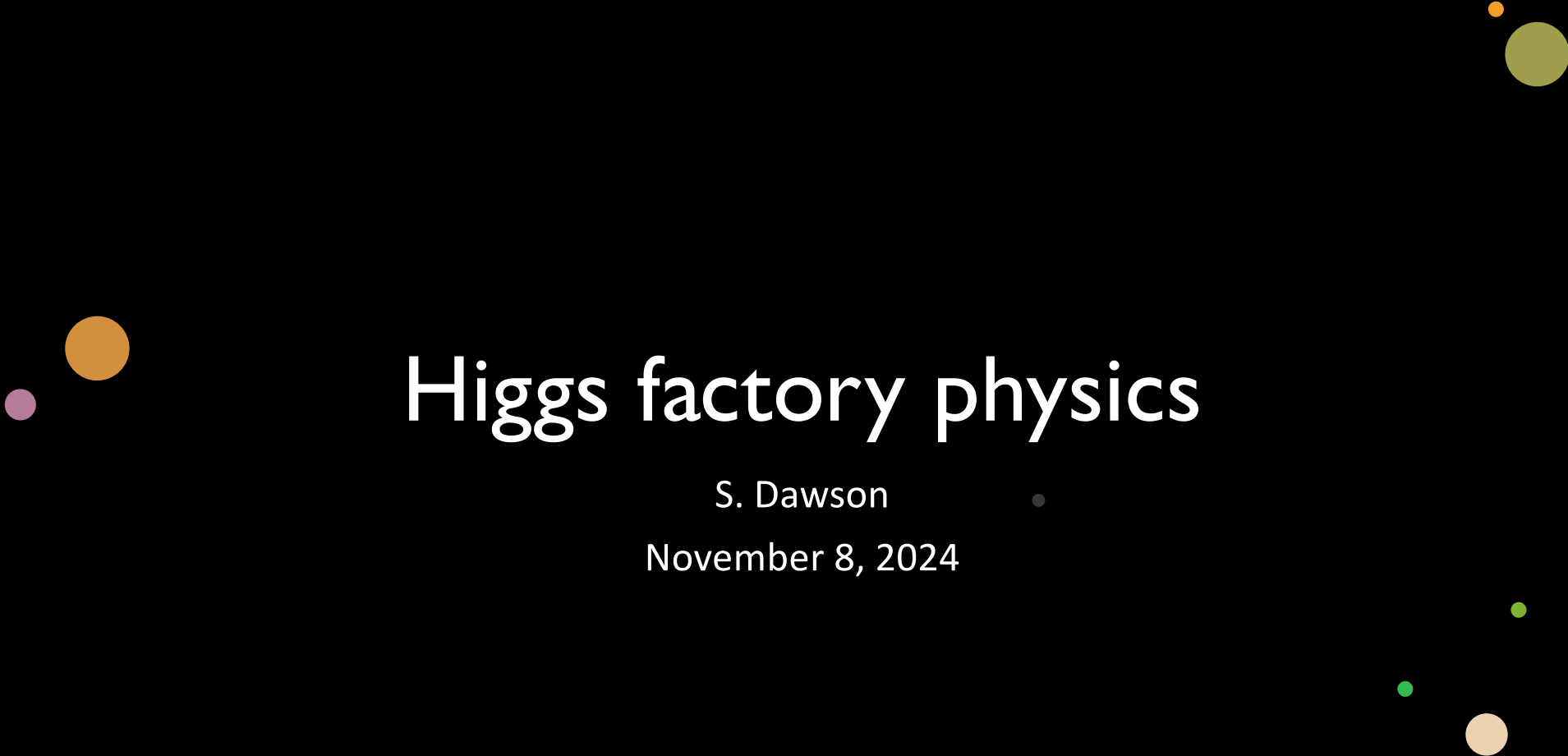


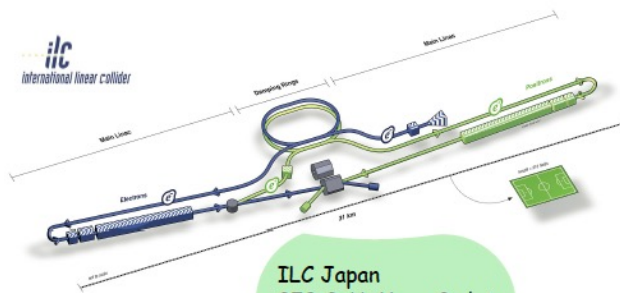
The slide features a black background with several decorative colored circles. In the top right corner, there is a small orange circle and a larger olive green circle. On the left side, there is a small purple circle and a larger orange circle. In the bottom right corner, there is a small green circle, a small orange circle, and a larger light orange circle. The title 'Higgs factory physics' is centered in a large, white, sans-serif font.

Higgs factory physics

S. Dawson

November 8, 2024

Linear e⁺e⁻ / Circular e⁺e⁻

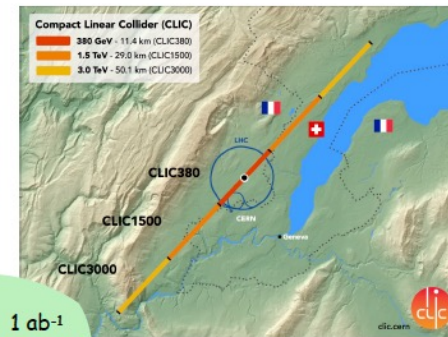


+ polarization

ILC Japan
250 GeV, 11y → 2 ab⁻¹
500 GeV, 8.5y 4 ab⁻¹
1000 GeV, 8.5y 8 ab⁻¹



Cool Copper Collider
250 GeV → 1.3×10³⁴/cm²s
550 GeV 2.4×10³⁴/cm²s

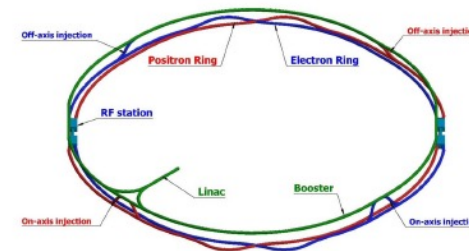


CLIC, CERN
380 GeV, 8y → 1 ab⁻¹
1500 GeV, 7y 2.5 ab⁻¹
3000 GeV, 8.5y 5 ab⁻¹



FCC-ee, CERN
m_Z, 4y → 150 ab⁻¹
2 m_W, 1-2y 10 ab⁻¹
240 GeV, 3y 5 ab⁻¹
2 m_{top}, 5y 1.5 ab⁻¹

Now, 10.8 ab⁻¹



CEPC, China
m_Z, 2y → 16 ab⁻¹
2 m_W, 1y 2.6 ab⁻¹
240 GeV, 7y 5.6 ab⁻¹



Physics program

EW Precision
(needed for max
Higgs precision)

