

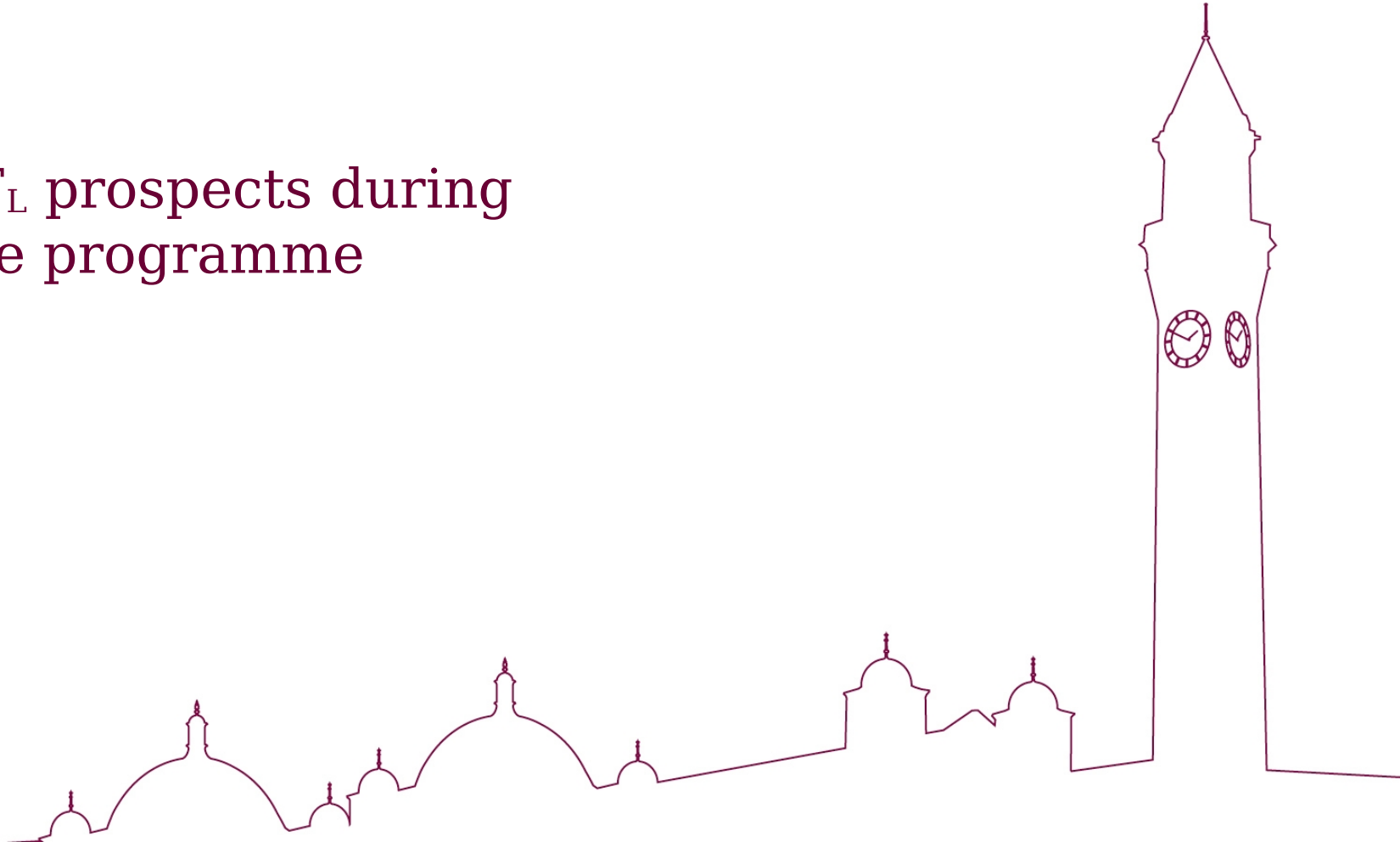


UNIVERSITY OF  
BIRMINGHAM

SCHOOL OF  
PHYSICS AND  
ASTRONOMY

# Update on $F_L$ prospects during early science programme

S. Maple



# Rosenbluth method to obtain $F_L$

$$Y_{\pm} = 1 \pm (1 - y)^2$$

- Inclusive cross section computed from 3 structure functions:

