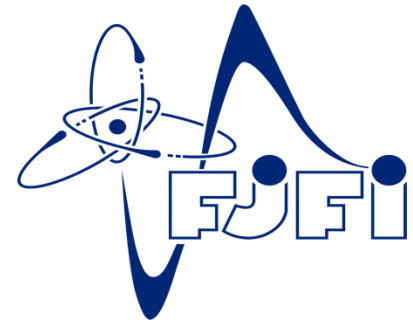
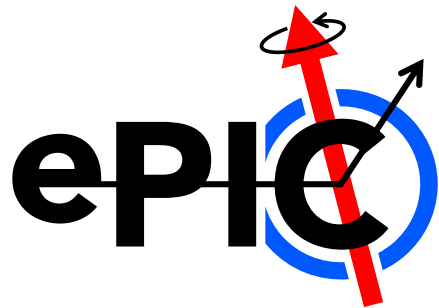


# Neutral energy reconstruction via charged hadron correction in nHCal

Subhadip Pal

Czech Technical University in Prague



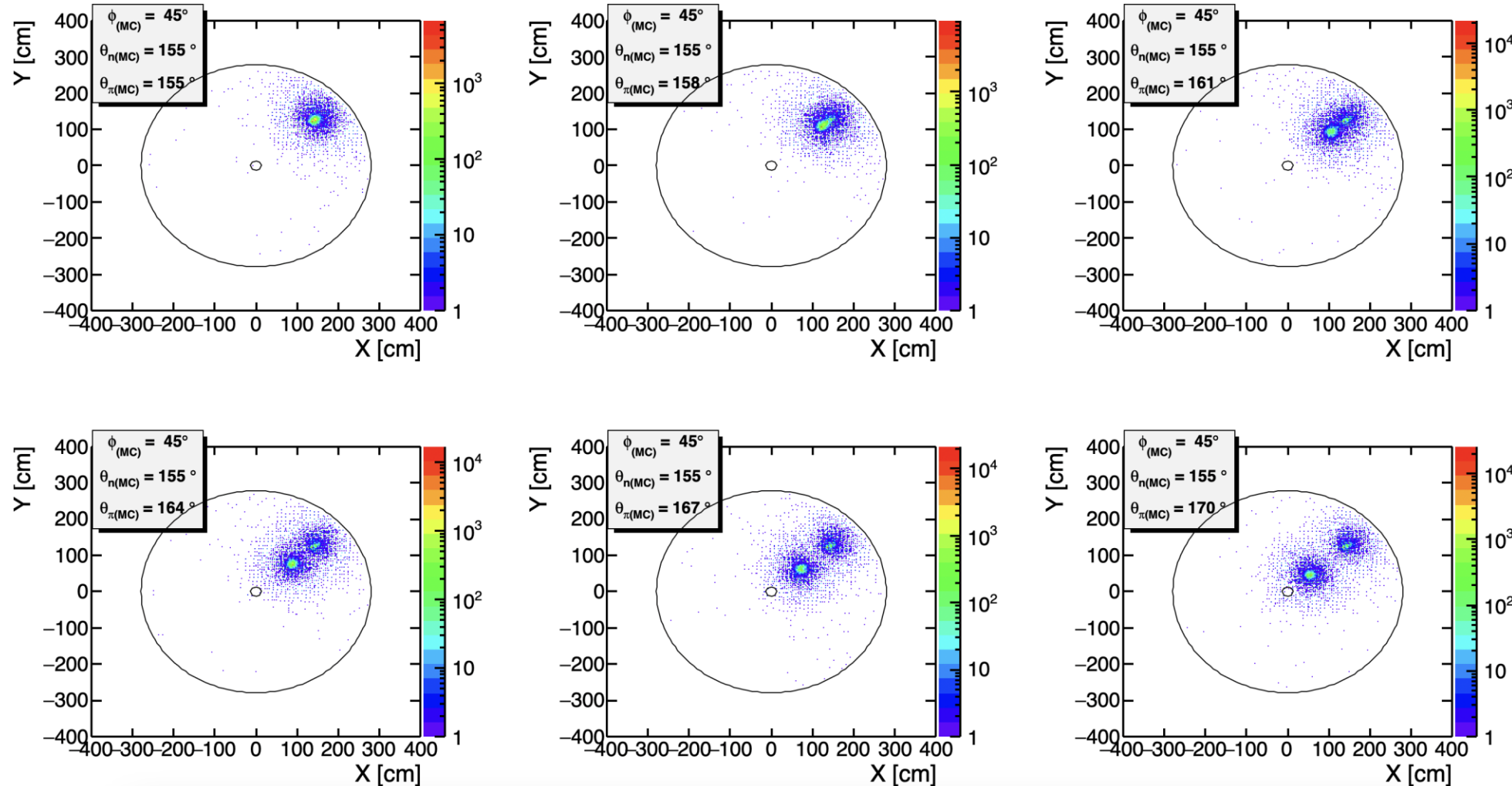
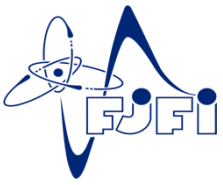
*ePIC calorimetry meeting–December 17, 2024*

**Objective** : Use clusters to distinguish between neutron/pion shower reconstruction.

- ☐  $(1 n + 1 \pi^-) / \text{event.}$  ---- Standalone ddsim
- ☐  $\varphi = 45^\circ$ 
  - $\theta_n = 155^\circ$  ( $\eta = -1.51$ ) ----- fixed
  - $\theta_\pi = 155^\circ$  ( $\eta = -1.51$ ),  $158^\circ$  ( $\eta = -1.64$ ),  
 $161^\circ$  ( $\eta = -1.79$ ),  $164^\circ$  ( $\eta = -1.96$ ),  
 $167^\circ$  ( $\eta = -2.17$ ),  $170^\circ$  ( $\eta = -2.44$ )

- Only Backward HCal was taken into account [not the whole ePIC geometry – scattering effects neglected]
- $-4.14 < \eta < -1.18$
- Alternating Steel and Scintillator slices
- 10 cm. x 10 cm. Polystyrene tiles

# Cluster Positions (xy coordinates)



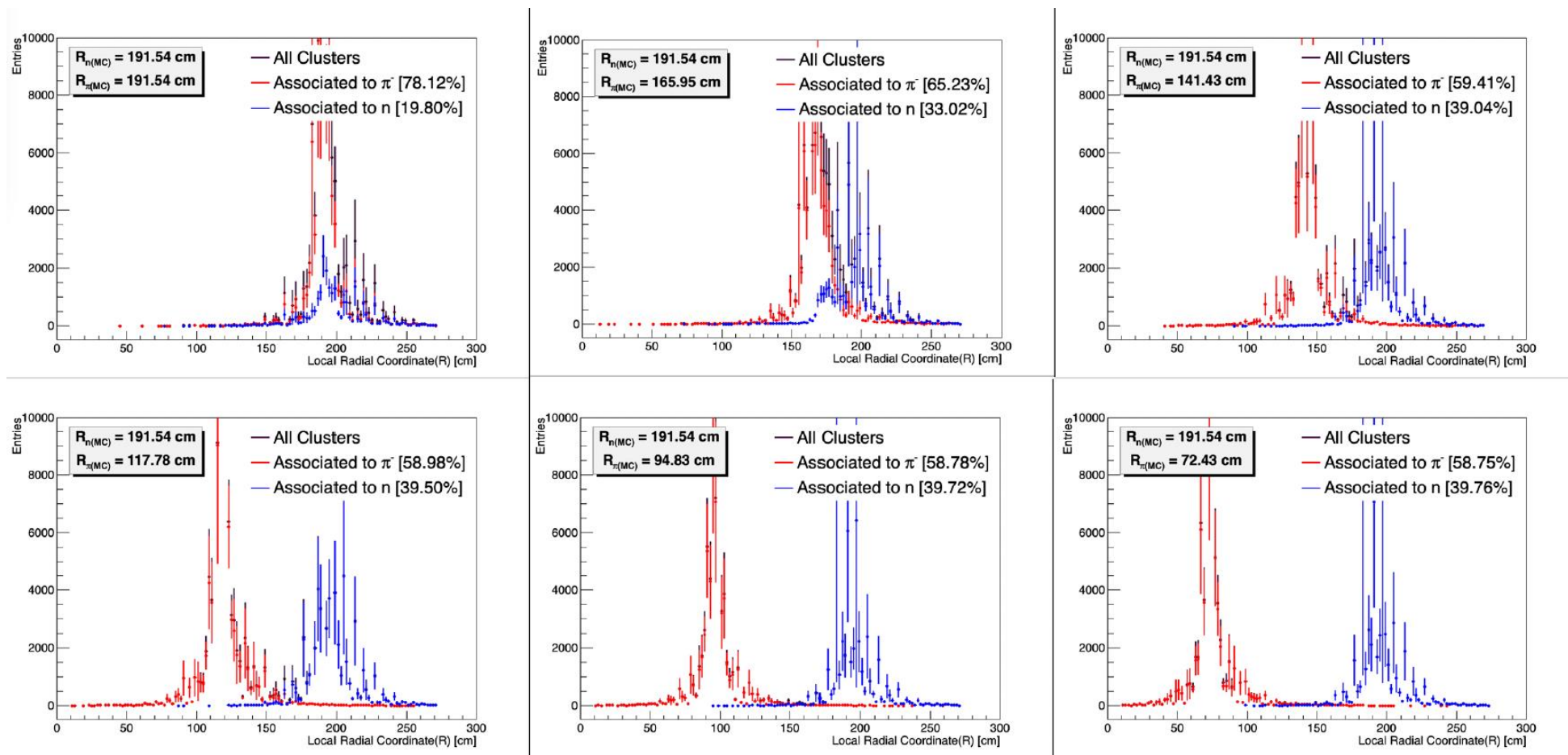
Cluster (x,y) are shown along with simulated angular coordinates

$p = 1 \text{ GeV}/c$

[neutron showers in outer region; pion showers in inner region]

Distributions are becoming more distinguishable as  $(\theta_{\pi} - \theta_n)$  increases...

# Cluster Radial Coordinates



$p = 1 \text{ GeV}/c$

Percentages (fraction of clusters identified as  $\pi$ -/ $n$  clusters) are based on ClusterMCParticle associations

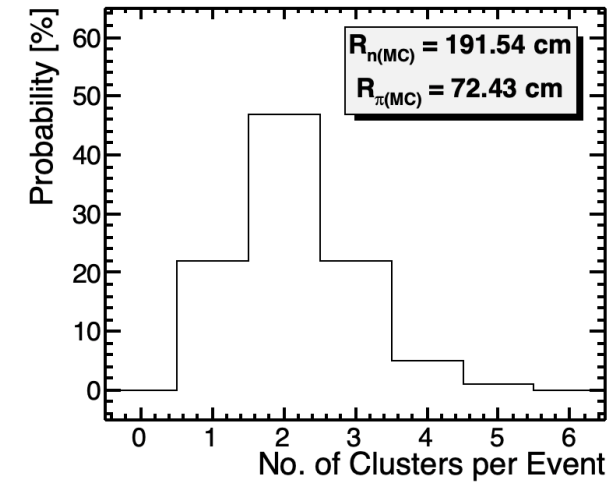
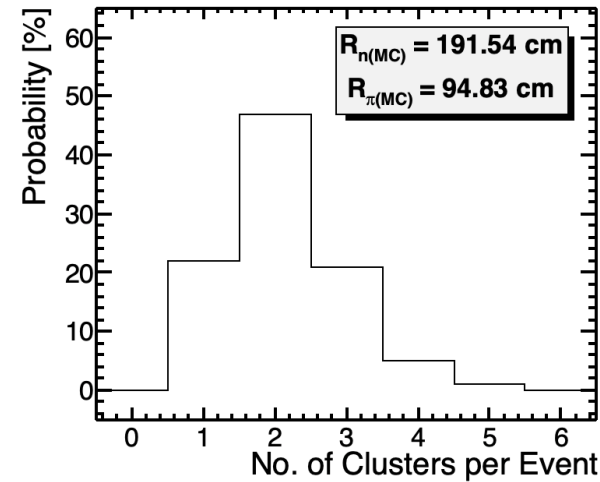
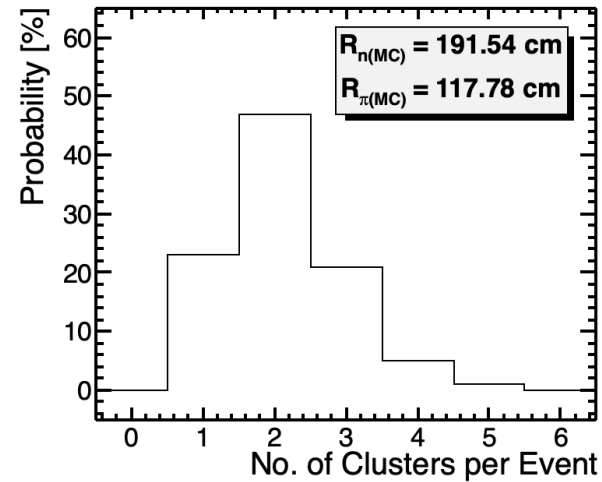
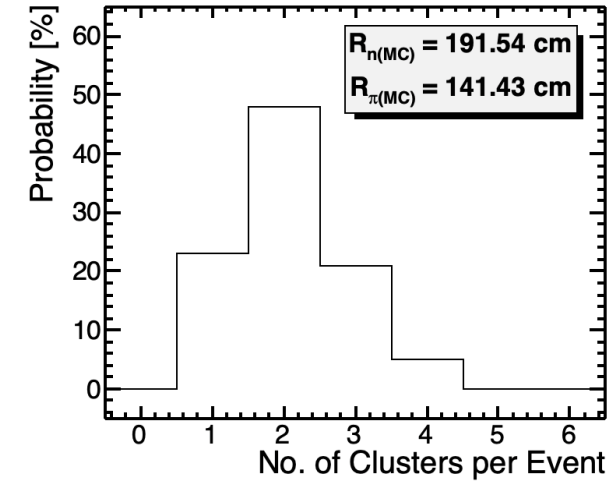
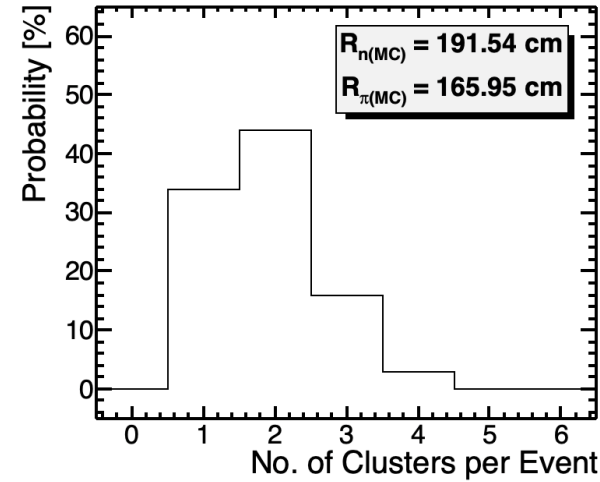
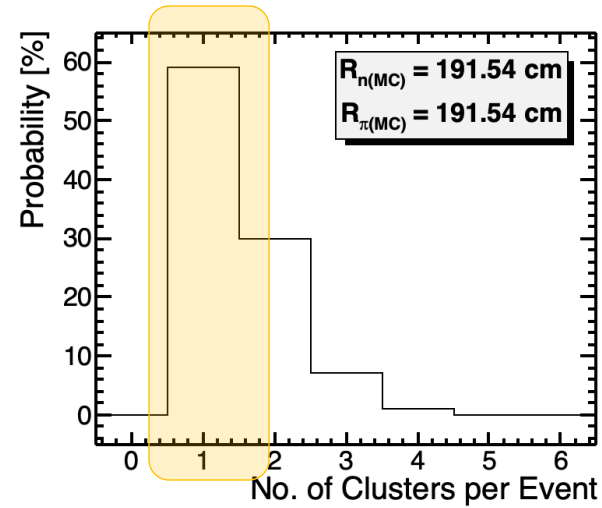
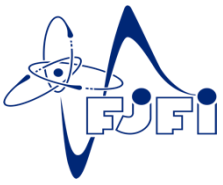
[better performance as the  $\pi$ - $n$  distance increases]

