

***Effective denoising diffusion  
probabilistic models for  
fast and high fidelity whole-event  
simulation in high-energy  
heavy-ion experiment***

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Yihui Ren<sup>a</sup>, Yi Huang<sup>a</sup>, Tim Rinn<sup>b</sup>

a: Brookhaven National Laboratory

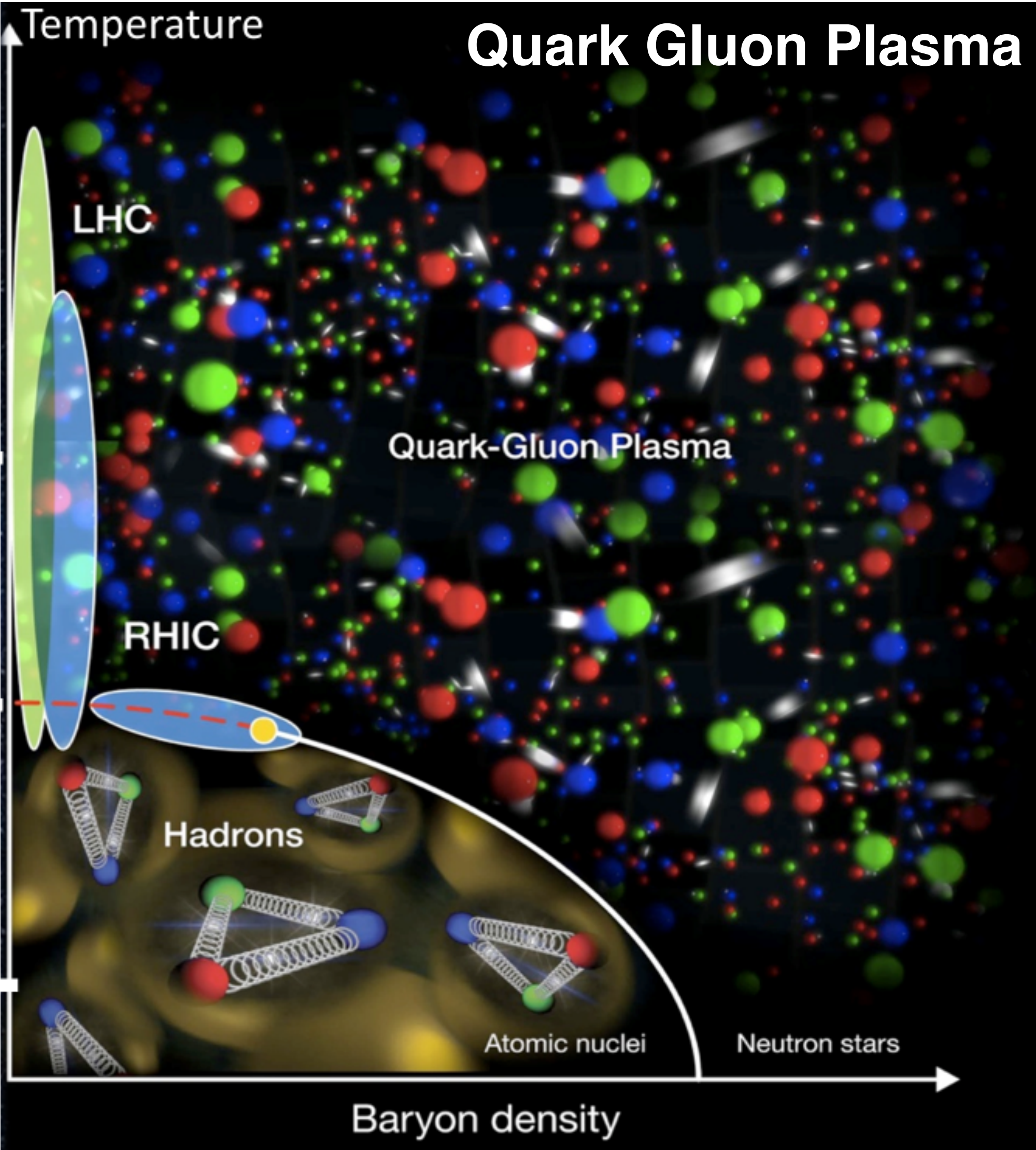
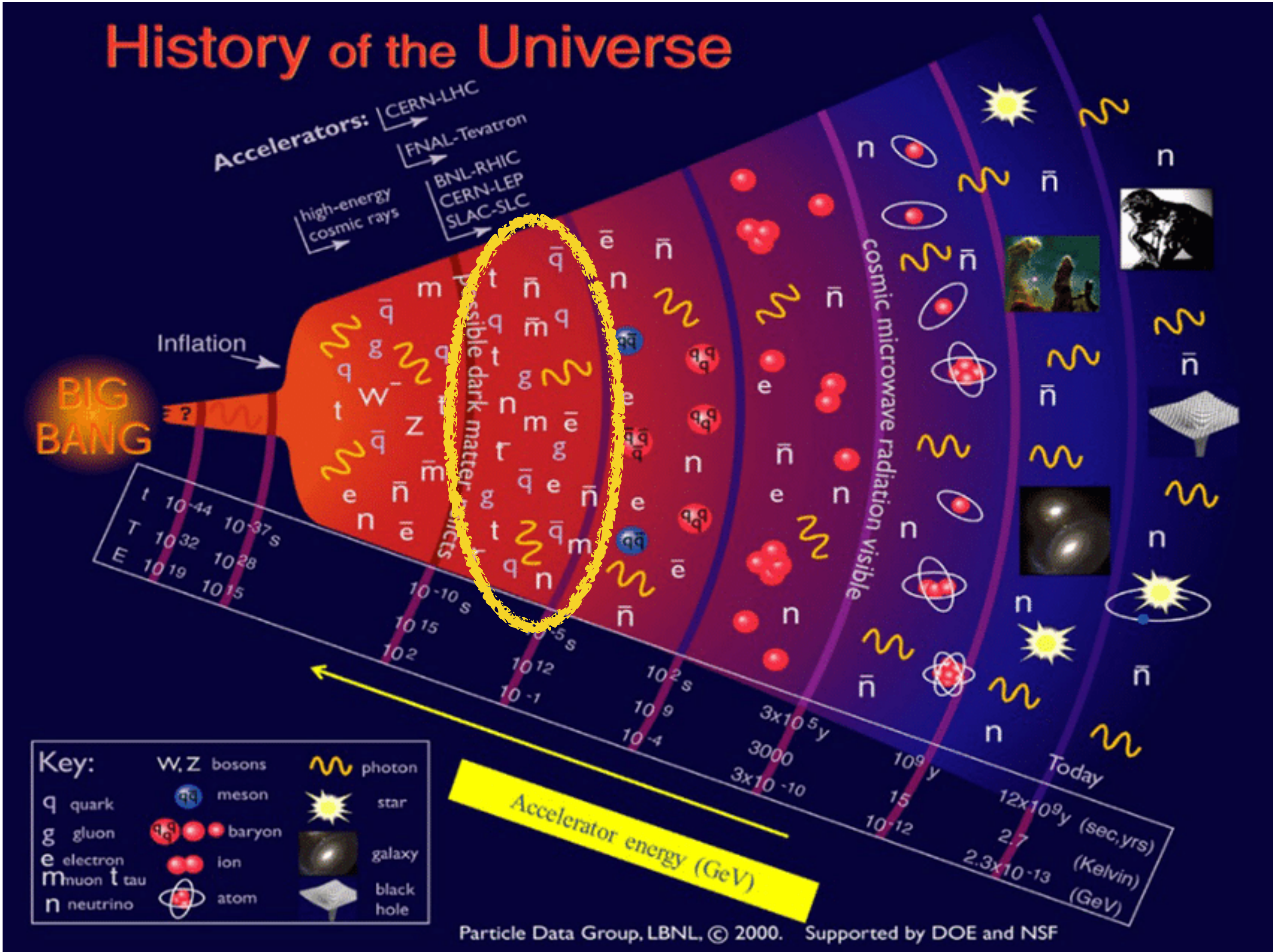
b: Los Alamos National Laboratory

*BNL Physics 8th Joint Meeting on AI/ML  
Apr. 3, 2024*

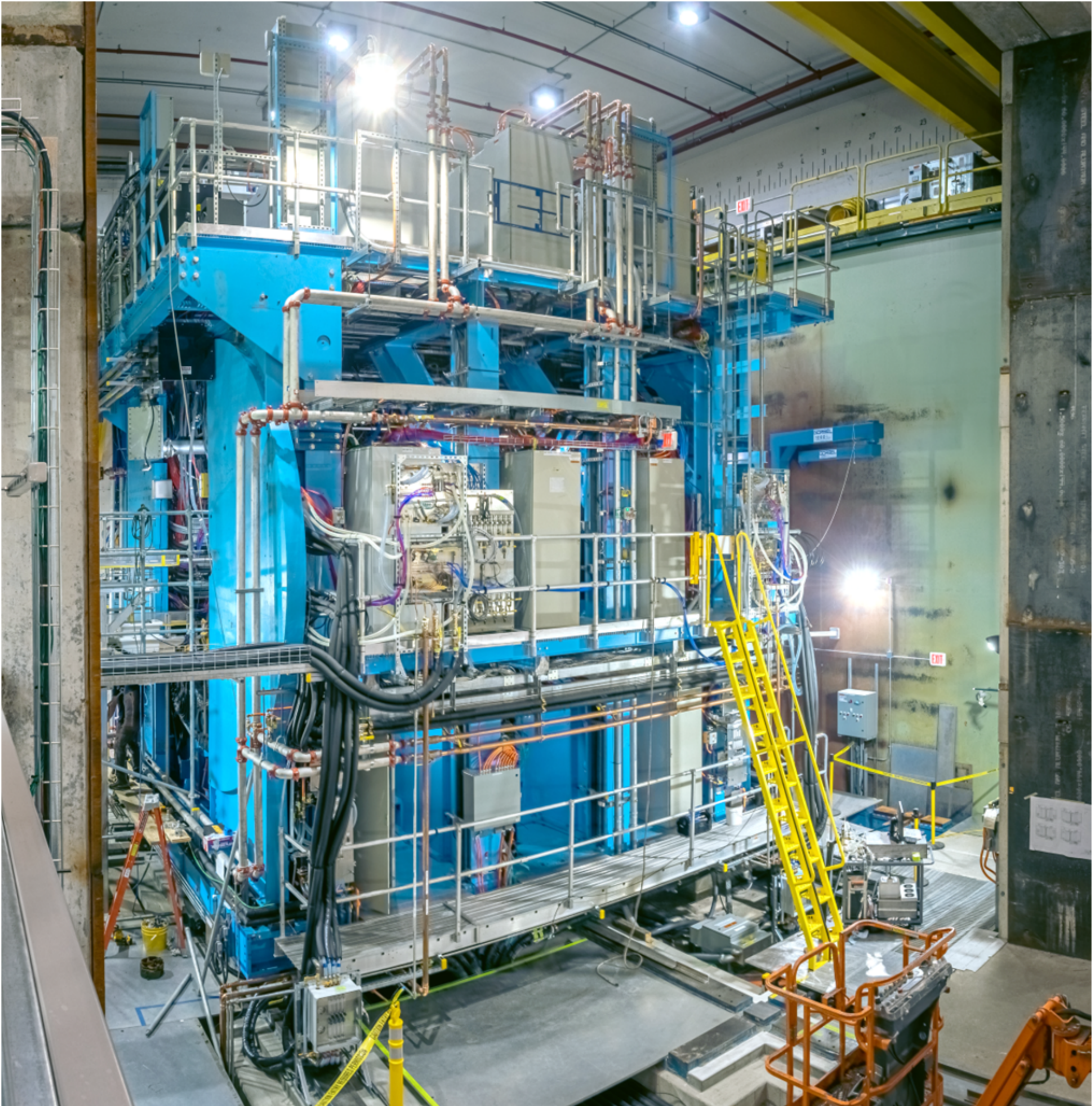


**Brookhaven**  
National Laboratory

# Early Universe and Quark Gluon Plasma



# sPHENIX Detector at RHIC



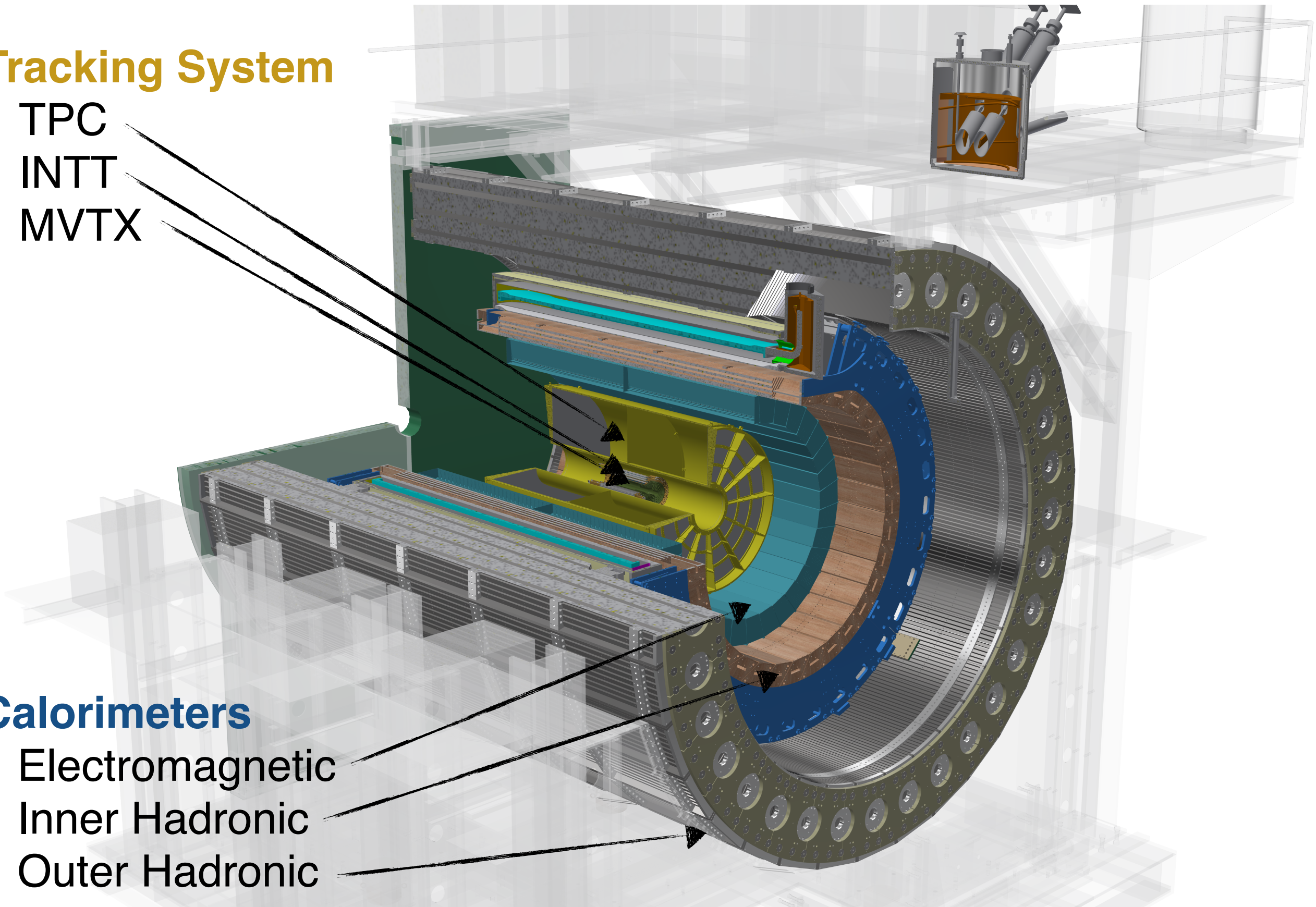
## Tracking System

- TPC
- INTT
- MVTX

## Calorimeters

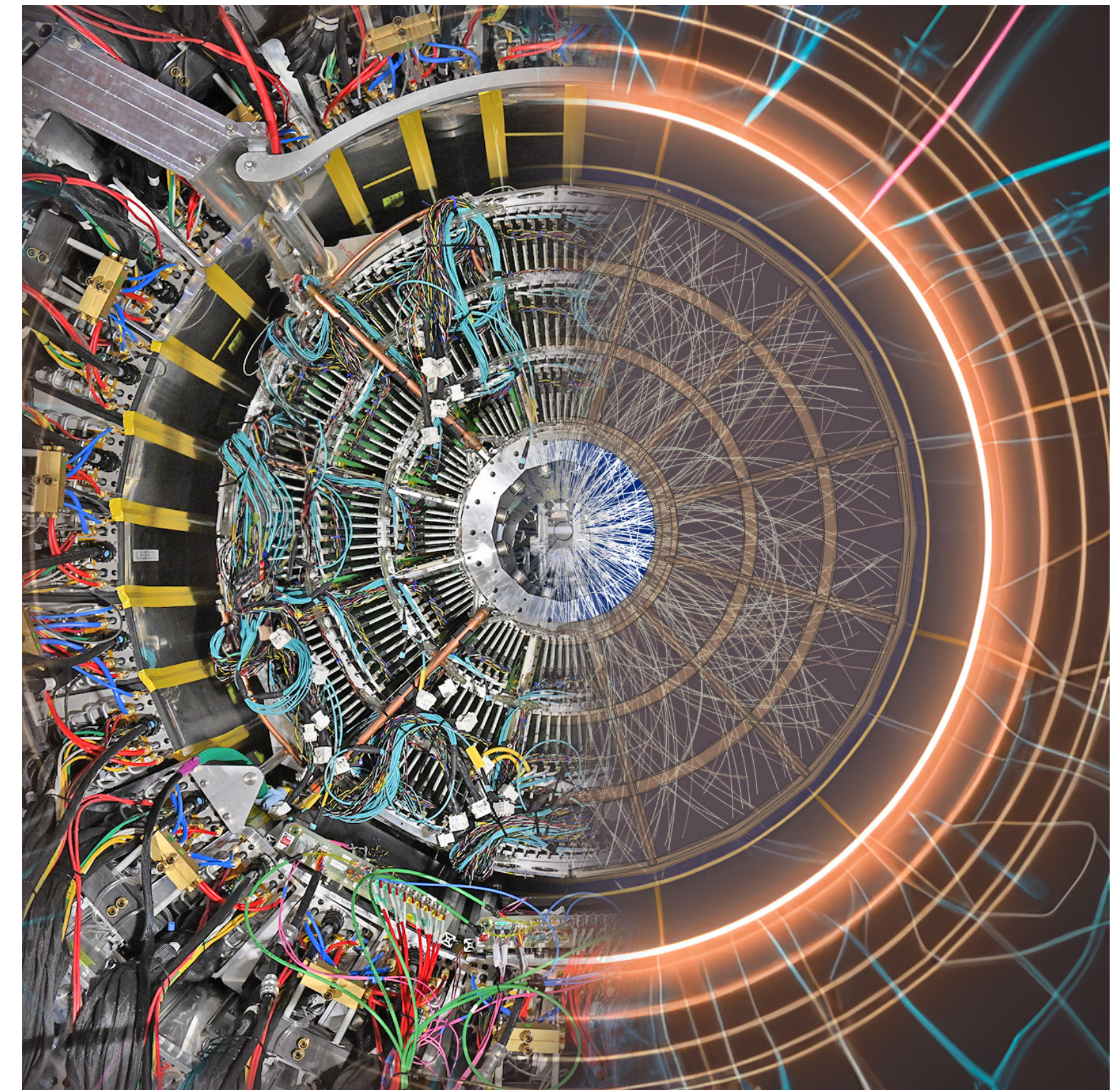
- Electromagnetic
- Inner Hadronic
- Outer Hadronic

