General TOF Meeting

2024/10/02 (Wed)

Shunichiro Muraoka

Hiroshima University

TOF Simulation motivation

■Impact of BTOF material budget onto hpDIRC

• Currently, Barrel TOF material budget is required \sim 1% X/X0 I



For angular resolution @ hpDIRC surface (6 GeV/c $\rightarrow \Delta\theta = 0.5$ [mrad])

→ BTOF design is restricted by the material budget limitation

The design restriction has the potential to be a problem for the detector cooling (carbon does not have good thermal conductivity, limited amount of water for water cooling)

If we could increase the material budget...

More flexibility to change to a material with better thermal conductivity (e.g. Aluminum)

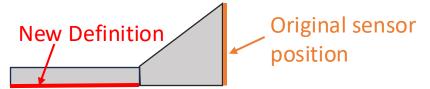


- BTOF simulation with changing its material budget is necessary to test the effects on hpDIRC
- → Quantitative Evaluation the BTOF material budget effects on the angular resolution at the hpDIRC surface

Determine the upper limit of material budget for BTOF

Simulation

- 1. Define the surface of hpDIRC using Geant4 (hpDIRC surface)
 - Because no particles are detected on the surface of the hpDIRC
 - To obtain MC information of particles at hpDIRC surface



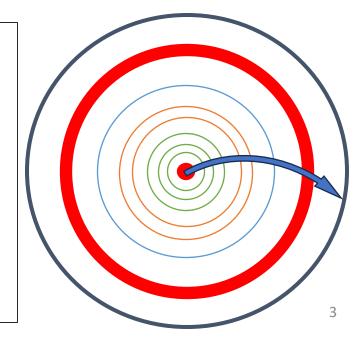
- 2. Calculate angle of incident particles from hit information (momentum) to detector
 - MC info(mc.theta): Use MC information of the detector defined in 1.
 - Track info(track.theta): Get values from propagation of reconstructed tracks from tracker

Tracker Detectors (Barrel)

- > Silicon Vertex Tracker × 3
- Silicon Barrel Tracker × 2
- Inner MPGD (Micro Pattern Gas Detector)
- Barrel TOF
- Outer MPGD

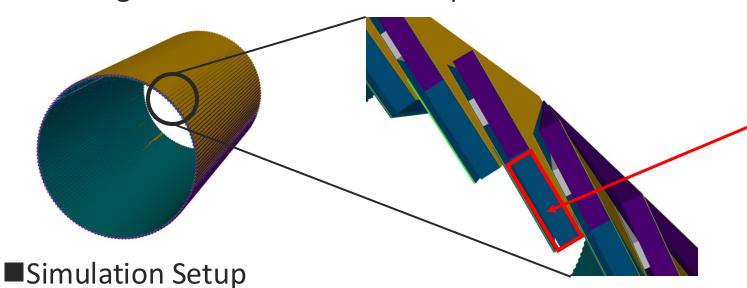
Kalman filter to reconstruct tracks

Using track parameter information on hpDIRC surface (r = 75.5 cm)



Simulation

3. Change the BTOF material and perform the same simulation



Carbon foam: 0.09 g/cm³, 5.8mm

~ 0.7 % (X/X0)

↓ Change material

Aluminum: 2.65 g/cm³

~ 7.1 % (X/X0)

• ElCrecon: Particle collision reconstruction using phythia8, Geant4, and track reconstruction algorithms

using ePIC detector structures are available.

• Single particle : π^- (1000 events)

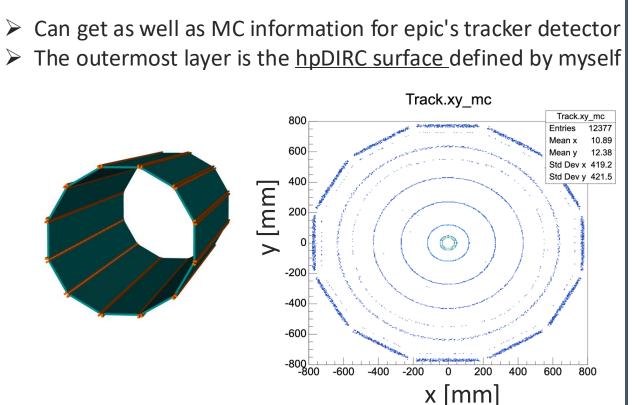
• Momentum : 1, 2, 4, 6, 8, 10 [GeV/c]