Neutron clusters are “confused” to be pion clusters as the showers start to overlap.

$\pi : n \approx 60:40$  when  $\Delta R_{\text{clusters}} \geq 50.11 \text{ cm}$

$\approx 80:20$  when  $\Delta R_{\text{clusters}} = 0 \text{ cm}$

# Cluster Reconstruction



As the showers start to overlap, neutron hits are “hijacked” into pion clusters.

- ❑ Tests of a particle flow algorithm with CALICE test beam data, 2011  
[CALICE Collaboration \(https://doi.org/10.1088/1748-0221/6/07/P07005\)](https://doi.org/10.1088/1748-0221/6/07/P07005)
- ❑ Particle flow calorimetry and the PandoraPFA algorithm, 2009  
[M.A. Thomson \(https://doi.org/10.1016/j.nima.2009.09.009\)](https://doi.org/10.1016/j.nima.2009.09.009)

The previous four stages of the PandoraPFA algorithm are found to perform well for jets with energy less than about 50 GeV. At higher energies the jet energy resolution degrades due to the increasing overlap between the hadronic showers from different particles. It is possible to detect such reconstruction failures by comparing the charged cluster energy,  $E_C$ , with the momentum of the associated track,  $p$ . A possible reconstruction failure is identified if  $|(E_C - p)/\sigma_{E_C}| > \text{ChiToAttemptReclustering} [3.0]$ . In this case the PandoraPFA algorithm attempts to find a more self-consistent clustering of the calorimeter hits. If, for example, a 10 GeV track is associated with a 20 GeV calorimeter cluster, shown schematically in Fig. 5(a), a potential reconstruction failure is identified. One possible approach would be to simply remove hits from the cluster until the cluster energy matched the track momentum. However, this does not use the full information in the event. Instead, the clustering algorithm is modified iteratively

Not done in this study

<https://www.hep.phy.cam.ac.uk/~thomson/pandoraPFA/>

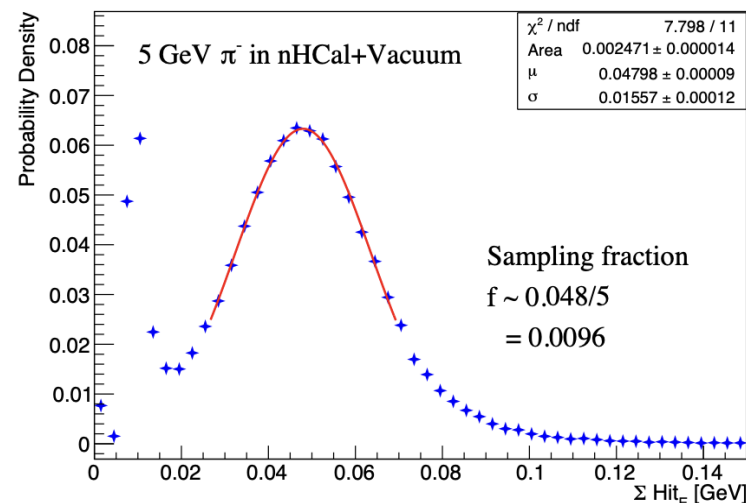
$$|(E_C - p)/\sigma_{E_C}| > \text{ChiToAttemptReclustering} [3.0].$$

Condition to determine possible reconstruction failure and make charged particle correction

$E_C$  = Energy of the cluster that is matched to a track

$p$  = Momentum obtained from tracking

$\sigma_{E_C}$  = uncertainty on the cluster energy due to hadronic nature of energy deposition





$$|(E_C - p)/\sigma_{E_C}| > \text{ChiToAttemptReclustering} [3.0].$$

$E_C$  = Energy of the cluster that is matched to a track

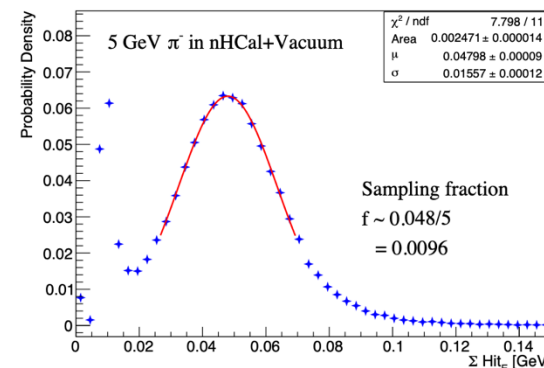
$p$  = Momentum obtained from tracking

$\sigma_{E_C}$  = uncertainty on the cluster energy due to hadronic nature of energy deposition

Energy of Pion Cluster based on ClusterMCParticleAssociation

Momentum of generated Pion

$$\sigma_{E_C} = \frac{\sigma f_p}{f_{EICreco}} E_C$$




Uncertainty in sampling fraction ( $f$ ) depending on the momentum ( $p$ ) of the track



If  $|(E_C - p)/\sigma_{E_C}| > \text{ChiToAttemptReclustering [3.0]}$ .

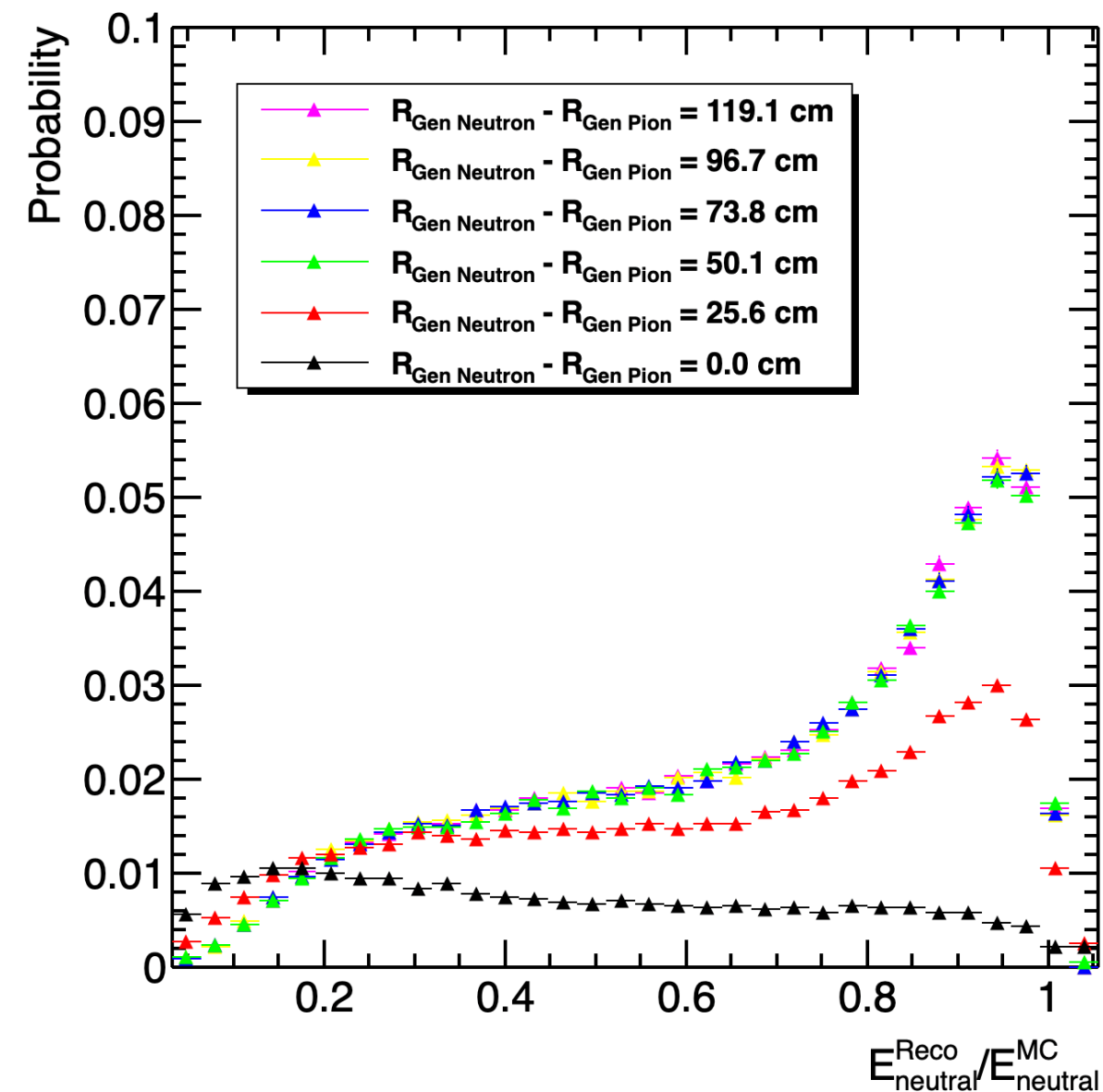
$$E_{neutral}^{Reco} = E_{total}^{Reco} - p$$



Energy hijacking  
(aka “confusion”)  
was involved

Else,  $E_{neutral}^{Reco} = E_{total}^{Reco} - E_{charged}^{Reco}$

# Charged Particle Correction



When,  $|(E_{\text{charged}}^{\text{Reco}} - p) / \sigma_{E_{\text{charged}}^{\text{Reco}}}| > 3.0$

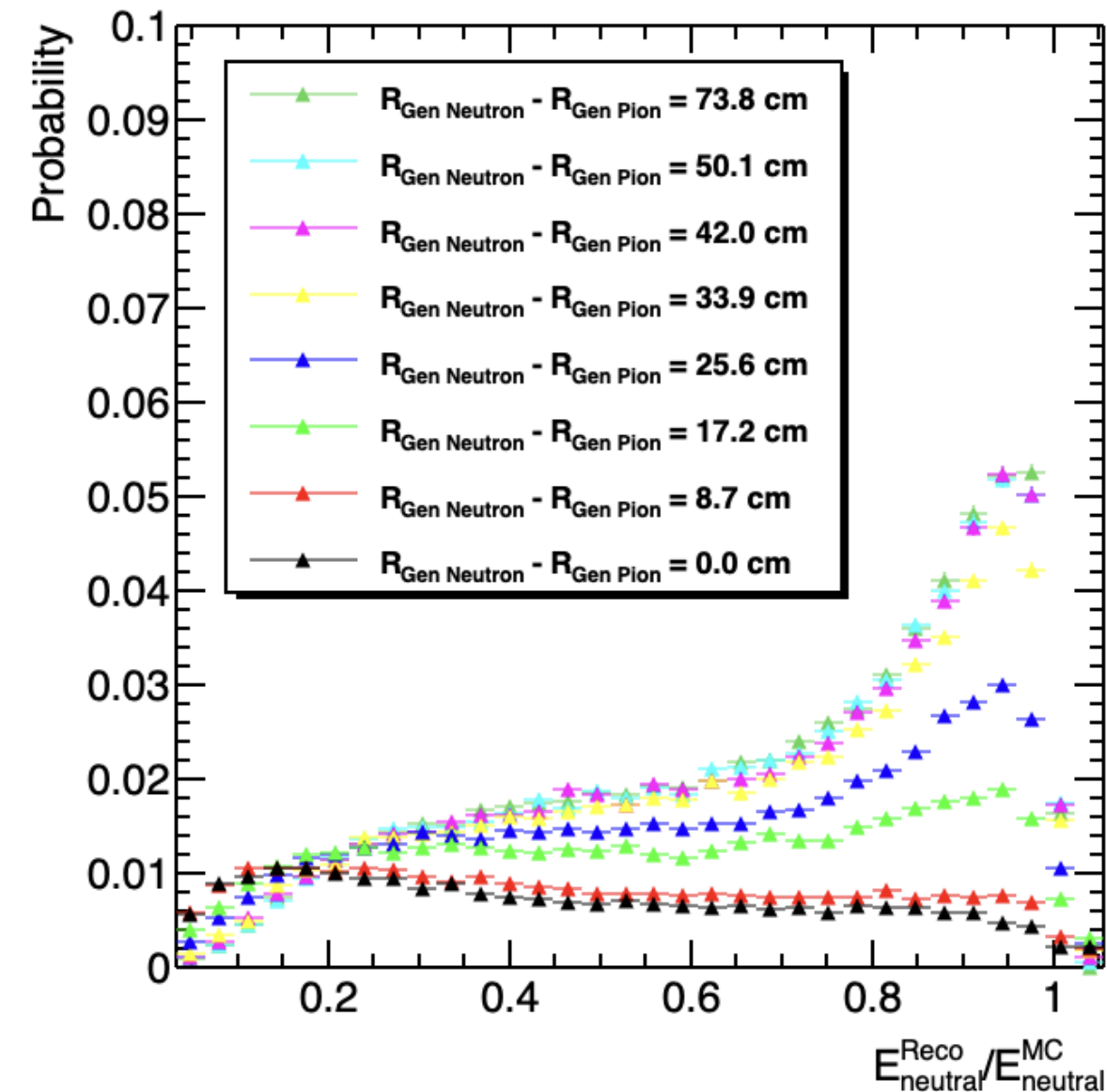
$$E_{\text{neutral}}^{\text{Reco}} = E_{\text{total}}^{\text{Reco}} - p$$