- Data taking began last year!
- High-precision **tracking system** + Hermetic Electromagnetic & Hadronic **calorimeters**



# Simulations of Relativistic Heavy Ion Collisions

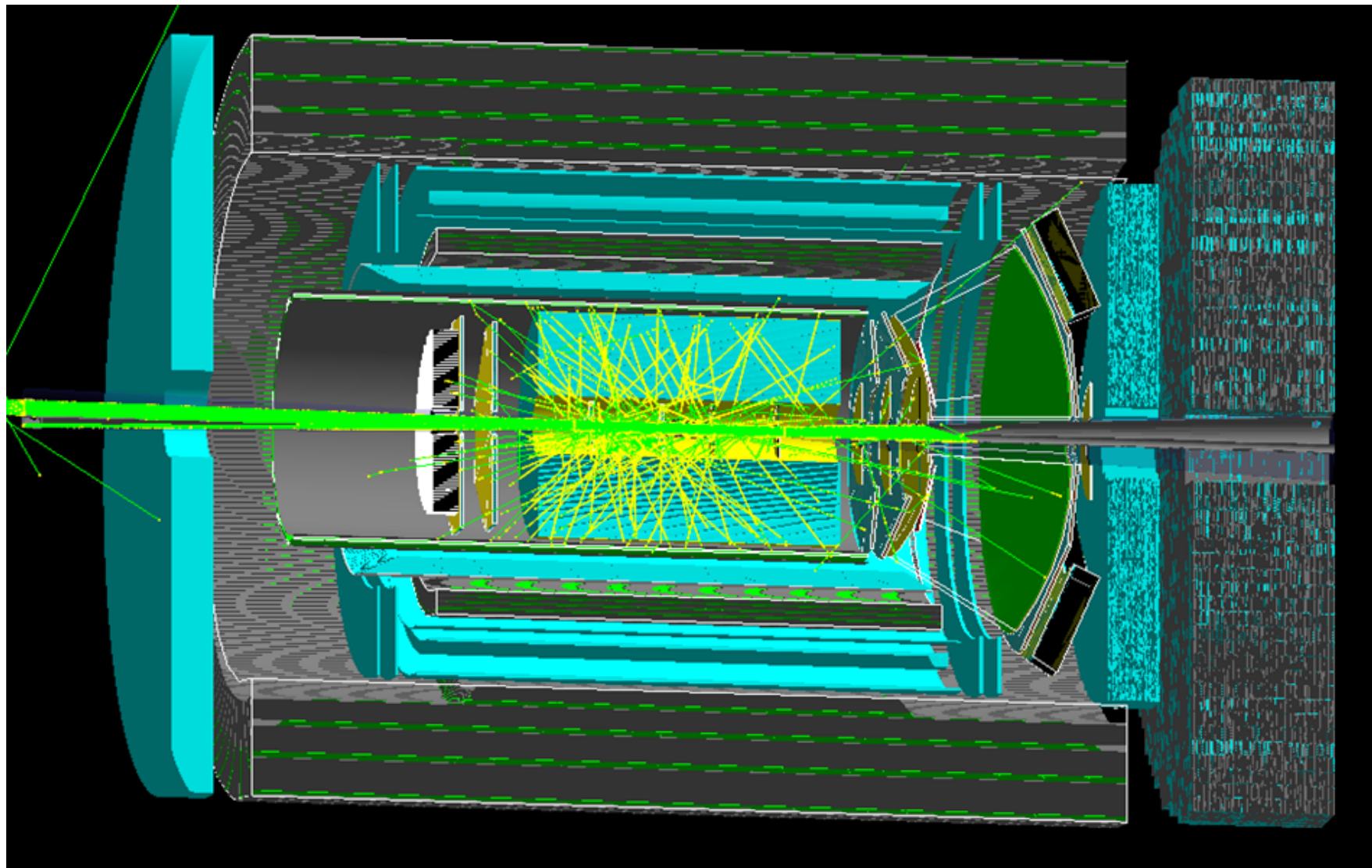
- $O(1000)$  particles in one nuclear collision event  
+ *thousands shower steps* per particle
- ➔ Simulation of the interaction of particles with detectors is **high complexity and computationally intensive work**



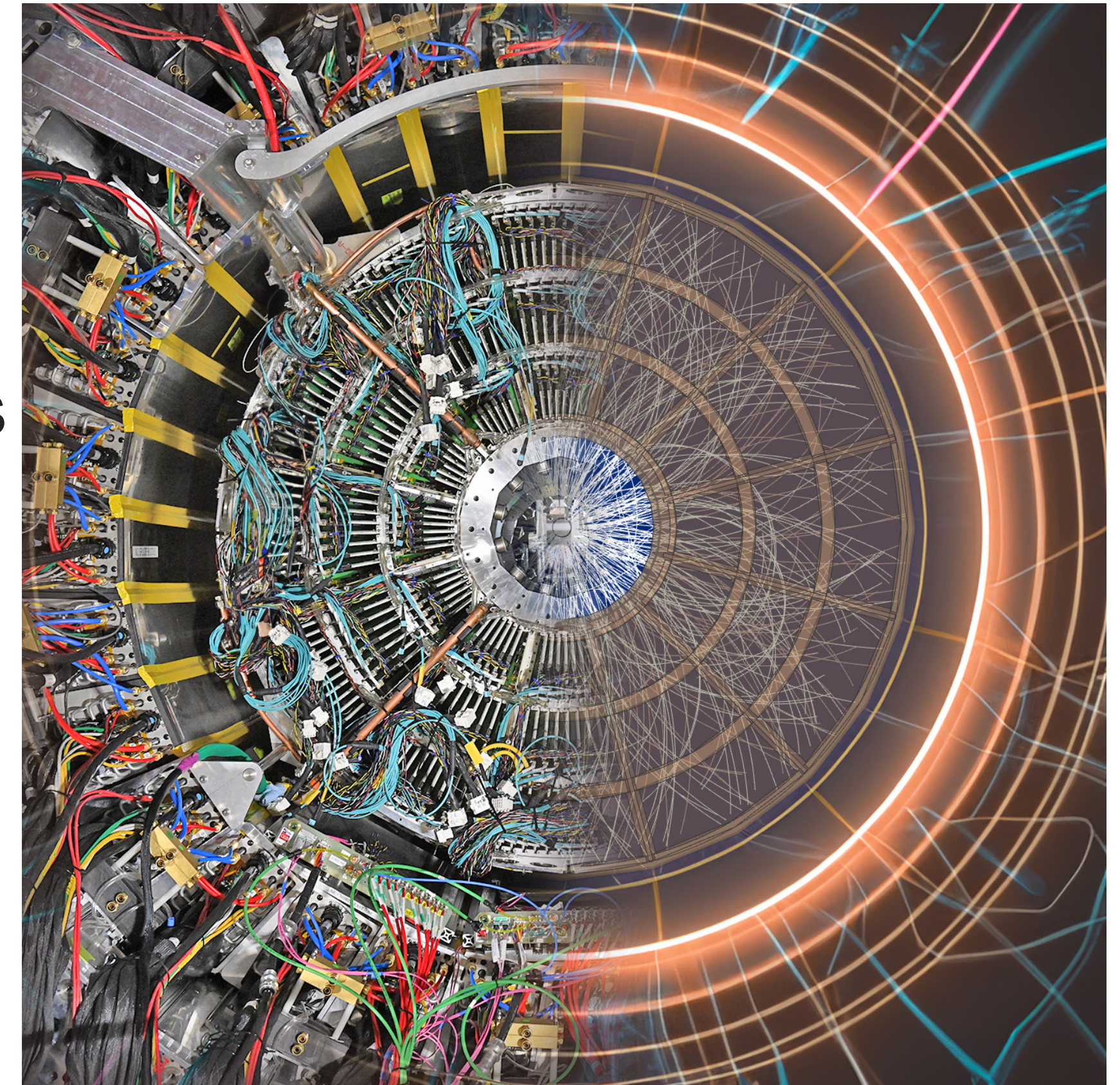
sPHENIX TPC

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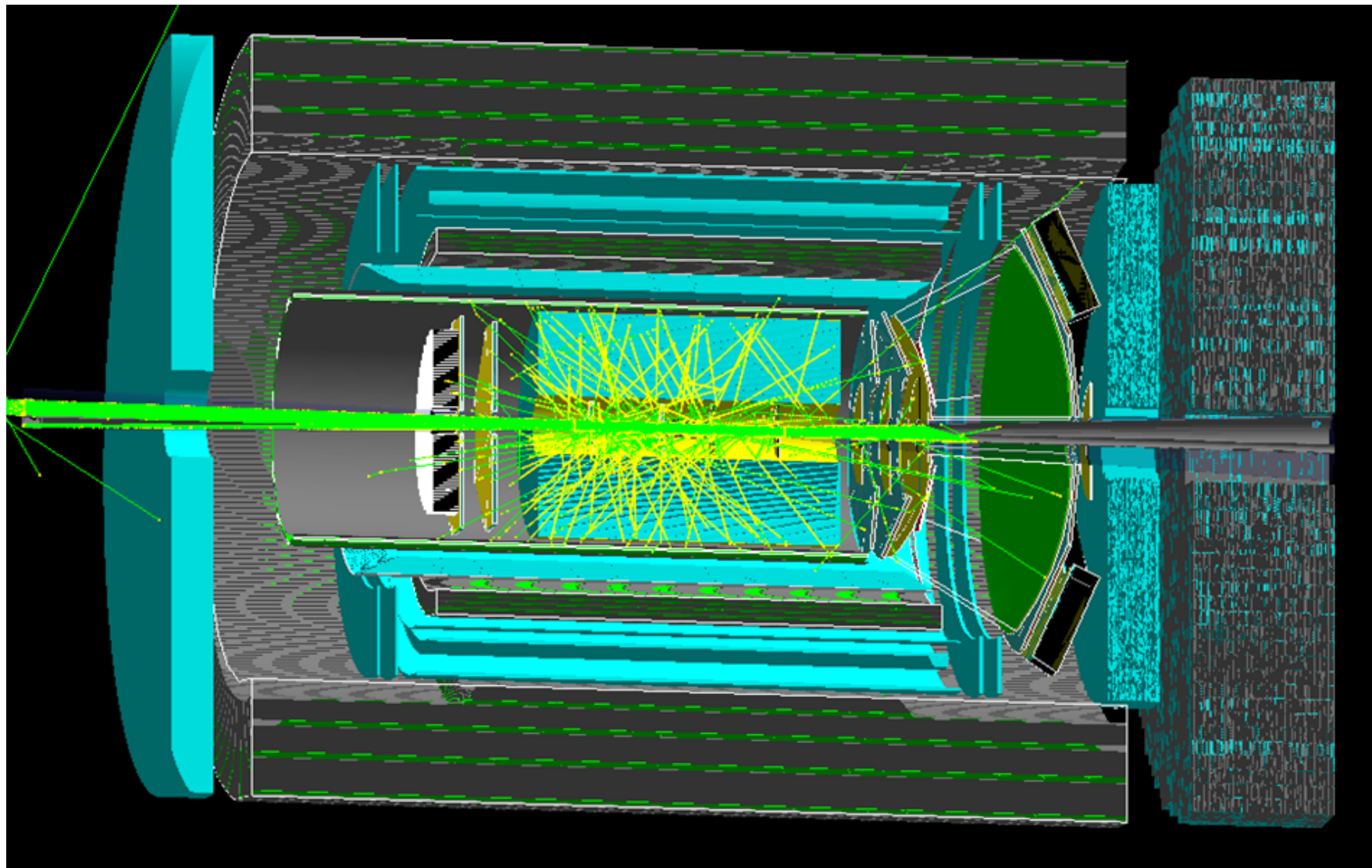
EIC CDR



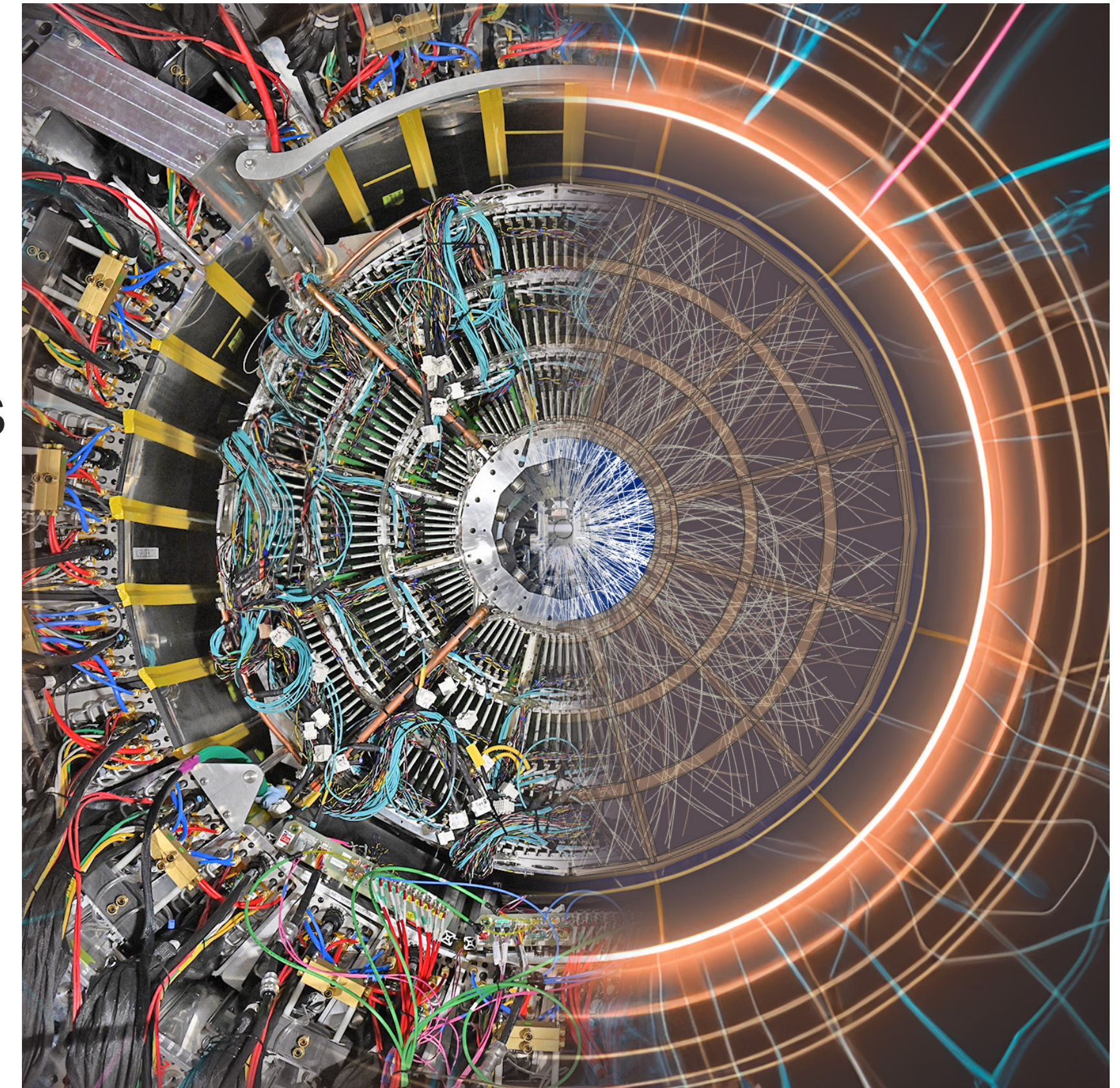
sPHENIX TPC

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- *Electron-Ion Collider* will need a large amount of simulations of full detector with both physics and machine background
- ML can speed up and produce large amount of the heavy ion event simulations!



