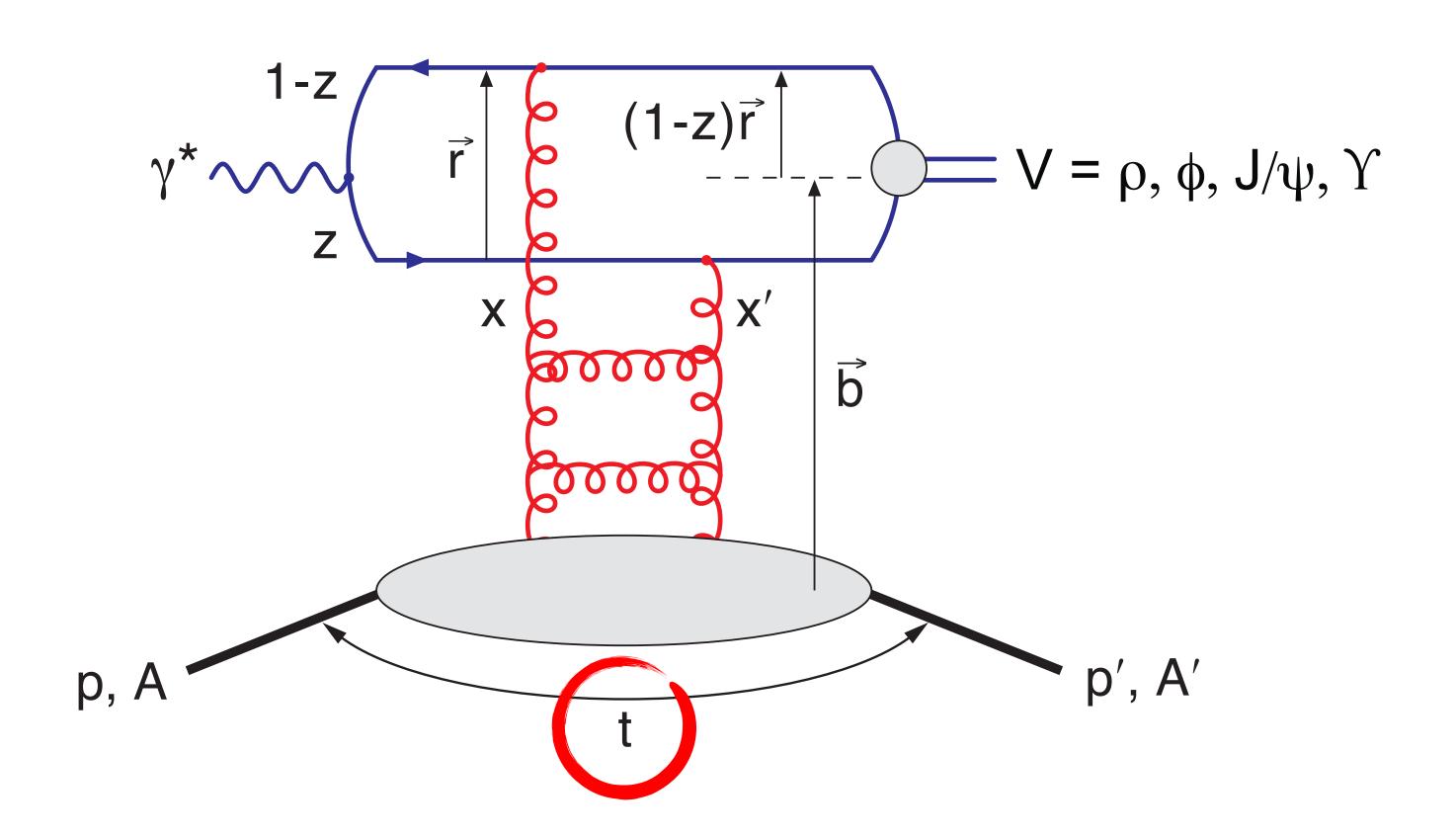
On the Calculation of *t* in Diffractive VM production and DVCS



Thomas Ullrich EIC WG Meeting

October 8, 2020



Simulations

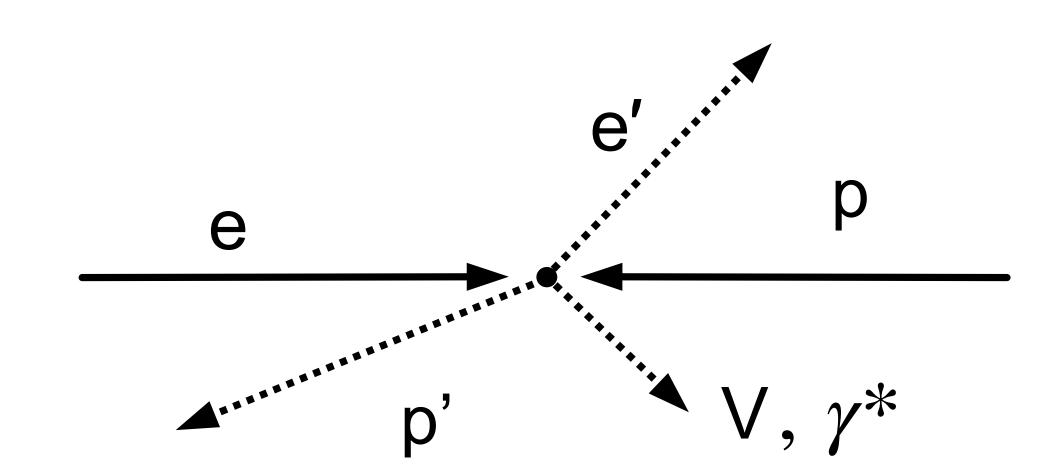
- All Simulations with Sartre for e+Au
 - ▶ 18+110 GeV
 - bnonSat model
- Beam divergence
 - separately in x, y
 - separately for e and Au beam
 - taken from (pre)CDR
- Beam momentum spread
 - separately for e and Au beam
 - taken from (pre)CDR

e+p

In e+p we can follow the definition of t:

$$t = (p_A - p_{A'})^2$$

 p_A is known (beam) and $p_{A'}$ is measured by forwards proton spectrometers (Roman Pots etc)