• Direction $: 0^{\circ} \le \phi \le 360^{\circ}$,

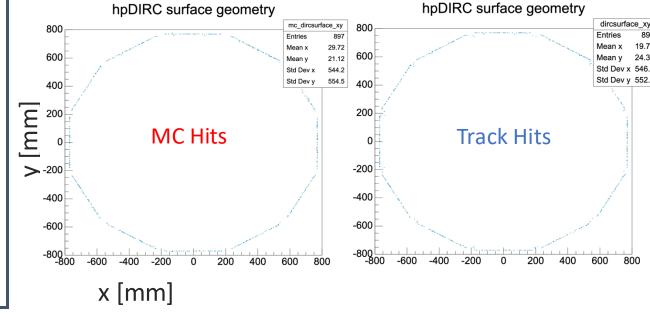
 $92^{\circ} \le \theta \le 94^{\circ} \Rightarrow \langle \eta \rangle = -0.05$

Results - Hit position on hpDIRC surface

- ■Generates 1000event single particles (6 GeV/c, $0^{\circ} \le \phi \le 360^{\circ}$, $92^{\circ} \le \theta \le 94^{\circ}$)
 - Get particle information on hpDIRC surface defined by Geant4 (MC info)



MC information and particle information obtained by propagating tracks on hpDIRC surface



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Results - Angular distribution on hpDIRC surface

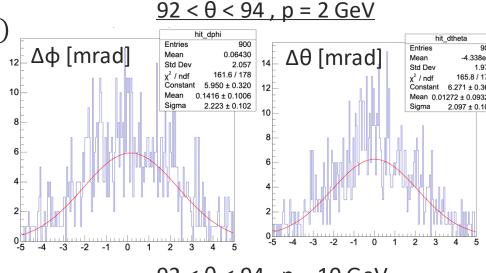
- ■Angular resolution calculated from particle momentum in MC and track information
 - $\Delta\theta = \theta(track) \theta(MC)$, $\Delta\phi = \phi(track) \phi(MC)$

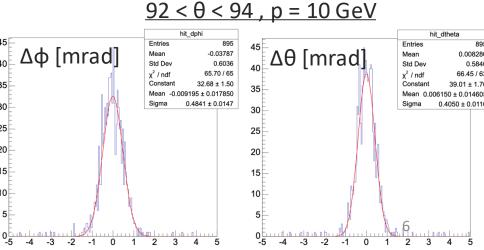
$$\Delta \phi = \phi(track) - \phi(MC)$$

•
$$\theta = arctan2\left(\sqrt{p_x^2 + p_y^2}, p_z\right), \qquad \phi = arctan2(p_y, p_x)$$

• The higher the momentum, the better the angular resolution.

 $\Delta\theta$ [mrad], 92 < θ < 94, p = 6 GeV $\Delta \phi \, [mrad] \, , \, 92 < \theta < 94 \, , \, p = 6 \, GeV$ **Entries** 897 **Entries** 0.001966 25 0.02478 Std Dev 91.52 / 92 y^2 / ndf 21.29 ± 0.98 18.78 ± 0.96 20 Mean 0.003930 ± 0.026578 Mean 0.02498 ± 0.03050 0.7147 ± 0.0213 0.7944 ± 0.0297 15 10 ²⁰²track.phi – mc.phi [mrad] track.theta – mc.theta [mrad]





Angular distribution on hpDIRC surface

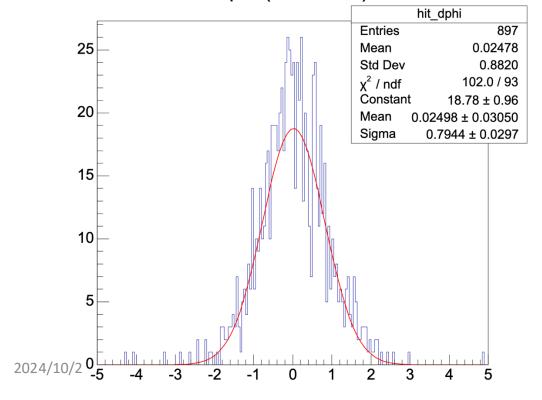
• Single particle : π^- (1000 events)

• Momentum : 1,2,4,6.8,10 [GeV/c]

• Direction $:0^{\circ} \le \phi \le 360^{\circ}$,

 $92^{\circ} \le \theta \le 94^{\circ} \Rightarrow \langle \eta \rangle = -0.05$

 $\Delta \phi$ [mrad], 92 < θ < 94, p = 6 GeV dphi (track-true)

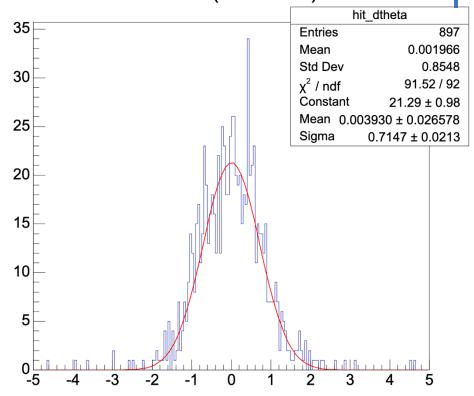


 $\sigma = 0.7147 \pm 0.0213 \, [mrad]$

Even if we use the carbon form (default setting), we cannot fulfill the request from hpDIRC