EIC CDR

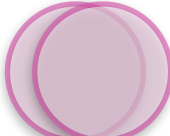


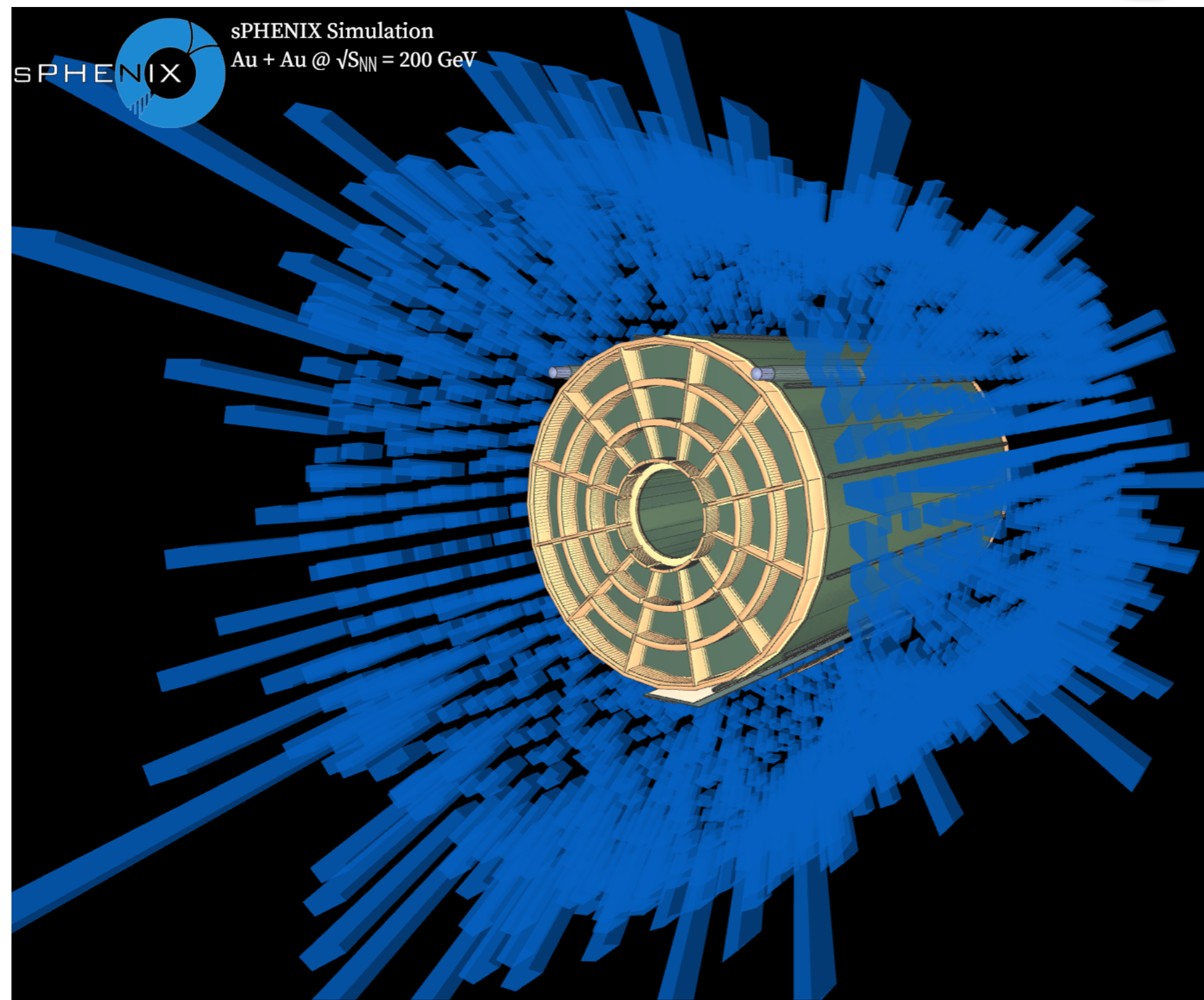
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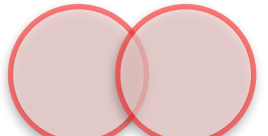
We introduce **full detector whole-event ML simulations** for heavy ion collisions

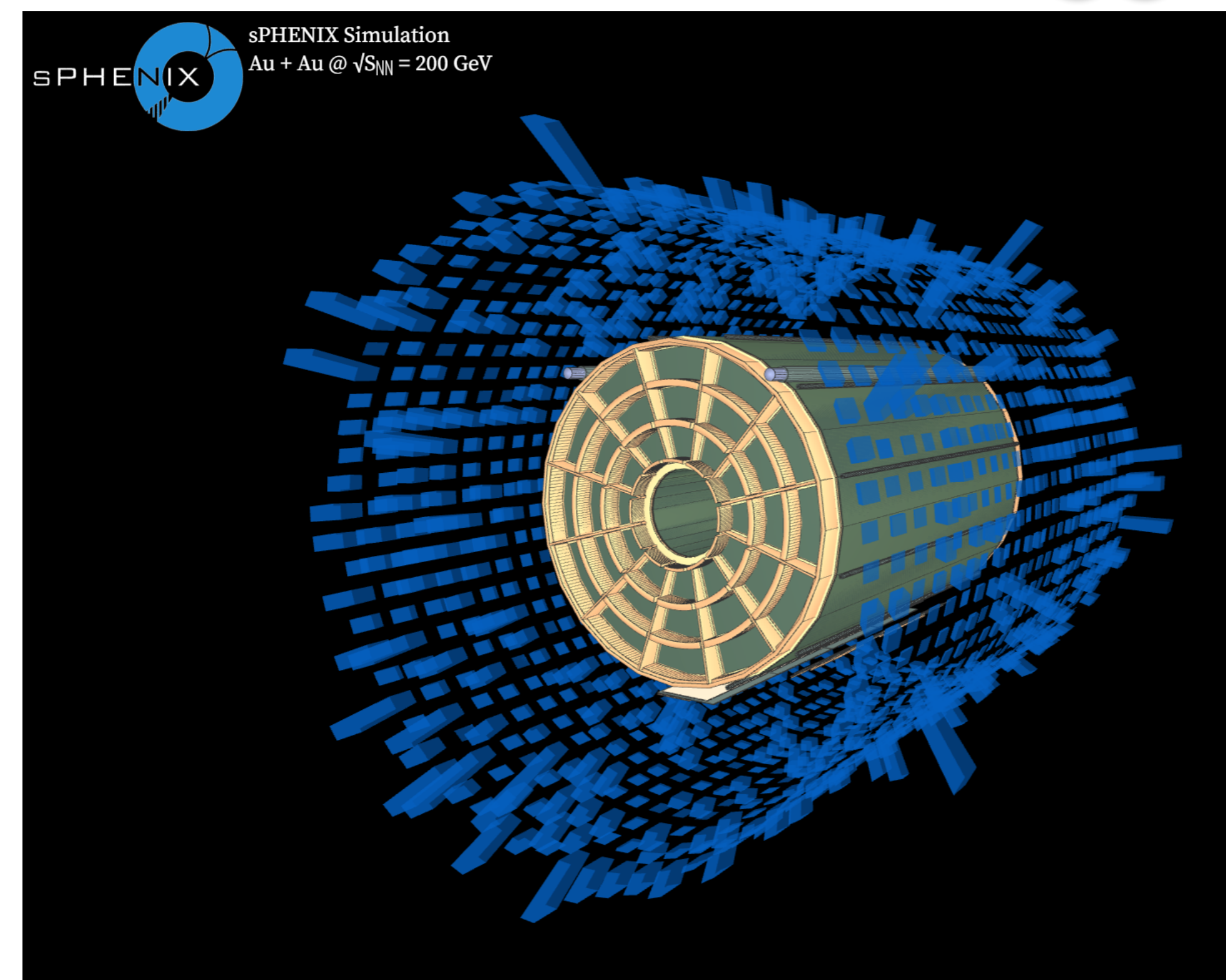
# Heavy Ion Collision Event

- **HIJING** Monte Carlo event generator for Au+Au collisions at  $\sqrt{s_{NN}}=200$  GeV
- **Geant4** full detector simulation with the sPHENIX geometry

Head-on collision (0-10% Centrality) 

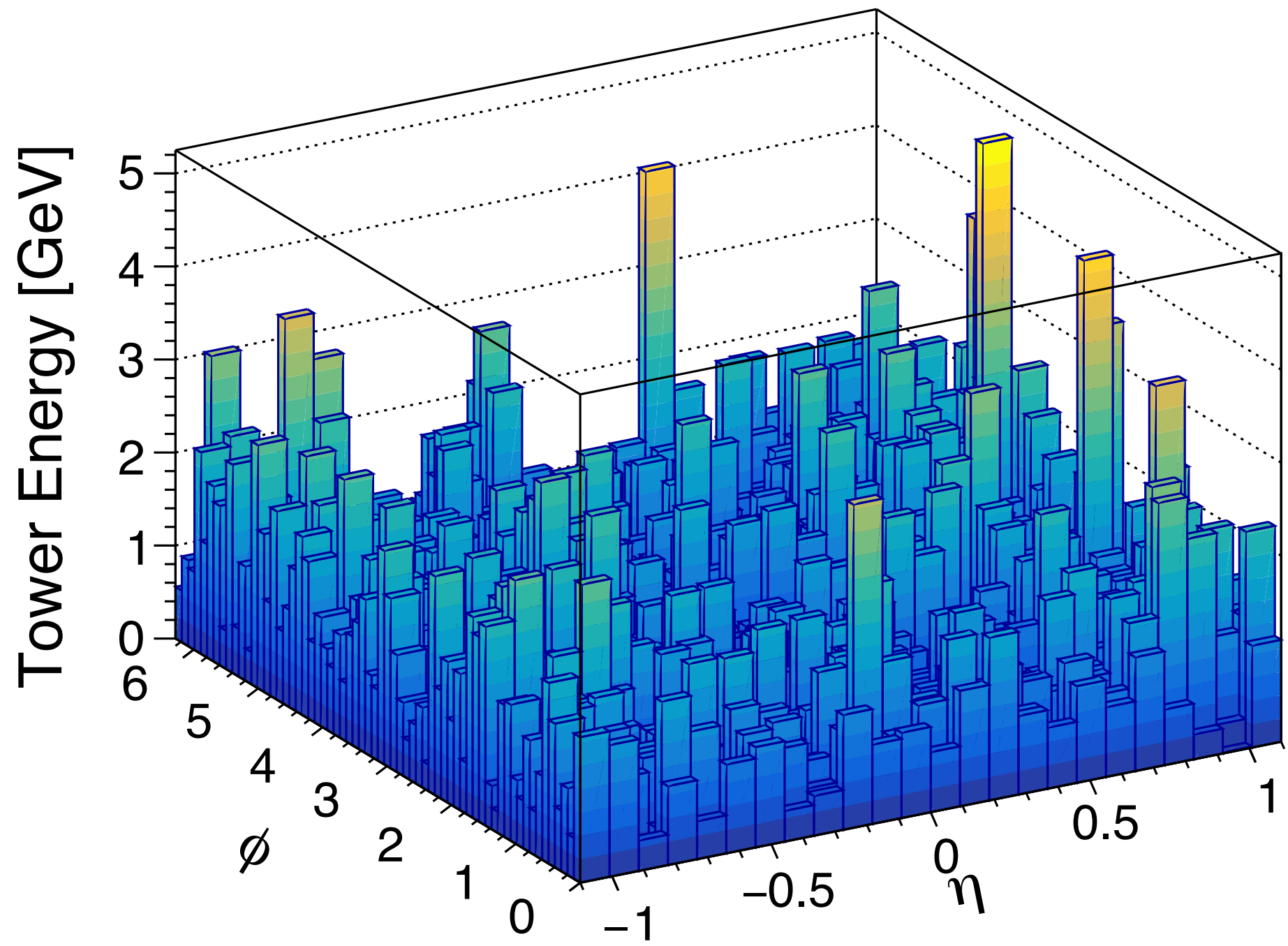


Side collision (40-50% Centrality) 

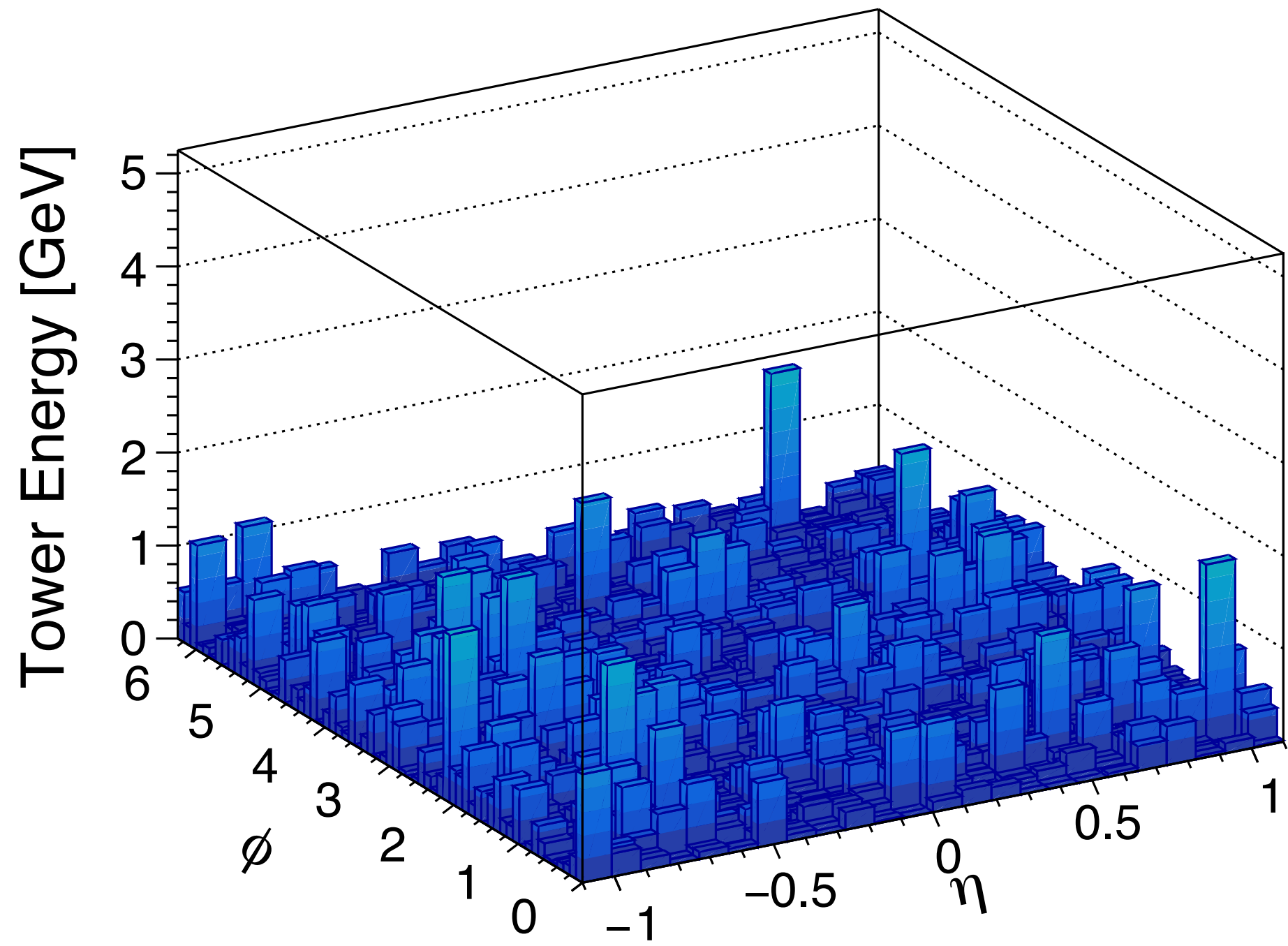


# Tower Distributions

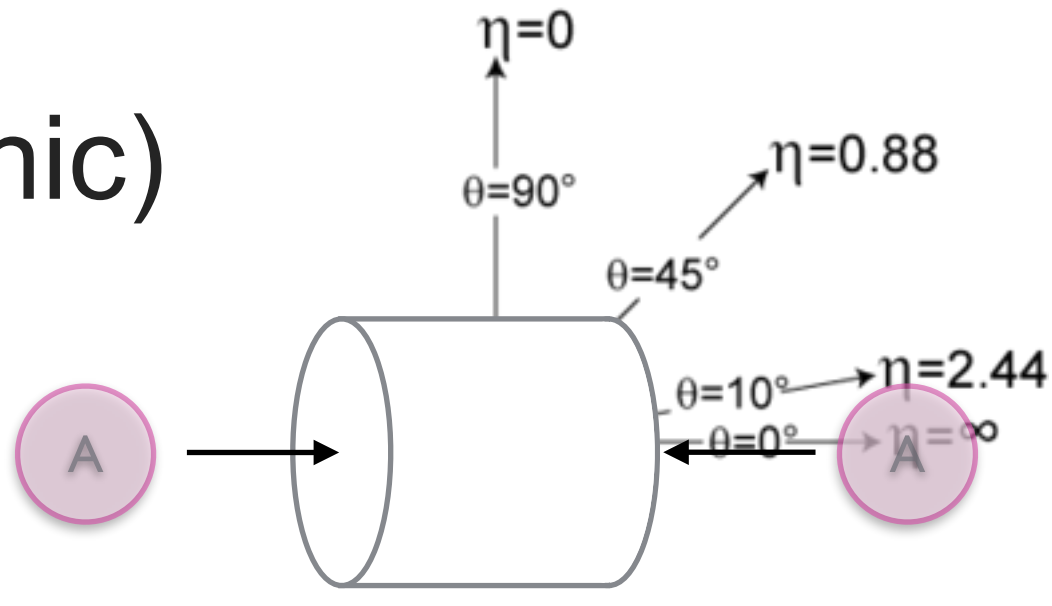
0-10% Centrality 



40-50% Centrality 



- Full calorimeter **towers** (Electromagnetic + Inner hadronic + Outer hadronic)
  - ➔  $-1.1 < \eta < 1.1, \quad 0 < \phi < 2\pi$
  - ➔ (24 x 64) bins in  $(\eta, \phi)$



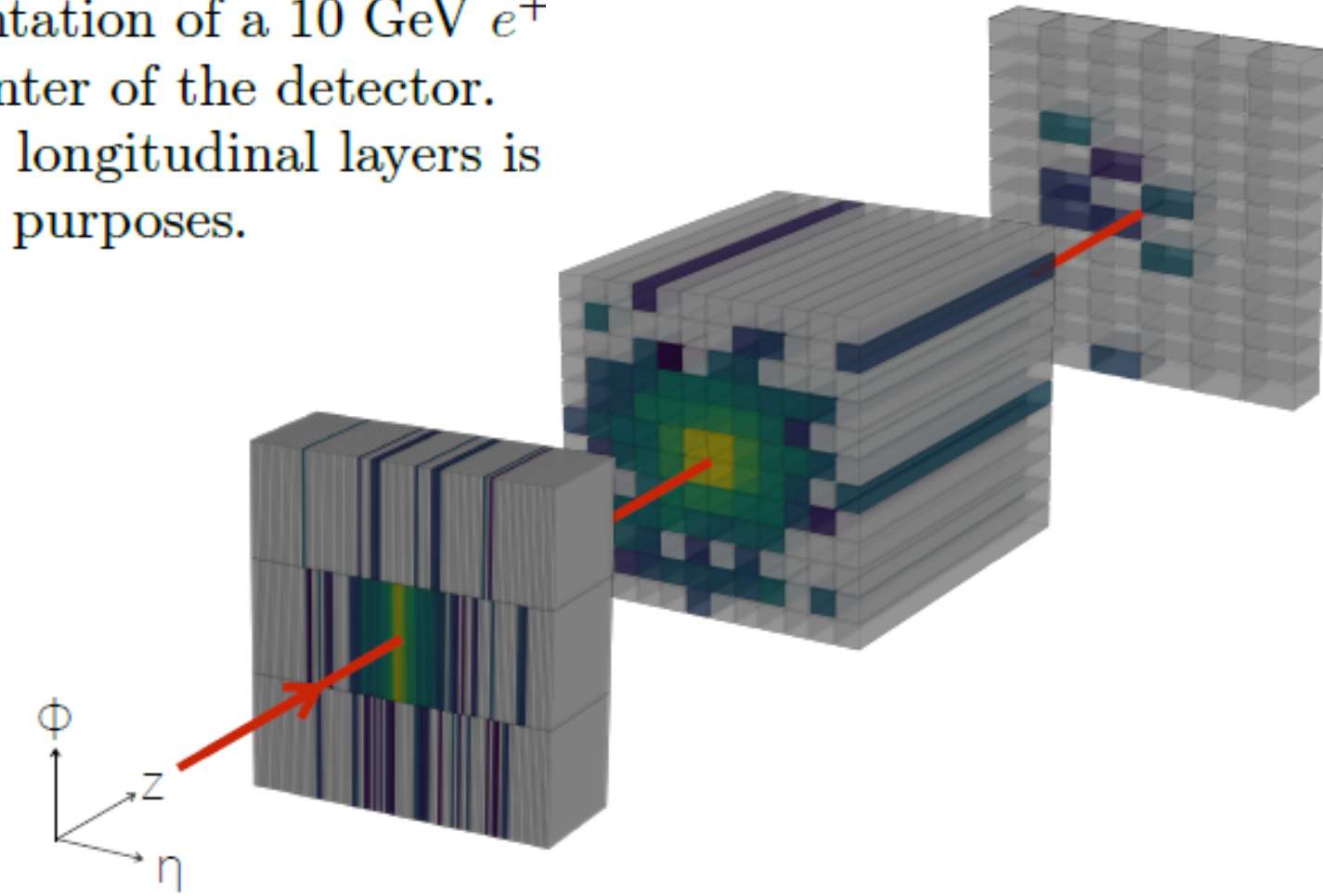


# Generative AI

- **Generative Adversarial Networks (GAN)**

- ➔ actively used in high energy physics  
(e.g. [arXiv:1712.1032](#), [arXiv:2209.07559](#),  
[EPJC 80 \(2020\) 688](#), [arXiv:2210.14245](#))

FIG. 2: Three-dimensional representation of a 10 GeV  $e^+$  incident perpendicular to the center of the detector. Not-to-scale separation among the longitudinal layers is added for visualization purposes.