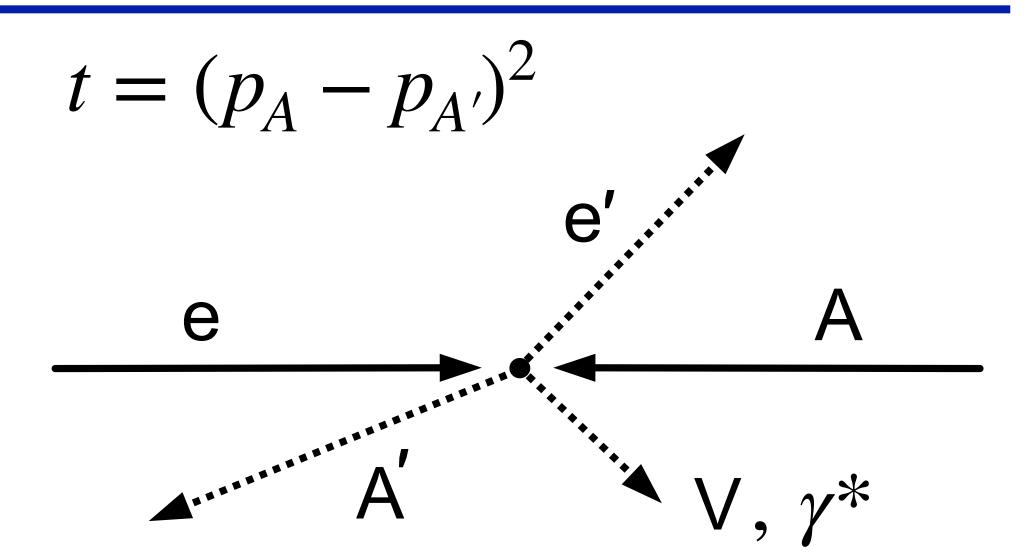
How well that ultimately works in terms of σ_t/t one has to see.

In any case alternative methods should be considered either to improve the precision or for systematic cross-checks.

e+A

In e+A we cannot measure pA':

- coherent: t kick not big enough to get heavy ions out of the beam pipe
- incoherent: unlikely we can measure all fragments and reconstruct the whole ion and its momentum.



In general t cannot be measured w/o knowing $p_{A'}$ except in exclusive vector meson production:

$$e + A \rightarrow e' + A' + V$$

since 4-momenta from e, A, e' and V are known

Method E

One can directly calculate t as:

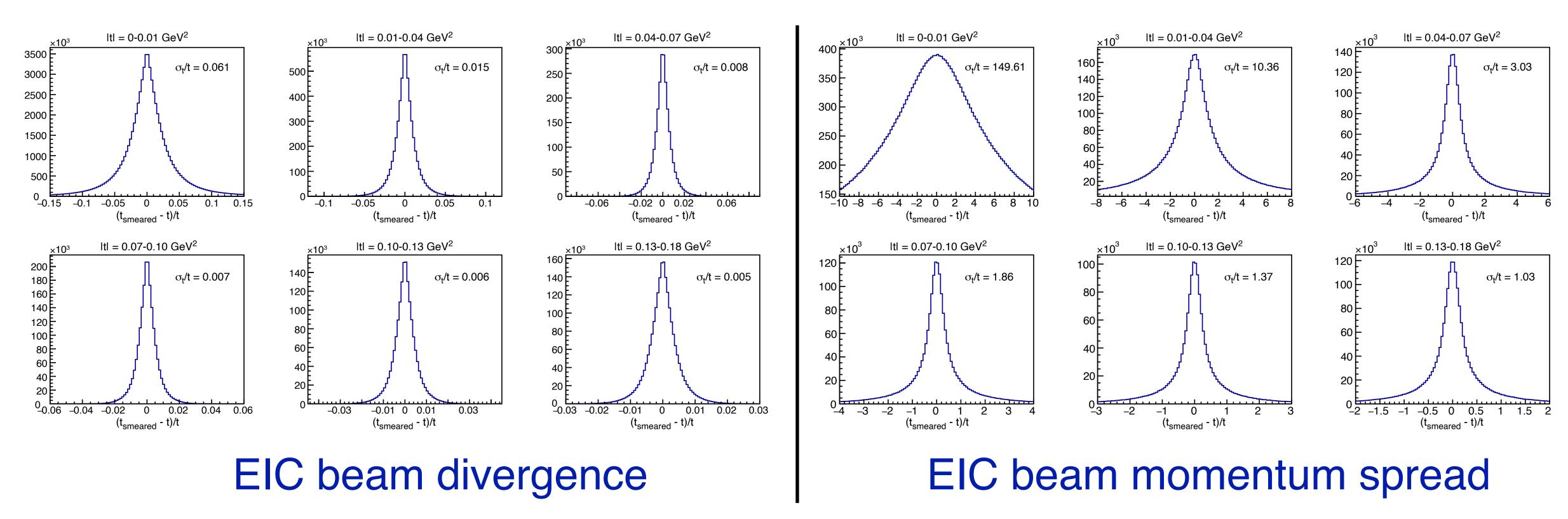
$$t = (p_A - p_{A'})^2 = (p_V + p_{e'} - p_e)^2$$

we call this method E (exact)