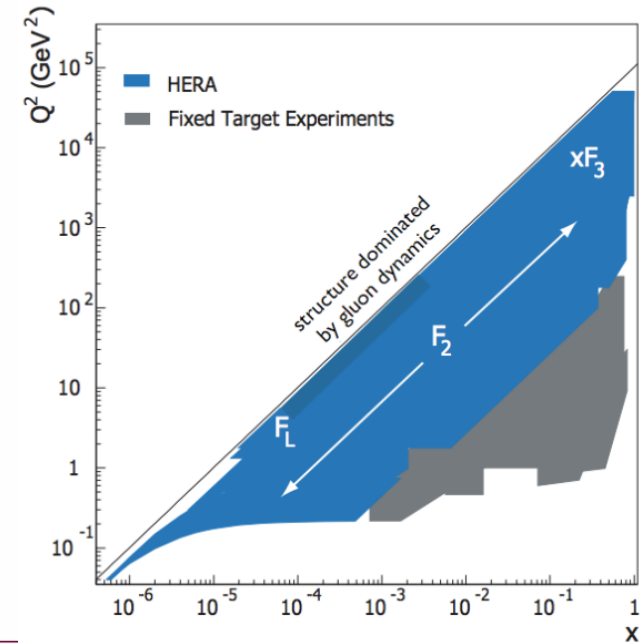
$$\sigma_r = \frac{xQ^4}{2\pi\alpha^2 Y_+} \left[ \frac{d^2\sigma}{dx dQ^2} \right] = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) + \frac{Y_-}{Y_+} x F_3$$

$$F_2 \propto x \sum_q (q + \bar{q})$$

- At LO, these are  $x F_3 \propto x \sum_q (q - \bar{q})$   $F_L = 0$

- $F_L$  is a pure QCD effect → gives an independent way of probing gluons:  $xg(x, Q^2) \approx 1.77 \frac{3\pi}{2\alpha_S(Q^2)} F_L(ax, Q^2)$

- Direct measurement of  $F_L$  via measurement of  $\sigma_{\text{red}}$  at same  $x$ - $Q^2$  but different  $y$  → different c.o.m. energies



# Rosenbluth method to obtain $F_L$

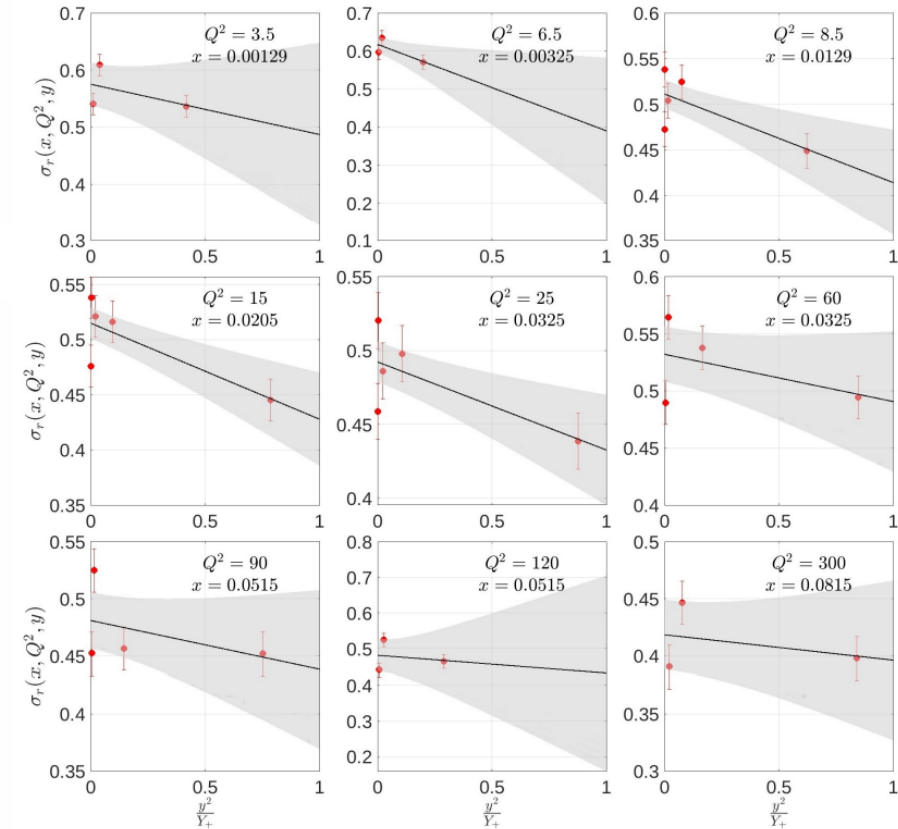
<https://arxiv.org/pdf/2412.16123>

- $F_L$  obtained as slope of  $\sigma_{\text{red}}$  vs  $y^2/Y_+$

$$\sigma_r = \frac{xQ^4}{2\pi\alpha^2 Y_+} \left[ \frac{d^2\sigma}{dx dQ^2} \right] = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) + \frac{Y_-}{Y_+} x F_3$$