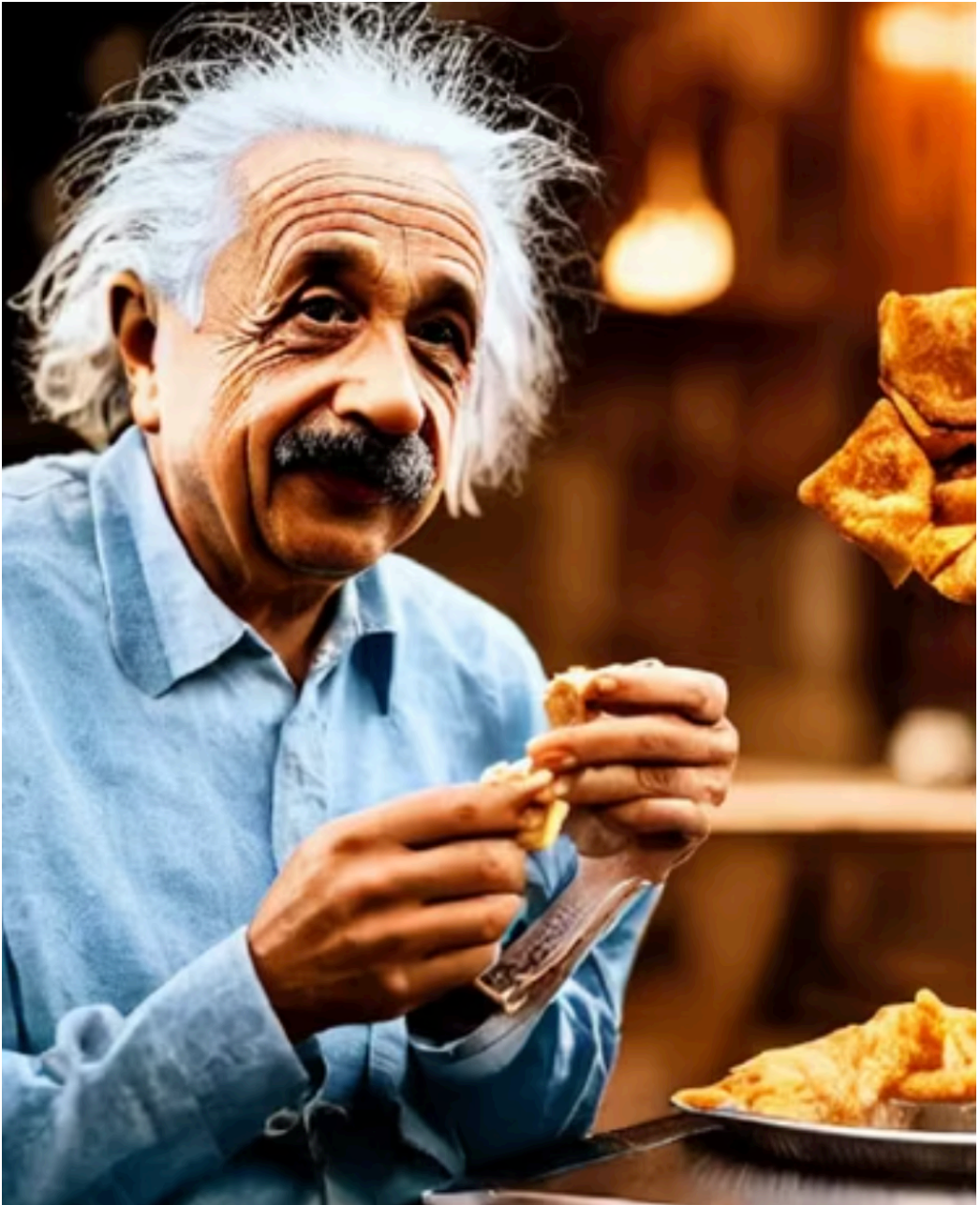
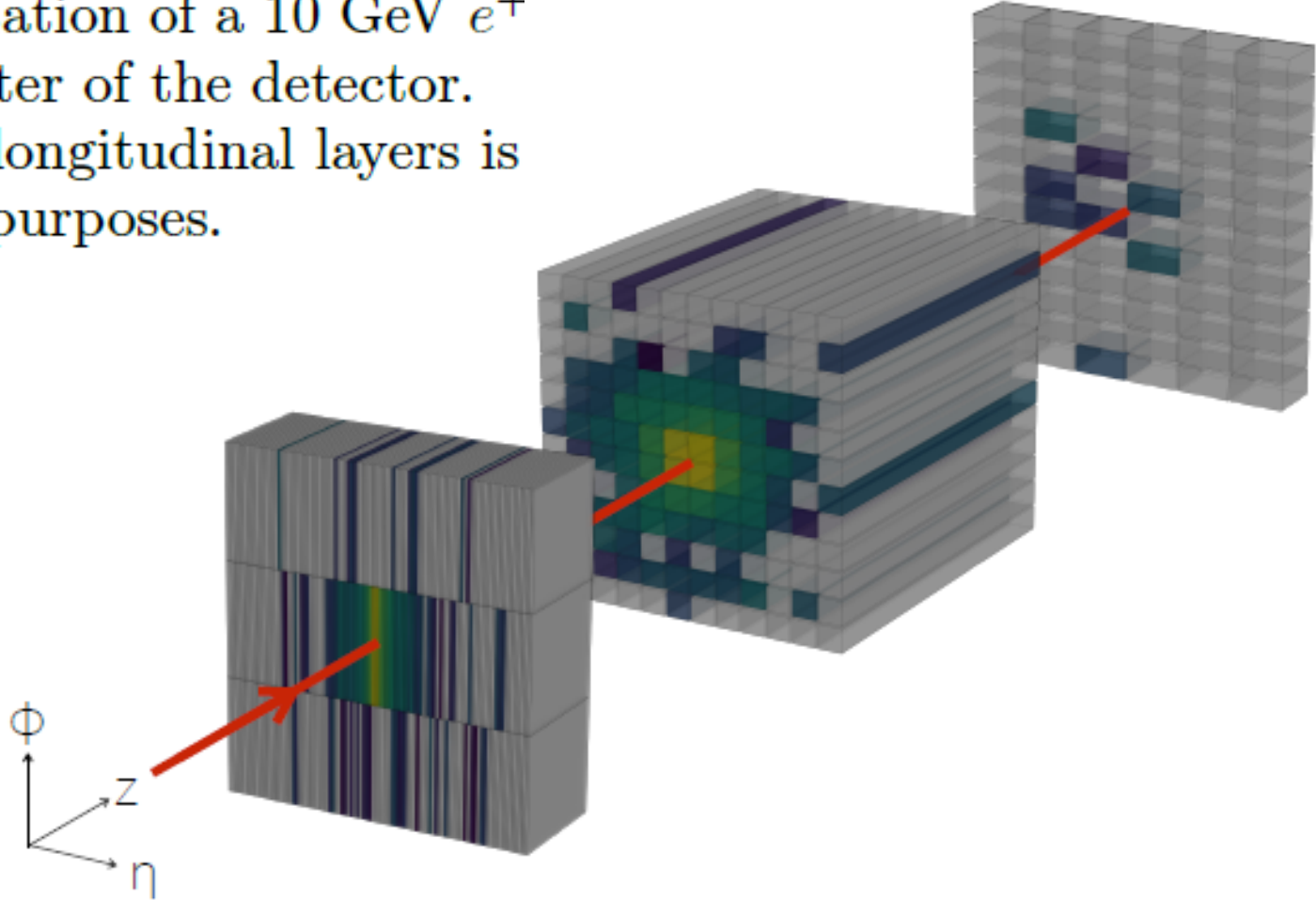
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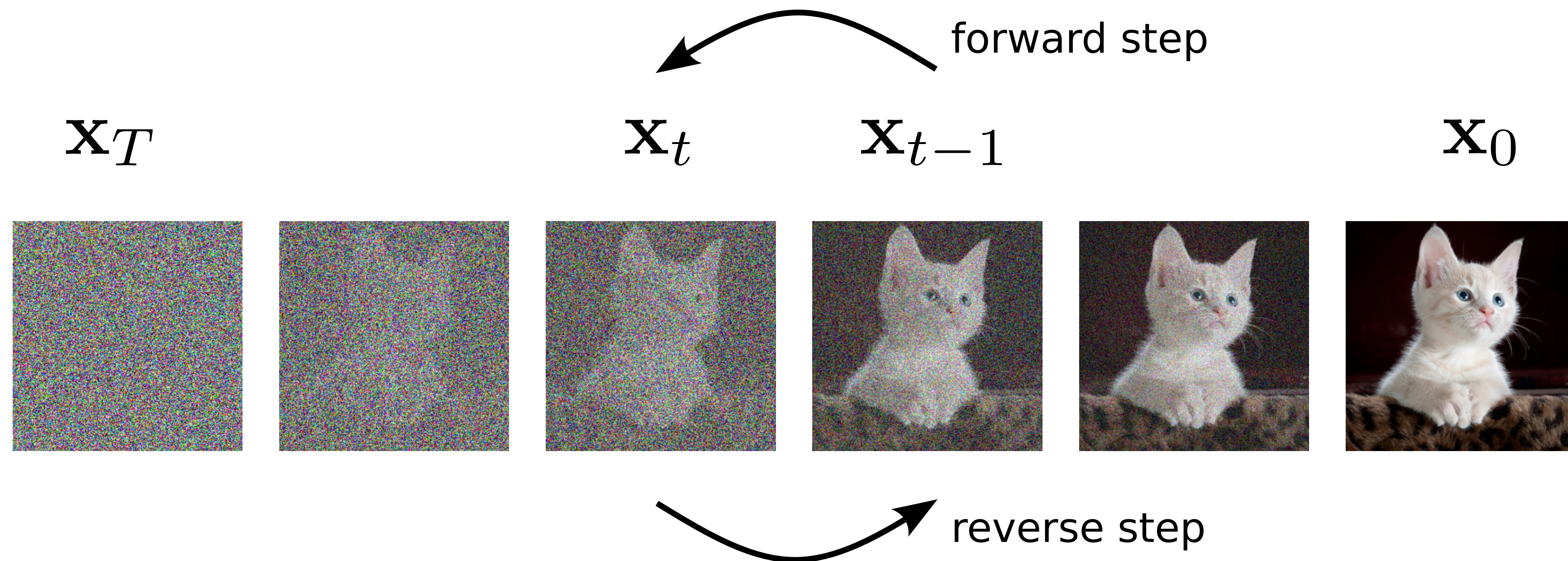
- **Diffusion Models:** text-to-image generation in industry  
(e.g. StableDiffusion, Midjourney, Dalle-2)

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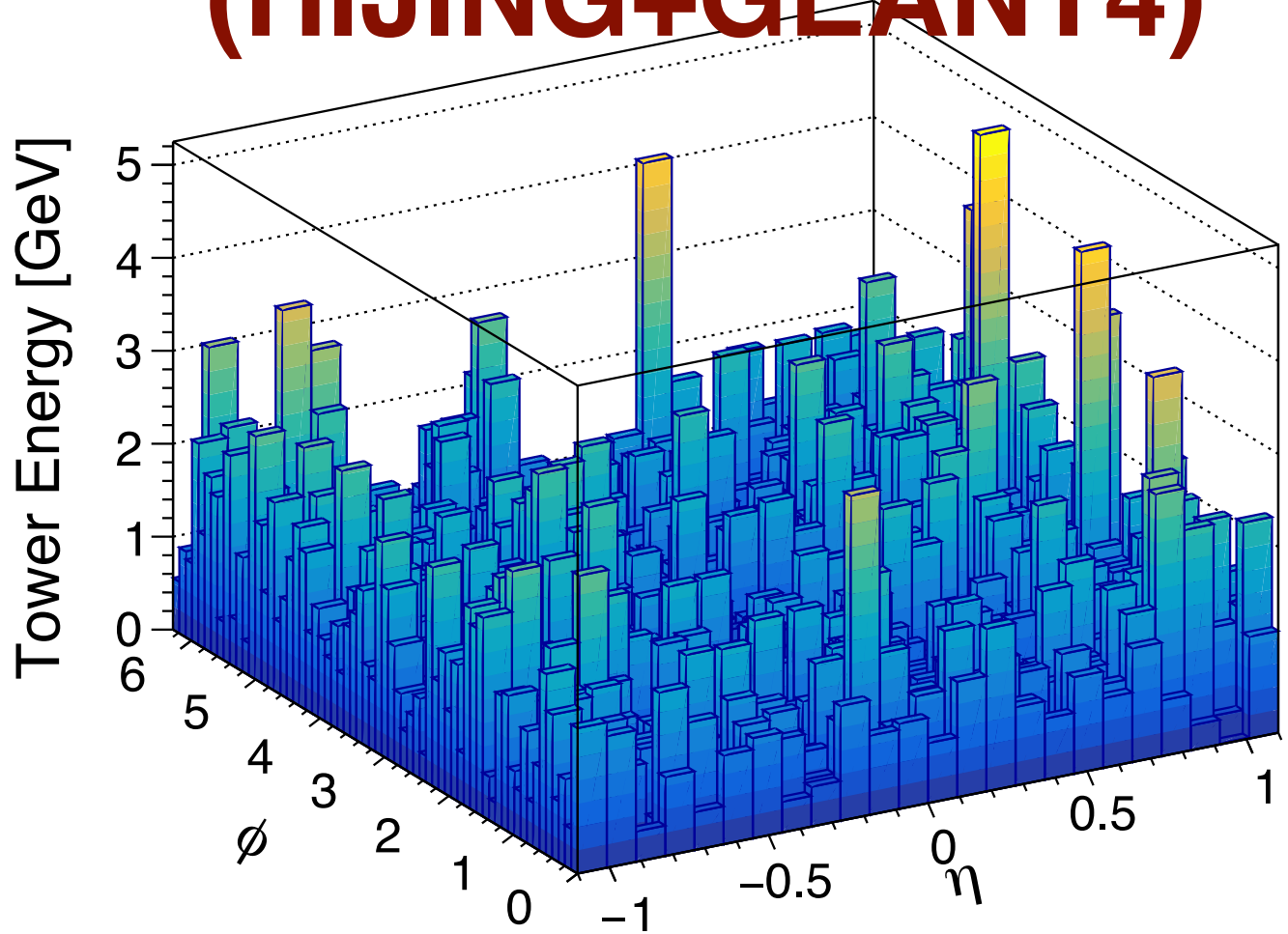
# Denoising Diffusion Probabilistic Model (DDPM)

- DDPM provides *high quality data from random noise*
- **Forward** process: add random gaussian noise
- **Reverse** process: use neural network and generate data
- In real application,  $O(1,000)$  steps are used

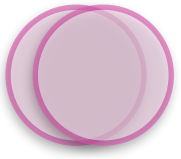


# Display of Generated Events

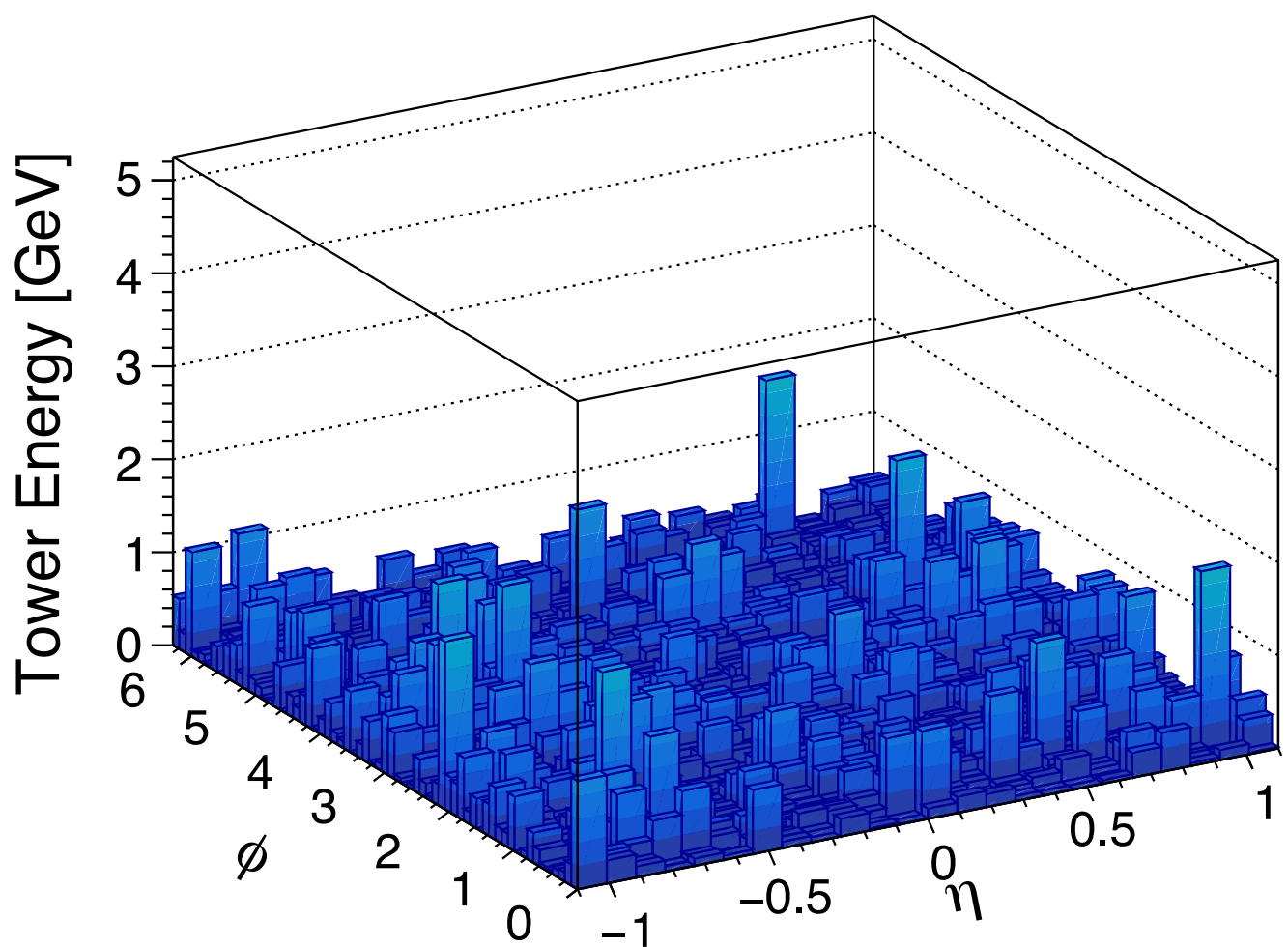
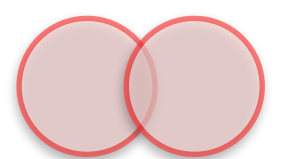
**Training sample  
(HIJING+GEANT4)**