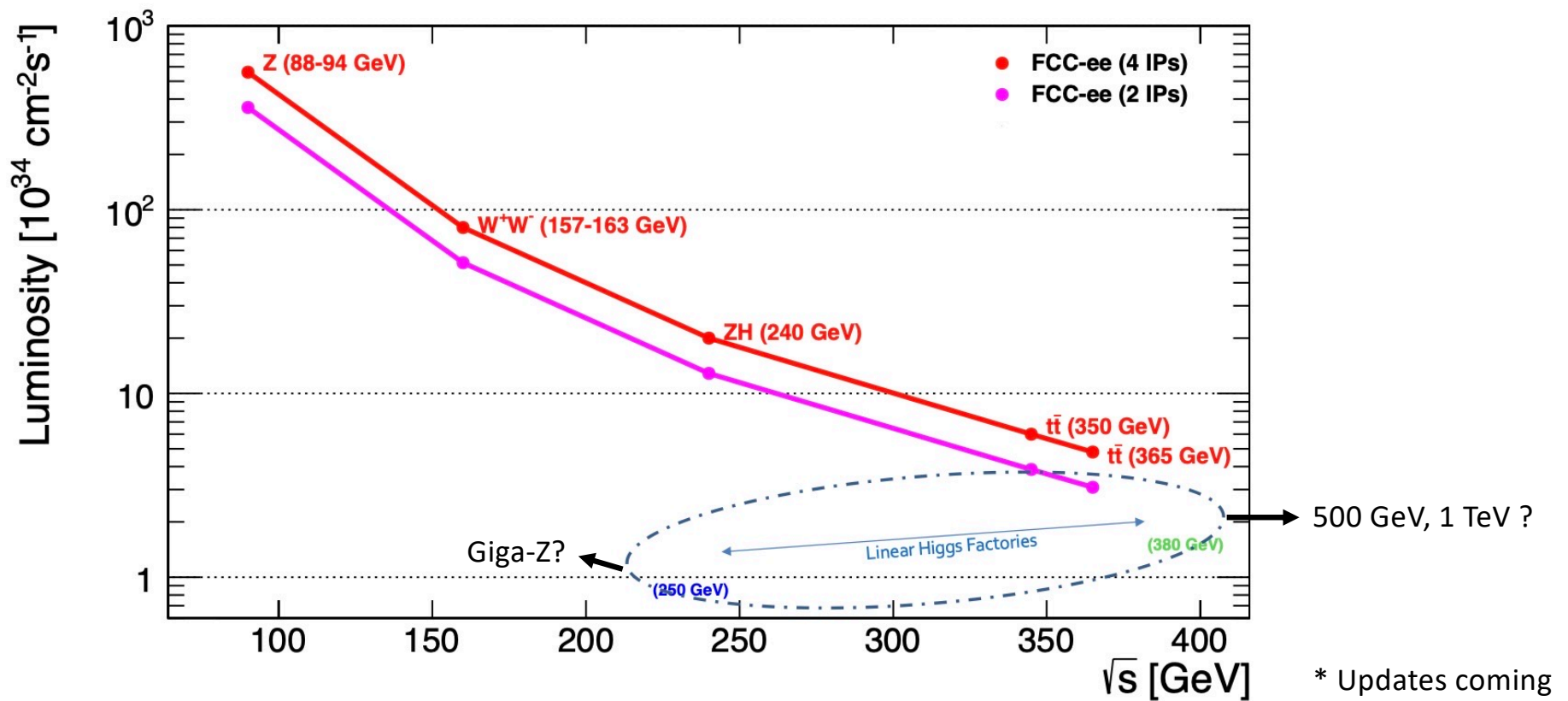
τ , B physics, light new
particles (ALPs, dark
photons,....)

Broad
programs

Higgs Precision: Higgs
couplings, self coupling,
width, mass

Top Physics: couplings,
mass, width

Scenarios



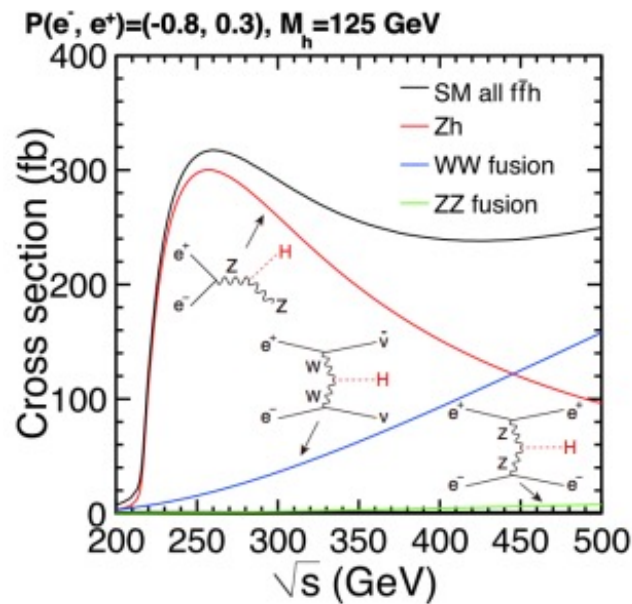
Precision

- Snowmass assumptions

Many updates
since then

Collider	$\sqrt{s}$	P [%] e^-/e^+	L_{int} ab^{-1}
ILC	250 GeV	$\pm 80 / \pm 30$	2
	350 GeV	$\pm 80 / \pm 30$	0.2
	500 GeV	$\pm 80 / \pm 30$	4
	1 TeV	$\pm 80 / \pm 20$	8
ILC-GigaZ	m_Z	$\pm 80 / \pm 30$	0.1
CLIC	380 GeV	$\pm 80 / 0$	1
	500 GeV	$\pm 80 / 0$	2.5
	1 TeV	$\pm 80 / 0$	5
CEPC	m_Z		60 / 100
	$2m_W$		3.6 / 6
	240 GeV		12 / 20
	$2m_t$		– / 1
FCC-ee	m_Z		150
	$2m_W$		10
	240 GeV		5
	$2m_t$		1.5

Higgs factory



- Sensitivity to both Higgstrahlung and VBF improves precision on couplings
- At $\sqrt{s} > 450 \text{ GeV}$, VBF dominates

1.5 ab^{-1} at 365 GeV
 200K HZ events
 50K WW $\rightarrow$ H events

5 ab^{-1} at 240 GeV
 10^6 HZ events
 25K WW $\rightarrow$ H events

Higgstrahlung cross section $\sim 20\%$ larger with polarization

Higgs in a nutshell

- Absolute measurements of couplings (recoil method)
 - (LHC makes assumptions)
- Improvement of coupling measurements from HL-LHC
- Width measurement ($e^+e^- \rightarrow ZH$, $H \rightarrow ZZ^*$ plus $WW \rightarrow H$)
- Higgs trilinear coupling
- Indirect sensitivity to new physics through loops
- Electron Yukawa at FCC-ee?
- Light quark Yukawas (much work since Snowmass)

Establish Higgs
mechanism

Indirect new
physics
sensitivity

Flavor, Dark Matter?

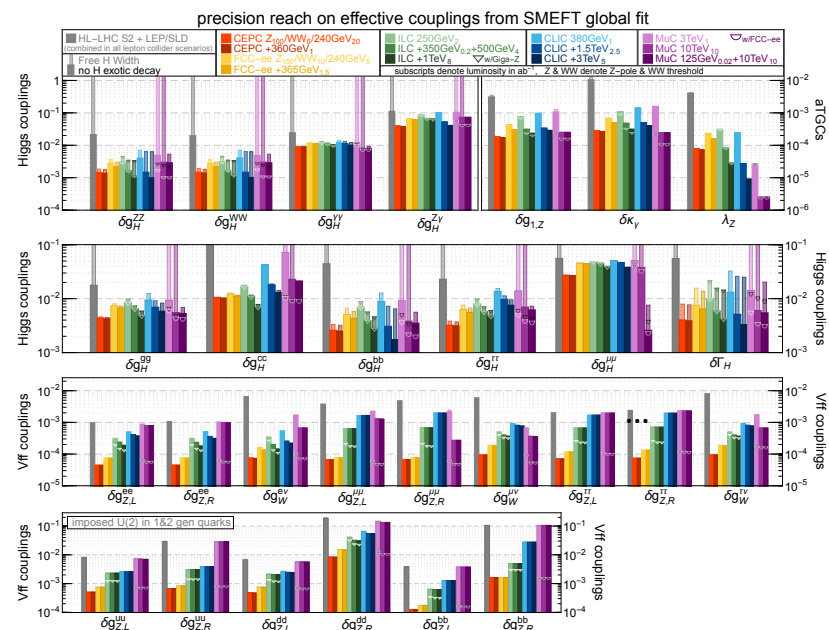
What this talk is

- This is not a sales pitch for the wonders of e^+e^- colliders
 - We're all convinced!
- I was asked to discuss some of the **basic differences** between opportunities at circular and linear colliders
 - I will point out some **general** physics features