Otherwise,

$$E_{\text{neutral}}^{\text{Reco}} = E_{\text{total}}^{\text{Reco}} - E_{\text{charged}}^{\text{Reco}}$$

$E_{\text{neutral}}^{\text{MC}}$  = MC energy deposition by neutron

# Charged Particle Correction



When,  $|(E_{\text{charged}}^{\text{Reco}} - p)/\sigma_{E_{\text{charged}}^{\text{Reco}}}| > 3.0$

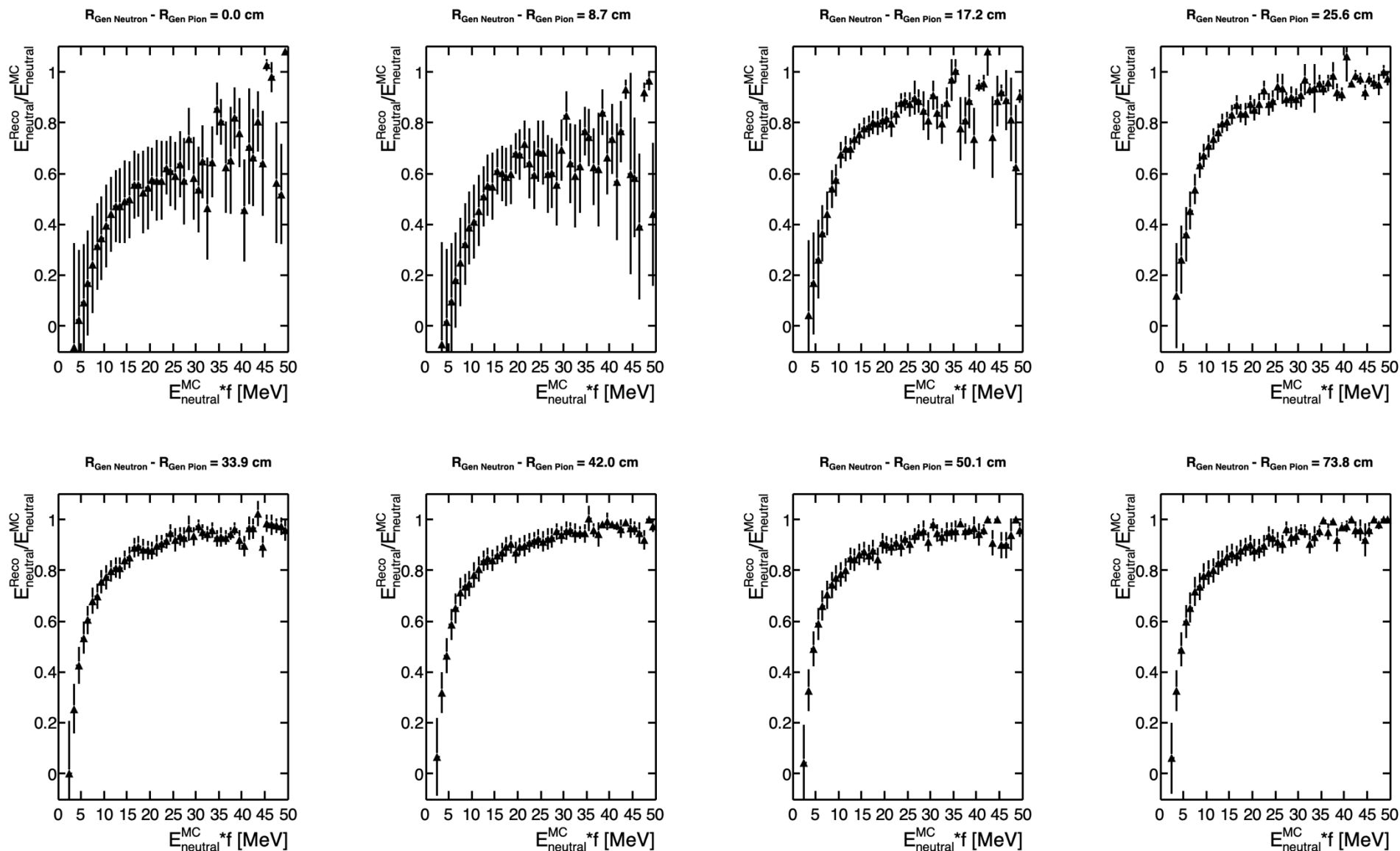
$$E_{\text{neutral}}^{\text{Reco}} = E_{\text{total}}^{\text{Reco}} - p$$

Otherwise,

$$E_{\text{neutral}}^{\text{Reco}} = E_{\text{total}}^{\text{Reco}} - E_{\text{charged}}^{\text{Reco}}$$

$$E_{\text{neutral}}^{\text{MC}} = \text{MC energy deposition by neutron}$$

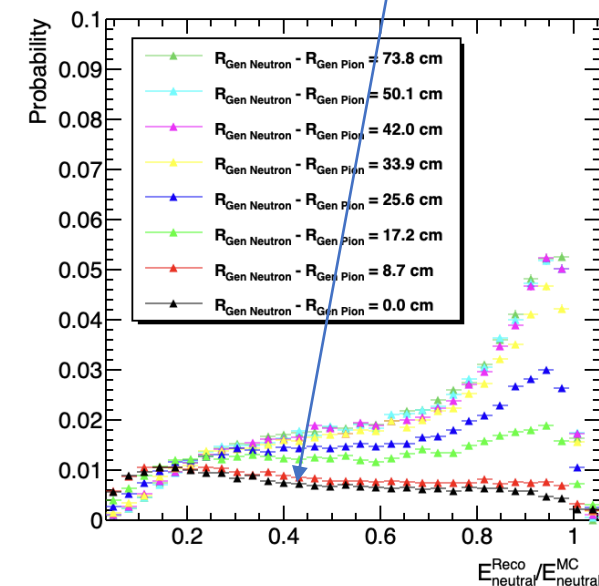
# Charged Particle Correction



$E_{\text{neutral}}^{\text{MC}} * f$  = the actual (not corrected to sampling fraction) energy deposition on the Sci-tiles

Performance improves with increasing  $E_{\text{neutral}}^{\text{MC}} * f$

Plots with more uncertainty corresponds to flat distributions below

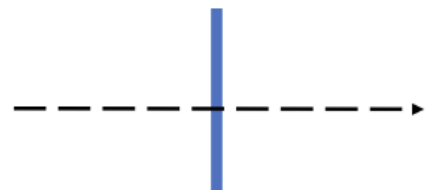




When,  $|(E_{charged}^{Reco} - p)/\sigma_{E_{charged}^{Reco}}| > 3.0$

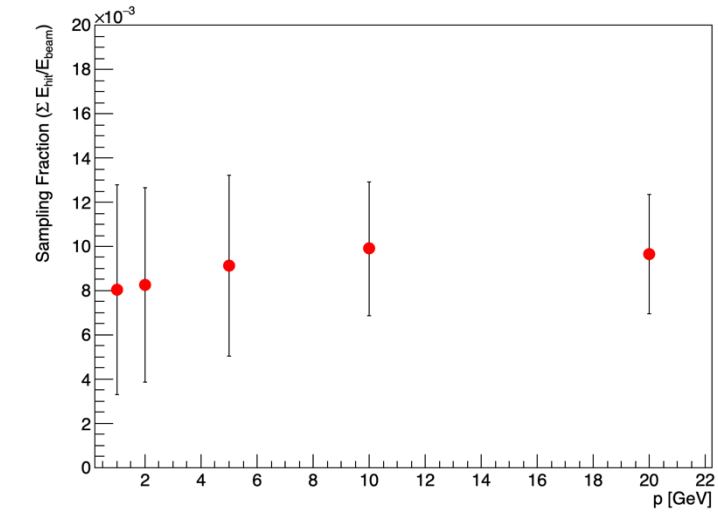
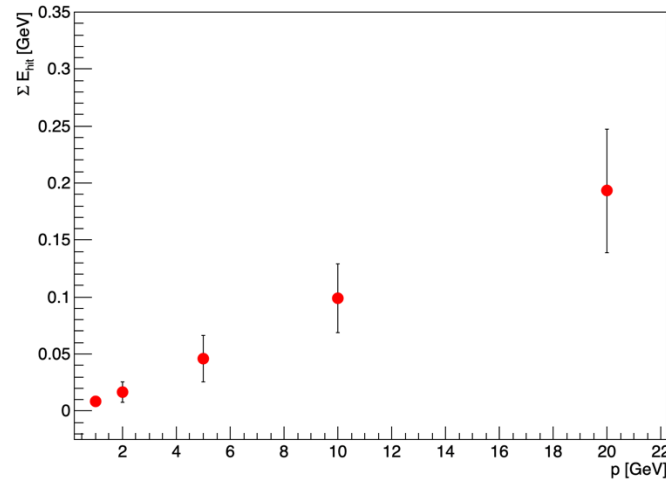
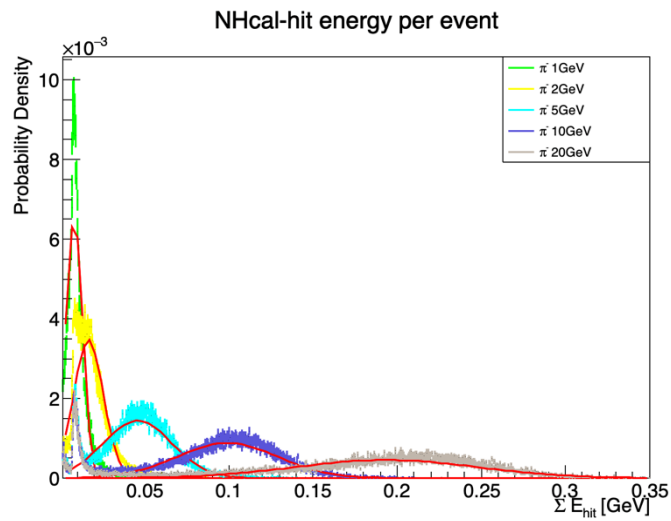
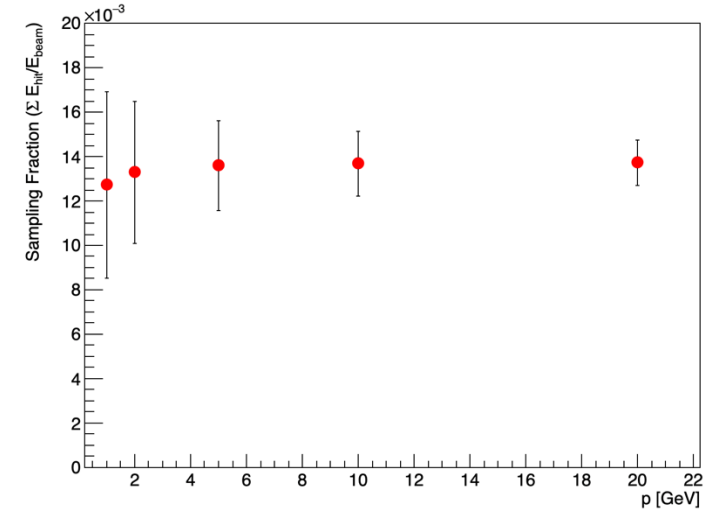
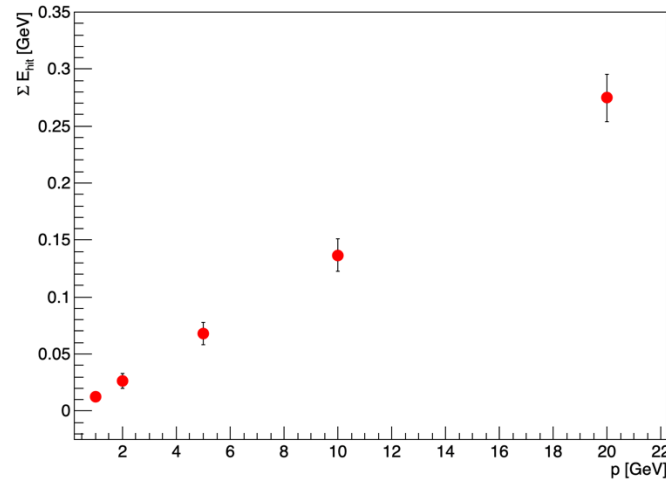
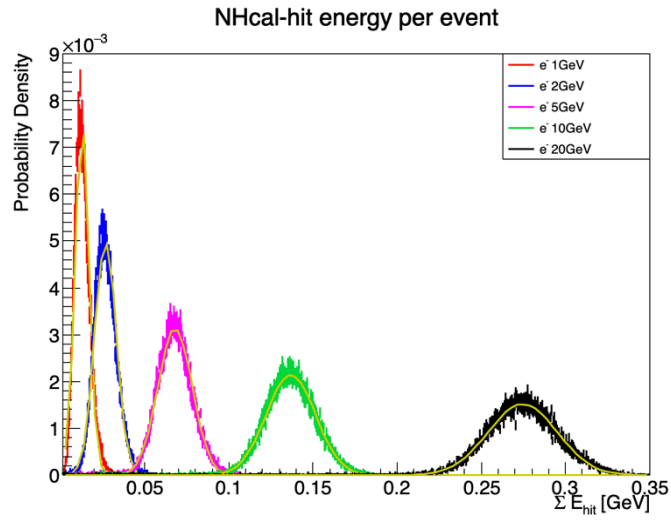
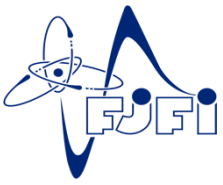
$$E_{neutral}^{Reco} = E_{total}^{Reco} - p$$

$\sigma_{E_c}$  = uncertainty on the cluster  
energy due to hadronic  
nature of energy deposition


$$\sigma_{E_c} = \frac{\sigma f_p}{f_{EICrecon}} E_c$$

What sampling fraction (depends on  
particle species and momentum) value  
should we use?

