

# LLNL FPY Modeling and Evaluation

Nicolas Schunck, Marc Verriere, Antonio Bjelcic, Pooja Siwach

Nuclear Data and Theory Group, Nuclear and Chemical Science Division, LLNL, Livermore CA 94550, USA

Petar Marevic

Theoretical Physics Department, University of Zagreb, 10000 Zagreb, Croatia

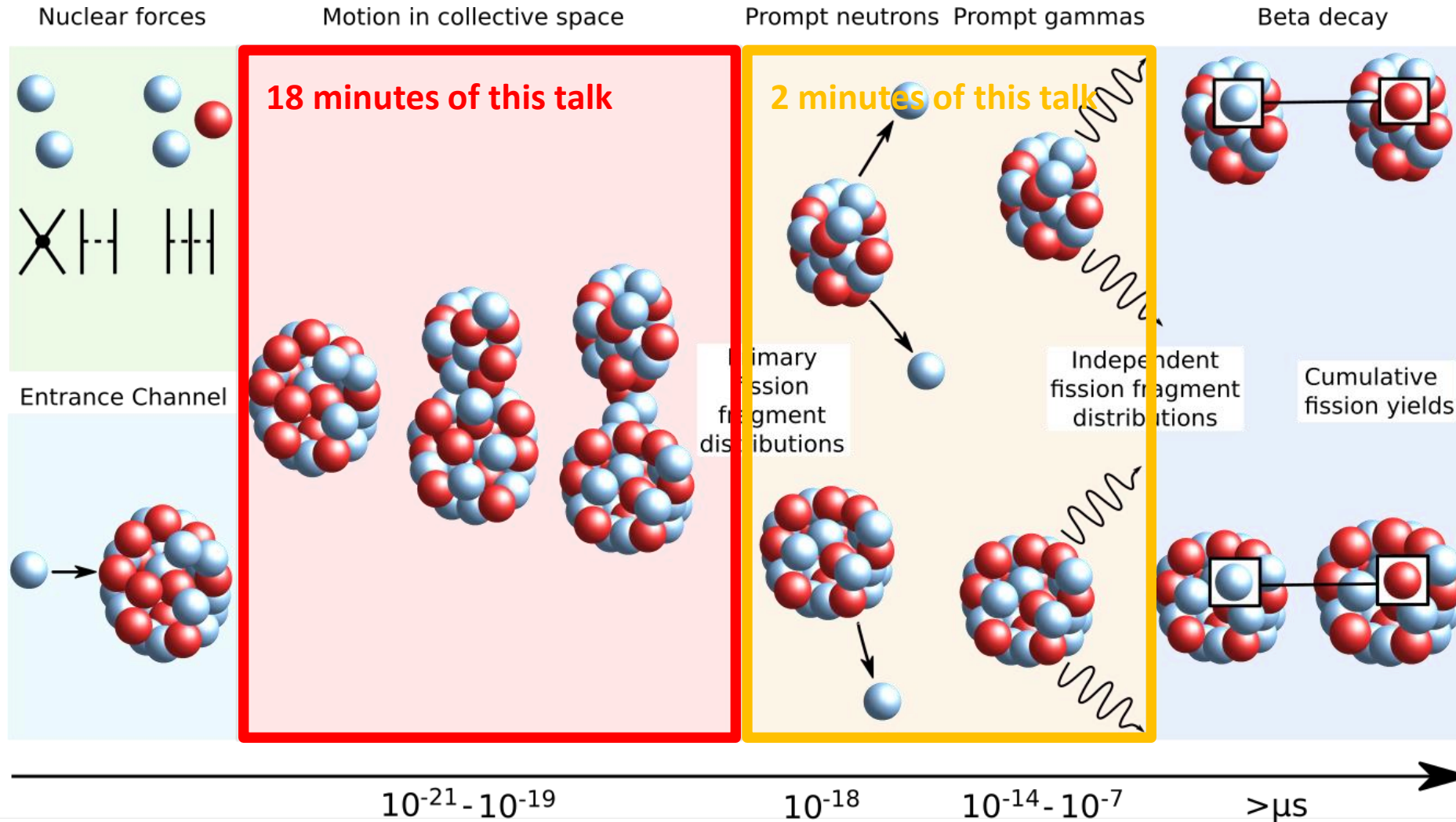


# Outline

- Fission modeling: Predictions of fission fragments initial conditions
  - Mass distribution of fission fragments: Plutonium isotopes (2D simulations)
  - Number of particles in fragments: Collective fluctuations on particle number
  - (Spin distributions: Combined AMP+PNP)
  - Total kinetic energy: Projection + direct Coulomb
- New computational capabilities
  - FPY: FELIX-3D (ASC/PEM L2 milestone)
  - Real-time Fission events: TDHFB solver
  - Evaluation: FETA framework

# Fission Science

Two major research areas for fission theory: cross sections (~ probabilities that fission happens) and fission products (includes neutrons, gammas, fragments, etc.)





# Fission Theory Pipeline

Physics-based fission models involve calculations of static nuclear properties (=nuclear structure) and time-dependent simulations (=large-amplitude collective motion)