The “best” machine is the one that gets built

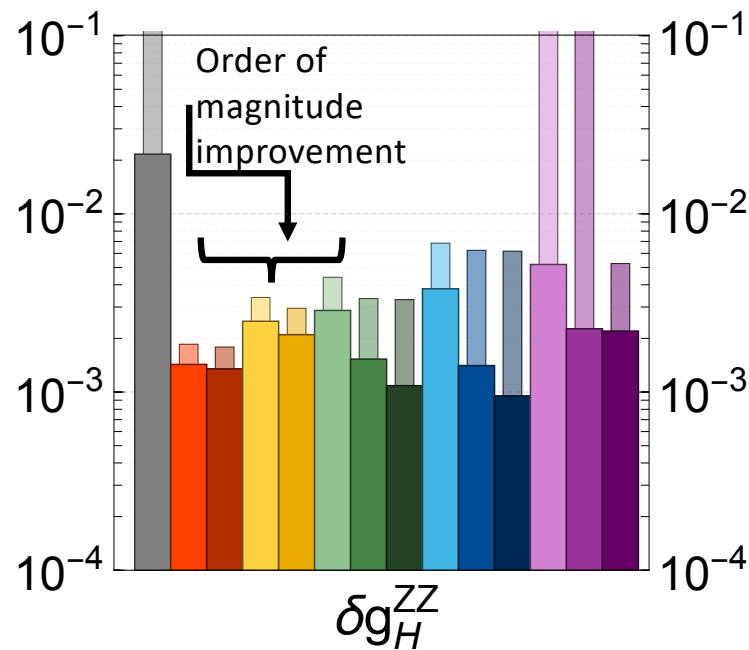
Higgs Coupling Measurements

- All Higgs Factories have similar reach with Snowmass assumptions: Polarization vs Luminosity
- Coupling measurements $O(1\%)$ at Higgs factories
- Running at 2 energies improves sensitivity at both FCC-ee and ILC
- Improvement in precision over LHC



[Snowmass], 2209.08078

Drill down on couplings



- Darker solid shades include running at 2 energies
- FCC-ee numbers include Z pole, ILC numbers do not include Z pole

■ HL-LHC S2 + LEP/SLD (combined in all lepton collider scenarios)	■ CEPC $Z_{100}/WW_6/240\text{GeV}_{20}$	■ ILC 250GeV_2	■ CLIC 380GeV_1	■ MuC 3TeV_1	▽ w/FCC-ee
■ Free H Width	■ CEPC $+360\text{GeV}_1$	■ ILC $+350\text{GeV}_{0.2}+500\text{GeV}_4$	■ CLIC $+1.5\text{TeV}_{2.5}$	■ MuC 10TeV_{10}	
■ no H exotic decay	■ FCC-ee $Z_{150}/WW_{10}/240\text{GeV}_5$	■ ILC $+1\text{TeV}_8$	■ CLIC $+3\text{TeV}_5$	■ MuC $125\text{GeV}_{0.02}+10\text{TeV}_{10}$	
	■ FCC-ee $+365\text{GeV}_{1.5}$	▽ w/Giga-Z			

subscripts denote luminosity in ab^{-1} , Z & WW denote Z-pole & WW threshold

Coupling updates (Thanks to M. Peskin)

- ILC (2 ab^{-1} at 250 GeV), FCC-ee (10.5 ab^{-1} at 240 GeV), CEPC (20 ab^{-1} at 240 GeV)

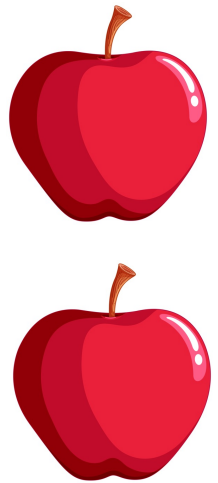
- EFT fit

Coupling
projections
in %

All numbers
include HL-LHC
(which is crucial
for $\mu\mu$ and $\gamma\gamma$)

Assume NNLO
theory plus
precision m_b , m_c
from lattice

Coupling	ILC	FCC-ee	CEPC
bb	0.98	0.54	0.43
cc	1.82	0.89	0.68
gg	1.62	0.80	0.62
$\tau\tau$	1.12	0.60	0.48
WW	0.46	0.37	0.33
ZZ	0.46	0.36	0.32
$\mu\mu$	3.97	3.44	3.04
$\gamma\gamma$	1.09	0.97	0.92
Γ (MeV)	2.30	1.20	0.94
INV (95% EXC)	0.36	0.26	0.25
Untagged	1.60	0.78	0.60



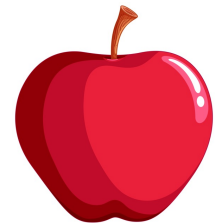
Coupling updates (Thanks to M. Peskin)

- ILC (2 ab^{-1} at 250 GeV + 200 fb^{-1} at 350 GeV + 4 ab^{-1} at 550 GeV), FCC-ee (10.5 ab^{-1} at 240 GeV + 3.25 ab^{-1} at 360 GeV + Tera-Z), CEPC (20 ab^{-1} at 240 GeV + 1 ab^{-1} at 360 GeV + Tera-Z)

- EFT fit

Coupling
projections
in %

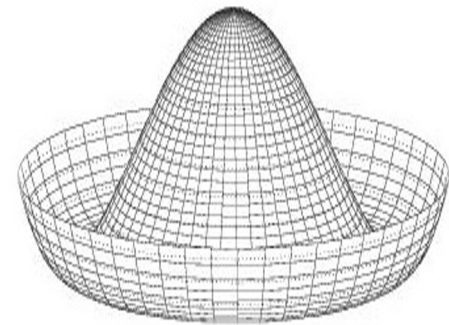
Coupling	ILC (full)	FCC-ee (full)	CEPC (full)
bb	0.58	0.45	0.41
cc	1.17	0.79	0.65
gg	0.96	0.68	0.59
$\tau\tau$	0.75	0.51	0.45
WW	0.35	0.28	0.29
ZZ	0.35	0.27	0.28
$\mu\mu$	3.75	3.31	3.01
$\gamma\gamma$	1.00	0.94	0.91
Γ (MeV)	1.56	1.01	0.90
INV (95% EXC)	0.32	0.23	0.24
Untagged	1.19	0.66	0.58



Higgs Self Coupling

$$V = \mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$
$$= \frac{M_H^2}{2} H^2 + \lambda_3 H^3 + \lambda_4 H^4$$

$$\lambda_3 = \frac{M_H^2}{2v} \sim .13v \quad \lambda_4 = \frac{M_H^2}{8v^2} = .03$$

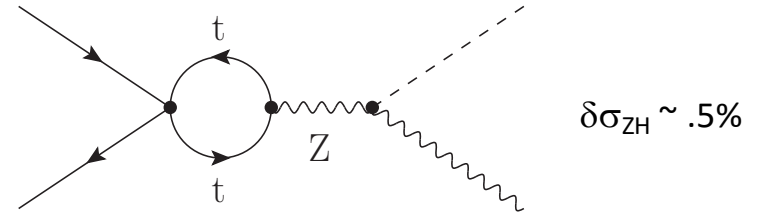
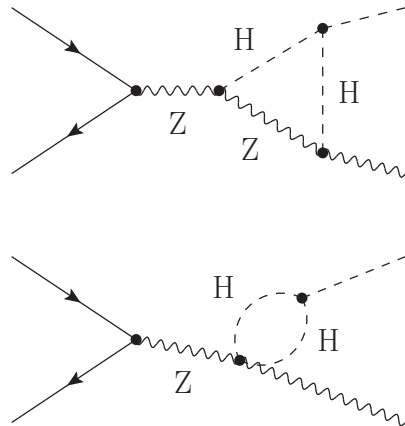


