# **On the Calculation of** *t* **in Diffractive VM production and DVCS**



 $V = \rho, \phi, J/\psi, \gamma$ 

#### *Thomas Ullrich EIC WG Meeting*

*October 8, 2020* 



 $p'$ ,  $A'$ 

# Simulations

- All Simulations with Sartre for e+Au
	- ‣ 18+110 GeV
	-
- bnonSat model<br>• Beam divergence
	- ‣ separately in x, y
	- ‣ separately for e and Au beam
	-
- taken from (pre)CDR<br>• Beam momentum spread
	- ‣ separately for e and Au beam
	- ‣ taken from (pre)CDR



In e+p we can follow the definition of *t*:

#### $t = (p_A - p_A)$ 2

pA is known (beam) and pA' is measured by forwards proton spectrometers (Roman Pots etc)



How well that ultimately works in terms of  $\sigma_t/t$  one has to see. the precision or for systematic cross-checks.



# In any case alternative methods should be considered either to improve

### e+A

In e+A we *cannot* measure pA':

- coherent: *t* kick not big enough to get heavy ions out of the beam pipe
- •incoherent: unlikely we can measure all fragments and reconstruct the whole ion and its momentum.

In general *t* cannot be measured w/o knowing pA' except in exclusive vector meson production: since 4-momenta from  $e, A, e'$  and  $V$  are known  $e + A \rightarrow e' + A' + V$ 





# $JA'$

# Method E

One can directly calculate *t* as: we call this method E (exact)  $t = (p_A - p_A)$  $2 = (p_V + p_{e'} - p_e)^2$ 

• In absence of any distortions (e.g. MC) this method delivers the true t



# Method E







- Beam divergence affects little:  $\sigma_t/t \sim 6\%$  to 0.5%
- 

#### EIC beam divergence The EIC beam momentum spread

• Beam momentum spread is devastating:  $\sigma_t/t \sim 15000\%$  to 103%

# Method E

Have to subtract large incoming and large outgoing momenta to get the "longitudinal part" of *t*. So a small error/smearing/inaccuracy in these has enormous effect on *t* momentum spread and the spread of the spread and act farge in

 $t = (p_V + p_e' - p_e)$ 2

Why does it fail:





### Effect on *dσ*/*dt*:

### Approximate method:

Rely only on the transverse momenta of the vector meson and the scattered electron ignoring all longitudinal momenta. Therefore beam momentum fluctuations do not enter the calculations. This method was extensively used at HERA in diffractive vector meson studies.

lighter vector mesons such as  $\phi$  and  $\rho$ . In what follows we refer to this method as method A.

• This formula is valid only for small *t* and small *Q2*. It also performs better for



$$
t = \left[\overrightarrow{p}_T(e') + \overrightarrow{p}_T(V)\right]^2
$$



# Method A

#### Downside:



- Even absence of any distortions (e.g. MC) this method us underestimating the true *t,*  although the difference is minimal
	- ‣ Offset is largest at Q2 =1-2 GeV2 with around 2% and decreases towards larger  $Q^2$  to 1% at  $Q^2$  = 9-10 GeV2 . The offset is absent for photoproduction (Q2 < 0.01 GeV2).
	- of 1.3%.



• For 1< Q<sup>2</sup> < 10 GeV<sup>2</sup> and including the offset we obtain  $\sigma_t$ /*t*resolutions (r.m.s.) of 10% t < 0.01 GeV2, 1.8 % at t = 0.10 GeV2, and 1.6% at t = 0.16 GeV2. In photoproduction we observe no t smearing except at the lowest  $t$  ( $t < 0.01$  GeV<sup>2</sup>)



# A New Approach: Method L

### Triggered by T. Lappi (Notes from March 18, 2020)



 $2, 3, -20$  $T$ houghts on measuring  $T$ ,  $M_y$  keep farget mass Romptel by T.U.'s presentation for ECC YR, elisemion with Hn) k  $k$  del's work in frame where  $91 = 0$  $e^{2k-k}$  and  $e^{2\pi k}$  This is a small  $m \geq m_{\gamma}$   $M_{\gamma}$  mortly I boat and rotation away pi from DIScollides detectasframe

p t a arders of magnitude are same as in  $A^{\pm} \equiv \frac{1}{\sqrt{r}} (A^{\circ} \pm A^3)$  detector