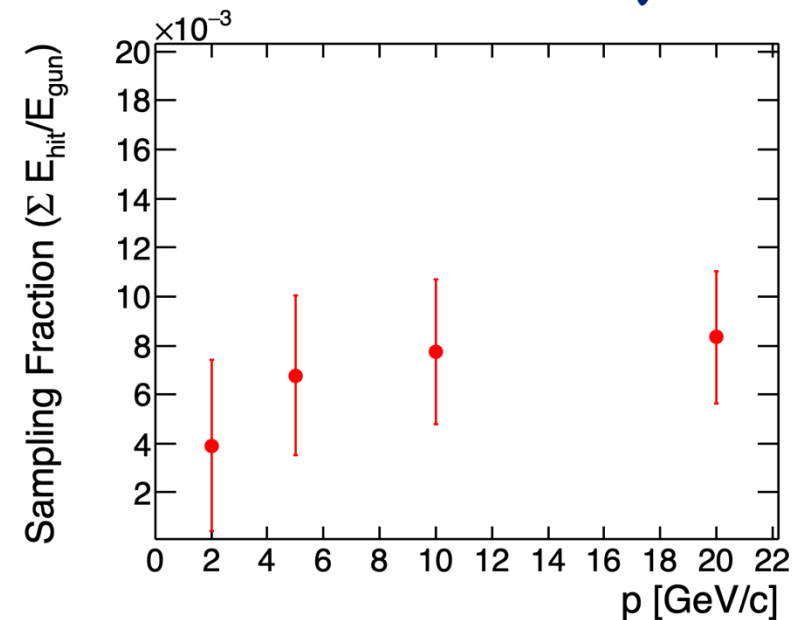
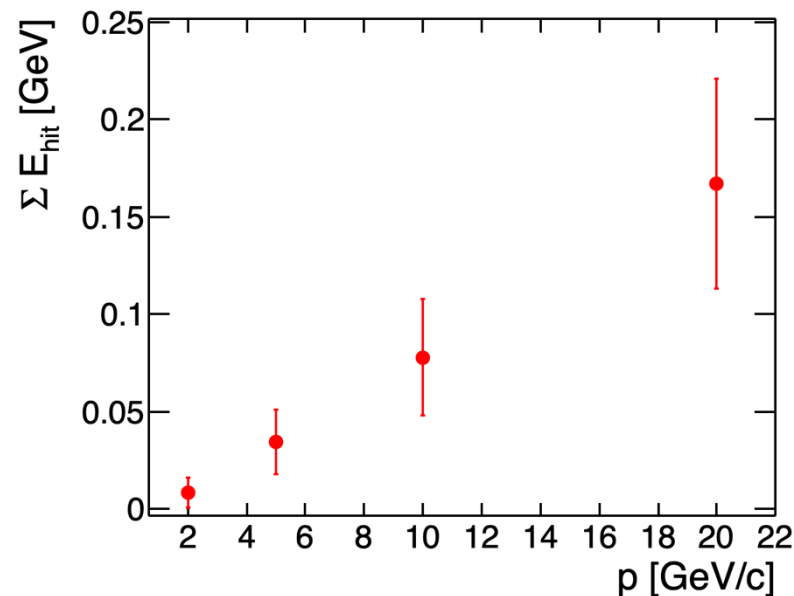
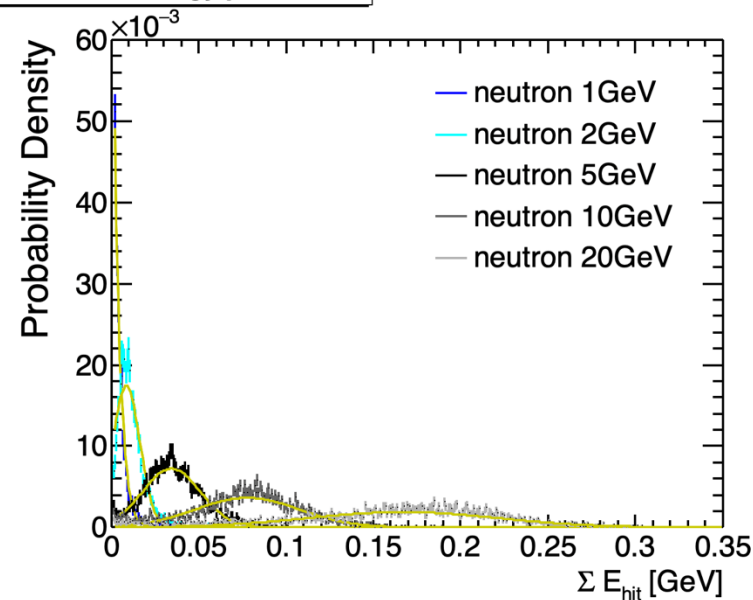
# Charged Particle Correction : Sampling Fraction



# Charged Particle Correction



NHcal-hit energy per event

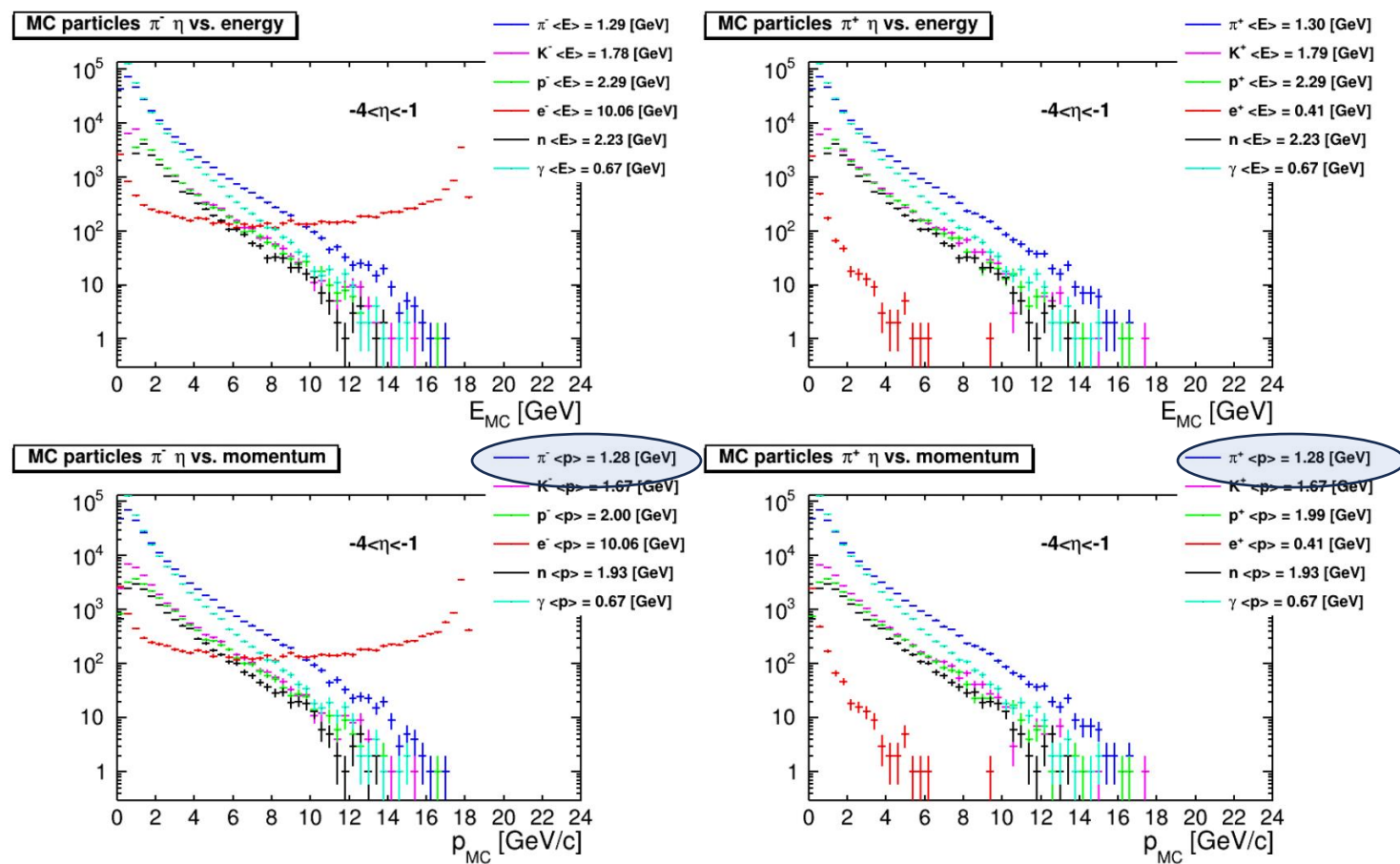


Particle	Momentum (GeV/c)	Sampling Fraction (%)	Uncertainty (%)
Electron	1.0	1.28	± 0.42
Electron	2.0	1.33	± 0.31
Electron	5.0	1.36	± 0.21
Electron	10.0	1.37	± 0.15
Electron	20.0	1.37	± 0.10
Pion	1.0	0.79	± 0.46
Pion	2.0	0.83	± 0.44
Pion	5.0	0.91	± 0.40
Pion	10.0	0.98	± 0.31
Pion	20.0	0.96	± 0.27
Neutron	1.0	N/A	N/A
Neutron	2.0	0.40	± 0.32
Neutron	5.0	0.67	± 0.30
Neutron	10.0	0.79	± 0.30
Neutron	20.0	0.84	± 0.39

Table 1: Sampling Fraction of nHCal for Different Particle Species



# Charged Particle Correction



Particle	Momentum (GeV/c)	Sampling Fraction (%)	Uncertainty (%)
Electron	1.0	1.28	$\pm 0.42$
Electron	2.0	1.33	$\pm 0.31$
Electron	5.0	1.36	$\pm 0.21$
Electron	10.0	1.37	$\pm 0.15$
Electron	20.0	1.37	$\pm 0.10$
Pion	1.0	0.79	$\pm 0.46$
Pion	2.0	0.83	$\pm 0.44$
Pion	5.0	0.91	$\pm 0.40$
Pion	10.0	0.98	$\pm 0.31$
Pion	20.0	0.96	$\pm 0.27$
Neutron	1.0	N/A	N/A
Neutron	2.0	0.40	$\pm 0.32$
Neutron	5.0	0.67	$\pm 0.30$
Neutron	10.0	0.79	$\pm 0.30$
Neutron	20.0	0.84	$\pm 0.39$

Table 1: Sampling Fraction of nHCal for Different Particle Species

**Figure 8.105:** Top: Primary, generated particle  $E$  distributions in nHCal acceptance  $-4.0 < \eta < -1.0$ . Bottom: Primary, generated particle  $p$  distributions in nHCal acceptance  $-4.0 < \eta < -1.0$ .

- ❑ The neutral energy component is obtained by subtracting the expected energy of charged particles, determined from the momentum measurement.
- ❑ Reconstruction performance depends on how much energy was deposited by neutron.
- ❑ Neutron and pion clusters can be distinguished when separated by  $\approx 30$  cm.

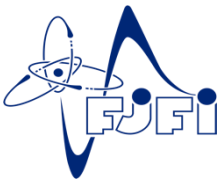
## **Limitations:**

1. Did not take into account unusual split clusters ( $> 1$  clusters for one-particle gun).
2. Track-Cluster Matching not used. Relying on ClusterMCParticle association.

Thank You

# Backup

# Charged Particle Correction



$E_c$  = Energy of the charged cluster obtained from EICrecon

$f_{EICrecon}$  = Sampling fraction incorporated in EICrecon

Lets call it  $E_c^{uncorrected}$

$f_{EICrecon} E_c$  = Uncorrected energy of cluster corresponding to actual energy deposition without the sampling fraction correction.