(<u>delta_angle=0.5mrad@6GeV</u>)

 $\Delta\theta$ [mrad], 92 < θ < 94, p = 6 GeV dtheta (track-true)



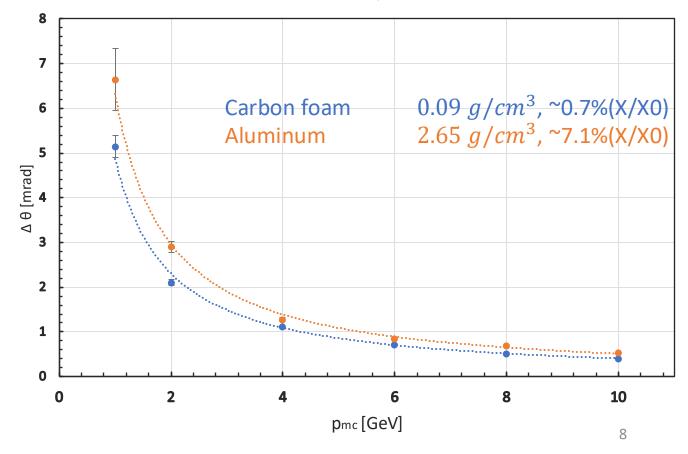
Results - Angular resolution on hpDIRC surface

- ■Results for some changes in particle momentum and BTOF material.
 - Part of BTOF Carbon foam changed to Aluminum
 - The value of $\Delta\theta$ increases



- Current structure (Carbon foam) does not satisfy hpDIRC requirements.
- Please tell me your opinion on this simulation

$$92 < \theta < 94$$
, $<\eta> = -0.05$



Back up

Data generation

■ Data Generation Settings

- ElCrecon: Particle collision reconstruction using phythia8, Geant4, and track reconstruction algorithms using ePIC detector structures are available.
- ddsim
- Single particle : π^- (1000 events)
- Momentum : 1, 2, 4, 6, 8, 10 [GeV/c]
- Direction $:0^{\circ} \le \phi \le 360^{\circ}, \\ 92^{\circ} \le \theta \le 94^{\circ} \to \langle \eta \rangle = -0.05$

```
ddsim --compactFile=$DETECTOR_PATH/epic.xml
    -N=1000
    --random.seed 1
    --enableGun
    --gun.particle "pi-"
    --gun.momentumMin "10*GeV" --gun.momentumMax "10*GeV"
    --gun.thetaMin 92.0*deg --gun.thetaMax 94.0*deg
    --gun.distribution uniform
    --outputFile epic fakedirc pi 10GeV_1000event_ddsim.edm4hep.root
```

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Detector settings

■BTOF material (epic/compact/tracking/tof_barrel.xml)

```
<module name="BarrelTOF Module1" vis="TOFBarrelModuleVis">
 <module_component name="sensor" material="Silicon" sensitive="true" width="BarrelTOF_Sensor_width" length="BarrelTOF_length1" thickness="BarrelTOF_Sensor_thickness" vis="TOFSensorVis" >
   <position x="BarrelTOF_Sensor_position" y="0" z="0" />
 </module component>
 <module_component name="hybridtop" material="Kapton" sensitive="false" width="BarrelTOF_Module_width" length="BarrelTOF_length1" thickness="BarrelTOF_Hybrid_thickness" vis="TOFHybridVis" >
   <position x="BarrelTOF_Service_position" y="0" z="0" />
 </module component>
 <module component name="cfskintop" material="CFRPMix2" sensitive="false" width="BarrelTOF Module width" length="BarrelTOF length1" thickness="BarrelTOF CFSkin thickness" vis="TOFCSkinVis" >
   <position x="BarrelTOF_Service_position" y="0" z="0" />
 </module component>
 <module_component name="coolingtube" material="Aluminum" sensitive="false" width="BarrelTOF_CoolingTube_width" length="BarrelTOF_length1" thickness="BarrelTOF_CoolingTube_thickness" vis="TOFCoolingTubeVis"</pre>
   <position x="BarrelTOF_CoolingTube_position" y="0" z="0" />
 </module component>
 <module_component name="coolant" material="NOVEC7200" sensitive="false" width="BarrelTOF_Coolant_width" length="BarrelTOF_length1" thickness="BarrelTOF_Coolant_thickness" vis="TOFCoolantVis" >
   <position x="BarrelTOF_Coolant_position" y="0" z="0" />
 </module_component>
 <module_component name="cfoam" material="Aluminum5083" sensitive="false" width="BarrelTOF_CFoam_width" length="BarrelTOF_length1" thickness="BarrelTOF_CFoam_thickness" vis="TOFCFoamVis" >
 <!--- <module_component name="cfoam" material="CarbonFoam" sensitive="false" width="BarrelTOF_CFoam_width" length="BarrelTOF_length1" thickness="BarrelTOF_CFoam_thickness" vis="TOFCFoamVis" > -->
   <position x="BarrelTOF_CFoam_position" y="0" z="0" />
 </module component>
 <module_component name="choneycomb" material="CFRPMix" sensitive="false" width="BarvelTOF_CHoneycomb_width" length="BarrelTOF_length1" thickness="BarrelTOF_CHoneycomb_thickness" vis="TOFCHoneycombVis" >
   <position x="BarrelTOF_CHoneycomb_position" y="0" z="-1*BarrelTOF_CFoam_thickness" />
 </module_component>
 <module_component name="cfskinbottom" material="CFRPMix2" sensitive="false" width="BarrelTOF_Module_width" length="BarrelTOF_length1" thickness="BarrelTOF_CFSkin_thickness" vis="TOFCSkinVis" >
   <position x="BarrelTOF_Service_position" y="0" z="0" />
 </module component>
 <module_component_name="hybridbottom" material="Kapton" sensitive="false" width="BarrelTOF_Module_width" length="BarcelTOF_length1" thickness="BarrelTOF_Hybrid_thickness" vis="TOFHybridVis" >
   <position x="BarrelTOF_Service_position" y="0" z="0" />
 </module component>
```

