#### Transverse energy-energy correlators at the EIC

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SURGE collaboration



California EIC Consortium Meeting



# Energy-energy correlators (EEC)

- Two-point energy correlator
- Particles weighted by their energy
  - $\Rightarrow$  Less sensitive to the nonperturbative IR region
    - One of the first infrared-safe event shapes in QCD Basham, Brown, Ellis, Love, Phys.Rev.Lett. 41 (1978) 1585, Phys.Lett.B 85 (1979) 297-299

• 
$$e^+ + e^- \rightarrow X$$
:

$$\frac{\mathrm{d}\Sigma_{e^+e^-}}{\mathrm{d}\cos\chi} = \sum_{i,j} \int \mathrm{d}\sigma \; \frac{E_i E_j}{Q^2} \delta(\cos\theta_{ij} - \cos\chi)$$



Moult, Zhu, 1801.02627

- Collinear limit:  $\chi \approx 0$ 
  - Probes jet substructure

Dixon, Moult, Zhu, 1905.01310

- Back-to-back limit:  $\chi \approx \pi$ 
  - Probes TMD physics

Moult, Zhu, 1801.02627



### Transverse energy-energy correlators (TEEC)



$$\mathsf{TEEC} = \frac{\mathrm{d}\sigma}{\mathrm{d}\tau\,\mathrm{d}y_{\mathsf{e}}\,\mathrm{d}^{2}\boldsymbol{p}_{\mathcal{T}}^{\mathsf{e}}} = \sum_{h} \int \mathrm{d}\sigma_{\mathrm{DIS}}\,\frac{\boldsymbol{E}_{\mathcal{T},l}\boldsymbol{E}_{\mathcal{T},h}}{\boldsymbol{E}_{\mathcal{T},l}\sum_{i}\boldsymbol{E}_{\mathcal{T},i}}\delta\bigg(\tau - \frac{1+\cos\phi}{2}\bigg)$$

- Generalization of the EEC Ali, Pietarinen, Stirling, Phys.Lett.B 141 (1984) 447-454
- $\bullet\,$  Back-to-back region in the azimuthal plane:  $\phi\approx\pi\Leftrightarrow\tau\ll1$

J. Penttala (UCLA)

- We calculate using TMD factorization at small x
- Note: factorization for this process is yet to be proven
  - However, factorization has been shown for similar processes such as lepton-jet production Liu et al., 1812.08077; Arratia et al., 2007.07281
- Assuming factorization, we write

$$\mathsf{TEEC} = \frac{\mathrm{d}\sigma}{\mathrm{d}\tau\,\mathrm{d}y_e\,\mathrm{d}^2\boldsymbol{p}_T^{\mathrm{e}}} = \sigma_0 H(Q,\mu) \sum_q e_q^2 \frac{p_T^{\mathrm{e}}}{\sqrt{\tau}} \int_0^\infty \frac{\mathrm{d}b}{\pi} \cos(2b\sqrt{\tau}p_T^{\mathrm{e}}) f_q(x,b,\mu,\zeta) J_q(b,\mu,\hat{\zeta})$$

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$$\sigma_0 = rac{2lpha_{
m em}^2}{sQ^2}rac{\hat{s}^2+\hat{u}^2}{\hat{t}^2}$$
 (the leading-order partonic cross section)

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 $f_q(x, b, \mu, \zeta)$  is the TMD quark distribution

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•  $f_q(x, b, \mu, \zeta)$  satisfies the TMD evolution equations for the scales  $\mu$  and  $\zeta$ 

$$\frac{\mathrm{d}}{\mathrm{d}\ln\sqrt{\zeta}}\ln f_q(\mathbf{x}, \mathbf{b}, \mu, \zeta) = K(\mathbf{b}, \mu) \qquad \qquad \frac{\mathrm{d}}{\mathrm{d}\ln\mu}\ln f_q(\mathbf{x}, \mathbf{b}, \mu, \zeta) = \gamma^q_\mu \big[\alpha_s(\mu), \zeta/\mu^2\big]$$

• We can write:  $f_q(x, b, \mu, \zeta) = f_q(x, b, \mu_{b_*}, \mu_{b_*}^2) \exp[-S_{\text{pert}}(\mu, \mu_{b_*}, \zeta)]$ where the perturbative Sudakov factor

$$S_{\mathsf{pert}}(\mu,\mu_{b_*},\zeta) = -\mathcal{K}(b_*,\mu_{b_*})\ln\left(\frac{\sqrt{\zeta}}{\mu_{b_*}}\right) - \int_{\mu_{b_*}}^{\mu} \frac{\mathrm{d}\mu'}{\mu'} \gamma_{\mu'}^q \left[\alpha_s(\mu'),\frac{\zeta}{\mu'^2}\right]$$

evolves the quark TMD from the initial scale  $\mu_{b_*}$  to the scales  $\mu=\sqrt{\zeta}=Q$ 

• Note: nonperturbative Sudakov factor assumed to be part of the initial condition