**0-10%  
Centrality**

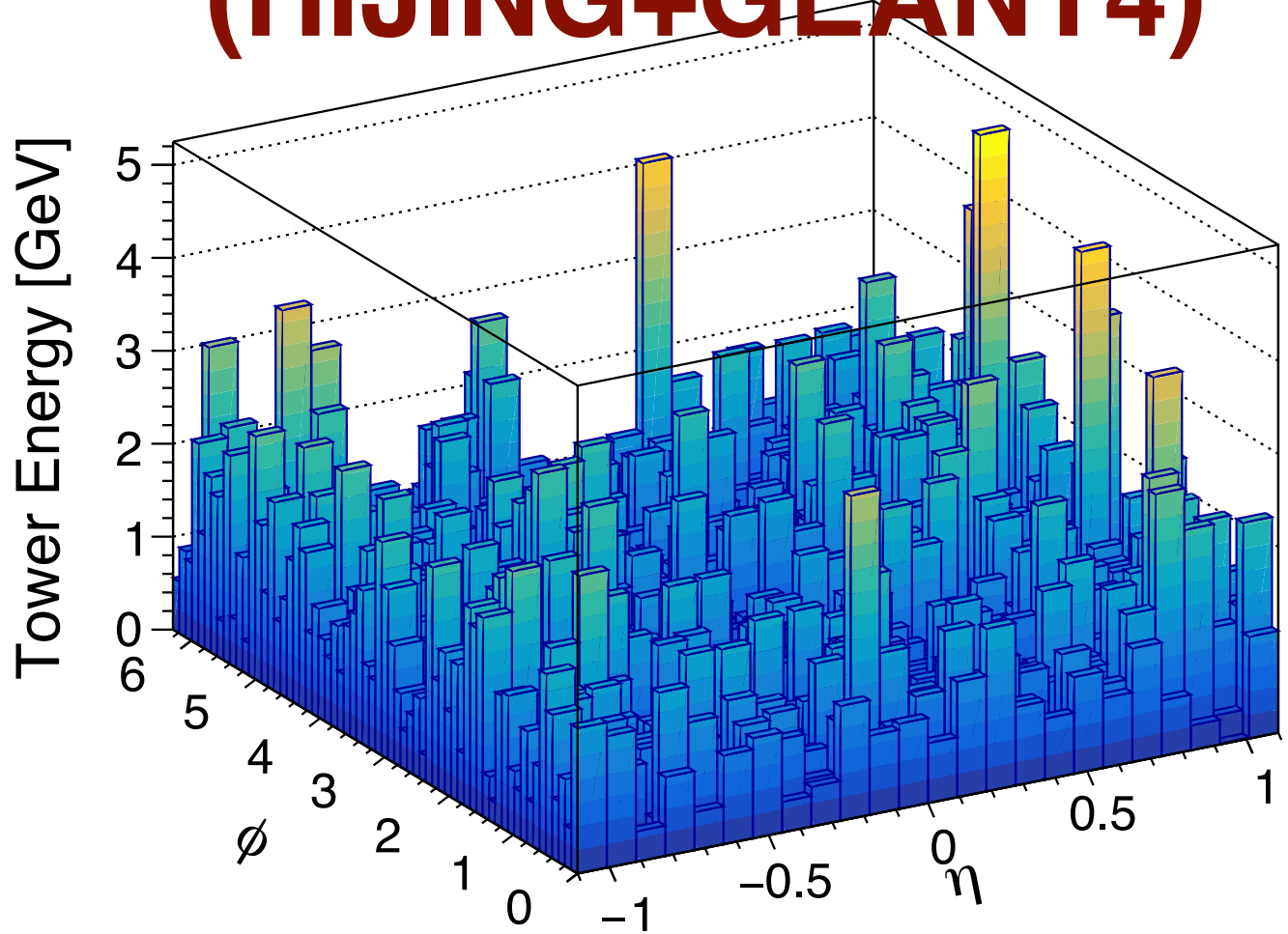


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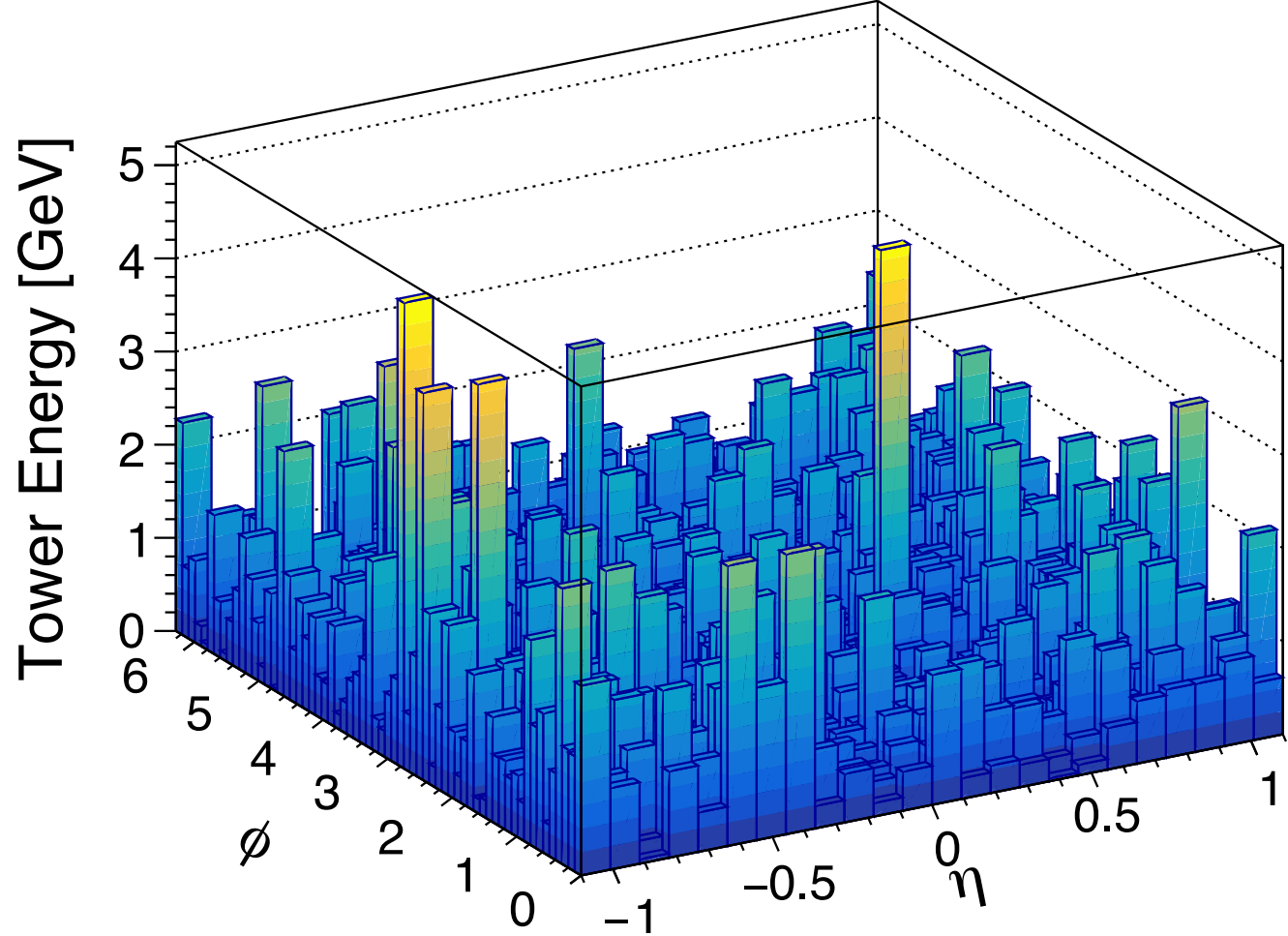


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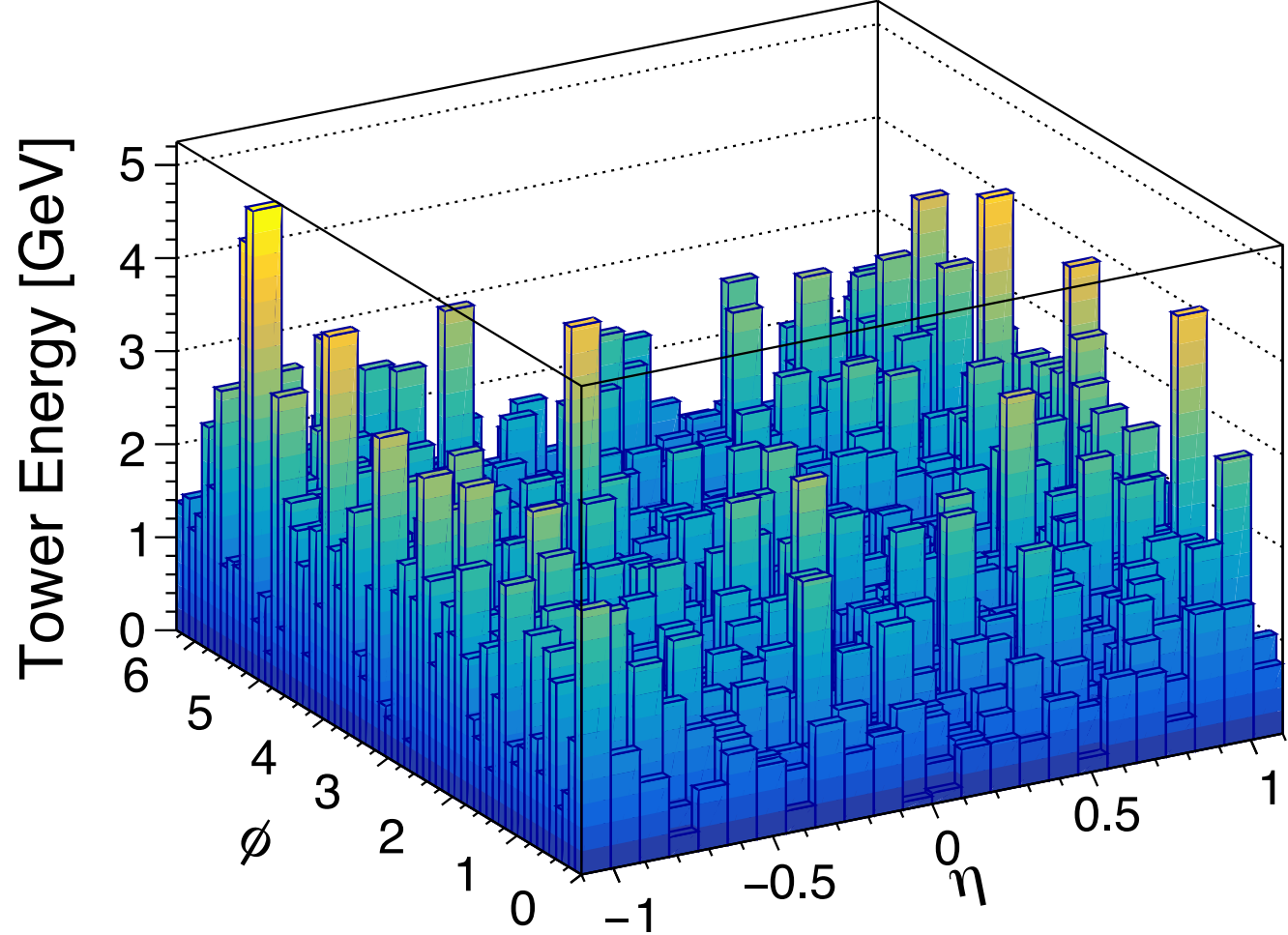
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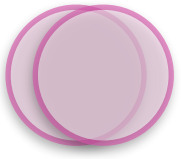
**Generated (DDPM)**



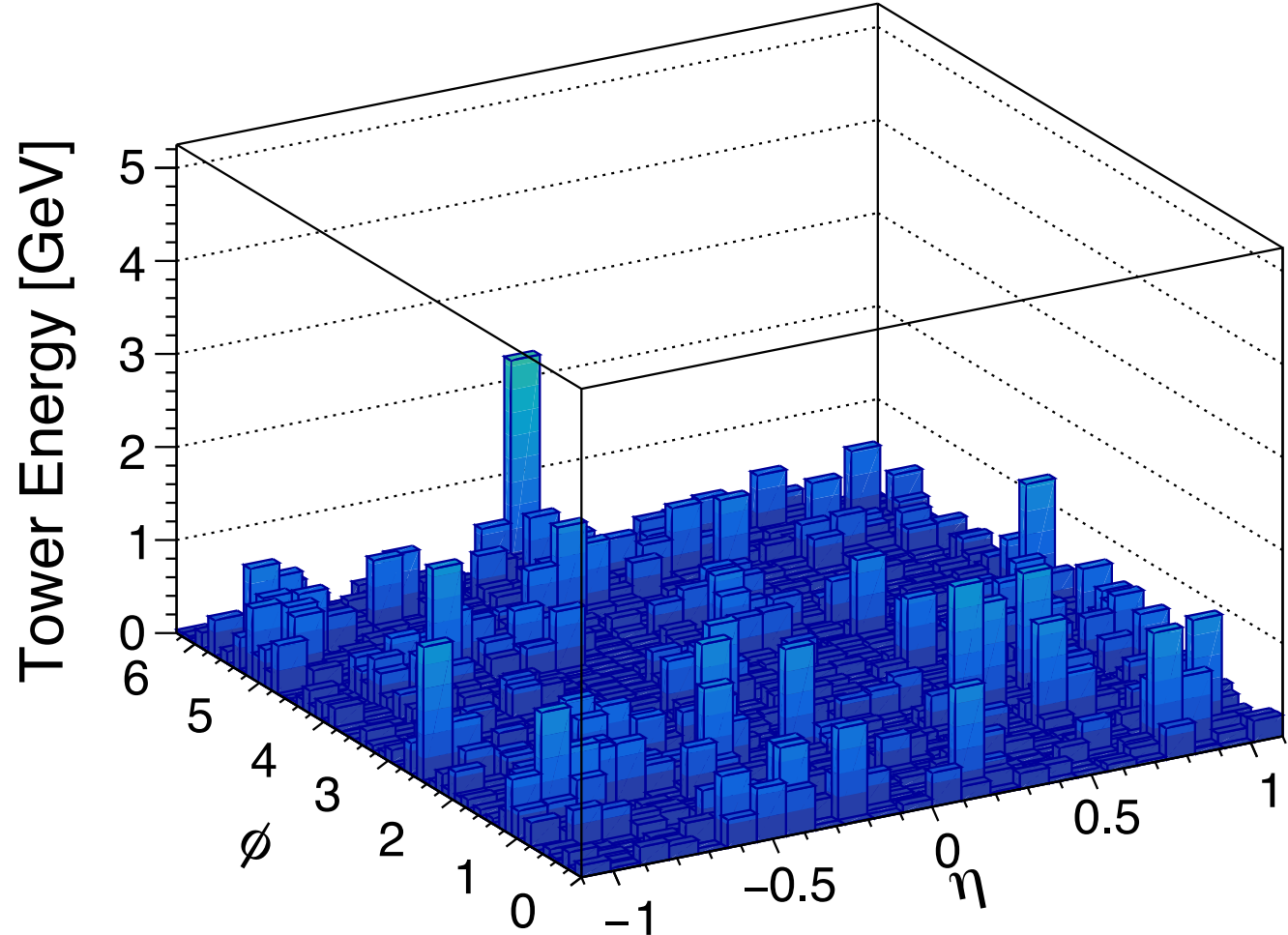
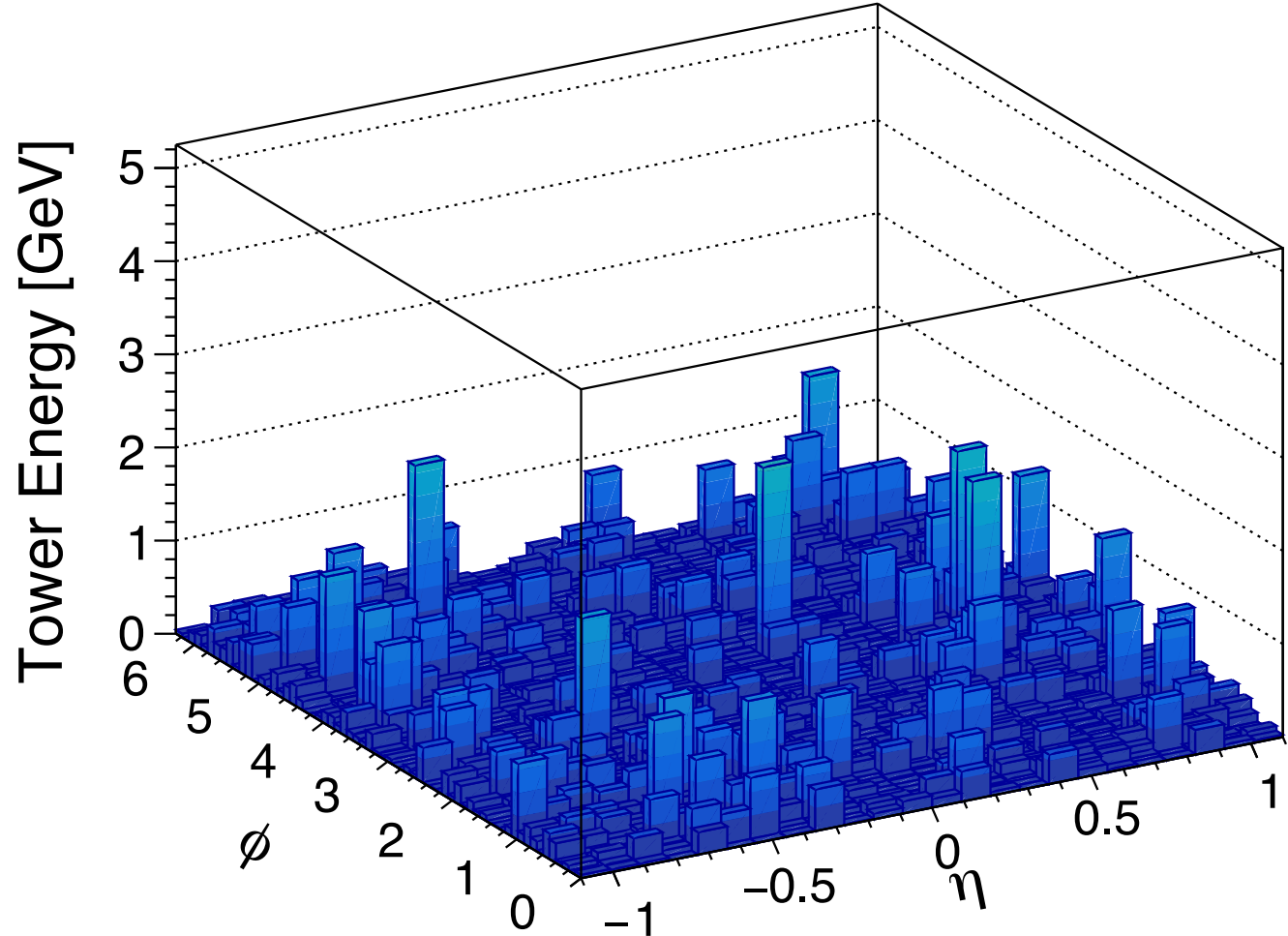
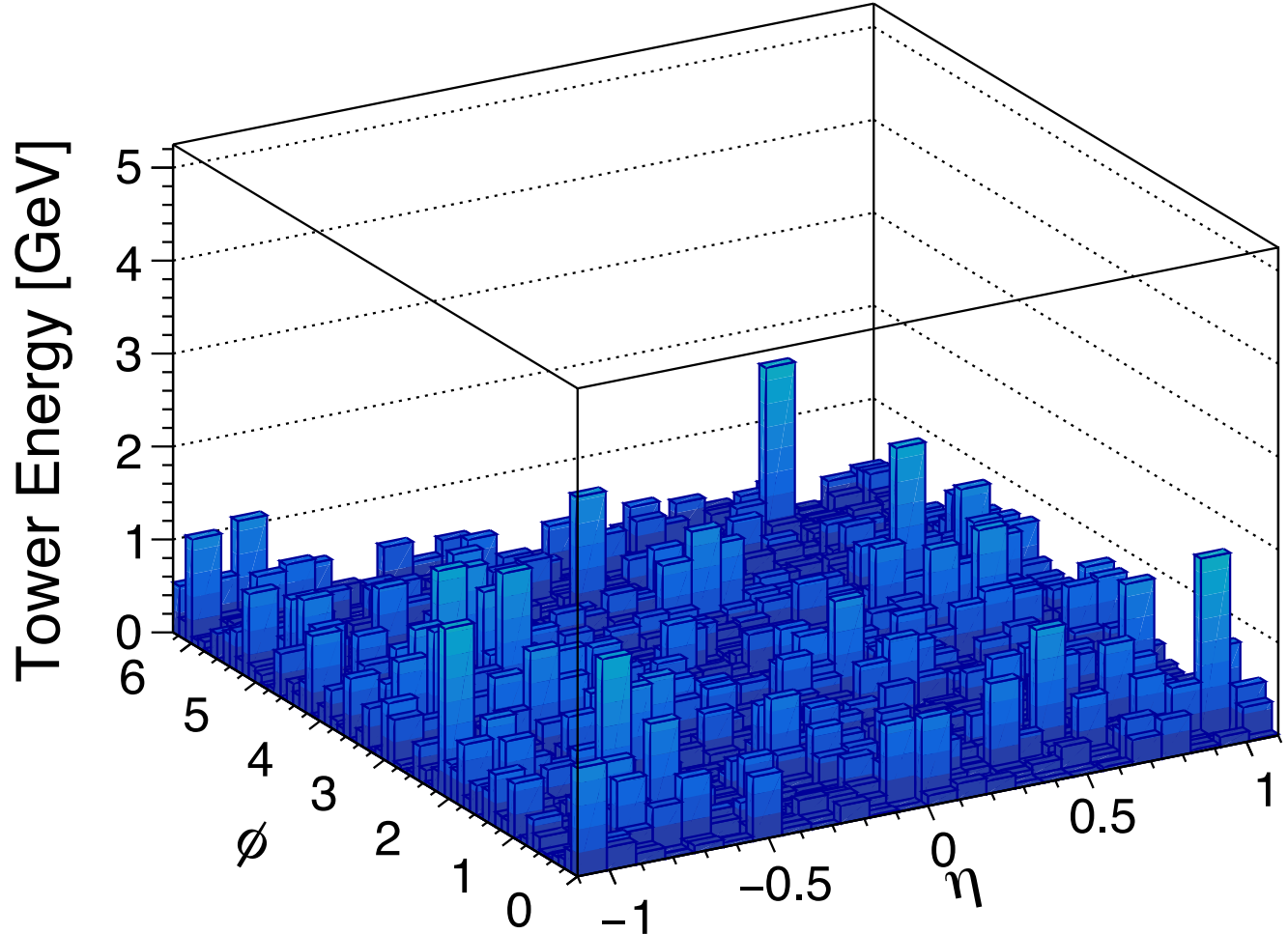
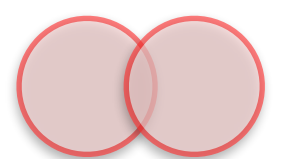
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**40-50%  
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# Performance: Transverse Energy (0-10%)