Changed material Default material

Detector settings

■hpDIRC surface (Referring to https://github.com/eic/athena/compact/fake_dirc.xml)

```
<constant name="DIRCModule_count"</pre>
                                                value="12" />
                                                value="17*mm" />
 <constant name="DIRCBar_thickness"</pre>
 <constant name="DIRCBar_length"</pre>
                                                value="DIRC_length-8*cm" />
 <constant name="DIRCSkinFront_thickness"</pre>
                                                value="2.5*mm" />
 <constant name="DIRCSkinBack_thickness"</pre>
                                                value="2.5*mm" />
                                                value="20*mm"/>
 <constant name="DIRCFrame_width"</pre>
 <constant name="DIRCFrame_length"</pre>
                                                value="DIRC_length"/>
 <constant name="DIRCFrame_thickness"</pre>
 <constant name="DIRCModule_rmax"</pre>
                                                value="DIRC_rmin + DIRCBar_thickness + DIRCSkinFront_thickness + DIRCSkinBack_thickness"/
                                                value="DIRCModule rmax - DIRC rmin" />
 <constant name="DIRCModule thickness"</pre>
 <constant name="DIRCFrame_rmax"</pre>
                                                value="DIRC_rmin + DIRCFrame_thickness" />
 <constant name="DIRCModule_halfangle"</pre>
                                                value="180*degree/DIRCModule_count" />
 <constant name="DIRCModule_width"</pre>
                                                value="2*DIRC_rmin * tan(DIRCModule_halfangle)"/>
 <constant name="DIRCModule_rmin"</pre>
                                                value="DIRC_rmin + 1*cm"/>
</define>
 <detector id="BarrelDIRC_ID" name="FakeDIRC" type="epic_FakeDIRC" readout="DIRCBarHits" vis="DIRCVis">
   <dimensions rmin="DIRC_rmin" rmax="DIRC_rmax" length="DIRC_length" />
    <position x="0" y="0" z="DIRC_offset" />
    <comment> Fake DIRC modules </comment>
    <module name="DIRCModule" vis="DIRCModuleVis">
     <module component name="FrontSkin"
             material="CarbonFiber"
             sensitive="false"
             width="DIRCModule_width"
             thickness="DIRCSkinFront_thickness"
             vis="DIRCSupportVis"
             length="DIRCBar_length" />
      <module_component name="QuartzBar"
             material="Quartz"
             sensitive="true"
             width="DIRCModule_width"
             thickness="DIRCBar thickness"
             vis="DIRCBarVis"
             length="DIRCBar_length" />
      <module_component name="BackSkin"
             material="CarbonFiber"
             sensitive="false"
             width="DIRCModule width"
             thickness="DIRCSkinBack_thickness"
             vis="DIRCSupportVis"
             length="DIRCBar_length" />
     <frame material="StainlessSteel"</pre>
             width="DIRCFrame_width"
              length="DIRCFrame_length"
             thickness="DIRCFrame_thickness" />
    </module>
```

```
</module>
            <comment> Fake DIRC layers </comment>
            <layer module="DIRCModule" id="1" vis="DIRCLayerVis">
               <barrel_envelope</pre>
                 inner_r="DIRC_rmin"
                 outer_r="DIRC_rmax"
                 z_length="DIRC_length" />
               <rphi_layout</pre>
                phi_tilt="0"
                 nphi="DIRCModule_count"
                 phi0="0"
                 rc="0.5*(DIRCModule_rmin+DIRCModule_rmax)"
                dr="0" />
               <z layout
                 dr="0.0*mm"
                 z0="0.0*mm"
                 nz="1" />
            </laver>
          </detector>
        </detectors>
        <readouts>
          <readout name="DIRCBarHits">
            <segmentation type="CartesianGridXY" grid size x="3.0*mm" grid size y="3.0*mm" />
            <id>system:8, layer:4, module:8, section:4, x:32:-16, y:-16</id>
          </readout>
        </readouts>
135
      </lccdd>
```