- Contribution to  $\sigma_{\text{red}}$  is typically small (compared to e.g.  $F_2$ )
- Therefore, to measure  $F_L$  accurately we require:

→ **Small systematic errors on  $\sigma_{\text{red}}$**   
→ **As many data points as possible**  
**...over a large range in  $y^2/Y_+$**



# Early science ep runs

- The most recent early science matrix has 3 ep runs at two different energies

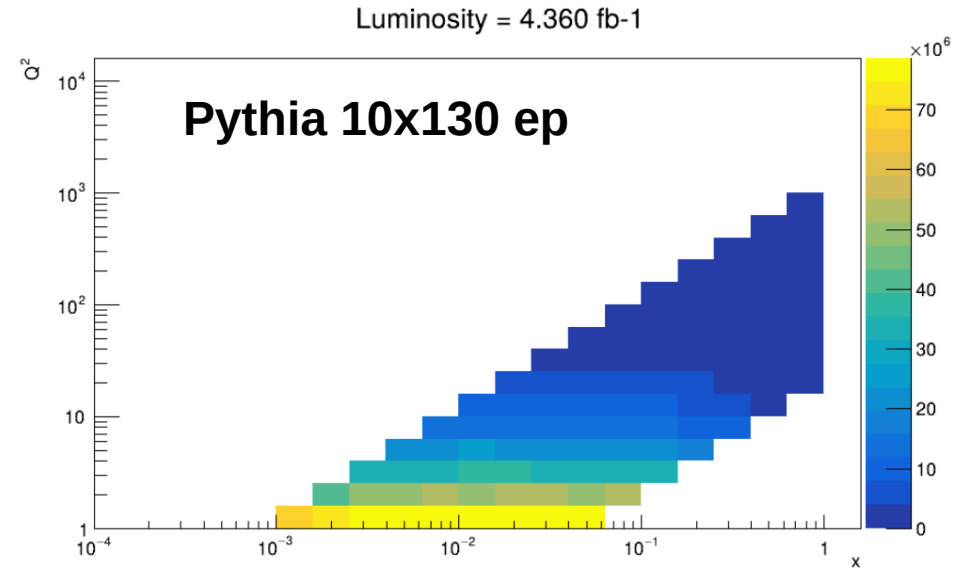
	Species	Energy (GeV)	Luminosity/year (fb <sup>-1</sup> )	Electron polarization	p/A polarization
YEAR 1	e+Ru or e+Cu	10 x 115	0.9	NO (Commissioning)	N/A
YEAR 2	e+D e+p	10 x 130	11.4 4.95 - 5.33	LONG	NO TRANS
YEAR 3	e+p	10 x 130	4.95 - 5.33	LONG	TRANS and/or LONG
YEAR 4	e+Au e+p	10 x 100 10 x 250	0.84 6.19 - 9.18	LONG	N/A TRANS and/or LONG
YEAR 5	e+Au e+3He	10 x 100 10 x 166	0.84 8.65	LONG	N/A TRANS and/or LONG

→ Small systematic errors on  $\sigma_{\text{red}}$   
→ ~~As many data points as possible~~  
...over a large range in  $y^2/Y_+$

→ Small systematic errors on  $\sigma_{\text{red}}$   
→ Two data points  
...over up to ~0.2 units in  $y^2/Y_+$

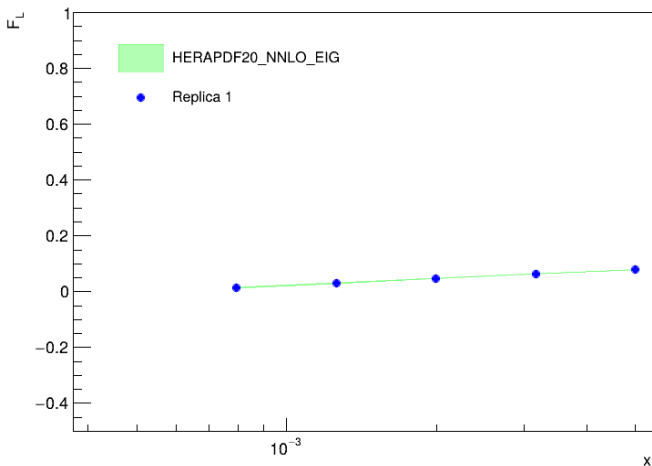
# Setup

- Create grids with 5 logarithmically spaced bins per decade in  $x$  and  $Q^2$
- Remove bins with any area that doesn't meet cuts  $Q^2 > 1\text{GeV}^2$  and  $0.005 < y < 0.96$
- Stat errors estimated from pythia
- Systematics use two scenarios:
  - Pessimistic: 3.4% normalisation (uncorrelated between runs), 1.9% point to point
  - Optimistic: 1% everywhere
- Procedure: smear cross sections according to total uncertainties → Rosenbluth technique for