• In absence of any distortions (e.g. MC) this method delivers the true t

Method E

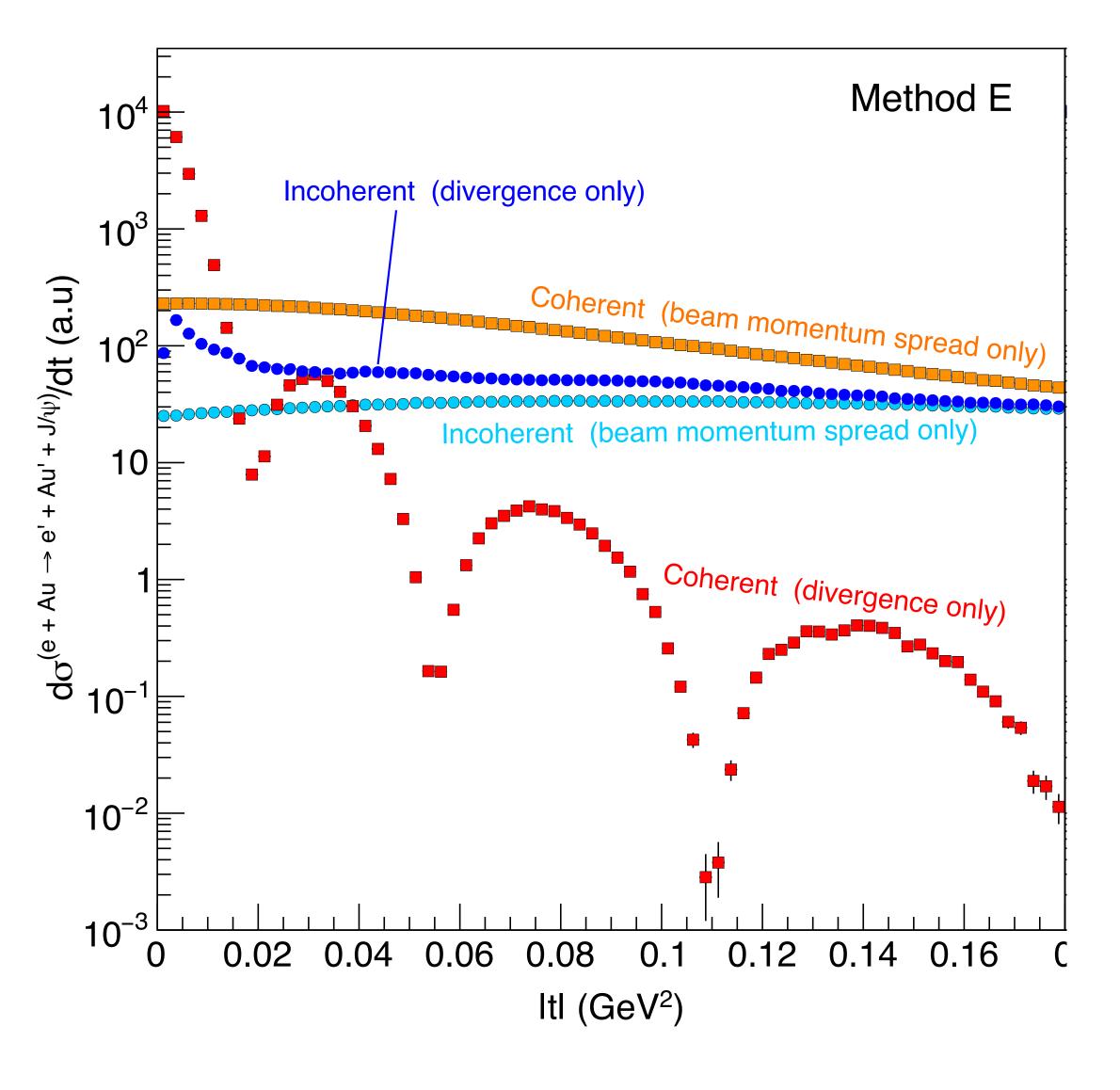
Sensitivity to beam effects: $\sigma_t/t = (t_{\rm measured} - t_{\rm true})/t_{\rm true}$



- Beam divergence affects little: $\sigma_t/t \sim 6\%$ to 0.5%
- Beam momentum spread is devastating: $\sigma_t/t \sim 15000\%$ to 103%

Method E

Effect on $d\sigma/dt$:



$$t = (p_V + p_{e'} - p_e)^2$$

Why does it fail:

Have to subtract large incoming and large outgoing momenta to get the "longitudinal part" of *t*. So a small error/smearing/inaccuracy in these has enormous effect on *t*

Method A

Approximate method:

Rely only on the transverse momenta of the vector meson and the scattered electron ignoring all longitudinal momenta. Therefore beam momentum fluctuations do not enter the calculations. This method was extensively used at HERA in diffractive vector meson studies.