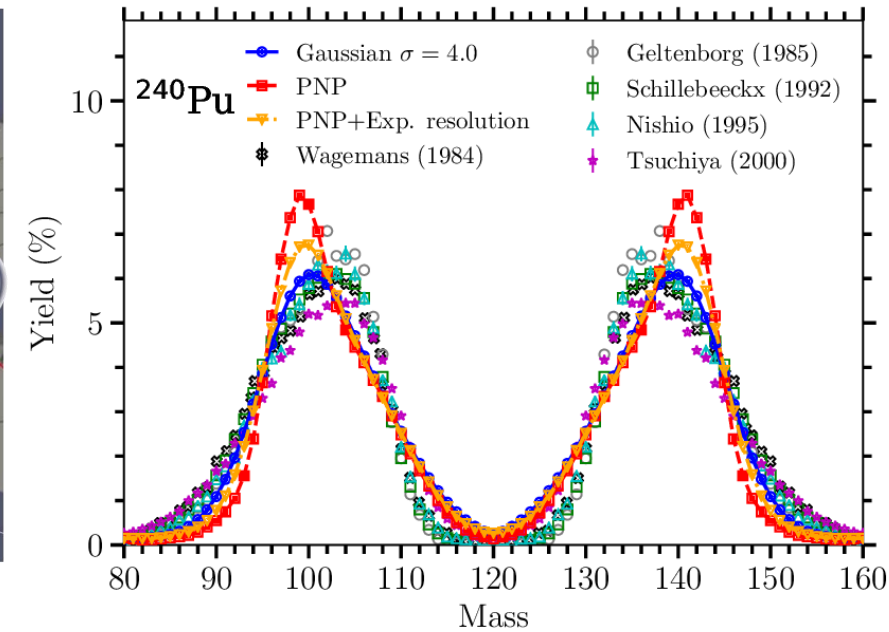
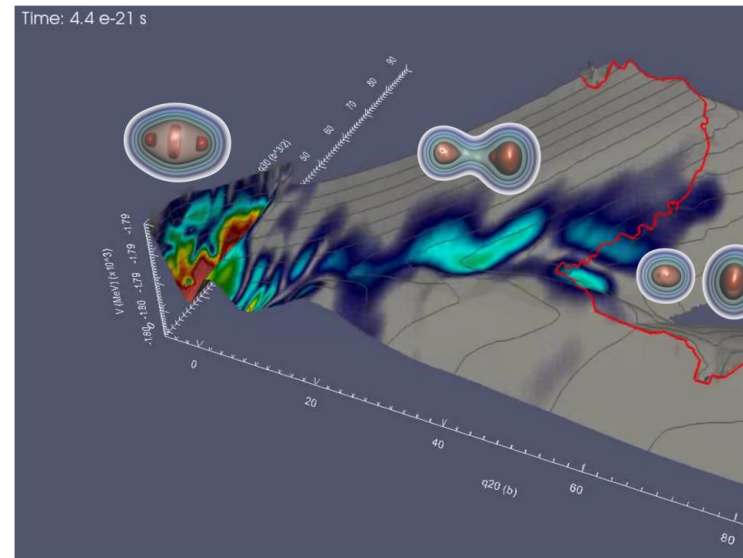
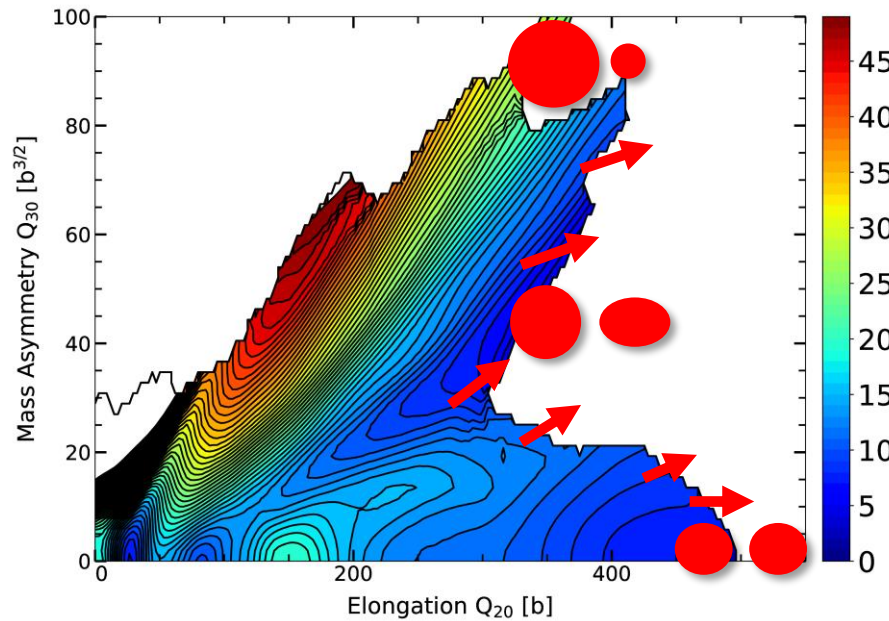
Potential energy surface



Time-dependent dynamics



Actual observables



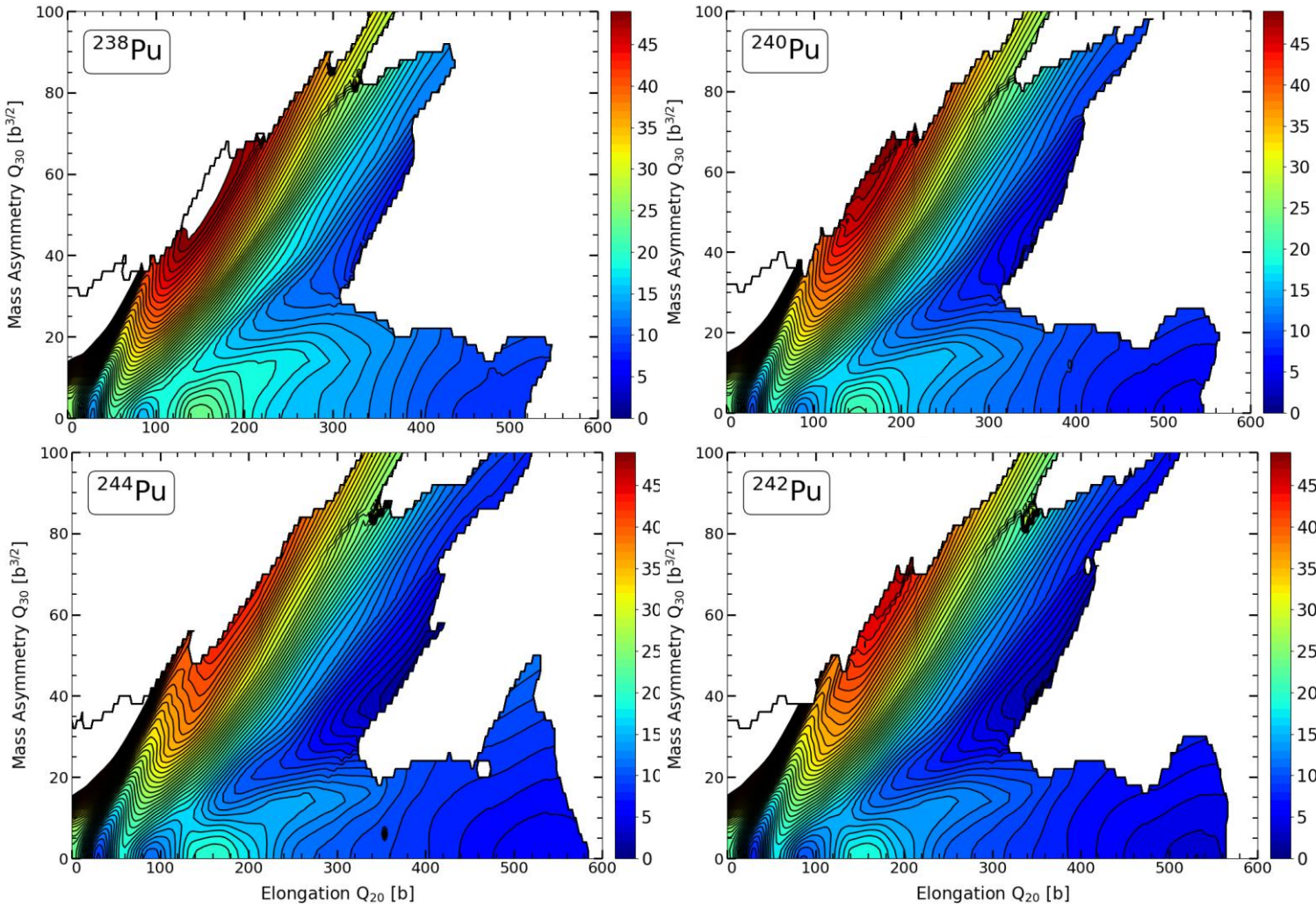
- Particle number (PNP)
- Spin distribution (AMP)
- Excitation energy (PNP, TDHFB)

- Fission fragment distributions (TDGCM)
- Real-time fission events (TDHFB)