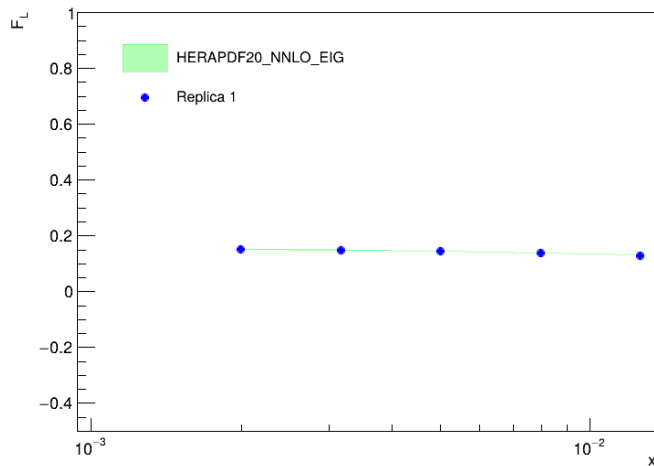


# Check with no smearing (low $Q^2$ )

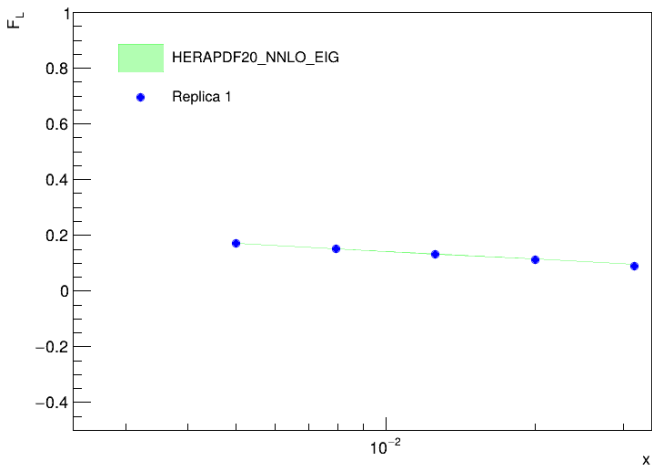
$Q^2 = 1.995 \text{ GeV}^2$



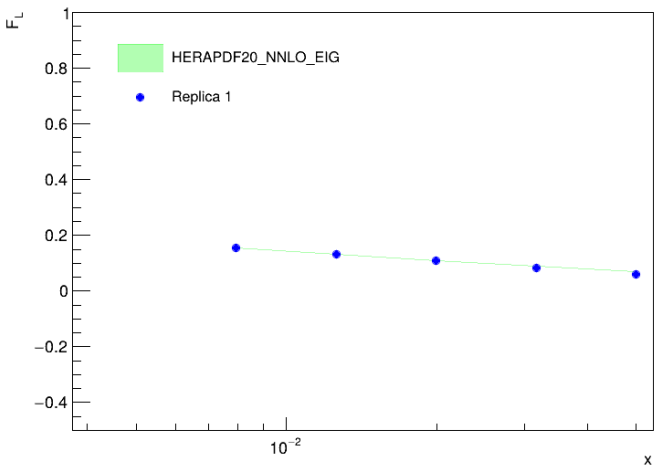
$Q^2 = 5.012 \text{ GeV}^2$



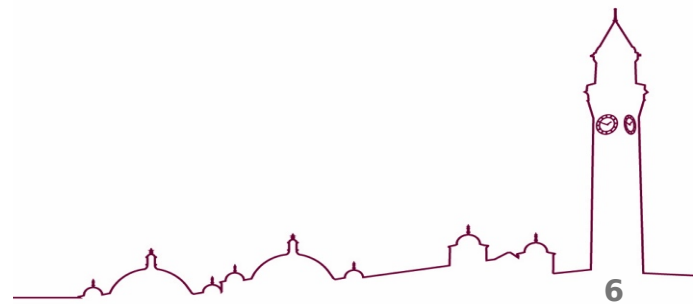
$Q^2 = 12.589 \text{ GeV}^2$



$Q^2 = 19.953 \text{ GeV}^2$

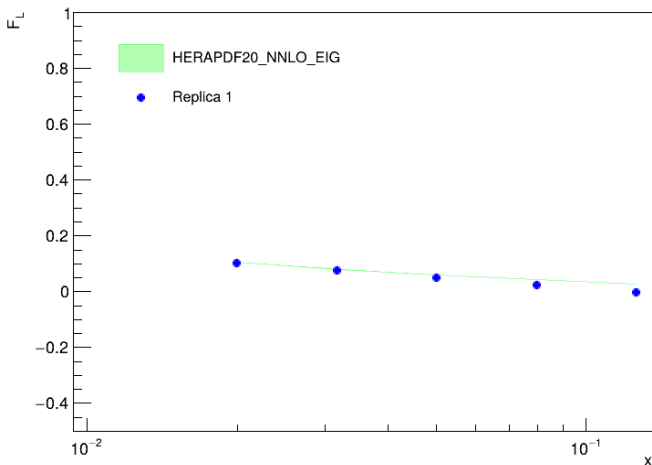


Rosenbluth method gives fairly compatible result to PDF prediction **at low  $Q^2$**