About Analysis Code

■MC information (edm4hep::SimTrackerHit)

```
304 ~
          std::vector<std::string> sim data names = {
              "VertexBarrelHits",
                                          // Vertex
              "SiBarrelHits",
                                          // Barrel Tracker
              "MPGDBarrelHits",
                                          // MPGD
              "TOFBarrelHits",
              "OuterMPGDBarrelHits",
                                          // MPGD DIRC
              "TrackerEndcapHits",
                                          // End Cap tracker
              "TOFEndcapHits",
                                          // End Cap TOF
              "DIRCBarHits",
          for(int i = 0; i < sim_data_names.size(); i++ ) {</pre>
              auto data_name = sim_data_names[i];
              const auto &hits = *static_cast<const edm4hep::SimTrackerHitCollection*>(event->GetCollectionBase(data_name));
              const char* Data_name = data_name.c_str(); //fprintfに出力する際に文字化けを防ぐための措置
              for(auto hit: hits) {
                  auto& mcinfo = hit.getMCParticle();
                  auto& pos = hit.getPosition();
                  auto& mom = hit.getMomentum();
                  auto r = sqrt(pos.x*pos.x + pos.y*pos.y + pos.z*pos.z);
                  auto rt = sqrt(pos.x*pos.x + pos.y*pos.y);
                  auto p = sqrt(mom.x * mom.x + mom.y * mom.y + mom.z * mom.z);
                  auto pt = sqrt(mom.x * mom.x + mom.v * mom.v);
                  auto eta = -log(tan(atan2(sgrt(mom.x*mom.x*mom.y*mom.y),mom.z)/2.));
                  auto phi = atan2(mom.y, mom.x);
                  auto theta = atan2(sqrt(mom.x*mom.x + mom.y*mom.y), mom.z);
                  if (mcinfo.getGeneratorStatus() != 1) continue;
                  auto pdg = mcinfo.getPDG();
                  auto& mcmom = mcinfo.getMomentum();
                  auto status = mcinfo.getGeneratorStatus();
                  auto mcp = sqrt(mcmom.x * mcmom.x + mcmom.y * mcmom.y + mcmom.z * mcmom.z);
                  auto mceta = -log(tan(atan2(sgrt(mcmom.x*mcmom.x*mcmom.y*mcmom.y),mcmom.z)/2.));
                  Track_xy_mc -> Fill(pos.x, pos.y);
                  if(pos.x > 0)Track_rz_mc -> Fill(pos.z, rt);
                      else Track rz mc -> Fill(pos.z, -rt);
           fprintf (outputfileMC, "%s r:%f, rt:%f, p:%f, eta:%f, phi:%f, theta:%f, cp:%f, mceta:%f, pdg:%d\n",Data_name, r, rt, p, eta, phi, theta, mcp, mceta, pdg); 2024/10/2
```