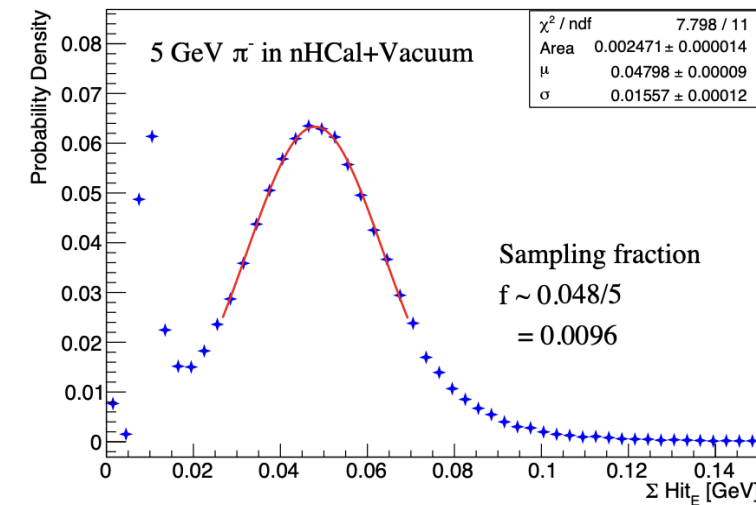
Objective : To find out the error in  $E_c$  due to uncertainty in sampling fraction.

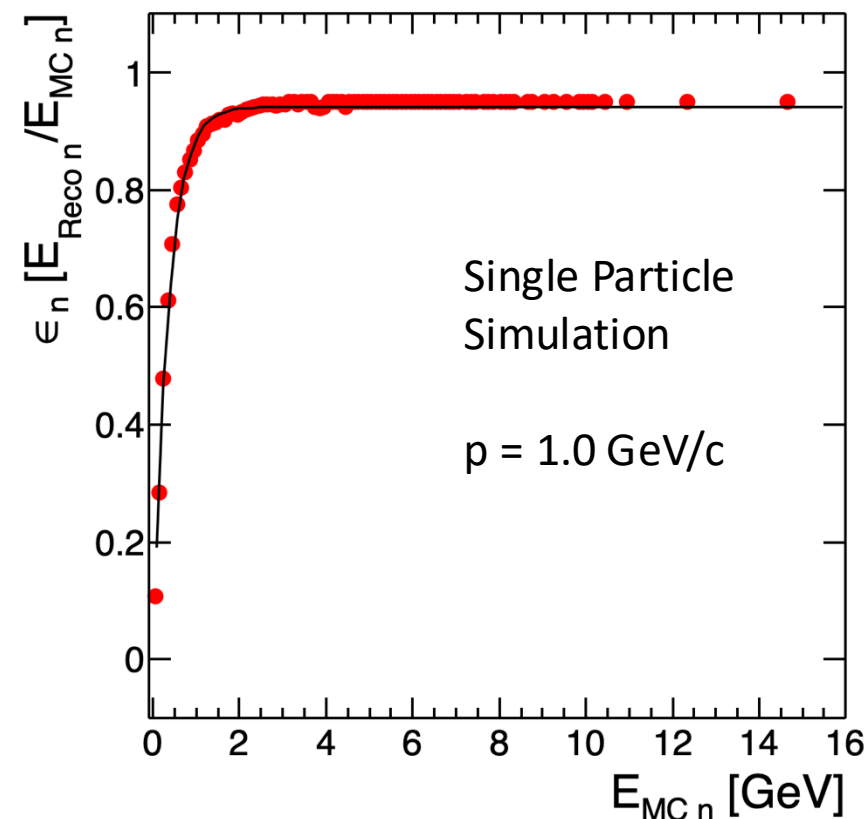
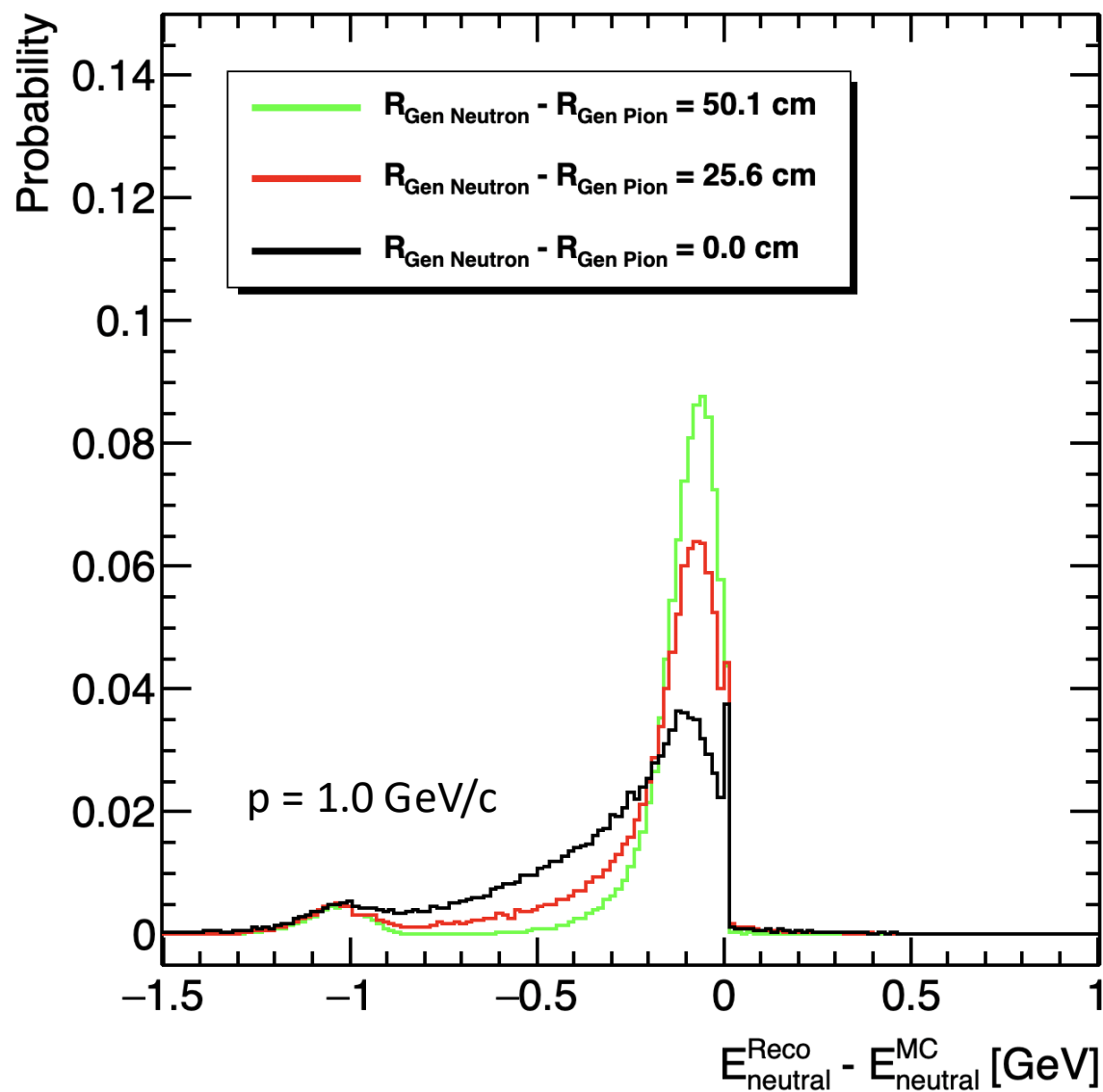
$$E_c^p = \frac{E_c^{uncorrected}}{f_p} \quad p = \text{momentum of the track matched to the cluster}$$

$$\frac{\sigma E_c^p}{E_c^p} = \frac{\sigma f_p}{f_p} \Rightarrow \sigma E_c^p = \frac{\sigma f_p}{f_p} E_c^p$$

$$\sigma E_c^p = \frac{\sigma f_p}{f_p^2} E_c f_{EICrecon} \approx \frac{\sigma f_p}{f_{EICrecon}} E_c$$

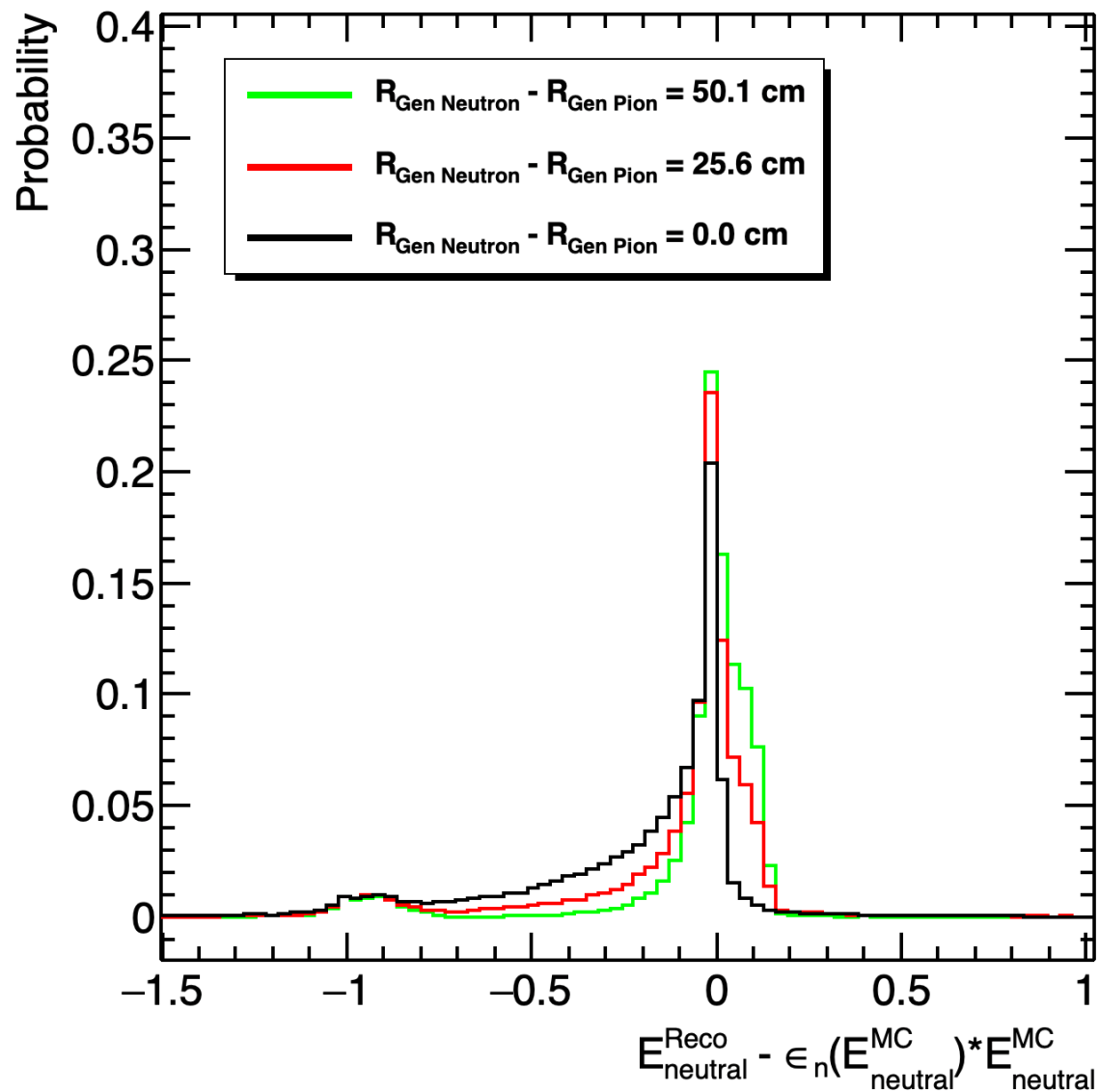
$f$  does not change  
much with  $p$





When,  $|(E_{\text{charged}}^{\text{Reco}} - p) / \sigma_{E_{\text{charged}}^{\text{Reco}}}| > 3.0$

$$E_{\text{neutral}}^{\text{Reco}} = E_{\text{total}}^{\text{Reco}} - p$$



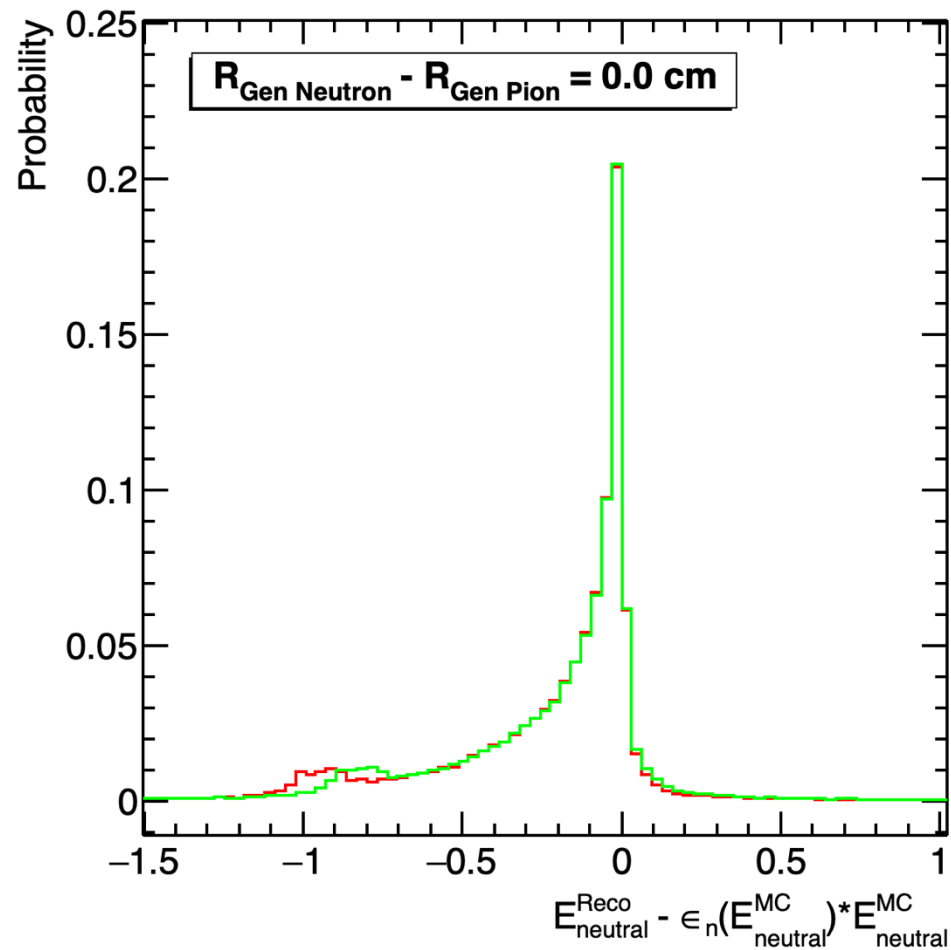
## Limitations:

1. Did not take into account unusual split clusters (> 1 clusters for a pion gun).
2. Track-Cluster Matching not used. Relying on ClusterMCParticle matching.