- We need to verify the shape of the Higgs potential
- Higgs trilinear is sensitive to beyond the SM physics
- λ_3 and λ_4 **ARE NOT FREE PARAMETERS**

Consistent study requires use of effective field theory

Indirect Access below HH Threshold

- Indirect sensitivity from effects in loops
- Many other operators contribute
- Can be cancellations/correlations
 - **ie, only a clean measurement of trilinear coupling in specific UV scenarios**

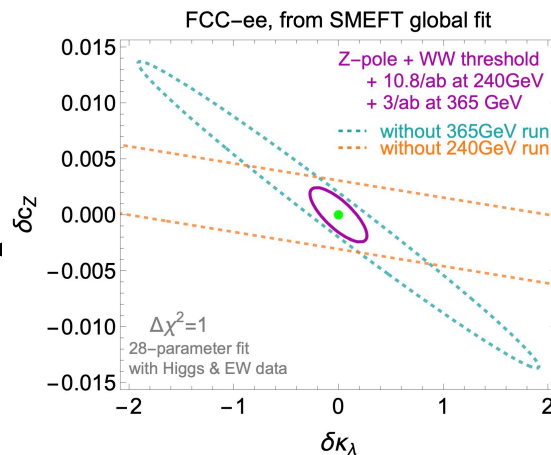


Note strong interplay with Z pole measurements

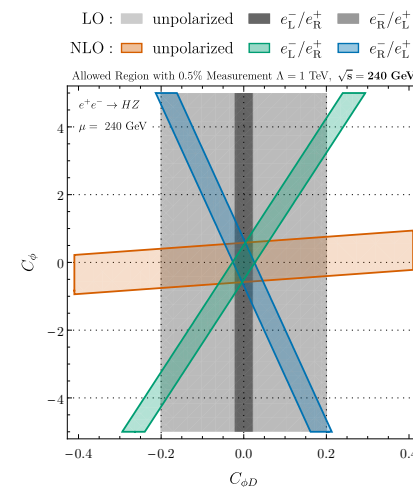
Higgs self-coupling from indirect measurements

- Runs at different energies critical to separate effects of different operators

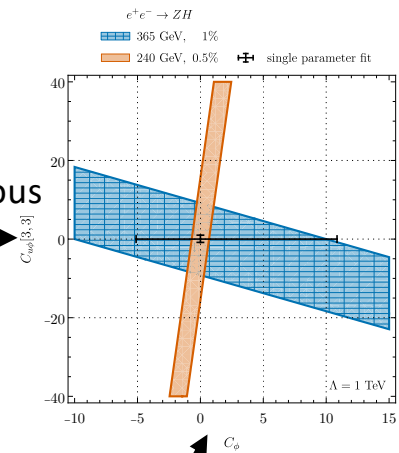
Modification of HZZ vertex (contributes at tree level)



Higgs tri-linear



tW anomalous coupling $\rightarrow$



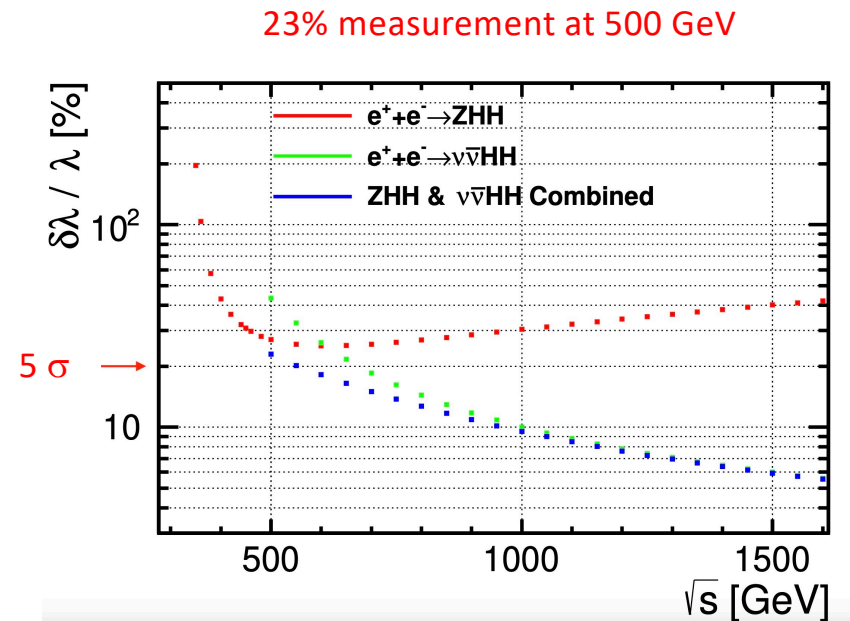
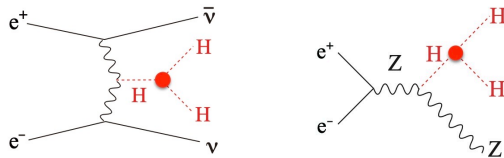
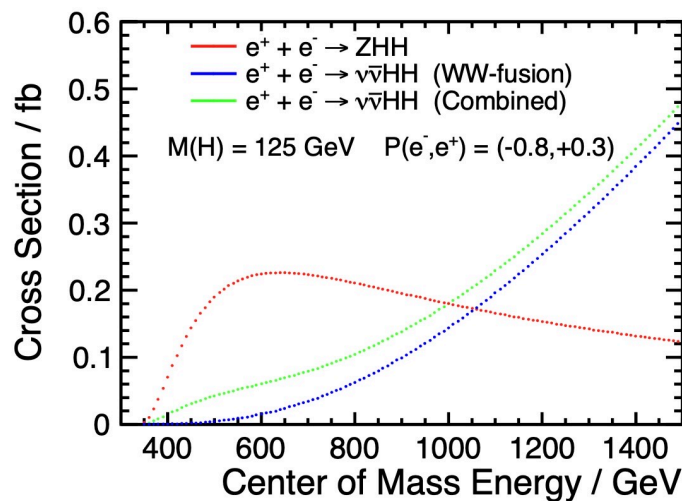
Higgs tri-linear

- Polarization gives another handle to separate effects
- 2 energies can separate effects

- Not yet clear how to extract best value of Higgs tri-linear from indirect measurements