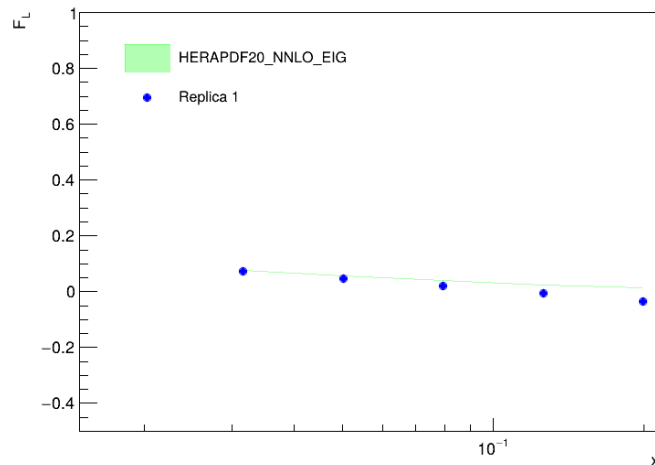


# Check with no smearing (moderate/high $Q^2$ )

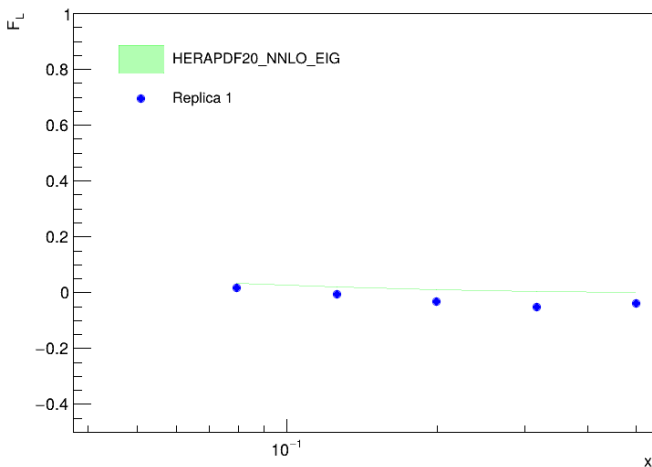
$Q^2 = 50.119 \text{ GeV}^2$



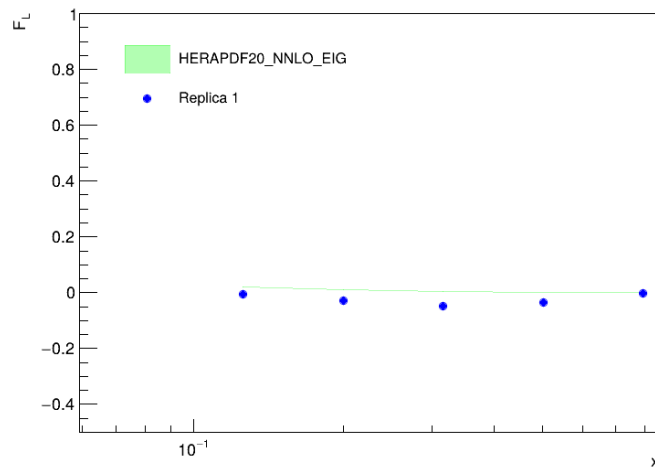
$Q^2 = 79.433 \text{ GeV}^2$



$Q^2 = 199.526 \text{ GeV}^2$



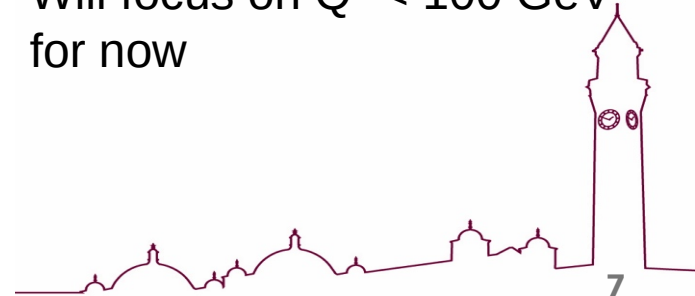
$Q^2 = 316.228 \text{ GeV}^2$



- Not quite as consistent for larger  $Q^2$  / larger  $x$
- Not really the region that we'd look at for  $F_L$  but would still be good to understand