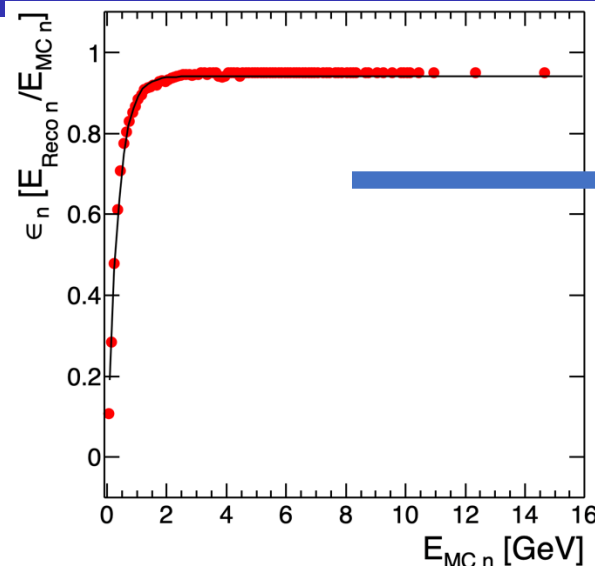
Can add more histograms corresponding to in-between distances (if needed)



# Charged Particle Correction



$p = 1.0 \text{ GeV}/c$



Considering it  
would not be  
species dependent

When,  $|(E_{\text{charged}}^{\text{Reco}} - p) / \sigma_{E_{\text{charged}}^{\text{Reco}}}| > 3.0$

$$E_{\text{neutral}}^{\text{Reco}} = E_{\text{total}}^{\text{Reco}} - p$$

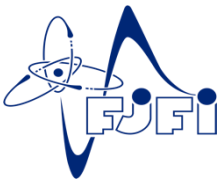
$$E_{\text{neutral}}^{\text{Reco}} = E_{\text{total}}^{\text{Reco}} - \epsilon(p) * p$$

Old  
New

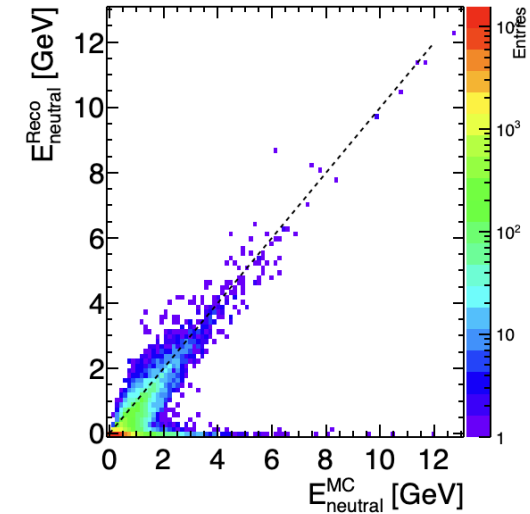
Otherwise,

$$E_{\text{neutral}}^{\text{Reco}} = E_{\text{total}}^{\text{Reco}} - E_{\text{charged}}^{\text{Reco}}$$

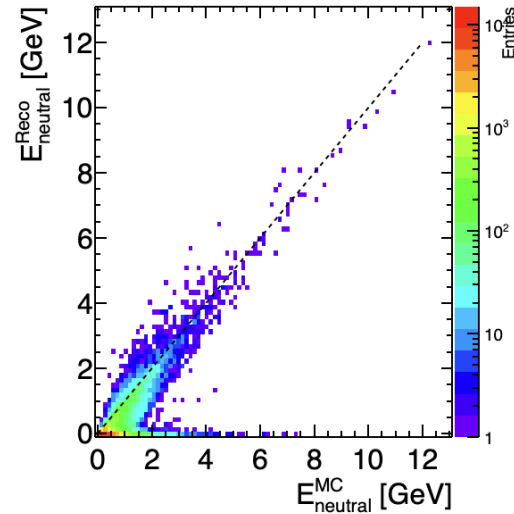
# Charged Particle Correction



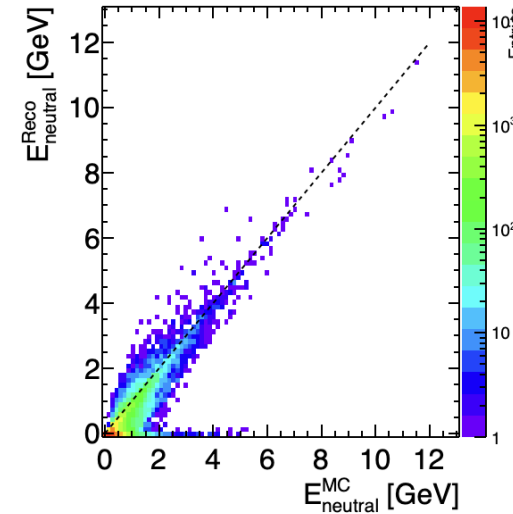
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 0.0 \text{ cm}$



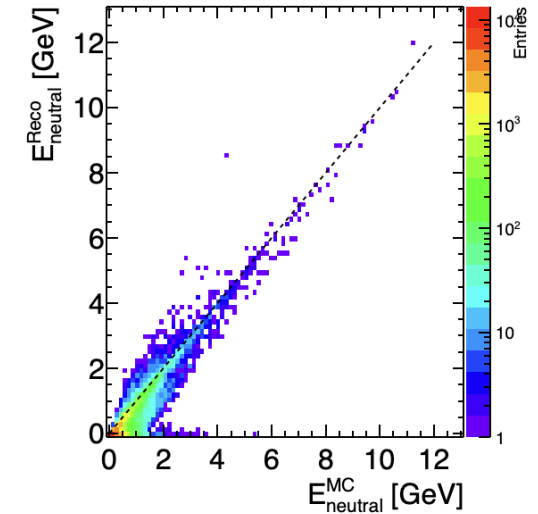
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 8.7 \text{ cm}$



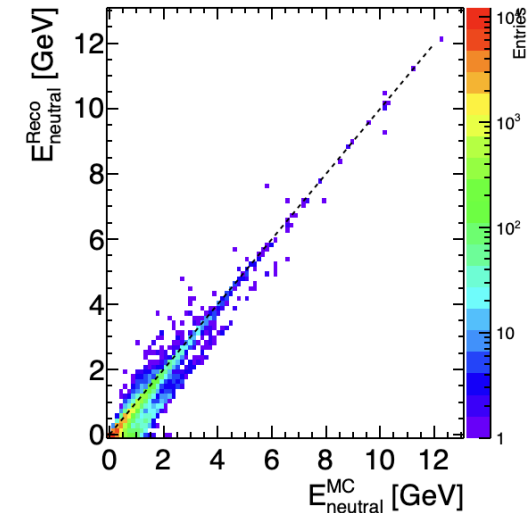
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 17.2 \text{ cm}$



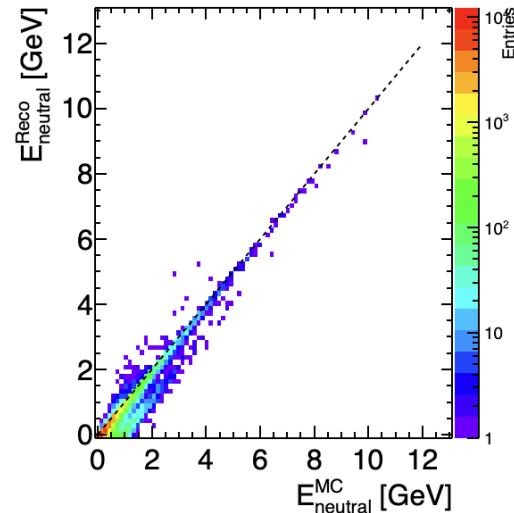
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 25.6 \text{ cm}$



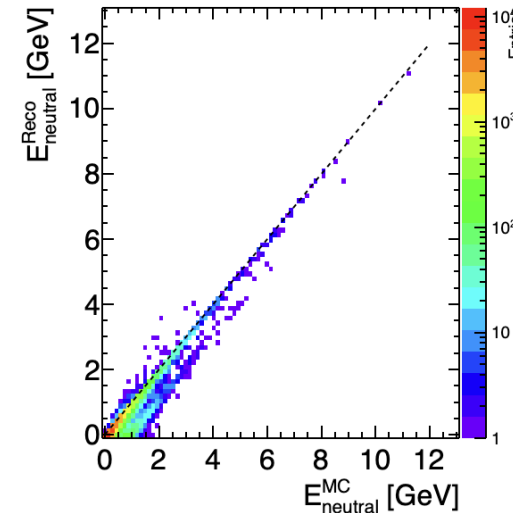
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 33.9 \text{ cm}$



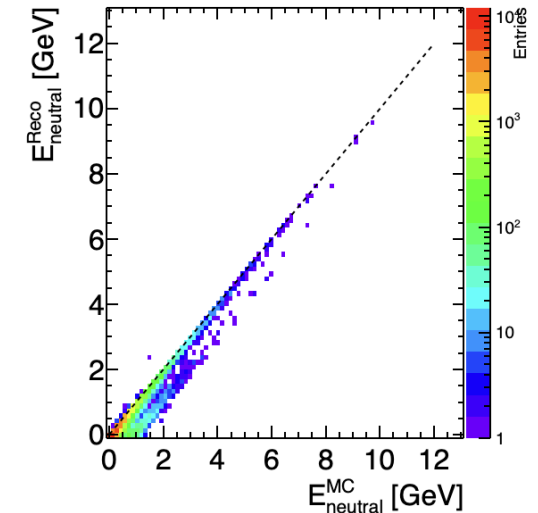
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 42.0 \text{ cm}$



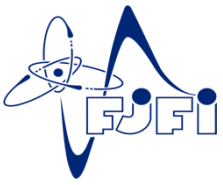
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 50.1 \text{ cm}$



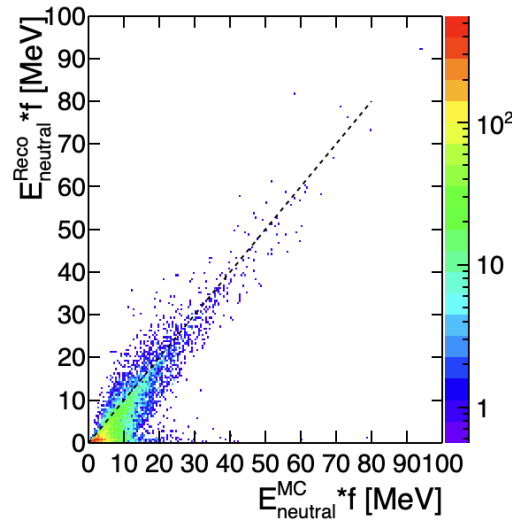
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 73.8 \text{ cm}$



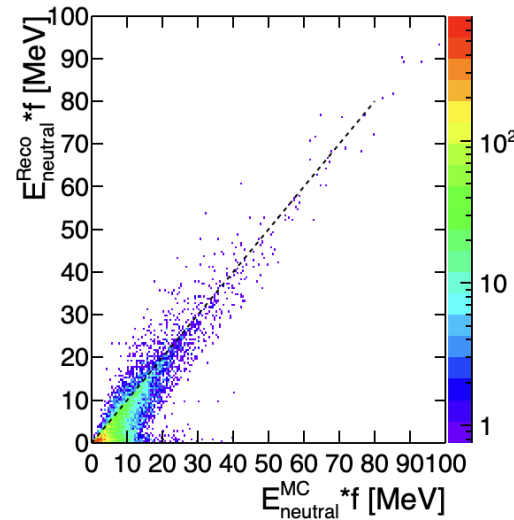
# Charged Particle Correction



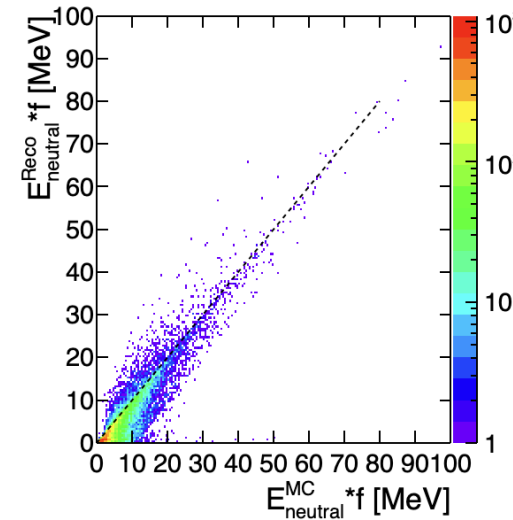
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 0.0 \text{ cm}$