$$t = \left[\overrightarrow{p}_T(e') + \overrightarrow{p}_T(V)\right]^2$$

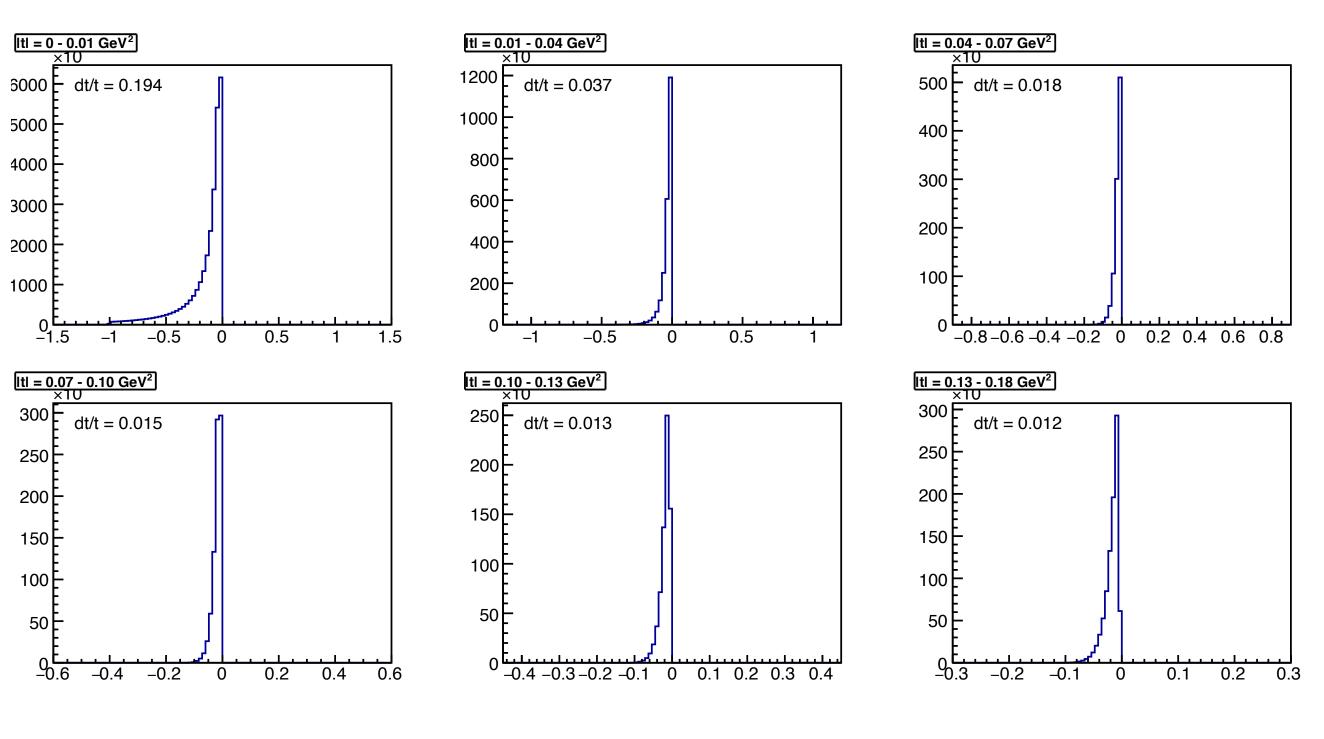
• This formula is valid only for small t and small Q^2 . It also performs better for lighter vector mesons such as ϕ and ρ . In what follows we refer to this method as method A.

Method A

Downside:

- Even absence of any distortions (e.g. MC) this method us underestimating the true t, although the difference is minimal
 - ▶ Offset is largest at Q² =1-2 GeV² with around 2% and decreases towards larger Q² to 1% at Q² = 9-10 GeV². The offset is absent for photoproduction (Q² < 0.01 GeV²).</p>

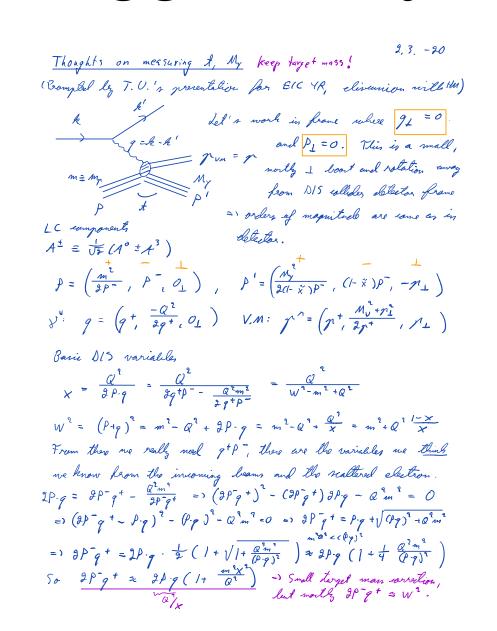
$1 < Q^2 < 10 \text{ GeV}^2$

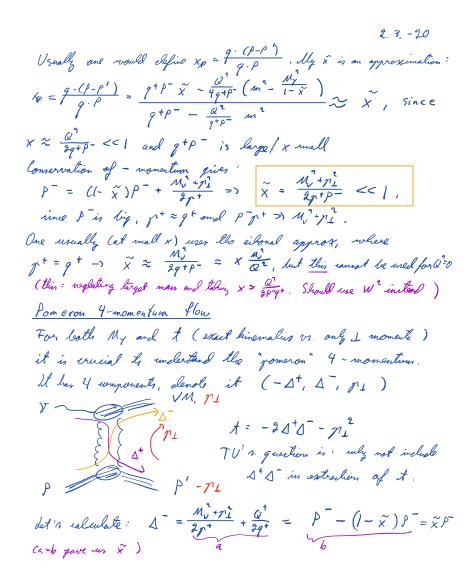


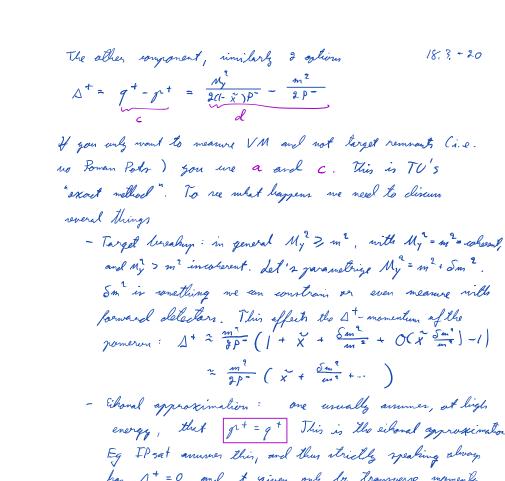
For 1< Q² < 10 GeV² and including the offset we obtain σ_t/t resolutions (r.m.s.) of 10% t < 0.01 GeV², 1.8 % at t = 0.10 GeV², and 1.6% at t = 0.16 GeV². In photoproduction we observe no t smearing except at the lowest t (t < 0.01 GeV²) of 1.3%.