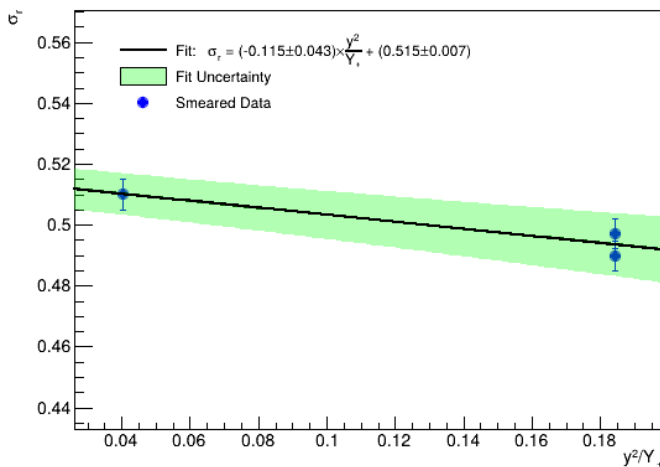
**Comments welcome!**

- Will focus on  $Q^2 < 100 \text{ GeV}^2$  for now



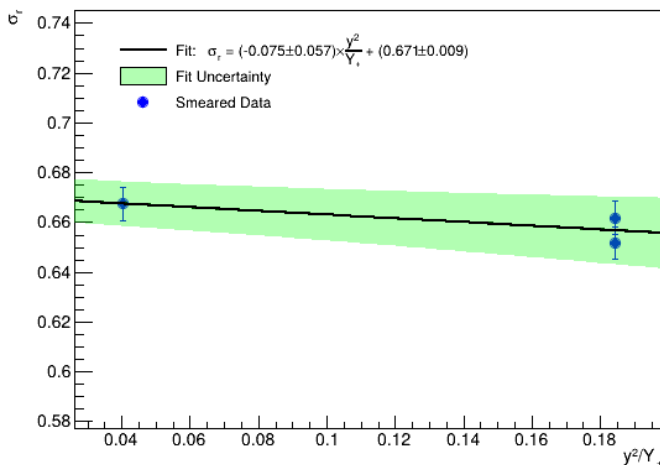
# Optimistic scenario (1% errors everywhere)

$Q^2 = 3.162 \text{ GeV}^2, x = 0.0013$



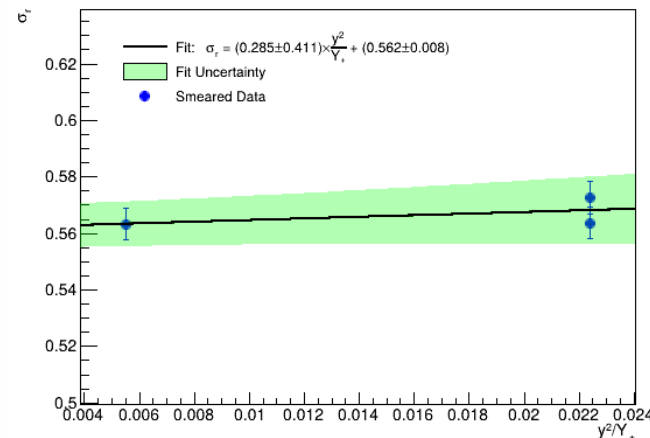
- Only 3 points and 2 c.o.m. energies
  - Left point intersected, right hand points split roughly down middle
- Only  $\sim 0.14$  range in  $y^2/Y_+$   $\rightarrow$  lower c.o.m. energies needed to fill this out

$Q^2 = 7.943 \text{ GeV}^2, x = 0.0032$



- With these settings it's fairly common to get a positive gradient i.e. negative  $F_L$  (note tiny range on x axis)