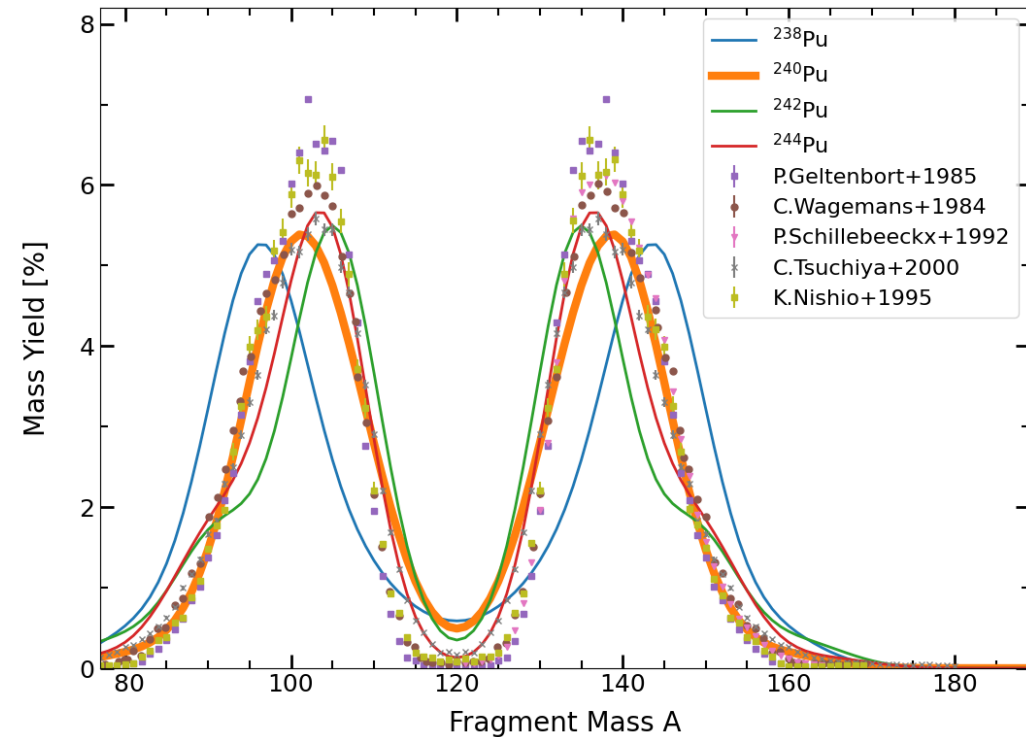
- Fission evaluation (FETA)

# Modeling: Distribution of fission fragments

We computed the systematics of initial fission fragment distributions at  $E_n \approx 1$  MeV for plutonium isotopes with our PESO framework

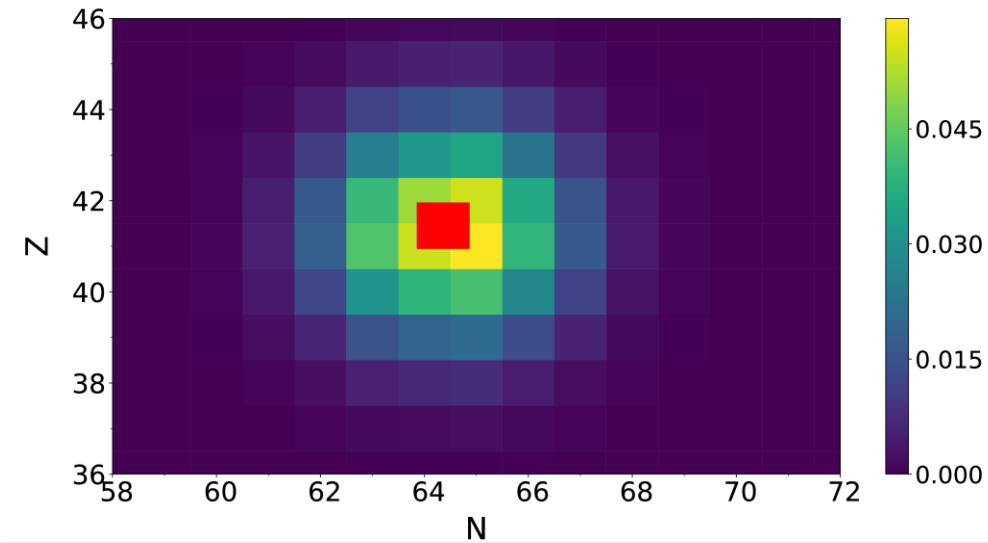
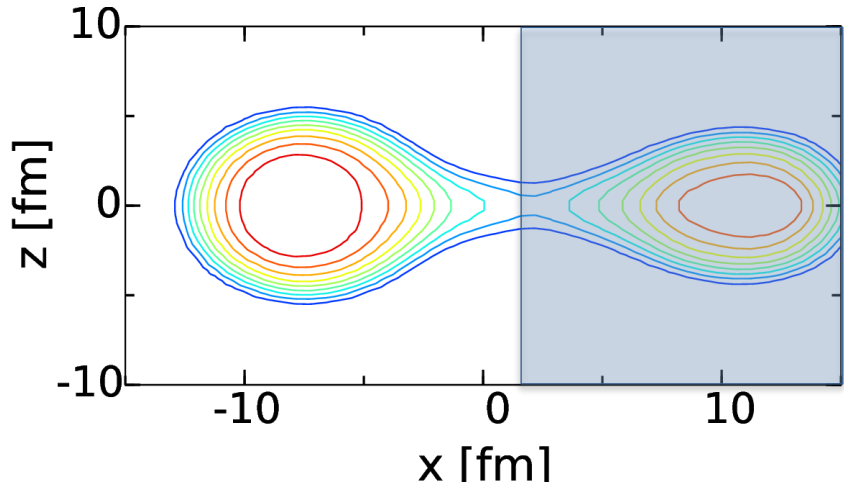


Initial mass distribution of fission fragments in even-even Plutonium isotopes (SkM\*)



# Modeling: Number of particles

Particle number projection techniques can be extended to estimate a distribution of particle number in fission fragments for each scission configuration



- Average number of particles in fission fragments obtained by integrating the density
- Better estimates with particle number projection:
  - Integer values...
  - Distribution of particle numbers at each scission point
- Collective dynamics in deformation space implies:

$$\langle \text{Fragment} | \hat{P}_N \hat{P}_Z \hat{P}_{N_f} \hat{P}_{Z_f} | \text{Fragment} \rangle \neq 0$$

What is the impact of collective correlations on particle number in fission fragments?