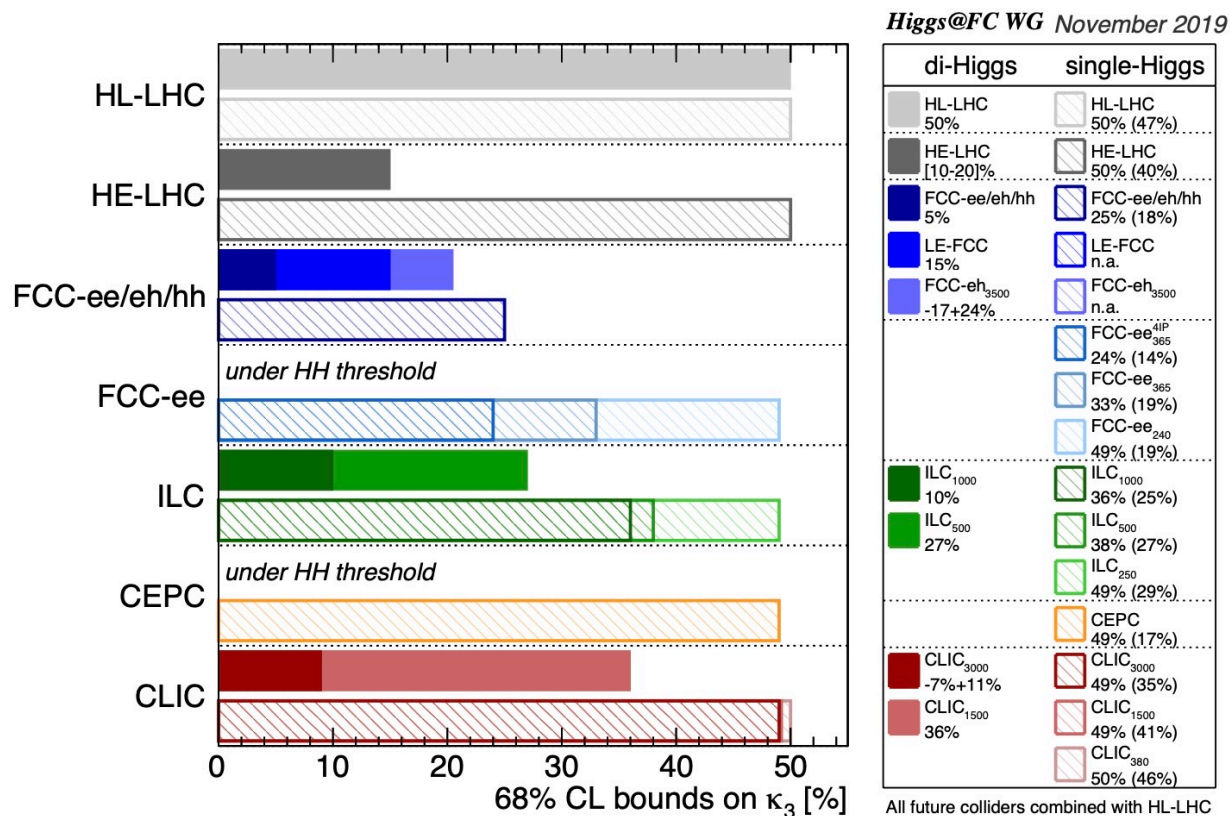
[1809.10041](#), [2409.11466](#)

Higgs self coupling from direct production



*Assumed luminosity scaled with energy

Higgs self-coupling



Direct and indirect measurements have different theory assumptions.

- 23% sensitivity: 5σ discovery
- 50% sensitivity: H^3 coupling non-zero @95% CL

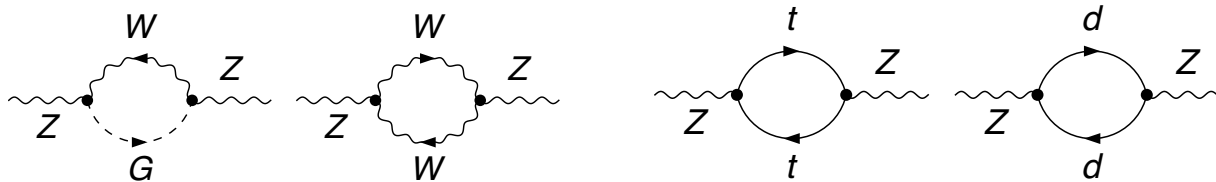
Old plot, but underlying physics is the same

Why Precision Electroweak?

- Relationships between SM parameters changed by loop corrections

$$M_W^2 = \frac{M_Z^2}{2} \left\{ 1 + \sqrt{1 - \frac{4\pi\alpha}{\sqrt{2}G_\mu M_Z^2} (1 + \Delta r)} \right\}$$

- Could be new particles in loops



- Interpretation of results requires precise knowledge of SM parameters
- eg* prediction of $H \rightarrow \gamma\gamma$ depends on SM inputs, so you need them to search for BSM physics

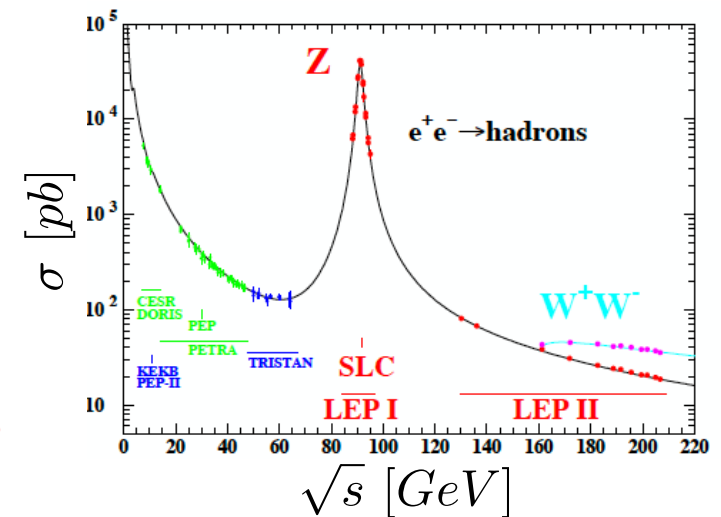
Precision Z pole

- Z pole run:
 - LEP/SLC $\sim 10^7 Z \rightarrow O(.1\%)$
 - ILC (Giga-Z) $10^9 Z$
 - FCC-ee (Tera-Z) $10^{12} Z$
- Many observables at Z pole: M_Z , Γ_Z , A_{FB}
 - **Unpolarized beams sensitive to fermion couplings to Zs**

$$A_f = \frac{g_{fL}^2 - g_{fR}^2}{g_{fL}^2 + g_{fR}^2} \quad A_{FB}^f = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} A_e A_f$$

- Lower luminosity at linear collider, but can be somewhat compensated by polarization
 - More observables with polarization

$$A_{LR,FB} = \frac{3}{4} A_f \quad A_{LR,FB} = \frac{3}{4} A_f$$



Z Pole

- $m_Z, \Gamma_Z, \alpha_s(m_Z)$ improvements by factors of 20-50 from today
- First direct measurement of $\alpha(m_Z)$
- More lumi at circular colliders, but beam polarization at linear colliders improves sensitivity and can help control systematics
- Below WW threshold, beam energy can be precisely calibrated using resonant depolarization at circular colliders giving precise m_Z, m_W
- Linear colliders need physical mass (Z) for calibration
- At linear colliders, largest experimental systematic from polarization calibration
- At circular collider, modeling uncertainties for hadronic final states dominant systematic error