About Analysis Code

■ Track information (Referring to https://github.com/eic/EICrecon/src/algorithms/tracking/TrackPropagation.cc)

```
const auto &dirc = *static_cast<const edm4hep::SimTrackerHitCollection*>(event->GetCollectionBase("DIRCBarHits"));
                                                                                                                                                      auto reso eta = (eta - mceta)/mceta * 100;
for(auto hit: dirc) {
                                                                                                                                                      auto reso phi = (phi - mcphi)/mcphi * 100;
    auto& mcinfo = hit.getMCParticle();
                                                                                                                                                      auto reso theta = (theta - mctheta)/mctheta * 100;
   auto& mcpos = hit.getPosition();
                                                                                                                                                      auto deta = (eta - mceta)* 1000;
   auto& mcmom = hit.getMomentum();
                                                                                                                                                      auto dphi = (phi - mcphi)* 1000;
                                                                                                                                                      auto dtheta = (theta - mctheta)* 1000;
   if (mcinfo.getGeneratorStatus() != 1) continue;
   if (i != 0 ) continue;
                                                                                                                                                      hit_true_eta -> Fill(mceta);
                                                                                                                                                      hit_true_phi -> Fill(mcphi);
    auto mcr = sqrt(mcpos.x*mcpos.x + mcpos.y*mcpos.y + mcpos.z*mcpos.z);
                                                                                                                                                      hit_true_theta -> Fill(mctheta);
    auto mcrt = sqrt(mcpos.x*mcpos.x + mc
                                                                                                                                                      hit resolution eta -> Fill(reso eta);
   auto mcp = sqrt(mcmom.x * mcmom.x + m <error-type> &mcmom lom.z * mcmom.z);
                                                                                                                                                      hit_resolution_phi -> Fill(reso_phi);
   auto mcpt = sqrt(mcmom.x * mcmom.x + mcmom.y * mcmom.y);
                                                                                                                                                      hit_resolution_theta -> Fill(reso_theta);
    auto mceta = -log(tan(atan2(sqrt(mcmom.x*mcmom.x+mcmom.y*mcmom.y),mcmom.z)/2.));
                                                                                                                                                      hit_deta -> Fill(deta);
   auto mctheta = atan2(sqrt(mcmom.x*mcmom.x + mcmom.y*mcmom.y), mcmom.z);
                                                                                                                                                      hit_dphi -> Fill(dphi);
                                                                                                                                                      hit_dtheta -> Fill(dtheta);
    auto mcphi = atan2(mcmom.y, mcmom.x);
                                                                                                                                                      Hitpoints_dircsurface_mc_xy -> Fill(mcpos.x, mcpos.y);
                                                                                                                                                      Hitpoints_dircsurface_mc_z -> Fill(mcpos.z);
                                                                                                                                                      fprintf (outputfileMC, "DIRCsurface r:%f, rt:%f, p:%f, eta:%f, phi:%f, theta:%f\n", mcr, mcrt, mcp, mceta, mcphi, mctheta);
   std::unique_ptr<edm4eic::TrackPoint> hpdirc_point;
    const auto hpdircR = mcrt;
   const auto hpdircMinZ = -2526.0;
    const auto hpdircMaxZ = 1850.0;
    auto hpdircBounds = std::make_shared<Acts::CylinderBounds>(hpdircR, (hpdircMaxZ-hpdircMinZ)/2);
    auto hpdirc_t = Acts::Translation3(Acts::Vector3(0, 0, (hpdircMaxZ+hpdircMinZ)/2));
   auto hpdirc_trf = Acts::Transform3(hpdirc_t);
    hpdirc_surface = Acts::Surface::makeShared<Acts::CylinderSurface>(hpdirc_trf, hpdircBounds);
   try {hpdirc_point = m_propagation_algo.propagate(edm4eic::Track{}), trajectory, hpdirc_surface);}
   catch(std::exception &e) {throw JException(e.what());}
   if(!hpdirc_point) {
                                                                                                                                                                     Get the parameters of the reconstructed track
    fprintf (outputfileTrack,"could not propagate!\n");
                                                                                                                                                                        at any r.
       auto pos = hpdirc_point->position;
       auto mom = hpdirc point->momentum;
       auto length = hpdirc point->pathlength;
       auto theta = hpdirc_point->theta;
       auto phi = hpdirc_point->phi;
                                                                                                                                                                        (Trajectory
       auto eta = -log(tan(atan2(sqrt(mom.x*mom.x + mom.y*mom.y),mom.z)/2.));
       auto r = sqrt(pos.x*pos.x + pos.y*pos.y + pos.z*pos.z);
       auto rt = sqrt(pos.x*pos.x + pos.y*pos.y);
                                                                                                                                                                        → CentralCKFActsTrajectories)
       Track_xy -> Fill(pos.x, pos.y);
       Hitpoints_dircsurface_xy -> Fill(pos.x, pos.y);
       Hitpoints_dircsurface_z -> Fill(pos.z);
       if(pos.x > 0)Track_rz -> Fill(pos.z, rt);
               else Track_rz -> Fill(pos.z, -rt);
       hit_propagate_eta -> Fill(eta);
       hit_propagate_phi -> Fill(phi);
```

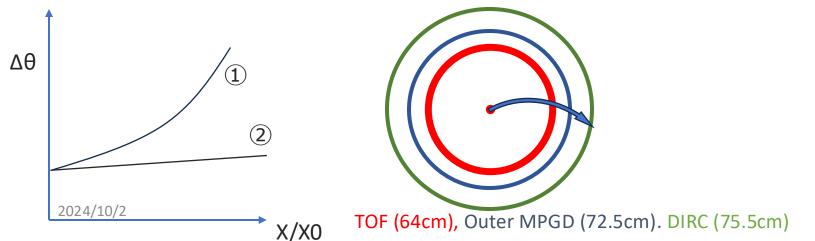
_hit_propagate_theta -> Fill(theta);
fprintf (outputfileTrack, "Reconstructed DIRC hit x:%f, y:%f, z:%f, r:%f, rt:%f, theta:%f, phi:%f\n", pos.x, pos.y, pos.z, length, rt, theta, phi);