 $\frac{1}{2}$   $p = \left(\frac{m}{\hat{x}p^2}, \ \hat{P}^T, \hat{Q}_\perp\right)$ ,  $p' = \left(\frac{M_y}{\hat{x}(1-\hat{x}')p^2}, (1-\hat{x})p^T, -M\right)$  $y'' = g = (g^+, \frac{-Q^2}{2g^+, q_-} g^+$  v.m.  $\gamma^* = (g^+, \frac{M_v + g^+ h^+}{2g^+}, \gamma^+ \gamma^-)$ 

Basic DIS variables 2  $\frac{d^{2}p}{dx^{2}-y^{2}} = \frac{d^{2}m^{2}}{dx^{2}-y^{2}} = \frac{1}{w^{2}-w^{2}+Q}$  $29^{+}P$ 

 $W^{2} = (\rho_{1g})^{q} = m^{1} - Q^{1} + \partial P \cdot g = m^{1} - Q^{1} + \frac{Q^{1}}{X} = m^{1} + Q^{1} \frac{1-X}{X}$ From there we really need  $p^+P^-$ , there are the variables we think we know from the incoming beams and the scattered electron.  $P - q = \theta P - q^+ - \frac{\alpha m}{\theta P - q^+} = \left(\theta P - q^+\right) - \left(\theta P - q^+\right) \theta P - q^-\right.$  $P^{\dagger}q^+ - P^{\dagger}q^+ - P^{\dagger}q^0 = Q^{\dagger}q^0$  o.a.  $\partial P^{\dagger}q^+ = P^{\dagger}q^+P^{\dagger}q^0$  o.a.  $P^{\dagger}q^0$  o.a.  $= \int \frac{1}{\beta \rho} \int_{\gamma}^{2} t^{2} = 2 \int_{\gamma}^{2} \frac{1}{\beta} \left( 1 + \sqrt{1 + \frac{\alpha^{2} \omega^{2}}{(\rho \gamma)^{2}}} \right) \approx 2 \rho_{\gamma} \left( 1 + \frac{\alpha^{2} \omega^{2}}{(\rho \gamma)^{2}} \right)$ So  $\frac{2\beta g}{}^+$  a  $\frac{2\beta g}{}^+$  /  $\frac{1}{\alpha^4}$  ) Small target man correction  $\frac{1}{\alpha \alpha \sqrt{2}}$  lead moith  $\frac{1}{2}$  and  $\frac{1}{2}$ 

 $2.7 - 20$ Usually one roould elefine  $x_p = \frac{q \cdot (p-p^2)}{q \cdot p}$ . My  $\tilde{x}$  is an approximation:  $\frac{q \cdot (1-p^{1})}{q \cdot P} = \frac{1-p^{1-p} \cdot \tilde{x} - \frac{Q^{2}}{q^{1-p} \cdot (m^{2} - \frac{M\tilde{y}}{1-\tilde{x}})}{p^{1-p} - \frac{Q^{2}}{1-\tilde{x}^{2}} m^{2}} \approx \tilde{x}$  $\sqrt{p^2 + p^2 - \frac{a^2}{p^2 p^2} m^2}$   $\sim$  X, since  $9 + p$  $x \approx \frac{Q}{\partial q^2 P} - << 1$  and  $q^+ P$  is large x small  $Concentration$  of - momentum gives  $P^{-} = (l - \frac{N}{X})P^{-} + \frac{M\sqrt{4\pi}}{r} \Rightarrow \frac{N}{X} = \frac{M\sqrt{4\pi}}{r} \ll l$  $\lim_{n\to\infty}$  P is big,  $\int_1^1 z^2 e^{-z} dz$  only  $\int_1^1 z^3 e^{-z} dz$ One usually (at small x) user the eihonal approx, where  $g^+=g^+\rightarrow \widetilde{\chi}\approx \frac{mg}{2q+p} \approx X\frac{mg}{\omega^2}$ , but this cannot be used for  $\omega^2$ (this: neglecting target man and taking  $x$  =  $\frac{a^2}{\theta^2}$  or Should use  $w^2$  instead) Pomeron 4 momentum flow For both  $M_\gamma$  and  $t$  (exact kinematics  $v_1$  and  $\bot$  momente) it is crucial  $t_i$  understand the "pomeron" 4 - momentum. It has 4 wagnements, cleared it  $(-\Delta^+, \Delta^-, p)$ <sup>r</sup> g VM  $m_1$   $t = -2\sqrt{2} - n_1$ TU + quertiers is mely not include  $p \sim p'$  -  $p_1$  at  $\Delta$  in extraction of it det's calculate:  $\Delta = \frac{\overline{p} + \overline{p}}{2p^*} + \frac{\overline{p}}{2p^*} = P - (1 - \widetilde{x})P = \widetilde{x}P$  $\c{c}$ a bgave us  $\widetilde{x}$  a b