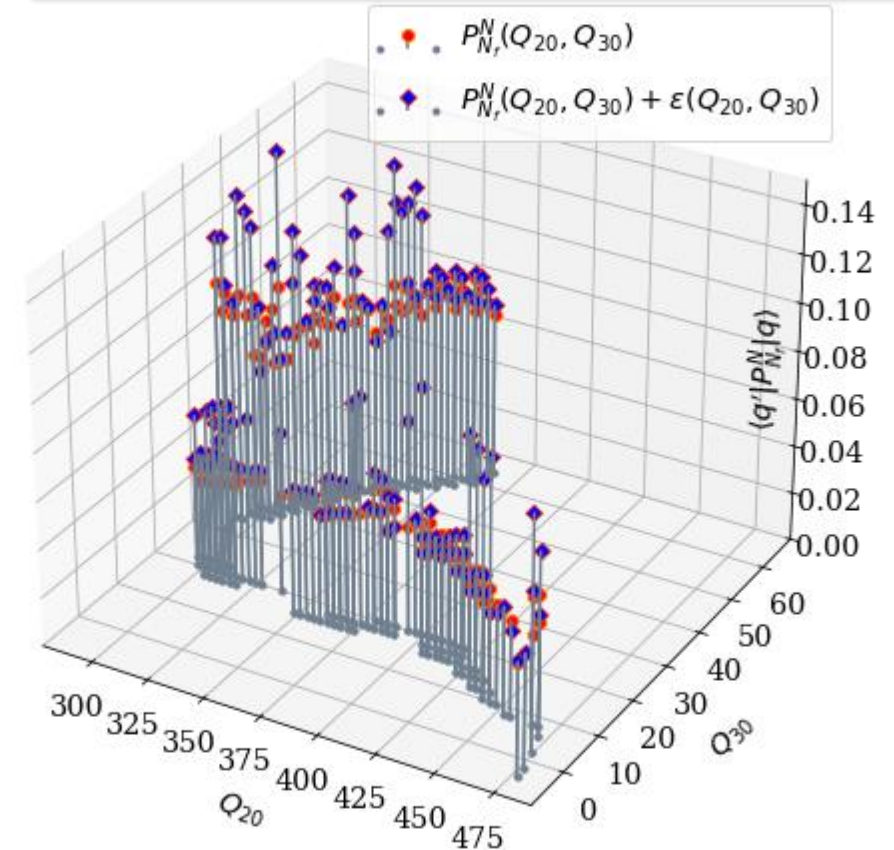
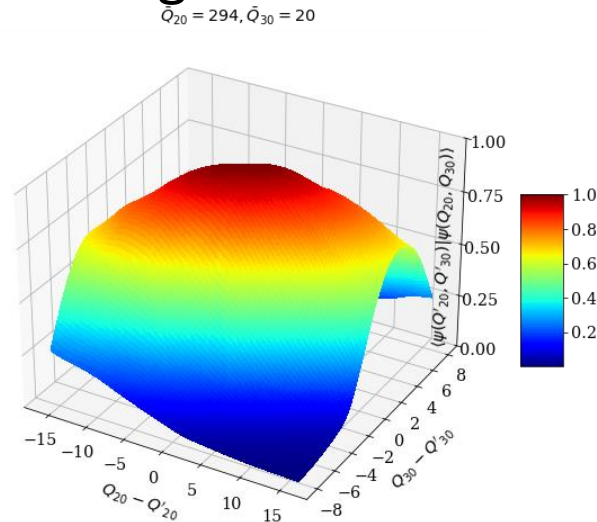
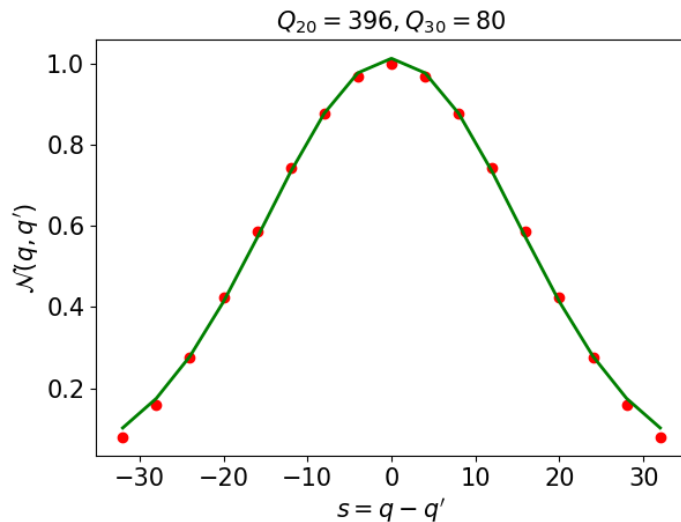
# Modeling: Number of particles

We are extending the generator coordinate method with Gaussian overlap approximation (GOA) to include quantum corrections in estimates of particle numbers in fission fragments



- Extend GCM+GOA to the projection operator on particle numbers in fission fragments
  - Equation of motion for change in particle number from deformation
  - Probability of  $(Z_f, N_f)$  modified by quantum correction term
- Validity of GOA determines validity of the calculation
- Technical challenges due to non-orthogonal bases

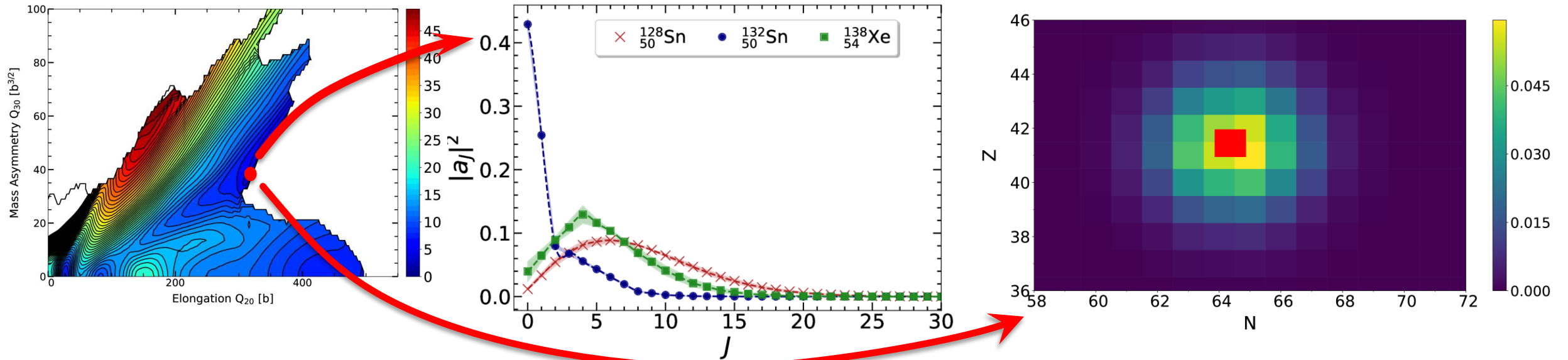
Probability of having  $N_f$  neutrons in scission configurations with average value  $\langle N_f \rangle$



# Modeling: Spin distributions of fission fragments



We combine angular momentum projection, particle number projection and large-amplitude collective dynamics to predict the spin distributions of fission fragments



- Angular momentum projection (AMP) gives spin distribution of in scission configuration  $\mathbf{q}$
- Particle number projection gives particle content at each scission configuration  $\mathbf{q}$
- TDGCM gives probability of populating scission configuration  $\mathbf{q}$
- All of the above combined will give spin distribution of fission fragment with  $Z_f$  protons and  $N_f$  neutrons



# Modeling: Predicting TKE

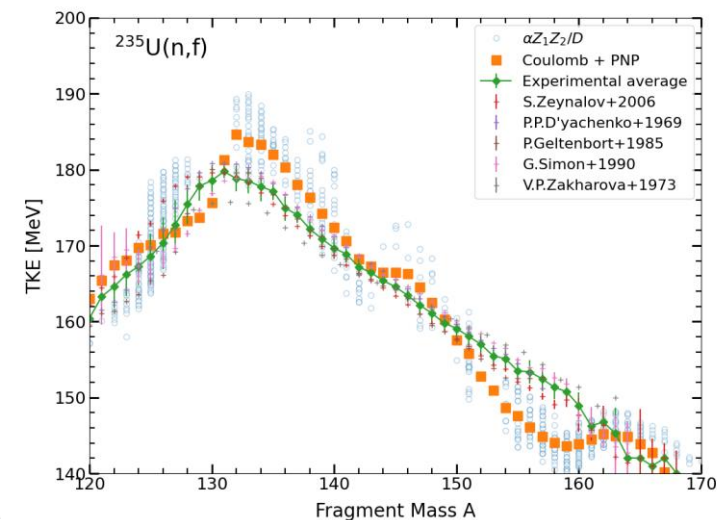
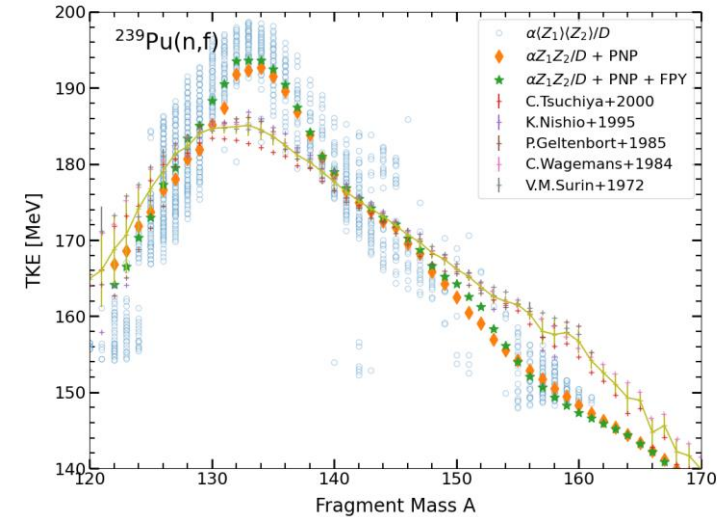
We are developing a model to predict TKE in fission by leveraging particle number projection techniques and estimates of the Coulomb repulsion between fragments