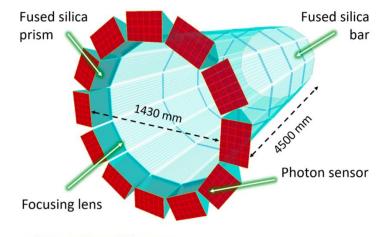
fprintf (outputfileTrack, "MC DIRCsurface x:%f, y:%f, z:%f, r:%f, rt:%f, theta:%f, phi:%f, p:%f\n", mcpos.x, mcpos.y, mcpos.z, mcr, mcrt, mctheta, mcphi, mcp)

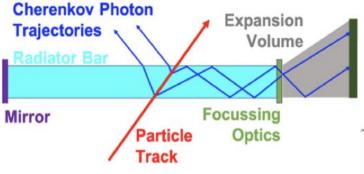
Motivation

■ Estimating the impact of BTOF material budgets on the backward detector (hpDIRC)

- > hpDIRC (high performance Detection of Internally Reflected Cherenkov light)
- Cherenkov Particle Identification Detector
- Particle identification from the emission angle of Cherenkov light emitted by charged particles
- \rightarrow Angular resolution at the surface is important (6 GeV/c \rightarrow $\Delta\theta$ = 0.5 [mrad])
- ➤ Increase in BTOF material budget
 →Angular resolution degrades due to multiple scattering effects? ①
 or
 - → The presence of MPGD reduces the effects of multiple scattering? ②





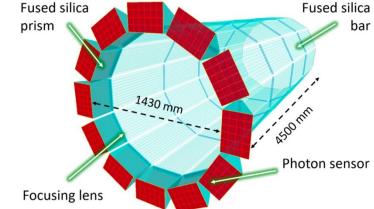


Motivation

- Estimating the impact of BTOF material budgets on the backward detector (hpDIRC)
 - > hpDIRC (high performance Detection of Internally Reflected Cherenkov light)
 - Cherenkov Particle Identification Detector
 - Particle identification from the emission angle of Cherenkov light emitted by charged particles
 - \rightarrow Angular resolution at the surface is important (6 GeV/c \rightarrow $\Delta\theta$ = 0.5 [mrad])

X/X0

- ➤ Increase in BTOF material budget
 →Angular resolution degrades due to multiple scattering effects? ①
 or
 - → The presence of MPGD reduces the effects of multiple scattering? ②



Δθ

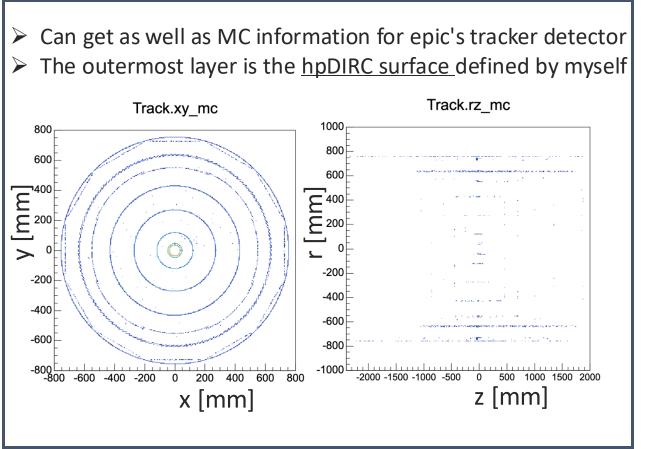
Quantitative evaluation of the relationship between angular resolution and BTOF material budget on hpDIRC surfaces



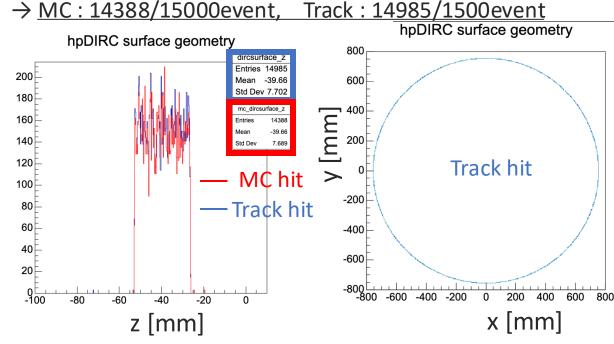
Determine the upper limit of material budget for BTOF

Results - Hit position on hpDIRC surface

- ■Generates 15000event single particles (6 GeV/c, $0^{\circ} \le \phi \le 360^{\circ}$, $92^{\circ} \le \theta \le 94^{\circ}$)
 - Get particle information on hpDIRC surface defined by Geant4 (MC info)