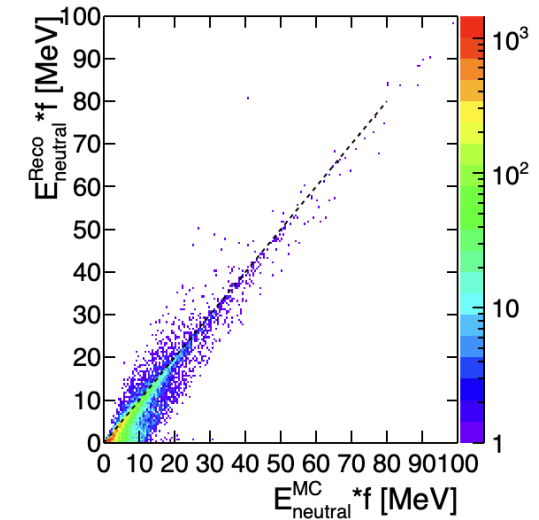
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 8.7 \text{ cm}$



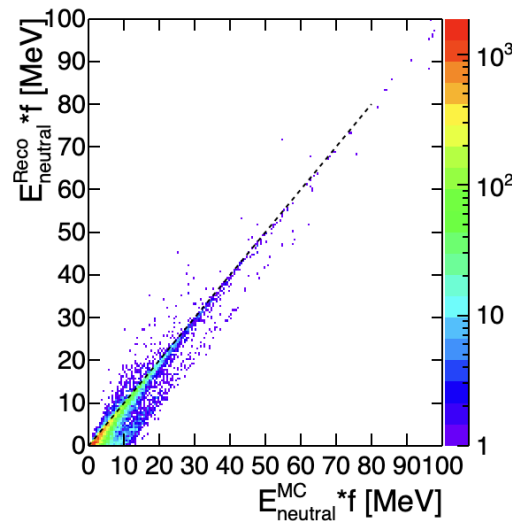
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 17.2 \text{ cm}$



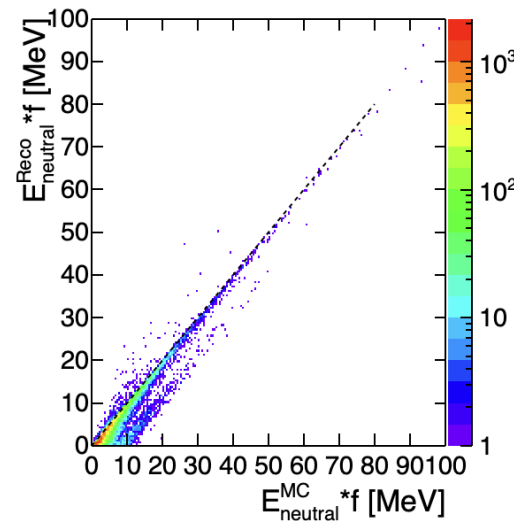
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 25.6 \text{ cm}$



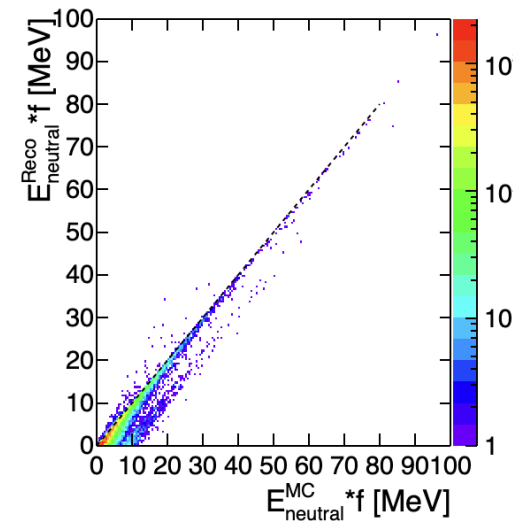
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 33.9 \text{ cm}$



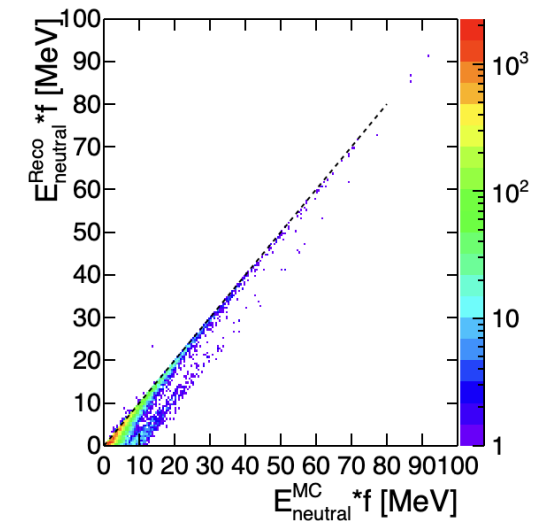
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 42.0 \text{ cm}$



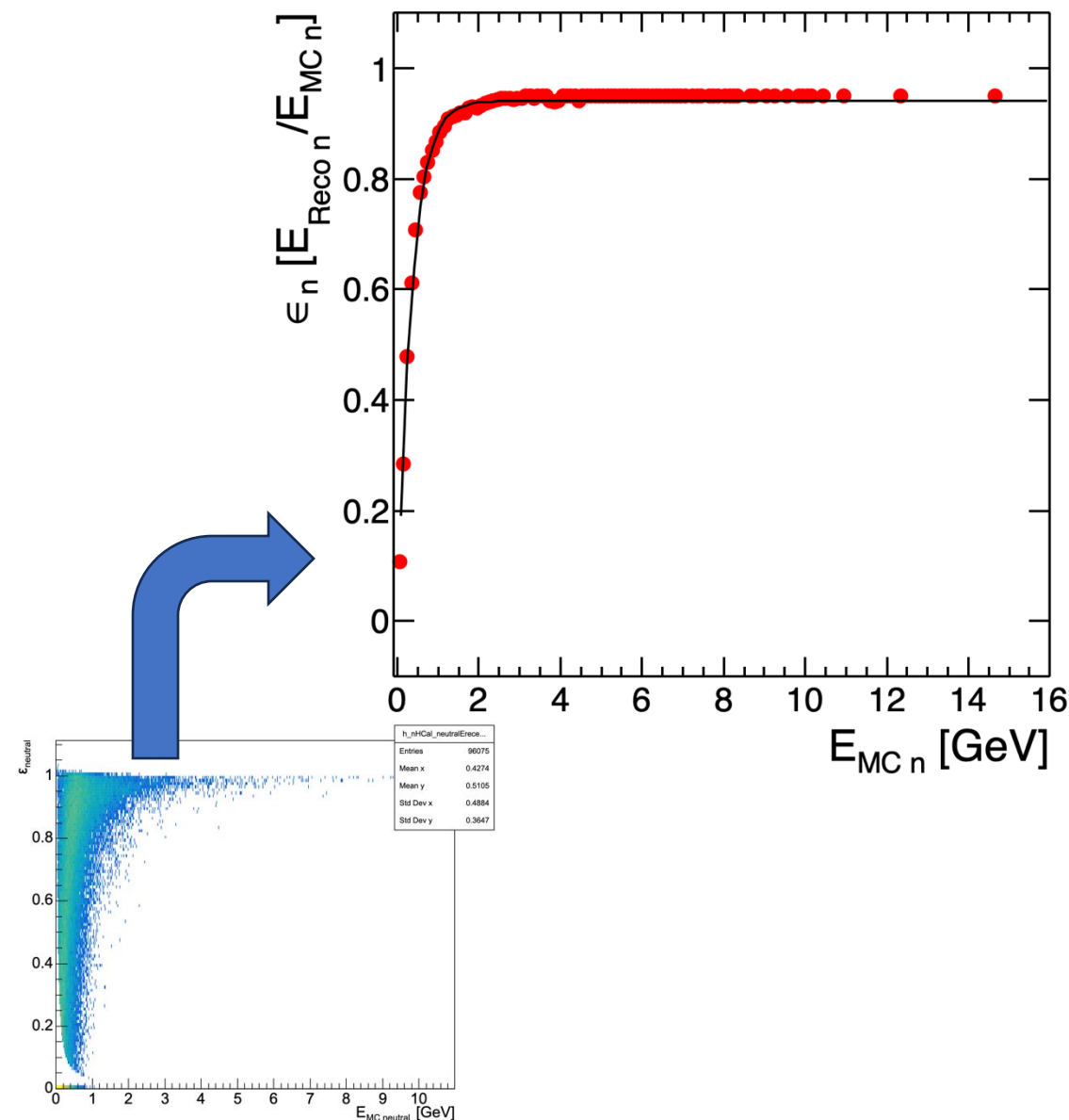
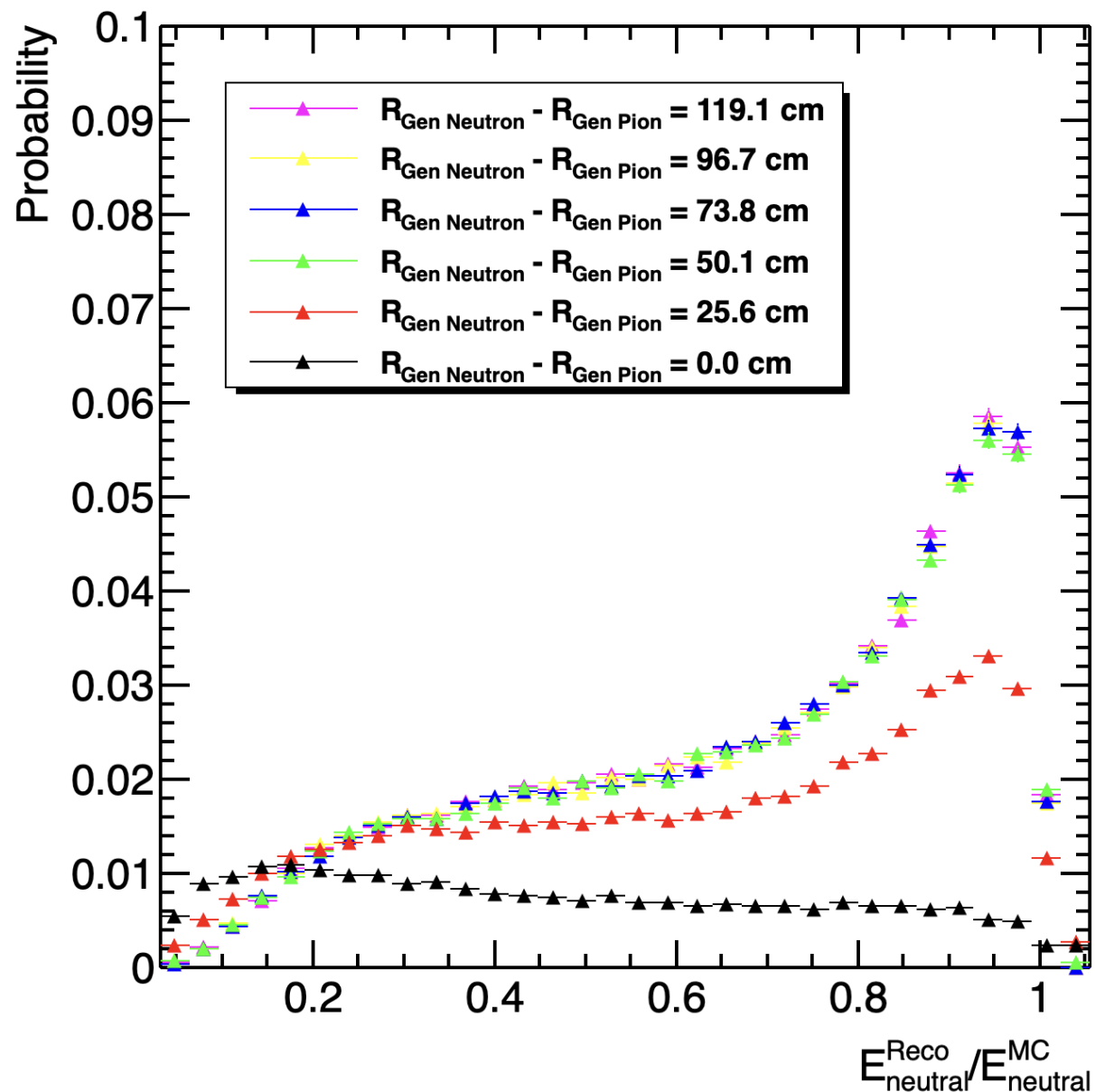
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 50.1 \text{ cm}$