A New Approach: Method L

Triggered by T. Lappi (Notes from March 18, 2020)







energy, that $p^+ = q^+$ This is the eibonal approximation. Eg IP sat answers this, and thus strictly speaking always has $\Delta^+ = 0$ and it given only by transverse momente. Also for the sakerent process $p^+ - q^+ \sim m_{\chi}^2$ and one after neglects target man varietions.

But in fact we see from C = d that this samuel be exactly true, but, even for $\delta m^0 = 0$, we have $\Delta^+ = q^+ p^+ \cong \frac{m^0}{2P^-} \times 0$

- Electron beam energy: if there is a digerision in the electron beam energy, this leads to an unvertainty is g^+ , lihewise experimental uncertainties in measuring k' and p^+ (from V.M. cleray leptons). There are small effects, but they are important, because they are servedion, to Δ^+ which is very very small.

The atlee companent Δ^- is easies. Even without detecting P' it is $\Delta^- = \frac{M_V^2 + p_1^2}{2p^+} + \frac{Q^2}{2q^+}$. Here, unlike in $\Delta^+ = q^+ - p^+$, there is no cancellation between different sign terms. Thus

it is $\Delta = \frac{1}{2p^{+}} + \frac{1}{2q^{+}}$. Here, unlike in $\Delta^{+} = q^{+} - p^{+}$, there is no concellation between eliflerent sign terms. Thus we can here cafely replace $p^{+} \times q^{+}$ and get $\Delta^{-} \propto \frac{Q^{2}}{2q^{+}} \left(1 + \frac{Mv^{+} + N^{2}}{Q^{2}}\right) = \times P^{-} \left(1 + \frac{x^{2}m^{2}}{Q^{2}}\right)^{-1} \left(1 + \frac{Mv^{+} + N^{2}}{Q^{2}}\right)^{-1} \left(1 + \frac{Mv^{+} + N^{2}}{Q^{2}}\right)^{-1}$ Now the longitudinal contribution to t is $(P^{-}$ cancels) $2\Delta^{+}\Delta^{-} = m^{2} \times \left(\tilde{\chi}^{-} + \frac{\delta m^{2}}{m^{2}} + ...\right) \left(1 + \frac{Mv^{+} + N^{2}}{Q^{2}}\right)^{-1}$ (recall $\tilde{\chi}^{-} = \frac{Mv^{+} + N^{2}}{2q^{+}P^{-}} \approx \frac{Mv^{+} + N^{2}}{Q^{2}} \times \frac{Mv^{+} + N^{2}}{Q^{2}}$ For stateproduction we write in terms of $W^{2} \approx 2q^{+}P^{-}$ $\tilde{\chi}^{-} = \frac{Mv^{+} + N^{2}}{W^{2}} + \frac{Mv^{+} + N^{2}}{Q^{2}} = \frac{Mv^{+} + N^{2}}{W^{2}} = \frac{Mv^{+} + N^{2}}{W^{2}}$ $\frac{2}{2}\Delta^{+}\Delta^{-} = m^{2} \left(\frac{Mv^{+} + N^{2}}{W^{2}} + \frac{\delta m^{2}}{m^{2}}\right) + \frac{Mv^{+} + N^{2}}{W^{2}}$

To summarize how to measure t

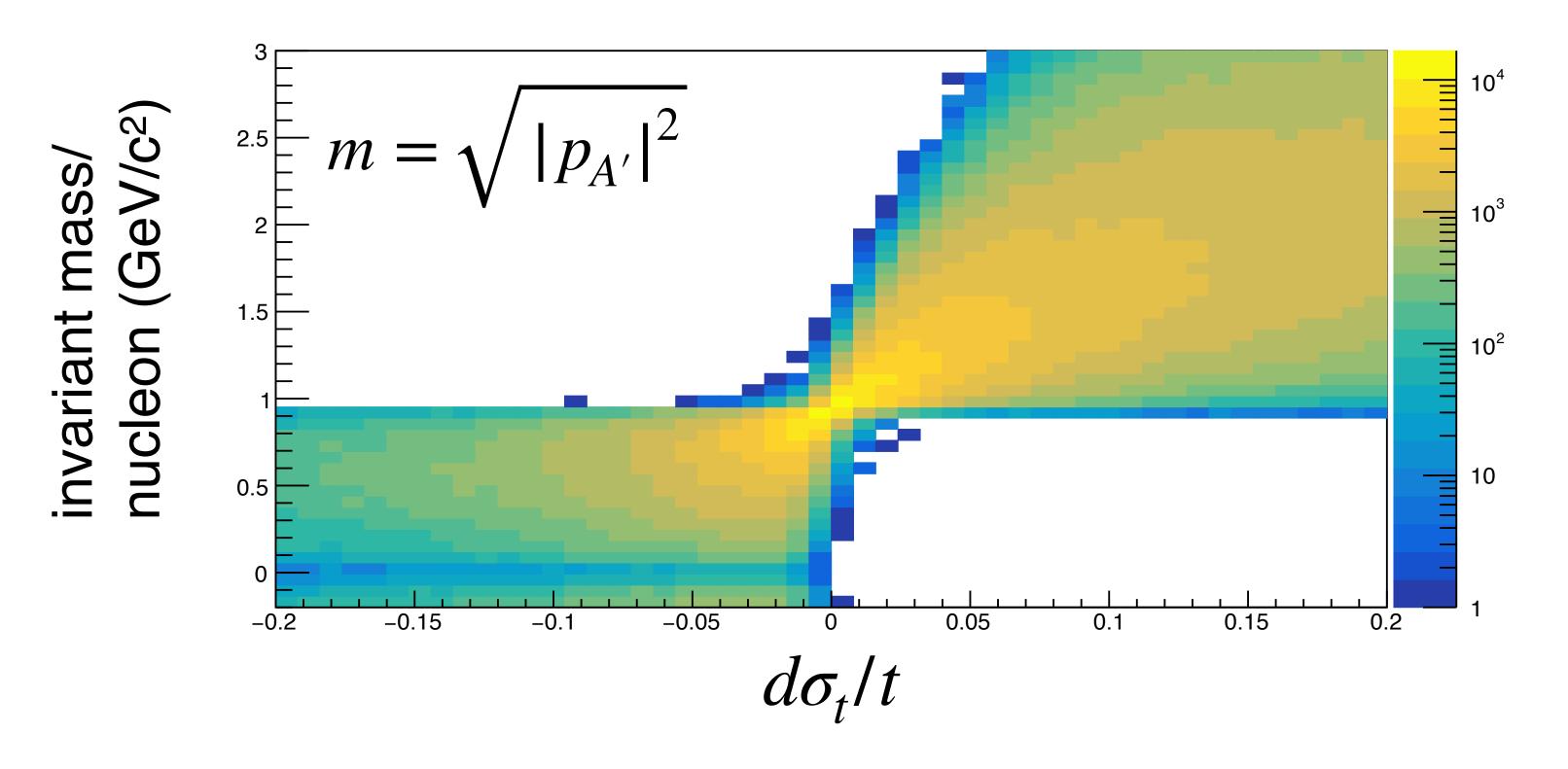
- In uncertainty in the beam electron k^+ propagates into an uncertainty in the pameron Δ^+ . Even a small unorbinity is serious, because this quantity is very small: $\Delta^+ \approx \frac{m^2}{2\,p^-}\,\tilde{\chi}$ for whereat production.
- We have to veto incoherent events anyway. If we can turn thin into an upper limit on the target fragment man $M_y^2 = m^2 + \delta m^2$ with a mall δm^2 , we can turn this into an upper limit on the longitudinal contribution to $\delta M_y^2 = m^2 \times (\tilde{\chi} + \frac{\delta m^2}{m^2} + ...) \left(1 + \frac{M_y^2 + \eta_1^2}{G^2}\right)$. So even a relatively inaccurate measurement of M_y can give a better constraint on $\delta M_y^2 = M_y^2$.

