, I. Vassiliev, YJ. Zhou // BLUE: Theory // RED: Experiment //

Alexander von Humboldt Foundation



**Thank you very much for your attention!**

Dear Declan:

With physics insights and *real* leadership, you have made tremendous contributions to the physics programs at the STAR experiment: in the study of Collectivity, Criticality, Femtoscopy and BES and more. STAR is shining brightly *because of you*.

Congratulations all of the achievements!  
Best wishes for your new endeavors!

**Thank you!**