- TKE are used to determine total excitation energy (TXE) of fission reaction from energy conservation
  - Direct measurements of  $E^*$  of each fragment not possible in  $< 10^{-15}$ s...
  - Calculations of  $E^*$  among the most challenging
- TKE  $\approx$  (Direct) classical Coulomb interaction energy between fragments  $\propto \alpha Z_L Z_H / D$

$$\text{TKE}(A_f) \propto \sum_{\mathbf{q}} \mathbb{P}(\mathbf{q}) \times \sum_{Z_f + N_f = A_f} p(Z_f, N_f, \mathbf{q}) \alpha \frac{Z_f(\mathbf{q})(Z - Z_f(\mathbf{q}))}{D(\mathbf{q})}$$

Quality of TKE very dependent on quality of potential energy surface and scission configurations



# Capabilities: FELIX3D

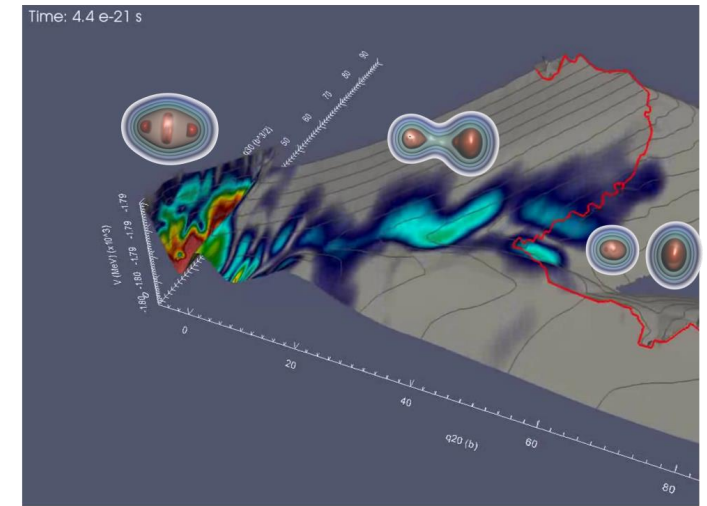
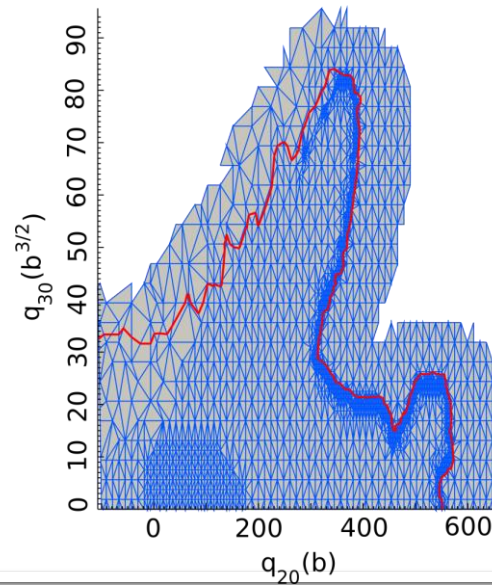
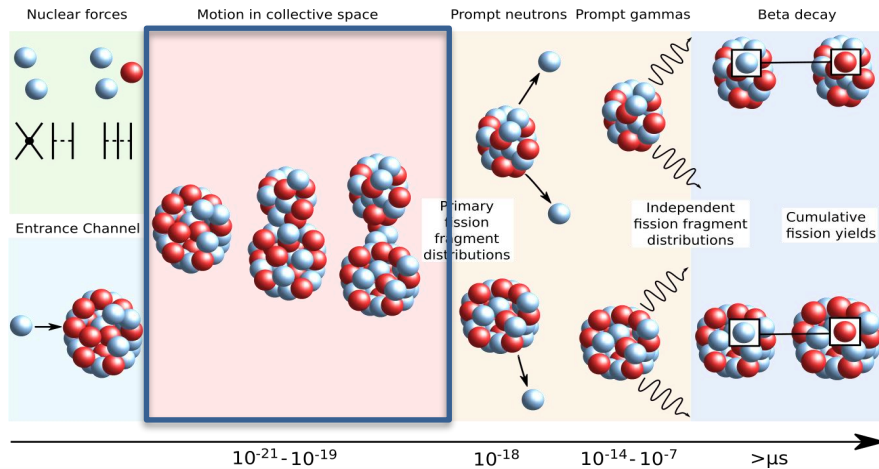
We have extended the capability of our TDGCM code to simulate fission dynamics in 3-dimensional deformation spaces



- DEFTNESS: Static properties of nuclei
  - HFBTHO: axial symmetry
  - HFODD: no symmetry
- FELIX: Large-amplitude collective dynamics**
- TDHFB: Real-time nuclear dynamics
- FETA: Evaluation of fission data based on statistical reaction theory