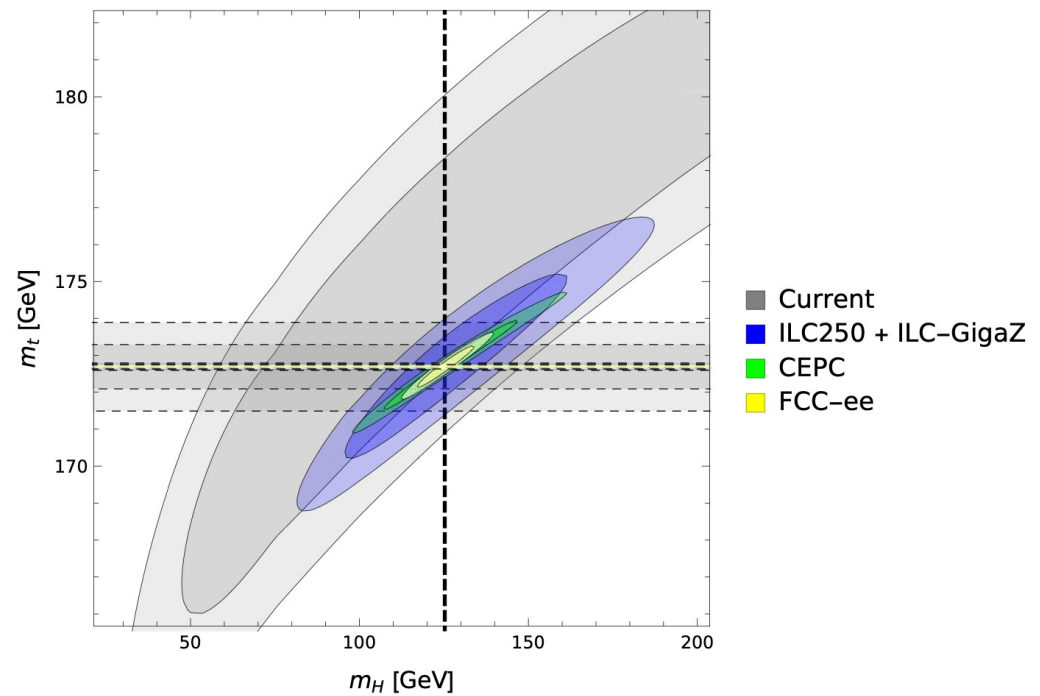
Quantity	current	ILC250	ILC-GigaZ	FCC-ee	CEPC	CLIC380
$\Delta\alpha(m_Z)^{-1} (\times 10^3)$	17.8*	17.8*		3.8 (1.2)	17.8*	
Δm_W (MeV)	12*	0.5 (2.4)		0.25 (0.3)	0.35 (0.3)	
Δm_Z (MeV)	2.1*	0.7 (0.2)	0.2	0.004 (0.1)	0.005 (0.1)	2.1*
Δm_H (MeV)	170*	14		2.5 (2)	5.9	78
$\Delta\Gamma_W$ (MeV)	42*	2		1.2 (0.3)	1.8 (0.9)	
$\Delta\Gamma_Z$ (MeV)	2.3*	1.5 (0.2)	0.12	0.004 (0.025)	0.005 (0.025)	2.3*
$\Delta A_e (\times 10^5)$	190*	14 (4.5)	1.5 (8)	0.7 (2)	1.5 (2)	60 (15)
$\Delta A_\mu (\times 10^5)$	1500*	82 (4.5)	3 (8)	2.3 (2.2)	3.0 (1.8)	390 (14)
$\Delta A_\tau (\times 10^5)$	400*	86 (4.5)	3 (8)	0.5 (20)	1.2 (20)	550 (14)
$\Delta A_b (\times 10^5)$	2000*	53 (35)	9 (50)	2.4 (21)	3 (21)	360 (92)
$\Delta A_c (\times 10^5)$	2700*	140 (25)	20 (37)	20 (15)	6 (30)	190 (67)
$\Delta\sigma_{\text{had}}^0$ (pb)	37*			0.035 (4)	0.05 (2)	37*
$\delta R_e (\times 10^3)$	2.4*	0.5 (1.0)	0.2 (0.5)	0.004 (0.3)	0.003 (0.2)	2.5 (1.0)
$\delta R_\mu (\times 10^3)$	1.6*	0.5 (1.0)	0.2 (0.2)	0.003 (0.05)	0.003 (0.1)	2.5 (1.0)
$\delta R_\tau (\times 10^3)$	2.2*	0.6 (1.0)	0.2 (0.4)	0.003 (0.1)	0.003 (0.1)	3.3 (5.0)
$\delta R_b (\times 10^3)$	3.1*	0.4 (1.0)	0.04 (0.7)	0.0014 (< 0.3)	0.005 (0.2)	1.5 (1.0)
$\delta R_c (\times 10^3)$	17*	0.6 (5.0)	0.2 (3.0)	0.015 (1.5)	0.02 (1)	2.4 (5.0)

Table 3: EWPOs at future e^+e^- colliders: statistical error (estimated experimental systematic error). Δ (δ) stands for absolute (relative) uncertainty, while * indicates inputs taken from current data [6]. See Refs. [23, 30, 35, 36, 46, 47].

[\[Snowmass\]](#)

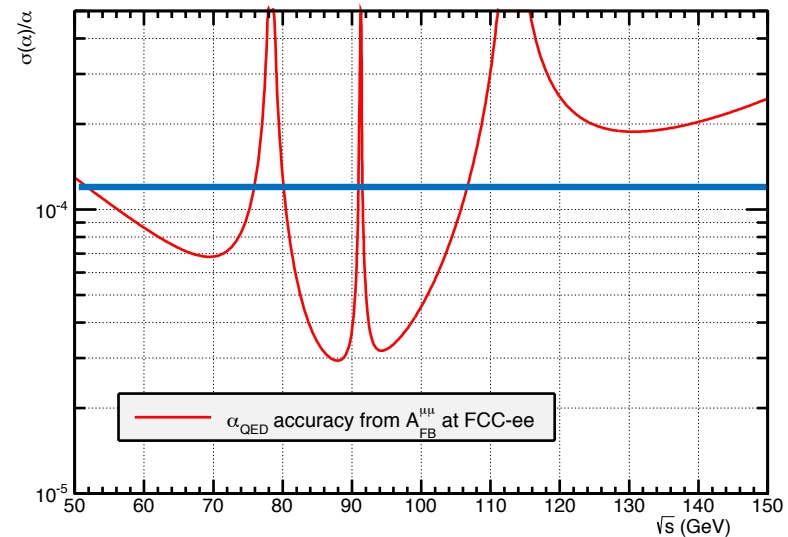
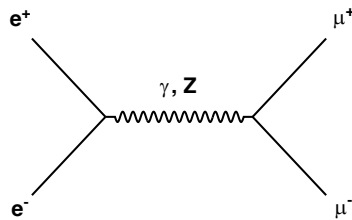
Precision

- Verify consistency of SM at levels far beyond current knowledge



Measurement of α_{QED}

- $A_{\mu\mu}^{FB}(M_Z)$ gives first direct measurement of $\alpha_{\text{QED}}(M_Z)$
- Measurement is statistics dominated and needs more theory



Don't want to be limited by theory

- Need a concerted theory effort

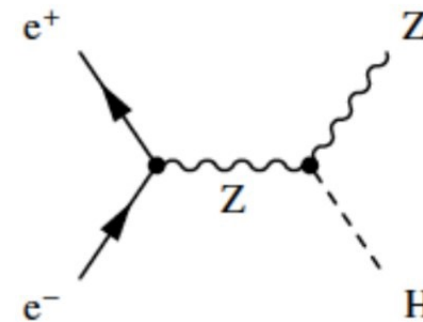
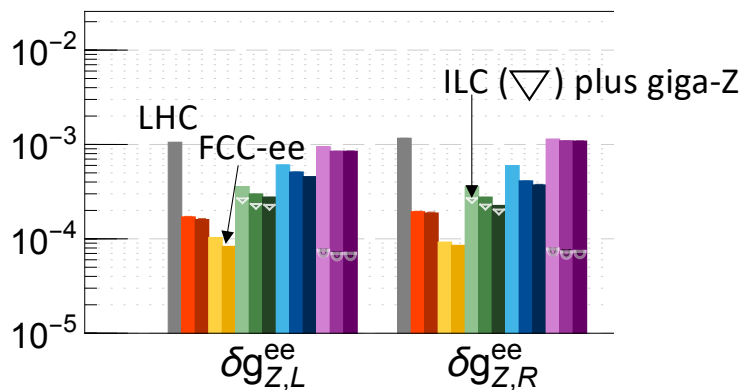
[Freitas,Heinemeyer,Beneke,Blondel,Dittmaier,Gluzh,Hoang,Jadach,Janot,Reuter,Reimann;Schwinn,Skrzypek,Weinzierl]

	current exp.	FCC _{ee} , CEPC /ILC	current th.	~3(4)-loop
M_W [MeV]	12	0.5/3	4 ($\alpha^3, \alpha^2\alpha_s$)	1
Γ_Z [MeV]	2.3	0.1/1	0.4 ($\alpha^3, \alpha^2\alpha_s, \alpha\alpha_s^2$)	0.15
R_ℓ [10^{-3}]	25	1/10	5 ($\alpha^3, \alpha^2\alpha_s$)	1.5
R_b [10^{-5}]	66	6/15	10 ($\alpha^3, \alpha^2\alpha_s$)	5
$\sin^2 \theta_{eff}^\ell$ [10^{-5}]	~ 13	0.6/1.3	4.5 ($\alpha^3, \alpha^2\alpha_s$)	1.5

Why do we need precision?