Measuring My

The bereaky man My distribution depends on roft confinement nale physics. One would early if it can be measured at E(C an HERT. The problem is the converse of the above: into an unprecise knowledge of My is more constraining than the incoming eletron energy, it follows that q+oned p+, i.e. incoming, outgoing and cleray leptons would need to be known extremely accurately to measure My from them.) Think this is hopeless: you can only get to My with find delectors measuring the breakup uplens.

Method is based on method E but overcomes several of its shortcomings. It is, however, strictly only applicable for coherent events. While in method E we are not using any information about the target nucleus at all, in method L we make use of the fact that the longitudinal momentum has to get transferred to the target due to 4-momentum conservation.

• Calculate A' 4-momentum: $p_{A'} = p_A - (p_V + p_{e'} - p_e)$



method E

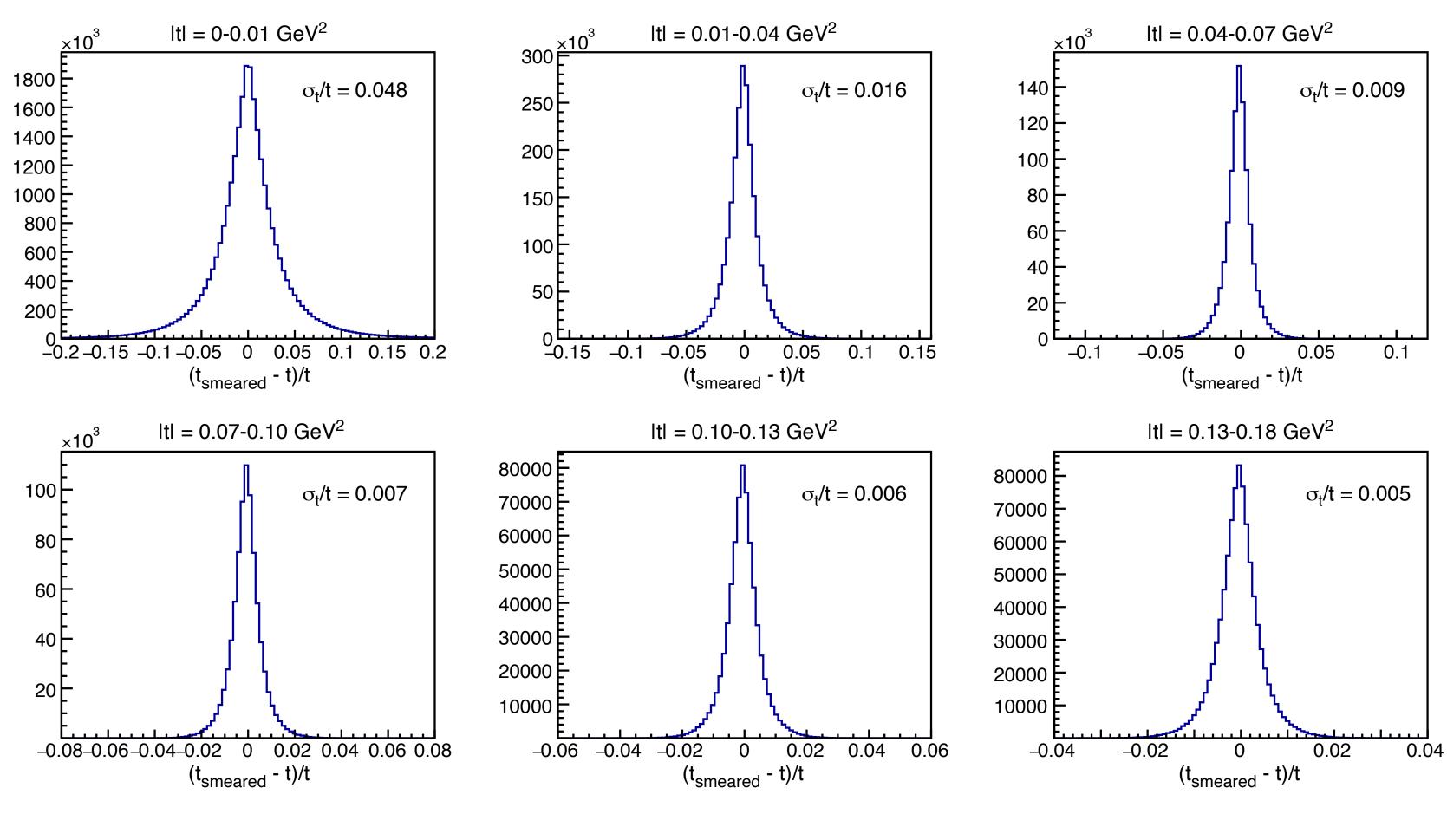
 Any smearing of the longitudinal momentum difference will change the invariant mass of the target