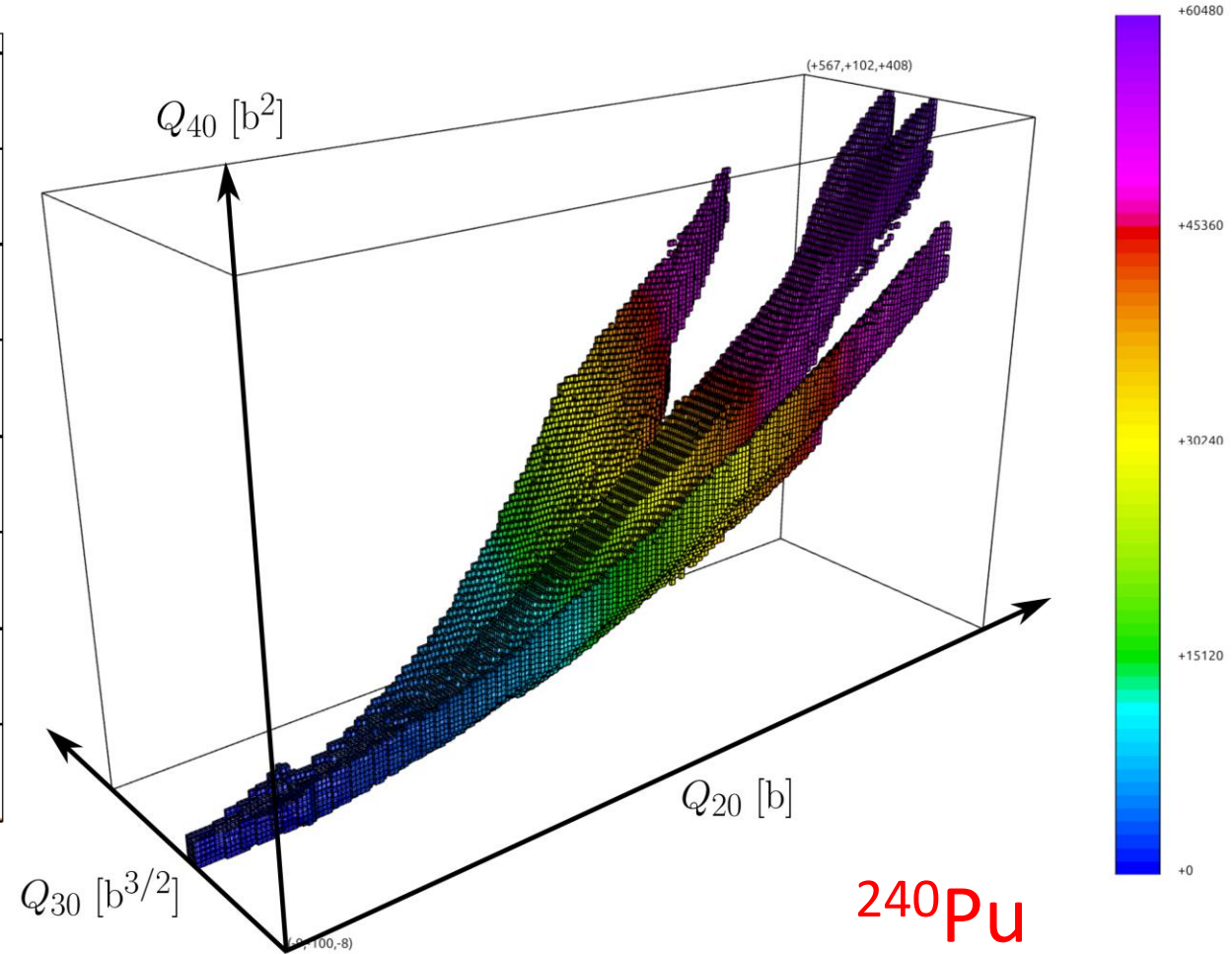
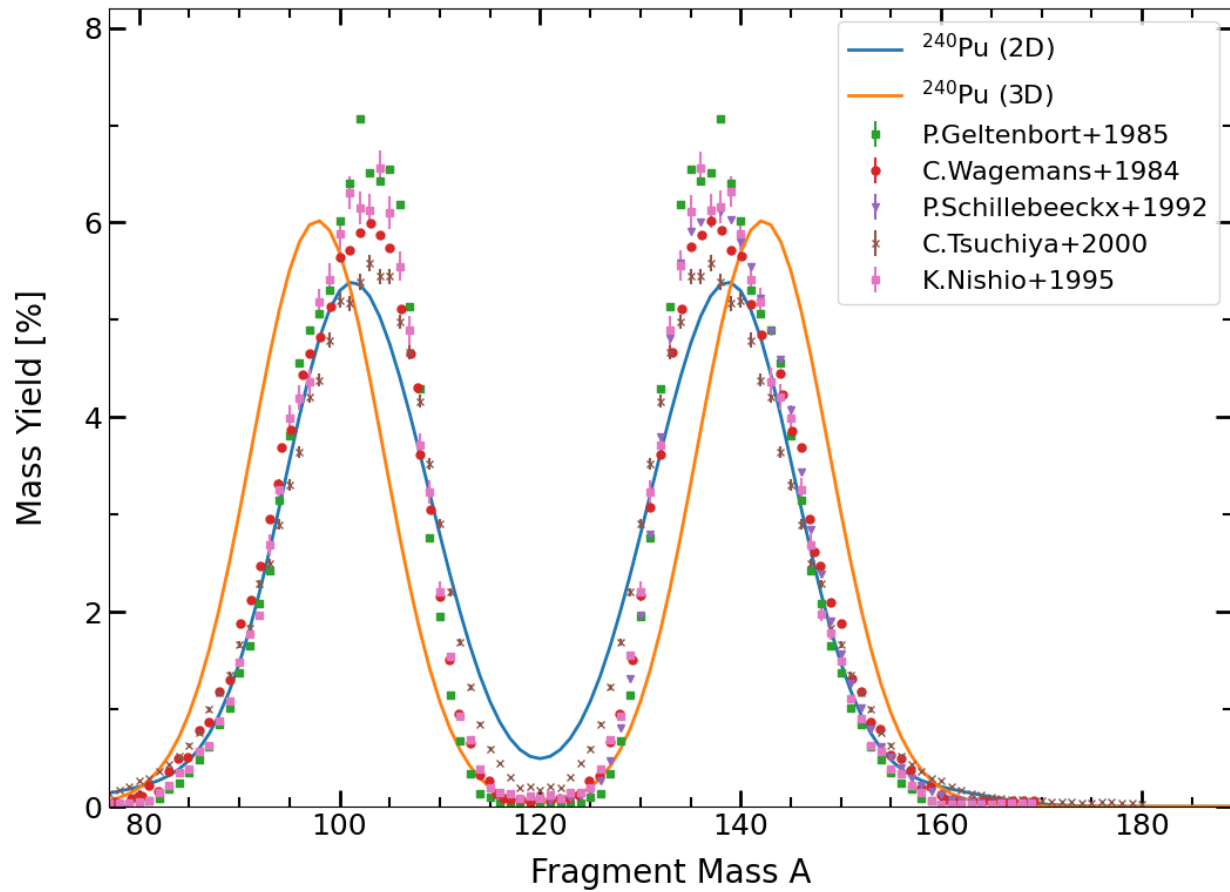
- FELIX gives the probability for the fissioning nucleus to have a given shape  $\mathbf{q}$  at time  $t$
- Solution of a Schrödinger-like equation

$$i\hbar \frac{\partial g(\mathbf{q}, t)}{\partial t} = \left[ -\frac{\hbar^2}{2} \gamma^{-\frac{1}{2}}(\mathbf{q}) \nabla \cdot \gamma^{\frac{1}{2}}(\mathbf{q}) B(\mathbf{q}) \nabla + V(\mathbf{q}) - iA(\mathbf{q}) \right] g(\mathbf{q}, t)$$



# Capabilities: FELIX3D

Very preliminary results with a sub-par 3D potential energy surface give encouraging results: symmetric fission is (too much...) hindered compared to simulations in 2D collective spaces.





# Capabilities: TDHFB Solver

We have developed a new code to solve the time-dependent Hartree-Fock-Bogoliubov (TDHFB) equation to simulate real-time fission events and extract the excitation energy of fission fragments

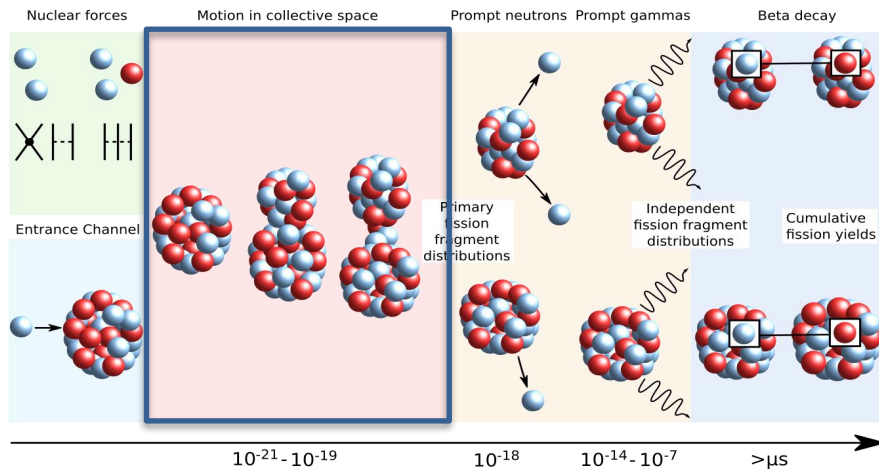


- DEFTNESS: Static properties of nuclei
  - HFBTHO: axial symmetry
  - HFODD: no symmetry
- FELIX: Large-amplitude collective dynamics
- **TDHFB: Real-time nuclear dynamics**
- FETA: Evaluation of fission data based on statistical reaction theory

- Modular, template-based C++ code
  - Expansion of time-dependent HFB spinors in one-center harmonic oscillator basis
  - Fully interfaced with HFBTHO and with a newly-developed Skyrme HFB solver
  - OpenMP threading and placeholder for GPU accelerations through placeholders for performance portability layers (RAJA, KOKKOS, etc.)