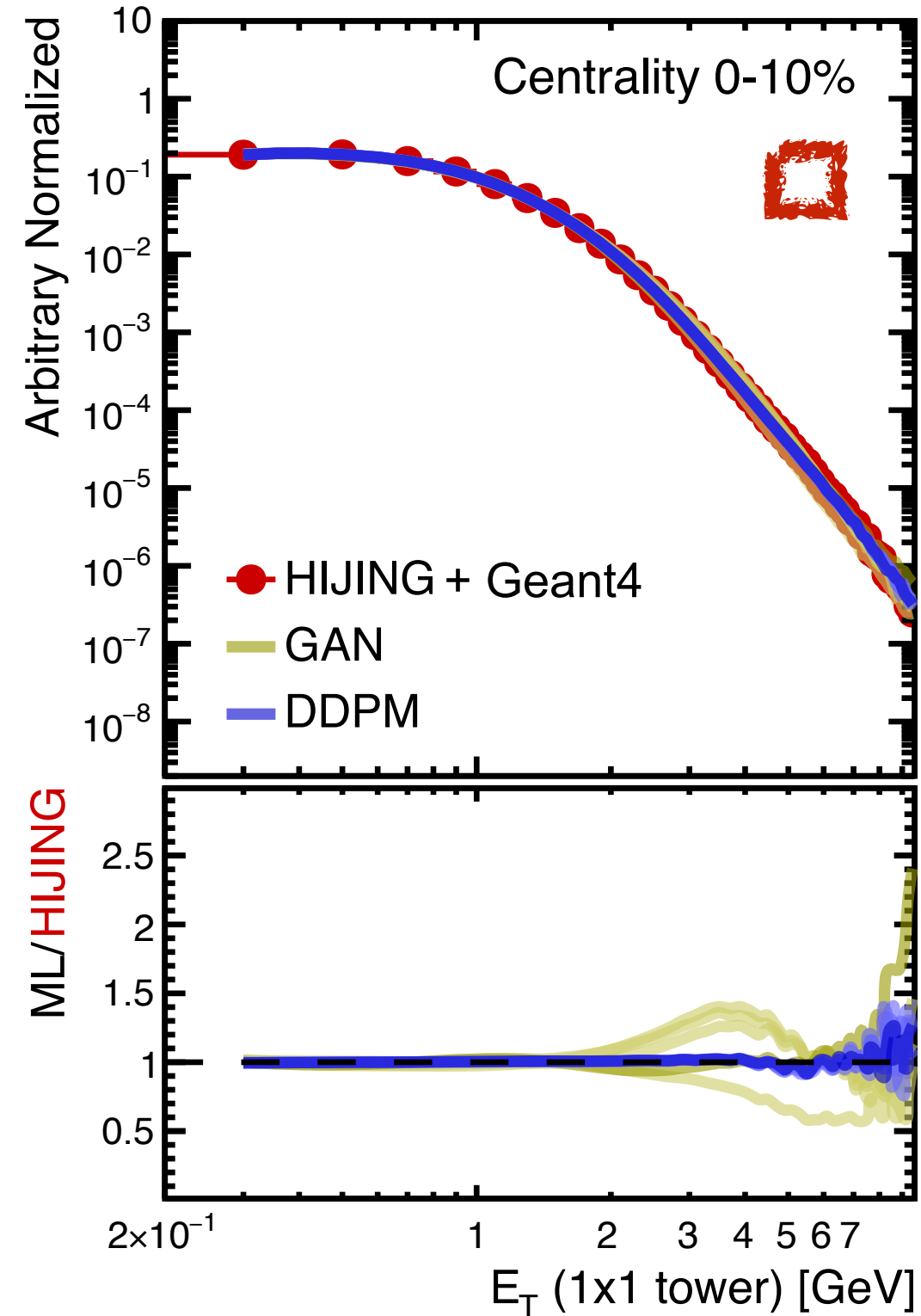
1x1 Tower

4x4 Tower

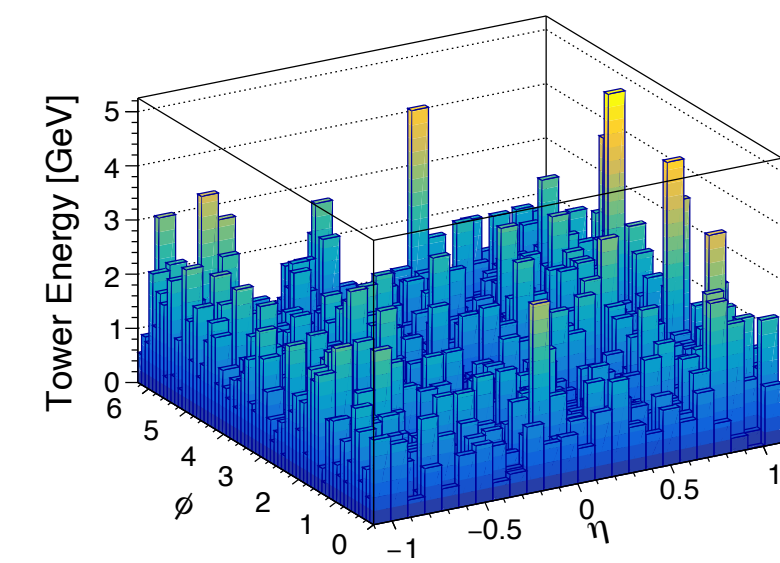
7x7 Tower

11x11 Tower

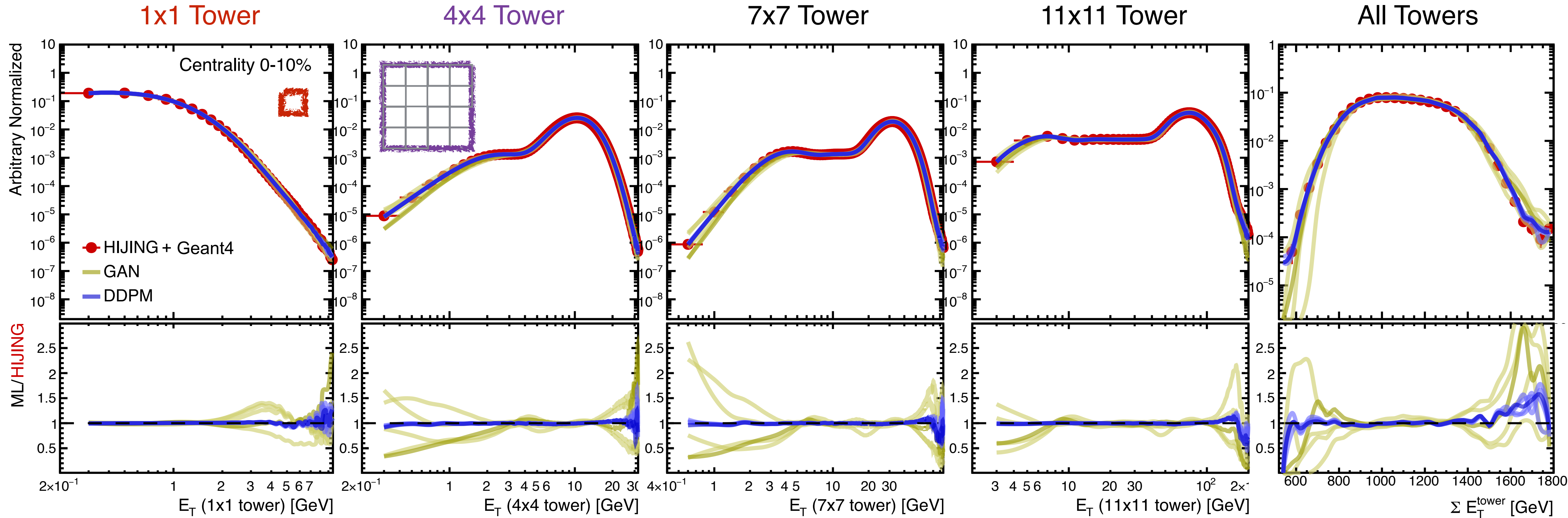
All Towers



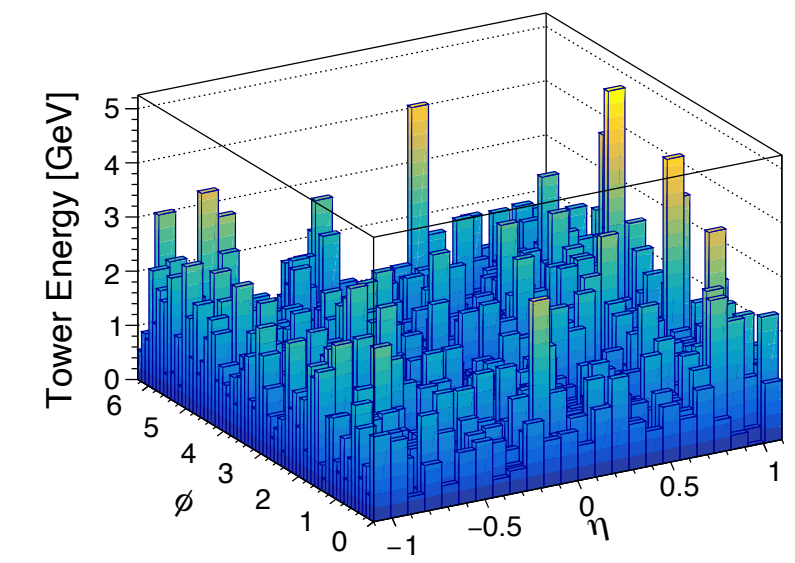
- Each model is retrained 5 times with different random seeds
- **HIJING+Geant4** used as training data (600k events) and testing data (100k events)
- Both **DDPM** and **GAN** reproduce the data distribution where the data are abundant
- **DDPM** outperforms **GAN** in overall distribution w/ great stability and accuracy



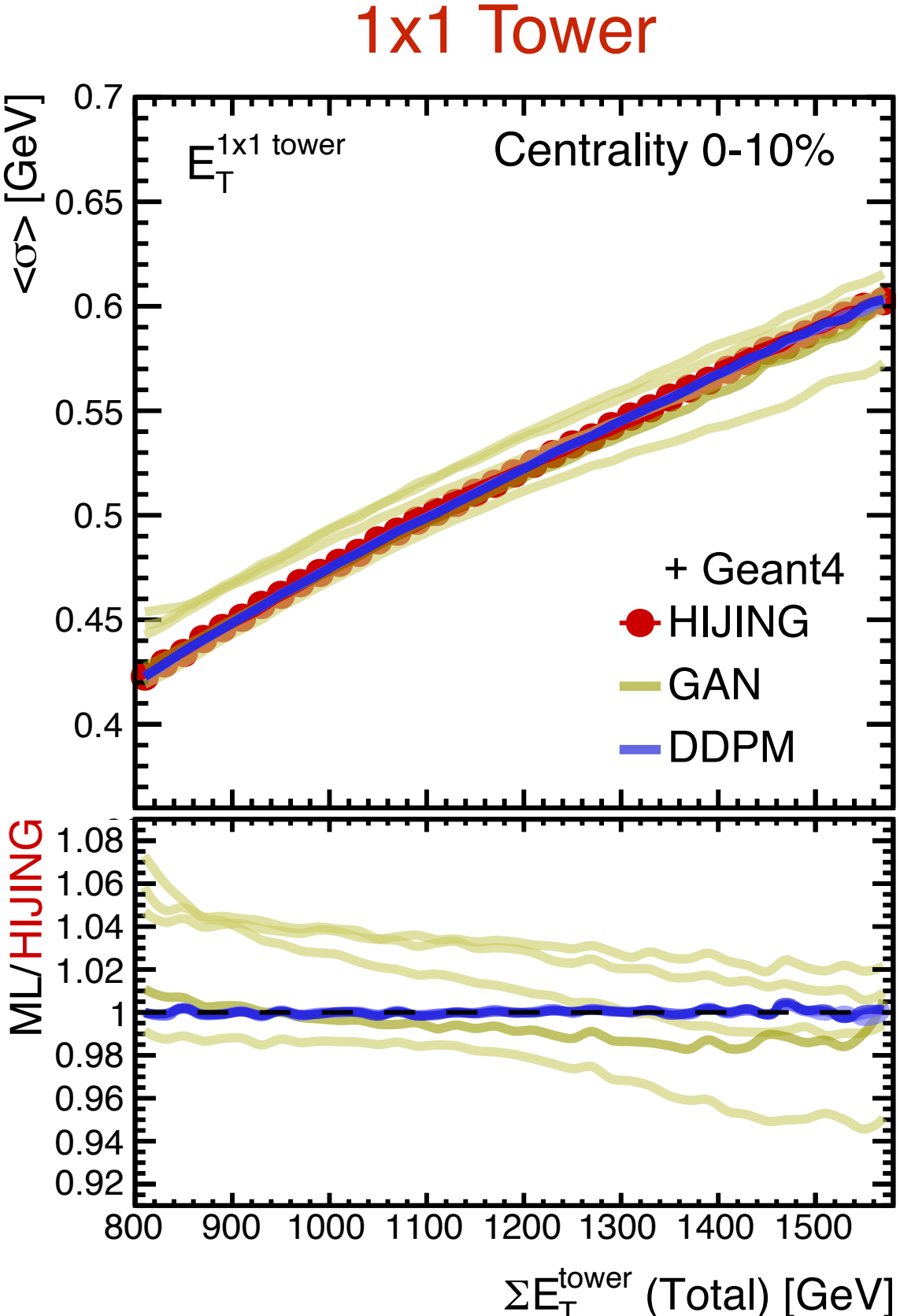
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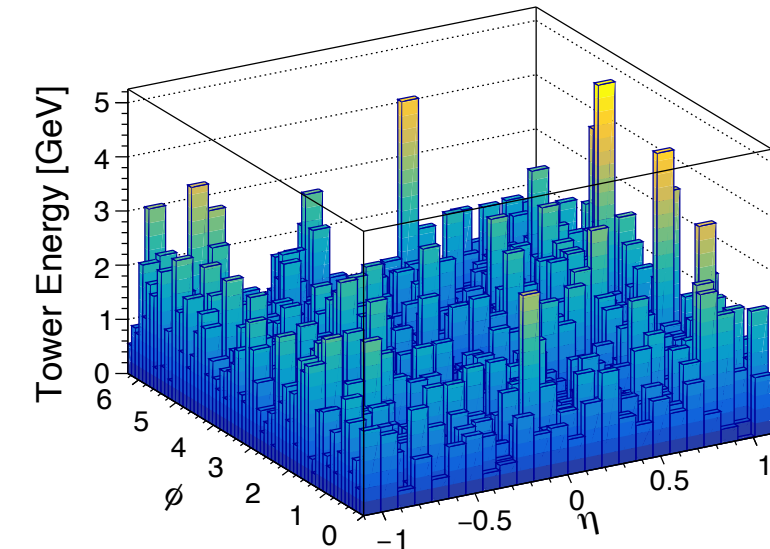