Zee couplings needed to get maximum precision from $e^+e^- \rightarrow ZH$ measurements

Higgs coupling projections typically assume these improvements on Z couplings!



ILC gets precision Zee couplings without Giga-Z

HL-LHC S2 + LEP/SLD (combined in all lepton collider scenarios)	CEPC $Z_{100}/WW_6/240\text{GeV}_{20}$	ILC 250GeV_2	CLIC 380GeV_1	MuC 3TeV_1 ∇ w/FCC-ee
Free H Width	CEPC $+360\text{GeV}_1$	ILC $+350\text{GeV}_{0.2}+500\text{GeV}_4$	CLIC $+1.5\text{TeV}_{2.5}$	MuC 10TeV_{10}
no H exotic decay	FCC-ee $Z_{150}/WW_{10}/240\text{GeV}_5$	ILC $+1\text{TeV}_8$ ∇ w/Giga-Z	CLIC $+3\text{TeV}_5$	MuC $125\text{GeV}_{0.02}+10\text{TeV}_{10}$
subscripts denote luminosity in ab^{-1} , Z & WW denote Z-pole & WW threshold				

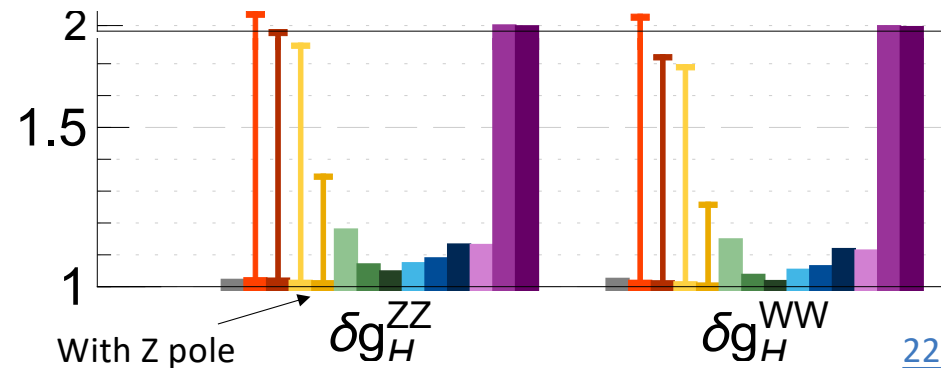
[2206.08326 \[Snowmass\]](#)

More on precision

Precision measurements at Z pole and WW threshold improve precision on Higgs couplings and 3 gauge boson couplings by roughly a factor of 2 at FCC-ee

Measurement
precision/ precision
with perfect EW
measurements

No improvement in Z
pole measurements

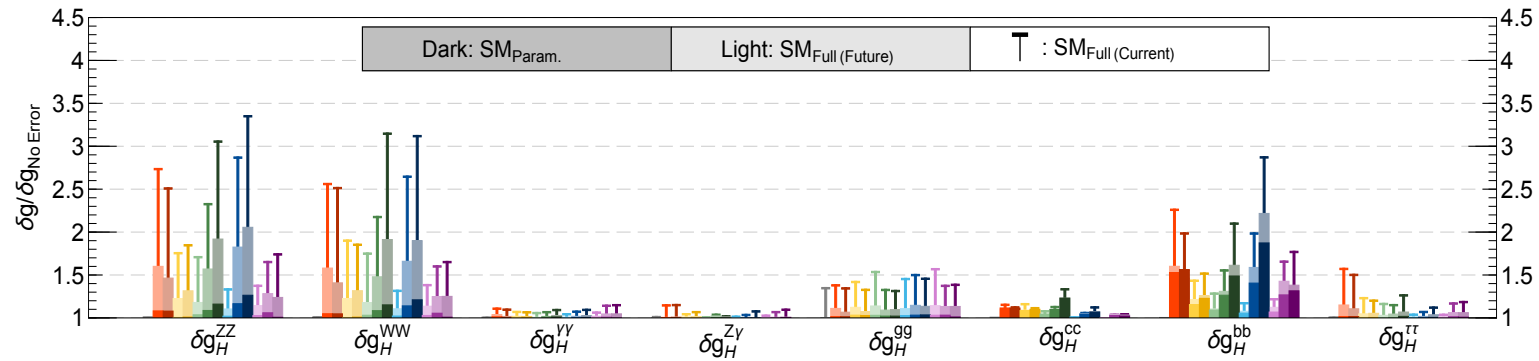


[2209.08078, \[Snowmass\]](#)

■ HL-LHC S2 + LEP/SLD (combined in all lepton collider scenarios)	■ CEPC Z ₁₀₀ /WW ₆ /240GeV ₂₀	■ ILC 250GeV ₂	■ CLIC 380GeV ₁	■ MuC 3TeV ₁	▽ w/FCC-ee
■ Free H Width	■ CEPC +360GeV ₁	■ ILC +350GeV _{0.2} +500GeV ₄	■ CLIC +1.5TeV _{2.5}	■ MuC 10TeV ₁₀	
■ no H exotic decay	■ FCC-ee Z ₁₅₀ /WW ₁₀ /240GeV ₅	■ ILC +1TeV ₈	■ CLIC +3TeV ₅	■ MuC 125GeV _{0.02} +10TeV ₁₀	
	■ FCC-ee +365GeV _{1.5}				