The ather component, rimilarly 2 options  $18.3 - 20$  $\Delta^{+}$  of  $f^{-}$   $\Delta^{+}$   $\Delta^{+}$   $\Delta^{0}$   $\Delta^{0}$   $\Delta^{0}$   $\Delta^{0}$   $\Delta^{0}$   $\Delta^{0}$ <sup>c</sup> d

If you only want to measure VM and not larget remnants Ci.e. no Roman Pats you are <sup>a</sup> and <sup>c</sup> This is TU's "exact method". To we what beggens we need to discuss reveral things - Target bereakup in general  $M_{\gamma}^{2}\geq m^{2}$  , with  $M_{\gamma}^{2}$  =  $m^{2}$  = coherent, and  $M_y$   $>$   $m^2$  incoherent det's parametrize  $M_y$  =  $m^2$  +  $\delta m^2$ . Sm in something we can constrain or even meaning with forward detectors. This affects the  $\Delta^+$ -momentum afthe pomerun:  $\Delta^+ \approx \frac{m^2}{\pi P} \left(1 + \frac{v}{X} + \frac{Sm^2}{m^2} + O(X^2 \frac{Sm^2}{m^2}) - l\right)$  $\frac{m^2}{2\beta^2}\left(x^2+\frac{\delta u}{u^2}+\cdots\right)$ - Eikonal approximation : one usually annumer, at ligh

energy, that  $f^+ = g^+$  this is the eitenal approximation Eg IP sat anumer this, and thus strictly speaking always has  $\Delta^+=0$  and it given only by transverse moments. the for the caherons process  $p^+$ -g<sup>+</sup> ~ m; and one aften neglects target man iarrections. But in fact we ree from  $c$  =  $d$  that this cannot be exactly true, but, even for Sm =0, we have  $\Delta^+ = \rho^+ \rho^+ \approx \frac{m}{\partial \rho^-} \hat{x}$ 

The breakup man My distribution depends on raft confinement male physics One could ask if it can be measured at ECC an HERA The problem is the converse of the above: nino an unprecise knowledge of My is mare combaining than the incoming elettren energy, it follows that g<sup>+</sup>omelp<sup>+</sup>, i.e. incoming, outgoing and decay leptons would need to be known extremely accurately to measure My from them. I think this is hopeless : you can only get to My with fund detectors meannring the breakup uplen.









2 Measuring My

Method is based on method E but overcomes several of its shortcomings. It is, however, strictly only applicable for coherent events. While in method E we are not using any information about the target nucleus at all, in method L we make use of the fact that the longitudinal momentum has to get transferred to the target due to 4-momentum conservation.

- Electron beam energy : if there is a dispersion in the electron beam energy, this leads to an unserlainty in g+, likewise experimental uncertainties in measuring k and p<sup>+</sup> Chrom V.M. desay leptous). There are small effects, but they are important, because they are correction, to A<sup>+</sup> which is very very mall.

The ather component  $\Delta$  is earies. Even without detecting  $P'$ it is  $\Delta = \frac{M_{v} + p_{\perp}}{2p^{4}} + \frac{Q^{3}}{2q^{4}}$  $\overline{a_{p1}}$  +  $\overline{a_{q1}}$  . Here, unlike in  $\Delta^{+}$  =  $g^{+}$ there is no concellation between different sign terms. Thus we can here safely replace  $\rho^+ \propto \rho^+$  and get  $\Delta^{-} \propto \frac{\partial^{2}}{\partial \rho^{4}} \left( 1 + \frac{M_{\nu} + M_{\nu}}{\rho^{2}} \right) = \chi \rho^{2} \left( 1 + \frac{\chi^{2} m^{2}}{\rho^{2}} \right)^{1/2} \left( 1 + \frac{\chi^{2} M_{\nu}}{\rho^{2}} \right)$  $n$ egligible, unless  $\omega$  =  $o$ Now the longitudinal contribution to t is (1 cancels)  $2\Delta^+\Delta^-$  =  $m^2 \times (\tilde{\chi} + \frac{\delta m^2}{m^2} + ...)$   $(1 + \frac{M_v \cdot \gamma_i}{\alpha^2})$  $\left(\text{recall } \tilde{\chi} = \frac{M_v^3 + p_{\perp}^3}{2p^2p^-} \approx \frac{M_v^3 + p_{\perp}^7}{2p^2p^-} \approx \frac{M_v^3 + p_{\perp}^3}{Q^2} \times \right)$ For phateproduction we write in terms of  $W \triangleq 3g^{4/3}$  $\tilde{x} = \frac{mv^2 + 1}{w^2}$ ,  $\Delta = \frac{mv^2 + 1}{2g^2} = \frac{mv^2 + 1}{w^2} \Delta$  and  $34\Delta^4$  =  $m^4$   $\left(\frac{M_v^4 M_v^2}{W^4} + \frac{5m^2}{m^4} + \right) \frac{M_v^4 M_v^2}{W^2}$ 