4x4 Tower

7x7 Tower

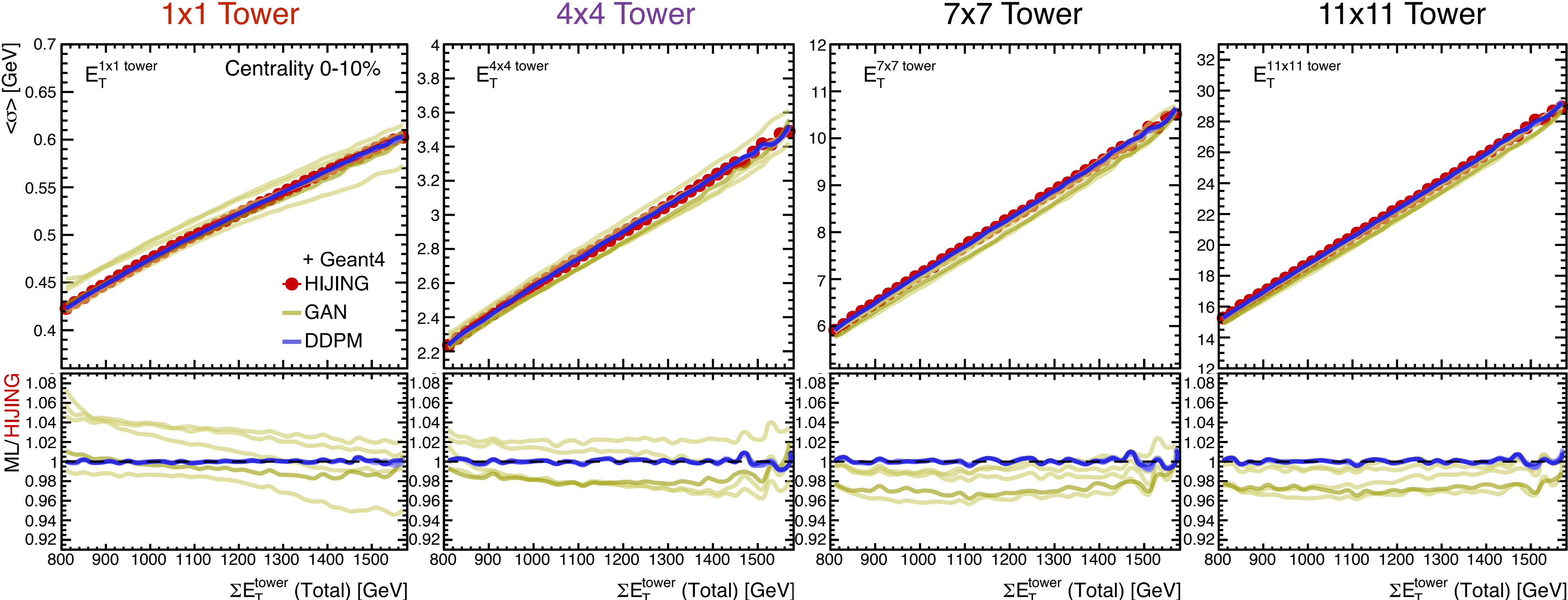
11x11 Tower

- **GAN** fails to describe fluctuation
- **DDPM** outperforms **GAN** w/ great stability, a few percent-level accuracy

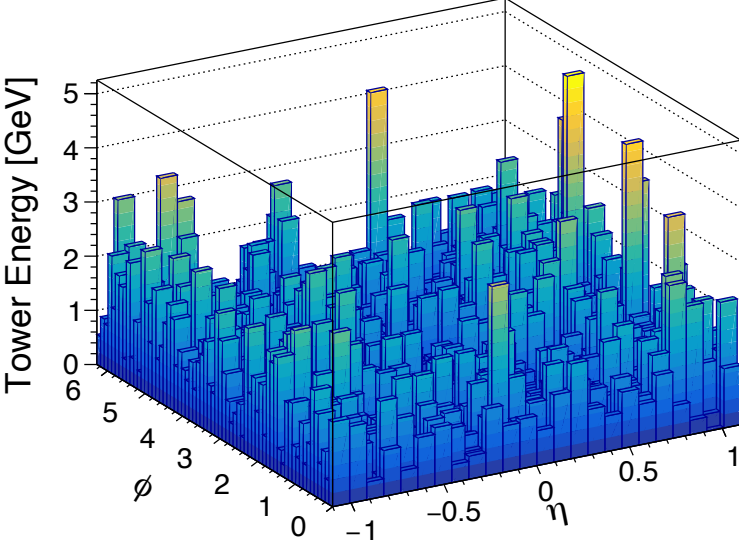




# Performance: Transverse Energy Fluctuation (0-10%)



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# Performance: Transverse Energy (40-50%)

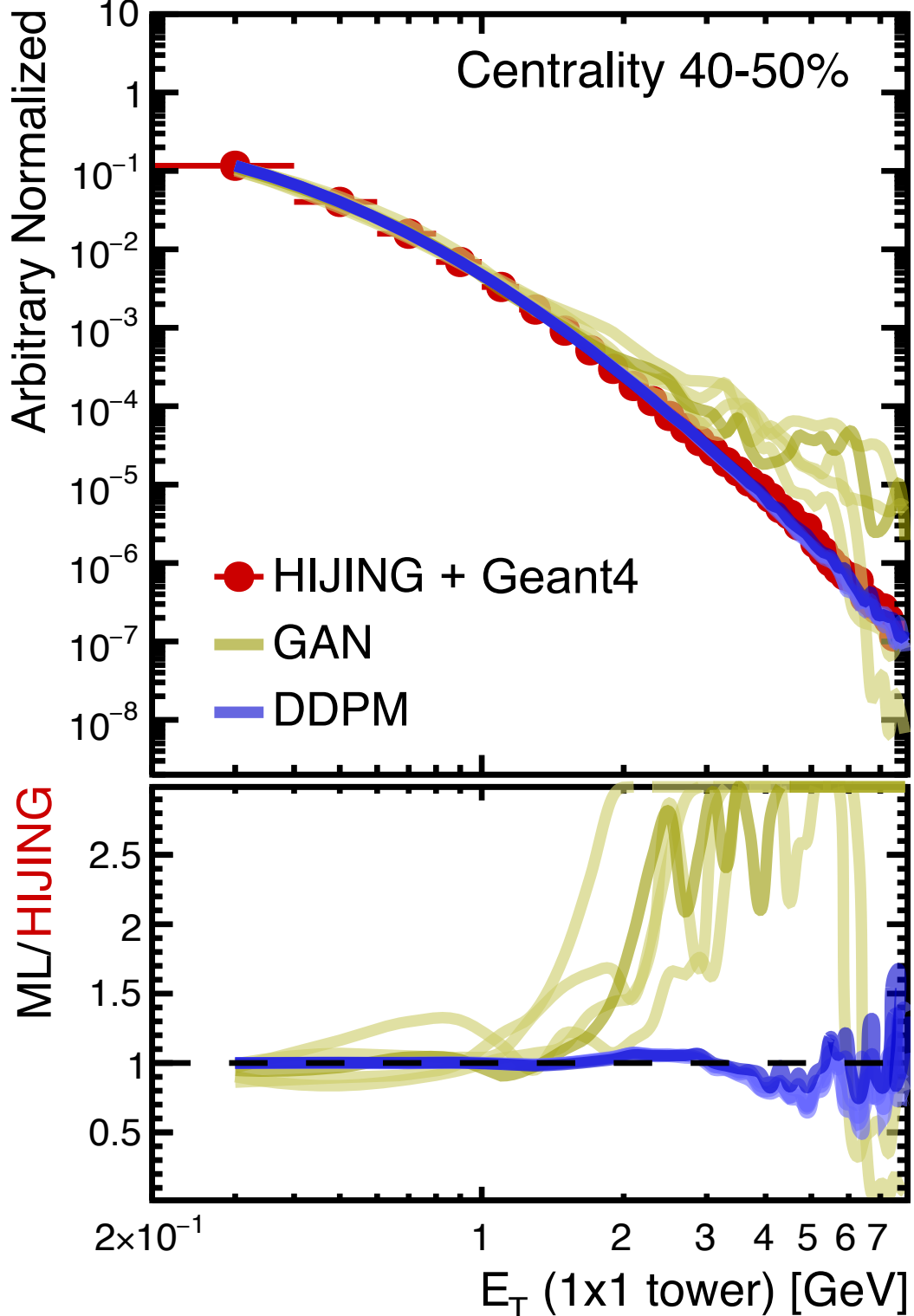
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4x4 Tower

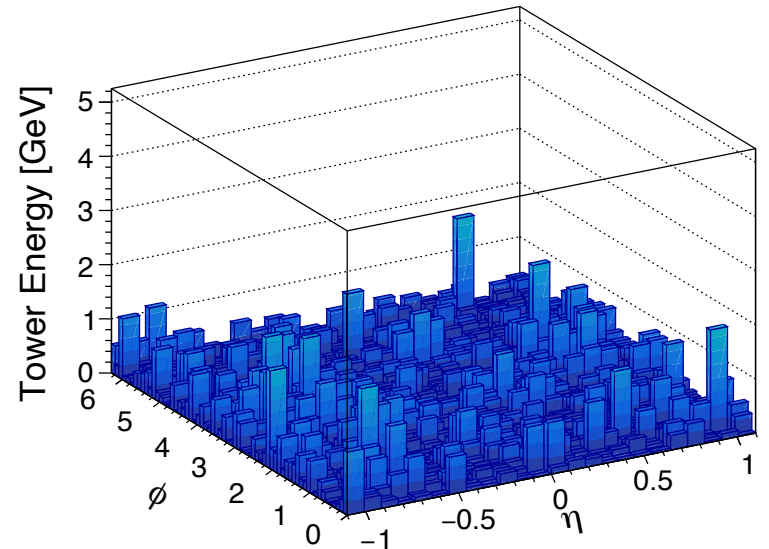
7x7 Tower

11x11 Tower

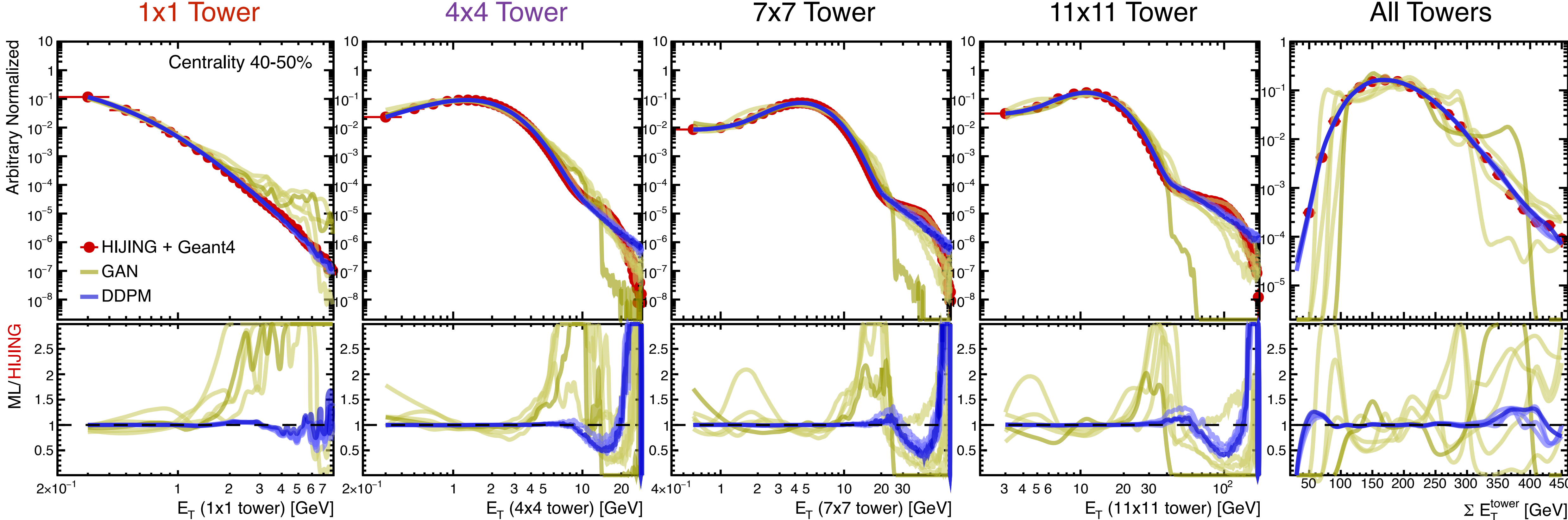
All Towers



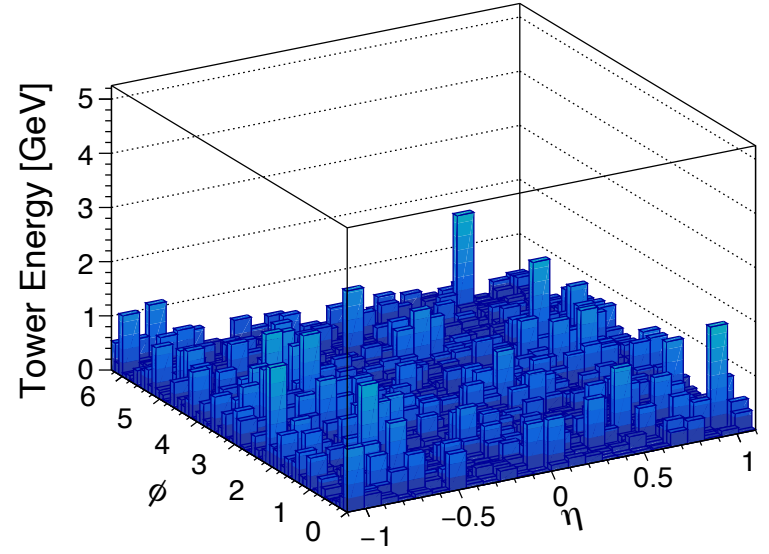
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  - ➔ great stability, good agreement with HIJING+G4 at high probability region