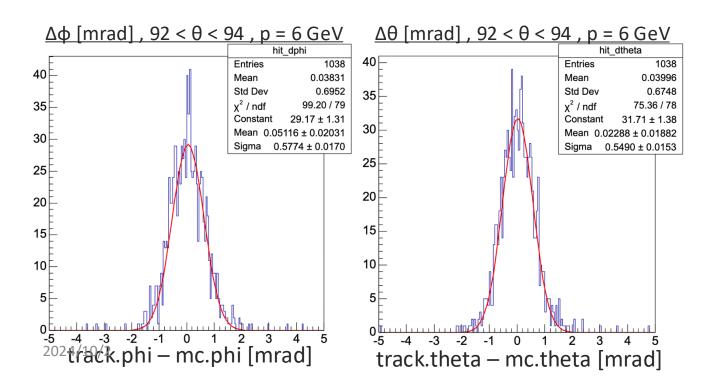
MC information and particle information obtained by propagating tracks on hpDIRC surface

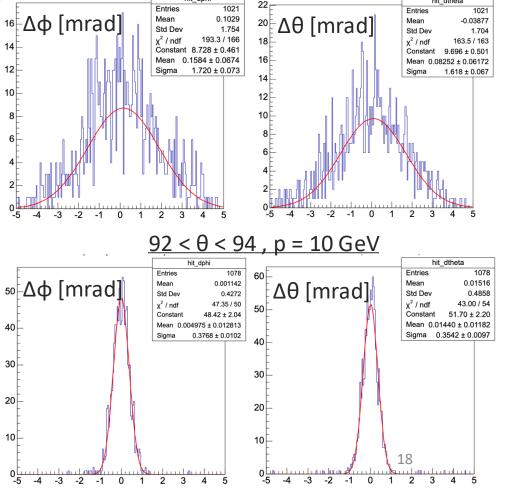


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Results - Angular distribution on hpDIRC surface

- ■Angular resolution calculated from particle momentum in MC and track information
 - $\Delta \theta = \theta(track) \theta(MC), \qquad \Delta \phi = \phi(track) \phi(MC)$
 - $\theta = arctan2\left(\sqrt{p_x^2 + p_y^2}, p_z\right), \qquad \phi = arctan2(p_y, p_x)_{16}$
 - The higher the momentum, the better the angular resolution.





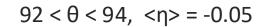
 $92 < \theta < 94$, p = 2 GeV

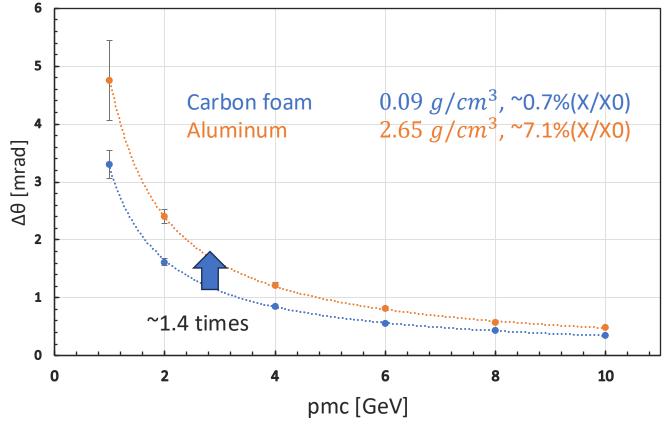
Results - Angular resolution on hpDIRC surface

- ■Results for some changes in particle momentum and BTOF material.
 - Part of BTOF Carbon foam changed to Aluminum
 - The value of $\Delta\theta$ increases



- Angular resolution $\Delta\theta$ is bad
- Maybe there is a mistake in the calculation method, etc.

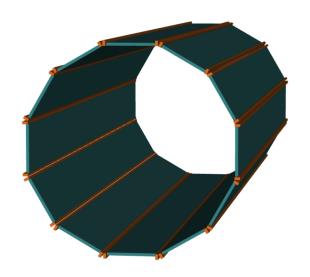


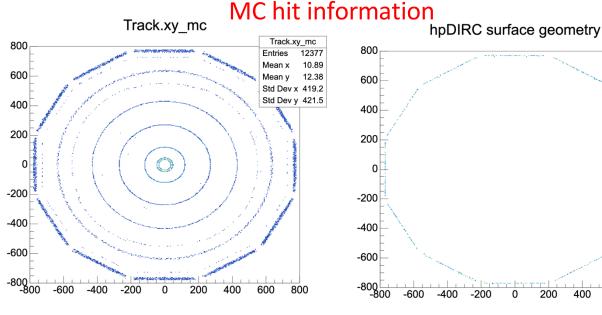


hpDIRC surface geometry (defined by Geant4)

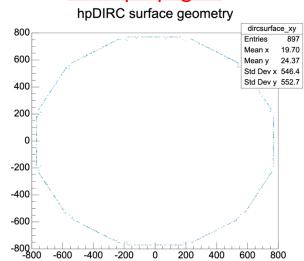
■New geometry

Improved structure of regular dodecagonal columns instead of cylindrical





Track propagate



mc_dircsurface_xy

Std Dev x

Std Dev y

400

600

29.72

21.12

544.2

554.5