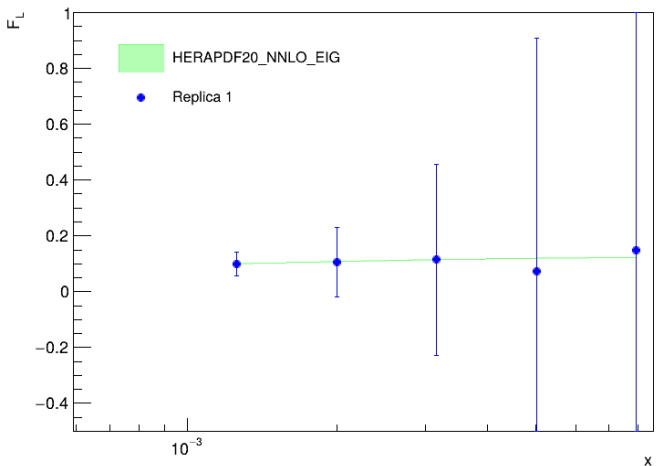
$Q^2 = 7.943 \text{ GeV}^2, x = 0.0079$



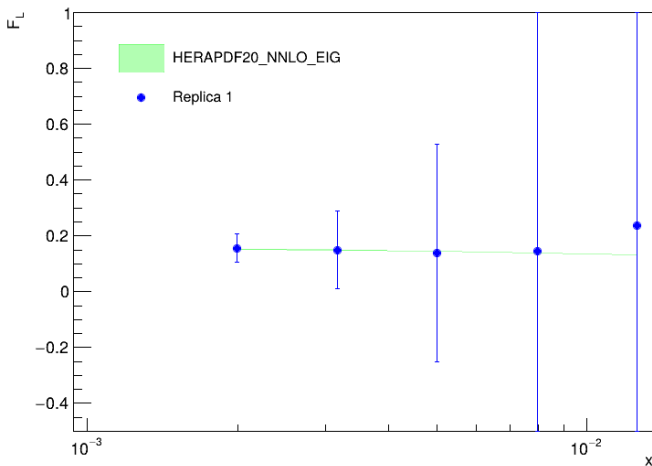


# Optimistic scenario (1% errors everywhere)

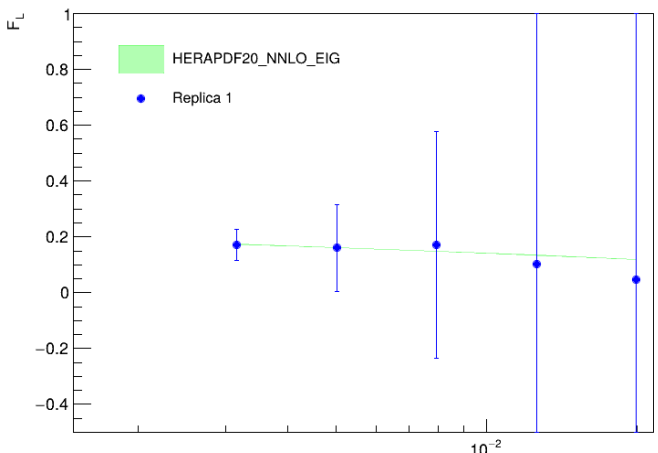
$Q^2 = 3.162 \text{ GeV}^2$



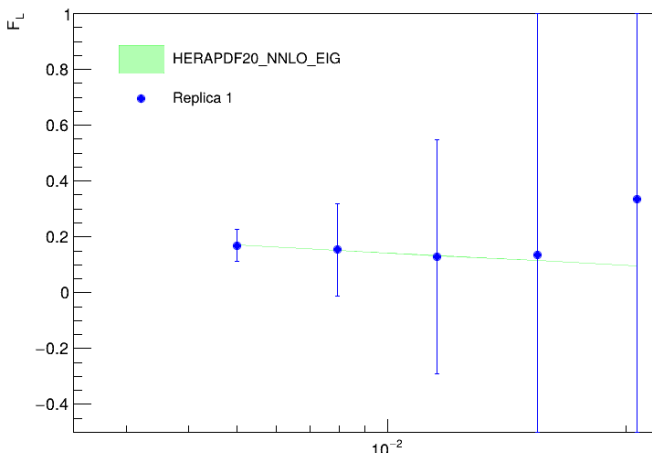
$Q^2 = 5.012 \text{ GeV}^2$



$Q^2 = 7.943 \text{ GeV}^2$



$Q^2 = 12.589 \text{ GeV}^2$

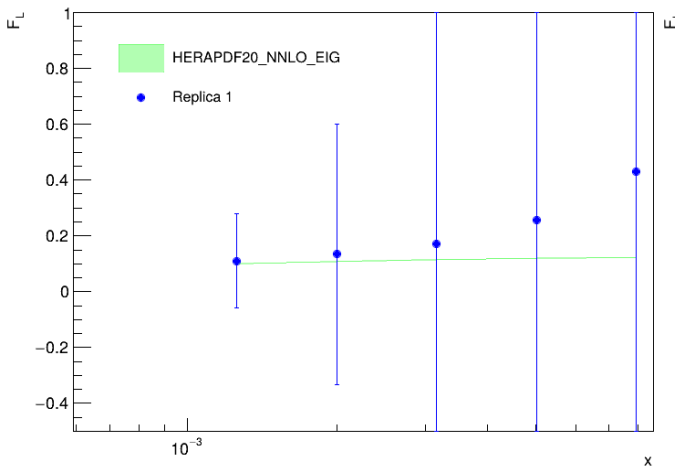


\*Highest  $x$  points should be centred on prediction for more replicas

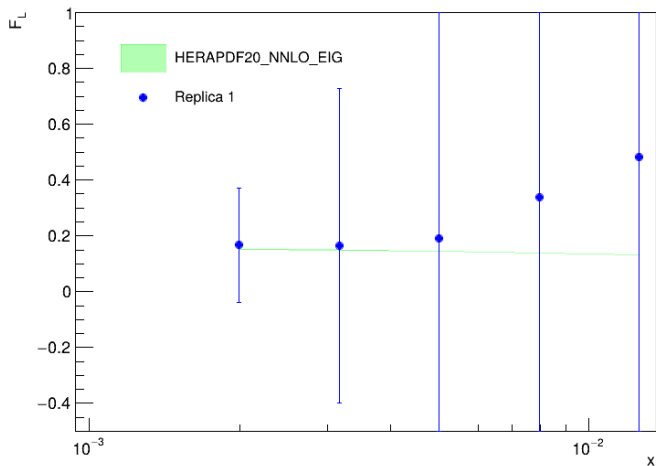
- Repeat smearing procedure over 1000 replicas
- Central point is mean value reconstructed for  $F_L$
- Error bars are standard deviation of reconstructed values
- With 3 points / 2 energies we get a couple of meaningful points per  $Q^2$  range

# Pessimistic scenario (1.9% p2p, 3.4% norm)

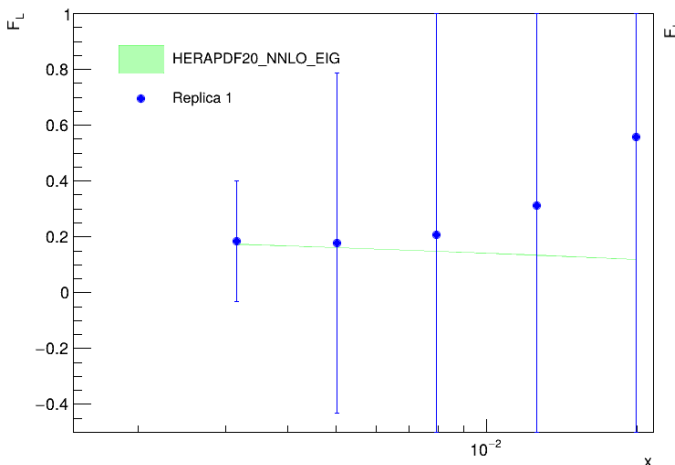