To summarize how to measure  $t$ 

An uncertainty in the beam electron k<sup>+</sup> propagates into an uncertainty in the pameron  $\Delta^+$ . Even a small uncertainty is serious, because this quantity is very mall:  $\Delta^+ \approx \frac{m}{3p} - \chi$ for caherent production.

We have to veto incoherent events anyway. If we can turn this into an upper limit em the target fragment man  $M_{y}^{\epsilon}$  =  $m^{2}$  +  $\delta m^{2}$  with a mall  $\delta m^{2}$ , we can turn this into an upper limit on the longitudinal contribution to  $t \t 3\Delta^{4} \Delta^{-} = m^{2} \times (\tilde{\chi} + \frac{\partial m^{-}}{m^{2}} + ...) \left( 1 + \frac{M_{\nu} + \eta_{L}}{Q^{2}} \right)$ So even <sup>a</sup> relatively inaccurate measurement of My can give a better *constraint* on  $t$  than knowing  $k^+$ 

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as coherent  $\implies$  Important analysis/cross-check tool

• For coherent events this essentially indicates the failure of method E due to beam and detector smearing effects or that the event was mischaracterized



- How the method works
	- ▶ Calculate p of outgoing A':  $p_{A'} = p_A (p_V + p_{e'} p_e)$
	- Express and correct the outgoing nucleus

• 
$$
p_{A'}^+ = E_{A'} + p_{z,A'}
$$
  
\n•  $p_{T,A'}^2 = p_{x,A'}^2 + p_{y,A'}^2$   
\n•  $p_{A'}^- = (M_A^2 + p_{T,A'}^2)/p_{A'}^+$  where  $p_{A'}^-$  is now  
\nThe corrected 4-momentum of the out  
\n $p_{A'}^{\text{corr}} = \left[ p_{x,A'}, p_{y,A'}, (p_{A'}^+ - p_{A'}^-)/2, (p_{A'}^+)\right]$ 

and pz,A' simultaneously.

‣ Now simply: *t*  $p_{A} - p_{A'}^{\text{corr}}$ 2

$$
-(p_V + p_{e'} - p_e)
$$
  
cleus in light cone variables:

 $\Phi(p_{A'}^T = (M_A^2 + p_{T,A'}^2)/p_{A'}^+$  where  $p_{A'}^-$  is now modified by using the true mass  $M_A^2$ . outgoing nuclei is now *A*′ +*p*<sup>−</sup>  $\overline{A'}$ )/2

▶ In short, you are using the true invariant mass of the nucleus to compensate the smearing in the larger component of the electron 4-momentum by modifying  $E_{A}$ 





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#### All beam effects on



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#### Method L left column is for photoproduction and the right for 1 *< Q*<sup>2</sup> *<* 10 GeV<sup>2</sup>. Shown, from top to bottom are *p* T**urbell p** *p*<sub>T</sub> is the scattered electron. Right: Same for , and the scattered electron. Right: Same for , and the scattered electron. Right: Same for  $\alpha$





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![](_page_13_Picture_2.jpeg)

#### • Method L with beam effects and nominal  $p_T$  resolution

![](_page_14_Picture_13.jpeg)

![](_page_14_Figure_2.jpeg)

![](_page_14_Picture_660.jpeg)

#### Method L and A give similar t resolutions

![](_page_14_Picture_7.jpeg)

# Summary

- Method E fails in the presence of beam momentum resolution
- Method L is an extension and a huge improvement
	- ‣Only applicable for coherent events
	- ‣We confirmed in simulations that all results obtained by method L for coherent processes are identical or very similar to that of method A in the studies discussed below.
- Ultimately, in the actual analysis once the EIC is realized, both methods (A and L) should be carefully compared and studied.
	- ‣For coherent processes method L is likely the better choice as it does not rely on any approximations
	- ▶ For incoherent processes method A is the only option available

![](_page_15_Picture_13.jpeg)

![](_page_15_Picture_14.jpeg)