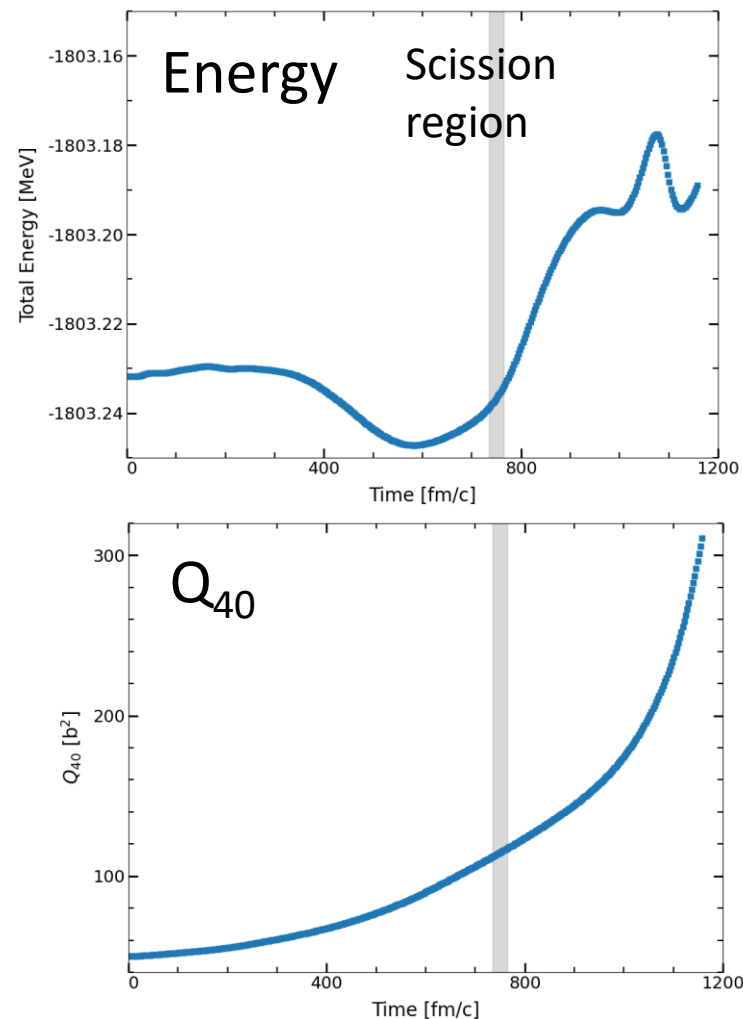
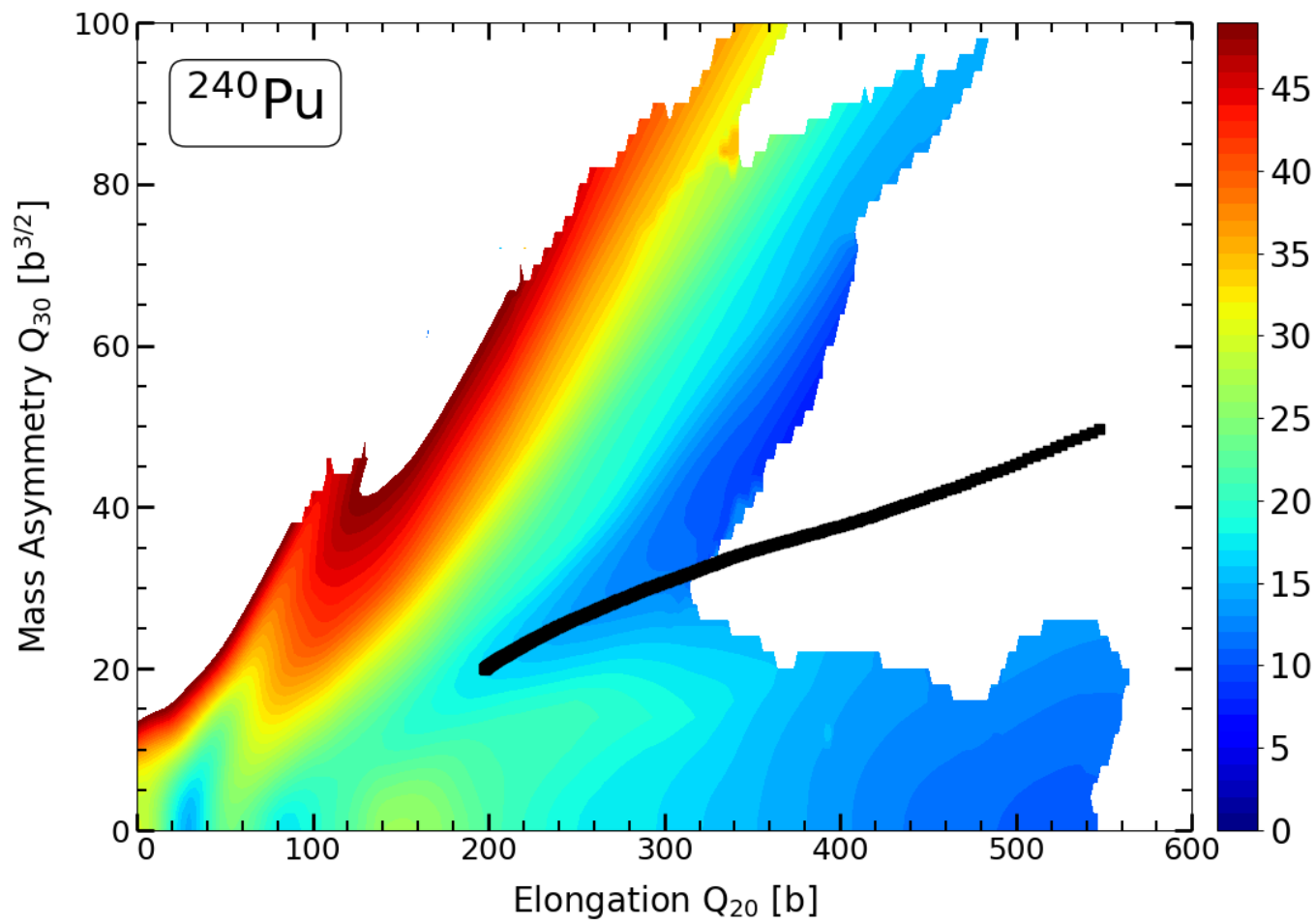
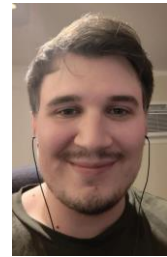
## Version 1: proof of principle

- ✓ Verify system can actually fission...
- ✓ Quantify conservation of energy and particle number
- ✓ Quantify drift in center of mass (0 if infinite basis)