$Q^2 = 3.162 \text{ GeV}^2$



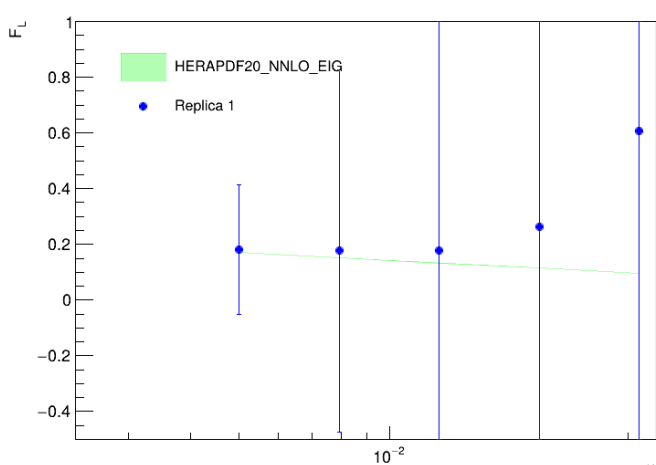
$Q^2 = 5.012 \text{ GeV}^2$



$Q^2 = 7.943 \text{ GeV}^2$



$Q^2 = 12.589 \text{ GeV}^2$



Same procedure as before

Very difficult to get meaningful measurements out for these settings

→ need more beam energy configurations to get something out with these systematics

# Summary

- The early science runs offer 2 different ep beam energies
  - In principle this is enough to extract  $F_L$  with the Rosenbluth technique
- Well controlled systematics required to get any useful  $F_L$  measurement out using the early science runs alone → we will need to do better than HERA

## Next Steps

- A single run with a lower c.o.m. configuration after the early science period may offer significant improvements → verify