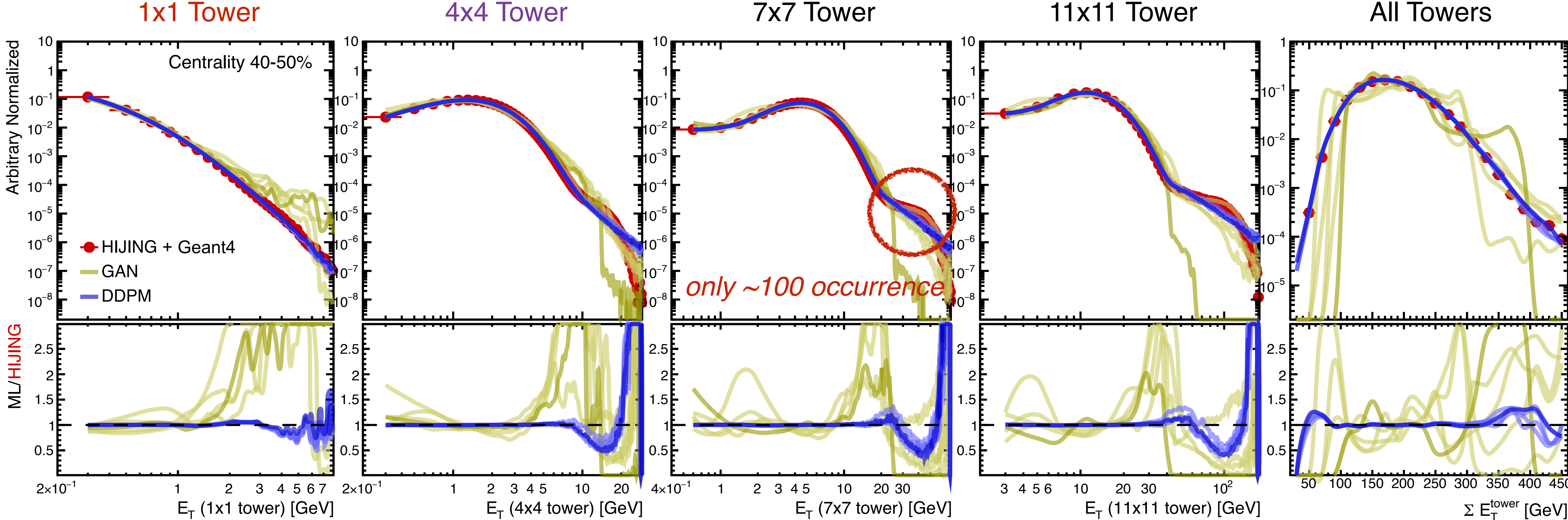
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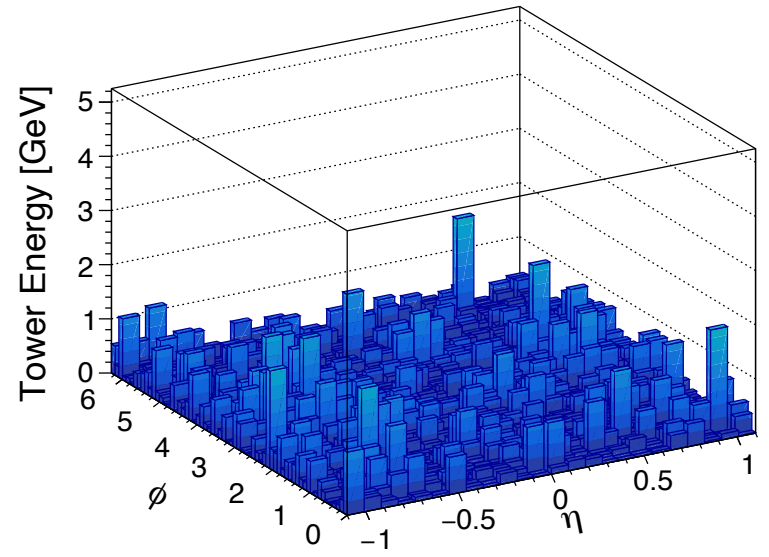
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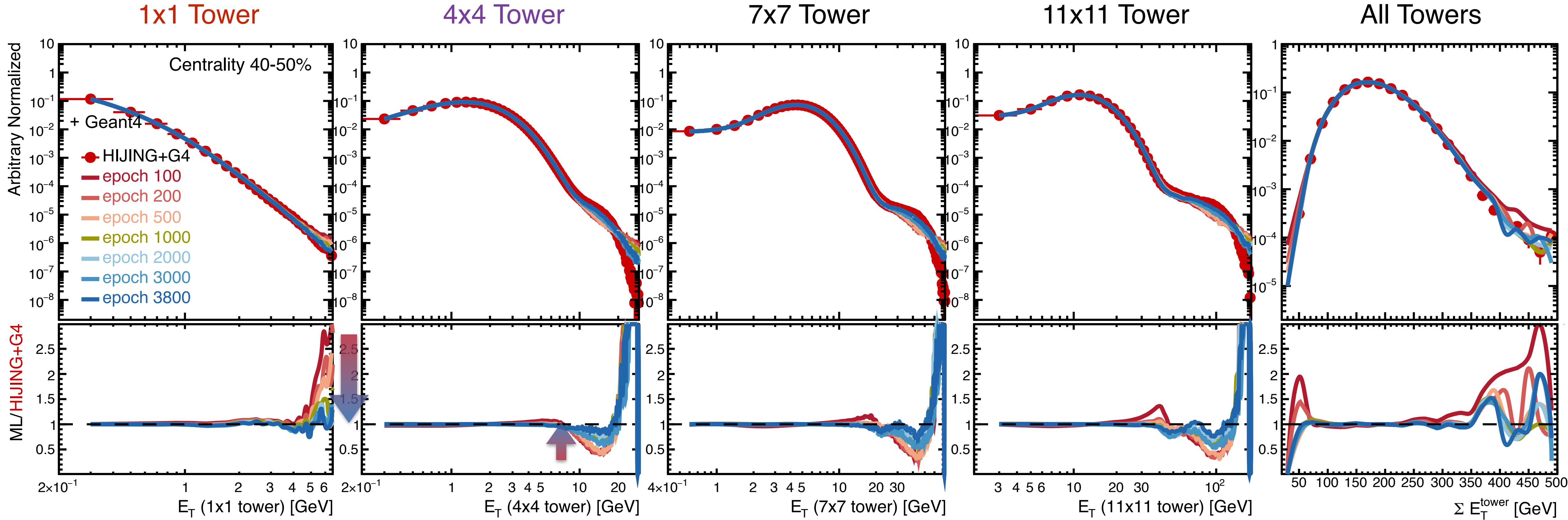
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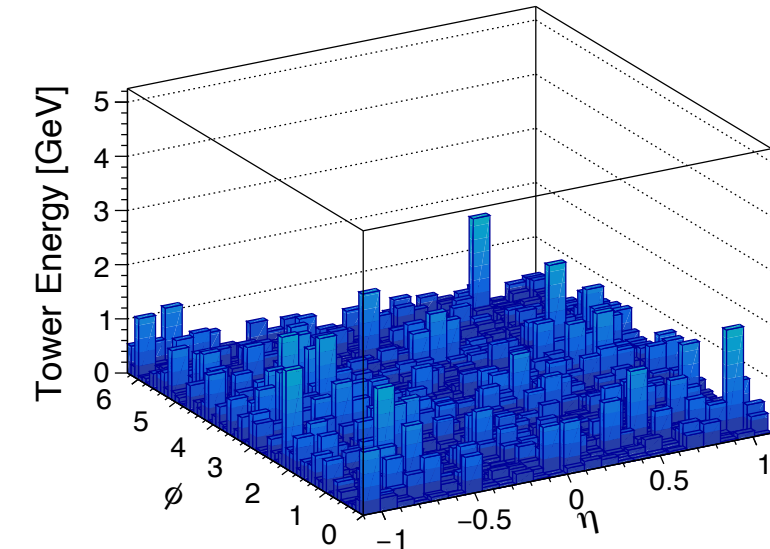
- DDPM outperforms GAN
  - ➔ great stability, good agreement with HIJING+G4 at high probability region
- Non-gaussian rare tail at the high energy region → challenge to reproduce



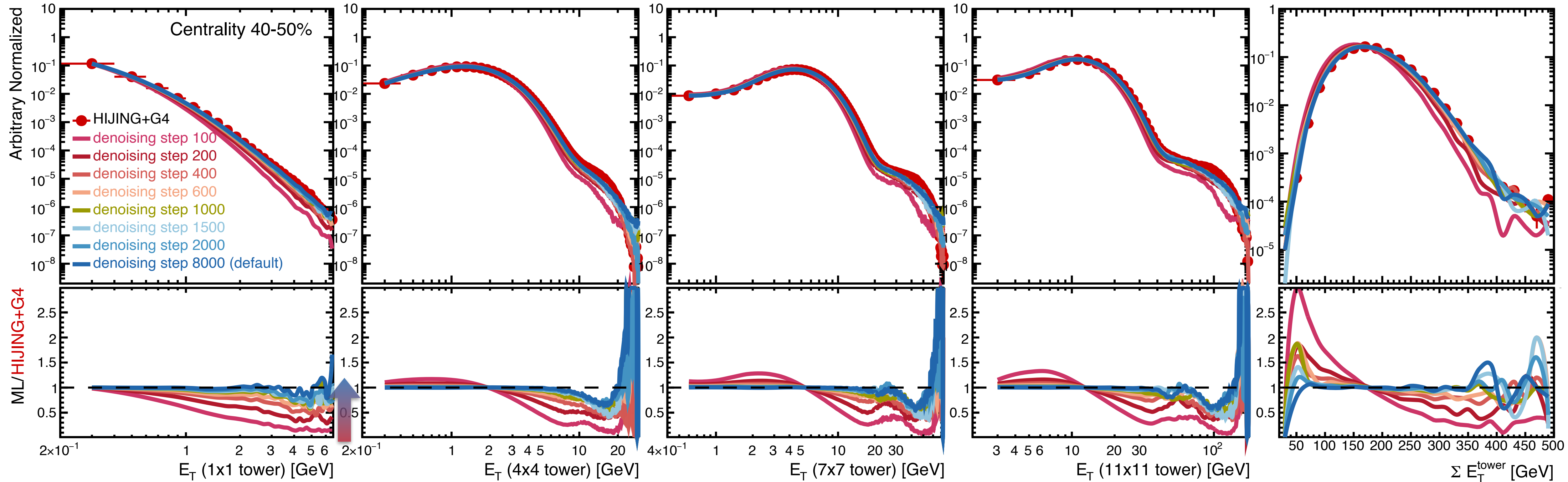
# Trade-off between Training time and Fidelity



- epoch ~ training duration
- **DDPM** models with the **higher epochs** give **better performance!**
- ➔ but, the **higher the epochs**, the *longer the training time*



# Trade-off between Generation time and Fidelity



- **DDPM** models with the **higher de-noising steps** give **better performance!**  
➔ but, the **higher the de-noising**, the *longer the generation time*

# How long does it take to simulate a large sample?

	Generating time	Speedup	CPU/GPU
HIJING + GEANT4 (Conventional)	40 minutes / event	1	Single CPU
DDPM	1.34 s / event	~1,800X	NVIDIA RTX A6000
GAN	0.42 ms / event	~5,700,000X	NVIDIA RTX A6000

- **GAN** is faster, but the **DDPM** exhibits high fidelity in describing the truth ground (**HIJING+GEANT4**)
- **DDPM** provide a speedup of  $O(100)$ , considering a 32-core CPU equivalent to a GPU

# Conclusion and Future work

- Simulations of high energy nuclear experiments
  - ➔ **highly complex** and **computationally intensive**
  - ➔ *both fidelity and speed is important*



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  - ➔ **highly complex** and **computationally intensive**
  - ➔ *both fidelity and speed is important*
- **Diffusion model (DDPM)** was used to generate the whole-event full-detector simulated calorimeter data in high fidelity for the first time in heavy ion collisions
  - ➔ **GAN** used as a reference
  - ➔ **DDPM** outperforms **GAN** for scientific fidelity
  - ➔ trade-off found between training / generation duration and the quality of reproducing the rare feature

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  - ➔ trade-off found between training / generation duration and the quality of reproducing the rare feature
- **Outlook**
  - ➔ future work includes improvement of performance in the region where data are rare
  - ➔ using diffusion model to study rare probes (e.g. jets) in heavy ion collisions

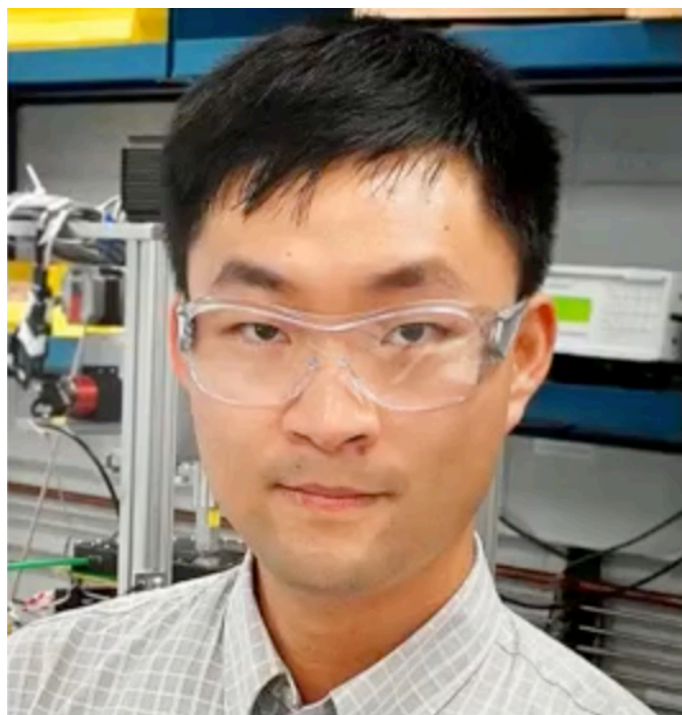
# Our Team



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Dmitrii Torbunov



Jin Huang



Yihui Ren

- Contacts: {ygo, dtorbunov, jhuang, yren}@bnl.gov



Tim Rinn



Yi Huang



Haiwang Yu



Shinjae Yoo



Meifeng Lin



Brett Viren

### **Acknowledgement**

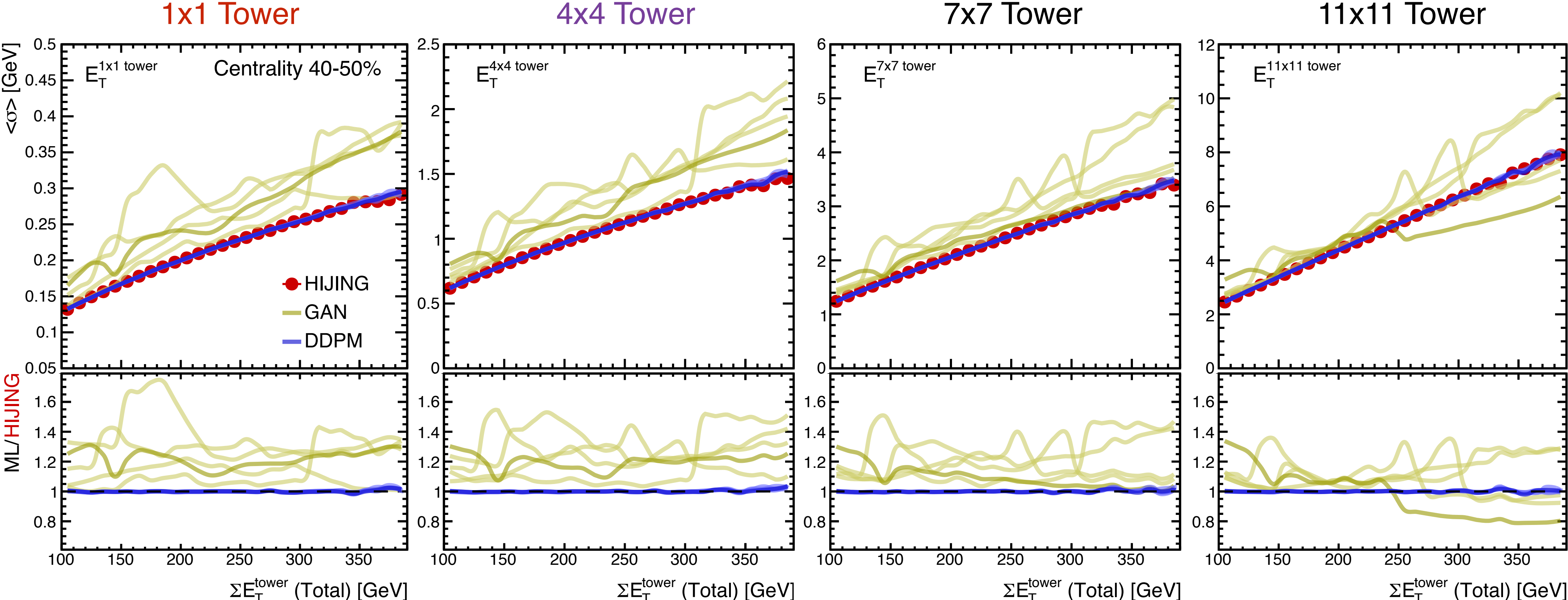
- *The LDRD Program at Brookhaven National Laboratory, sponsored by DOE's Office of Science under Contract DE-SC0012704, supported this work.*
- *We acknowledge sPHENIX. Its simulation data was used to demonstrate our algorithms.*

# BACKUP

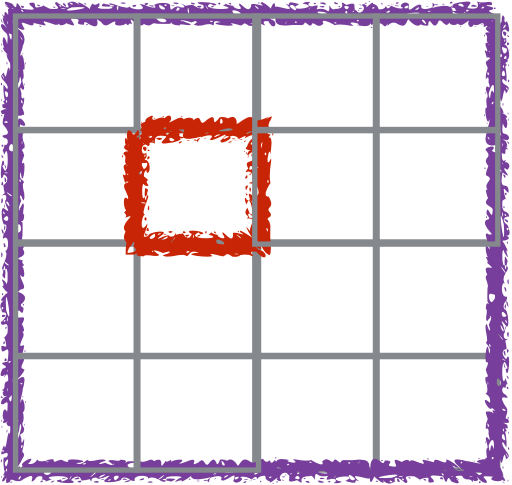
# DDPM Configuration

- number of diffusion steps  $T$ : default 8000 / variation [1000, 16000]
- variance schedule  $\beta_t$ : default 0.1 / variation [0.02, 0.2]
- training batch size: default 128 / variation [100, 12500]
- training steps per epoch: default 2000
- epoch: default 4000 / variation [100, 4000]
- training with the Adam optimizer with learning rate  $10^{-4}$
- trained with 600,000 events per each centrality bin
- tested with 100,000 events per each centrality bin
- neural network architecture (U-ResNet + Attention)
- depth/width of the model
  - ➔ U-Net encoder-decoder stage, channels per stage: 32, 64, 128  
each of which comprised of two ResNet blocks

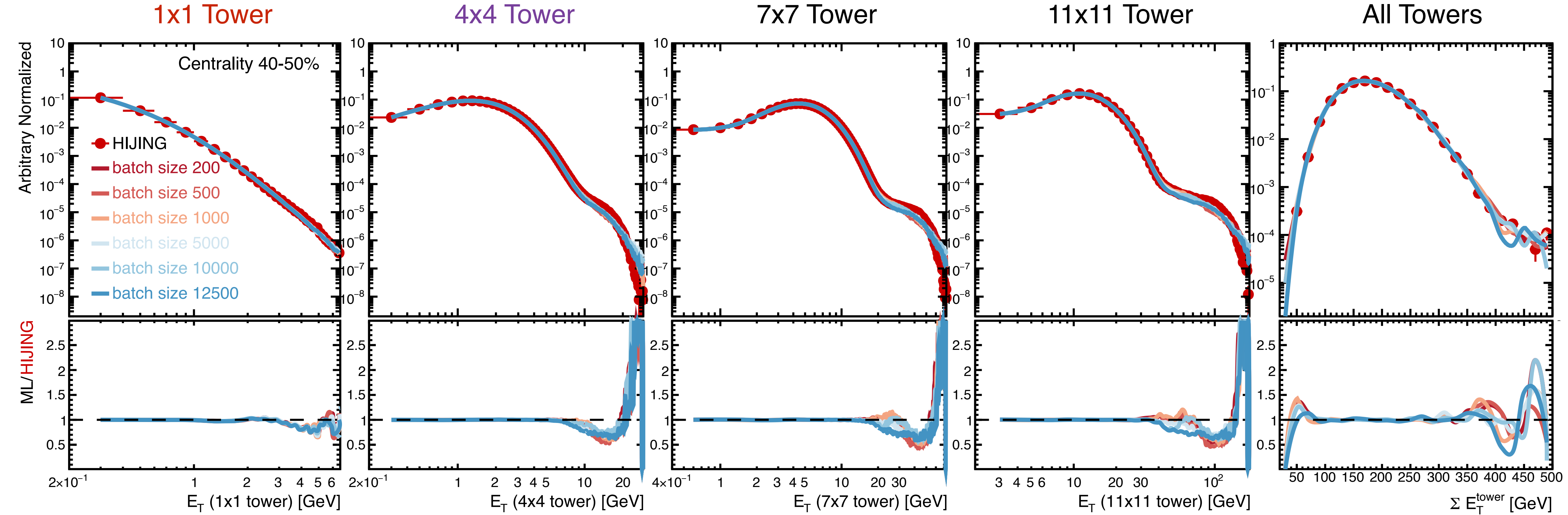
# Performance: Transverse Energy Fluctuation (40-50%)



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# Batch Size Dependence



- Batch size not only introduces different random seeds and but also changes variance schedule ( $\beta_t$ )