 For coherent events this essentially indicates the failure of method E due to beam and detector smearing effects or that the event was mischaracterized as coherent ⇒ Important analysis/cross-check tool

- How the method works
 - Calculate p of outgoing A': $p_{A'} = p_A (p_V + p_{e'} p_e)$
 - Express and correct the outgoing nucleus in light cone variables:
 - $p_{A'}^+ = E_{A'} + p_{z,A'}$
 - $p_{T,A'}^2 = p_{x,A'}^2 + p_{y,A'}^2$
 - $p_{A'} = (M_A^2 + p_{T,A'}^2)/p_{A'}^+$ where $p_{A'}^-$ is now modified by using the true mass M_A^2 .
 - ▶ The corrected 4-momentum of the outgoing nuclei is now

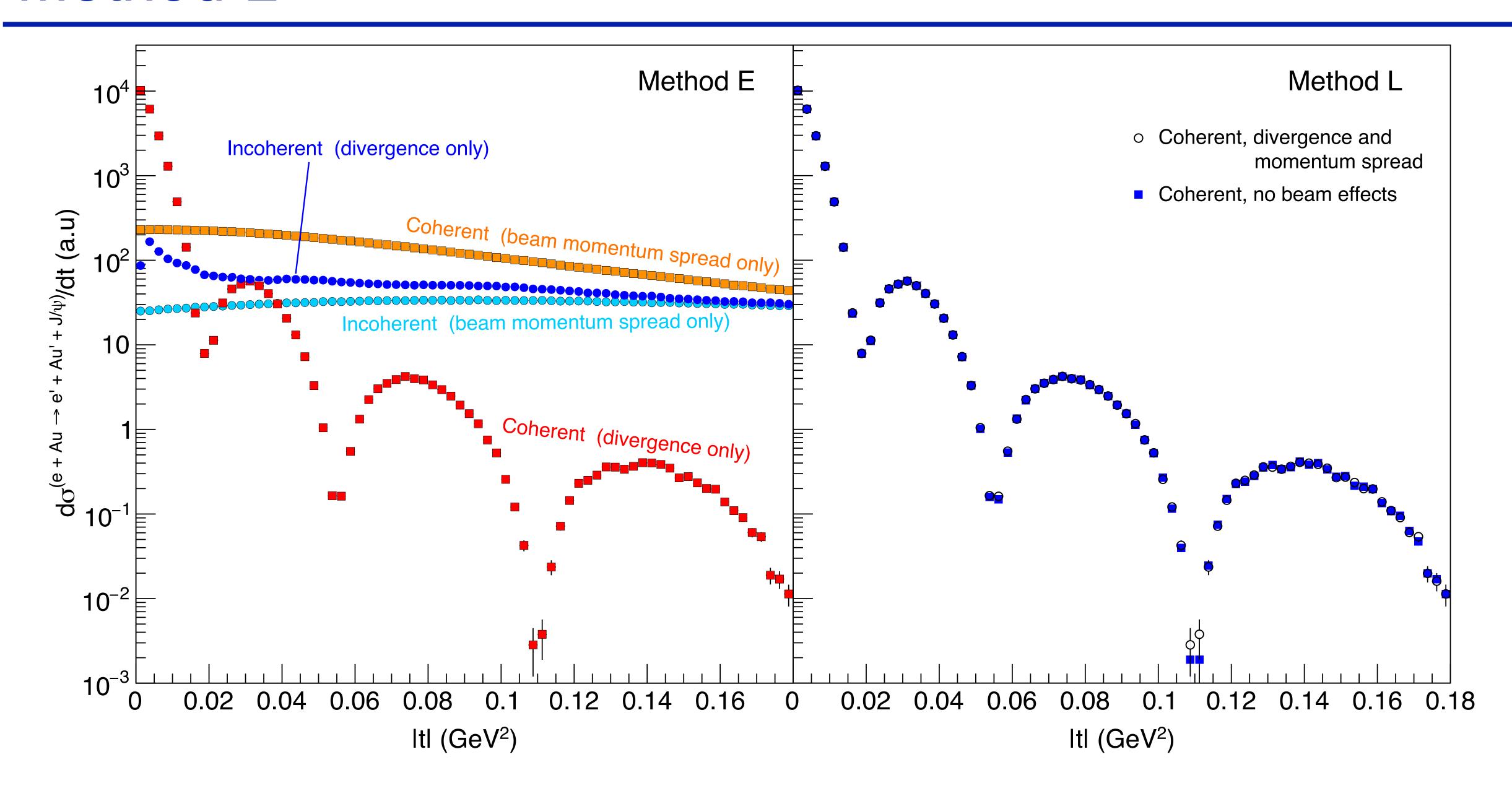
$$p_{A'}^{\text{corr}} = \left[p_{x,A'}, p_{y,A'}, (p_{A'}^+ - p_{A'}^-)/2, (p_{A'}^+ + p_{A'}^-)/2 \right]$$