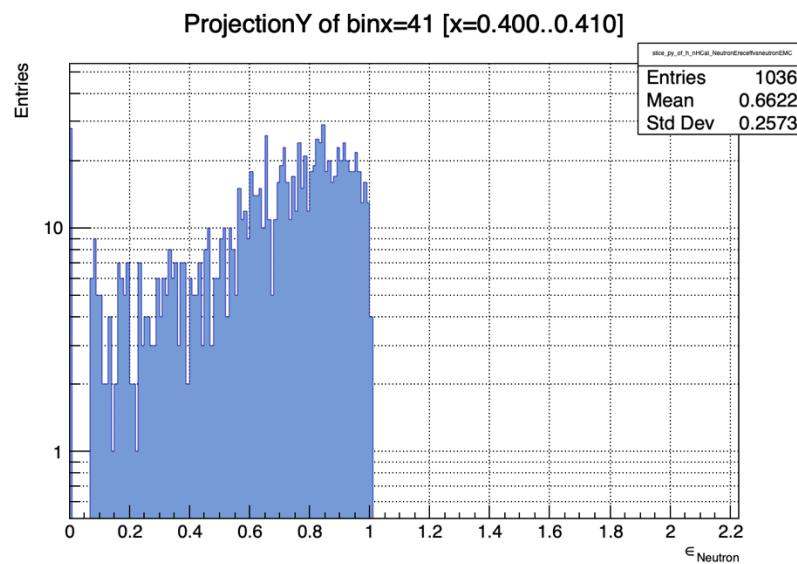
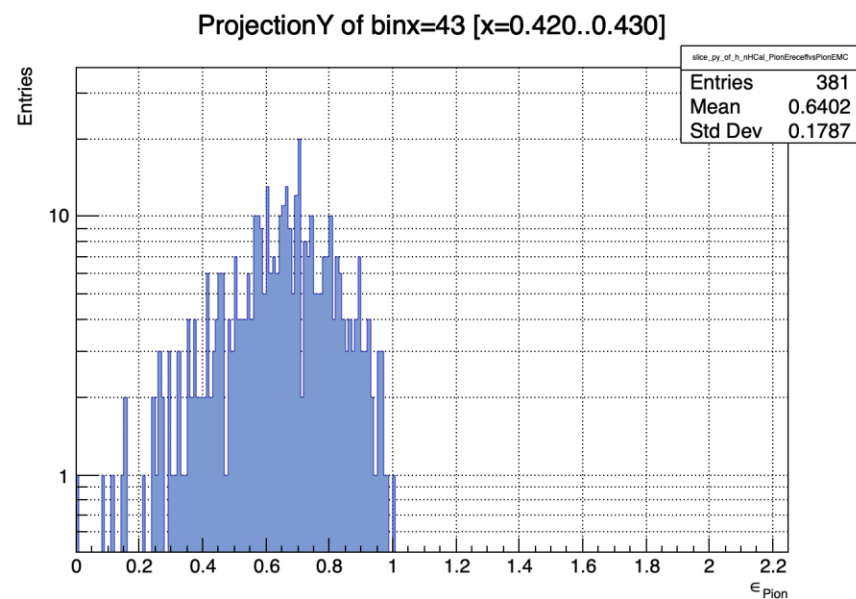
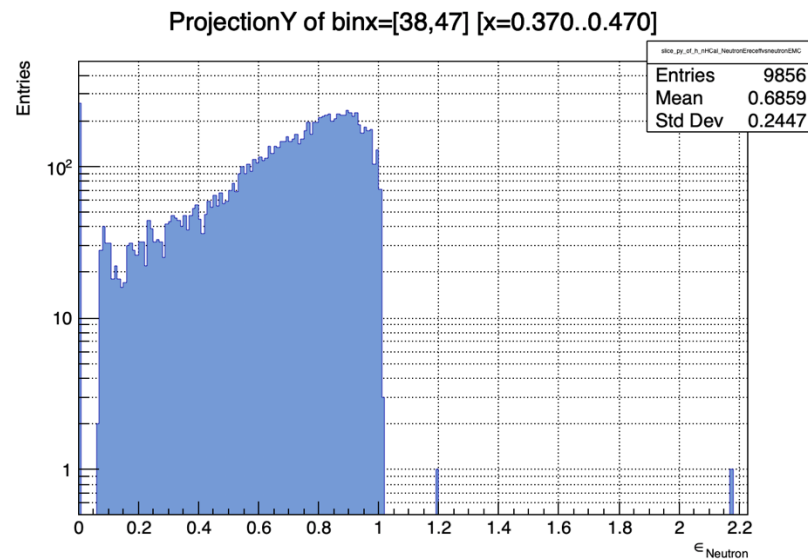
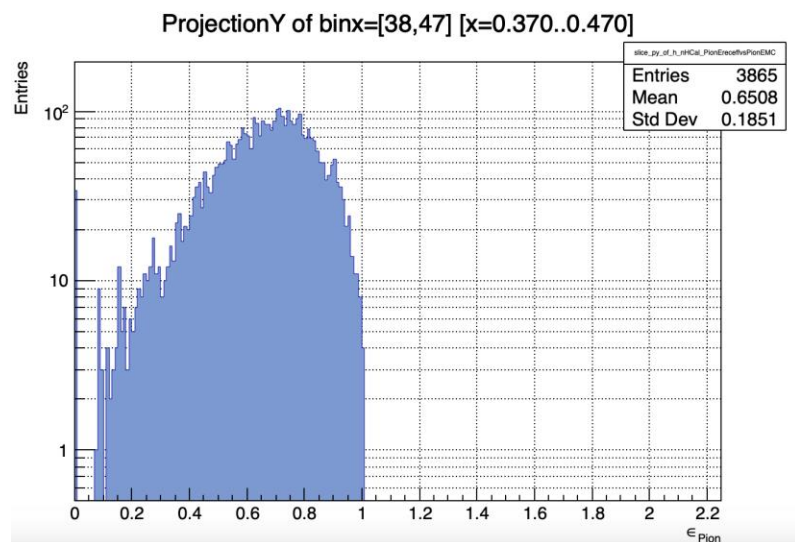
$R_{\text{Gen Neutron}} - R_{\text{Gen Pion}} = 73.8 \text{ cm}$



# Charged Particle Correction



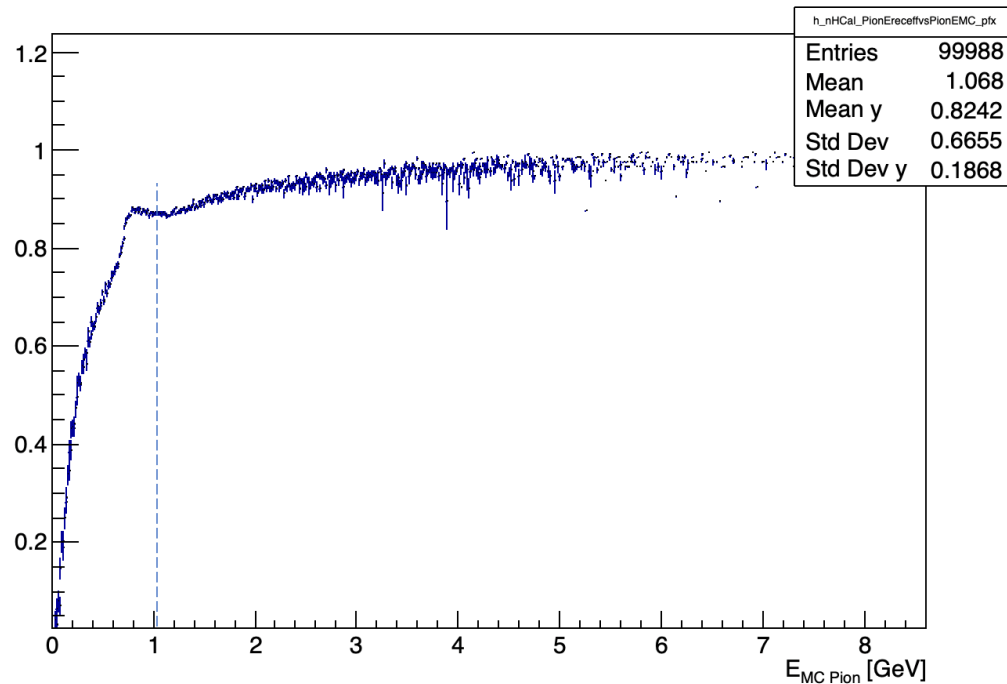
$$R_{\text{gen Neutron}} - R_{\text{gen Pion}} = 119.11 \text{ cm}$$



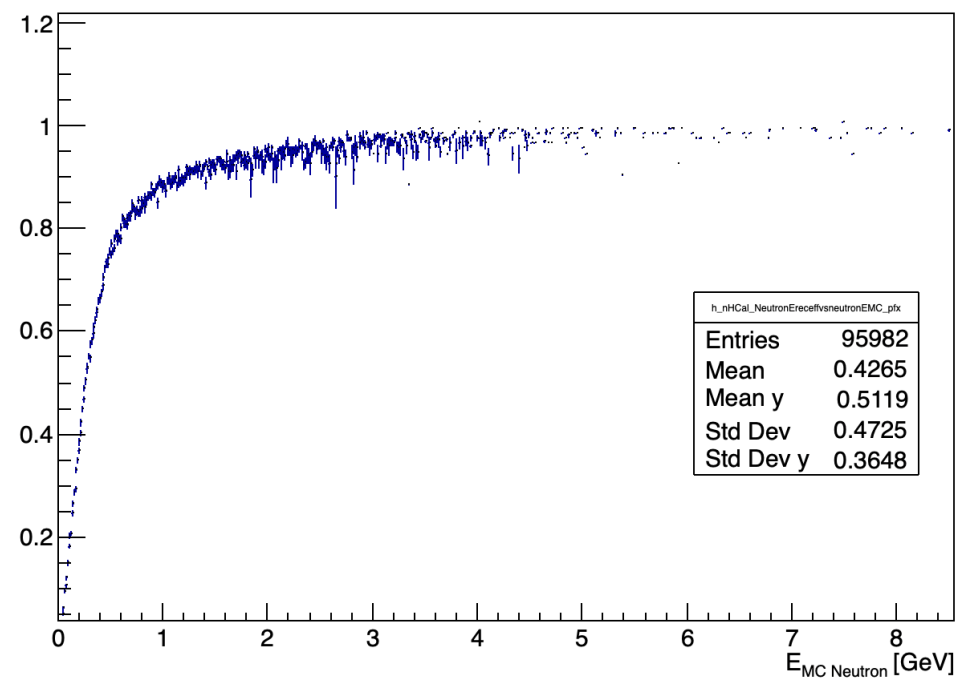
$$R_{\text{gen Neutron}} - R_{\text{gen Pion}} = 119.11 \text{ cm}$$



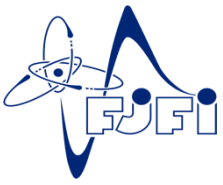
Pion cluster energy rec eff vs. Pion cluster energy MC



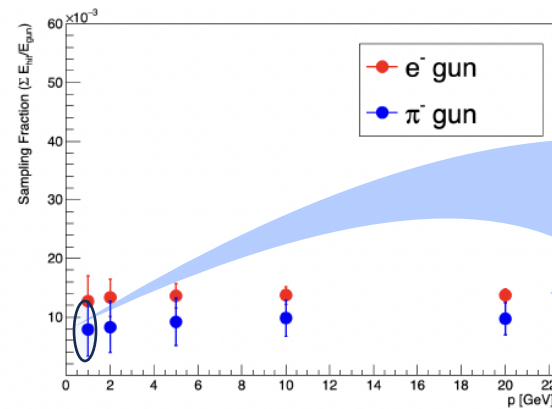
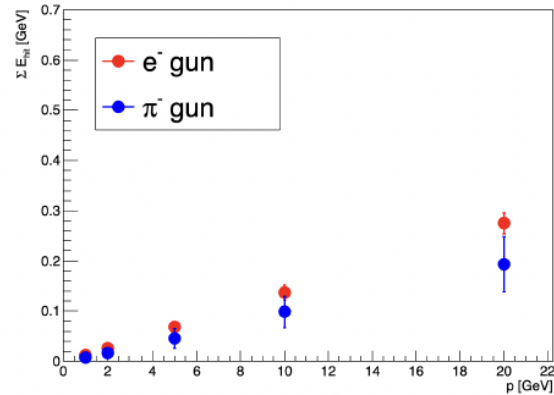
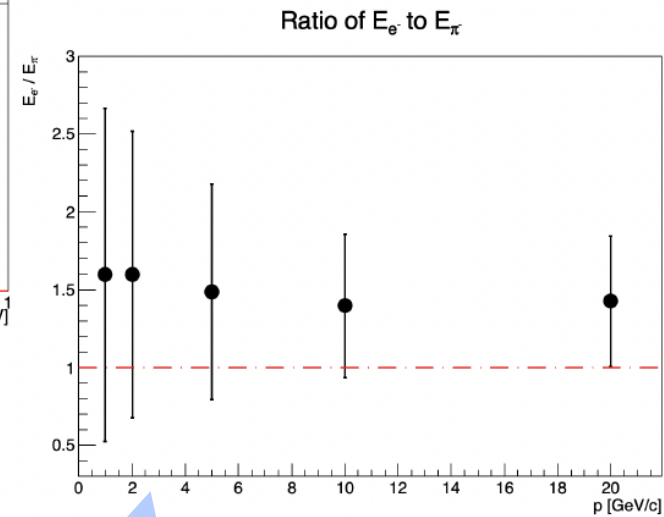
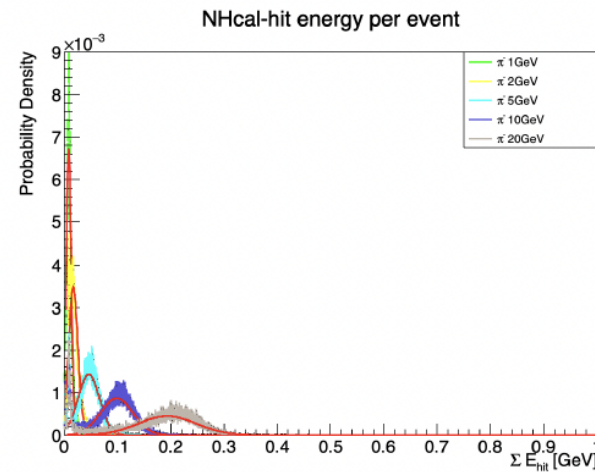
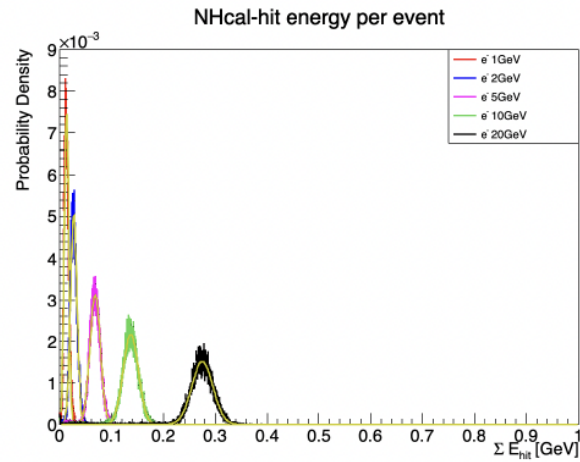
Neutron cluster energy rec eff vs. Neutron cluster energy MC



# Recap – e/h study



Steel/Scint = 10:1; 10 layers [40 mm Steel + 4 mm Scint]



$$f = 0.0080 \pm 0.0046$$