Initial condition for the TMD evolution using small-x dipole amplitudes  $\mathcal{S}_{\mathsf{x}}$ 

$$\begin{aligned} & \times f_q \left( x, b, \mu_{b_*}, \mu_{b_*}^2 \right) = \frac{N_c S_\perp}{8\pi^4} \int \mathrm{d}\epsilon_f^2 \, \mathrm{d}^2 \mathbf{r} \, \frac{(\mathbf{b} + \mathbf{r}) \cdot \mathbf{r}}{|\mathbf{b} + \mathbf{r}||\mathbf{r}|} \epsilon_f^2 \\ & \times \, \mathcal{K}_1(\epsilon_f |\mathbf{r}|) \Big[ 1 + \mathcal{S}_x(|\mathbf{b}|) - \mathcal{S}_x(|\mathbf{b} + \mathbf{r}|) - \mathcal{S}_x(|\mathbf{r}|) \Big] \end{aligned}$$

where the initial scale is  $\mu_{b_*}=2e^{-\gamma_E}/b_*$  and  $b_*=b/\sqrt{1+b^2/b_{\max}^2}$  with  $b_{\max}=1.5~{\rm GeV^{-1}}$ 



Marquet, Xiao, Yuan, 0906.1454

We consider two different models for the dipole amplitude:

• The Golec-Biernat–Wüsthoff (GBW) model:

$$\mathcal{S}_{\mathsf{x}}(r) = \exp\left(-rac{r^2 Q_{\mathrm{s}}^2(x)}{4}
ight)$$

where the saturation scale  $Q_{
m s}$  reads:  $Q_{
m s}^2(x)=1~{
m GeV}^2 imes \left(rac{x_0}{x}
ight)^\lambda$ 

McLerran–Venugopalan model at x<sub>0</sub>

$$\mathcal{S}_{\mathsf{x}_0}(r) = \exp\left[-rac{r^2 Q_{s,0}^2}{4} \ln\left(rac{1}{r \Lambda_{\mathsf{QCD}}} + e_c \cdot e
ight)
ight]$$

with the running-coupling Balitsky-Kovchegov (rcBK) evolution equation

 $\frac{\partial}{\partial \ln(1/x)} \mathcal{S}_{x}(|\mathbf{r}|) = \int d^{2}\mathbf{r}' \, \mathcal{K}(\mathbf{r},\mathbf{r}') \Big[ \mathcal{S}_{x}(|\mathbf{r}'|) \mathcal{S}_{x}(|\mathbf{r}-\mathbf{r}'|) - \mathcal{S}_{x}(|\mathbf{r}|) \Big] \text{ for the } x \text{ dependence}$ 

### **TEEC** jet function

• The TEEC jet function is given in terms of the TMD fragmentation functions  $D_{1,h/q}$ :

$$J_q(b,\mu,\hat{\zeta}) \equiv \sum_{h} \int_0^1 \mathrm{d}z \, z \widetilde{D}_{1,h/q}(z,b,\mu,\hat{\zeta})$$

where we sum over all hadrons in the final state and choose  $\mu=\sqrt{\hat{\zeta}}=Q$ 

• The TMD FFs can be further written in terms of the collinear FFs as

$$\widetilde{D}_{1,h/q}\left(z,b,\mu,\hat{\zeta}\right) = \sum_{i} \int_{z}^{1} \frac{\mathrm{d}y}{y} C_{i\leftarrow q}\left(\frac{z}{y},b\right) D_{h/i}(y,\mu_{b_{*}}) \times \exp\left[-S_{\mathsf{pert}}\left(\mu,\mu_{b_{*}},\hat{\zeta}\right)\right] \times \exp\left[-S_{\mathsf{NP}}\left(z,b,Q_{0},\hat{\zeta}\right)\right]$$

where  $C_{i \leftarrow q}\left(\frac{z}{y}, b\right)$  are matching coefficients and the Sudakov factors  $S_{pert}$  and  $S_{NP}$  take care of the TMD evolution

• Nonperturbative Sudakov modeled as:  $S_{\text{NP}}\left(z, b, Q_0, \hat{\zeta}\right) = \frac{g_2}{2} \ln\left(\frac{b}{b_*}\right) \ln\left(\frac{\sqrt{\hat{\zeta}}}{Q_0}\right) + g_1^D \frac{b^2}{z^2}$ 

- Studied in the EIC kinematics
- Sensitivity to the dipole amplitude: Up to a factor 2 difference between rcBK and GBW at  $p_T^e = 2 \text{ GeV}$
- Low-momentum region most sensitive to gluon saturation
  - $\Rightarrow$  potentially a good process to study saturation effects



#### Numerical results – nuclear suppression

• We model nuclei by changing the saturation scale

$$Q_{s,\mathcal{A}}^2 = c \, \mathcal{A}^{1/3} \, Q_s^2$$
 where  $c \in [0.5,1]$  to estimate uncertainty in the nuclear geometry

• To study nuclear suppression we consider the quantity

$${\sf R}_{\sf A} = rac{1}{{\sf A}} \left. rac{{
m d}\sigma_{e{\sf A}}}{{
m d} au {
m y}_e {
m d}^2 {m 
ho}_T^e} 
ight/ rac{{
m d}\sigma_{ep}}{{
m d} au {
m d} y_e {
m d}^2 {m 
ho}_T^e}$$

- Without saturation  $R_A 
  ightarrow 1$ 
  - Smaller dipoles probed when  $\sqrt{ au} p_T^e$  large
    - $\Rightarrow$  saturation effects smaller in this region
- ullet Nuclear modification of 15 20% can be expected for  $\tau\ll 1$



- TEEC is an infrared-safe event-shape observable
  - Probes TMD physics in the back-to-back region
- We have considered TEEC for DIS using the combined TMD and small x framework
  - The quark TMD and the jet function evolved with the TMD evolution
  - The initial condition for the quark TMD modeled using the small-x dipole amplitude
- TEEC found to be sensitive to saturation in the back-to-back limit  $au \ll 1$ 
  - $\Rightarrow$  An interesting process to measure at the EIC!