# Capabilities: TDHFB Solver

We find that a heavy actinide nucleus such as  $^{240}\text{Pu}$  can fission even when TDHFB implemented in the HO basis and that conservation laws are obeyed with excellent precision

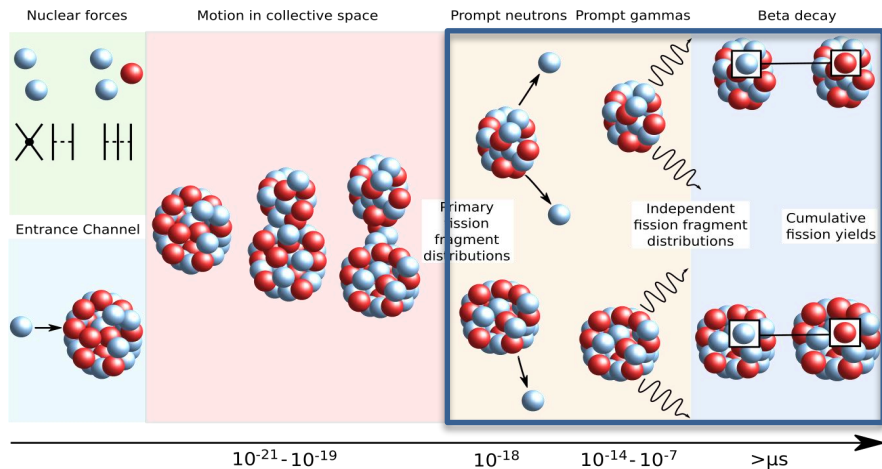


# Capabilities: Fission Evaluation Tools and Analytics (FETA)

We are developing a suite of tools to compute independent (and cumulative) fission yields as well as the prompt (and delayed) fission spectrum

- DEFTNESS: Static properties of nuclei
  - HFBTHO: axial symmetry
  - HFODD: no symmetry
- FELIX: Large-amplitude collective dynamics
- TDHFB: Real-time nuclear dynamics
- **FETA: Evaluation of fission data based on statistical reaction theory**

- Design principle: every physics input/model should be easily replaced by the user
- Modular Python-based framework
  - Characteristics of fission fragments at scission externally provided by user through tables, experimental data or preset inputs
  - Fission fragments decayed with YAHFC
  - Fission observables reconstructed from YAHFC outputs
- Version 1: observables
  - Independent fission yields
  - Prompt neutron and gamma spectrum





# Capabilities: Fission Evaluation Tools and Analytics (FETA)

FETA is easy to use – it relies on a YAML configuration file and runs all fragment decay in parallel using MPI

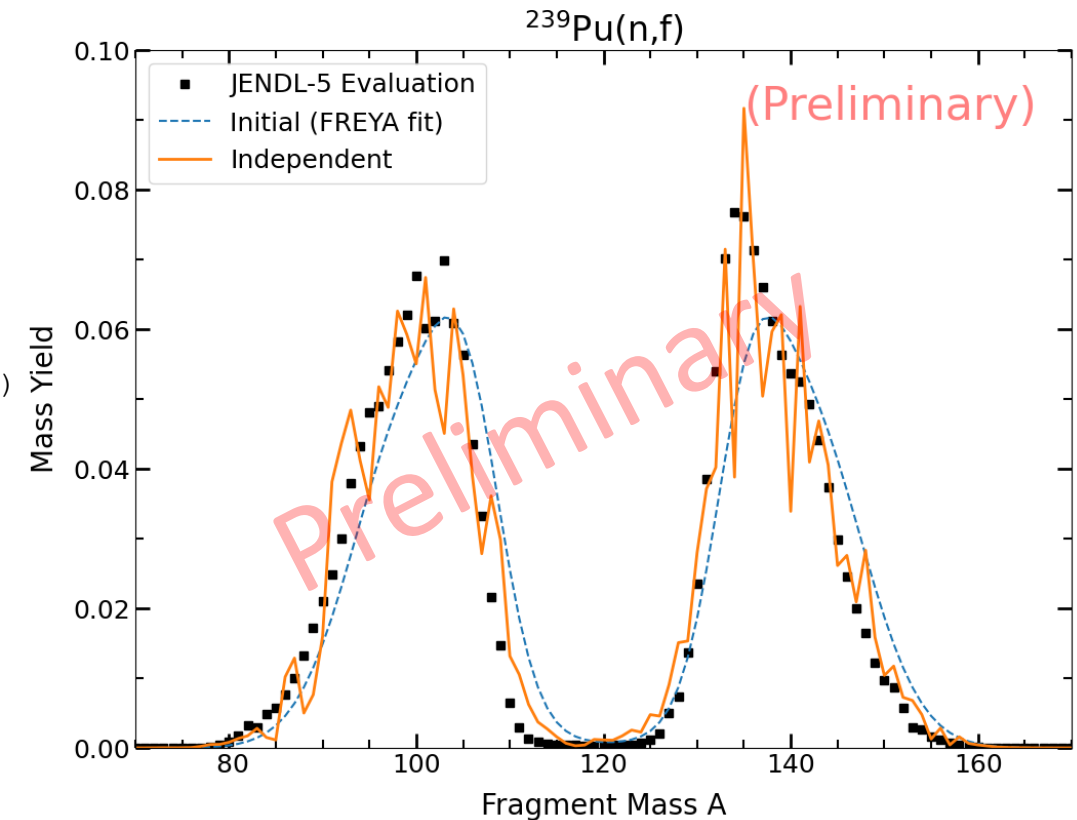
```
from fpy import config,yields,task_manager,io

# setup MPI environment
do_mpi = True
mpi_setup = task_manager.MPISetup(do_mpi)

# rank 0 reads configuration (only relevant if MPI is active)
conf_0 = None
if mpi_setup.rank == 0:
    conf_0 = config.Configuration('/home/toto/git/fpy/tests/fpy.yaml')
if do_mpi:
    conf = mpi_setup.comm.bcast(conf_0, root=0)
else:
    conf = conf_0

# define instance for independent yields and decay fission fragments
new_yields = yields.IndependentYields(conf, mpi_setup)
dico_decay = new_yields.run_decays()

# rank 0 computes yields and records the results
if mpi_setup.rank == 0:
    mat = new_yields.set_transitions(dico_decay)
    all_Y_ind = new_yields.get_yields()
    output = io.IO(conf.conf_data['Files']['Yields']['Write'])
    output.write(dico_decay, new_yields)
```



# Conclusions

LLNL effort is focused on developing and applying microscopic models to describe the initial conditions of fission fragments and provide guidance for evaluations

- We have focused our modeling efforts on
  - Efficiently generating FPY at scission with PESO framework and FELIX (2D)
  - Improving estimates of particle number in FFs with quantum corrections
  - Developing a semi-phenomenological model for TKE
- We have extended our FELIX capability by allowing simulations of FPY in 3D collective spaces
- We have developed two new capabilities
  - TDHFB solver in a basis to estimate excitation energy of fission fragments
  - FETA framework based on YAHFC (for now) to perform in-house FPY evaluations
- On-going work:
  - Finalizing study of quantum corrections on particle numbers in FFs
  - Predict spin distributions of fission fragments by combining AMP+PNP+FPY
  - The fun stuff: Physics studies with new FELIX-3D and TDHFB tools



**Disclaimer**

This document was prepared as an account of work sponsored by an agency of the United States government. Neither the United States government nor Lawrence Livermore National Security, LLC, nor any of their employees makes any warranty, expressed or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States government or Lawrence Livermore National Security, LLC. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States government or Lawrence Livermore National Security, LLC, and shall not be used for advertising or product endorsement purposes.