- ▶ In short, you are using the true invariant mass of the nucleus to compensate the smearing in the larger component of the electron 4-momentum by modifying E_{A'} and p_{z,A'} simultaneously.
- Now simply: $t_{\rm corr} = \left| p_A p_{A'}^{\rm corr} \right|^2$

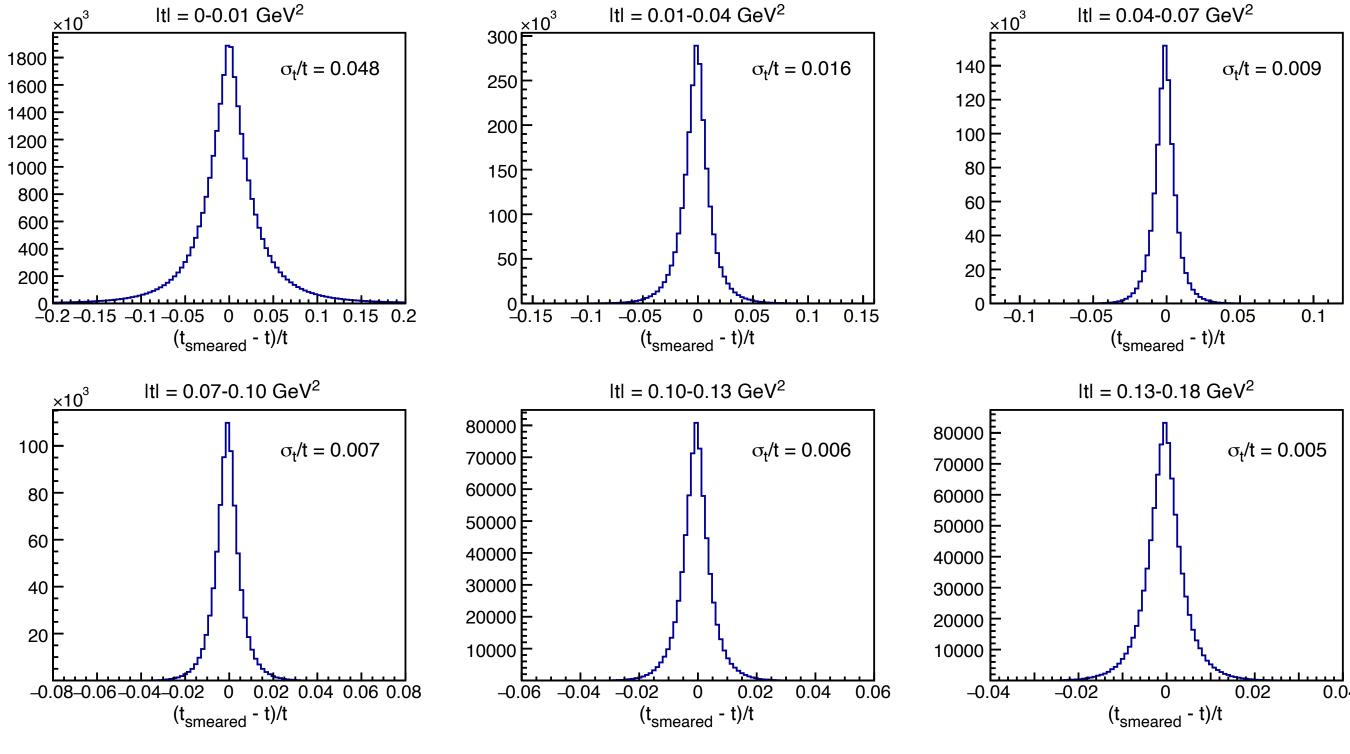


All beam effects on

		t-range (GeV ²)							
method	effect	0-0.1	0.1-0.4	0.04 - 0.07	0.07 - 0.10	0.10 - 0.13	0.13 - 0.18		
\mathbf{E}	beam divergence	0.061	0.015	0.008	0.007	0.006	0.005		
E	beam mom. spread	149.61	10.36	3.03	1.86	1.37	1.03		
L	divergence & mom. spread	0.048	0.016	0.009	0.007	0.006	0.005		



Method L with beam effects and nominal p_T resolution



,	MO	1			(((1,12))				
measurement	MS	t-range (GeV ²)							
precision term for	term for barrel								
barrel (backward) (%)	(backward) (%)	0-0.1	0.1-0.4	0.04 - 0.07	0.07 - 0.10	0.10 - 0.13	0.13 - 0.18		
0.05 (0.1)	1.0 (2.0)	4.58	0.45	0.25	0.19	0.16	0.14		
0.1 (0.2)	1.0 (2.0)	4.71	0.46	0.25	0.20	0.17	0.14		
0.025 (0.05)	1.0 (2.0)	4.54	0.45	0.24	0.19	0.16	0.14		
0.05 (0.1)	0.5(2.0)	3.53	0.38	0.21	0.17	0.14	0.12		
0.05 (0.1)	0.5 (1.0)	1.29	0.22	0.12	0.10	0.08	0.07		
0.05 (0.1)	0.5 (0.5)	0.78	0.16	0.09	0.07	0.06	0.05		
0.05 (0.1)	0.25 (0.5)	0.49	0.12	0.07	0.05	0.05	0.04		
0.05(0.1)	0.25 (0.25)	0.36	0.09	0.05	0.04	0.04	0.03		

Method L and A give similar t resolutions

Summary

- Method E fails in the presence of beam momentum resolution
- Method L is an extension and a huge improvement
 - Only applicable for coherent events
 - We confirmed in simulations that all results obtained by method L for coherent processes are identical or very similar to that of method A in the studies discussed below.
- Ultimately, in the actual analysis once the EIC is realized, both methods (A and L) should be carefully compared and studied.
 - For coherent processes method L is likely the better choice as it does not rely on any approximations
 - For incoherent processes method A is the only option available