subscripts denote luminosity in ab⁻¹, Z & WW denote Z-pole & WW threshold

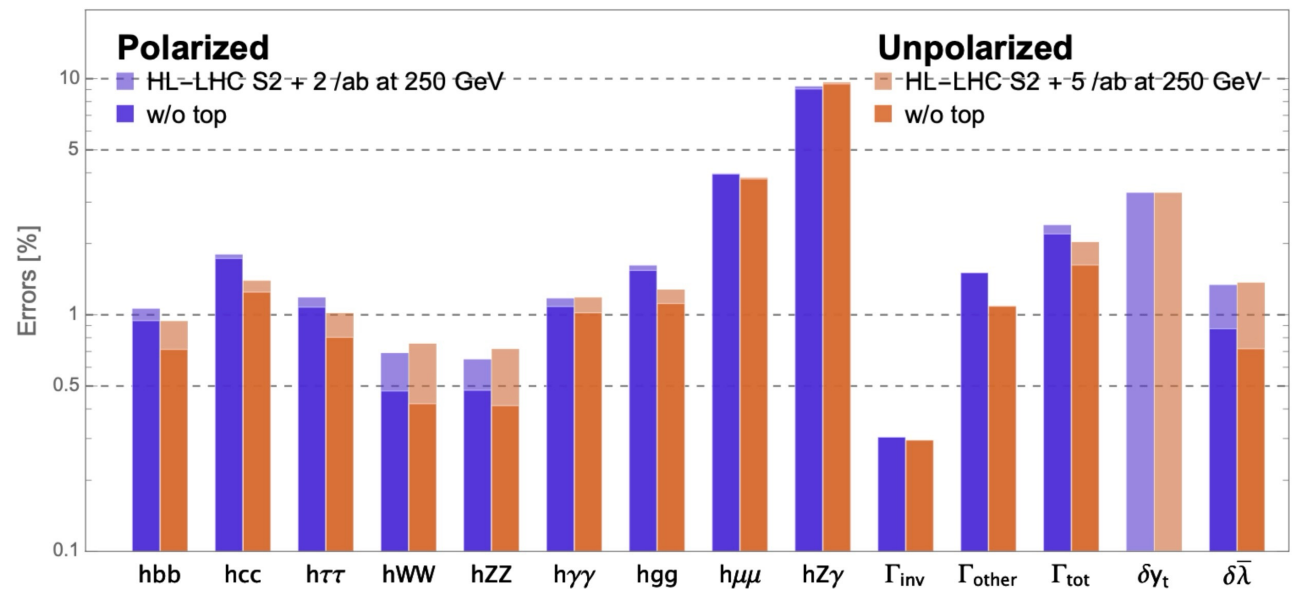
More improvements



Top physics

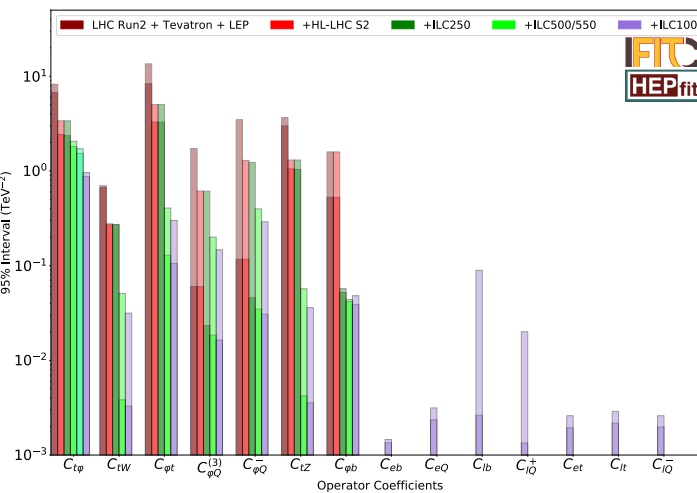
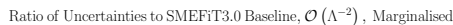
- e^+e^- threshold scan:
 - $\delta m_t \sim 50$ MeV
 - $\delta \Gamma_t = 45$ MeV
 - (Currently, $\delta m_t = 330$ MeV)
- Improvement in Higgs fits with top data
- Dominant uncertainty is theory
 - **Need 3-4 loop EW corrections with masses**

Top mass fundamental input into theory predictions for Higgs physics



[2006.14631](#)

Insight into top interactions



Note improvement on top couplings with increased energy

FCC-ee $\rightarrow$ typical reduction in uncertainty on top operators by factor ~ 6 from LHC (FCC-ee with 10 ab^{-1})

2404.12809

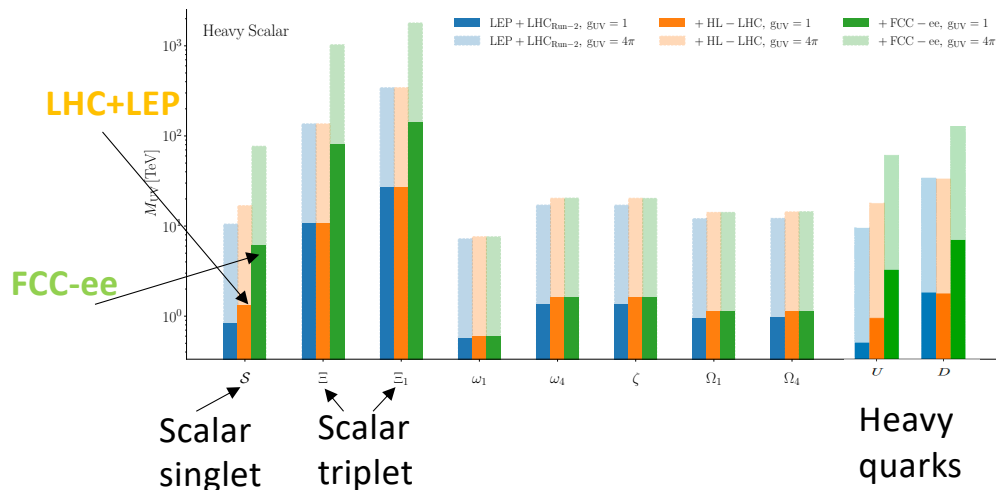
2206.08326

Precision and new physics

- Heavy new physics manifests itself in deviations from predicted SM interactions
- Can parameterize in terms of effective field theory (SMEFT)

$$L_{SMEFT} = L_{SM} + \sum_i \frac{C_i}{\Lambda^2} O_i$$

- Match Cs to specific UV models



When new physics contributes to EWPOs, large increase in precision at e^+e^- colliders

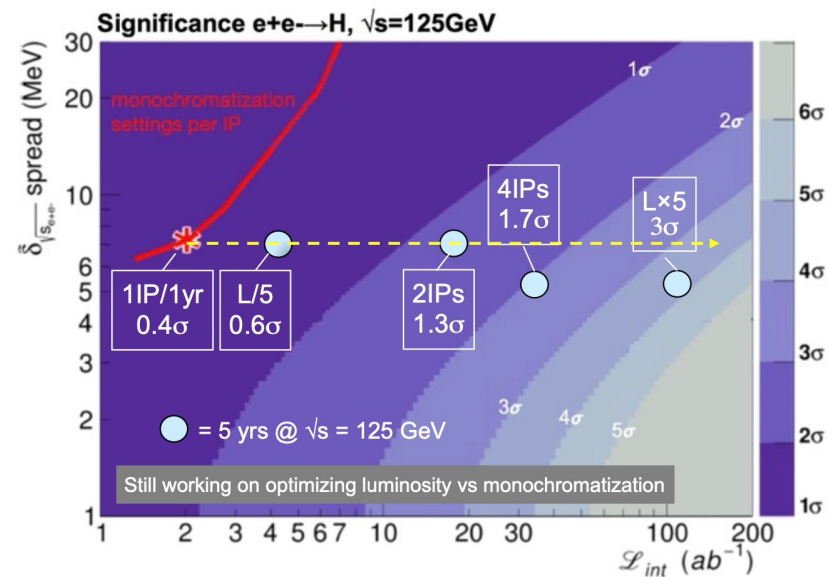
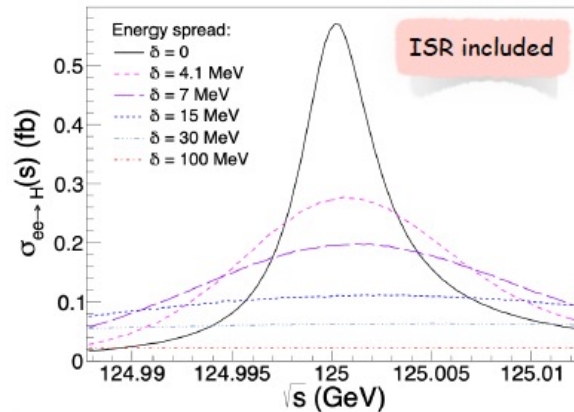
Sadly, there is no target

[2404.12809](https://arxiv.org/abs/2404.12809)

Fit includes top and WW data

Electron Yukawa (Aspirational)

- Run on the Higgs pole, $e^+e^- \rightarrow H$
- Want to establish Higgs coupling to 1st generation
- Need M_H to a few MeV, very large luminosity, precise control of beam energy



Note luminosity requirement

Closing Thoughts

- All proposed e^+e^- colliders give outstanding insights into Higgs couplings and SM parameters
- All proposed e^+e^- colliders give insights into BSM physics
- Many more opportunities than presented here
 - I did not discuss physics at the WW threshold
 - I did not discuss flavor (B and τ)
 - I did not discuss light quark Yukawas
- To maximize impact of the experimental measurements, a concerted theory effort is needed